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## PAPER

## Quasi non-diffractive electron Bessel beams using direct phase masks with applications in electron microscopy

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Electron-beam shaping opens up novel imaging possibilities in electron microscopy (EM). The implementation of a phase or amplitude mask in the condenser lens system allows the generation of electron beams with various shapes. Non-diffractive Bessel beams (BBs) are of interest for numerous applications due to their extraordinary large depth of focus. We present an experimental demonstration of single high-intensity quasi non-diffractive electron BBs generated by direct phase masks (PMs). The PM fabrication by focused ion beam is optimized using custom scan routines. The propagation of the electron beam after transmission through several PMs is analyzed in detail. A sub nm-sized non-diffractive electron beam is realized in the object plane of a transmission electron microscope. The experiments agree well with simulations and a route towards a beneficial application of non-diffractive electron beams in EM is discussed.

**1. Introduction**

Shaping the electron beam for novel applications in scanning transmission electron microscopy (STEM) has attracted tremendous interest since the first experimental observation of an electron vortex beam, i.e. a beam carrying orbital angular momentum [1]. Beam shaping is typically achieved by using phase masks (PMs) or amplitude masks (AMs) fabricated using a focused ion beam (FIB). The masks influence the illuminating electron plane wave in a way that the desired electron beam amplitude and phase profile is realized in a plane below the mask. One of the most popular types of beam-shaping masks is the holographic mask whose shape is calculated from a superposition of the desired target wave function and a reference wave, e.g. a tilted plane wave. The hologram is then either transferred in a 3D structured electron-transparent thin-film membrane (holographic PM), where the thickness variations are linked to the desired phase profile, or the hologram is binarized and structured into an obstructing aperture (holographic AM). One drawback of such holographic masks is the generation of multiple electron beams which hinders application as the desired beam exhibits a low intensity and has to be separated from the remaining beams. Direct PMs, which produce a single, high-intensity, electron beam with the desired shape are therefore better suited for practical application [2–4]. Of particular interest are programmable PMs which are not limited to a specific beam shape [5].

In addition to electron vortex beams, which have been intensively studied by numerous groups [6–10], beam shaping has been applied to create Airy [11], Bessel [12, 13] or arbitrary beam shapes [4] and also to correct for aberrations [14]. Among these, (quasi) non-diffractive electron Bessel beams (BBs) are promising to find an application in probe forming for various STEM techniques. Non-diffractive beams have been proposed in light optics by Durkin [15] and were realized in an electron microscope only recently using holographic PMs [13], nano-structured slits [16, 17] or a magnetic material [18]. The beam profile of BBs is given by a Bessel function which exhibits radial symmetry and whose shape is, at least in theory, constant upon beam propagation, i.e. the beam is non-diffractive. In the experiment, the use of a finite aperture limits the non-diffractive property to a specific propagation length  $z_{\max}$  along the beam path beyond the beam-shaping mask. For typical microscopes

and state-of-the-art structuring possibilities,  $z_{\max}$  is in the range of a few cm to m, being sufficiently large to be used as illuminating beam in STEM. The major advantage of a BB is the extraordinary high depth of focus (DOF), which is significantly higher than in conventional STEM where the DOF is dependent on the convergence angle and typically is in the range of a few tens of nm and even lower for aberration-corrected probes [19]. Additionally, BBs exhibit a self-reconstructing property which implies that their original beam profile is (partially) restored after a scattering event. Both, the self-reconstructing property and the high DOF makes imaging with BBs of thick specimens and in STEM tomography highly promising [20, 21]. In fact, BBs benefit modern fluorescence light microscopy [22, 23].

In this work we fabricated direct PMs to generate single BBs with a high intensity for application in EM. The PM fabrication is optimized to obtain high quality smooth masks. The electron-beam evolution after transmission through the PM is analyzed in detail by a low-magnification (LM) setup in a transmission electron microscope and the experimental results agree well with corresponding simulations. PMs installed in the condenser lens system yield sub nm-sized BBs in the object plane of the microscope where the sample is placed. Possible routes leading to an application are discussed.

## 2. Fabrication of a PM

The PM fabrication starts with a Si wafer in (100) orientation coated with low-stress silicon nitride (in the following denoted as  $\text{Si}_3\text{N}_4$ ) on both sides (Microchemicals GmbH, Ulm, Germany). The backside  $\text{Si}_3\text{N}_4$  layer is patterned using photolithography and reactive ion etching so that a following KOH wet etch results in  $\text{Si}_3\text{N}_4$  membranes with a size of  $100 \times 100 \mu\text{m}^2$ . The membranes are arranged on dodecagonal chips imitating round TEM grids with 3 mm diameter. Pt apertures (diameter 10–50  $\mu\text{m}$ ) are then fabricated in a second photolithographic step followed by physical vapor deposition of a Cr/Pt layer (3.5/150 nm) and a lift-off process. The individual chips can be separated by manual fracturing.

Instead of fabricating the membranes in-house, commercially available TEM grids with  $\text{Si}_3\text{N}_4$  membranes can also be used. However, then the Pt apertures cannot be fabricated by a lift-off process and focused-ion-beam milling has to be applied. During the FIB milling of the round aperture in the deposited Pt, the roughness of the membranes is increased due to the crystallinity of the Pt layer. Additionally, the fabrication is serial and thus rather time-consuming. A 5 nm thick amorphous carbon layer is deposited on the backside of the obtained membranes by carbon thread evaporation (MED020, Leica Microsystems) to reduce charging during FIB milling and in TEM. The PM structure is finally milled into the  $\text{Si}_3\text{N}_4$  membrane with a Helios G4 FIB system (Thermo Fisher Scientific) using a beam current between 40 and 260 pA.

