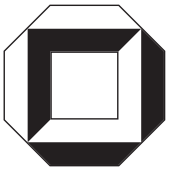

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Letters to the IEEE Computer Arithmetic Standards Revision Group

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Letters to the IEEE Computer Arithmetic Standards Revision Group

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Abstract

The IEEE standards 754 and 854 for floating-point arithmetic have been under revision for some time. The work is pushed forward by the Floating-Point Working Group (ca. 100 scientists) of the Standards Committee of the IEEE Computer Society. The group meets monthly near Palo Alto/San Jose in California. At present Dec. 2006 is the deadline for the new standard. The author has tried to influence the development of the new standard by several letters he has sent to the working group. The text of these letters follows.

Key words: computer arithmetic, floating-point arithmetic, interval arithmetic, elementary functions, arithmetic standards.

May 2005

Dear colleagues,

recently I have been asked by several colleagues to comment on the ongoing IEEE 754 revision work. So I am trying today to comment a little on interval arithmetic. Perhaps later I will send you comments on other topics.

The IEEE standard, adopted in 1985, seems to support interval arithmetic. It requires the basic four arithmetic operations with rounding to nearest, towards zero, and with rounding downwards and upwards. The latter two are needed for interval arithmetic. But almost all processors that provide IEEE arithmetic separate the rounding from the operation, which proves to be a severe drawback. In a conventional floating-point computation this does not cause any difficulties. The rounding mode is set only once. Then a large number of operations is performed with this rounding mode each one in a single cycle. However, when interval arithmetic is performed the rounding mode has to be switched very frequently. The lower bound of the result of every interval operation has to be rounded downwards and the upper bound rounded upwards. Thus, the rounding mode has to be reset for every arithmetic operation. If setting the rounding mode and the arithmetic operation are equally fast this slows down the computation of each bound unnecessarily by a factor of two in comparison to conventional floating-point arithmetic. On almost all existing commercial processors, however, setting the rounding mode takes a multiple (three, five,

ten) of the time that is needed for the arithmetic operation. Thus an interval operation is unnecessarily at least eight (or twenty and even more) times slower than the corresponding floating-point operation not counting the necessary case distinctions for interval multiplication and interval division. This actually kills interval arithmetic. The rounding should be an integral part of the arithmetic operation. Every one of the rounded arithmetic operations with rounding to nearest, downwards or upwards should be equally fast and executed in a single cycle. (Of course I know to code around all that. But I do not need a standard for that).

Interval arithmetic is an essential extension of floating-point arithmetic. It will only be widely accepted, used, and understood if it is equally fast. I append a paper which shows how interval arithmetic should be implemented on computers. The IEEE 754 standard should more precisely specify how interval arithmetic should be supported on computers.

I also append the title page of a new book which in the chapter "Interval Arithmetic Revisited" gives more (easily readable) information on the subject.

I wish you all much success with the IEEE 754 revision work. Progress in scientific computing depends critical on that standard.

With best regards

Ulrich Kulisch

Kulisch, U.: *Advanced Arithmetic for the Digital Computer - Design of Arithmetic Units.* Springer-Verlag 2002.

Kirchner, R. and Kulisch, U.: *Hardware Support for Interval Arithmetic.* Reliable Computing, January 2006.

June 2005

Dear colleague,

In early May I sent you a letter concerning interval arithmetic and the IEEE 754 revision work. I thank everybody who sent me comments. Apart from some misunderstandings about my meaning, all comments have been positive.

Today I would like to comment on another topic. It is related to interval arithmetic and is equally directed at increasing the speed of computation and the reliability of computed results.

Undoubtedly for elementary floating-point computation the IEEE standard arithmetic is thorough, consistent, and well defined. It has been widely accepted and can be found in virtually every processor developed since 1985. This has greatly improved the portability of floating-point programs.

However, computer technology has been dramatically improved since 1985. Arithmetic speed has gone from megaflops to gigaflops to teraflops, and it is already approaching the petaflops range. This is not just a gain in speed. A qualitative difference goes with it. At the time of the megaflops computer a conventional error analysis was recommended in every numerical analysis textbook. Today the PC is a gigaflops computer. For the teraflops computer conventional error analysis is no longer possible. An avalanche of numbers is produced when a teraflops computer runs for a few hours. If these numbers were to be printed they would need a pile of paper that reaches from the earth to the sun. Computing indeed has already reached astronomical dimensions!

