Iron NRT- and arc-displacement cross sections and their covariances


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Abstract
Displacement damage cross sections have been calculated for natural iron and its constituent individual isotopes based on the latest versions of the evaluated neutron data libraries ENDF/B-VIII.0 and TENDL-2017 using the conventional NRT and recently introduced athermal recombination-corrected (arc) displacement concepts. Their covariance matrices, which quantify the uncertainties and the associated energy-energy correlations, were assessed for the first time based on TENDL-2017 random data files representing the covariances of the underlying nuclear data. In addition to the nuclear data, the covariances due to the ion energy partition, the primary defect survival efficiency and the lattice threshold energy were also propagated to the damage quantities. The arc-dpa was computed employing all available results from molecular dynamics and binary collision simulations. The comparison of the spectrum-averaged arc-dpa with the few available measurements at fission reactors has demonstrated a reasonable agreement within the experimental and calculation uncertainties. The comparison with the current NRT-dpa standard, provided by ASTM up to 20 MeV but without uncertainty, has indicated differences up to 8% above 0.5 keV and 60% below.

1. Introduction

The NRT concept of displacement damage cross section (dpa – displacements per atom), proposed by Norgett et al. [1], provides a basis for the quantification of neutron and ion induced radiation effects in materials. It is also can be used as a scaling factor for the comparison and extrapolation of radiation databases accumulated at existing nuclear facilities to projected ones. Recently a new damage concept based on “athermal recombination-corrected (arc) dpa”, has been proposed by the OECD Primary Radiation Group [2] and has been adopted for the calculation of damage cross section data by the IAEA Coordinate Research Project on Radiation Damage [3]. Arc-dpa quantify the total number of primary lattice defects (i.e., the vacancy-interstitial pairs denoted as Frenkel pairs) which survive after annealing of the hot recoil cascade during the first 10–100 ps after initiation of the nuclear reaction.

The present work provides evaluations of NRT- and arc-dpa cross sections for the naturally occurring isotopes of iron and elemental iron based on the latest evaluated neutron cross section data files up to 200 MeV. Initial comparative studies of the NRT- and arc-dpa cross sections and spectrally averaged values for fission, fusion and material testing facilities were carried out but involved only lower energies and used the neutron data available at that time [4–5]. Furthermore, estimates of the dpa covariance matrices (i.e., the uncertainties and associated energy-energy correlations) are provided for the first time as resulting from the involved nuclear data and material physics modelling. This work is an extension of our previous study on the iron main isotope, 56Fe [6], covering now the covariance determination for the displacement damage in natural iron.

2. Methods used to compute NRT- and arc-dpa and their covariances

2.1. Definitions and computing of the damage energy and displacement cross sections

The damage energy DE at neutron energy E which will be transferred to atoms displaced from their lattice sites in metal can be computed either in the frame of the conventional NRT or the new arc concepts according to the formulations given, e.g. in [1,2,7]. Since we used the NJOY code to compute DE, only a simplified formula is given here to show the variables which we derived or sampled but omitting others such as integration over scattering angle etc.:
\[ D_{E_{\text{NRT}}} = \sum_{i,j} \int_{E_j}^{E_i} \frac{d\sigma(E, T_j)}{dT_j} \bar{\nu} E_j dT_j \quad \text{DE}_{\text{unc}} \]

\[ = \sum_{i,j} \int_{E_j}^{E_i} \nu(T_j) \frac{d\sigma(E, T_j)}{dT_j} \tilde{\nu} E_j dT_j \quad \text{where} \quad \tilde{\nu} = \begin{cases} 2 \frac{E_j}{E_i}, & E_j < E_i < E_d \\ 0, & 0 < P(T_j)T_i < 2E_d/0.8 \\ E_d/P(T_j)T_i, & 2E_d/0.8 < P(T_j)T_i < \infty \end{cases} \quad (1) \]

In Eq. (1), \( d\sigma(E, T_i)/dT_i \) is the energy differential cross section for the production of primary knock-on atoms (PKA) or charged particles i with kinetic energy \( T_i \) for the neutron-induced reaction channel j; \( P(T) \) - the ion energy partition function (i.e., the fraction of recoil energy that becomes available for damage) [1,7]; \( \nu(T) \) - primary defects survival efficiency or fraction of Frenkel pairs (FP) left after athermal cascade annealing phase; \( E_d \) - lattice threshold energy or averaged minimum energy needed to create one FP.