The thickness profile  $T$  of a direct PM creating a single BB is given by equation (1) in dependence of the cylindrical coordinates  $r$  and  $\varphi$  [24]:

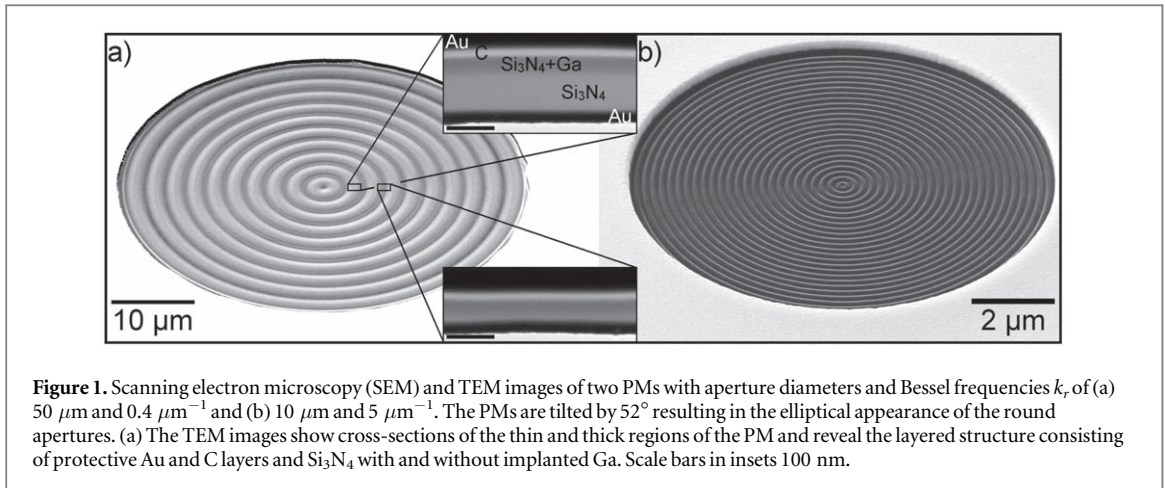
$$T(r, \varphi) = t_0 + t_a[1 - \cos(2\pi r k_r + m\varphi)]; r < D. \quad (1)$$

The offset thickness  $t_0$  is given by the remaining thickness of the membrane and  $2t_a$  is the amplitude between minimum and maximum thickness of the structured profile.  $T$  is present only within the aperture diameter  $D$ . The parameter  $m$  defines the order of the resulting BB and introduces an orbital angular momentum to the electron beam. In this work we focused on BBs of zeroth order, i.e.  $m = 0$  implying  $T$  is rotationally symmetric and describes concentric circles. The Bessel frequency  $k_r$  determines the pitch between the structured circles and the properties of the resulting BB. The thickness profile  $T$  leads to the phase profile  $\Phi$  of an electron plane wave transmitted through the PM which depends on the interaction constant  $\sigma$  and the mean inner potential  $V_{\text{MIP}}$  of  $\text{Si}_3\text{N}_4$ :

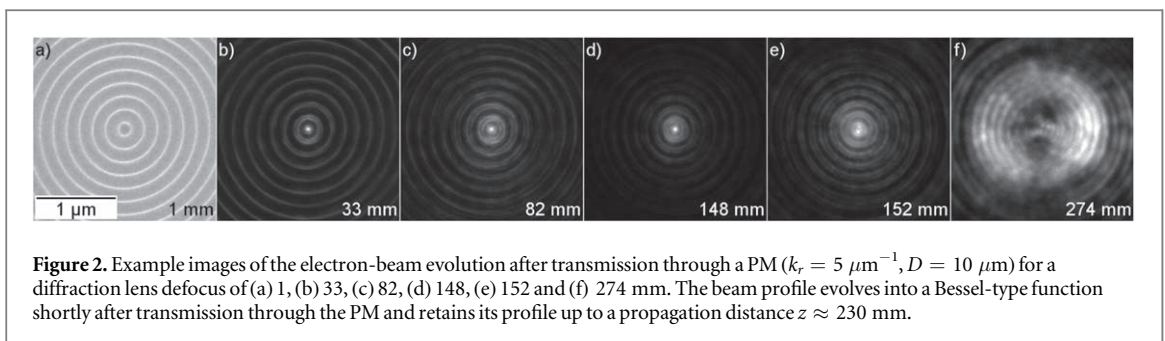
$$\Phi(r) = \sigma T(r) V_{\text{MIP}}. \quad (2)$$

Of course,  $\text{Si}_3\text{N}_4$  is not a pure phase object but alters the amplitude of the electron wave as well. Electrons scattered to higher angles in the PM are absorbed by apertures or contribute to the background signal of the resulting BB. In simulations conducted in this work we use a simple model of a total mean free path  $\lambda_{\text{mfp}}$ , including elastic and inelastic scattering, to calculate the amplitude damping of the electron wave.  $\lambda_{\text{mfp}}$  corresponds to the thickness of the PM material at which the fraction of unscattered electrons has decreased to  $\frac{1}{e}$  after propagation through the PM. In our approach, the amplitude  $A$  of an illuminating plane wave ( $A_0 = 1$ ) is then damped to  $A_T = \exp(-T/\lambda_{\text{mfp}})$  depending on the thickness  $T$  of the PM. A more accurate consideration would require multi-slice simulation of the wave after transmission through the PM but is not needed as our approach gave good agreement with the experiment.

To transfer the desired thickness profile in the  $\text{Si}_3\text{N}_4$  membrane in an optimum way, a stream file is created which determines the FIB path and dwell time. In case of high  $k_r$ , the stream file starts with a single point in the center of the PM followed by vector-written circles with linearly increasing radius. The FIB is not blanked in between the circles. The distance between the circles is given by  $1/k_r$  in order that only the deepest parts of the



**Figure 1.** Scanning electron microscopy (SEM) and TEM images of two PMs with aperture diameters and Bessel frequencies  $k_r$ , of (a)  $50 \mu\text{m}$  and  $0.4 \mu\text{m}^{-1}$  and (b)  $10 \mu\text{m}$  and  $5 \mu\text{m}^{-1}$ . The PMs are tilted by  $52^\circ$  resulting in the elliptical appearance of the round apertures. (a) The TEM images show cross-sections of the thin and thick regions of the PM and reveal the layered structure consisting of protective Au and C layers and  $\text{Si}_3\text{N}_4$  with and without implanted Ga. Scale bars in insets  $100 \text{ nm}$ .



**Figure 2.** Example images of the electron-beam evolution after transmission through a PM ( $k_r = 5 \mu\text{m}^{-1}$ ,  $D = 10 \mu\text{m}$ ) for a diffraction lens defocus of (a)  $1$ , (b)  $33$ , (c)  $82$ , (d)  $148$ , (e)  $152$  and (f)  $274 \text{ mm}$ . The beam profile evolves into a Bessel-type function shortly after transmission through the PM and retains its profile up to a propagation distance  $z \approx 230 \text{ mm}$ .

