The MIPAS HOCl climatology

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Abstract. Monthly zonal mean HOCl measurements by the Michelson Interferometer for Passive Atmospheric Sounding (MIPAS) are presented for the period from June 2002 to March 2004. Highest molar mixing ratios are found at pressure levels between 6 and 2 hPa, whereby largest mixing ratios occasionally exceed 200 ppt. The mixing ratio maximum is generally higher at lower altitudes in the summer hemisphere than in the winter hemisphere except for chlorine activation conditions in polar vortices, where enhanced HOCl abundances are also found in the lower stratosphere below about 10 hPa. During nighttime the maximum is found at higher altitudes than during daytime. Particularly low values (below 80 ppt) during daytime are found in subpolar regions in the winter hemisphere where HOCl photolysis is still strong but where HOCl precursors are less abundant than at other latitudes. The Antarctic polar winter HOCl distribution in 2002, the year of the split of the southern polar vortex, resembles northern polar winters rather than other southern polar winters. Increased HOCl amounts in response to the so-called Halloween solar proton event in autumn 2003 affect the representativeness of data recorded during this particular episode. Calculations with the EMAC model reproduce the measured HOCl distribution reasonably well. MIPAS measurements confirm that the reaction rate constants for HO2 + ClO → HOCl + O2 from the most recent JPL recommendation allow much more realistic modelling of HOCl than reaction rate constants from earlier recommendations. Modeled HOCl mixing ratios, however, are still too low except in the polar winter stratosphere where the model overestimates the HOCl abundance.

1 Introduction

HOCl is a short-lived reservoir of ClO x and HO x and thus links stratospheric chlorine and odd hydrogen chemistry. The HOCl catalytic cycle is an important mechanism for mid-latitude stratospheric ozone loss (Daniel et al., 1999; Millard et al., 2003). In the polar vortices HOCl has heterogeneous sources and sinks and thus can contribute to the polar chlorine chemistry (Hanson and Ravishankara, 1992; Abbatt and Molina, 1992; Crutzen et al., 1992; Prather, 1992; von Clarmann et al., 2009a). It also serves as indicator for perturbed HO x chemistry (von Clarmann et al., 2005). Occasional HOCl measurements exist from balloon--, space-, and airborne infrared solar absorption experiments (Larsen et al., 1985; Toon et al., 1992; Raper et al., 1987), balloon-borne far infrared limb emission (Chance et al., 1989; Traub et al., 1990; Johnson et al., 1995), as well as balloon-borne infrared limb emission (von Clarmann et al., 1997) measurements. The MIPAS (Michelson Interferometer for Passive Atmospheric Sounding) onboard Envisat provided the first global HOCl data set (von Clarmann et al., 2006). Further global HOCl measurements have been provided by the Microwave Limb Sounder (MLS) (Cofield and Stek, 2006) and JEM/SMILES (Kasai et al., 2009; Kikuchi et al., 2010; Baron et al., 2011).

Large discrepancies between measured and modeled HOCl abundances were found by Kovalenko et al. (2007), suggesting that reaction rate coefficients for HOCl formation from ClO and HO2 as published by Stimpfle et al. (1979) might be more appropriate than the JPL-2006 recommendation valid at that time (Sander et al., 2006). This has been
confirmed by von Clarmann et al. (2009a) and is also stated in World Meteorological Organization (2011). Since then these rate constants have been revised in the most recent JPL recommendation (Sander et al., 2010).

In this paper we present the first climatology of global altitude-resolved HOCl measurements, covering a full annual cycle, based on MIPAS measurements and compare these data to model calculations based on different rate coefficients of HOCl formation, including those by Stimpfle et al. (1979), Sander et al. (2006), and the most recent JPL recommendation by Sander et al. (2010).

2 MIPAS HOCl data

MIPAS is a Fourier transform limb emission spectrometer operated to measure vertical profiles of temperature and mixing ratios of many trace species (Fischer et al., 2008). MIPAS is one of three atmospheric chemistry related instruments on the Envisat research satellite. Envisat has been launched in a sun-synchronous polar orbit of about 800 km altitude, 98.55° inclination, orbital period of 100.6 min, and equator crossing at approximately 10:00 LT (local time). In its original nominal measurement mode MIPAS recorded one set of 17 limb measurements at tangent altitudes from 6 to 68 km per 76.5 s, i.e. per 510 km ground track at a spectral resolution of 0.05 cm$^{-1}$ per 510 km. After failure of the interferometer slide, regular operation was interrupted in 2004. Since 2005 MIPAS is operational again, however at reduced spectral but improved spatial resolution. While for many trace species the change of operation mode turned out to be advantageous in terms of precision, altitude-, and along-track horizontal resolution (Chauhan et al., 2009; von Clarmann et al., 2009b), HOCl could not yet successfully be retrieved from these reduced resolution measurements, because its lines could not be well enough resolved among the much stronger lines of interfering species. Thus MIPAS HOCl retrievals are available only from June 2002 to March 2004.

