Pointing errors in solar absorption spectrometry – correction scheme and its validation

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Abstract

A method for quantification of sun-pointing inaccuracies in solar absorption spectrometry is presented along with a correction scheme for the resulting errors in trace gas vertical column or profile retrievals. A posteriori correction of pointing errors requires knowledge of both coordinates of the mispointing vector on the solar disk. In principle, quantitative information on the mispointing can be retrieved from Doppler shifts of solar lines derived from measured spectra. However, this yields only one component of the mispointing vector, namely the one which is perpendicular to the solar rotation axis. Missing information on the second vector component has hindered a posteriori correction of mispointing errors so far. Our idea to overcome this problem is to obtain estimates of both coordinates of the mispointing by combining subsequent measurements with differing orientations of the solar rotation axis relative to the zenith direction. An implementation of this original concept is demonstrated using measurements from the solar absorption Fourier transform infrared (FTIR) spectrometer at the Zugspitze (47.42° N, 10.98° E, 2964 m a.s.l.). Soundings in the September 2012 to September 2014 time interval were impacted by mispointing problems due to a non-optimum solar tracking optics configuration. They show a mean mispointing in zenith direction of −0.063°. This causes biases in vertical soundings of trace gases, e.g. −2.82 ppb in monthly means of dry-air column-averaged mole fractions of methane (XCH₄). Measurements made with the more stable pre-September 2012 and post-September 2014 optics configurations show considerably smaller mispointing effects. Applying the mispointing correction, the April 2006–March 2014 XCH₄ trend determined from Zugspitze measurements is reduced from 6.45 [5.84, 7.04] to 6.07 [5.55, 6.59] ppb yr⁻¹. The correction thereby restores consistency with results from the nearby Garmisch FTIR site (47.48° N, 11.06° E, 743 m a.s.l.). The mispointing correction is applicable to solar absorption measurements in the mid infrared and near infrared. It will be of particular benefit for refining existing records of high-accuracy-and-precision
greenhouse gas soundings for the purpose of improved trend analysis or source-sink inversions.

1 Introduction

Solar Fourier Transform Infrared (FTIR) spectrometry is one of the key measurement techniques for highly accurate ground-based vertical soundings of atmospheric trace gases. Measurements of a large number of atmospheric species have been performed for about two decades within the Network for the Detection of Atmospheric Composition Change (NDACC, http://www.ndacc.org) using solar FTIR measurements in the mid-infrared (MIR) spectral range. Measured parameters involve total column amounts of atmospheric species such as ozone (e.g. Rinsland et al., 1996; Schneider and Hase, 2008), chlorine species (Liu et al., 1992; Rinsland et al., 2003; Kohlhepp et al., 2012; Mahieu et al., 2014), fluorine species (Zander et al., 1987), or climate gases like $\text{N}_2\text{O}$ (Zander et al., 1994; Sussmann and Schäfer, 1997), water vapor (e.g. Sussmann et al., 2009; Palm et al., 2010), or methane (e.g. Sussmann et al., 2011, 2012; 2013; Sepulveda et al., 2012; Ostler et al., 2014, 2015). Additionally, low-resolution vertical profile retrievals have been shown, e.g. for ozone (Pougatchev et al., 1996; Vigouroux et al., 2008), carbon monoxide (Pougatchev and Rinsland, 1995; Borsdorf and Sussmann, 2009), and water vapor (e.g. Schneider et al., 2006). More recently, these measurements have been supplemented by high-accuracy-and-precision retrievals of climate gases from the Total Carbon Column Observing Network (TC-CON, http://www.tccon.caltech.edu), which relies on solar absorption spectra in the near-infrared (NIR) (e.g. Washenfelder et al., 2003; Wunch et al., 2011).

Since solar absorption spectrometers are using the sun as light source, all such instruments contain a device for active tracking of the solar position. However, the continuous alignment of the instrument’s line of sight with the center of the solar disc is generally prone to inaccuracies. Tracking errors in vertical direction cause the air mass observed by the spectrometer to differ from the air mass assumed in trace gas
retrievals (Hase, 2000). To a good approximation, this air mass error results in an equal relative error in the retrieved trace gas columns. Additionally, mispointing may result in further errors in retrieved column amounts, such as instrumental line shape variations if apertures inside the spectrometer are not fully illuminated.

As outlined in Hase (2000), a mispointing of 0.1° in zenith direction results in about 1% trace gas column error for an apparent solar zenith angle (sza) of 80°. These errors exceed current accuracy requirements for measured column amounts, e.g. the 0.5% accuracy requested for the TCCON network (Toon et al., 2006). It is therefore an issue to determine and correct for the influence of mispointing in solar FTIR measurements.

Information on the mispointing is contained in solar lines which appear in ground-based solar spectra in addition to the terrestrial absorption features. Mispointing perpendicular to the solar rotation axis causes rotational Doppler shifts in the solar lines. Measurements of the solar line shift therefore enable the determination of mispointing perpendicular to the solar rotation axis (Gisi et al., 2011). However, these measurements do not permit complete determination of the mispointing direction and norm since they do not constrain the mispointing component parallel to the solar rotation axis. This is the basic reason why there is currently no method available that enables a correction of mispointing-induced retrieval errors. In this study, we present a method to overcome this limitation and thereby enable a posteriori-correction of mispointing effects, to our knowledge for the first time.