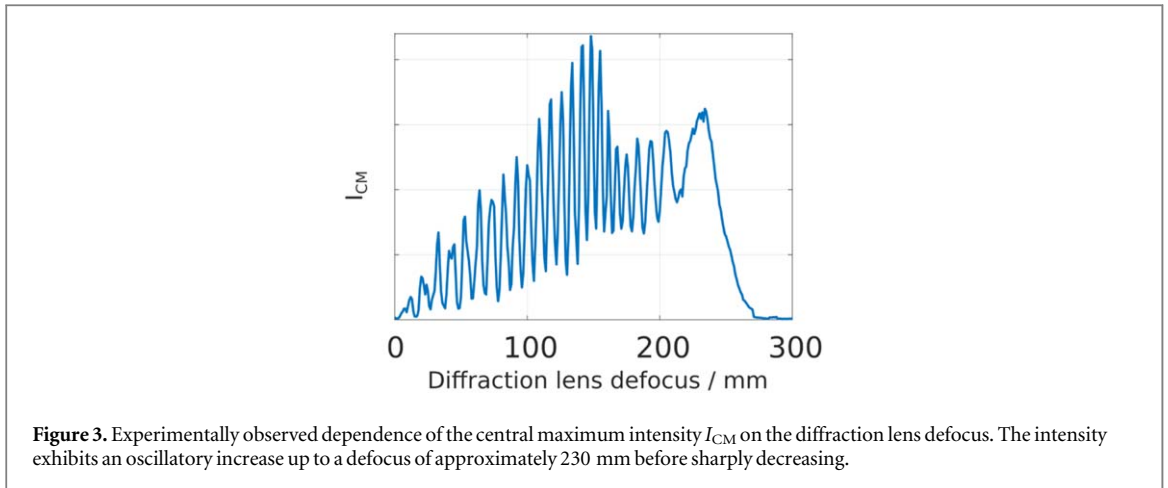
structures are actually irradiated with the FIB. The FIB dwell time was chosen to be between  $50$  and  $100 \mu\text{s}$ , depending on the size of the PM. To ensure a similar depth of the central spot compared to the surrounding circles, the corresponding dwell time is increased by a factor of  $5$ . The whole path is milled approximately  $30$  times with each pass being rotated by an offset angle. In this setup, redeposition effects are minimized and a homogeneous structure is achieved as shown in the SEM image in figure 1(b). The actual form of the depth profile is defined by the FIB beam profile and slightly differs from the desired sinusoidal form (equation (1)).

For  $k_r < 5 \mu\text{m}^{-1}$ , gray scale milling is applied, meaning that the distance between the structured circles is fixed and the dose for each circle is calculated by equation (1). Figure 1 shows SEM and cross-section TEM images of two example PMs. The TEM images reveal the implantation of Ga in the  $\text{Si}_3\text{N}_4$  up to a depth of approximately  $35 \text{ nm}$ . The presence of Ga will influence  $V_{\text{MIP}}$ . However, the thickness of the  $\text{Si}_3\text{N}_4 + \text{Ga}$  layer is constant in the area of the PM and only affects the offset phase  $\phi_0 = \sigma t_0 V_{\text{MIP}}(\text{Si}_3\text{N}_4 + \text{Ga})$  and can therefore be neglected in the simulations. The penetration depth of Ga in  $\text{Si}_3\text{N}_4$  also determines the minimum offset thickness  $t_0$  as the milling rate is drastically increased once a considerable fraction of Ga ions penetrate through the PM. For PMs with low  $k_r$  values, the offset and amplitude thickness are determined by cross-section TEM to  $2t_a = 74 \text{ nm}$  of  $\text{Si}_3\text{N}_4$  and  $t_0 = 35 \text{ nm}$  of  $\text{Si}_3\text{N}_4 + \text{Ga}$ .

### 3. Properties of electron BBs

A PM with  $k_r = 5 \mu\text{m}^{-1}$  and  $D = 10 \mu\text{m}$  is inserted as specimen in a FEI Titan 80-300 (Thermo Fischer Scientific) operated at  $300 \text{ kV}$  to analyze the properties of the resulting BB. The LM mode with a slightly excited objective lens (OLs) ( $4\%$ – $5\%$ ) is used to trace the evolution of the electron wave after transmission through the PM by defocussing the diffraction (i.e. the first intermediate) lens. The beam profile evolution is imaged with a Gatan Ultrascan CCD camera controlled by a DigitalMicrograph script. Adjustment of the rotation center and both, objective and diffraction, stigmators is crucial to minimize artifacts in the imaging process. As it is not possible to simultaneously correct for astigmatism in the whole necessary range of diffraction lens excitation, slight distortions are still visible in the acquired TEM images.

Figure 2 shows six example images of an acquired image series of the electron-beam evolution with in total  $341$  images and a defocus range of  $0$ – $340 \text{ mm}$ . The exposure time of each image was altered to keep the maximum count number at approximately  $4000$  per pixel and the image contrast was adjusted to improve feature visibility. A movie of the entire electron-beam evolution as function along  $z$  can be found in



supplementary movie 1 [stacks.iop.org/NJP/21/033007/mmedia](https://stacks.iop.org/NJP/21/033007/mmedia). A suitable method to display the electron-beam evolution in a more simplified way is to measure the intensity of the central maximum  $I_{CM}$  in each image. Figure 3 shows the evolution of  $I_{CM}$  for the acquired image series revealing an oscillatory increase up to a diffraction lens defocus of around 230 mm before the intensity sharply decreases.

The second image of the series is displayed in figure 2(a) and shows the electron wave 1 mm after transmission through the PM. Concentric rings are clearly visible but a central maximum is not observed because a BB has not yet formed. In the image at a diffraction lens defocus of 33 mm, corresponding to the third maximum in figure 3, the electron wave is similar to a Bessel function of the first kind and 0th order which can be recognized by the central maximum of high intensity and the surrounding rings with decreasing intensity (figure 2(b)). The shape of the Bessel function is then preserved upon propagation as visible in figures 2(c)–(e). This preservation of the shape of the electron beam is called the non-diffractive property. While figures 2(a)–(d) correspond to local maxima in figure 3, the image acquired at 152 mm (figure 2(e)) depicts the wave at a local minimum where the central maximum vanished and its intensity shifted to the first ring. This shows that although the overall Bessel-type shape persists upon propagation, the intensity distribution is subject to change.

