

[Extended Abstract]

# Stability investigations of an elastic rotor supported by actively deformed journal bearings considering the associated spectral system

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#### Introduction

Due to the non-linear fluid-solid interaction within journal bearings instability phenomena (often referred to as 'oil-whirl' and/or 'oil-whip') can be observed at higher revolution speeds, which can lead to unwanted oscillations of the corresponding rotor-dynamic system. To improve this behaviour, various methods which are based on the idea of non-circular bearing geometries have been proposed in literature. E.g. in [1] first approaches of a simple two-lobe bearing with an actively controlled change in geometry are investigated in order to suppress the above mentioned instability phenomena. In the present work a more elaborated model of a journal bearing with modifiable geometry is developed. Afterwards, this bearing is implemented in an elastic Jeffcott rotor and the associated spectral system is derived and analysed.

# 1. Modelling of the Jeffcott rotor in actively deformed journal bearings

# 1.1 Geometry of the deformed bearing

As depicted in figure 1 the initially circular bearing of inner radius  $R_0$  is deformed by two oscillating vertical forces  $F(\tau) = \widehat{F}(1-\delta_F\cos((\Omega/\omega)\tau))$  with given dimensionless time  $\tau = \omega t$ . The bearing is modelled as thin, circular beam with middle radius R and Young's modulus E. The rectangular cross-section is characterized by its width  $B \ll R$  and its height  $A \ll R$ . It is assumed that the deformation is not influenced by the fluid pressure at all and that inertia terms can be neglected. Using the classical bending theory for curved beams (cf. [2]), the radial deflection  $w(\varphi,\tau)$  from the undeformed state can be calculated.

A normalisation on the initial bearing clearance  $C = R_0 - R_W = (R - A/2) - R_W$  leads to:

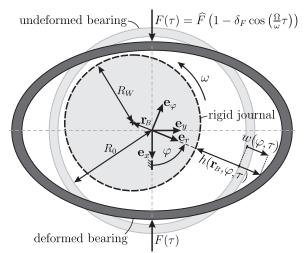


Figure 1. deformed journal bearing

$$W(\varphi,\tau) = \frac{w(\varphi,\tau)}{C} = \frac{3R^3}{CBA^3} \frac{F(\tau)}{E} \begin{cases} \frac{4}{\pi} - \sin\varphi + \left(\varphi - \frac{1}{2}\pi\right)\cos\varphi & 0 \le \varphi < \pi\\ \frac{4}{\pi} + \sin\varphi + \left(\frac{3}{2}\pi - \varphi\right)\cos\varphi & \pi \le \varphi \le 2\pi \end{cases} \tag{1}$$

# 1.2 Pressure distribution

With the deflection from equation (1) and the depicted kinematic relations in figure 1 the non-dimensional pressure  $\Pi(\varphi, \overline{z})$  can be modelled according to the non-dimensional Reynolds equation:

$$\frac{\partial}{\partial \varphi} \left( \frac{\partial \Pi}{\partial \varphi} H^3 \right) + \gamma^2 \frac{\partial}{\partial \overline{z}} \left( \frac{\partial \Pi}{\partial \overline{z}} H^3 \right) = 6 \frac{\partial H}{\partial \varphi} + 12 \frac{\partial H}{\partial \tau} \quad \text{with} \quad H = \frac{h}{C} = 1 + W - X_B \cos \varphi - Y_B \sin \varphi, \quad (2)$$

with the boundary conditions  $\Pi(\overline{z}=\pm 1)=0$ ,  $\Pi(\varphi=0)=\Pi(\varphi=2\pi)$  and  $\partial^{\Pi}/\partial\varphi|_{\varphi=0}=\partial^{\Pi}/\partial\varphi|_{\varphi=2\pi}$ . The normalised journal coordinates are given by  $^{\mathrm{r}_B}/C=X_B\mathbf{e}_x+Y_B\mathbf{e}_y$ . Assuming a rather short bearing  $(2R_0/B=\gamma\gg 1)$  the Galerkin approach  $\Pi=(1-\overline{z}^2)g(\varphi)$  is used to reduce the Reynolds equation (2) to a one-dimensional problem in  $\varphi\in[0,2\pi]$ , which is solved by using a finite-difference scheme.

## 1.3 Bearing forces

With the semi-discrete pressure values  $\Pi_i(\overline{z}) = (1 - \overline{z}^2)g(\varphi_i)$  for i = 1..N the non-dimensional bearing forces  $f_x$  and  $f_y$  are calculated. After integrating along the axial coordinate  $\overline{z}$  the circumferential integration in  $\varphi$  is performed by means of the trapezoidal rule whereby negative pressure values are neglected.

### 1.4 Equations of motion

Having derived the bearing forces, the equations of motion of the Jeffcott rotor (cf. [3]) are given by:

$$\overline{\omega}^{2}X_{R}^{\prime\prime\prime} + \overline{d}_{a}\overline{\omega}X_{R}^{\prime} + \frac{X_{R} - X_{B}}{\Gamma} = f, \quad \eta \overline{\omega}^{2}X_{B}^{\prime\prime\prime} + \frac{X_{B} - X_{R}}{\Gamma} - \sigma \overline{\omega}f_{x} = 0,$$

$$\overline{\omega}^{2}Y_{R}^{\prime\prime\prime} + \overline{d}_{a}\overline{\omega}Y_{R}^{\prime\prime} + \frac{Y_{R} - Y_{B}}{\Gamma} = 0, \quad \eta \overline{\omega}^{2}Y_{B}^{\prime\prime\prime} + \frac{Y_{B} - Y_{R}}{\Gamma} - \sigma \overline{\omega}f_{y} = 0,$$
(3)

with the dimensionless parameters  $\overline{d}_a$  for damping,  $\eta$  for the masses allocated at the bearing seats,  $\overline{\omega}$  for the revolution speed,  $\Gamma$  for the shaft compliance,  $\sigma$  for the bearing characteristic and f for a vertically acting external load.  $X_R$  and  $Y_R$  thereby describe the centre coordinates of the rotor and  $(.)' = {}^{\mathrm{d}}/{}^{\mathrm{d}}\tau(.)$  represents the derivative with respect to the non-dimensional time  $\tau$ .

#### 1.5 Derivation of the spectral system

As the time-varying bearing deformation (1) enters the equations in (3) as a parameter, the system is exposed to parametric- <u>and</u> self-excitation, which can lead to quasi-periodic behaviour. Therefore, the associated spectral system is derived according to the suggested method of Schilder [4], such that quasi-periodic trajectories can be easily described and analysed.

# 2. Simulation results

With the previously mentioned spectral system a fast analysis of the dynamic behaviour by means of solution continuation algorithms is possible even for originally quasi-periodic behaviour.

The results reveal a high potential to decrease large rotor amplitudes by selecting an appropriate time-varying deformation (1), i.e. it is possible to shift the beginning of the above mentioned instability phenomena to even higher revolution speeds.

#### References

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- [4] F. Schilder, W. Vogt, S. Schreiber, and H. Osinga. Fourier methods for quasi-periodic oscillations. *International journal for numerical methods in engineering*, 67(5):629–671, 2006.