

# Linear-to-Branched Micelles Transition: A Rheometry and Diffusing Wave Spectroscopy (DWS) Study

C. Oelschlaeger,<sup>\*,†</sup> M. Schopferer,<sup>†</sup> F. Scheffold,<sup>‡</sup> and N. Willenbacher<sup>†</sup>

*Institute of Mechanical Process Engineering and Mechanics, University Karlsruhe, Gotthard-Franz-Str. 3, 76128 Karlsruhe, Germany, and Department of Physics, University of Fribourg, 1700 Fribourg Perolles, Switzerland*

*Received July 25, 2008. Revised Manuscript Received October 1, 2008*

The frequency-dependent shear modulus of aqueous wormlike micellar solutions of cetylpyridinium chloride (CPyCl) and sodium salicylate (NaSal) has been measured over a broad frequency range from  $10^{-2}$  to  $10^6$  rad/s using diffusing wave spectroscopy (DWS) based tracer microrheology as well as mechanical techniques including rotational rheometry and oscillatory squeeze flow. Good agreement between mechanical and optical techniques is found in the frequency range from  $10^{-1}$  to  $10^5$  rad/s (Willenbacher, N.; Oelschlaeger, C.; Schopferer, M.; Fischer, P.; Cardinaux, F.; Scheffold, F. *Phys. Rev. Lett.* **2007**, *99* (6), 068302). At intermediate frequencies between 10 and  $10^4$  rad/s, squeeze flow provides most accurate data and is used to determine the plateau modulus  $G_0$ , which is related to the cross-link density or mesh size of the entanglement network, as well as the scission energy  $E_{\text{sciss}}$ , which is deduced from the temperature dependence of the shear moduli in the plateau zone. In the frequency range above  $10^4$  rad/s, DWS including a new inertia correction is most reliable and is used to determine the persistence length  $l_p$ . The system CPyCl/NaSal is known to exhibit two maxima in zero-shear viscosity and terminal relaxation time as the salt/surfactant ratio  $R$  is varied (Rehage, H.; Hoffman, H. *J. Phys. Chem.* **1988**, *92* (16), 4712–4719). The first maximum is attributed to a transition from linear to branched micelles (Lequeux, F. *Europhys. Lett.* **1992**, *19* (8), 675–681), and the second one is accompanied by a charge reversal due to strongly binding counterions. Here, we discuss the variation of  $G_0$ ,  $E_{\text{sciss}}$ , and  $l_p$  with salt/surfactant ratio  $R$  at constant surfactant concentration of 100 mM CPyCl.  $G_0$  increases at the linear-to-branched micelles transition, and this is attributed to the additional contribution of branching points to the cross-link density.  $E_{\text{sciss}}$  exhibits two maxima analogous to the zero-shear viscosity, which can be understood in terms of the variation of micellar length and variation of the amount of branched micelles and contour length between branching points consistent with the results of a comprehensive cryo-transmission electron microscopy (TEM) study (Abezgaux, L.; Ramon, O.; Danino, D. Department of Biotechnology and Food Engineering, Technion, Haifa, Israel. European Colloid and Interface Society, Geneva, 2007). The persistence length decreases with increasing  $R$ . This decrease is stronger than expected from the decrease of Debye length according to the Odijk–Skolnick–Fixman (OSF) theory and is attributed to the penetration of salicylate ions into the micelles; the linear-to-branched transition obviously does not have an effect on  $l_p$ .

## 1. Introduction

In solution, amphiphilic surfactant molecules can self-assemble to form various structures such as spherical or wormlike micelles, vesicles, or hexagonal and lamellar liquid crystalline structures. These different aggregation structures can show distinct rheological properties. Surfactant solutions with wormlike micellar structures are widely used in home and personal care products as well as enhanced oil recovery but also as drag reduction agents in district heating systems or most recently as templates for asymmetric and aligned nanostructures as well as sieving matrix for separation of DNA fragments.<sup>5,6</sup> The structural and rheological properties of wormlike micelles (WLMs) have been investigated intensively not only because of their wide application range, but also because they show many analogies to covalently bonded polyelectrolytes and can be used as model systems to study the structure and dynamics of polymers. Since micelles break and reform (rate constant  $k$ ), they are often termed “equilibrium” or

“living” polymers. Small changes in surfactant structure, counterion type and concentration, added electrolytes, or temperature can alter the length, flexibility, and interactions of micelles, drastically resulting in pronounced effects on macroscopic rheological properties. In particular, various ionic surfactants show a pronounced maximum of the zero-shear viscosity as the salt/surfactant ratio is varied.<sup>7–11</sup> This is of significant interest from an application point of view, since this viscosity maximum is closely related to the application properties of corresponding surfactant systems, but also from a scientific point of view, since the structural changes corresponding to this viscosity maximum are still not really clear. Several studies support the transition from linear to branched micelles: for example, a combined cryo-transmission electron microscopy (TEM), small-angle neutron scattering (SANS), and rheology study on the system erucyl-bis(hydroxyethyl)methylammonium chloride (EHAC)/KCl consistently revealed a transition from linear to branched micelles around the viscosity maximum.<sup>12</sup> In contrast to ordinary polymers, these branch points can slide along the micelles and hence provide

<sup>†</sup> University Karlsruhe.

<sup>‡</sup> University of Fribourg.

(1) Willenbacher, N.; Oelschlaeger, C.; Schopferer, M.; Fischer, P.; Cardinaux, F.; Scheffold, F. *Phys. Rev. Lett.* **2007**, *99*(6), 068302.

(2) Rehage, H.; Hoffmann, H. *J. Phys. Chem.* **1988**, *92*(16), 4712–4719.

(3) Lequeux, F. *Europhys. Lett.* **1992**, *19*(8), 675–681.

(4) Abezgaux, L.; Ramon, O.; Danino, D. Department of Biotechnology and Food Engineering, Technion, Haifa, Israel. European Colloid and Interface Society, Geneva, 2007.

(5) Walker, L. M. *Curr. Opin. Colloid Interface Sci.* **2001**, *6*(5–6), 451–456.

(6) Yang, J. *Curr. Opin. Colloid Interface Sci.* **2002**, *7*(5–6), 276–281.

(7) Candau, S. J.; Khatory, A.; Lequeux, F.; Kern, F. *J. Phys. IV* **1993**, *3*, 197–209.

(8) Cappelare, E.; Cressely, R. *Colloid Polym. Sci.* **1998**, *276*, 1050–1056.

(9) Cappelare, E.; Cressely, R. *Rheol. Acta* **2000**, *39*, 346–353.

(10) Raghavan, S. R.; Kaler, E. W. *Langmuir* **2001**, *17*, 300–306.

(11) Schubert, B. A.; Kaler, E. W.; Wagner, N. J. *Langmuir* **2003**, *19*, 4079–4089.

(12) Croce, V.; Cosgrove, T.; Maitland, G.; Hughes, T.; Karlsson, G. *Langmuir* **2003**, *19*, 8536–8541.

69 a high number of degrees of freedom for reptation resulting in  
70 the observed viscosity reduction. In contrast, for the system cetyl  
71 triammonium chloride (CTAC) and sodium salicylate (NaSal),  
72 cryo-TEM images did not reveal significant branching around  
73 the viscosity maximum and the viscosity drop was attributed to  
74 a change in micellar breakage time.<sup>14</sup> For the systems cetyl  
75 triammonium bromide (CTAB)<sup>14,15</sup> and cetyl pyridinium chloride  
76 (CPyCl) with NaSal as strongly binding counterion,<sup>2</sup> even a  
77 second viscosity maximum is observed when the salt concentra-  
78 tion is further increased, but the underlying structural or dynamic  
79 change of the system has not been resolved yet. In this study,  
80 we use a recently established experimental approach<sup>1</sup> combining  
81 mechanical high frequency rheology and optical microrheology  
82 to get new insight into structural and dynamic changes ac-  
83 companying the characteristic viscosity maxima observed in the  
84 CPyCl/NaSal system at characteristic surfactant-to-salt ratios  $R$ .  
85 The newly established approach gives access to the linear  
86 viscoelastic properties of these solutions at frequencies up to 1  
87 MHz. We investigate the dependence of the plateau modulus  $G_0$ ,  
88 the scission energy  $E_{\text{sciss}}$ , and the persistence length  $l_p$  with salt/  
89 surfactant ratio  $R$  at constant surfactant concentration of 100  
90 mM CPyCl. On the one hand, despite the large amount of literature  
91 for this system, no results on the scission energy and bending  
92 stiffness are available so far. On the other hand, this system is  
93 particularly suited for the proposed study, since it has been shown  
94 that there is good agreement between mechanical rheometry data  
95 and optical microrheology<sup>1,16</sup> in a very broad frequency range,  
96 and thus, the high frequency linear viscoelastic properties can  
97 be characterized thoroughly.