This brings to the fore the question of whether the computed result really solves the given problem. The only way to answer this question is by the computer itself. Mathematical methods that provide an answer to this question are available for very many problems. Computers, however, are not at present built in a way that allows these methods to be used effectively.

During the last several decades of numerical analysis, methods for a large variety of problems have been developed which allow the computer itself to validate or verify its computed results. These methods compute unconditional bounds for a solution and can iteratively improve the accuracy of the computed result. Hardly any of these methods needs higher precision floating-point arithmetic. Double precision floating-point arithmetic is the basic arithmetical tool.

Two additional arithmetical features are fundamental and necessary:
1. **fast interval arithmetic** and
2. a **fast and accurate** *multiply and accumulate* **instruction**.[1]

How fast interval arithmetic can be implemented was described in my earlier letter. To obtain **close** bounds for the solution interval arithmetic has to be combined with defect correction or iterative refinement techniques. To be effective these techniques require an accurate *multiply and accumulate* instruction or, what is equivalent to this, an accurate scalar product. It is realized by accumulating products of the full double length into a wide fixed-point register. This fixed-point accumulation is completely free of truncation error. Fast hardware circuitry for an accurate *multiply and accumulate* instruction for all kinds of computers is discussed in the first chapter of my new book: *Advanced Arithmetic for the Digital Computer - Design of Arithmetic Units.* See the Appendix.

A very natural pipelining of the *multiply and accumulate* instruction leads to very fast and simple circuits. The hardware expenditure for it is comparable to that for a fast multiplier with an adder tree, accepted years ago. A speed increase by a factor of four, compared to a possibly wrong accumulation of the products in conventional floating-point arithmetic, is easily achieved.

With the fast and accurate *multiply and accumulate* instruction, fast quadruple or multiple precision arithmetic also easily can be provided. A multiple precision number is represented as an array of floating-point numbers. The value of this number is the sum of its components. It can be represented in the wide fixed-point register. Addition and subtraction of multiple precision variables or numbers can easily be performed in this register. Multiplication of two such numbers is simply a sum of products of floating-point numbers. It can be computed by means of the accurate *multiply and accumulate* instruction which is very fast. For instance in case of a fourfold precision the product of two such numbers $a = (a_1 + a_2 + a_3 + a_4)$ and $b = (b_1 + b_2 + b_3 + b_4)$ is obtained by

$$\begin{aligned} a \times b &= (a_1 + a_2 + a_3 + a_4) \times (b_1 + b_2 + b_3 + b_4) \\ &= a_1b_1 + a_1b_2 + a_1b_3 + a_1b_4 + a_2b_1 + \cdots + a_4b_3 + a_4b_4 \\ &= \sum_{i=1}^{4} \sum_{j=1}^{4} a_i b_j. \end{aligned}$$

By using the accurate *multiply and accumulate* instruction the result is inde-

[1] To achieve high speed all conventional vector processors provide a 'multiply and accumulate' instruction. It is, however, not accurate. By pipelining, the accumulation (continued summation) is executed very swiftly. The accumulation is done in floating-point arithmetic. The pipeline usually has four or five stages. What comes out of the pipeline is fed back to become the second input into the pipeline. Thus four or five sums are built up and are finally added together. This so-called partial sum technique alters the sequence of the summands and causes errors in addition to the usual floating-point errors. A vectorizing compiler uses this 'multiply and accumulate' operation within a user's program as often as possible, since it greatly speeds up the execution. Thus the user loses complete control of his computation.

pendent of the sequence in which the summands are added.

In Summary: Interval arithmetic can bring guarantees into computation while an accurate *multiply and accumulate* instruction can bring high accuracy via defect correction methods and at high speed. It also is the key operation for fast multiple precision arithmetic.

Fast and accurate hardware support for 1. and 2. must be added to conventional floating-point arithmetic. Both are necessary extensions. Instead of the computer being merely a fast calculating tool they would turn it into a scientific instrument of mathematics. Computing that is continually and greatly speeded up makes this step necessary and it is that very speed that calls conventional computing into question.