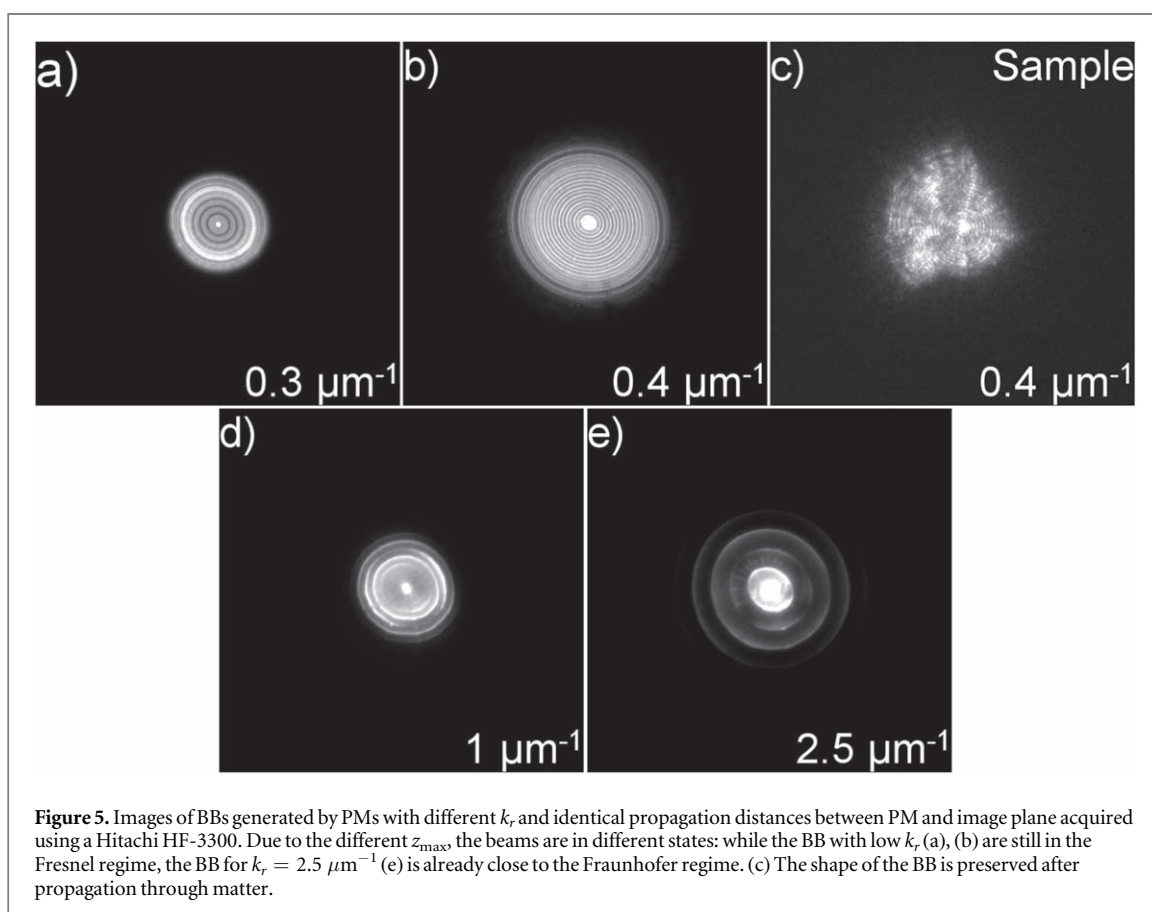
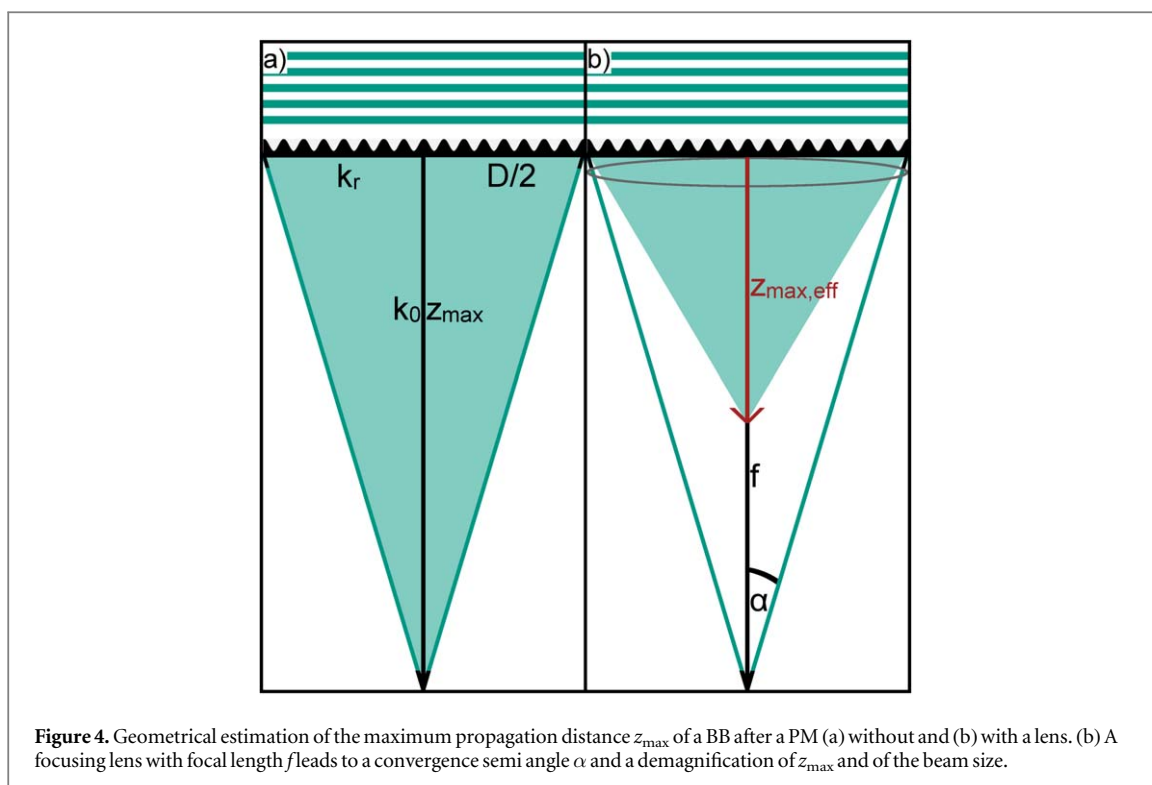
The electron wave is quasi non-diffractive as the shape is only preserved up to a maximum propagation distance  $z_{max}$ . Figure 2(f) shows an image of the electron beam outside the non-diffractive range ( $> z_{max}$ ) which is not described by a Bessel function anymore. The value for  $z_{max}$  can be estimated from a simple geometric consideration (figure 4):

