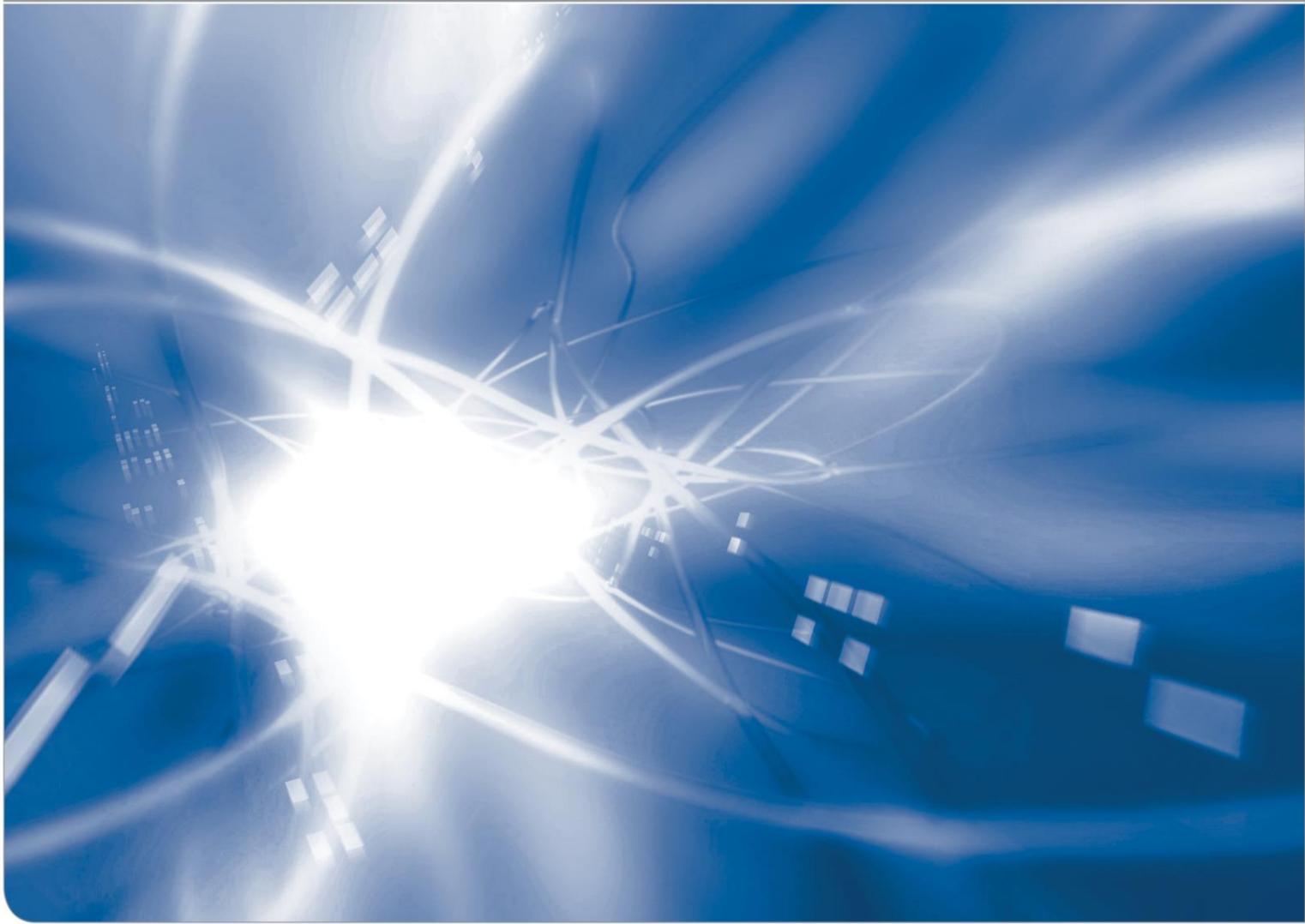


Further improvement of (n,p) and (n, α) reaction cross-sections calculated using the TALYS code

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Abstract

A simple approach is proposed for the improvement of calculated cross-sections. The idea is to search for regularities in deviations of measured and calculated reaction cross-section, and the use of obtained information for correction of calculated values.

The approach was applied for improvement of (n,p) and (n,α) reaction cross-sections at 14.5 MeV calculated using the TAYLS code.

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1. Introduction

A discrepancy between experimental and calculated nuclear reaction cross sections is caused mainly by deficiency of nuclear models, uncertainty of model parameters used for calculations, including lack of parameterizations of values used for description of nuclear level density and non-equilibrium particle and cluster emission, and shortcomings of measurements.

The goal of this work is a search for regularities in the deviation of measured and calculated (n,p) and (n,α) reaction cross-sections, and the use of obtained information for an improvement of calculated values. The analysis of deviations is performed for cross-sections calculated using the TALYS code [1] and cross-sections obtained in Refs.[2,3] from the analysis of different experiments for incident 14.5 MeV neutrons for (n,p) and (n,α) reactions.

Details of calculations, the analysis of deviations, and the improvement of calculated data are briefly discussed below.

2. Search for regularities in deviation of experimental and calculated cross-sections

When using modern nuclear models, approximations, and parameterizations as implemented in the TALYS code, the description of the nature of possible systematic deviations of experimental and calculated values in advance is hardly possible.

Consequently, a “blind search” of possible correlations seems a reasonable procedure to analyse deviations of experimental and calculated cross-sections. Some analogy with development of modern systematics of nuclear reaction cross-sections can be found in Refs.[3,4].

In the present work correlations were explored between deviations of calculated and measured cross-sections, and combinations of values such as shell and pairing corrections, separate energies, and elements of systematic formulas [2-4] .

The (n,p) and (n,α) reaction cross-sections at 14.5 MeV were calculated using the TALYS code for target nuclei with atomic number from 18 to 83. The Fermi gas model with the energy dependent level density parameter combined with the “constant temperature” model [1] was applied for calculations of nuclear level density,

which selection corresponds to the input TALYS variable *lmodel* equal to one.

The analysis of the difference between theoretical and measured cross-sections was carried out using data from Refs.[2,3] adopted as an “experimental basis” for construction of systematics for (n,p) and (n,α) reaction cross-sections at 14.5 MeV. Data [2,3] were obtained from the analysis of different measurements, and as a result a single value of (n,p) and (n,α) reaction cross-section was attributed to each target nucleus.

The following deviation factors [5] were used for the quantification of difference between experimental (σ^{exp}), calculated or evaluated (σ) cross-sections

$$H = \frac{1}{N} \sum_{i=1}^N \left(\frac{\sigma_i^{\text{exp}} - \sigma_i}{\Delta\sigma_i^{\text{exp}}} \right)^2, \quad (1)$$

$$F = 10^{\left(\frac{1}{N} \sum_{i=1}^N \left[\log(\sigma_i^{\text{exp}}) \log(\sigma_i) \right]^2 \right)^{1/2}}, \quad (2)$$

$$R^{\text{EC}} = \frac{1}{N} \sum_{i=1}^N \frac{\sigma_i^{\text{exp}}}{\sigma_i}, \quad (3)$$

$$R^{\text{CE}} = \frac{1}{N} \sum_{i=1}^N \frac{\sigma_i}{\sigma_i^{\text{exp}}}, \quad (4)$$

where N is the number of target nuclei,

2.1 (n,p) reaction cross-section

The deviation of experimental and calculated cross-sections was analysed for 125 targets with atomic number from 18 to 83 at primary neutron energy 14.5 MeV.

Figs.1-3 show H, F, and R^{CE} deviation factors calculated for various N values growing with the increase of atomic number of target nucleus. The total value of deviations factor, as usually used for comparison of experimental and theoretical data [5], corresponds to the data on Figs.1-3 for the atomic number 83.