This paper is structured as follows: in Sect. 2, we formulate the mispointing problem and outline the basic idea to its correction. Section 3 gives a detailed description of the mispointing determination scheme and the subsequent trace gas column correction. Section 4 contains an example for the implementation of the correction procedure using FTIR measurements at the Zugspitze (47.42° N, 10.98° E, 2964 m a.s.l.). Finally the correction results are validated via XCH₄ bias and trend analysis using reference solar FTIR measurements at the nearby Garmisch site (47.48° N, 11.06° E, 743 m a.s.l.). In Sect. 5 we summarize the results along with some concluding remarks.
2 Formulation of the mispointing problem and basic idea for a correction method

For all sun-tracking spectrometers, the alignment of the instrument’s line-of-sight with the sky position of the solar disc center is prone to inaccuracies. The zenith direction component of this mispointing causes the air mass assumed in trace gas column retrievals to differ from the real air mass during the measurement. This error in air mass results in an equally large relative error in the retrieved trace gas column.

The component of mispointing perpendicular to the solar rotation axis causes a Doppler shift in the solar lines of measured spectra. This solar line shift can be determined by a fit to the spectra (Gisi et al., 2011) and thereby provides a determination of the mispointing perpendicular to the solar rotation axis. Nevertheless, a single solar shift determination contains no information about the mispointing component parallel to the solar rotation axis. Therefore, the component of mispointing in zenith direction that causes bias in the retrieved trace gas columns cannot be deduced directly from such measurements.

However, the orientation of the solar axis relative to the zenith direction varies over time. If the change of the mispointing between two measurements is negligible compared to the magnitude of the mispointing, the changing axis orientation enables the determination of zenith and horizontal component of mispointing. The mispointing can therefore be fully constrained from a set of shift measurements at times $t_1$, $t_2$ with different axis orientations $\alpha_{axis,1}$ and $\alpha_{axis,2}$ (Fig. 1). In the following, the vector from the center of the solar disc to the actual pointing coordinates is designated as mispointing vector $m$.

Neglecting differential solar rotation, i.e. assuming constant angular velocity at all solar latitudes, a single shift measurement constrains the mispointing to lie on the straight line $s$ parallel to the solar rotation axis $a$. The distance between $s$ and $a$ is proportional to the measured solar line shift $\Delta \nu/\nu$. Combining two measurements with different axis orientations $\alpha_{axis,1}$ and $\alpha_{axis,2}$, the mispointing vector $m$ is then defined by
the intersection coordinates of the corresponding straight lines $s_1$ and $s_2$, respectively. In order to reduce errors due to inaccurate solar line shift measurements, it is favorable to combine larger sets of measured spectra to compute a mean mispointing vector instead of using only two measurements. In this case, the mean mispointing is defined by the mean intersection coordinates of all pairs of measurements that can be selected from a given set of spectra. Note that this approach relies on the assumption that changes of the mispointing within the set of spectra used to compute one mean value of $m$ are negligible compared to the magnitude of the mispointing itself.

3 Detailed implementation of the mispointing quantification and correction

In the following, the steps required to implement the mispointing determination approach are described in detail. As a first step, the time series of measured spectra is divided in time bins. We outlined in the previous section that the mispointing determination method relies on the assumption of approximately constant mispointing within each of the time bins. Therefore, the suitable choice of time bins results in a tradeoff between low statistical errors in mispointing results achieved by a large bin size and improved fulfillment of the underlying assumption of constant mispointing within each time bin that results from a smaller bin size. An example for the bin size adjustment in the case of the Zugspitze measurements is discussed in Sect. 4.2.

For all measured spectra, the solar line Doppler shift $\Delta \nu/\nu$ has to be determined. In our analysis, this task is performed using the PROFFIT software (Hase et al., 2004). The fit is performed on spectra measured with the optical bandpass filter used for CH$_4$ column retrievals, which covers the wavenumber range $2400 < \nu < 3100$ cm$^{-1}$. In order to assess the accuracy of the solar line shift fit, we compare these results to solar line shift measurements in the adjacent $2000 < \nu < 2650$ cm$^{-1}$ filter.

In addition to solar line shifts, the mispointing calculation requires knowledge of the orientation $\alpha_{axis}$ of the solar rotation axis relative to the zenith direction for each measured spectrum. More precisely, the orientation angle used in the mispointing calcu-
lation is the apparent angle from zenith direction to sun axis direction at the time and location of the measurements, i.e. the angle between projections of zenith direction and sun axis direction on a plane perpendicular to spectrometer’s line of sight. All necessary steps for calculation of $\alpha_{\text{axis}}$ are outlined in Appendix A.

Systematic mispointing is assumed to be caused by deviations of the sun tracker optics geometry from an idealized setup. Possible scenarios include e.g. inaccuracies in mirror orientation or misalignment of the quadrant diode that allows continuous adjustment of the instrument’s line of sight to follow the sun position. For such sources of tracking error, it is plausible to assume constant mispointing during limited time intervals in a coordinate system valid in the spectrometer, contrary to e.g. the azimuth/elevation coordinate system in the sky. Due to the sun tracker optics, the image of the sun undergoes reflections and rotations when transferred to the spectrometer entrance aperture. Therefore, the resulting image of the sun on the entrance aperture has to be calculated for each measurement.