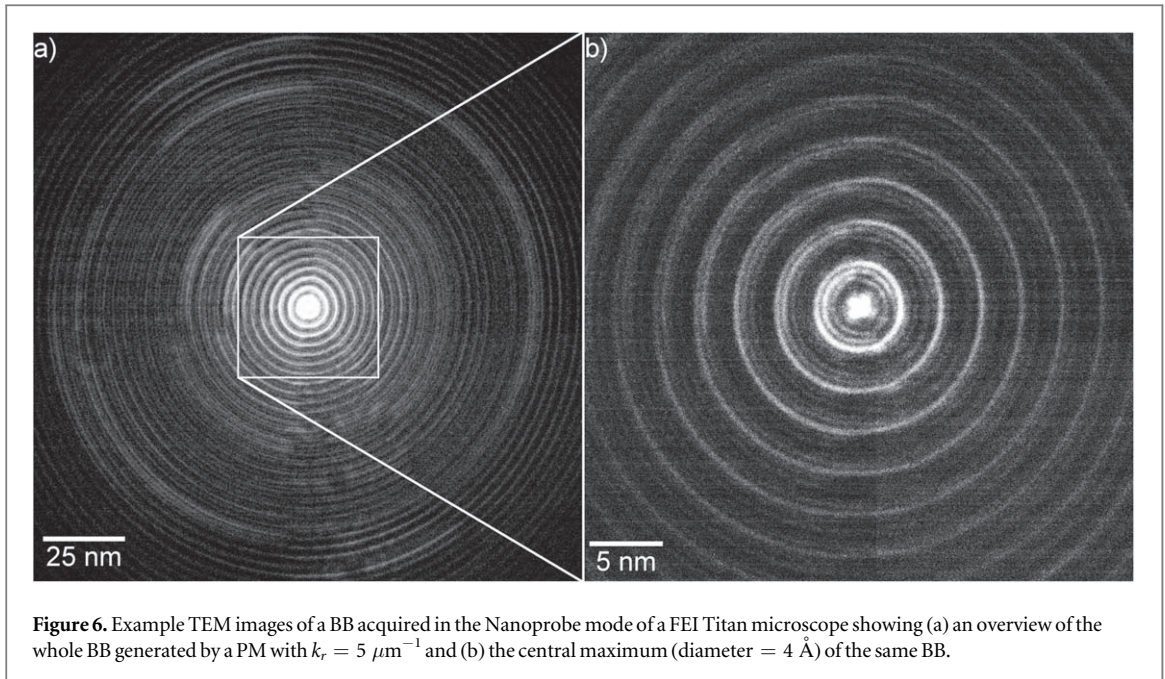
$$z_{max} = M \frac{Dk_0}{2k_r} \quad (3)$$

$z_{max}$  depends on the diameter of the PM  $D$ , the electron wave vector  $k_0$  and the Bessel frequency  $k_r$ . Figure 4 shows a sketch of the determination of  $z_{max}$  without (figure 4(a)) and with an additional lens (b). The presence of a lens can cause a (de-)magnification of the electron beam and affects the effective value of  $z_{max}$  which is reflected by the magnification factor  $M$  in equation (3) and can be inferred from figure 4(b). Due to the weakly excited OLs, the space behind the PM is not completely field-free. Consideration of the experimental parameters  $D = 10 \mu\text{m}$ ,  $k_r = 5 \mu\text{m}^{-1}$  and an electron energy of 300 keV results in  $z_{max} = 500 \text{ mm}$ . By comparison with the experimentally determined value of  $z_{max} = 230 \text{ mm}$ ,  $M$  can be estimated to  $\approx 0.5$  for the applied diffraction lens defocus. The demagnification is not constant but slightly changes with the varying excitation of the diffraction lens ( $M = M(I_{Lens})$ ). This is reflected by a minor decrease in size of the BB with increasing diffraction lens defocus (figures 2(b)–(e)). The effect of a focusing lens on the electron-beam evolution is further analyzed later.

The experimental results obtained on the electron-beam evolution by analysis of the PM using the LM mode in figure 3 in TEM agree well with those reported in literature [12, 13, 15, 24, 25].

Instead of using the diffraction lens to change the effective propagation distance between specimen and image plane, we also studied the propagation of BBs with different  $k_r$  for a fixed propagation distance. The experiment was performed by inserting the PM ( $D = 50 \mu\text{m}$ ) above the first condenser lens in a Hitachi HF-3300 (see figure 7) and turning off all lenses except for the last projection lens which was used to magnify the propagated BB onto a Gatan Ultrascan 1000 camera. Figure 5 shows the obtained results and reveals that due to the different values of  $k_r$  and thus  $z_{max}$ , the BBs are observed in different states. While the BB generated by PMs with low  $k_r$ , (a), (b) have only propagated a small fraction of  $z_{max}$ , the BB with  $k_r = 1 \mu\text{m}^{-1}$  has already propagated a larger fraction of  $z_{max}$ . For  $k_r = 2.5 \mu\text{m}^{-1}$  (e), the propagated distance is almost far enough to reach the Fraunhofer regime of the PM. Figure 5(c) shows an image of a BB obtained from the identical PM as in (b)





**Figure 6.** Example TEM images of a BB acquired in the Nanoprobe mode of a FEI Titan microscope showing (a) an overview of the whole BB generated by a PM with  $k_r = 5 \mu\text{m}^{-1}$  and (b) the central maximum (diameter = 4 Å) of the same BB.

but which has propagated through a test specimen (Grating replica, TedPella Prod. No. 607) inserted in the sample plane of the microscope. The shape of the BB and the edge of the sample grid bars are visible.

#### 4. Generation of BBs in the sample plane

In this section we present BBs generated in the sample plane by implementation of PMs in the condenser lens system of two different microscopes. The effect of the PM positioning and the lens settings on the BBs are assessed. A comparison of an acquired image series with simulations allows to reconstruct the phase profile of the PM.