Increasing the value of factors of H, F, and R^{CE} for atomic numbers above 50 indicates systematic deviations of experimental and calculated cross-sections. Further analysis shows, that in particular for targets with $Z > 50$ calculated (n,p) reaction cross section can be subsequently improved.

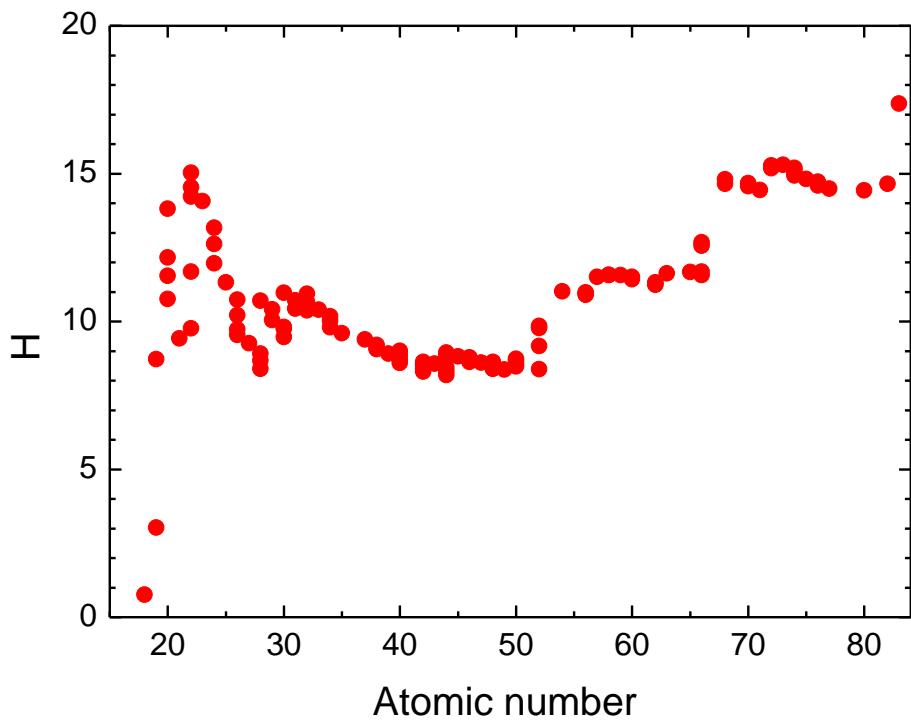


Fig.1 The H-factor, Eq.(1) for (n,p) reaction at 14.5 MeV corresponding to results of TALYS calculations obtained for various N values growing with the increase of atomic number of target nucleus. See details in the text.

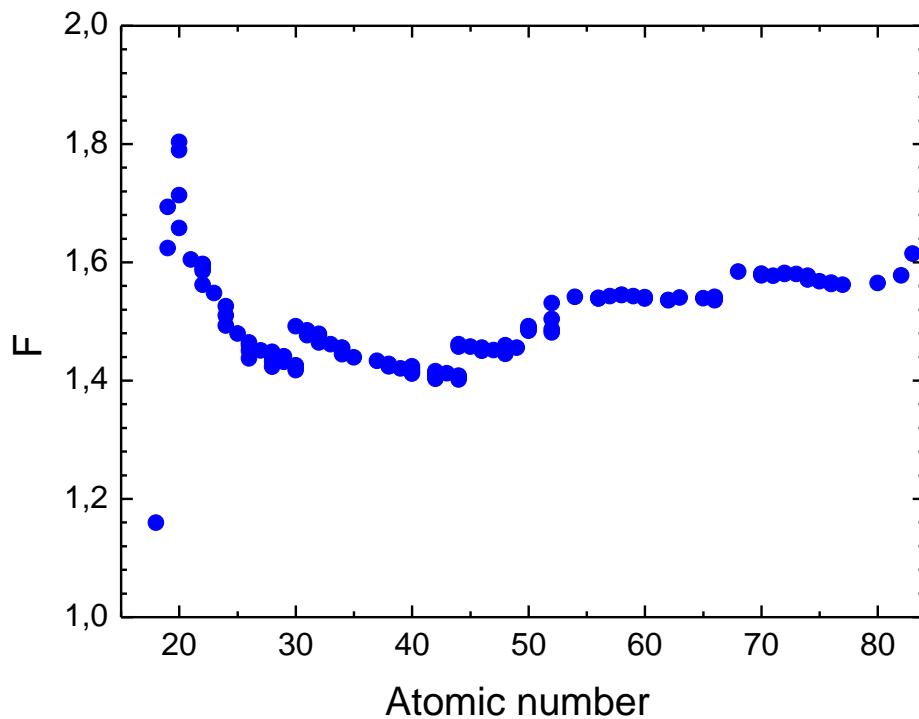


Fig.2 The F-factor, Eq.(2) for (n,p) reaction at 14.5 MeV corresponding to results of TALYS calculations obtained for various N values growing with the increase of atomic number of the target.

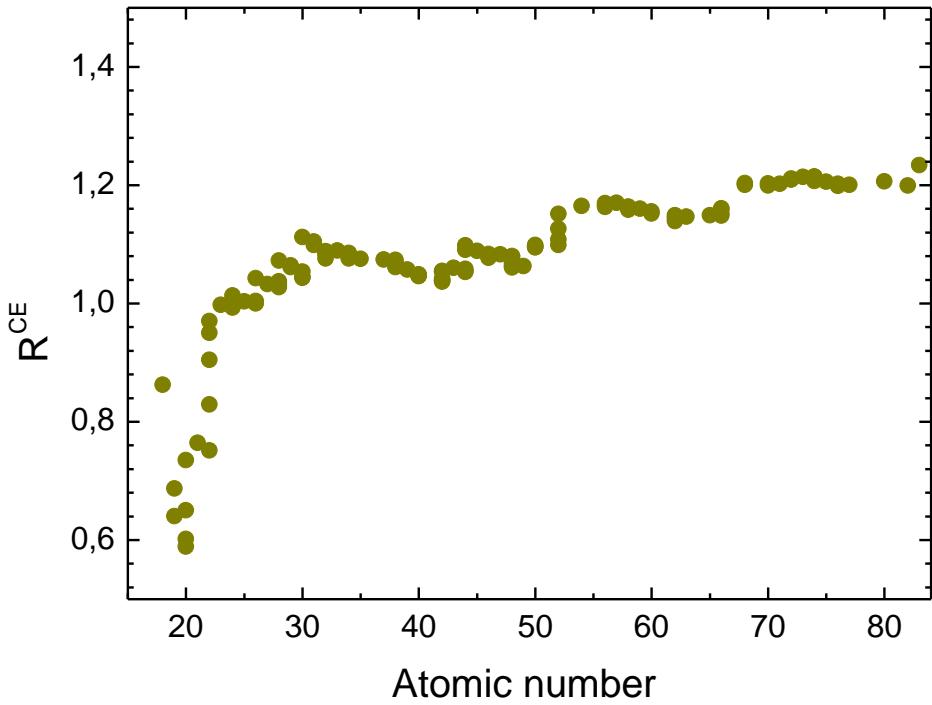


Fig.3 The R^{CE} -factor, Eq.(4) for (n,p) reaction at 14.5 MeV corresponding to results of TALYS calculations obtained for various N values growing with the increase of atomic number of the target.

In contrast to the (n, α) reaction, the deviation of experimental and calculated cross sections has a rather weak correlation (<0.3) with different combinations of shell and pairing corrections, binding energies etc.