The transformation of the solar image due to the solar tracker optics can be described by a concatenation of $3 \times 3$ imaging matrices resulting in an overall transfer matrix $T$. The orientation of the sun axis on the entrance aperture is then calculated by multiplying a vector with orientation $\alpha_{\text{axis}}$ with the correct transfer matrix $T$. For the retransformation of a mispointing vector $m$ derived in spectrometer coordinates to sky coordinates $m_{\text{sky}}$, $m$ has to be multiplied with the inverse of the transfer matrix, that is $m_{\text{sky}} = T^{-1} m$.

Contrary to the simplified solution scheme presented in Sect. 2, the angular velocity of solar rotation depends on solar latitude $\varphi$, a phenomena called differential solar rotation. The latitude-dependent angular velocity of solar rotation $\omega(\varphi)$ is described approximately by the following relation:

$$\omega(\varphi) = c_1 + c_2 \sin^2 \varphi + c_3 \sin^4 \varphi.$$  

Currently accepted values for the constants $c_1$, $c_2$, and $c_3$ are: $c_1 = 14.713 \pm 0.0491 \, \degree \, \text{d}^{-1}$, $c_2 = -2.396 \pm 0.188 \, \degree \, \text{d}^{-1}$, $c_3 = -1.787 \pm 0.253 \, \degree \, \text{d}^{-1}$ (Snodgrass and Ulrich, 6185).
1990). Due to differential solar rotation, a single solar line shift measurement does not constrain the mispointing to lie on a straight line as depicted in Fig. 1, but on a line with constant angular velocity $\omega(\phi)$.

The radial mispointing in degree perpendicular to the solar rotation axis $m_{\text{rad}}$ can be calculated from solar line shift measurements:

$$ m_{\text{rad}} = [\Delta \nu/\nu \cdot c/\omega(\phi)] \cdot r_{\text{sun, apparent}}/r_{\text{sun}}, $$

where $c = 2.99792458 \times 10^8 \text{ m s}^{-1}$, $r_{\text{sun}} = 6.958 \times 10^8 \text{ m}$, $r_{\text{sun, apparent}} = 0.266^\circ$.

In this study, instead of using Eq. (2) for mispointing calculation, a linear approximation to this relation is performed (see Fig. 2). Mispointing results determined from Zugspitze measurements suggest this approximation induces no significant additional error in the results. While the mean relative error of mispointing over the Zugspitze measurement time series is 9.5 %, the error of radial mispointing induced by the linear approximation is 0.36 %, which is negligible compared to the mispointing error.

The following steps are performed to obtain the linear approximation:

1. A mean factor for conversion of solar shifts into mispointing is determined iteratively from our dataset. To obtain the conversion factor, the distributions of mispointing values parallel and perpendicular to the solar equator are assumed to be similar. Using the shift-mispointing conversion given in Gisi et al. (2011), a typical distribution of mispointing values parallel to the solar rotation axis is then calculated from the solar line shift measurements. By means of Eq. (1), this mispointing distribution can be converted to a typical angular velocity distribution for the given dataset. The mean value of this $\omega(\phi)$ distribution is then used to calculate an improved shift-mispointing conversion factor replacing $\omega(\phi)$ in Eq. (2) by the mean value of the angular velocity distribution. The above steps are repeated iteratively until convergence is reached. This results in an adjusted shift-mispointing conversion of

$$ m_{\text{rad, mean}} = \Delta \nu/\nu \cdot 38.771.4^\circ. $$ (3)
ii. The distribution of mispointing parallel to the equator $m_{\text{rad}}$ can now be calculated using Eq. (3). We assume that the distribution of mispointing parallel to the sun axis $m_{\text{axis}}$ is similar to the distribution of $m_{\text{rad}}$. A solar latitude distribution for our data set can now be derived using $\varphi = \arcsin(m_{\text{axis}}/r_{\text{sun, apparent}})$. This enables calculating $\omega(\varphi)$ by means of Eq. (1).

iii. A linear fit to the mispointing values calculated using Eq. (2) and the angular velocity values determined in step ii is then performed. The final result for the best fit linear approximation is

$$m_{\text{rad, lin}} = \Delta \nu/\nu \cdot (a + b \cdot m_{\text{axis}}),$$

where $a = 38\,301.9 \pm 2.9^\circ$ and $b = 13\,363 \pm 63$.

Equation (4) implies that a solar shift measurement constrains the mispointing to lie on a pair of rays $r$ with a distance to the solar rotation axis on the solar equator of $m_0 = \Delta \nu/\nu \cdot a$, and at an angle relative to the zenith direction of $\alpha_{\text{corr}} = \alpha_{\text{axis}} \pm \Delta \alpha$, where $\Delta \alpha = \arctan(\Delta \nu/\nu \cdot b)$, as shown in Fig. 3.

Given the orientation of the solar axis and the conversion of solar line shift to mispointing, we can now calculate mispointing results. As described at the beginning of this section, the measurement time series is distributed in time bins. For each bin, all possible combinations of measurement pairs are considered. For each of the $n(n-1)/2$ possible pairs selected from the $n$ measurements within a time bin, a mispointing vector $m$ is calculated. Finally, the mean of the mispointing over each time bin is calculated as the error-weighted mean of all $m$. The computation of the weighted means requires an estimate of the uncertainty of intersection coordinates. The uncertainty estimate was deduced from the difference of coincident solar shift measurements in adjacent optical filters. A detailed description of this uncertainty estimate is given in Appendix B.