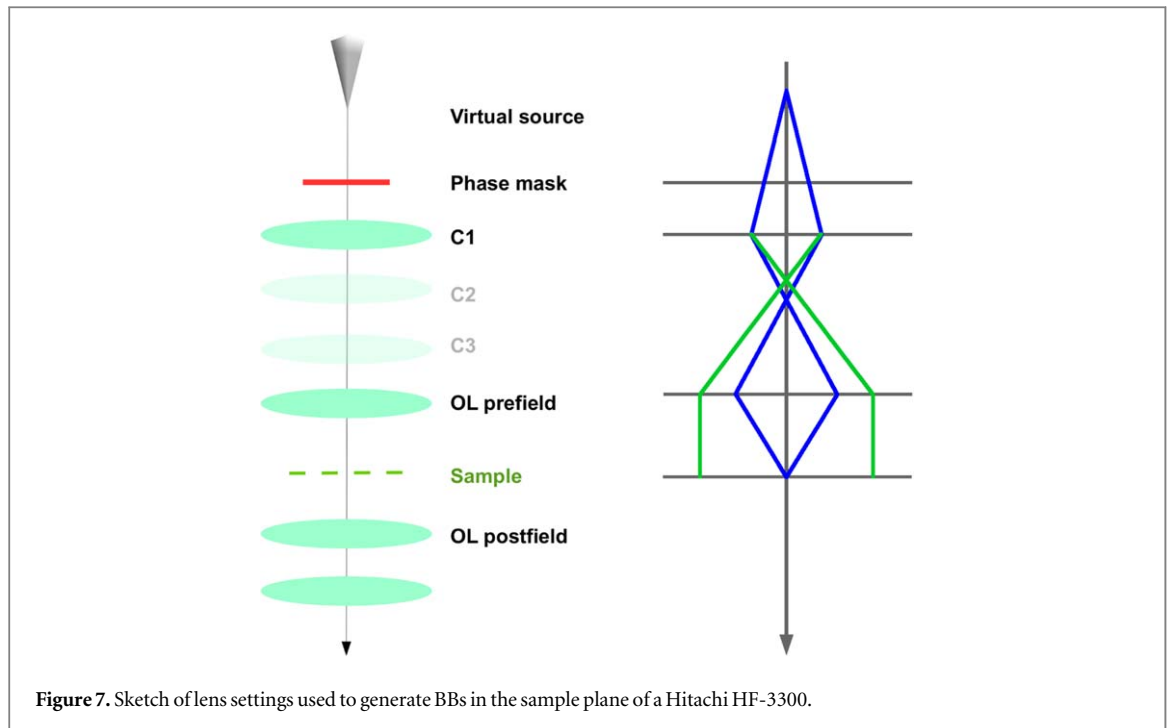
##### 4.1. PM in C2 condenser aperture

A PM with a diameter  $D = 10 \mu\text{m}$  and  $k_r = 5 \mu\text{m}^{-1}$  was inserted in the C2 condenser aperture of a FEI Titan transmission electron microscope. In conventional electron microscopy (EM), the condenser lenses are adjusted in a way that the specimen is either illuminated with an image (plane wave, TEM) or the back focal plane (focused probe, STEM) of the C2 aperture. The BB evolves in the Fresnel regime of the PM (figure 4) and thus both modes are not applicable to generate a BB in the specimen plane. In the Nanoprobe mode of the microscope, the effective propagation distance of the BB between the PM and the specimen plane can be defined by the C3 lens excitation ('Brightness'). Supplementary movie 2 [stacks.iop.org/NJP/21/033007/mmedia](https://stacks.iop.org/NJP/21/033007/mmedia) shows the BB evolution from image to back focal plane acquired by recording TEM images of the BB for varying C3 lens excitations. An increasing demagnification with time (with C3 lens excitation and effective propagation distance) can be observed.

Figure 6 shows an image of a BB at low (a) and high magnification (b) taken close to  $z_{\text{max}}$ . The BB exhibits numerous rings ( $n_{\text{rings}} = \frac{D}{2} \cdot k_r = 25$ ) and a central maximum with a full-width at half maximum of 4 Å. Although the central beam diameter is small, the intensity in the central maximum represents only a small fraction of the overall beam intensity. In fact, the reduced intensity in the central maximum is an intrinsic feature of non-diffractive beams and the intensity is approximately given by  $1/n_{\text{rings}}$ . This leads to a lower signal-to-noise ratio if applied in STEM as the high-resolution signal stemming from the central maximum is weak compared to the contribution from the surrounding rings. Additionally, the aperture diameter  $D = 10 \mu\text{m}$  is small compared to typical STEM apertures with diameters between 50 and 150  $\mu\text{m}$  meaning that the overall intensity is small. These effects make STEM imaging with the beam displayed in figure 6 not beneficial.

A comparison between the experimentally obtained beam size of 4 Å with the size expected from the PM parameters without a focusing lens allows to determine the demagnification. The theoretical beam size can be calculated from the first zero of the Bessel function which lies at  $d \approx \frac{2}{k_r}$  which amounts to 0.4  $\mu\text{m}$  for the implemented PM with  $k_r = 5 \mu\text{m}^{-1}$ . The achieved demagnification thus is  $1/M = 1000$ .

To increase both the overall intensity and the relative intensity of the central maximum, we chose to increase the PM diameter while simultaneously decreasing  $k_r$  and thus  $n_{\text{rings}}$ . As this leads to larger sizes of the central



maximum, the demagnification achievable by implementation of the PM in the C2 aperture is not sufficient to generate reasonably small central beam sizes. Therefore the next section contains the results obtained from an implementation of respective PMs above the C1 condenser lens of a Hitachi HF-3300.

#### 4.2. PM in C1 condenser aperture

Figure 7 shows a schematic drawing of the electron-optical setup of the Hitachi HF-3300 with cold field emission source operated at 300 keV used for the experiments. We implemented a PM ( $D = 50 \mu\text{m}$ ,  $k_r = 0.4 \mu\text{m}^{-1}$ ) in an aperture just above the C1 lens and used the C1 lens and the OLs prefield to generate a BB at the sample plane. In this setup we achieved a high demagnification at a moderate convergence semi angle  $\alpha$ . The C1 lens excitation can be used to either obtain an image (high excitation, green lines in figure 7) or a diffraction pattern (low excitation, blue lines) of the PM in the sample plane. As the BB evolves in the Fresnel regime between image and diffraction plane, the C1 lens excitation is adjusted in between these excitations to obtain a BB in the sample plane.