The latest official version 99 of the nuclear data processing code NJOY-2012 [7], was used to compute the damage energy for each stable iron isotope \( ^{54,56,57,58}\text{Fe} \) from the latest versions of the modern nuclear data evaluations ENDF/B-VIII.0 [8] and TENDL-2017 [9].

The NJOY code implements a model for the damage energy that is not consistent with the NRT damage energy definition in Eq. (1) in the interval \( E_d \leq E_j < 2E_d/0.8 \). In the case of iron this results in an underestimation of the NRT- and dpa-cross sections by factor of 2.0/0.8 = 2.5 at neutron energy \( E = E_dA/4 = 0.65\text{keV} \), where A is atomic mass number. For a rigorous implementation of the NRT definition we modified the HEATR module of NJOY as documented in [10].

The corresponding NRT- and arc-dpa cross sections are then derived according to:

\[ \sigma_{\text{NRT-dpa}}(E) = \frac{0.8}{2E_d} D_{E_{\text{NRT}}}(E) \quad \text{or} \quad \sigma_{\text{arc-dpa}}(E) = \frac{0.8}{2E_d} D_{E_{\text{unc}}}(E) \quad (2) \]

The DE- and dpa-cross sections for natural iron were produced from isotopic cross sections by the MIXR module of NJOY taking into account the isotope abundances \( a_i \) \( ^{54}\text{Fe} = 5.9\%, \quad ^{56}\text{Fe} = 91.72\%, \quad ^{57}\text{Fe} = 2.1\%, \quad ^{58}\text{Fe} = 0.28\% \).

In the present work the uncertainties and energy-energy correlations of \( D(E) \) or \( \sigma_{\text{dpa}}(E) \) were computed independently from the different underlining data or models, namely from: nuclear data, PKA energy partition function, FP survival efficiency and Ed. It means when one component was randomized, the others were used unperturbed.

2.2. Computation of the damage cross section covariances from TENDL-2017 evaluated neutron data files

The covariance matrix for DE- and dpa-cross sections were computed from five hundred TENDL-2017 random files which were generated by the Bayesian Monte Carlo method (i.e. by sampling and assigning the proper weights for the input parameters of the underlying nuclear reaction models) [9]. Each of these 500 random files were also processed by the NJOY code and additionally grouped into 228 energy bins to reduce the rank of covariance matrices but still retaining a rather detailed energy representation of cross sections. The energy group structure of VITAMIN-J 175 was chosen, which covers the energies from \( 10^{-5}\text{eV} \) to 19.64 MeV, plus \( 1-2\text{ MeV} \) wide bins up to 200 MeV.

The first order covariance matrix for values \( y_i \) (i.e., either \( D(E_i) \) or \( \sigma_{\text{dpa}}(E_j) \)) in every bin \( i \) was calculated from the \( N_{\text{random}} \) ensemble following the general definitions [11]:

\[ \text{cov}(y_i, y_j) = \sum_{k=1}^{N_{\text{random}}} \frac{(y_{ik} - \bar{y}_i)(y_{jk} - \bar{y}_j)}{N_{\text{random}}} \quad (3) \]

where indices i or j refer to the k random value of quantity \( y_i^k \) in the specific energy groups and \( \bar{y}_i \) is an averaged value. The diagonal elements \( (i = j) \) of the covariance matrix provide the variance or square of the standard deviation \( \sigma_i \):

\[ \sigma_i^2 = \text{cov}(y_i, y_i) \quad (4) \]