The deviation of experimental and calculated cross-sections decreases after a simple correction of calculated values

$$\sigma_{\text{eval}} = \sigma_{\text{calc}} \exp \left(\left[\alpha_1 \frac{A - 2Z}{A} + \alpha_2 \right] Q_n \right), \quad (5)$$

where Z and A are the atomic number and the atomic mass number of the target, Q_n is the separation energy for neutron in the compound nucleus (Z,A+1), the parameter values $\alpha_1 = -0.8209$, and $\alpha_2 = 0.07845$ correspond to target nuclei with $Z \geq 50$.

Table 1 shows the deviation factors, Eq.(1)-(4) corresponding to (n,p) reaction cross-sections calculated using TALYS, σ_{calc} and cross-sections “corrected” using Eq.(5), σ_{eval} . The improvement achieved is moderate. Nevertheless Eq.(5) may be used as an additional information about (n,p) reaction cross sections at 14.5 MeV.

Table 2 presents (n,p) reaction cross-sections for target nuclei with the atomic number between 50 and 84 with the half-life $T_{1/2}$ more than one hour calculated using the TALYS code and Eq.(5).

Table 1. Deviation factors for (n,p) reaction cross-sections at 14.5 MeV for 46 nuclei with atomic number from 50 to 83.

Factor	Cross-sections calculated using TALYS	Cross-sections evaluated using Eq.(5)
H	32.8	14.2
F	1.85	1.80
R^{EC}	0.91	1.39
R^{CE}	1.53	0.98

2.2 (n,α) reaction cross-section

The analysis of deviations of theoretical and experimental cross-sections was performed for 120 targets with atomic number from 18 to 83.

As opposed to the (n,p) reaction, the deviations for (n,α) reaction show definite correlations (up to 0.75) with definite combinations of values relating to neutron interactions with investigated nuclei. The proposed formula for the subsequent improvement of calculated cross-sections is as follows

$$\sigma_{eval} = \sigma_{calc} \exp \left(\left[\beta_1 \frac{A-2Z}{A} + \beta_2 \right] \left[Q_n - Q_p + \delta W_{Z,A} - \delta W_{Z-1,A-3} - \delta_{Z,A} - \delta_{Z-1,A-3} \right] \right), \quad (6)$$

where Z and A are the atomic number and the atomic mass number of the target, Q_n and Q_p are separation energies for neutron and proton in (Z,A+1) nucleus, parameter values $\beta_1 = -1.523$ and $\beta_2 = 0.07503$ correspond to target nuclei with the atomic number from 18 to 83.

Table 3 shows the deviation factors for cross-sections calculated using TALYS and cross-sections improved using Eq.(6). Fig.4 shows the ratio of calculated and corrected cross-sections to experimental ones. In contrast to (n,p) reaction the improvement achieved is essential.

Table 2. (n,p) reaction cross-sections at 14.5 MeV for target nuclei (“Z A”) with the atomic number between 50 and 84 with the half-life more than one hour evaluated using Eq.(5) (“Improved”), calculated using the TALYS code (“TALYS”), and obtained from the analysis of experimental data (“Expr data”).

Z	A	Improved	TALYS	Expr data	Z	A	Improved	TALYS	Expr data
50	110	185.7	180.0		54	131	7.677	13.89	5.94 ± 0.75
50	112	73.62	79.24	21.8 ± 9.4	54	132	3.687	5.776	
50	113	43.85	51.70		54	133	5.431	10.39	
50	114	17.76	21.03		54	134	2.690	4.500	
50	115	24.22	31.85		54	135	3.559	7.118	
50	116	8.577	10.92		54	136	0.302	0.435	
50	117	11.43	16.72	14.5 ± 1.5	55	127	25.76	32.88	
50	118	4.357	5.900	5.93 ± 0.59	55	129	17.49	24.03	
50	119	6.191	9.996	6.98 ± 2.16	55	131	13.41	19.63	
50	120	1.947	2.792		55	132	18.68	31.57	
50	121	3.455	6.075		55	133	9.654	14.96	
50	122	0.745	1.127		55	134	14.11	25.74	
50	123	1.793	3.390		55	135	6.909	11.42	
50	124	0.259	0.410		55	136	10.35	19.82	
50	125	0.878	1.772		55	137	2.068	2.987	
50	126	0.0776	0.128		56	126	140.8	156.4	
50	127	0.323	0.694		56	128	41.39	49.92	
51	117	32.30	39.41		56	129	35.56	48.26	
51	119	19.86	26.07		56	130	20.80	27.08	
51	121	12.43	17.52		56	131	21.08	31.42	
51	122	19.79	32.73		56	132	11.69	16.26	
51	123	8.415	12.54		56	133	13.42	21.78	
51	124	13.99	25.11		56	134	7.796	11.55	
51	125	5.383	8.449		56	135	9.893	17.31	
51	126	10.16	19.52		56	136	5.813	9.196	7.22 ± 0.72
51	127	3.413	5.622		56	137	6.602	12.20	8.28 ± 1.95
51	128	7.200	14.68		56	138	1.186	1.699	2.80 ± 0.28
51	129	2.184	3.728		56	139	1.924	3.239	
52	116	145.5	153.1		56	140	0.533	0.786	
52	117	85.81	98.33		57	132	38.27	53.21	
52	118	54.87	63.31		57	133	21.59	29.22	
52	119	42.68	55.18		57	135	16.20	23.39	
52	120	21.87	27.38		57	137	12.45	19.37	
52	121	25.48	36.63		57	138	16.09	28.30	
52	122	11.40	15.32	14.2 ± 1.4	57	139	4.854	6.937	3.87 ± 0.39
52	123	15.29	24.13		57	140	8.768	14.38	
52	124	6.825	9.729		57	141	2.858	4.291	
52	125	10.16	17.46		57	142	5.799	9.742	
52	126	4.338	6.523	3.48 ± 0.35	58	132	53.35	63.16	
52	127	6.365	11.79		58	133	43.92	57.98	
52	128	2.837	4.490	1.67 ± 0.36	58	134	28.51	36.61	
52	129	4.394	8.663		58	135	25.65	37.11	
52	130	1.607	2.671	0.805 ± 0.467	58	136	16.51	22.65	
52	132	1.086	1.895		58	137	17.63	27.94	
53	120	65.27	78.38		58	138	11.45	16.93	
53	121	39.72	47.76		58	139	11.46	19.43	
53	123	23.56	30.63		58	140	3.027	4.244	7.21 ± 0.72
53	124	28.60	42.18		58	141	4.305	6.964	
53	125	15.49	21.57		58	142	1.924	2.785	4.44 ± 0.46
53	126	21.13	33.94		58	143	2.458	4.168	
53	127	9.677	14.31		58	144	0.809	1.185	
53	129	7.141	11.10		59	137	33.68	44.71	
53	130	12.30	23.03		59	139	21.17	30.41	
53	131	4.959	8.137		59	141	9.196	12.71	9.64 ± 0.96
53	132	8.371	16.64		59	142	14.32	22.31	
53	133	3.191	5.534		59	143	26.50	38.53	
53	135	0.671	0.976		59	145	3.641	5.331	
54	122	71.12	80.62		60	138	38.73	48.79	
54	123	53.42	67.03		60	140	23.26	31.74	
54	124	29.52	36.37		60	141	20.76	31.93	
54	125	27.92	38.94		60	142	7.127	9.606	12.8 ± 1.3
54	126	15.57	20.63		60	143	8.395	12.76	
54	127	17.43	26.69		60	144	4.702	6.580	
54	128	8.974	12.66		60	145	5.235	8.437	
54	129	11.58	19.29		60	146	1.980	2.834	3.56 ± 0.36
54	130	5.773	8.607						