## 2. Relationship between Dynamical and Structural Features of Entangled Wormlike Micellar Solutions

100 Long and flexible linear micelles, commonly referred to as  
101 “wormlike” micelles, can be described by a number of structural  
102 parameters, which cover a broad range of length scales. The  
103 overall length of the micelles is referred to as the contour length  
104  $L$  and varies from a few nanometers to micrometers. A mean  
105 field treatment of the growth process for highly screened micelles  
106 has been obtained from the models derived by Cates<sup>17–19</sup> and  
107 predicts an exponential distribution of length  $N(L)$ :

$$108 \quad N(L) \propto \exp\left(-\frac{L}{\bar{L}}\right) \quad (1)$$

109 with the average length given by

$$110 \quad \bar{L} \cong \varphi^{0.5} \exp\left(\frac{E_{\text{sciss}}}{2k_B T}\right) \quad (2)$$

111 where  $\varphi$  is the surfactant volume fraction,  $T$  is the temperature,  
112 and  $E_{\text{sciss}}$  is the scission energy of the micelle, that represents the  
113 excess free energy for a pair of hemispherical end-caps relative  
114 to a rodlike region containing an equal number of surfactants.  
115 Slight changes in the composition of surfactant solutions are  
116 expected to affect their overall length, which is directly related  
117 to the scission energy. In the present study, we investigate the

(13) Clausen, T.; Vinson, P. K.; Minter, J. R.; Davis, H. T.; Talmon, Y.; Miller, W. G. *J. Phys. Chem.* **1992**, 96(1), 474–484.

(14) Nemoto, N.; Kuwahara, M.; Yao, M.-L.; Osaki, K. *Langmuir* **1995**, 11, 30–36.

(15) Galvan-Miyoshi, J.; Delgado, J.; Castillo, R. *Eur. Phys. J. E.* **2008**, 26(4), 369–377.

(16) Buchanan, M.; Atakhorrami, M.; Palierno, J. F.; Schmidt, C. F. *Macromolecules* **2005**, 38, 8840–8844.

(17) Cates, M. E. *J. Phys. (Paris)* **1988**, 49, 1593.

(18) Cates, M. E. *Macromolecules* **1987**, 20, 2289.

(19) Israelachvili, J.; Mitchell, D. J.; Ninham, B. W. *J. Chem. Soc., Faraday Trans. 2* **1976**, 72, 1525.

118 influence of the scission energy on the dynamics and structure  
119 of micellar solutions. For charged systems, this quantity has two  
120 contributions:

$$121 \quad E_{\text{sciss}} = E_c - E_e \quad (3)$$

122  $E_c$  is the energy required to create two hemispherical end-caps  
123 as a result of scission of the wormlike micelles and reflects the  
124 differences in surfactant packing in the end-caps versus the  
125 cylindrical body of the micelles. For nonionic micelles or for  
126 ionic micelles at high ionic strength,  $E_{\text{sciss}} = E_c$ . For ionic micelles,  
127 repulsion between charged head groups favors micelle breaking  
128 and lowers  $E_{\text{sciss}}$ ; this effect is summarized in  $E_e$ . According to  
129 the theory of Cates and Granek,<sup>57</sup> the scission energy  $E_{\text{sciss}}$  is  
130 related to the temperature dependence of the moduli  $G'$  and  $G''$   
131 at intermediate frequencies, in the so-called entanglement regime,  
132 where  $G'$  exhibits a plateau and  $G''$  ( $\ll G'$ ) goes through a  
133 minimum (in so-called Cole–Cole plots, significant deviations  
134 occur from the semicircular shape expected for Maxwell fluids).  
135 In this regime, the ratio  $G''_{\text{min}}/G_0$  is related to  $l_e$  (contour length  
136 between two successive entanglements) and  $\bar{L}$  according to<sup>57</sup>

$$137 \quad \frac{G''_{\text{min}}}{G_0} \sim \frac{l_e}{\bar{L}} \sim \varphi^{-1.85} \exp\left(-\frac{E_{\text{sciss}}}{2k_B T}\right) \quad (4)$$

138 In the case of formation of branched micelles which correspond  
139 to the formation of equilibrium cross-links arising through local  
140 fusion of micelles, a model based on the coupled reptation/  
141 reaction for branched micelles was developed by Lequeux.<sup>3</sup> In  
142 the frame of this model, all the results concerning the rheology  
143 of linear wormlike micelles can be applied to branched micelles,  
144 provided that one substitutes  $\bar{L}$  by  $\bar{L}_c$ , where  $\bar{L}_c$  represents the  
145 harmonic mean between the average distance from one point  
146 along the micelle to the first cross-link and the average distance  
147 from that point to the first end-cap. Consequently, we determine  
148 the scission energy using the same method (section 4.2.2) for  
149 linear as well as for branched micelles. Another key structural  
150 parameter for wormlike micellar solutions investigated here is  
151 the plateau modulus  $G_0$ . This parameter, determined at inter-  
152 mediate frequencies, is directly related to the mesh size  $\xi$  of the  
153 system with  $G_0 \sim \xi^{-3}$  and is typically independent of temperature.<sup>1</sup>  
154 We also investigate the high frequency range; in this regime, the  
155 stress relaxation, for linear micelles as well as for branched  
156 micelles, is controlled by the internal dynamics of short micelle  
157 segments and the moduli  $G'$  and  $G''$  show characteristic scaling  
158 behavior.

$$159 \quad G' \sim G'' \sim \omega^\alpha \quad (5)$$

160 First, the Rouse–Zimm modes dominate and  $\alpha = 1/2 - 2/3$ .

161 At even higher frequencies, internal bending modes of single  
162 Kuhn segments determine  $G'$  and  $G''$ , and hence, these dynamic  
163 parameters are related to the bending modulus  $\kappa$  as a structural  
164 parameter;  $\kappa$  is often expressed in terms of the persistence length  
165  $\kappa = k_B T/l_p$ . In this frequency range, the scaling exponent  $\alpha =$   
166  $3/4$  as predicted by Morse,<sup>20</sup> and Gittes and MacKintosh.<sup>21</sup>

167 The transition between these scaling regimes is marked by the  
168 inverse of the shortest Rouse relaxation time  $\omega_0 = \tau_0^{-1}$  which  
169 is directly related to the persistence length  $l_p$ .

$$170 \quad \omega_0 = \frac{k_B T}{8\eta_s l_p} \quad (6)$$

171 where  $\eta_s$  is the solvent viscosity.

(20) Morse, D. C. *Phys. Rev. E* **1998**, 58(2), R1237–R1240.

(21) Gittes, F.; MacKintosh, F. C. *Phys. Rev. E* **1998**, 58(2), R1241–R1244.