Of course, often the computer would have to do more work to obtain verified results. But the mathematical safety should be worth it. The step from assembler to higher programming languages or the use of convenient operating systems also consumes a lot of computing power and nobody complains about it. Fast computers in particular are often used for safety critical applications. Severe, expensive, and tragic accidents can occur if the eigenfrequencies of a heavy electricity generator, for instance, are erroneously computed, or if a nuclear explosion is incorrectly simulated.

The IEEE standards 754 and 854 have been under revision for some time. I hope that the revision does not get bogged down in details but that it will also consider the more basic features of high speed scientific computing. The computer should not be just a glorified calculator for another twenty years.

Again, I wish you all much success with the IEEE 754 revision work. A major breakthrough is necessary for scientific computing.

With best regards

Ulrich Kulisch

August 8, 2005

Dear Colleague,

It really is not easy to follow a discussion from far away. So I am not sure whether I correctly understand everything what I read about 'Static Mode Declarations'. Nevertheless I do have a comment about the rounding mode.

I think the old way (of IEEE 754), first to set the rounding mode and then to call the arithmetic operation, is well established and I have no complaint about it nor did my earlier letter request its elimination.

However, for interval arithmetic we need to be able to call each of the operations $+>$, $->$, $*>$, $/>$, and $+<$, $-<$, $*<$, $/<$ (here $>$ means rounding upwards and $<$ means rounding downwards) as one single instruction. (I simply call these operations 'my operations'). This requires new operation codes! These operations are distinct from the other approach where first the rounding mode has to be set and then the arithmetic operation is called.

I see a need for the older mechanism as well, in particular for those applications where the rounding mode is to be selected randomly. I think in this case the status register should provide a new mode for choosing the rounding mode randomly (by a hardware random number generator). Then all standard roundings would be performed with roundings that change at random. This would not have any effect on 'my operations' since they are called by other operation codes.

I would appreciate it very much if, with a new arithmetic standard, denotations for arithmetic operations with different roundings would be introduced. They could be: $+, -, *, /$ for operations with rounding to the nearest floating-point number, $+>$, $->$, $*>$, $/>$ for operations with rounding upwards, $+<$, $-<$, $*<$, $/<$ for operations with rounding downwards, and $+|, -|, *|, /|$ for operations with rounding towards zero (chopping).

We would have to convince the language designers that this is much simpler and leads to much more easily readable expressions than for instance the use of operators like .addup. or .adddown. in Fortran. In languages like C++ which just provide operator overloading and do not allow user defined operators these operations would be called as functions or via assembler. Our C-XSC, for instance, does not provide operations with directed roundings. They are hidden within the interval operations.

With best regards

Ulrich Kulisch

October 2005

HIGH SPEED COMPUTING WITH HIGH ACCURACY

Dear colleague: In my second letter to the IEEE 754 revision group (in June 2005) I proposed an *accurate multiply and accumulate operation* for inclusion in the revised IEEE arithmetic standard. Some of my colleagues have since urged me to expand on the significance of this operation in a further mail. My comments are the following:

A pipelined *multiply and accumulate operation* is the key to obtaining high speed on all existing vector processors. However, the way this operation has been implemented causes errors beyond those of conventional floating-point. I append the *GAMM-IMACS Resolution* and the *GAMM-IMACS Proposal* which address these errors.

The proposed *accurate multiply and accumulate operation*, or equivalently an *accurate scalar product*, comes with the same gain in speed (multiplication and accumulation are performed in one pipeline). In addition it delivers a fully accurate result and it is the key operation for high speed multiple precision arithmetic and multiple precision interval arithmetic. These latter two in turn are the key operations for controlling the accuracy in a computation.

As far as I understand the drafts of the IEEE revision work, quadruple precision arithmetic will be part of the next IEEE arithmetic standard. Of course the entire computing community would be grateful for this. But this should not be the only way to higher accuracy. If the attainable accuracy in a particular class of problems is insufficient with double precision, then it will very often be insufficient with quadruple precision as well. I think it is necessary, therefore, also to provide a basis for improving the accuracy rather than simply providing higher precision. Hardware implementation of a full quadruple precision arithmetic is much more costly than implementation of the accurate scalar product. The latter only requires fixed-point accumulation of double precision products. Fast multiple precision arithmetic and multiple precision interval arithmetic can easily be provided as a by-product.