Table 2 continued

60	147	3.117	5.297		66	157	14.33	23.00	
60	148	1.165	1.716		66	158	8.530	12.56	
60	149	2.116	3.855		66	159	9.733	16.42	
60	150	0.677	1.069		66	160	5.307	8.084	7.61 ± 0.97
61	143	16.44	21.64		66	161	6.088	10.75	
61	144	22.32	32.38		66	162	3.768	5.978	3.99 ± 0.40
61	145	11.10	15.34		66	163	3.540	6.417	3.08 ± 0.31
61	146	16.70	25.75		66	164	1.492	2.380	2.48 ± 0.27
61	147	7.033	10.09		66	165	1.853	3.390	
61	148	12.57	20.27		66	166	0.837	1.361	
61	149	5.107	7.573		67	161	10.33	15.56	
61	150	9.221	16.60		67	163	7.334	11.52	
61	151	3.176	5.084		67	165	3.996	6.414	
62	142	62.73	78.19		67	166	5.900	10.55	
62	144	16.13	20.52	23.4 ± 4.6	67	167	2.460	4.016	
62	145	18.04	25.36		68	158	21.85	28.42	
62	146	9.142	12.18		68	160	14.59	20.13	
62	147	10.18	15.29		68	161	16.68	26.20	
62	148	5.502	7.584	11.6 ± 2.2	68	162	10.90	15.74	
62	149	6.408	10.29		68	163	12.33	20.52	
62	150	2.788	3.985	6.39 ± 0.64	68	164	7.617	11.48	
62	151	5.211	9.162		68	165	8.615	15.05	
62	152	2.637	4.042		68	166	4.540	7.119	
62	153	3.996	7.389		68	167	4.740	8.420	1.50 ± 0.45
62	154	1.881	3.018		68	168	2.523	4.027	2.58 ± 0.26
62	156	0.748	1.215		68	169	2.795	5.063	
63	145	26.49	32.67		68	170	1.315	2.140	
63	146	33.04	44.11		68	171	1.493	2.754	
63	147	19.13	24.93		68	172	0.520	0.848	
63	148	25.73	36.80		69	163	18.42	25.99	
63	149	12.38	16.89		69	165	12.62	18.70	
63	150	18.67	28.40		69	166	15.58	26.31	
63	151	8.670	12.46		69	167	8.781	13.61	
63	152	13.93	23.66		69	168	11.61	20.07	
63	153	6.204	9.517	4.96 ± 0.66	69	169	5.333	8.580	
63	154	10.31	18.37		69	170	7.137	12.61	
63	155	4.225	6.803		69	171	3.294	5.423	
63	156	6.726	12.15		69	172	5.078	9.093	
63	157	2.390	3.905		69	173	1.849	3.042	
64	146	39.78	47.01		70	164	17.89	24.31	
64	147	29.30	37.57		70	166	12.51	17.83	
64	148	20.33	25.46		70	168	9.629	14.38	
64	149	18.99	26.27		70	169	10.03	17.00	
64	150	10.88	14.29		70	170	6.597	10.24	
64	151	11.77	17.56		70	171	6.323	11.12	
64	152	6.324	8.706		70	172	4.051	6.500	
64	153	9.629	15.80		70	173	3.737	6.696	
64	154	5.475	8.062		70	174	1.978	3.187	2.86 ± 0.29
64	155	7.345	12.74		70	175	2.189	3.944	
64	156	4.179	6.476		70	176	0.892	1.468	1.76 ± 0.19
64	157	4.787	8.557		70	177	1.011	1.901	
64	158	2.348	3.720		70	178	0.251	0.404	
64	159	2.722	4.999		71	169	15.91	23.37	
64	160	1.105	1.791		71	170	18.23	29.69	
65	147	64.29	73.18		71	171	10.78	16.48	
65	148	50.17	60.85		71	172	13.04	22.19	
65	149	34.59	42.32		71	173	7.711	12.27	
65	150	40.90	53.38		71	174	9.196	16.04	
65	151	22.18	28.65		71	175	4.705	7.605	5.08 ± 4.05
65	152	30.10	42.71		71	176	6.310	11.12	
65	153	15.05	20.54		71	177	3.064	5.079	
65	154	21.17	33.32		71	179	1.648	2.769	
65	155	11.18	16.23		72	170	16.71	23.52	
65	156	15.41	25.68		72	171	16.80	26.68	
65	157	8.163	12.49		72	172	11.63	17.18	
65	158	11.05	19.06		72	173	12.05	19.93	
65	159	5.111	8.052	5.72 ± 0.57	72	174	8.427	12.87	
65	160	7.735	13.83		72	175	8.497	14.68	
65	161	3.184	5.252		72	176	5.212	8.186	
66	152	25.50	31.45		72	177	4.973	8.783	
66	153	23.48	32.30		72	178	3.180	5.128	2.54 ± 0.25
66	154	13.35	17.41		72	179	3.046	5.586	
66	155	18.83	28.36		72	180	1.696	2.764	1.94 ± 0.38

Table 2 continued

72 181	1.678	3.059	78 195	2.176	4.291	
72 182	0.767	1.256	78 196	0.934	1.572	
72 183	0.914	1.677	78 197	1.173	2.358	
72 184	0.323	0.527	78 198	0.453	0.770	
73 173	19.08	27.58	78 200	0.174	0.296	
73 174	21.32	34.08	78 202	0.0563	0.0970	
73 175	12.94	19.40	79 175	223.2	225.8	
73 176	14.73	24.73	79 191	9.117	14.24	
73 177	8.579	13.51	79 192	13.88	24.85	
73 179	5.542	8.997	79 193	6.421	10.42	
73 180	7.525	13.45	79 194	10.05	18.72	
73 181	3.330	5.419	3.55 ± 0.35	79 195	4.231	7.070
73 182	4.733	8.470		79 196	6.926	13.29
73 183	2.091	3.418		79 197	2.440	4.218
73 184	3.437	6.285		79 198	4.505	8.740
74 176	12.44	18.05		79 199	1.487	2.613
74 177	12.82	20.97		80 192	10.26	15.55
74 178	9.088	13.79		80 193	11.15	19.69
74 180	5.954	9.350		80 194	6.596	10.35
74 181	6.138	10.90		80 195	7.571	13.98
74 182	3.293	5.236	4.36 ± 0.44	80 196	4.164	6.803
74 183	3.356	6.006	4.81 ± 0.48	80 197	4.669	8.877
74 184	1.567	2.514	2.96 ± 0.30	80 198	2.660	4.506
74 185	2.004	3.712		80 199	2.853	5.531
74 186	0.750	1.222	1.64 ± 0.16	80 200	1.561	2.663
74 187	1.057	1.992		80 201	1.806	3.602
74 188	0.264	0.429		80 202	0.898	1.561
75 181	10.44	16.13		80 203	1.050	2.147
75 182	13.08	22.80		80 204	0.366	0.641
75 183	6.514	10.23		81 195	13.04	20.41
75 184	8.256	14.48		81 196	16.89	29.86
75 185	4.013	6.453		81 197	9.373	15.25
75 186	6.184	11.18		81 198	12.19	22.48
75 187	2.580	4.224	4.08 ± 0.45	81 199	7.064	11.93
75 188	4.313	7.980		81 200	8.953	16.91
75 189	1.358	2.286		81 201	4.202	7.328
76 181	17.18	27.89		81 202	6.157	11.91
76 182	11.73	17.60		81 203	2.546	4.554
76 183	12.40	20.96		81 204	4.107	8.135
76 184	7.625	11.68		81 205	1.350	2.484
76 185	7.840	13.75		82 198	12.41	19.53
76 186	4.472	7.016		82 199	12.03	21.91
76 187	4.670	8.517		82 200	8.627	14.09
76 188	2.453	3.910	4.95 ± 0.56	82 201	8.063	15.23
76 189	2.833	5.378	6.83 ± 2.39	82 202	5.423	9.173
76 190	1.269	2.079		82 203	5.275	10.26
76 191	1.541	3.023		82 204	3.407	5.937
76 192	0.436	0.732		82 205	3.292	6.585
76 193	0.704	1.394		82 206	1.975	3.596
76 194	0.185	0.308		82 207	1.569	3.092
77 184	20.51	33.39		82 208	0.215	0.313
77 185	13.58	20.43		82 209	0.343	0.572
77 186	17.02	28.93		82 210	0.0943	0.139
77 187	8.930	14.10		82 212	0.0430	0.0641
77 188	11.19	19.83		83 201	17.68	28.48
77 189	5.817	9.296		83 202	20.41	37.23
77 190	8.337	15.48		83 203	13.78	22.99
77 191	3.912	6.446		83 204	15.90	29.91
77 192	6.032	11.59		83 205	10.43	18.02
77 193	2.315	3.935	2.89 ± 0.77	83 206	12.69	24.44
77 194	4.299	8.291		83 207	8.845	15.79
77 195	1.245	2.153		83 208	9.914	19.02
78 185	22.43	35.69		83 209	2.836	4.300
78 186	14.48	21.00		83 210	4.637	7.499
78 187	14.28	24.29		83 212	3.569	5.983
78 188	9.569	14.45		84 204	15.17	24.54
78 189	9.895	17.64		84 205	14.28	26.28
78 190	5.208	8.098		84 206	10.73	17.93
78 191	6.180	11.53		84 207	10.63	20.16
78 192	3.045	4.885		84 208	8.384	14.58
78 193	3.896	7.533		84 209	7.580	14.27
78 194	1.944	3.214		84 210	3.245	4.794