172 The persistence length  $l_p$  can also be determined from the  
173 absolute values of  $G'$  and  $G''$  in the  $\alpha = 3/4$  scaling regime  
174 according to a relationship based on a statistical mechanical  
175 treatment of the single filament stress response of semiflexible  
176 chains presented in ref 21:

$$G^* = \frac{\rho}{15} Kl_p \left( \frac{-2i\zeta}{K} \right) \omega^{3/4} - i\omega\eta_s \quad (7)$$

178 where  $\zeta$  is the lateral drag coefficient and  $\rho$  is the area density  
179 of micelles. The latter can be calculated as  $\rho = \phi_{\text{surf}}/((\pi/4)d_{\text{mic}}^2)$   
180 where  $\phi_{\text{surf}}$  is the surfactant concentration (vol/vol) and  $(\pi/4)d_{\text{mic}}^2$   
181 is the cross-sectional area of the micelles. So far,  $l_p$  has been  
182 determined using various scattering techniques including small-  
183 angle neutron scattering (SANS)<sup>22–24</sup> as well as static and  
184 dynamic light scattering.<sup>14,25–27</sup> Birefringence measurements  
185 can also be used to determine  $l_p$ .<sup>28</sup> Recently, it has been  
186 demonstrated that also another neutron scattering technique,  
187 namely, neutron spin echo (NSE), can be used to determine the  
188 persistence length.<sup>29</sup> Robust and reliable models are available to  
189 analyze scattering data, and SANS is a well established tool to  
190 characterize wormlike micelles. However, limited access to large  
191 scale facilities hinders its broad application for systematic  
192 investigations with careful parameter variation. Light scattering  
193 techniques are suitable for stiff micelles ( $l_p \approx 100$  nm) only, due  
194 to the different  $q$ -range which is accessed. Birefringence  
195 measurements require the knowledge of optical constants which  
196 are often not known. Recently, we have demonstrated that the  
197 high frequency range where the  $\omega^{3/4}$ -scaling occurs can be  
198 accessed by optical as well as mechanical rheometry. Accordingly,  
199 these techniques can be used to determine  $l_p$  according to eqs 5  
200 and 6 even for  $l_p$  values down to a few nm.<sup>1</sup> In order to improve  
201 the quality of the DWS data and to increase the accessible  
202 frequency range to the MHz range, a self-consistent inertia  
203 correction has been introduced<sup>1,30–32</sup> for the DWS data.

204 All these structural features, the characteristic length scales,  
205 and the corresponding characteristic relaxation times strongly  
206 depend not only on the chemical nature and concentration of the  
207 surfactant or surfactant mixture under consideration, but also on  
208 the nature and concentration of the counterion (binding vs  
209 nonbinding) and the ionic strength of the solution. This has been  
210 studied intensively not only by rheological experiments but also  
211 by using electron microscopy and various scattering tech-  
212 niques.<sup>11,28,33,34</sup> Cryo-TEM, for example, has been used to  
213 visualize entanglements, branching, and the semiflexible, worm-  
214 like nature of the micelles directly.<sup>12,13,35–37</sup>

215 In the first part of this paper, we establish the relationship  
216 between dynamical and structural features of entangled solutions  
217 of wormlike micelles and we compare results from mechanical

218 rheometry and optical microrheology. We focus on three different  
219 parameters: plateau modulus, scission energy, and persistence  
220 length. In the second part of the paper, we investigate the effect  
221 of salt concentration on these three parameters for the system  
222 CPyCl in the presence of NaSal.

### 223 3. Materials and Methods

224 **3.1. Sample Characteristics.** Aqueous solutions of surfactant/  
225 counterion mixtures cetylpyridinium chloride/sodium salicylate  
226 (CPyCl/NaSal) were used as model systems. CPyCl and NaSal were  
227 both obtained from C. Roth. The sample solutions were prepared  
228 by gently stirring the surfactant and salt in deionized water. For  
229 equilibrium measurements, they were stored for at least 1 day at 20  
230 °C. This solution exhibits a very strong viscoelastic response in the  
231 temperature range between 20 and 40 °C.<sup>38,39</sup>

232 **3.2. DWS Based Optical Microrheology.** The basic idea of  
233 optical microrheology is to study the equilibrium thermal response  
234 of small (colloidal) particles embedded in a material and thereby  
235 obtain quantitative information about the macroscopic loss and storage  
236 moduli,  $G'(\omega)$  and  $G''(\omega)$ , over an extended range of frequencies.  
237 The modern way of using this technique was introduced in the mid-  
238 1990s when Mason and Weitz proposed a quantitative relation  
239 between the tracer mean-squared displacement  $\langle \Delta r^2(t) \rangle$  and the  
240 complex shear modulus  $G^*(\omega)$ .<sup>40</sup> The Laplace transform of the  
241 particle mean squared displacement  $\langle \Delta r^2(i\omega) \rangle$  is related to the complex  
242 modulus of the sample via a generalized Stokes–Einstein equation  
243 (GSE):

$$G^*(\omega) = \frac{k_B T}{\pi a i \omega \langle \Delta r^2(i\omega) \rangle} = G'(\omega) + iG''(\omega) \quad (8)$$

244 Assuming that the complex fluid can be treated as an isotropic,  
245 incompressible continuum around a sphere, this relation was later  
246 confirmed theoretically.<sup>41</sup> Under this condition, the GSE is valid  
247 essentially for all cases of practical interest except for the limit of  
248 ultrahigh frequencies where inertia effects start to play a role. At  
249 times much shorter than  $10^{-5}$  s, or frequencies well above  $\omega = 10^5$   
250 rad/s, inertia effects become significant.<sup>30</sup> This means that  $\langle \Delta r^2(t) \rangle$   
251 not only is given by the viscous (or viscoelastic) properties of the  
252 medium as assumed above but is distorted by inertia effects at times  
253 much shorter than  $10^{-4}$  s. The goal is therefore to recover the motion  
254 pattern one would observe in the absence of inertia effects. In order  
255 to be able to access this interesting ultrahigh frequency regime, we  
256 have recently introduced a simple (self-consistent) correction  
257 scheme.<sup>1</sup> Previous studies on dense colloidal suspensions have shown  
258 that the effective high frequency viscosity determines the influence  
259 of fluid inertia.<sup>31</sup> From the raw  $G''(\omega)$  data, we determine the effective  
260 high frequency viscosity of approximately 3 mPas from a fit to  
261 the loss modulus  $G''(\omega) = \eta(\omega)\omega$  in the regime  $\omega = 10^5$ – $10^6$  s<sup>-1</sup>.  
262 We then correct the particle mean square displacement for inertia  
263 effects based on the theory of Hinch<sup>32</sup> developed for the motion of  
264 a sphere in a simple fluid with viscosity  $\eta$ . In a second iteration step,  
265 we again fit the resulting loss modulus and repeat this procedure  
266 several times. In our case, the correction factor attains its smallest  
267 value of 0.7 for the shortest time analyzed  $\tau = 5 \times 10^{-7}$  s.  
268

269 For a quantitative interpretation of the raw experimental data  
270  $\langle \Delta r^2(t) \rangle$ , the Laplace transformation is the most critical part of the  
271 analysis. To reduce truncation errors, we apply a procedure suggested  
272 by Mason and co-workers. We estimate  $\tilde{G}(s)$  by substituting  $\langle \Delta r^2(t) \rangle$   
273 into an algebraic Stokes–Einstein form:<sup>42</sup>

(35) Lin, Z. *Langmuir* **1996**, *12*(7), 1729–1737.

(36) Bernheim-Groswasser, A.; Wachtel, E.; Talmon, Y. *Langmuir* **2000**, *16*(9), 4131–4140.

(37) Bernheim-Groswasser, A.; Zana, R.; Talmon, Y. *J. Phys. Chem. B* **2000**, *104*(51), 12192–12201.

(38) Rehage, H.; Hoffmann, H. *Mol. Phys.* **1991**, *74*, 933.

(39) Fischer, P.; Rehage, H. *Rheol. Acta* **1997**, *36*, 13.

(40) Mason, T. G.; Weitz, D. A. *Phys. Rev. Lett.* **1995**, *74*, 1250.

(41) Levine, A. J.; Lubensky, T. C. *Phys. Rev. E* **2001**, *63*, 1–4.

(22) Magid, L. J.; Han, Z.; Li, Z.; Butler, P. D. *J. Phys. Chem. B* **2000**, *104*(29), 6717–6727.

(23) Hoffmann, H.; Kalus, J.; Schwandner, B. *Ber. Bunsen-Ges.* **1987**, *91*, 99–106.

(24) Pedersen, J. S.; Laso, M.; Schurtenberger, P. *Phys. Rev. E* **1996**, *54*, R5917–5920.

(25) Brown, W.; Johansson, K.; Almgren, M. *J. Phys. Chem.* **1989**, *93*(15), 5888–5894.

(26) Imae, T. *J. Phys. Chem.* **1990**, *94*, 5953–5959.

(27) Buhler, E.; Munch, J. P.; Candau, S. J. *J. Phys. II* **1995**, *5*(6), 765–787.