HOCl is retrieved from MIPAS spectra using the IMK/IAA scientific MIPAS processor (von Clarmann et al., 2003) by constrained least-squares fitting of simulated to measured spectral radiances. Details of the retrieval settings are discussed in von Clarmann et al. (2006). A Tikhonov-type first order finite differences constraint, modified to allow an altitude-dependent choice of the strength of the regularization (Steck and von Clarmann, 2001) has been chosen in order to avoid biasing of retrievals towards the a priori information. The measurement error was found to be largely dominated by measurement noise. The precision of a single profile measurement is estimated at 30 to 80 ppt, i.e. about 25 % of the peak molar mixing ratio. The altitude resolution is about 9 km, due to the strong smoothing constraint needed to obtain stable retrievals at low signal/noise ratio. MIPAS averaging kernels are shown in Fig. 1. They are well-behaved in an altitude-range between about 20 and 45 km, in a sense that they are approximately symmetric around their nominal altitudes. In this altitude range the MIPAS HOCl profiles can be regarded as a smoothed version of the true HOCl profiles. At altitudes above 45 km and below 20 km the sensitivity of the MIPAS HOCl retrievals is largely reduced, and the asymmetric averaging kernels shift information from these altitudes into the altitude range where MIPAS is sensitive. In the presence of HOCl at these altitudes, application of the MIPAS averaging kernels is thus particularly important to make high-resolution model results comparable to MIPAS measurements (cf., e.g. Jackman et al., 2008). Since the MIPAS a priori profiles are zero throughout, this transformation reduces to

$$x_{\text{degraded}} = Ax_{\text{fine}},$$

where $x_{\text{fine}}$ is the high-resolution HOCl profile, $x_{\text{degraded}}$ is the degraded profile which should be used for the comparison, and $A$ is the MIPAS averaging kernel matrix. MIPAS averaging kernels have the quite same structure and characteristics for all seasons and latitude bands; small to moderate differences reflect the seasonal and latitudinal temperature variation. No substantial differences between daytime and nighttime averaging kernels are observed. This is because at relevant altitudes the atmosphere is rather transparent, leading to linear radiative transfer and thus independence of the Jacobians (and thus averaging kernels) from the actual mixing ratio of HOCl. Beyond random error and smoothing effects, the systematic error due to uncertainties of spectroscopic data contributes to the total error budget. It is estimated at 10 % (von Clarmann et al., 2006).

MIPAS zonal mean HOCl mixing ratios were found to agree within one standard deviation with trend-corrected balloon-borne far-infrared measurements reported by Chance et al. (1989, 1996) (von Clarmann et al., 2006). The most recent version of MIPAS HOCl data is V3O_HOCl.4. Improvements with respect to previous data versions are obtained by consideration of horizontal temperature gradients, stronger regularization of N$_2$O profiles which are jointly fitted, a finer monochromatic wavenumber grid used in the radiative transfer calculation, a larger number of pencil beams for radiance integration over the instantaneous field of view, and some updates of spectroscopic data of gases used in the radiative transfer calculations. V3O_HOCl.4 data agree well with earlier data versions and none of the improvements has led to any major changes in the results. These data are available via http://www.imk-asf.kit.edu/english/308.php to registered users.