Corrected trace gas column amounts can be calculated from the mispointing results with two distinct correction methods: the a posteriori correction method consists in subtracting the mispointing in zenith direction $m_{y,\text{sky}}$ from the apparent sza taken from
the trace gas retrieval ray trace calculation. Corrected air mass values can then be calculated according to

\[ airmass_{corr} = 1 / \cos(sza - m_y,sky). \]  

We then multiply retrieved trace gas columns with \( airmass/airmass_{corr} \) to obtain corrected columns.

The second (a priori) correction method takes into account that in addition to the effect on the conversion of slant path to vertical column, the mispointing has slight influence on the forward spectral calculations performed in the retrieval. The a priori method therefore uses the mispointing-corrected \( sza \) as an input to the retrieval. The retrieval is then repeated with the corrected input values resulting in corrected trace gas column results.

4 Example correction for Zugspitze FTIR

4.1 Solar FTIR and tracker setup

The solar FTIR instrument considered in the example correction is located at the Zugspitze (47.42° N, 10.98° E, 2964 m.a.s.l.). The system is based on a Bruker IFS 125 instrument, and is described in detail in Sussmann and Schäfer (1997). For the validation of correction results we furthermore use data from the nearby Garmisch FTIR (47.48° N, 11.06° E, 743 m.a.s.l.).

The geometry of the Zugspitze sun tracker is depicted schematically in Fig. 4. The custom-made tracker is located in an astronomical dome above the spectrometer that is opened for measurements. The tracker optics consists of a first plane 45° elevation mirror (M1) to adjust the elevation angle \( (el) \) of the instrument’s line of sight. Sunlight is then guided to the spectrometer below by a second plane 45° mirror (M2). The azimuth of the line of sight \( (az) \) is adjustable by rotation of both mirrors on an arm.
same sky position can be reached by the tracker system with two distinct arm orienta-
tions with 180° position difference: Flip 1, used for most measurements and depicted in
Fig. 4a and Flip 0, used for measurements with az < 116° or az > 296° since Septem-
ber 2012, see Fig. 4b.

The setup in place since September 2012 furthermore contains an off-axis mirror
(M_3, f = 478 mm) that changes beam orientation to horizontal again and creates an
image of the sun on the aperture A_1. The image of the sun is centered on the aper-
ture A_1 by a quadrant diode continuously giving feedback for tracker positioning. Since
September 2014, the active tracking by means of the quadrant diode has been replaced
by a Camtracker (Gisi et al., 2011) system inside the spectrometer. Before Septem-
ber 2012, horizontal beam direction and creation of an image on A_1 was achieved by
the parabolic mirror M'_3 (f = 1920 mm) and an additional plane mirror M'_4, instead of
the off-axis mirror M_3 (see Fig. 4c).

4.2 Implementation of correction

The first step in the implementation of the mispointing correction procedure consists in
deducing solar line shifts from the measured spectra as described in Sect. 3. Figure 5
shows the time series of solar line shifts obtained from the Zugspitze measurements.

As mentioned in Sect. 3, the transformation of the solar image by the tracker optics
can be characterized by 3×3 imaging matrices that describe changes in beam direction
and changes of the solar image in the image plane perpendicular to the beam direction.
In the following, we establish those transfer matrices for the optics setup described in
Sect. 4.1. The corresponding transfer matrices are established for the configurations
Flip 1 and Flip 0 in the current optical setup shown in Fig. 4a and b and the Flip 1
configuration for the pre-September 2012 setup shown in Fig. 4c.

The complete transformation can be described by a concatenation of three differ-
ent types of operations: (i) reflections on a plane mirror perpendicular to the beam
direction, (ii) rotation of the coordinate system and finally (iii), reflection on 45° mirrors.
Operation (i) corresponds to mirror matrices $M$, e.g. for a mirror in the $xy$-plane

$$M_{xy} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -1 \end{pmatrix}. \quad (6)$$

Operation (ii) is described by the standard $R^3$ rotational matrices $R_{x/y/z, \varphi}$, where $x/y/z$ designates the direction of the rotation axis and $\varphi$ the rotation angle in mathematical orientation. Note that a rotation of the coordinate system by an angle $\varphi$ corresponds to $R_{x/y/z, -\varphi}$. Reflection on 45° mirrors (iii) can be further decomposed in a combination of rotation according to (ii) to a coordinate system in which the mirror lies in a plane of base vectors, e.g. the $xy$-plane. This rotation is followed by a reflection according to (i) and a final backwards rotation of the coordinate system. In the following, the transfer matrices for 45° mirrors are designated $S_{x/y \pm}$, where the $x/y$-index specifies the coordinate axis parallel to the mirror if the $z$ axis is orientated in beam direction prior to the reflection. The sign in the index is “−” if the third axis points towards the mirror and “+” if the third axis points away from the mirror. The matrices $S_{x/y \pm}$ have the following form:

$$S_{x \pm} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & \pm 1 \\ 0 & \pm 1 & 0 \end{pmatrix}, \quad S_{y \pm} = \begin{pmatrix} 0 & 0 & \pm 1 \\ 0 & 1 & 0 \\ \pm 1 & 0 & 0 \end{pmatrix}. \quad (7)$$