In this setup the physical distance  $d_{\text{phys}}$  between PM and sample is fixed. By changing the C1 lens excitation, the effective propagation distance  $d_{\text{eff}}$  of the BB between PM and sample plane can be expressed by equation (4):

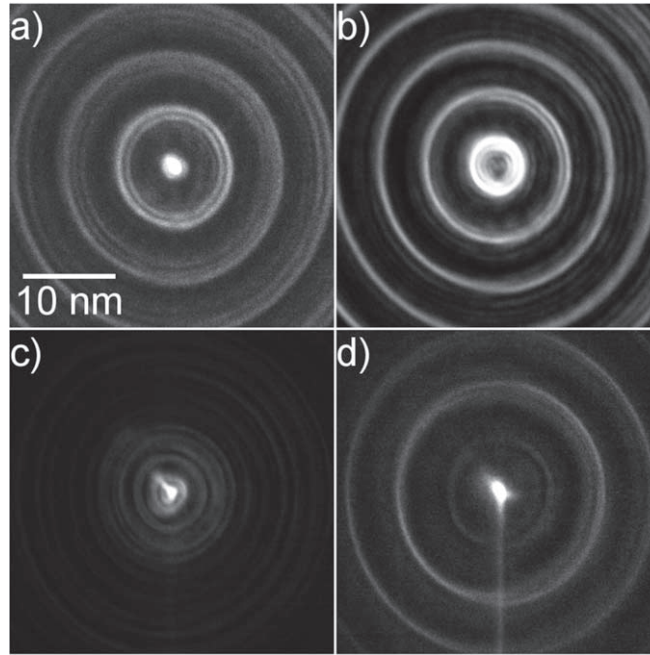
$$d_{\text{eff}}(I_{\text{C1}}) = \frac{d_{\text{phys}}}{M(I_{\text{C1}})}$$

$$M(I_{\text{C1}}) = c_{\text{demag}} \cdot (I_{\text{C1}} - I_{\text{C1,BFP}}) \quad (4)$$

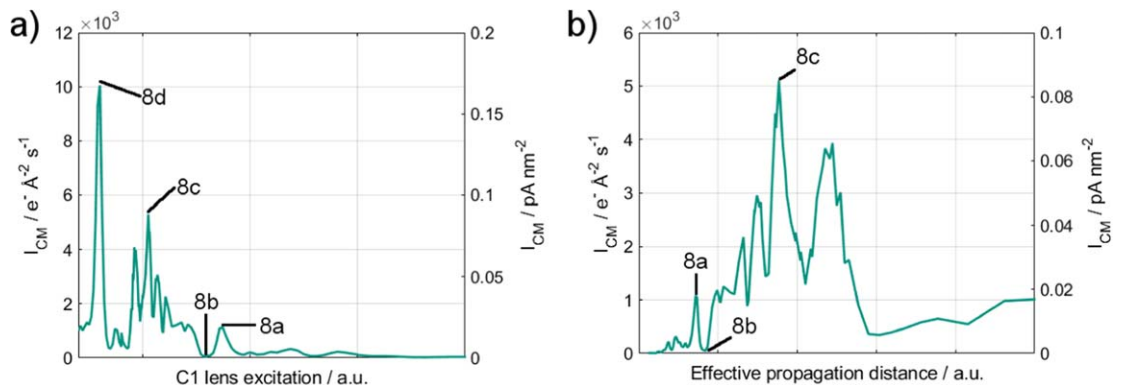
$I_{\text{C1}}$  is the C1 lens excitation,  $I_{\text{C1,BFP}}$  is the C1 lens excitation for which a diffraction pattern of the PM is observed, and  $M(I_{\text{C1}})$  is the demagnification of the PM in the sample plane in dependence of  $I_{\text{C1}}$ .  $M(I_{\text{C1}})$  is expressed by means of a fitting constant  $c_{\text{demag}}$  which is determined by measuring the demagnification of the PM in the sample plane in dependence of  $I_{\text{C1}}$ .

We acquired an image series of the generated BBs with  $I_{\text{C1}}$  being varied between image plane and BFP of the PM. The BBs were recorded using the conventional TEM mode of the imaging lenses, a Gatan Ultrascan 1000 camera and MAESTRO scripting [26]. The movie of the image series can be found in supplementary movie 3 [stacks.iop.org/NJP/21/033007/mmedia](https://stacks.iop.org/NJP/21/033007/mmedia). Figure 8 shows four characteristic BBs taken from the series. A BB observed close to the image plane is depicted in figure 8(a) which reveals a bright maximum with a diameter of  $\approx 5 \text{ \AA}$  surrounded by rings as expected for a Bessel function of 0th order and first kind. The image displayed in figure 8(b) reveals a BB with a central minimum obtained for a slightly lower C1 lens excitation which is however still in the Fresnel regime of the PM. The BB with the highest intensity of the central maximum is shown in figure 8(c). Due to the larger demagnification at this plane, the distance between the central maximum and its surrounding rings is strongly decreased compared to figures 8(a) and (b). Additionally, minor distortions are visible in the image, which could be attributed to aberrations, the fact that the PM was slightly tilted relative to the incident beam, imperfections in the PM structure and also to a high value of  $\phi_a$  (see following section). The





**Figure 8.** Example images obtained from a PM with a grating of  $0.4 \mu\text{m}^{-1}$  acquired using a Hitachi HF-3300. (a) and (b) BBs observed in the Fresnel regime close to the image plane of the PM. (c) The BB obtained close to  $z_{\text{max}}$  shows a small distance between the central maximum and the surrounding rings. (d) BFP of the PM. The vertical streak results from the fast readout of an electron beam with high intensity.



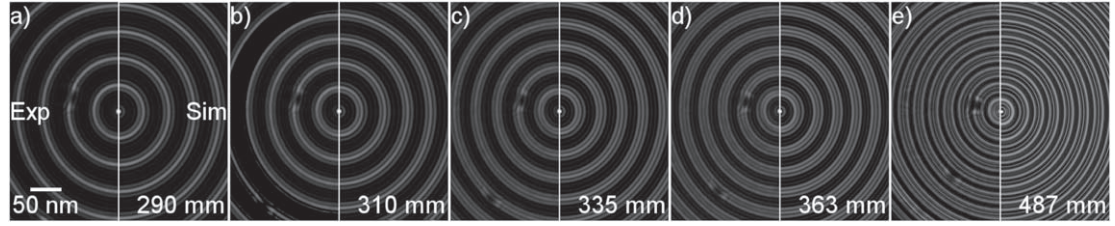
**Figure 9.** Experimentally observed  $I_{\text{CM}}$  in  $\text{e}^- \text{Å}^{-2} \text{s}^{-1}$  (left axis) and  $\text{pA nm}^{-2}$  (right axis) in dependence of (a) the C1 lens excitation  $I_{\text{C1}}$  and (b) the calculated effective propagation distance  $d_{\text{eff}}$ .

diffraction pattern of the PM (figure 8(d)) closely resembles the BB from (a) but exhibits a more pronounced central maximum. An estimation of the demagnification in this setup yields  $1/M = 10^4$ .