3 Method

MIPAS HOCl climatologies have been prepared in compliance with the methodical and data format requirements of the SPARC (Stratospheric Processes and their Role in Climate) Data Initiative (Hegglin and Tegtmeier, 2011). The
climatology consists of zonal monthly mean fields of HOCl molar mixing ratios and their standard deviations and sample sizes. In order to account for the diurnal variability of HOCl, separate mean fields are provided for a.m. and p.m. measurements. The altitude grid is 300, 250, 200, 170, 150, 130, 115, 100, 90, 80, 70, 50, 30, 20, 15, 10, 7, 5, 3, 2, 1.5, 1.0, 0.7, 0.5, 0.3, 0.2, 0.15, 0.1 hPa, and the centers of the equidistant latitude bins are $-87.5^\circ$, $-82.5^\circ$, ..., $82.5^\circ$, $87.5^\circ$. Each profile was first interpolated to the pressure grid using MIPAS pressure and temperature profiles (von Clarmann et al., 2006) and then averaged. Since MIPAS measured one profile each 510 km ground track distance from a polar orbit, only one or two profiles per orbit segment fall within a latitude bin. Since the measurement sequence is re-initialized at a fixed latitude during each orbit, this leads to a systematic sampling bias, i.e. the MIPAS measurement does not generally represent the nominal central latitude of the latitude bin. In order to avoid related artefacts, it has been decided to linearly interpolate the MIPAS measurements to the nominal latitudes. Standard deviations and the number of measurements are provided along with the molar mixing ratios. The number of profile measurements per monthly zonal mean and time of the day (a.m. or p.m.) was typically between 400 and 800. Since the interpolation of these quantities to the nominal latitude grid is not a trivial task, particularly if both measurement errors and natural variability contribute to the variance, related operations are discussed in detail in Appendix A.

4 Model calculations

In order to assess how well HOCl chemistry is understood on a global scale, MIPAS climatologies are compared to model calculations of the Chemistry Climate Model (CCM) EMAC (ECHAM5/MESSy Atmospheric Chemistry model) (Jöckel et al., 2006). EMAC has been developed at the Max-Planck-Institute for Chemistry in Mainz and is a combination of the general circulation model ECHAM5 (Roeckner et al., 2006) and different submodels such as the chemistry submodel MECCA1 (Sander et al., 2005) combined through the Modular Earth Submodel System MESSy (Jöckel et al., 2005).

For this study data from a simulation from 1994 to 2011 with EMAC Version 1.10 are used. The simulation was performed with horizontal resolution $T42$ ($2.8^\circ \times 2.8^\circ$) and with 39 layers, covering the atmosphere from the surface up to 0.01 hPa ($\approx 80$ km). A Newtonian relaxation technique of the prognostic variables surface pressure and temperature, vorticity and divergence above the boundary layer and below 10 hPa towards ECMWF operational analysis data has been applied, in order to nudge the model dynamics towards the observed meteorology. The boundary conditions for greenhouse gases are from the IPCC-A1B scenario (IPCC, 2001) adapted to observations from the AGAGE database (Prinn et al., 2001) and for halogenated hydrocarbons from the WMO-Ab scenario (World Meteorological Organization, 2007).

The simulation includes a comprehensive atmospheric chemistry setup for the troposphere, the stratosphere and the lower mesosphere. Reaction rate constants and photochemical data follow in general the JPL-2002 recommendations (Sander et al., 2003) except for $\text{HO}_2 + \text{ClO} \rightarrow \text{HOCl} + \text{O}_2$ for which JPL-2009 (Sander et al., 2010) is used. Additional sensitivity calculations were performed where the rate constant for the latter reaction was changed according to JPL-2006 (Sander et al., 2006) or Stimpfle et al. (1979) (this particular rate constant did not change from JPL-2002 to JPL-2006). The applied submodels are the same as in the simulations in Kirner (2008). In particular we used a new parameterisation of polar stratospheric clouds based on the efficient growth and sedimentation of NAT-particles in the submodel PSC (Kirner et al., 2011).

Monthly mean modeled HOCl fields, sampled at the respective local time (10:00 a.m./10:00 p.m.) are smoothed by the MIPAS averaging kernels and presented for comparison.