Using the basic operations (i), (ii), and (iii) we can now deduce transfer matrices $T$ for the Zugspitze sun tracker system. The initial coordinate system valid in the sky is defined with the $x$ axis in horizontal, the $y$ axis in zenith direction and the $z$ axis along the line of sight towards the instrument. After each sub step of the path through the tracker optics, the coordinate system is rotated to orient the $z$ axis in ingoing beam direction.
The individual steps can be tracked in Fig. 4. For the current setup and Flip 1 configuration (Fig. 4a), the transfer matrix components and final result are:

\[
T_{F1}^{-1} = T_{F1} = R_x,90^\circ S_x + R_z,az R_x,-90^\circ S_x - R_z,el R_y,-90^\circ S_y + \\
\begin{pmatrix}
-\cos(-az + el) & -\sin(-az + el) & 0 \\
-\sin(-az + el) & \cos(-az + el) & 0 \\
0 & 0 & 1
\end{pmatrix}
\]

Note that \( T_{F1} \) describes the transfer to a spectrometer coordinate system in which the \( x \) and \( y \) axes are rotated relative to the horizontal and vertical direction by a constant angle \( c \). As visible in Fig. 4, this constant rotation angle \( c \) depends on the orientation of the spectrometer and is equal for all measurements in all optical configurations. Since a transformation to a common spectrometer coordinate system with arbitrary orientation is sufficient for our analysis, the constant rotation is neglected in all transfer matrices.

In Flip 0 configuration (Fig. 4b), the corresponding matrix is given by

\[
T_{F0}^{-1} = T_{F0} = R_x,90^\circ S_x + R_z,az R_x,180^\circ R_y,180^\circ M_{xy} R_z,-el R_y,90^\circ S_y - \\
\begin{pmatrix}
\cos(az + el) & -\sin(az + el) & 0 \\
-\sin(az + el) & -\cos(az + el) & 0 \\
0 & 0 & 1
\end{pmatrix}
\]

For the optical setup before September 2012 and Flip 1 configuration (Fig. 4c), we obtain:

\[
T_{F1old}^{-1} = R_x,-90^\circ S_x + R_y,180^\circ M_{xy} R_z,az R_x,-90^\circ S_x - R_z,el R_y,-90^\circ S_y + \\
\begin{pmatrix}
\cos(-az + el) & \sin(-az + el) & 0 \\
-\sin(-az + el) & \cos(-az + el) & 0 \\
0 & 0 & 1
\end{pmatrix} \neq T_{F1old}^{-1}
\]
The next analysis step consists in dividing the measurement time series in time bins. For the Zugspitze measurements, each time bin was chosen to comprise the number of measurement days necessary to reach a total number of at least $n_{\text{min}}$ spectra in the bin. The choice of time bin size $n_{\text{min}}$ results from a tradeoff between the statistical uncertainty of the mispointing result and the degree of fulfillment of the assumption that mispointing is approximately constant within each time bin. Figure 6a demonstrates this tradeoff: the mean error of the mispointing result in zenith direction ($\Delta m_y$) declines with increasing bin size. Variations of the mispointing within a time bin result in scatter of the intersection coordinates for different measurement pairs included in the bin. Therefore, the scatter of the intersection coordinates as given by their standard deviation divided by the norm of the mispointing vector indicates how well the assumption of constant mispointing is fulfilled. As visible in Fig. 6a, the median of this intra-bin scatter increases with increasing $n_{\text{min}}$, indicating more variability of mispointing within time bins. As an indicator to find an optimum $n_{\text{min}}$, we use the mean of XCH$_4$ diurnal variation over the measurement time series (see Sussmann et al., 2011). Since the underlying real XCH$_4$ diurnal variation can be assumed to be significantly lower than the measured values, $n_{\text{min}}$ is chosen to minimize the measured diurnal variation. As shown in Fig. 6b, a bin size of $n_{\text{min}} = 20$ is chosen for the Zugspitze measurements based on this criterion.

4.3 Results and validation via methane trend analysis

In this section, the mispointing results based on the Zugspitze measurements and their validation by means of XCH$_4$ trend analysis are presented. We consider the time interval from April 2006 until March 2015. This time interval was chosen based on three criteria: it coincides with the phase of renewed increase of atmospheric methane concentrations (e.g. Sussmann et al., 2012). Furthermore, the interval includes the most
up-to-date measurements available. The last criterion is that the interval length is a multiple of a one-year period, which is crucial for avoiding bias in the trend analysis.

The time series of mispointing in spectrometer coordinates and the zenith component of the mispointing in sky coordinates is shown in Fig. 7. The mean mispointing in zenith direction over the measurements made in the April 2006 to September 2012 time interval, which corresponds to the optics setup shown in Fig. 4c, is $0.024 \pm 0.001^\circ$. Within the September 2012 to September 2014 interval (optics setup shown in Fig. 4a and b and quadrant diode) the mean mispointing is $-0.063 \pm 0.005^\circ$, and for the October 2014–March 2015 interval (optics setup shown in Fig. 4a and b and Camtracker) it is $0.024 \pm 0.008^\circ$.

The mispointing determination scheme relies on the basic assumption of approximately constant mispointing within each time bin. The validity of this assumption can be evaluated as outlined in Sect. 4.2, namely by analysis of the intra-bin scatter of mispointing results. Throughout the September 2012 to September 2014 time interval, the median of the scatter of mispointing results within each time bin was only 46 % of the mispointing vector norm in spectrometer coordinates, which means that the assumption of constant mispointing within each time bin is appropriate and leads to a meaningful trace gas column correction. For the April 2006–September 2012 and October 2014–December 2014 phases, the intra-bin mispointing scatter corresponds to 108 and 152 % of the mispointing vector norm in spectrometer coordinates, respectively. Therefore, the basic assumption of constant mispointing is only poorly fulfilled in these phases. This is due to the fact that the mispointing values in these phases were generally very small, which makes a mispointing determination with small relative error challenging. However, due to the small mispointing values, the mispointing correction has only very minor influence on the XCH$_4$ values in these time intervals.