The *accurate multiply and accumulate operation* is realized by accumulating the products of the full double length into a wide fixed-point register. Fixed-point accumulation is simple, error free, and fast. No under- or overflow can occur during a scalar product computation, if the width of this register is appropriately chosen. There is a specific technique for absorbing a possible carry before it appears (see the first chapter of my book on 'Advanced Computer Arithmetic'). Of course it is most convenient to supply enough local memory on the arithmetic unit for all scalar products of double precision data to be computed to full accuracy. We did this on our chip. However if this much memory or register space is not available, compromises are quite possible. See the section 'Hardware Accumulation Window' in my book. For example in the case of the data format 'long' of the /370 architecture all scalar products that do not cause an over- or

underflow can be computed to full accuracy in a register space of 624 bits. If this register space is available on the arithmetic unit the vast majority of scalar products could be computed to full accuracy on very fast hardware. In case of an over- or underflow, an underlying software routine (exception handling) would take over. Thus in every case a fully accurate result is computed.

There are many good reasons to urge very strongly that the *accurate multiply and accumulate operation* be included in a future IEEE arithmetic standard. For obtaining high accuracy it is the ultimate solution. A hardware implementation of the accurate scalar product, by the way, brings a considerable speed up compared to a conventional computation of the scalar product in floating-point, while any software simulation will be considerably slower than the latter. This is also the case if quadruple precision and/or computing the second part of an operation and/or other aids like multiply and add fused are available. Computer arithmetic without the *accurate multiply and accumulate operation* is incomplete and unnecessarily slow.

With best regards

Ulrich Kulisch

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January 28, 2006

To: Nelson H. F. Beebe and to stds-754@IEEE.ORG

Dear colleague, in your mail of Nov. 22, 2005 to stds-754@IEEE.ORG and to me you refer to the *GAMM-IMACS Proposal for Accurate Floating-Point Vector Arithmetic*. Methods that realize the proposal are developed in my book [KUL]. In the same mail you mention the paper [ORO], and in another mail of Jan. 4, 2006 the paper [ROO]. I also appreciate these excellent papers. All these papers [ORO], [ROO], and [KUL] claim to provide fast methods that compute accurate sums and dot products. The question is: fast in comparison with what?

[ORO] and [ROO] just use conventional floating-point arithmetic. The methods are fast compared with other software methods that compute highly accurate sums and dot products. The computing time comes surprisingly close to the time T needed for (a possibly wrong) computation in conventional floating-point arithmetic. The speed mildly decreases with increasing condition number.

[KUL] suggests hardware solutions. The methods are fast compared with other hardware solutions. The computing time is independent of the condition number. It is less than T. This high speed is reached because the actions: *loading the data, computing, shifting, and accumulation of the products* are performed in one pipeline. Furthermore fixed-point accumulation of the products is simpler than accumulation in floating-point arithmetic. Many intermediate steps that are executed in a floating-point accumulation such as normalization and rounding of the products and of the intermediate sum, composition into a floating-point number and decomposition into mantissa and exponent for the next operation do not occur in the fixed-point accumulation. It simply is performed by a shift and addition of the products of full double length into a wide fixed-point register. Fixed-point accumulation is error free! If supported by a (conventional) vectorizing compiler the method would boost both the speed of a computation and the accuracy of the result! The [KUL] method does not just solve the problem with faithful rounding. Sums and dot products are computed to full accuracy. This allows an easy and very fast realization of multiple precision floating-point and interval arithmetics.