5 Twenty-two months of HOCl observations

5.1 Climatology

MIPAS HOCl observations are available from June 2002 to March 2004. The typical features are: The pressure level of maximum mixing ratio varies between 6 and 2 hPa.
Largest mixing ratios occasionally exceed 200 ppt. The altitude of largest mixing ratios is generally lower in the summer hemisphere than in the winter hemisphere (Fig. 2), except sometimes for polar vortices. This feature is in tendency also reproduced by the model calculations. The HOCl equilibrium concentration depends on its photolysis rate, temperature, and, among others, on the concentrations of HO2, ClO, and OH, which have altitude-dependent diurnal and annual cycles in themselves (Brasseur and Solomon, 2005), leading, as a net effect, to the observed behaviour. Further, mixing ratios are in general higher in the summer hemisphere than in the winter hemisphere, and maximal mixing ratios are found in the lower midlatitudes of the summer hemisphere. These maxima coincide with those of ClO, which is also measured by MIPAS (Glatthor et al., 2004). This suggests that the latitudinal HOCl distribution is largely driven by the availability of ClO. Both the altitude of the maximum as well as its latitude are well reproduced by the model. Also the modeled and measured mixing ratios agree reasonably well at most latitudes and altitudes, if the rate constant for HO2 + ClO \rightarrow HOCl + O2 from the JPL-2009 recommendation (Sander et al., 2010) is used. The use of the rate constant from the JPL-2006 recommendation (Sander et al., 2006) leads to HOCl mixing ratios underestimated by about 40 %, while rate constants suggested by Stimpfle et al. (1979) produce too high HOCl mixing ratios (second and third panel in Fig. 3). Some residuals, particularly in the Northern hemisphere, still persist: even with rate constants from the most recent recommendation (JPL-2009) HOCl amounts are underestimated particularly in the midlatitude summer maximum and overestimated in the polar winter upper stratosphere.

When EMAC is run in its default mode, stratospheric HOCl concentrations are largely overestimated during polar night conditions (bottom panel in Fig. 3). This is because EMAC uses by default a family approach for HOCl and other comparatively short-lived chlorine species for transport modelling, probably because in this mode the model better satisfies the conservation of mass; this means that after the integration of chemical changes, which is calculated explicitly for each species, transport is calculated for the related family. Afterwards, the partitioning is re-adjusted according to the partitioning before the transport time step. This leads to artefacts particularly if air is transported from the illuminated part of the vortex into the dark part. Re-partitioning as described above then represents an airmas which has always been in the dark while it actually had been illuminated before. To obtain realistic results, it is important to simulate HOCl explicitly rather than as a member of a family. The model calculations presented in this paper are based on explicit modeling of both the chemistry and the transport of HOCl.

During nighttime the maximum of the HCl mixing ratio is found at higher altitudes than during daytime (Fig. 4). The approximate altitude (ca. 39 km or 3 hPa during nighttime)
Modeled mean HOCl distributions in December 2002 for different model setups: top three panels: explicit HOCl modeling and rate constants from JPL-2009, JPL-2006, and Stimpfle et al. (1979) (top to bottom); lowermost panel: EMAC in its default mode (1977). White areas in the model fields represent negative data caused by side wiggles of MIPAS averaging kernels.

Timeseries of HOCl zonal mean molar mixing ratios for every month and latitude bin is about 30 to 70 ppt. Under polar conditions this HOCl maximum is in general well reproduced by the model in a qualitative sense but modeled mixing ratios are somewhat too high.

In Figure 6 the HOCl distribution of December 2003 is shown for both a.m. and p.m. measurements. The polar winter HOCl distribution is in general displaced or inhomogeneously composed polar vortices or rapid composition changes within the averaging period. The oscillation of the peak mixing ratios with an amplitude of 2–3 ppt per month is also observed in Southern winter (Fig. 2, second panel). The secondary minimum is more pronounced in the modeled distributions than in the measurements; it is, however, visible in the observed HOCl climatology and thus on availability of sunlight, this HOCl maximum is well known that chlorine activation through heterogeneous chemistry is much more frequent and efficient in southern midlatitudes. During nighttime this minimum disappears, is also observed in the lower stratosphere over the North Pole and ClO, which suggests that this effect is driven by their own altitude-dependent diurnal cycle. Again, this behaviour is the net effect of several interacting processes depending on the concentrations of HOCl and ClO and on photolysis rates, which all have their own altitude-dependent diurnal cycle.

Fig. 3. Modeled mean HOCl distributions in December 2002 for different model setups: top three panels: explicit HOCl modeling and rate constants from JPL-2009, JPL-2006, and Stimpfle et al. (1979) (top to bottom); lowermost panel: EMAC in its default mode with family approach for HOCl and HOCl formation rate constant from JPL-2006. White areas in the model fields represent negative data caused by side wiggles of MIPAS averaging kernels.