(28) Shikata, T.; Dahman, S. J.; Pearson, D. S. *Langmuir* **1994**, *10*(10), 3470–3476.

(29) Nettesheim, F.; Wagner, N. J. *Langmuir* **2007**, *23*, 5267–5269.

(30) Weitz, D. A.; Pine, D. J.; Pusey, P. N.; Though, R. J. A. *Phys. Rev. Lett.* **1989**, *63*, 1747.

(31) Ladd, A. J. C.; Gang, H.; Zhu, J. X.; Weitz, D. A. *Phys. Rev. Lett.* **1995**, *74*, 318.

(32) Hinch, E. *J. Fluid Mech.* **1975**, *72*, 499.

(33) Cates, M. E.; Candau, S. J. *J. Phys.: Condens. Matter* **1990**, *2*, 6869–6892.

(34) Magid, L. J.; Li, Z.; Butler, P. D. *Langmuir* **2000**, *16*, 10028–10036.



$$\tilde{G}(s) = \frac{k_B T}{\pi a \langle \Delta r^2(t) \rangle \Gamma[1 + (\partial \ln \langle \Delta r^2(t) \rangle / \partial t)^{1/s}]} \quad (9)$$

In order to reduce scatter, we first fit  $\langle \Delta r^2(t) \rangle$  with a polynomial of order 6 or 7 and then use eq 9 to extract the moduli  $G'(\omega)$  and  $G''(\omega)$ . We have checked that the choice of the polynomial order and the range of data selected do not influence the results. Finally, it is worthwhile to note that, contrary to mechanical measurements, the in- and out-of-phase contributions are not measured independently but have to be extracted from a single value of the slope  $\partial \ln \langle \Delta r^2(t) \rangle / \partial t$ . As a consequence, if  $G'(\omega)$  and  $G''(\omega)$  are of different magnitude, the lower value extracted from DWS measurements is often not very well defined.

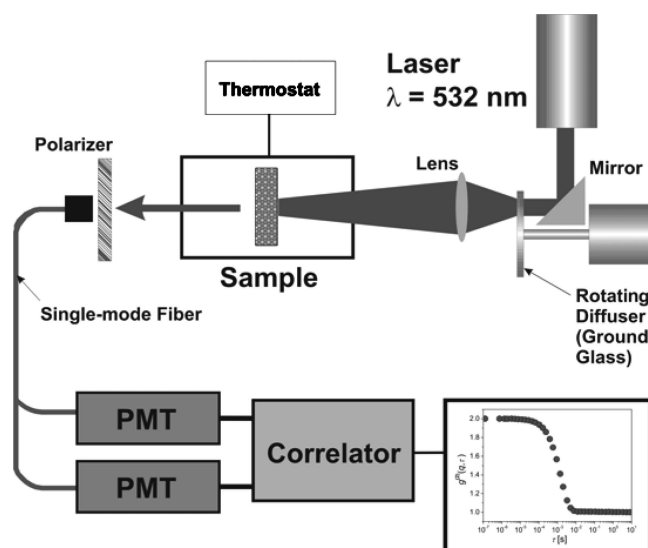
A number of methods have been applied successfully to measure the particle mean square displacement, notably single particle tracking by microscopy, laser deflection, and diffusing wave spectroscopy (DWS).<sup>43–45</sup> In this work, we have chosen DWS as the only technique that provides access to frequencies well above  $10^4$  rad/s. The DWS technique is an extension of dynamic light scattering (DLS) to soft materials exhibiting strong multiple scattering.<sup>46</sup> The method allows one to monitor the displacement of micrometer sized colloidal particles with subnanometer precision and on time scales as short as 10 ns. In recent years, significant progress has been made in development of the DWS approach, and it has been successfully applied to the study of fluid and solid media, for example, colloidal suspensions, gels, and biocolloids (yogurt and cheese) as well as ceramic slurries and green bodies.<sup>47–50</sup> In a DWS experiment, coherent laser light impinges on one side of a turbid sample and the intensity fluctuations of the light propagated through the sample are then analyzed either in transmission or backscattering geometry. A diffusion model is used to describe the propagation of photons across the sample. Analogous to traditional dynamic light scattering (DLS), for the case of noninteracting particles, it is possible to express the measured intensity autocorrelation function (ICF)  $g_2(\tau) - 1 = \langle I(t) I(t + \tau) \rangle / \langle I \rangle^2 - 1$  in terms of the mean square displacement of the scattering particle,

$$g_2(\tau) - 1 = \left[ \int_0^\infty ds P(s) \exp(-s/l^* k^2 \langle \Delta r^2(\tau) \rangle) \right]^2 \quad (10)$$

with  $k = 2\pi n/\lambda$  being the wavenumber of light in a medium with refractive index  $n$ .  $P(s)$  is the distribution of photon trajectories of length  $s$  in the sample, and it can be calculated within the diffusion model taking into account the experimental geometry. For the case of transmission through a slab (plane-wave illumination), one obtains

$$g_2(\tau) - 1 = \left[ \frac{(L/l^* + 4/3) \langle \sqrt{k_0^2 \Delta r^2(\tau)} \rangle}{\sinh[(L/l^* + 4/3) \langle \sqrt{k_0^2 \Delta r^2(\tau)} \rangle]} \right]^2 \quad (11)$$

The transport mean free path  $l^*$  characterizes the typical step length of the photon random walk, given by the individual particle scattering properties and particle concentration, and  $l^*$  can be determined independently by a comparison of the measured count rate to the one obtained with a sample of known  $l^*$  (ref 51) and therefore enters the analysis as a constant parameter. Equation 11 numerically calculated the particle mean square displacement  $\langle \Delta r^2(t) \rangle$



**Figure 1.** Schematic diagram of our DWS setup. Laser light is scattered from a ground glass rotated by a fast stepper motor, and the transmitted light is collected by a lens to illuminate the sample. A single mode fiber collects the scattered light in transmission. The collected light is subsequently analyzed by a single-photon detector and digital photon counter.

from the measured autocorrelation function  $g_2(t)$ . In our experiments, we added 2% polystyrene sulfonate particles (diameter 720 nm, IDC Corporation, Portland, OR) to the micellar solution temporarily heated to 60 °C in order to reduce the viscosity. The sample was filled in standard glass cuvettes (Hellma) with a path length of 2 mm and a width of 10 mm. The temperature was controlled within  $\pm 0.1$  °C using a home-built temperature control chamber. A frequency doubled neodymium:yttrium vanadate (Nd:YV04) laser (Verdi, Coherent) operating at a wavelength  $\lambda = 532$  nm was used to illuminate a circular ground glass mounted on a two phase stepper motor (KH42HM2-851 from Japan Servo). Putting a fast rotating diffuser in the optical path between the laser and sample allows for more efficient ensemble averaging.<sup>52</sup> We collected the transmitted light coming from the ground glass and focused it onto the sample with a spot size diameter of roughly 5 mm. The scattered laser light was then collected using a single-mode optical fiber and single photon counter and subsequently analyzed by using a digital correlator (Correlator.com, NJ). By numerical analysis using eq 11, we extracted the particle mean square displacement  $\langle \Delta r^2(t) \rangle$  from the ICF typically over a range of values  $g_2 = 0.01 - 0.99$ . Figure 1 shows a schematic diagram of our DWS setup.

**3.3. Squeeze Flow.** Oscillatory squeeze flow experiments were performed using a piezo-driven axial vibrator (PAV). General theory of squeeze flow is covered in standard textbooks of fluid mechanics.<sup>53</sup> The theory of the PAV as well as the mechanical and electronic setup are thoroughly discussed elsewhere,<sup>54,55</sup> and therefore, this is summarized here only briefly. The actor is a thin-walled quadratic copper tube with a thick stainless steel plate on top. Four piezoelectric actuators are attached to two opposite walls of the tube in order to exert the vibrations, and four additional piezoelectric sensors are fixed to the remaining sides in order to pick up the response signal. Direct coupling of excitation and detection is avoided by four partial cuts of the tube parallel to the longitudinal axis. This lower part of the device is surrounded by a double-walled cylinder allowing for circulation of a thermostating fluid, and the temperature is controlled

(42) von Berlepsch, H.; Harnau, L.; Reineker, P. *J. Phys. Chem. B* **1998**, *102*, 7518.