The use of the a posteriori correction method presented in Sect. 3 instead of the full a priori correction results in a 5 % bias in the zenith component of the mispointing for the Zugspitze measurement time series. This corresponds to only $\sim 0.02$ % bias in XCH$_4$. Therefore, the a posteriori method can be considered to provide a fair approxi-
mation to the a priori results that has the advantage of not having to repeat the trace gas retrieval procedure after the mispointing determination.

Figure 8a shows a comparison of the corrected and uncorrected Zugspitze time series of XCH$_4$ monthly means for the phase of renewed methane increase since 2006. In Fig. 8b, the mispointing correction applied to the original time series is shown. The mean of XCH$_4$ correction over all measurements made in the time interval most affected by the mispointing (September 2012–September 2014) is $-2.82 \pm 2.08$ ppb.

The mispointing results are validated by means of methane trend analysis. To perform this analysis, monthly means are calculated from the uncorrected and corrected XCH$_4$ time series. The trend analysis is performed as described in Gardiner et al. (2008) and Sussmann et al. (2012). In summary, all months with $n > 7$ measured spectra are included in the analysis. We then calculate monthly means and subtract the mean annual cycle fitted as a third order Fourier series from the time series of XCH$_4$ monthly means. Finally a trend is fitted to the deseasonalized time series. The trend uncertainty is determined by means of bootstrap reanalysis.

Table 1 shows the Zugspitze XCH$_4$ trend for the April 2006–March 2014 time interval and its 95% confidence interval. Due to the major perturbations in the pointing accuracy in the September 2012–September 2014 interval (Fig. 8), the uncorrected Zugspitze trend is no longer consistent with the trend determined from measurements at the nearby Garmisch site. (Note, trend consistency could be shown for the time period before September 2011, see Sussmann et al., 2012). However, applying mispointing correction restores the consistency of Zugspitze and Garmisch trend results for the whole time series. This holds both for a posteriori-corrected and a priori-corrected results. As outlined in Appendix C, mispointing correction also restores consistency in the bias between the Zugspitze and Garmisch XCH$_4$ monthly means for the phases with differing optical configurations.
5 Summary and conclusions

We presented a strategy to determine pointing errors in solar absorption spectrometry due to the sun tracking device not perfectly targeting at the center of the solar disk. Knowledge of the mispointing allows for subsequent correction of resulting errors in trace gas total column or vertical profile retrievals. Our approach relies on the determination of the Doppler shift of solar spectral lines from measured spectra. However, knowledge of solar line shifts allows a determination of only one component of the mispointing vector on the solar disk, namely the component perpendicular to the solar rotation axis. This does not provide sufficient information to deduce the mispointing component in zenith direction, which causes errors in trace gas retrievals. We demonstrate, to our knowledge for the first time, a way to overcome this problem. The necessary knowledge of both vector components of the mispointing can be obtained using multiple solar line shift measurements at different orientations of the solar rotation axis relative to the zenith direction.

An application of our original mispointing correction strategy was demonstrated via measurements made with the Zugspitze solar FTIR system. We found that a short period of the measurement series (i.e. September 2012–September 2014) was notably affected by mispointing problems caused by a non-optimum optical configuration, and a mean vertical mispointing of $-0.063 \pm 0.005^\circ$ was derived. As an example for the impact on trace gas retrievals, this mispointing was shown to lead to a mean bias of $-2.82 \pm 2.08$ ppb in retrieved $\text{XCH}_4$ monthly means.

The results of the mispointing correction were validated by means of methane trend analysis. The trend derived from uncorrected $\text{XCH}_4$ monthly means in the April 2006–March 2015 time interval for the Zugspitze site is $6.45 \ [5.84, \ 7.04] \ \text{ppb yr}^{-1}$, inconsistent with the $5.22 \ [4.77, \ 5.65] \ \text{ppb yr}^{-1}$-trend of the nearby Garmisch site. Mispointing correction resolves this inconsistency, resulting in a trend of $6.07 \ [5.55, \ 6.59] \ \text{ppb yr}^{-1}$ for Zugspitze and $5.20 \ [4.74, \ 5.64] \ \text{ppb yr}^{-1}$ for Garmisch. Furthermore, applying mispoint-
ing correction is shown to restore consistency in the bias between the Zugspitze and Garmisch measurements for the phases with differing optical configurations.

In conclusion, the mispointing correction presented in this study is applicable to all kind of solar absorption spectrometric measurements, i.e. soundings in the mid infrared and near infrared. First of all, the correction yields benefit for total vertical column retrievals, and we showed an easy-to-implement a posteriori correction, which is simply correcting the retrieved slant column according to the zenith component of the derived mispointing vector. We also presented a more sophisticated correction approach that uses the mispointing-corrected zenith angle as an input to repeated trace gas retrievals. The benefit of this (a priori) correction approach is that also the ray tracing in the forward spectral calculations in the retrieval is performed more accurately according to an improved knowledge of the true zenith angle. While this optional a priori correction approach leads only to minor improvements in terms of the total vertical column result, the a priori correction approach should be preferred if the retrieved target product is the trace gas profile shape (because of the more realistic ray tracing for each atmospheric layer). Finally, the outcome of our paper could be of particular benefit for refining existing records of high-accuracy-and-precision greenhouse gas soundings for improved trend analysis and source-sink inversions.