The second paragraph in your mail of Nov. 22 reads: *One implementation of this proposal would use internal accumulators wide enough to hold the entire exponent range, requiring width of hundreds to tens of thousands of bits (for the 32-bit, 64-bit, 80-bit, and 128-bit formats).*

Other methods only consider the 32-bit and the 64-bit formats. Who knows how they would perform for a 128-bit format? The wording accumulator in your mail may be misleading the understanding of the situation. All that is actually needed in the case of the 64-bit format is a tiny local memory on the arithmetic unit of about 1K bytes. We really can and we should afford this at a time where computer memory is measured in gigabytes. The arithmetic itself is not much different from what is available on a conventional CPU. For larger

data formats see the section 'Hardware Accumulation Window' in my book. I very much appreciate your suggestion to further investigate the subject with regard to an emerging revised IEEE 754 standard. A new standard should also consider the more basic features of high speed scientific computing.

With best regards

Ulrich Kulisch

[ORO] Takeshi Ogita, Siegfried M. Rump, Shin'ichi Oishi: *Accurate Sum and Dot Product,* SIAM Journal on Scientific Computing, Vol. 26, No. 6, pp. 1955 - 1988, 2005.

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February 10, 2006

Dear colleagues

My thanks to everybody who sent me comments on my letter of January 28, 2006 to stds-754@IEEE.ORG and to Nelson Beebe. In the responses, the wordings accurate sum and dot product, exact sum and dot product, and faithfully rounded sum and dot product are used more or less synonymously. For me the meaning of the last differs from that of the others. An accurate or exact dot product means that the result is computed to the fullest possible accuracy. Not a single bit is lost.

Here is why I see the issue in this way:

A. The most natural way to accumulate numbers is fixed-point accumulation. It is simple, error free and fast. This is also true for the accumulation of floating-point numbers and of their products. If the result register is wide enough it can be done without exception. The result is exact. Not a single bit is lost. The arithmetic to achieve this is much the same as that of a conventional CPU. Fixed-point accumulation of floating-point sums and dot products can be realized in hardware at low cost. And it is very very fast. If supported by a vectorizing compiler it would boost both the speed of a computation and the accuracy of the result.

Fully accurate sums and dot products improve many applications. As a by-product, multiple precision real and interval arithmetic can be done at very high speed. With operator overloading they are very easy to use. With a long precision interval arithmetic, for instance, highly accurate enclosures of orbits of dynamical systems have been obtained for considerable long durations. Iterated defect correction is another important class of applications. The method can be applied to compute enclosures of arithmetic expressions or of polynomials with very high accuracy. The result is an enclosure as a long precision interval. Verified solution of badly conditioned systems of linear equations by use of the Rump-operator is another large class of important applications. Finally, of course, a faithfully rounded result can be obtained. All these and other applications of an accurate dot product come with very high speed. They can be considered as top-down approaches of a fully accurate dot product.

B. In contrast to this the Rump-Ogita-Oishi method is a bottom-up approach. I mentioned in my mail of January 26, 2006 that I very much admire this method. It achieves faithfully rounded sums and dot products just by using conventional floating-point arithmetic. The methods are fast in comparison with other software methods. This certainly is a great achievement of our field. Applications of these methods are inherently a subset of the applications of A.

I do not see any reason why we need the methods B. as justification for accurate sums and dot products in the next arithmetic standard. Fixed-point accumulation of sums and dot products is the additive equivalent of fast multiplication

techniques, for instance by an adder tree. The advantages, the cost and gain in speed of both techniques are similar. I do not see any reason why mathematicians should hesitate to require this mode of operation from a new arithmetic standard. If we do not require it we will never get it. We would not have got floating-point operations with directed roundings if IEEE 754 hadn't required it.

With best regards

Ulrich Kulisch

June 2006

Dear colleagues:

Following the discussion on elementary functions, my colleagues here urged me to comment to you on this subject. These are my comments:

Concepts like correct rounding, well rounded, faithful rounding, monotone rounding, and others have been discussed at length. I think a clear distinction should be made between arithmetic operations and elementary functions.

The IEEE 754 standard requires that arithmetic operations are provided with four different roundings: Rounding downwards, rounding upwards, rounding towards zero, and rounding to the nearest floating-point number (round to nearest even). All these roundings are monotone. Implementation of these operations is well understood and established. It is supported by hardware (guard digits, etc.). The error is less than 1 or 0.5 ulp respectively. But what is most important is that the potential error is known to the user so that he can deal with it.