(43) Xu, J.; Tseng, Y.; Carriere, C. J.; Wirtz, D. *Biomacromolecules* **2002**, *3*, 92–99.

(44) Mason, T. G.; Ganesan, K.; van Zanten, J. H.; Wirtz, D.; Kuo, S. C. *Phys. Rev. Lett.* **1997**, *79*, 3282–3285.

(45) Gardel, M. L.; Valentine, M. T.; Crocker, J. C.; Bausch, A. R.; Weitz, D. A. *Phys. Rev. Lett.* **2003**, *91*, 158302.

(46) Maret, G.; Wolf, P. E. *Z. Phys. B: Condens. Matter* **1987**, *65*, 409–413.

(47) Zakharov, P.; Cardinaux, F.; Scheffold, F. *Phys. Rev. E* **2006**, *73*, xxx.

(48) Scheffold, F.; Schurtenberger, P. *Soft Mater.* **2003**, *1*, 139.

(49) Schurtenberger, P.; Stradner, A.; Romer, S.; Urban, C.; Scheffold, F. *CHIMIA: Int. J. Chem.* **2001**, *55*(3), 155–159.

(50) Heinemann, C.; Cardinaux, F.; Scheffold, F.; Schurtenberger, P.; Escher, F.; Conde-Petit, B. *Carbohydr. Polym.* **2004**, *55*(2), 155–161.

(51) Kaplan, P. D.; Kao, M. H.; Yodh, A. G.; Pine, D. J. *Appl. Opt.* **1993**, *32*, 3828.

(52) Zakharov, P.; Cardinaux, F.; Scheffold, F. *Phys. Rev. E* **2006**, *73*, 011413.

(53) Bird, R. B.; Armstrong, R. C.; Hassager, C. *Dynamics of Polymeric Liquids, Vol. 1, Fluid Dynamics*, 2nd ed.; Wiley: New York, 1987.

(54) Crassous, J. J.; Regisser, R.; Ballauff, M.; Willenbacher, N. *J. Rheol.* **2005**, *49*, 851.

(55) Kirschenmann, L. Ph.D. Thesis, Universität Ulm, 2003, p 11.

with an accuracy of  $\pm 0.04$  °C. The whole setup is covered by a thick metal lid, which is the upper boundary of the gap and provides a complete sealing for the apparatus. The instrument is operated by a lock-in amplifier. The applied voltage of the driving piezos is proportional to the axial force. The instrument operates at a constant force amplitude  $F_0$ , and from the complex ratio of the dynamic displacement of the lower plate (amplitude  $\approx 5$  nm) with and without fluid  $x_f^*/x_0^*$  one can calculate the complex squeeze stiffness  $K^*$  of the fluid using an appropriate mechanical equivalent circuit and solving its equations of motion. In order to calculate  $K^*$  from the ratio of the output voltage  $U/U_0$  and the phase difference  $\Delta\varphi$  recorded by the lock-in amplifier with and without fluid, the mechanical properties (spring constant mass, resonance frequency) of the instrument itself have to be determined as described in ref 55. Finally,  $K^*$  is related to the complex shear modulus  $G^*$  and compressibility  $k_c^*$  by<sup>55</sup>

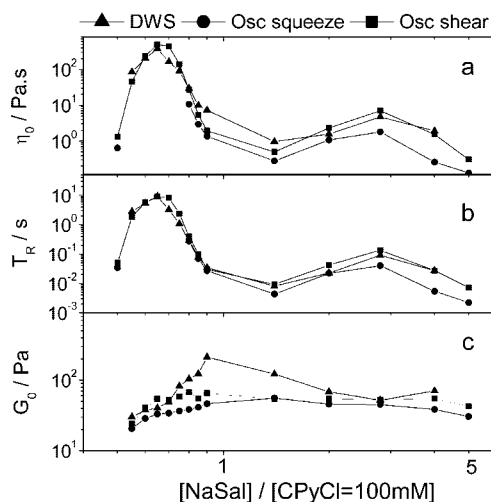
$$\frac{1}{K^*} = \frac{2d^3}{3\pi R^4} \left( \frac{1}{G^*} + \frac{3R^2}{2d^2} k_c^* \right) \quad (12)$$

where  $R$  (here 10 mm) is the radius and  $d$  is the height of the gap. The determination of  $G^*$  strongly depends on the exact knowledge of  $d$ , which is determined by calibration using Newtonian liquids with viscosities between 1 and 2000 mPas. Gap heights between 15 and 100  $\mu\text{m}$  have been used here. The required sample volume is on the order of 100  $\mu\text{L}$  depending on the height of the gap. Samples have to be degassed carefully in order to avoid artificial compressibility from entrapped air. In principle, the measured  $G^*$  values have to be corrected for the  $k_c^*$  contribution. For viscoelastic surfactant solutions investigated, here  $G^*$  is typically far below 1000 Pa and the compressibility is approximately that of water ( $k_{c,w} = 4.6 \times 10^{-10} \text{ Pa}^{-1}$  at 20 °C). Therefore, the corresponding correction to  $G^*$  is well below 5% and can thus be safely neglected. Dynamic shear moduli  $G^*$  in the range from 0.1 Pa to 10 kPa are accessible.

**3.4. Rotational Rheometry.** A rotational rheometer Thermo MARS II equipped with a cone-plate measuring cell (diameter  $d_{CP} = 35$  mm, cone angle  $\alpha_{\text{cone}} = 4^\circ$ ) was used to perform small amplitude oscillatory shear experiments covering the frequency range from 0.01 to 100 rad/s at a strain amplitude  $\gamma_0 = 0.1$ . Strain sweep experiments performed prior to the frequency sweeps confirm that this strain amplitude is sufficiently small to provide a linear material response at all investigated frequencies. Measurements were performed at temperatures between 20 and 40 °C. A solvent trap was used to avoid evaporation of the sample during the experiment.

## 4. Results and Discussion

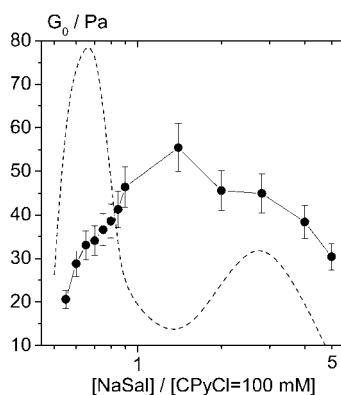
**4.1. Comparison of Mechanical Rheometry and DWS Measurements.** The variation of the dynamic shear moduli  $G'$  and  $G''$  as a function of frequency as determined from mechanical and optical rheometry has been investigated for the system CPyCl/NaSal at  $0.5 < R < 5$ . In general, good agreement is found between mechanical and optical methods. Results for  $R = 0.6$ , corresponding to the first viscosity maximum, have been reported earlier.<sup>1</sup> The shapes of the relaxation spectra from DWS and mechanical rheometry coincide very well over the whole frequency range, but the DWS absolute values of  $G'$  and  $G''$  are shifted with respect to the mechanical measurements. The reasons for this shift have already been discussed in ref 1; they can be attributed to uncertainties in experiment as well as residual perturbations of the complex fluid in the particle vicinity<sup>56</sup> as discussed below. Variations of the zero-shear viscosity  $\eta_0$ , the terminal relaxation time  $T_R$ , and the plateau modulus  $G_0$  as a function of  $R$  from mechanical and optical techniques are given in Figure 2.  $T_R$  and  $G_0$  are directly deduced from the modulus



**Figure 2.** Zero-shear viscosity  $\eta_0$  (a), terminal relaxation time  $T_R$  (b), and plateau modulus  $G_0$  (c) as a function of  $R = [\text{NaSal}]/[\text{CPyCl}]$  at constant surfactant concentration of 100 mM CPyCl obtained from DWS (triangles), oscillatory squeeze flow (circles), and rotational rheometry (squares).  $T = 20$  °C. All the error bars are as large as the size of the different symbols.