Appendix A: Orientation of solar rotation axis

In this section, we outline the calculation of $\alpha_{axis}$, which is defined as the angle between projections of zenith direction and sun axis on a plane perpendicular to the spectrometer’s line of sight. For a sun-viewing instrument, this projection plane corresponds to the plane defined by the day/night separation line on the Earth. The orientation angle $\alpha_{axis}$ consists of three distinct projections onto the day/night separation plane: the first contribution $\beta$ is the angle between the Earth rotation axis and the zenith direction, the second angle $\gamma$ spans from the ecliptic axis to the Earth’s rotation axis. The final contribution $\delta$ describes the angle between the sun axis and the ecliptic axis. In total,
\(\alpha_{\text{axis}}\) is calculated as:

\[
\alpha_{\text{axis}} = \beta + \gamma - \delta \tag{A1}
\]

The calculation of the component \(\beta\), ranging from the projections on the day/night separation plane of zenith direction to the Earth rotation axis is represented in Fig. A1a. The angle \(\beta\) has a daily cycle due to the Earth’s rotation. The amplitude \(\beta_{\text{max}}\) of this daily cycle shows a seasonal variability due to variations in the inclination \(\varepsilon\) of the Earth axis relative to the day/night separation plane. The inclination \(\varepsilon\) can be calculated as:

\[
\varepsilon = \arcsin(\sin(\varepsilon_{\text{max}}) \cdot \sin(YE)), \tag{A2}
\]

where \(YE\) designates the heliocentric ecliptic longitude of the Earth and \(\varepsilon_{\text{max}} = 23.43^\circ\). This leads to an amplitude of the daily cycle given by:

\[
\beta_{\text{max}} = \arctan(\tan(90^\circ - \text{observer latitude}) / \cos \varepsilon). \tag{A3}
\]

The angle \(\beta\) can then be expressed in terms of \(\beta_{\text{max}}\) and observation time

\[
\beta = - \arctan(\tan(\beta_{\text{max}}) \cdot \sin(\text{day fraction} \cdot 2\pi)), \tag{A4}
\]

where \(\text{day fraction} = \text{hours since local noon} / 24\text{ h}\).

The second orientation component \(\gamma\) is the angle between the Earth rotation axis and the ecliptic axis and has a seasonal cycle due to the inclination of Earth axis. As shown in Fig. A1b, the amplitude of this seasonal variability is equal to the inclination of the Earth axis relative to the ecliptic axis. Consequently, \(\gamma\) can be calculated as

\[
\gamma = - \arctan(\tan(\varepsilon_{\text{max}}) \cdot \cos(YE)). \tag{A5}
\]

The calculation of the third angle component \(\delta\), between sun axis and ecliptic axis, is outlined in Giles (2000). In summary,

\[
\delta = \arctan( - \cos(\eta - \Omega) \cdot \tan i), \tag{A6}
\]

where standard values for the constants \(i\) and \(\Omega\) are \(i = 7.25^\circ\), \(\Omega = 73.67^\circ + 0.013958^\circ (t \text{ [years]} - 1850.0)\), and \(\eta = YE + 180^\circ\).
Appendix B: Uncertainty estimate of intersection coordinates

In order to obtain an estimate of the intersection coordinate uncertainty, we adopted the following approach: an estimate of solar line shift uncertainty can be gained from the difference of coincident solar shift measurements in the adjacent 2400 < ν < 3100 and 2000 < ν < 2650 cm$^{-1}$ filters. A 15-min coincidence interval was chosen for this calculation.

Instead of infinitesimal-width rays as depicted in Fig. 3, the rays $r_1$ and $r_2$ are assumed to have a width corresponding to the measured solar shift difference. The ray widths $\Delta r_1$ and $\Delta r_2$ depend on the measured solar line shifts $\Delta s_1$ and $\Delta s_2$, respectively. Furthermore, due to differential solar rotation, the conversion from shift differences to ray widths depends on the intersection coordinates. The conversion is given by the quotient of the mispointing perpendicular to the solar axis $m_{\text{rad, lin}}$ according to Eq. (4) and the measured solar shift $s$:

$$\Delta r = \Delta s \cdot (m_{\text{rad, lin}} / s) \quad (B1)$$

Due to the finite ray widths $\Delta r_1$ and $\Delta r_2$, an overlap parallelogram (see Fig. B1) emerges instead of an intersection point. The length of the diagonals of the parallelogram ($e, f$) can be calculated as follows:

$$\Delta \alpha = \alpha_{\text{corr}, 2} - \alpha_{\text{corr}, 1}$$

$$a_1 = |\Delta r_1 / \sin(\Delta \alpha)|, a_2 = |\Delta r_2 / \sin(\Delta \alpha)|$$

$$e^2 = a_1^2 + a_2^2 - 2a_1a_2 \cos(\Delta \alpha)$$

$$f^2 = a_1^2 + a_2^2 - 2a_1a_2 \cos(180^\circ - \Delta \alpha). \quad (B2)$$

Finally, the $x$ and $y$ components of the uncertainty estimate, i.e. $\Delta x$, $\Delta y$, are given by the projection of the overlap parallelogram on the $x$ and $y$ axes, respectively. Note that the $y$ axis is defined to be equivalent to the zenith direction.