The energy-energy correlation matrix was then calculated as:

\[ \text{cov}(y_i, y_j) = \frac{\text{cov}(y_i, y_j)}{\sigma_i \sigma_j}, \quad \text{cov}(y_i, y_j) = 1 \quad (5) \]

The covariances matrices were firstly computed for each isotope \( ^{54,56,57,58}\text{Fe} \) from the corresponding isotopic TENDL-2017 random files. Then the covariance matrix for natural iron was obtained by summing up the variances of the individual isotopes taking into account the iron isotope abundancies \( a_i \) and absence of the cross isotope correlations in the TENDL-2017 random evaluation:

\[ \text{cov}_{\text{nat}}(E_i, E_j) = \sum_{n=1}^{4} a_n^2 \text{cov}(E_i, E_j) \quad (6) \]

For illustration, the results of the calculation of the NRT damage energy and its uncertainties resulting from the nuclear data for natural iron and two isotopes \( ^{54,56}\text{Fe} \) are shown in Fig. 1. It is interesting to note that \( ^{56}\text{Fe} \) gives a dominant contribution to the DE cross section and the uncertainty at all energies except in the vicinity of 8 keV where the \( n-\text{Fe} \) resonance prevails over \( ^{54}\text{Fe} \). The energy-energy correlation matrix derived from TENDL-2017 neutron random files shows two energy
domains of high correlations however without correlation between them, see Fig. 2.

2.3. Covariances due to involved materials physics modelling

In additional to the neutron-nucleus interaction cross section several other phenomena which reflect the material physics have impact on the calculation of the damage energy and the displacement cross sections.

Partitioning of the recoil atom energy between the kinetic energy delivered to the lattice knock-on atoms (real damage energy) and the ion energy losses due to Coulomb interaction with electrons. The most commonly used partition function was introduced by M. Robinson who has fitted J. Lindhard’s theory of energy splitting between atomic and electronic motion [12]. The uncertainties of three parameters used in Robinson’s formula were derived from the comparison with the spread of the number of NRT defects computed by the IOTA code [13]. Different approximations of the ion-ion scattering cross section were used, which eventually define the nuclear stopping power of ions. During the processing of the non-perturbed TENDL-2017 files by the NJOY code, we varied the parameters of the partition function within ± 12% and generated 500 random damage energy files. Their statistical analysis using Eq. (3) has resulted in the production of the covariance matrices for each Fe isotope. The mixing of four isotopes finally yields the damage energy covariance matrix for natural iron as a result of the partition function. The correlation matrix displayed in Fig. 3 shows strong correlations between practically all neutron energies.

Frenkel pair defect survival efficiency according to Eq. (1) affects only arc-dpa, since it depends on $\nu(T)$, but not NRT-dpa. The number of FP defects is usually computed by molecular dynamics (MD) simulations which depend on the interatomic potential used. The different potentials as well as statistical uncertainties due to a limited number of simulated tracks result in the variation of MD predictions for the survival efficiency.

Fig. 4 shows the MD results collected in the overview [2] and several additional independent ones [4,14,15] (the results obtained with the use of potentials published in the later paper will appear elsewhere soon) for the PKA energy up to 200 keV – that is sufficient for fission applications. To cover the energy range of recoils produced also in fusion and accelerator driven facilities, the survival efficiency has to be defined up to 1040 keV (fusion, maximum neutron energy 15 MeV) or 3830 keV (International Fusion Material Irradiation Facility IFMIF, maximum neutron energy 55 MeV). These values are the energies of $^{56}$Fe recoils emitted in forward direction by elastic neutron scattering on $^{56}$Fe (the exothermic $^{56}$Fe($n,\alpha$) reaction may produce Cr recoils with even higher energies, see Simakov et al. [5]).