Fig. 4. MIPAS zonal mean HOCl distribution in April 2003 at 10:00 p.m. (top panel) and 10:00 a.m. (second panel), and respective model calculations (third and fourth panel).
and the altitude difference between the nighttime and the daytime maximum of about 5 km are consistent with the profiles and their diurnal variation found by Chance et al. (1989, 1996) who measured HOCl in the far infrared spectral region from a balloon-borne platform. This shift in altitude of the maximum seems to be more pronounced at lower latitudes than at higher latitudes, leading to quite a flat distribution of the peak altitude over latitude during nighttime contrasting to a slightly more banana-shaped distribution during daytime. Again, this behaviour is the net effect of several interacting processes depending on the concentrations of HO₂ and ClO and on photolysis rates, which all have their own altitude-dependent diurnal cycle. No such diurnal variation of the altitude of maximal mixing ratios is observed in ClO, which suggests that this effect is driven by the equilibrium of HO₂-dependent production and loss through photolysis. Both the altitude of the HOCl maximum and the amount are slightly underestimated by EMAC, but the general tendency of nighttime enhancement in higher and daytime enhancement in lower altitudes is reproduced.

The representation of the data as a timeseries (Fig. 5) for tropical latitudes (equatorward of ±25°) shows a semiannual oscillation of the peak mixing ratios with an amplitude of about 30 ppt. Largest abundances are found in July/August and in January/February, i.e. during northern and southern summer when local noon solar elevation is lowest at equatorial latitudes. At equinox the peak mixing ratios start to decrease to reach their minimum at solstice.

In Fig. 6 the HOCl distribution of December 2003 is shown for both a.m. and p.m. measurements. The December 2003 monthly mean is dominated by measurements when the Northern polar vortex was still intact throughout all stratospheric altitudes, although a major warming happened in early January 2004, starting with a break-up of the vortex in the upper stratosphere in late December (Manney et al., 2005). Particular low HOCl mixing ratios (occasionally below 80 ppt at the maximum) are found during daytime in early winter higher midlatitudes. During nighttime this minimum disappears, suggesting that photochemical loss during daytime is no longer compensated by insolation-dependent production. This daytime minimum is surrounded by regions of more abundant HOCl. HOCl shows a maximum at lower mid-latitudes of the summer hemisphere and decreases towards high latitudes of both hemispheres, reflecting the decrease of the HOCl sources ClO and HO₂. At polar night, HOCl is enhanced due to the absence of HOCl loss. This leads to an HOCl minimum just outside of the polar night. The subpolar HOCl daytime minimum is also observed in Southern winter (Fig. 2, second panel).

The polar winter HOCl maximum is not exactly centered at the pole but slightly offset, forming a weakly pronounced minimum in the very inner part of the vortex over the pole where due to darkness no HO₃ chemistry is happening. This secondary minimum is more pronounced in the modeled distributions than in the measurements; it is, however, visible in the southern polar vortex June 2003 measurements (Fig. 2, second panel). The polar winter HOCl distribution is in general well reproduced by the model in a qualitative sense but modeled mixing ratios are somewhat too high.

A separated HOCl maximum is seen in the lower polar winter stratosphere around 50–10 hPa. This feature has first been observed by von Clarmann et al. (2009a) in the Antarctic winter of 2002 but is now seen in all polar winters for which MIPAS HOCl measurements are available (Figs. 7 and 8). This feature is in tendency reproduced by the model but to a much lesser extent (Fig. 7). This maximum has been attributed to heterogeneous chemistry, presumably to heterogeneous ClO formation preceding gas-phase HOCl formation. The fact that this feature is more pronounced in southern polar winters is quite plausible and supports the hypothesis of being linked to heterogeneous chemistry, because it is well known that chlorine activation through heterogeneous chemistry is much more frequent and efficient in southern polar vortices. Austral winter chlorine activation from May until September 2002 onward has been reported by Feng et al. (2005). Very early chlorine activation was reported for the northern winter 2002/2003 by Tilmes et al. (2003), both in consensus with our HOCl observations. Since generation of HOCl via reaction of HO₂ with ClO depends on HO₃ chemistry and thus on availability of sunlight, this HOCl maximum is not centered at the pole.

Figure 8 shows the temporal development of polar HOCl mixing ratios. Both the upper (3 hPa) and lower (20 hPa) polar winter maxima are clearly seen, as well as the illumination-dependent varying altitude of the maximum from local spring to fall.