$$\alpha_f = \arccos \left( \frac{a_2^2 - a_1^2 - f^2}{-2a_1f} \right) + \alpha_{\text{corr}, 2}$$
\[ \Delta x_e = \cos(\alpha_f) \cdot e, \Delta x_f = \sin(\alpha_f) \cdot f \]
\[ \Delta y_e = \sin(\alpha_f) \cdot e, \Delta y_f = \cos(\alpha_f) \cdot f \]
\[ \Delta x = \max(\Delta x_e, \Delta x_f), \Delta y = \max(\Delta y_e, \Delta y_f). \] (B3)

Appendix C: Bias of XCH\(_4\) monthly means between Zugspitze and Garmisch measurements

Due to the lower elevation of the Garmisch site and the decrease of methane concentration with increasing altitude, the XCH\(_4\) values measured at this station are generally higher than at the Zugspitze site. Since the mean shape of the methane number density profile is not expected to vary significantly over the time interval considered in this study, the relative bias between the Zugspitze and Garmisch values is expected to be consistent for different optical configurations. Table C1 shows the mean of XCH\(_4\) monthly mean bias over the following time intervals: September 2010–August 2012, i.e. the two-year period before the optics configuration was changed. Further intervals include September 2012–October 2014, i.e. the approximately two-year period with changed optics and November 2014–March 2015, i.e. the time interval since the setup of the Camtracker system. As visible in Table C1, the bias results are not consistent the three phases for the uncorrected measurements. However, applying the a posteriori mispointing correction results in consistent bias values for all three phases.

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Table 1. XCH₄ trend [ppb yr⁻¹] for the April 2006–March 2015 time interval and corresponding 95 % confidence intervals; Zugspitze and Garmisch sites, uncorrected, a posteriori and a priori corrected.

<table>
<thead>
<tr>
<th>Location</th>
<th>Uncorrected</th>
<th>A posteriori corrected</th>
<th>A priori corrected</th>
</tr>
</thead>
<tbody>
<tr>
<td>Garmisch</td>
<td>5.22 [4.77, 5.65]</td>
<td>5.20 [4.74, 5.64]</td>
<td>5.19 [4.74, 5.63]</td>
</tr>
</tbody>
</table>
Table C1. Bias of XCH$_4$ monthly means between Garmisch and Zugspitze measurements and corresponding 95\% confidence intervals. Results are presented for time intervals with different optical configurations and both a posteriori mispointing-corrected and uncorrected measurements.

<table>
<thead>
<tr>
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</thead>
<tbody>
<tr>
<td>bias uncorrected [%]</td>
<td>2.04 ± 0.18</td>
<td>1.46 ± 0.27</td>
<td>2.24 ± 0.37</td>
</tr>
<tr>
<td>bias a posteriori-corrected [%]</td>
<td>1.96 ± 0.19</td>
<td>1.60 ± 0.19</td>
<td>2.05 ± 0.36</td>
</tr>
</tbody>
</table>
Figure 1. Schematics of the mispointing determination strategy. Solar line shifts are measured at times $t_1$, $t_2$ with corresponding solar axis orientations $\alpha_{\text{axis},1}$ and $\alpha_{\text{axis},2}$. The mispointing vector $m$ is defined by the intersection of the lines $s_1$ and $s_2$ parallel to the solar rotation axes $a_1$ and $a_2$, respectively. Differential solar rotation is neglected in this figure.
Figure 2. Conversion of solar shift to radial mispointing. $m_{axis}$ designates the apparent distance from the solar equator. Blue: mean conversion factor given in Gisi et al. (2011). Green: iteratively determined mean conversion for the Zugspitze dataset according to Eq. (3). Black: conversion according to Eq. (2), using $\omega(\phi)$ values calculated with Eq. (1), $m_{axis}$ calculated using Eq. (3). Red: best fit linear conversion according to Eq. (4).
Figure 3. Linear approximation of differential rotation. A solar line shift measurement constrains the mispointing to lie on a line with constant angular velocity $\omega(\phi)$ (blue line). Linear approximation of this relation results in a constraint of mispointing on rays $r$ tilted away from the solar rotation axis by an angle $\Delta \alpha$ and with a minimum distance $m_0$ to the axis (red line).
Figure 4. Geometry of the Zugspitze solar tracker optics. (a) Current optical setup after September 2014, Flip 1. (b) Current setup, Flip 0. (c) Optical setup before September 2012.
**Figure 5.** Time series of solar line shifts determined from Zugspitze FTIR spectra in the 2400 < $\nu$ < 3100 cm$^{-1}$ optical filter.
Figure 6. Choice of time bin size for Zugspitze mispointing determination. (a) Mean zenith mispointing error (black) and median of the relative scatter of mispointing results within time bins (blue). (b) Mean $1\sigma$-XCH$_4$ diurnal variation.
Figure 7. Mispointing results determined from Zugspitze measurements. (a) $x$ component of mispointing in spectrometer coordinates. (b) $y$ component of mispointing in spectrometer coordinates. (c) Zenith component of mispointing in sky coordinates.
Figure 8. (a) Comparison of corrected (green) and uncorrected (red) Zugspitze XCH$_4$ monthly mean time series. (b) Time series of differences between corrected and uncorrected XCH$_4$ monthly.
Figure A1. Calculation of sun axis orientation relative to zenith direction. (a) $\beta$: zenith direction relative to Earth rotation axis. (b) $\gamma$: Earth rotation axis relative to ecliptic axis. Both subfigures represent projections on the day/night separation plane, direction of view towards the sun.
Figure B1. Calculation of mispointing uncertainty.