Since MD simulations are currently not capable of computing the number of FP at such high recoil energies, the binary collision approach (BCA) or its combination with MD simulations [16,17], is a practical way to estimate the defect survival efficiency - see available computational results in Fig. 4.

In the present calculations we eventually used the defect survival efficiency from the OECD fit [2] up to 200 keV (represented as a table) and the SRIM based MD-BCA results [16] at higher energies, after downscaling by the factor 0.8 to match the OECD fit. The uncertainties assessed in [2] amount only to ± (2–4)% that do not reflect the spread of the MD simulation results as seen in Fig. 4. To capture the latter effect we assigned a ± 20% uncertainty to the survival efficiency.

The recoil energy-energy correlations of the damage efficiency originate from the equations and parameters used in the MD simulations. We did not found in the literature quantitative information which helps us to construct the correlation matrix. On other hand some MD simulations studies, see in [2] and [14], have reported the statistical uncertainty within 10–20% for PKA energies below ~40 keV. As seen in Fig. 4, the statistical error bars are comparable with spread of
Fig. 5. The energy-energy correlation matrix for the natural iron arc damage energy which is caused by the uncertainties of the FP survival efficiency.

Individual results. The dominance of the statistical uncertainty below 40 keV means an absence of the energy-energy correlation for the defect survival efficiency. In the present work we accepted such correlation matrix for the whole energies of PKA.

The resultant energy-energy correlation matrix of the arc damage energy for elemental iron, which is induced by the uncertainties of the FP survival efficiency, is plotted in Fig. 5. As expected it shows no correlation. Exception is the neutron energies below 0.5 keV, where the (n,γ) reaction dominates in the production of recoils. Due to the kinematics of this reaction even neutrons with different energies up to 50 keV will produce recoils with the same energy, hence the computing of the number of survived defects will involve the equal survival defect efficiency. This results to the full energy-energy correlation matrix for neutrons below 0.5 keV.

Lattice Threshold Energy. K. Nordlund and co-workers have estimated the mean value and uncertainty of threshold energy for iron as $E_{th} = 40 \pm 2$ eV [18]. Following Eq. (2), this 5% relative uncertainty will directly propagate to the damage energy arc-dpa cross section, as seen in Figs. 6 and 7, is less than the NRT- and arc-dpa cross section can not be compared with experimental data and thus be validated since it is practically a non observable physical quantity. However an estimate of the arc-dpa for Fe can be that will be corrected in the next TENDL release. Due to this reason the nuclear data uncertainties and energy-energy correlations calculated from the TENDL-2017 random files above 30 MeV are not representative and will be reassessed after release of the corrected TENDL version. For comparison the ASTM E693-12 standard [19], which is an actual NRT reference for iron up to 20 MeV neutron energy, is also plotted in Fig. 6. It has to be noted that this standard was computed from the evaluated neutron cross sections library ENDF/B-VI which is nowadays obsolete. To show a difference resulting from the evolution of the ENDF library, the ratio of ASTM E693-12 to the ENDF/B-VIII.0 NRT-dpa cross section is plotted in Fig. 7. As expected it shows no correlation. Exception is the neutron energies below 0.5 keV, where the (n,γ) reaction dominates in the production of recoils. Due to the kinematics of this reaction even neutrons with different energies up to 50 keV will produce recoils with the same energy, hence the computing of the number of survived defects will involve the equal survival defect efficiency. This results to the full energy-energy correlation matrix for neutrons below 0.5 keV.

3. Discussion and comparison with experiments

Fig. 6 shows the NRT-dpa cross section for natural iron up to 200 MeV, derived from the latest evaluated neutron cross section libraries ENDF/B-VIII.0 and TENDL-2017 and the arc-dpa cross section, which additionally take into account the Frenkel pair survival efficiency from MD and BCA-MD simulations.