curves.  $T_R$  is given by the inverse angular frequency corresponding to the first crossover between  $G'$  and  $G''$ . For DWS and oscillatory squeeze flow,  $G_0$  is determined as the value of the modulus  $G'$  at the frequency at which  $G''$  has its local minimum,  $G_{\text{min}}''$ . For rotational rheometry,  $G_0$  is taken as the value of  $G'$  where it exhibits a constant plateau, since the minimum in  $G''$  is not accessible with this technique. The zero-shear viscosity is obtained by using the equation  $\eta_0 \approx G_0 T_R$ . The first observation is that the variations of  $\eta_0$ ,  $T_R$ , and  $G_0$  as a function of  $R$  are qualitatively the same values independent of the technique used. Both  $\eta_0$  and  $T_R$  pass through two maxima:<sup>2</sup> the first maximum occurs at  $R \sim 0.65$  and the second at  $R \sim 3$ . Interpretations of these variations will be discussed below. For  $T_R$ , the absolute values are in very good agreement for the different techniques, and the differences are within the experimental error. Concerning the variation of the plateau modulus, the results obtained by rotational rheometry and oscillatory squeeze flow are in good agreement at all salt concentrations investigated. On the contrary, the values of  $G_0$  deduced from DWS measurements show strong deviations (factor 1.5 up to 4.5) from mechanical results in a range of  $0.7 < R < 1.4$ . A similar result was obtained by Galvan-Miyoshi et al.<sup>15</sup> studying the micellar CTAB/NaSal system. They also compared DWS results with those obtained from mechanical rheometry and found differences between  $G_0$  values increasing with an increase of salicylate concentration. They speculate that large quantities of free ions ( $\text{Sal}^-$ ) in solution are responsible for this behavior. The free ions are not incorporated into the micelles and could therefore modify the mobility of the Brownian particles. This explanation is not valid in our case, because deviations occur at intermediate  $R$  values ( $0.7 < R < 1.4$ ) and not at the highest  $R$  values. Alternatively, tracer sedimentation was considered to be responsible for these deviations. In that case, the tracer concentration should increase toward the bottom of the cell, and as a consequence the transport mean free path  $l^*$  would be underestimated and accordingly  $G'$  and  $G''$  would be overestimated. This hypothesis can be rejected, because experimentally all  $l^*$  values are around a constant value of  $200 \pm 30$   $\mu\text{m}$  and such differences could not explain a shift factor of 4.5 in the plateau modulus. The compatibility of the tracers and the surrounding medium can be shown by measuring samples with and without tracers mechanically, and we find no measurable

(56) Chen, D. T.; Weeks, E. R.; Crocker, J. C.; Islam, M. F.; Verma, R.; Gruber, J.; Levine, A. J.; Lubensky, T. C.; Yodh, A. G. *Phys. Rev. Lett.* **2003**, *90*, 108301.

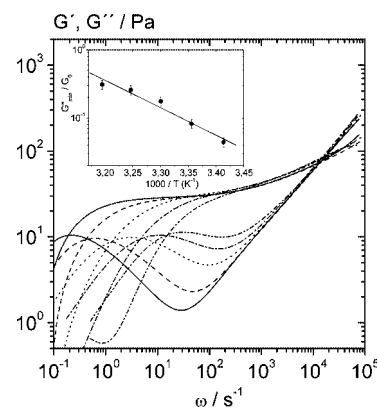


**Figure 3.** Plateau modulus  $G_0$  (circles) as a function of  $R$  obtained from oscillatory squeeze flow measurements at  $T = 20^\circ\text{C}$ . The dashed line represents the variation of the zero-shear viscosity  $\eta_0$  in an arbitrary unit.

458 differences within experimental errors. Nevertheless, this not to  
 459 exclude that a small fraction of surfactant may adsorb at the  
 460 surface of the tracer particles and therefore modify their mobility.  
 461 Such an adsorption may have no effect on mechanical measurements  
 462 but on DWS results. Aggregation of tracer particles or a  
 463 local structure formation hindering tracer motion may be other  
 464 possible scenarios which would reduce the plateau value of the  
 465 mean square displacement and thus result in an apparent increase  
 466 of  $G_0$ . We have no indication for heterogeneity of the solutions  
 467 investigated here, since they are all transparent and monophasic  
 468 at  $T = 20^\circ\text{C}$ . Aggregation seems to be an issue; we have observed  
 469 significant particle aggregation in aqueous suspensions by visual  
 470 inspection in an optical microscope at least for large tracer particles  
 471 ( $2.3\ \mu\text{m}$  diameter), and typically these aggregates consisted of  
 472 2–3 particles. Finally, we have performed DWS measurements  
 473 on the system for  $R = 0.9$ , for which  $G_0$  deviates the most from  
 474 mechanical data, using tracers with a larger diameter of  $1.3\ \mu\text{m}$ .  
 475 The shape of the curve is similar to that obtained with the  $0.72\ \mu\text{m}$   
 476 tracer diameter, but the plateau modulus has decreased from  
 477 211 to 100 Pa. This value is still 2 times higher than the mechanical  
 478 value (50 Pa), but it seems that the diameter of the tracer particle  
 479 may have some effect on the DWS measurements. Particle  
 480 aggregation as well as adsorption of surfactant on the tracer  
 481 surface is expected to depend on surfactant concentration, ionic  
 482 strength, as well as particle size and concentration. This  
 483 phenomenon is currently under investigation.

#### 4.2. Effect of Salt on Structural and Dynamic Properties.

484  
 485 **4.2.1. Plateau Modulus.** Almost all of the literature dealing with  
 486 the linear viscoelastic properties of wormlike micelles are based  
 487 on data from small amplitude oscillatory shear experiments  
 488 performed by conventional rotational rheometry and are thus  
 489 limited to the frequency range  $\omega < 100\ \text{rad/s}$ . In order to provide  
 490 the most accurate data at intermediate frequencies between 10  
 491 and  $10^4\ \text{rad/s}$ , we used oscillatory squeeze flow measurement to  
 492 determine the plateau modulus  $G_0$ , which is related to the cross-  
 493 link density or mesh size of the entanglement network. In Figure  
 494 3, we give the variation of the plateau modulus as a function of  
 495 the ionic strength for the system CPyCl/NaSal at a constant  
 496 surfactant concentration of 100 mM. The shear modulus varies  
 497 significantly with ionic strength. It increases by approximately  
 498 a factor of 2 from  $R = 0.5$  to 1.4, with the range corresponding  
 499 to the first zero-shear viscosity maximum, and then slightly  
 500 decreases up to  $R = 5$ . Cryo-TEM pictures taken for the same  
 501 salt/surfactant system, but at a surfactant concentration of 15  
 502 mM, clearly show a transition from linear to branched micelles  
 503 at the first maximum of zero-shear viscosity, with the branching

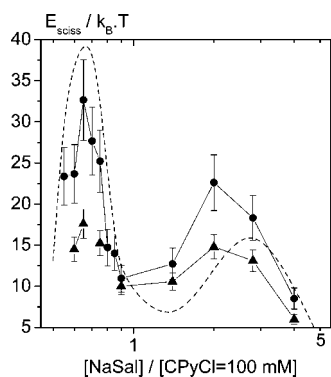


**Figure 4.** Dynamic shear moduli  $G'$  and  $G''$  of an aqueous solution of 100 mM CPyCl/60 mM NaSal as a function of temperature obtained from DWS measurements:  $20^\circ\text{C}$  (solid line),  $25^\circ\text{C}$  (dashed line),  $30^\circ\text{C}$  (dotted line),  $35^\circ\text{C}$  (dash-dotted line),  $40^\circ\text{C}$  (dash-dotted-dotted line). Inset: Ratio of the minimum value of  $G''$  and the plateau modulus  $G_0$  as a function of  $1/T$  for the same solution.

504 density increasing up to the minimum of  $\eta_0$ .<sup>4</sup> The increase in  $G_0$   
 505 can thus be attributed to the additional contribution of branching  
 506 points to the cross-link density. In a previous study performed  
 507 at a surfactant concentration of 60 mM,<sup>2</sup>  $G_0$  was found to be  
 508 independent of salt concentration. One possible explanation of  
 509 this contradictory observation is that, with 60 mM CPyCl, the  
 510 amplitude of the two zero-shear viscosity maxima is about a  
 511 factor of 10 lower compared to the system with 100 mM CPyCl.  
 512 Accordingly, the contribution of branching points to  $G_0$  is lower  
 513 and presumably within experimental uncertainty. The slight  
 514 decrease of  $G_0$  for  $R > 1.4$  can at least qualitatively be attributed  
 515 to a decrease of the branching density accompanied by an increase  
 516 of micelle length as shown by the cryo-TEM images taken for  
 517  $R$  values in the region of the second  $\eta_0$  increase. Furthermore,  
 518 TEM images for samples with  $R$  values corresponding to the  
 519 second  $\eta_0$  maximum show a shortening of the micelles and an  
 520 increase of the branching density, but also the formation of  
 521 micellar rings is observed. The formation of branching seems  
 522 not to compensate the formation of micellar rings, since  $G_0$  further  
 523 decreases.