Standard deviations of the monthly zonal means are normally in the range of 50 to 80 ppt in the altitude of the mixing ratio maximum. Comparison to the estimated single
Fig. 6. Zonal mean morning (top panel) and evening (second panel) HOCl distribution in Arctic winters (December 2003). Note low values in sub-polar regions. The third and fourth panel represent the respective model data sets.

Fig. 7. Increased HOCl amounts in the southern (July 2002, evening, upper panel) and northern (January 2003, morning, second panel) polar winter stratospheric vortex subsequent to chlorine activation, together with related model calculations (third and fourth panel). Note that in the polar night the time of the day is of no concern.
5.2 Particular events

During the observation period there were two very special events, which are scientifically interesting but require a caveat with respect to the climatological representativeness of the MIPAS data set. These are the split of the Antarctic polar vortex in the Austral winter of 2002, and the solar proton event around Halloween in 2003.

5.2.1 The split vortex event in 2002

The split vortex event in 2002 was characterized by a major warming (Allen et al., 2003; Sinnhuber et al., 2003; Krüger et al., 2005; Charlton et al., 2005) going along with pronounced wave activity involving planetary waves of wavenumber 1 to 3 (Wang et al., 2005; Newman and Nash, 2005) which led to a displacement, distortion, and finally a split of the polar vortex. While the lower stratospheric maximum of HOCl has been attributed to heterogeneous chemistry, large HOCl amounts near 4 hPa have been attributed to exposure of Cl$_2$-rich polar vortex air to sunlight due to vortex displacement, triggering HO$_x$ chemistry (von Clarmann et al., 2009a). Indeed, such large HOCl amounts were not observed in the Antarctic winter of 2003 (Fig. 9). The southern polar winter 2002 HOCl distributions resemble rather those of the northern winters within the observation period, where high HOCl concentrations at around 2 hPa seem to be the rule rather than the exception (c.f. Fig. 2 for comparison). This behaviour is not unexpected since due to larger northern hemispheric wave activity the polar vortex there is often displaced, distorted, and thus exposed to sunlight.

5.2.2 The Halloween solar storm in 2003

The Halloween solar proton event (SPE) in 2003 was one of the largest in the past fourty years (Degenstein et al., 2005) and resulted in ozone depletion subsequent to HO$_x$, NO$_x$ and chlorine chemistry perturbations (Jackman et al., 2005; López-Puertas et al., 2005a,b; Jackman et al., 2008; Verronen et al., 2008). Observations of HOCl enhancements in response to the solar proton event gave evidence of perturbed chlorine chemistry as well as the first experimental evidence of perturbed HO$_x$ chemistry (von Clarmann et al., 2005). These HO$_x$ perturbations were later confirmed by direct hydroxyl observations (Verronen et al., 2006). Within the context of this climatological analysis it is important to note that HOCl measurements in October and November 2003 might not be representative for this season, although the observed HOCl enhancements were very localized and lasted only a few days and thus are not resolved in the monthly zonal means.

6 Conclusions

The first global measurements covering nearly two annual cycles of stratospheric HOCl are presented. The most important features are (a) a mixing ratio maximum in summer midlatitudes at about 5 hPa; (b) an increase of the altitude of maximum mixing ratios during nighttime; (c) a minimum in winter high midlatitudes; (d) occasional enhancements in polar vortices, both in the altitude regimes of gas-phase and of heterogeneous chemistry. The observed features are generally well reproduced by the model calculations, which have been considerably improved by the most
recent update of the recommendation of chemical kinetics data by Sander et al. (2010). Some differences, however, remain: Modeled HOCl mixing ratios are still too low except in the polar winter stratosphere, where HOCl amounts are overestimated by the model. Large discrepancies between measurements and EMAC operated in its default mode in the mid-stratosphere during polar night could be traced back to the family approach used for HOCl transport.

The question to which extent this dataset is representative in a climatological sense or if it is dominated by particular atmospheric situations of the measurement period will be answered by a multi-instrument climatology involving also MLS and JEM/SMILES HOCl measurements.