Table 3. Deviation factors for (n,α) reaction cross-sections at 14.5 MeV for 120 nuclei with atomic number from 18 to 83.

Factor	Cross-sections calculated using TALYS	Cross-sections evaluated using Eq.(6)
H	25.6	12.5
F	2.89	1.66
R^{EC}	3.03	1.33
R^{CE}	0.75	0.95

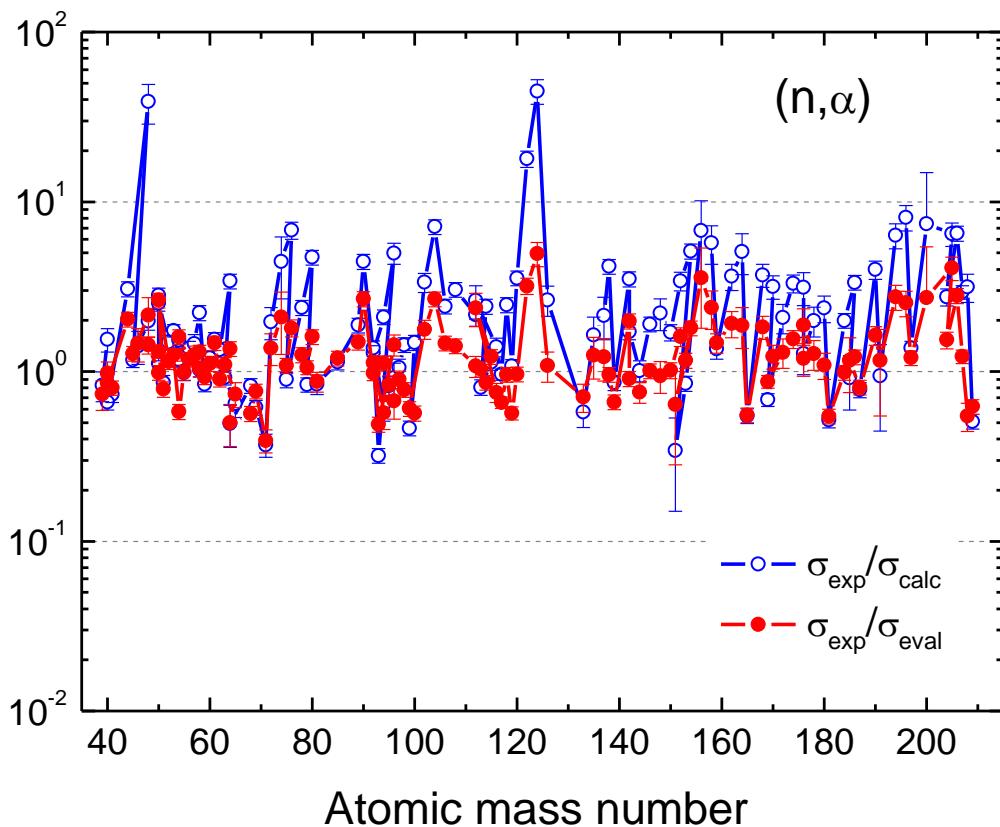


Fig.4 The ratio of experimental (n,α) reaction cross-sections for 120 target nuclei irradiated with 4.5 MeV neutrons to cross-sections calculated with TALYS and cross-sections evaluated using Eq.(6).

Observed improvement is a result of the use of the set of values in Eq.(6), which full explanation seems rather complicated. With some fantasy one can detect quantities relating to “coalescence” of α -particle from proton and “pre-formed” triton. One thing is clear – the formula Eq.(6) compensates in some way the shortcomings of the theory describing the non-equilibrium emission of α -particles, global parameterizations and nuclear model parameter systematics used for calculations.

Table 4 shows (n,α) reaction cross-sections for target nuclei with the atomic number between 18 and 84 with the half-life $T_{1/2}$ more than one hour calculated using the TALYS code, values improved using Eq.(6), and data obtained in Ref.[3] from the analysis of experimental data.

3. Conclusion

The simple approach is proposed for the improvement of calculated cross-sections. The idea concerns the search of correlations between deviations of measured and calculated reaction cross-section, and nuclear quantities relating to reactions investigated. The obtained information is used subsequently for correction of calculated values.

The approach was applied for improvement of (n,p) and (n,α) reaction cross-sections at 14.5 MeV calculated using the TAYLS code. The new evaluated cross-sections are given in Table 2 and Table 4.

Table 4. (n,α) reaction cross-sections at 14.5 MeV for target nuclei (“Z A”) with the atomic number between 18 and 84 with the half-life more than one hour evaluated using Eq.(6) (“Improved”), calculated using the TALYS code (“TALYS”), and obtained from the analysis of experimental data (“Expr data”).