524 **4.2.2. Scission Energy of Wormlike Micelles.**  $E_{\text{sciss}}$  is calculated  
 525 from the temperature dependence of the ratio  $G_{\text{min}}''/G_0$  according  
 526 to eq 4. The frequency range of oscillatory shear rheometry is  
 527 not always sufficient to determine this minimum correctly, but  
 528 mechanical squeeze flow gives reliable values for  $G_{\text{min}}''/G_0$   
 529 and thus allows for an accurate determination of the scission  
 530 energy. Figure 4 shows the relaxation spectra from DWS  
 531 measurements for the system with  $R = 0.6$  at four different  
 532 temperatures between 20 and  $40^\circ\text{C}$ . The terminal zone and the  
 533 Maxwell relaxation frequency  $\omega_r$  are strongly shifted at higher  
 534 frequencies, and the absolute value of  $G''$  around its minimum  
 535 at intermediate frequencies strongly increases as temperature is  
 536 raised. This directly shows that the micellar contour length  $\bar{L}$   
 537 decreases as temperature goes up. The plateau modulus,  $G_0$ , is  
 538 almost independent of temperature, which means that the mesh  
 539 size  $\xi$  of the entanglement network is essentially independent of  
 540 temperature, irrespective of the drastic change in  $\bar{L}$ . The insert  
 541 of Figure 4 represents the variation of  $G_{\text{min}}''/G_0$  with  $1/T$ .  $E_{\text{sciss}}$   
 542 can be extracted from the slope of this semilogarithmic plot of  
 543  $G_{\text{min}}''/G_0$  versus  $1/T$ . The variation of  $E_{\text{sciss}}$  as a function of  
 544 salt concentration is shown in Figure 5, where values extracted  
 545 from DWS and oscillatory squeeze flow are compared. For both

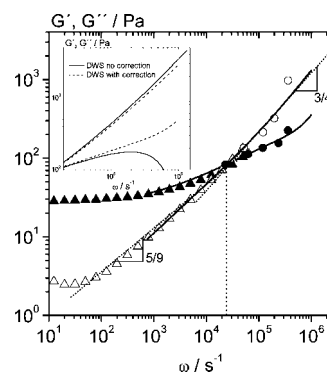




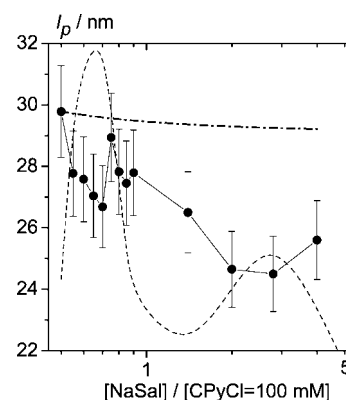
**Figure 5.** Dependence of scission energy  $E_{\text{sciss}}$  as a function of  $R$  obtained from DWS (circles) and oscillatory squeeze flow (triangles) measurements. The dashed line represents the variation of the zero-shear viscosity  $\eta_0$  in an arbitrary unit.

546 techniques,  $E_{\text{sciss}}$  exhibits two maxima analogous to the variation  
 547 of the zero-shear viscosity. The first increase in  $E_{\text{sciss}}$  directly  
 548 reveals the increase of the average length of the linear micelles,  
 549 which is due to the increasing screening of the electrostatic  
 550 repulsions between the charged head groups. This results in a  
 551 reduction of the optimal molecular area at the hydrocarbon–water  
 552 interface, leading to an increase in the end-cap energy and  
 553 accordingly to an increase in average micellar length. The decrease  
 554 of  $E_{\text{sciss}}$  after the first maximum is related to the formation of  
 555 branching points.<sup>4</sup> In that case, the scission energy is related to  
 556 the average contour length between branching points  $\bar{L}_c$ , and an  
 557 increase in the number of branching points will lead to a decrease  
 558 in  $\bar{L}_c$ , which corresponds to a decrease of the scission energy.  
 559 The second increase is again attributed to an increase of the  
 560 micellar length  $\bar{L}$ , and this is in agreement with the cryo-TEM  
 561 images showing a decrease of the branching density accompanied  
 562 by an increase of micellar length. And finally, the decrease of  
 563  $E_{\text{sciss}}$  after the second maximum can be rationalized in terms of  
 564 a shortening of the micelles and an increase of the branching  
 565 density as again confirmed by cryo-TEM images. In conclusion,  
 566 the variation of  $E_{\text{sciss}}$  directly shows changes in micellar structure  
 567 induced by the variation of ionic strength, and the results are  
 568 qualitatively in line with the cryo-TEM study on the same salt/  
 569 surfactant system performed at lower surfactant concentration.<sup>4</sup>  
 570 Finally, it should be noted that the DWS absolute values of  $E_{\text{sciss}}$   
 571 are about a factor 2 higher compared to the mechanical data. The  
 572 reason for this shift is due to deviations in the  $G_{\text{min}}''$  DWS data,  
 573 especially at temperatures of 20 and 25 °C where  $G'' \ll G'$ .  
 574 Contrary to mechanical measurements, the in- and out-of-phase  
 575 contributions are not measured independently in a DWS  
 576 experiment but have to be extracted from a single value of the  
 577 slope  $\delta \ln(\Delta^2(t))/\delta t$ . As a consequence, if  $G'(\omega)$  and  $G''(\omega)$   
 578 are of different magnitude, the lower value extracted from DWS  
 579 measurements is often not very well defined and here results in  
 580  $G_{\text{min}}''$  values much lower than that from mechanical measure-  
 581 ments. Consequently, the mechanical measurements are more  
 582 appropriate for a determination of absolute values of  $E_{\text{sciss}}$ .

583 **4.2.3. Persistence Length of Wormlike Micelles.** The persistence  
 584 length  $l_p$  has been determined from the absolute value of  
 585  $G^*$  in the  $\omega^{3/4}$ -scaling regime according to eq 7. In order to  
 586 obtain more reliable data in the ultrahigh frequency regime (up  
 587 to  $10^6$  rad/s), we applied a simple (self-consistent) correction  
 588 scheme to account for inertial effects when the motion of the  
 589 tracer particles changes from Brownian to ballistic. The inset of  
 590 Figure 6 shows the variations of  $G'$  and  $G''$  as a function of  
 591 frequency with and without inertial correction. In particular,  $G'$   
 592 is strongly modified by this correction and the unphysical



**Figure 6.** Dynamic shear moduli  $G'$  and  $G''$  of an aqueous solution of 100 mM CPyCl/60 mM NaSal at  $T = 20$  °C obtained from DWS (solid lines) and various mechanical rheometers ( $G'$ , solid symbols;  $G''$ , open symbols): oscillatory squeeze flow (triangles) and torsional resonators from ref 1 (circles). Inset:  $G'$ ,  $G''$  after inertial correction (dotted lines) of the DWS raw data (solid lines).



**Figure 7.** Dependence of persistence length  $l_p$  from DWS measurements (circles, 5% error bars) and from OSF theory normalized to the DWS  $l_p$  value at  $R = 0.5$  (dash-dotted line) as a function of  $R$ . The dashed line represents the variation of the zero-shear viscosity  $\eta_0$  in an arbitrary unit.