Appendix A

Interpolation of standard deviation and number of measurements

Let \( x_1 \ldots x_m \) be the measurements in latitude bin 1, and \( y_1 \ldots y_n \) the measurements in latitude bin 2. Zonal means \( \bar{x} \) and \( \bar{y} \) in each of these bins are

\[
\bar{x} = \frac{\sum_{i=1}^{m} x_i}{m}, \\
\bar{y} = \frac{\sum_{j=1}^{n} y_j}{n}.
\]

(A1)

Weighting by the inverse estimated error variances of the single measurements is intentionally not performed as to avoid biases due to atmospheric state dependent precision. For example, the MIPAS retrieval error is generally larger in a colder atmosphere, thus measurements in warmer parts of the atmosphere would be overrepresented. The standard deviation of the samples are

\[
\sigma_x = \sqrt{\frac{\sum_{i=1}^{m} (x_i - \bar{x})^2}{m-1}}.
\]

(A2)

\[
\sigma_y = \sqrt{\frac{\sum_{j=1}^{n} (y_j - \bar{y})^2}{n-1}}.
\]

The interpolation to the desired latitude is

\[
\tilde{z} = (v, w) \left( \begin{array}{c} \bar{x} \\ \bar{y} \end{array} \right) = v \bar{x} + w \bar{y}
\]

(A3)

where \( v \) and \( w \) are weighting factors depending on the distances between the initial mean measurement geolocations \( l_x \) and \( l_y \) and the geolocation of the interpolated measurement \( l_z \):

\[
v = \frac{l_z - l_y}{l_x - l_y} = 1 - \frac{l_x - l_z}{l_x - l_y}, \\
w = 1 - v
\]

(A4)

The standard deviation \( \sigma_z \) of the interpolated mixing ratio is, according to generalized Gaussian error estimation

\[
\sigma_z = \sqrt{(v, w) \begin{pmatrix} \sigma_x^2 & r \sigma_x \sigma_y \\ r \sigma_x \sigma_y & \sigma_y^2 \end{pmatrix} (v \ w)}
\]

\[
= \sqrt{v^2 \sigma_x^2 + 2 v w r \sigma_x \sigma_y + w^2 \sigma_y^2}.
\]

(A5)

For fully correlated \( x \) and \( y \) this reduces to simple linear interpolation of the standard deviation while for fully independent \( x \) and \( y \) this reduces to quadratic interpolation of variances. It is important to note, that interpolation of covariance
matrices from a coarser to a finer grid does not represent fine-scale variability which does not show up in the coarse grid. This caveat, however, does not apply to the application of this paper, because the target latitude grid is coarser than the initial one on which the MIPAS measurements were performed.

The virtual number of measurements

The data format of the SPARC Data Initiative also requires the number of measurements $k$ used to calculate the zonal mean. Also this quantity is not trivial to interpolate. We argue that the purpose of this quantity is that the user can calculate the standard error of the mean, $\sigma_{\text{stderr}}$. The usual recipe for this purpose assumes independent data and is

$$\sigma_{\text{ stderr}} = \frac{\sigma}{\sqrt{k}} \quad \text{(A6)}$$

We argue that the most useful estimate of the number of observations is that where Eq. (A6) holds, regardless how the standard deviation $\sigma$ was obtained. We thus define a “virtual number of measurements” $k_v$ which is defined as

$$k_v = \frac{\sigma^2}{\sigma_{\text{ stderr}}^2} \quad \text{(A7)}$$

The direct estimate of the interpolated zonal mean $z$ from the single measurements $x_i$ and $y_j$ is (averaging and interpolation in one step)

$$z = \begin{pmatrix} \frac{v_1}{m} & \ldots & \frac{v_m}{m} & \frac{w_1}{n} & \ldots & \frac{w_n}{n} \end{pmatrix} \begin{pmatrix} x_1 \\ \vdots \\ x_m \\ y_1 \\ \vdots \\ y_n \end{pmatrix} = g^T \begin{pmatrix} x_1 \\ \vdots \\ x_m \\ y_1 \\ \vdots \\ y_n \end{pmatrix} \quad \text{(A8)}$$

The standard error of $z$ is calculated by generalized Gaussian error propagation. We assume $m \leq n$ to allow for additional measurements (in one bin without counterpart in the other bin). We further assume zero correlation between multiple measurements within one latitude bin; this approximation is justified because these measurements belong mostly to different orbits, and with MIPAS it takes about three days until the same geolocation is observed again. In contrast, correlations between subsequent measurements of the same orbit but different latitude bins are considered, because these measurements are only 70 s and 510 km apart.