Z	A	Improved	TALYS	Expr data	Z	A	Improved	TALYS	Expr data
18	36	175.6	203.5		27	60	15.35	19.11	
18	37	121.6	116.0		27	61	8.732	8.260	
18	38	60.39	59.07		28	56	87.93	100.1	
18	39	46.11	43.14		28	57	119.8	109.1	
18	40	11.01	6.995	10.8 ± 1.7	28	58	104.9	105.9	$109. \pm 11.$
18	41	10.38	6.242		28	59	93.37	93.72	
18	42	2.820	0.663		28	60	56.36	52.32	62.8 ± 6.3
19	39	176.4	157.0	$130. \pm 26.$	28	61	30.17	28.69	44.4 ± 4.2
19	40	150.5	151.4		28	62	25.99	17.38	23.4 ± 2.3
19	41	41.54	45.61	33.3 ± 3.3	28	63	9.254	6.578	
19	42	40.16	49.44		28	64	2.766	1.106	3.77 ± 0.38
19	43	12.41	10.89		28	65	2.217	0.929	
20	40	149.6	193.8	$128. \pm 13.$	28	66	0.297	0.0553	
20	41	144.2	137.8		29	61	124.8	124.6	
20	42	59.18	59.47		29	63	40.46	48.05	44.4 ± 4.4
20	43	45.67	44.21		29	64	26.89	37.70	
20	44	13.64	9.033	27.7 ± 2.8	29	65	11.80	13.47	8.69 ± 1.48
20	45	8.990	5.399		29	67	3.365	3.232	
20	46	2.800	0.797		30	62	150.7	139.9	
20	47	1.345	0.319		30	64	72.87	73.58	36.4 ± 10.1
20	48	0.580	0.0321	1.25 ± 0.33	30	65	54.11	61.06	
21	43	220.7	159.2		30	66	28.27	25.36	
21	44	108.0	103.3		30	67	25.01	26.88	
21	45	44.26	48.20	56.4 ± 5.6	30	68	15.96	10.93	9.02 ± 0.90
21	46	29.15	35.54		30	70	6.706	2.896	
21	47	11.87	11.93		30	72	1.114	0.251	
21	48	3.360	3.555		31	66	98.15	114.5	
22	44	119.5	127.3		31	67	70.95	86.02	
22	45	122.8	112.1		31	68	51.91	75.05	
22	46	52.29	54.15	76.5 ± 16.9	31	69	26.37	32.85	20.2 ± 2.0
22	47	66.21	63.33		31	71	12.91	13.71	5.06 ± 0.78
22	48	23.73	17.16	34.0 ± 3.9	31	72	10.49	14.86	
22	49	10.49	7.517		31	73	3.649	2.968	
22	50	8.762	3.061	8.63 ± 0.86	32	66	115.5	105.9	
23	48	86.54	81.51		32	68	79.11	80.03	
23	49	43.97	46.26		32	69	75.66	85.42	
23	50	29.10	34.09	38.0 ± 1.5	32	70	31.76	29.81	
23	51	20.96	19.16	16.5 ± 1.7	32	71	28.46	31.25	
24	48	78.32	88.35		32	72	12.65	8.883	17.4 ± 3.7
24	50	37.89	39.52	99.7 ± 10.0	32	73	13.21	12.08	
24	51	44.96	44.63		32	74	3.762	1.776	7.89 ± 3.14
24	52	31.66	24.34	36.2 ± 3.6	32	75	5.803	3.201	
24	53	35.29	25.39	44.2 ± 3.7	32	76	1.398	0.371	2.52 ± 0.29
24	54	20.30	10.02	11.8 ± 1.2	32	77	1.703	0.551	
25	52	106.5	96.64		32	78	0.204	0.0307	
25	53	65.00	66.58		33	71	85.46	103.3	
25	54	41.05	45.51		33	72	65.18	96.80	
25	55	24.27	24.40	24.0 ± 2.4	33	73	34.36	45.64	
25	56	12.80	14.35		33	74	25.17	40.53	
26	51	229.5	129.8		33	75	9.860	11.95	10.7 ± 1.1
26	52	89.24	94.63		33	76	10.01	14.67	
26	54	56.95	59.61	91.1 ± 9.1	33	77	4.511	4.300	
26	55	64.02	63.58		33	78	3.402	3.804	
26	56	37.27	32.09	43.9 ± 4.4	34	72	76.26	76.64	
26	57	24.75	21.24	31.0 ± 4.0	34	73	96.96	106.9	
26	58	15.25	8.932	19.8 ± 2.0	34	74	40.99	38.04	
26	59	5.680	3.352		34	75	39.69	41.60	
26	60	2.139	0.692		34	76	13.89	10.04	
27	55	155.4	123.6		34	77	18.07	15.85	
27	56	151.8	134.3		34	78	6.230	3.282	7.81 ± 0.78
27	57	108.4	110.5		34	79	9.170	5.832	
27	58	62.73	73.68		34	80	2.052	0.699	3.29 ± 0.33
27	59	33.89	37.31	31.4 ± 3.1	34	82	0.585	0.101	
					35	75	77.52	92.12	

Table 4 continued

35	76	53.91	74.71			42	96	11.86	8.695	7.98 ± 1.77
35	77	33.08	43.49			42	97	9.356	7.957	8.41 ± 0.99
35	79	11.82	14.94	12.5 ± 1.2		42	98	7.705	4.195	6.02 ± 0.60
35	81	5.136	5.319	4.48 ± 0.59		42	99	8.300	5.583	
35	82	3.938	4.616			42	100	5.044	1.931	2.86 ± 0.29
35	83	1.944	1.273			43	93	44.95	51.29	
36	76	65.51	65.75			43	94	67.40	91.34	
36	77	84.87	90.29			43	95	38.24	55.81	
36	78	39.82	36.99			43	96	22.85	39.92	
36	79	44.95	48.22			43	97	15.86	23.41	
36	80	14.93	11.59			43	98	12.00	21.40	
36	81	17.27	15.90			43	99	10.02	13.06	6.06 ± 0.61
36	82	5.356	3.147			44	95	71.05	74.65	
36	83	7.759	5.630			44	96	48.70	49.39	
36	84	4.282	1.615			44	97	36.48	41.26	
36	85	2.586	1.211			44	98	22.92	20.26	
36	86	0.434	0.0762			44	99	18.36	18.56	
36	87	2.227	0.492			44	100	9.786	6.914	
36	88	0.679	0.120			44	101	10.18	8.621	
37	81	33.09	43.52			44	102	3.641	1.926	6.46 ± 0.82
37	83	12.84	16.84			44	103	4.790	3.297	
37	84	10.72	15.78			44	104	1.167	0.438	3.12 ± 0.31
37	85	4.982	5.255	5.97 ± 0.60		44	105	2.049	1.033	
37	86	5.199	5.432			44	106	0.633	0.162	
37	87	1.443	0.811			45	99	32.59	45.95	
38	80	71.50	71.59			45	100	25.51	43.05	
38	82	35.42	34.06			45	101	14.47	20.28	
38	83	44.88	48.02			45	102	12.30	21.33	
38	84	16.10	13.26			45	103	6.907	9.088	
38	85	18.28	17.05			45	105	2.850	3.214	
38	86	4.736	2.995			46	100	47.11	48.48	
38	87	6.233	4.421			46	101	42.15	48.57	
38	88	3.333	1.034			46	102	21.14	19.41	
38	89	6.968	2.903			46	103	22.87	24.43	
38	90	2.477	0.919			46	104	9.134	7.071	
38	91	1.888	0.738			46	105	10.56	9.924	
38	92	1.097	0.249			46	106	3.595	2.180	5.28 ± 0.53
39	85	33.57	43.66			46	107	5.729	4.550	
39	86	24.73	37.45			46	108	1.932	0.898	2.73 ± 0.27
39	87	12.20	15.22			46	109	3.055	1.893	
39	88	8.144	11.29			46	110	0.869	0.294	
39	89	4.210	3.346	6.27 ± 0.63		46	112	0.297	0.0684	
39	90	14.56	15.04			47	103	40.31	56.64	
39	91	4.949	5.758			47	104	31.92	52.94	
39	92	2.824	3.529			47	105	17.16	25.01	
39	93	2.629	2.360			47	107	7.217	9.774	
40	86	36.90	36.22			47	109	3.920	4.783	
40	87	43.12	46.82			47	111	2.295	2.341	
40	88	14.53	12.88			47	112	2.261	2.988	
40	89	16.17	16.38			47	113	1.132	0.878	
40	90	5.104	3.076	13.7 ± 1.4		48	106	24.90	24.42	
40	91	19.88	14.74			48	107	22.77	25.82	
40	92	9.522	7.229	9.32 ± 0.93		48	108	11.78	9.711	
40	93	6.941	5.580			48	109	12.43	12.71	
40	94	4.125	2.213	4.63 ± 0.46		48	110	4.590	3.036	
40	95	2.799	1.504			48	111	6.322	5.178	
40	96	1.615	0.465	2.32 ± 0.33		48	112	2.361	1.179	2.54 ± 0.36
40	97	1.358	0.411			48	113	3.477	2.259	
41	89	34.60	43.81			48	114	1.032	0.367	0.889 ± 0.089
41	90	29.99	43.51			48	115	1.737	0.839	
41	91	19.77	21.87			48	116	0.309	0.0755	
41	92	38.57	51.74			48	117	0.759	0.254	
41	93	18.12	27.69	8.85 ± 0.89		49	109	22.44	32.71	
41	94	11.82	20.84			49	110	18.78	33.34	
41	95	9.616	13.71			49	111	9.269	13.19	
41	96	5.358	8.640			49	113	4.298	5.508	4.45 ± 0.47
41	97	4.892	5.477			49	115	1.953	2.112	2.39 ± 0.24
42	90	34.63	34.56			50	110	50.20	51.72	
42	92	22.77	18.71	25.7 ± 2.6		50	112	18.99	17.12	44.9 ± 10.0
42	93	55.17	51.65			50	113	15.53	16.52	
42	94	22.78	20.42	13.0 ± 2.6		50	114	6.601	4.763	
42	95	15.48	15.68	12.9 ± 1.7		50	115	7.487	6.225	