For the first time the total uncertainty and energy-energy correlation for radiation damage quantities, as well as the partial contributions from used physical models, were estimated on the basis of the assumptions used here. As seen in the bottom of Fig. 6, the nuclear data lead to (5 -- 10)% uncertainties and strong positive energy-energy correlations within 2 large regions not correlating to each other (Fig. 2); ion energy partition -- (2 -- 5)% uncertainties and strong positive E-E correlations (Fig. 3); defect survival efficiency -- (5 -- 15)% and non-correlation except the energy range where (n,γ) reaction dominates (Fig. 5), lattice threshold -- 5% uncertainty and full E-E correlation.

The NRT- and arc-dpa cross section derived from TENDL-2017 random files drop off at 30 MeV. The reason was found to be an improper storage of relevant nuclear reaction data in the formatted files that will be corrected in the next TENDL release. Due to this reason the nuclear data uncertainties and energy-energy correlations calculated from the TENDL-2017 random files above 30 MeV are not representative and will be reassessed after release of the corrected TENDL version. For comparison the ASTM E693-12 standard [19], which is an actual NRT reference for iron up to 20 MeV neutron energy, is also plotted in Fig. 6. It has to be noted that this standard was computed from the evaluated neutron cross sections library ENDF/B-VI which is nowadays obsolete. To show a difference resulting from the evolution of the ENDF library, the ratio of ASTM E693-12 to the ENDF/B-VIII.0 NRT-dpa cross section is plotted in Fig. 7. As expected it shows no correlation. Exception is the neutron energies below 0.5 keV, where the (n,γ) reaction dominates in the production of recoils. Due to the kinematics of this reaction even neutrons with different energies up to 50 keV will produce recoils with the same energy, hence the computing of the number of survived defects will involve the equal survival defect efficiency. This results to the full energy-energy correlation matrix for neutrons below 0.5 keV.

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obtained in the experiments where the samples were irradiated at temperature below 10 °K thus preventing the dissociation and annealing of primarily created Frenkel pairs [20, 21, 22]. The measurements were carried in fast fission neutron spectra, and the number of defects was derived from the change of electrical resistivity. To perform a comparison we have folded the computed arc-dpa cross section with the prompt fission neutron spectrum (PFNS) well known for the thermal neutron induced fission of 235U [23]. The results listed in Table 1 and plotted in Fig. 7 show reasonable agreement with two of three existing experiments. The spectrum weighted NRT-dpa given there for comparison is 3.2 times larger than arc-dpa.

4. Summary

NRT- and arc- damage energy and displacement cross sections were computed for individual iron isotopes and natural iron at neutron energies from thermal to 200 MeV employing neutron induced cross sections from the latest nuclear data libraries ENDF/B-VIII.0 and TENDL-2017.

The comparison of the ENDF/B-VIII.0 NRT-dpa with the actual standard ASTM E693-12 available up to 20 MeV has shown an agreement within 8% except for energies below 0.5 keV where the lower Fe (n,γ) damage energy cross sections is a result of the NJOY processing of the latest version of the ENDF library. TENDL-2017 gives even lower NRT-dpa cross sections below 0.5 keV and additionally exhibits a discontinuity at 30 MeV.

The arc-dpa was calculated taking into account available MD and BCA-MD simulations of the number of Frenkel pairs surviving at the end of the ballistic cascade relaxation.

For the first time, the full uncertainty and the associated energy-energy correlations from all contributing components were constructed for NRT- and arc-dpa cross sections: nuclear data as represented by TENDL-2017 random files (5–15%), recoil energy partition function (2–5%), FP survival efficiency (5–15%) and lattice threshold energy (5%). It has to be stressed that the cross sections and covariances obtained from the TENDL-2017 random files are not valid above 30 MeV, where damage energy is systematically too low.

The arc-dpa averaged in fast fission neutron spectrum was shown to agree with measurements performed at cryogenic temperature in fission reactors. Neglecting the energy-energy correlation results in an underestimation of spectrum averaged dpa-rate uncertainty in nuclear facilities by a factor 3–4 [6].

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References

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