The situation is very different for elementary functions. Extremely accurate evaluation of elementary functions for all relevant argument values needs several guard digits in each individual case. In general, however, the hardware does not support enough guard digits. Their realization in software results in slow function evaluations. A practical compromise is to evaluate elementary functions just using machine precision. Function evaluation is then fast. Experience shows that for the double precision format this can be done for the conventional 24 elementary functions with an error that is less than 1.5 ulp. Even for a long data type elementary functions can be implemented with an error less than a few ulp.

Of utmost importance, however, is that all elementary functions must be provided with proven and reliable error bounds. This error bound must be made known to the user so that he can deal with it. He should know just what he gets if an elementary function is used in a program. It is the vendor's responsibility to deliver these error bounds. Error estimates or error statements based on speculation are simply not acceptable. Of course, deriving proven reliable *a priori* error bounds can take a lot of work. But this work has to be done only once. A great deal of it can be done by use of the computer and of interval arithmetic. For an individual elementary function different error bounds may be obtained for different evaluation domains. Their maximum then is a global error bound. Proven error bounds must consider all error sources, like the approximation error in a reduced range, errors resulting from range reductions, etc.

Correctly rounded, well rounded, faithfully rounded, or monotone rounded elementary functions would be desirable since they might preserve nice mathematical properties. For a 32 bit data format this may be a realistic requirement.

But they will be very very difficult to achieve for the longer data formats which are expected to be available in a new IEEE arithmetic standard. Of course, elementary functions should be provided for all data formats of a new arithmetic standard and possibly even for a dynamic data format. For a 128 bit data format, for instance, an error bound of 3 bits certainly would be acceptable. Directed rounding, of course, must deliver lower and upper bounds appropriately.

Comments on interval elementary functions have been solicited. Of course, high accuracy is desirable. However, to require results that differ from the correct result by only the monotone directed roundings is quite unrealistic. Speed also is an issue for interval arithmetic! For the double precision format the elementary functions have been implemented for interval arguments (just using double precision arithmetic) with proven reliable error bounds that differ from the best possible interval enclosure of the result by an error that is, say, less than 1.5 ulp for each of the bounds. This is fully acceptable!

A programming language or an arithmetic standard that supports interval arithmetic should provide highly accurate elementary functions for interval data for all data formats of the standard and for dynamic precision. These function evaluations suffer little from overestimation caused by interval arithmetic. For point intervals the computed bounds show immediately how accurately the function has been evaluated.

Lots of experience is available concerning the implementation of elementary and special functions for real and interval arguments with proven reliable error bounds for diverse data formats. I refer to published and unpublished work of Walter Kraemer, Werner Hofschuster, Frithjof Blomquist, and others.

For easy and fast evaluation of special functions and of complex elementary functions it would be extremely useful if a new standard would provide, in addition to the usual elementary functions, a number of auxiliary functions with proven *a priory* error bounds. Examples are: $f(x) = sqrt(1 + x) - 1$, $g(x) = 0.5 * log(x * x + y * y)$, $h(x) = exp(x) - 1$, $r(x) = sqrt(x * x - 1)$, and perhaps some others.

Beyond of these issues, it must be remembered that a most important elementary function is a fully accurate scalar product! As a side effect it would boost both the speed of a computation and the accuracy of its result. A fused multiply and add operation at the matrix level is inherent to it, and is fundamental to the whole of numerical analysis. Also, fast multiple precision arithmetic can easily be provided with it to a certain extent.

The vendor is responsible for the quality of the arithmetic and of the elementary functions, and he has to provide valid (guaranteed) error bounds. The user is responsible for the mapping of his problem onto the computer and for the interpretation of the computed result. These are distinct responsibilities. They should not be confused or conflated.

It is my personal opinion that a new arithmetic standard should primarily standardize certain data formats for ease of data transfer between different platforms. In my opinion it is not desirable that all platforms in all instances should be required to react in an identical way. Pinning details down at too early a stage may greatly hinder further progress. Competition is healthy and continued development depends on it.

This and my earlier letters to the IEEE754 revision group have the support of the GAMM-Fachausschuss on Computer Arithmetic and Scientific Computing.

With best regards

Ulrich Kulisch

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