$$\sigma_{\text{ stderr}}^2 = g^T \begin{pmatrix} \sigma_x^2 & 0 & r \sigma_x \sigma_y & 0 & 0 & 0 \\ 0 & \sigma_y^2 & 0 & r \sigma_x \sigma_y & 0 & 0 \\ r \sigma_x \sigma_y & 0 & \sigma_y^2 & 0 & 0 & 0 \\ 0 & 0 & 0 & \sigma_x^2 & 0 & 0 \\ 0 & 0 & 0 & 0 & \sigma_y^2 & 0 \\ 0 & 0 & 0 & 0 & 0 & \sigma_x^2 \end{pmatrix} g \quad \text{(A9)}$$

With $\sigma_z$ obtained from Eq. (A5) and $\sigma_{z,\text{ stderr}}^2$ obtained from Eq. (A9), the virtual number of measurements $k_v$ can be calculated using Eq. (A7). Although the result can be a fraction, in order not to confuse the user and to comply with the data format of the SPARC Data Initiative, we round the result to the nearest lower integer.

Estimation of the correlation coefficient

Ideally the correlation coefficient $r$ can be calculated in a straightforward manner along with the zonal means and their standard deviations. However, the given data structure may be obstructive for this purpose. We thus propose a scheme to estimate $r$ without going back to the single measurements. We assume that the total observed variability $\sigma_{\text{ observed}}$ (e.g. $\sigma_x$ or $\sigma_y$) is composed of measurement error $\sigma_{\text{ noise}}$ and natural variability $\sigma_{\text{ nat}}$ as

$$\sigma_{\text{ observed}}^2 = \sigma_{\text{ noise}}^2 + \sigma_{\text{ nat}}^2 \quad \text{(A10)}$$

Measurement errors are in good approximation uncorrelated between subsequent measurements ($r_{\text{ noise}} = 0$) while natural variations are supposed to be highly correlated ($r_{\text{ nat}} \approx 1$) between subsequent measurements. We infer $r$ by decomposing each value in a true component ($x_{\text{ true}}$ and $y_{\text{ true}}$, respectively) and a noise term ($\epsilon_i$ and $\gamma_i$, respectively):

$$r = \sum_{i=1}^{m} \frac{(x_i - \bar{x})(y_i - \bar{y})}{\left(\sum_{i=1}^{m} (x_i - \bar{x})^2\right)^{1/2} \left(\sum_{i=1}^{m} (y_i - \bar{y})^2\right)^{1/2}} \quad \text{(A11)}$$

$$= \sum_{i=1}^{m} \frac{(x_{\text{ true}} - \bar{x})(y_{\text{ true}} - \bar{y})}{\left(\sum_{i=1}^{m} (x_{\text{ true}} - \bar{x})^2\right)^{1/2} \left(\sum_{i=1}^{m} (y_{\text{ true}} - \bar{y})^2\right)^{1/2}} + \sum_{i=1}^{m} \frac{(x_{\text{ true}} - \bar{x}) \epsilon_i}{(m-1) \sigma_x \sigma_y} + \sum_{i=1}^{m} \frac{(y_{\text{ true}} - \bar{y}) \gamma_i}{(m-1) \sigma_x \sigma_y}$$

where the latter three terms are ignored because the noise terms are assumed to be uncorrelated and thus to have a tendency to cancel out. With

$$a = \frac{\sigma_{\text{ nat}}}{\sigma_x} \quad \text{(A12)}$$

and

$$b = \frac{\sigma_{\text{ nat}}}{\sigma_y} \quad \text{(A13)}$$

we can rewrite the surviving term of Eq. (A11) as

$$r = ab \frac{(x_{\text{ true}} - \bar{x})(y_{\text{ true}} - \bar{y})}{(m-1) \sigma_x \sigma_y} \quad \text{(A14)}$$

$$= ab \sqrt{\frac{\sigma_x^2 - \sigma_{x,\text{ noise}}^2}{\sigma_x \sigma_y}} \sqrt{\frac{\sigma_y^2 - \sigma_{y,\text{ noise}}^2}{\sigma_x \sigma_y}}$$
Since both the observed standard deviations $\sigma_x$ and $\sigma_y$ and error estimates $\sigma_{x,\text{noise}}$ and $\sigma_{y,\text{noise}}$ are available for MIPAS retrievals, we can estimate $r$ without retrieving information which pairs of measurements $x_i$ and $y_i$ belong together.

**Supplementary material related to this article is available online at:**
http://www.atmos-chem-phys.net/12/1965/2012/acp-12-1965-2012-supplement.zip.

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**References**