593 downward curvature at frequencies  $> 10^5$  rad/s is removed and  
 594  $G'$  follows the  $\omega^{3/4}$ -scaling analogous to  $G''$ . The inertia correction  
 595 also modifies  $G''$ , and we have used this data set to calculate  $l_p$ ,  
 596 since the  $\omega^{3/4}$ -scaling is more evident and extends over a broader  
 597 frequency range in  $G''$  than in  $G'$ . We fit the function  $G'' =$   
 598  $k_{\text{DWS}}\omega^{3/4}$  to the experimental data and calculate  $l_p$  from the  
 599 resulting  $k_{\text{DWS}}$  value according to eq 7. This equation requires a  
 600 lateral drag coefficient  $\delta = 4\pi\eta_s/\ln(0.6\lambda/d_{\text{mic}})$ . The characteristic  
 601 length  $\lambda$  is set equal to the mesh size,  $\eta_s$  is the solvent viscosity,  
 602 and for the micelle diameter we insert  $d_{\text{mic}} = 2.6$  nm.<sup>39</sup> This  
 603 results in  $\delta = 0.005$  N s/m<sup>2</sup>. Figure 7 shows the variation of  $l_p$   
 604 as a function of salt concentration from DWS measurements.  
 605 We observe a decrease of  $l_p$  from  $\sim 30$  to  $\sim 26$  nm over the total  
 606 range of salt concentration investigated. Obviously, the linear-  
 607 to-branched transition does not have a significant effect on  $l_p$ ,  
 608 and this increase in flexibility is considered to be an ionic strength  
 609 effect due to the screening of electrostatic repulsion. In order to  
 610 verify this assumption, we compared our results with the  
 611 predictions of the OSF theory. According to this theory, for  
 612 charged systems such as ordinary polyelectrolytes or wormlike  
 613 micelles of ionic surfactants, the persistence length  $l_p$  can be  
 614 expressed as a sum of an intrinsic component  $l_{p,0}$  and an  
 615 electrostatic component  $l_{p,e}$ .<sup>58,59</sup>

(58) Odijk, T. *J. Polym. Sci., Polym. Phys. Ed.* **1977**, *15*(3), 477–483.

(59) Skolnick, J.; Fixman, M. *Macromolecules* **1977**, *10*(5), 6717–6727.

$$l_p = l_{p,0} + l_{p,e} \quad (13a)$$

and the electrostatic contribution  $l_{p,e}$  is given by

$$l_{p,e} = \frac{1}{4\kappa^2 l_B} \quad (13b)$$

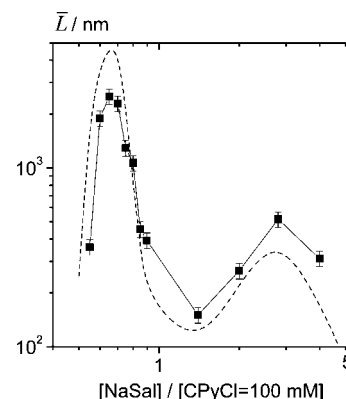
with the Bjerrum length  $l_B = 0.71$  nm and the Debye length  $\kappa^{-1}$  (nm) =  $0.304/(C_{\text{salt}})^{1/2}$ .

This electrostatic contribution has been investigated in various surfactant/salt systems,<sup>29,60–62</sup> but in the majority of cases no systematic investigations have been performed comparing experimental results for  $l_p$  and predictions of OSF theory. Schurtenberger et al.<sup>59</sup> made such a comparison for the system composed of nonionic hexaethylene glycol mono-*n*-hexadecyl ether ( $C_{16}E_6$ ) “doped” with a small amount of ionic surfactant 1-hexadecane sulfonic acid ( $C_{16}SO_3Na$ ) in the presence of nonpenetrating counterion (NaCl). They found that  $l_{p,e}$  absolute values were significantly higher than those predicted by the OSF theory, but they were not able to explain this systematic deviation. For the system investigated here, the variation of the persistence length  $l_p^{\text{OSF}}$  calculated from eq 13b is given in Figure 7. This electrostatic contribution is very small;  $l_p^{\text{OSF}}$  decreases by less than 1 nm in all the salt ranges investigated. Despite the experimental uncertainty of the  $l_p^{\text{DWS}}$  values, their decrease is significantly stronger than that predicted by OSF theory. Similar observations were obtained by Galvan-Miyoshi et al.<sup>15</sup> for the system CTAB/NaSal. Schubert et al.<sup>11</sup> also found a strong decrease of the persistence length with increasing salt for a mixed cationic/anionic micellar solution composed of cetyl trimethylammonium tosylate (CTAT) and sodium dodecyl benzyl sulfonate (SDBS) with added Na tosylate penetrating salt. The dependence on ionic strength follows the  $\kappa^{-2}$ -scaling predicted by OSF theory, but again the absolute values are much larger than expected by OSF theory. We assume that the increase in flexibility is due to the incorporation of more and more penetrating salicylate ions as  $R$  increases. Indeed, the penetration into the interior of the micelle by the salicylate ions can reverse the charge of the micelle from positive to negative, involving changes of dynamical properties, and can be responsible for the stronger increase in flexibility compared to the electrostatic contribution. In order to further elucidate this phenomenon, a similar study using a system with nonpenetrating counterions is in progress.

Finally, using our  $l_p^{\text{DWS}}$  experimental values, we calculated the contour length  $L$  of the micelles from the equations ( $G_{\text{min}}''/G_0$ )  $\approx (le/\bar{L})$  with  $le \approx \xi^{5/3} l_p^{2/3}$  and  $\xi = (k_B T/G_0)^{1/3}$ . Figure 8 shows the dependence of  $\bar{L}$  as a function of  $R$ .  $\bar{L}$  exhibits two maxima analogous to the scission energy, and this result confirms the findings on  $E_{\text{sciss}}$  in section 4.2.2 and demonstrates the consistency of our data analysis.

## 5. Conclusion

The system CPyCl/NaSal is known to exhibit two maxima in zero-shear viscosity as the salt concentration is varied.<sup>2</sup> The



**Figure 8.** Dependence of the contour length  $\bar{L}$  as a function of  $R$  obtained from DWS (squares). The dashed line represents the variation of the zero-shear viscosity  $\eta_0$  in an arbitrary unit.

different viscosities are a result of structural changes as confirmed by cryo-TEM imaging.<sup>4</sup> At low salt concentration, the micelles are linear and their average contour length increases with increasing ionic strength. The first viscosity maximum corresponds to a transition from linear to branched micelles. The second viscosity increase corresponds to a decrease of the branching density accompanied by an increase of micelle length, and the second viscosity maximum to a shortening of the micelles with an increase of the branching density. With further increase of salt concentration, the formation of micellar rings is also observed. We have used various mechanical techniques as well as DWS optical microrheology to characterize the linear viscoelastic properties of this surfactant/salt system in a broad frequency range from 0.01 up to  $10^6$  s<sup>-1</sup>. At a fixed surfactant concentration of 100 mM, we varied the salt/surfactant ratio  $R$  from 0.5 to 4. From these dynamic measurements, we can directly determine important structural features such as the cross-link density of the entanglement network, the scission energy, and the persistence length  $l_p$ . The persistence length  $l_p$  decreases monotonically with increasing salt concentration. This decrease is stronger than that predicted by the OSF theory which takes into account electrostatic screening effects. We attribute this to an additional increase in micellar flexibility due to the strongly binding salicylate counterion, which is known to penetrate into the micelles. This will be further investigated by a comparative study using a nonpenetrating counterion. The transition from linear to branched micelles obviously has no significant influence on  $l_p$ . The plateau modulus  $G_0$  increases at the linear-to-branched micelles transition, and this is attributed to the additional contribution of branching points to the cross-link density. The scission energy  $E_{\text{sciss}}$  exhibits two maxima analogous the zero-shear viscosity, which can be understood in terms of the variation of micellar length and variation of the amount of branched micelles and contour length between branching points.

**Acknowledgment.** The authors thank D. Danino (Department of Biotechnology and Food Engineering, Technion, Haifa, Israel) for providing unpublished results of her cryo-TEM experiments and for fruitful discussions.

(60) Sommer, C.; Pedersen, J. S.; Egelhaaf, S. U.; Cannavacciuolo, L.; Kohlbrecher, J.; Schurtenberger, P. *Langmuir* **2002**, *18*, 2495–2505.

(61) Cannavacciuolo, J.; Pederson, S.; Schurtenberger, P. *Langmuir* **2002**, *18*, 2922–2932.

(62) Magid, L. J.; Han, Z.; Li, Z.; Butler, P. D. *J. Phys. Chem. B* **2000**, *104*(29), 6717–6727.