Table 4 continued

50	116	2.495	1.346	1.88 ± 0.24	55	136	1.394	1.644
50	117	3.725	2.550	2.45 ± 0.19	55	137	1.522	0.721
50	118	1.229	0.478	1.18 ± 0.12	56	126	23.53	25.69
50	119	1.755	0.926	0.999± 0.087	56	128	13.59	13.24
50	120	0.467	0.127	0.450± 0.045	56	129	17.91	23.20
50	121	0.821	0.305		56	130	8.012	6.800
50	122	0.0693	0.0123	0.221± 0.024	56	131	11.04	12.13
50	123	0.190	0.0472		56	132	4.776	3.318
50	124	0.0160	0.00176	0.079± 0.013	56	133	6.646	6.216
50	125	0.0349	0.00540		56	134	3.268	1.818
51	117	6.742	12.08		56	135	4.483	3.406 5.58 ± 1.53
51	119	3.283	5.378		56	136	2.024	0.931
51	121	1.500	2.136		56	137	2.429	1.386 2.96 ± 0.83
51	122	1.717	3.271		56	138	2.418	0.558 2.32 ± 0.23
51	123	0.668	0.757		56	139	6.488	2.830
51	124	0.775	1.208		56	140	1.911	0.761
51	125	0.243	0.210		57	132	11.83	27.42
51	126	0.313	0.378		57	133	6.891	12.12
51	127	0.0779	0.0501		57	135	4.006	6.345
51	128	0.116	0.106		57	137	2.456	3.507
51	129	0.0228	0.0107		57	138	2.509	4.054
52	116	50.03	60.17		57	139	2.993	2.306 1.98 ± 0.20
52	117	45.65	68.22		57	140	5.547	7.717
52	118	26.00	28.08		57	141	1.854	2.434
52	119	27.81	38.87		57	142	1.470	2.176
52	120	12.26	10.89		58	132	16.33	17.23
52	121	16.28	18.92		58	133	21.95	29.60
52	122	6.105	4.259		58	134	9.682	8.927
52	123	8.996	8.380		58	135	12.63	14.58
52	124	3.082	1.635		58	136	5.937	4.584
52	125	5.035	3.852		58	137	7.586	7.742
52	126	1.734	0.711	1.88 ± 0.38	58	138	3.627	2.386
52	127	2.910	1.753		58	139	4.404	3.506
52	128	0.930	0.292		58	140	3.583	1.294
52	129	1.588	0.736		58	141	9.619	6.136
52	130	0.505	0.118		58	142	3.016	1.700 5.97 ± 0.60
52	132	0.351	0.0632		58	143	2.883	1.956
53	120	32.34	75.04		58	144	1.809	0.702
53	121	17.03	29.39		59	137	7.978	14.43
53	123	7.846	12.36		59	139	4.582	7.920
53	124	8.378	17.07		59	141	4.260	4.583
53	125	4.314	5.940		59	142	7.597	13.70
53	126	4.933	9.061		59	143	31.07	52.67
53	127	2.512	2.962		59	145	2.293	3.036
53	129	1.606	1.572		60	138	12.55	12.47
53	130	2.019	2.738		60	140	7.430	6.449
53	131	1.021	0.809		60	141	7.915	8.209
53	132	1.289	1.375		60	142	6.145	3.258 5.58 ± 0.56
53	133	0.607	0.372		60	143	13.61	11.43
53	135	0.783	0.199		60	144	5.359	4.002 4.05 ± 0.57
54	122	19.55	19.82		60	145	5.169	4.732
54	123	26.30	32.85		60	146	3.389	1.797 3.42 ± 0.34
54	124	10.46	9.186		60	147	3.459	2.632
54	125	14.09	16.06		60	148	1.654	0.707 1.56 ± 0.33
54	126	5.885	4.340		60	149	1.975	1.145
54	127	8.175	7.987		60	150	0.628	0.193
54	128	3.490	2.090		61	143	6.809	9.055
54	129	5.179	4.264		61	144	11.41	23.40
54	130	2.169	1.022		61	145	4.887	9.778
54	131	3.092	2.085		61	146	4.281	10.68
54	132	1.324	0.486		61	147	3.651	6.211
54	133	1.856	0.965		61	148	2.861	6.268
54	134	0.896	0.267		61	149	1.877	2.824
54	135	1.017	0.390		61	150	1.646	3.346
54	136	0.882	0.120		61	151	0.887	0.935
55	127	8.711	14.74		62	142	12.77	13.48
55	129	5.272	8.383		62	144	10.39	7.384
55	131	3.245	4.647		62	145	26.97	28.82
55	132	3.572	6.789		62	146	8.518	8.054
55	133	2.017	2.477	1.43 ± 0.27	62	147	8.585	10.13
55	134	2.310	3.671		62	148	5.419	4.133
55	135	1.258	1.260		62	149	6.011	6.114

Table 4 continued

62 150	3.069	1.833	3.12 ± 0.34	68 162	3.792	3.216
62 151	3.246	3.076		68 163	4.452	4.988
62 152	1.128	0.529	1.81 ± 0.23	68 164	2.375	1.769
62 153	1.362	0.808		68 165	2.639	2.594
62 154	0.461	0.163	0.833± 0.083	68 166	1.596	0.970
62 156	0.345	0.0882		68 167	1.602	1.175
63 145	13.23	20.19		68 168	0.907	0.448
63 146	18.91	41.40		68 169	0.783	0.467
63 147	8.900	19.74		68 170	0.499	0.194
63 148	7.215	19.89		68 171	0.454	0.205
63 149	5.558	11.30		68 172	0.303	0.0841
63 150	4.862	12.91		69 163	4.640	9.177
63 151	3.542	6.641	2.27 ± 1.27	69 165	3.411	6.057
63 152	2.657	6.655		69 166	3.394	7.709
63 153	1.343	1.830	1.56 ± 0.16	69 167	2.377	3.634
63 154	1.590	2.466		69 168	2.288	4.037
63 155	0.964	0.932		69 169	1.722	2.202
63 156	0.968	1.007		69 170	1.300	1.834
63 157	0.826	0.597		69 171	1.032	1.037
64 146	18.41	16.16		69 172	0.701	0.753
64 147	33.65	42.69		69 173	0.588	0.448
64 148	13.77	15.92		70 164	7.180	7.380
64 149	14.53	20.65		70 166	4.678	4.389
64 150	9.331	9.182		70 168	3.008	2.538
64 151	9.682	12.30		70 169	3.589	3.781
64 152	5.099	4.144		70 170	2.342	1.781
64 153	5.360	6.496		70 171	2.106	1.940
64 154	1.960	1.262		70 172	1.296	0.808
64 155	2.808	2.347		70 173	1.058	0.758
64 156	1.074	0.567	3.84 ± 1.91	70 174	0.745	0.351
64 157	1.504	0.963		70 175	0.632	0.368
64 158	0.773	0.321	1.84 ± 0.47	70 176	0.457	0.174
64 159	0.822	0.433		70 177	0.342	0.149
64 160	0.426	0.138		70 178	0.178	0.0416
65 147	28.47	49.86		71 169	3.862	7.524
65 148	37.36	89.06		71 170	4.233	9.833
65 149	16.70	42.48		71 171	3.149	5.641
65 150	13.68	39.88		71 172	2.715	5.831
65 151	10.26	25.03		71 173	2.299	3.633
65 152	8.775	26.39		71 174	1.753	3.101
65 153	5.687	12.40		71 175	1.672	2.159
65 154	4.358	12.52		71 176	1.185	1.750
65 155	2.388	4.040		71 177	1.044	1.192
65 156	2.946	5.944		71 179	0.490	0.403
65 157	1.742	2.344		72 170	5.588	5.902
65 158	1.992	3.116		72 171	6.755	9.357
65 159	1.505	1.637	2.22 ± 0.29	72 172	4.367	4.254
65 160	1.306	1.745		72 173	4.126	5.025
65 161	0.921	0.821		72 174	2.872	2.538
66 152	17.89	20.77		72 175	2.977	3.266
66 153	17.28	26.58		72 176	2.181	1.630
66 154	8.985	8.907		72 177	2.039	1.857
66 155	9.126	13.26		72 178	1.464	0.933
66 156	4.048	3.474		72 179	1.039	0.781
66 157	5.195	5.789		72 180	0.778	0.359
66 158	2.389	1.794		72 181	0.755	0.407
66 159	3.197	2.994		72 182	0.438	0.159
66 160	1.776	1.102		72 183	0.316	0.140
66 161	1.964	1.601		72 184	0.198	0.0560
66 162	1.006	0.530	1.93 ± 0.34	73 173	5.303	11.74
66 163	1.035	0.624		73 174	5.075	13.39
66 164	0.593	0.218	1.11 ± 0.30	73 175	3.817	7.592
66 165	0.527	0.254		73 176	3.431	8.582
66 166	0.272	0.0839		73 177	3.043	5.317
67 161	2.848	4.480		73 179	1.981	2.847
67 163	1.763	2.383		73 180	1.288	2.033
67 165	1.380	1.394	0.763± 0.076	73 181	1.181	1.244
67 166	0.970	1.152		73 182	0.869	1.053
67 167	0.668	0.560		73 183	0.868	0.792
68 158	7.412	7.860		73 184	0.506	0.541
68 160	6.025	5.703		74 176	5.531	5.687
68 161	6.676	8.396		74 177	5.255	6.994

Table 4 continued

74 178	3.347	3.157		79 193	1.135	1.638	
74 180	2.065	1.595		79 194	1.093	1.948	
74 181	1.682	1.599		79 195	0.572	0.653	
74 182	1.140	0.666		79 196	0.572	0.786	
74 183	1.113	0.814		79 197	0.309	0.272	0.373± 0.037
74 184	0.799	0.396	0.789± 0.079	79 198	0.245	0.245	
74 185	0.626	0.391		79 199	0.140	0.0922	
74 186	0.445	0.162	0.542± 0.054	80 192	2.521	2.184	
74 187	0.308	0.138		80 193	3.223	3.835	
74 188	0.169	0.0415		80 194	1.253	0.912	
75 181	2.796	4.965		80 195	1.746	1.730	
75 182	2.107	4.579		80 196	0.769	0.454	
75 183	1.756	2.453		80 197	0.944	0.721	
75 184	1.538	2.695		80 198	0.339	0.163	
75 185	1.211	1.537	1.41 ± 0.50	80 199	0.408	0.231	
75 186	0.893	1.405		80 200	0.170	0.0620	0.461± 0.461
75 187	0.655	0.678	0.529± 0.053	80 201	0.189	0.0897	
75 188	0.503	0.624		80 202	0.0687	0.0199	
75 189	0.347	0.274		80 203	0.0862	0.0313	
76 181	5.978	9.142		80 204	0.0306	0.00616	
76 182	3.921	4.031		81 195	1.919	3.667	
76 183	3.643	4.853		81 196	1.860	4.485	
76 184	2.450	2.182		81 197	1.192	2.028	
76 185	2.653	3.057		81 198	1.160	2.379	
76 186	1.592	1.228		81 199	0.676	0.977	
76 187	1.323	1.297		81 200	0.612	1.022	
76 188	0.850	0.483		81 201	0.445	0.512	
76 189	0.840	0.627		81 202	0.334	0.441	
76 190	0.415	0.170	0.678± 0.085	81 203	0.249	0.221	
76 191	0.383	0.198		81 204	0.156	0.150	
76 192	0.125	0.0317		81 205	0.127	0.0801	0.519± 0.082
76 193	0.136	0.0452		82 198	2.371	2.411	
76 194	0.0507	0.00885		82 199	2.755	3.714	
77 184	5.454	15.43		82 200	1.545	1.335	
77 185	3.765	7.838		82 201	1.566	1.719	
77 186	4.073	11.49		82 202	1.206	0.859	
77 187	2.692	5.325		82 203	0.869	0.761	
77 188	2.021	4.787		82 204	0.470	0.263	0.722± 0.082
77 189	1.451	2.219		82 205	0.406	0.274	
77 190	1.150	2.335		82 206	0.199	0.0853	0.556± 0.056
77 191	0.713	0.877	0.828± 0.437	82 207	0.299	0.125	0.366± 0.033
77 192	0.559	0.868		82 208	0.722	0.125	0.395± 0.075
77 193	0.321	0.300		82 209	0.467	0.190	
77 194	0.227	0.249		82 210	0.194	0.0796	
77 195	0.123	0.0866		82 212	0.111	0.0350	
78 185	9.764	16.77		83 201	2.903	7.515	
78 186	6.285	7.262		83 202	2.914	9.715	
78 187	6.969	11.64		83 203	1.893	4.572	
78 188	3.608	3.634		83 204	1.550	4.752	
78 189	3.776	5.107		83 205	1.239	2.800	
78 190	1.964	1.458		83 206	0.912	2.551	
78 191	2.084	2.268		83 207	0.745	1.660	
78 192	0.916	0.529		83 208	0.579	1.400	
78 193	1.075	0.853		83 209	0.949	1.160	0.590± 0.059
78 194	0.433	0.187	1.19 ± 0.20	83 210	1.344	3.154	
78 195	0.591	0.325		83 212	0.408	1.360	
78 196	0.220	0.0691	0.560± 0.096	84 204	5.274	7.198	
78 197	0.266	0.108		84 205	6.624	11.91	
78 198	0.0817	0.0183		84 206	3.617	4.678	
78 200	0.0330	0.00512		84 207	4.035	6.725	
78 202	0.0126	0.00138		84 208	2.714	3.324	
79 175	63.19	139.4		84 209	2.781	3.821	
79 191	2.366	4.083		84 210	4.631	3.471	
79 192	2.084	4.659					

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