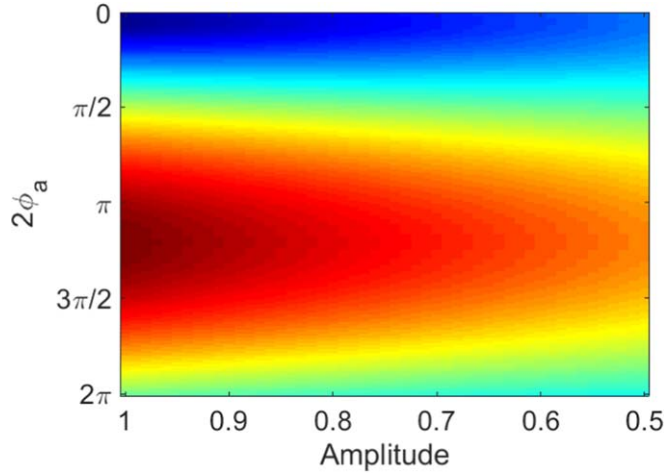
Similar to the LM setup (figure 3), we determined  $I_{\text{CM}}$  of the BB in  $\text{e}^-$  per  $\text{Å}^2 \text{s}$  which can be plotted in dependence of  $I_{\text{C1}}$  (figure 9(a)) as well as of  $d_{\text{eff}}$  (b), which is calculated with the help of equation (4). As the physical distance  $d_{\text{phys}}$  between PM and sample plane is not exactly known, the calculation of  $d_{\text{eff}}$  is only qualitative. The values of  $I_{\text{C1}}$  for which the images in figure 8 were acquired are marked at the respective values of  $I_{\text{C1}}$  and  $d_{\text{eff}}$  in figure 9. The BFP of the PM can be recognized by the highest peak at low  $I_{\text{C1}}$  (figure 9(a)) which is not plotted in (b) as it is located at very high  $d_{\text{eff}}$ . While the dependence of  $I_{\text{CM}}$  on  $I_{\text{C1}}$  can be described as reciprocal (figure 9(a)), the evolution shows the expected oscillations superimposed onto a linear increase in dependence of  $d_{\text{eff}}$  (b).

#### 4.3. Simulations of BB propagation

Simulations of the electron-beam evolution after transmission through the PM are conducted by Fresnel propagation using an in-house written Matlab program (The Mathworks). The simulations can be compared with the experimental results and allow a search of PM parameters for the generation of optimum BBs. To



**Figure 10.** Comparison of experimental (left) and simulated BBs (right) shows very good agreement for different effective propagation distances.



**Figure 11.** Simulated intensity of  $I_{CM}$  of a BB with  $k_r = 5 \mu\text{m}^{-1}$  and  $D = 10 \mu\text{m}$  propagated 432 mm ( $0.86 \cdot z_{\text{max}}$ ) after transmission through the PM in dependence of the phase ( $\phi_a$ ) and amplitude modulation ( $A_a$ ) of the generating PM.  $I_{CM}$  is color coded from blue (low intensity) to red (high intensity). The optimum PM induces a pure phase modulation of  $2\phi_a \approx 1.2\pi$ .

determine the actual phase and amplitude modulation  $\phi_a$  and  $A_a$  of a PM and the mean inner potential  $V_{\text{MIP}}$  as well as the mean free path  $\lambda_{\text{mfp}}$  of  $\text{Si}_3\text{N}_4$ , we compared simulated with experimentally observed BBs. The intensity in the object plane  $I_{\text{OP}} = |\Psi_{\text{OP}}|^2$  is calculated by Fresnel propagation of the electron wave function after transmission through the PM  $\Psi_{\text{PM}}$ :

$$\Psi_{\text{OP}} = \text{FT}^{-1}[\text{FT}(\Psi_{\text{PM}}) \cdot \exp(-i\pi\lambda d_{\text{eff}}k^2)] \quad (5)$$

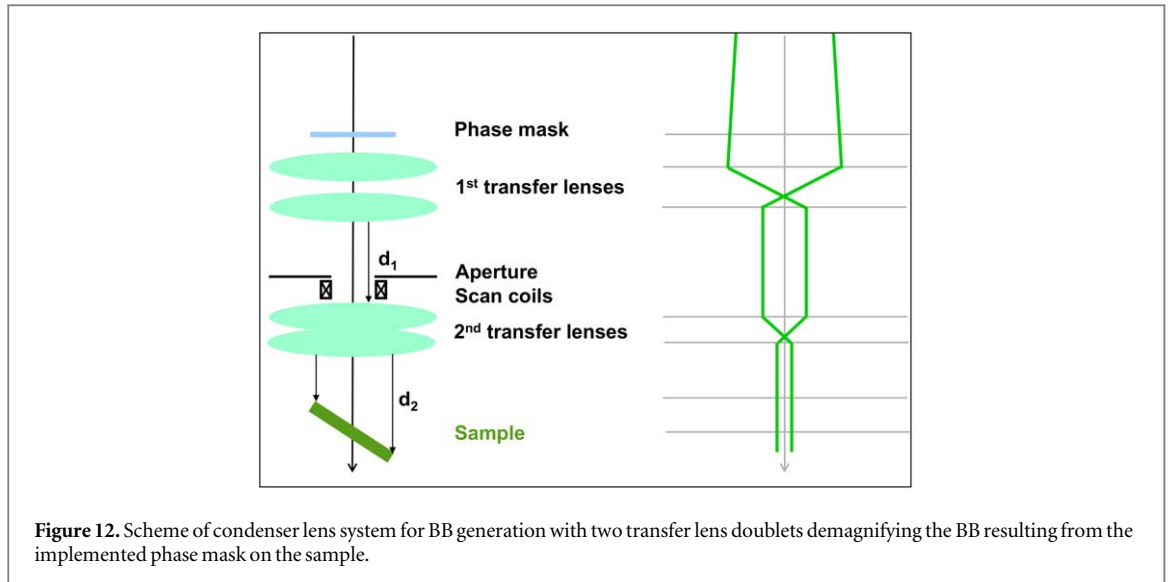
$$= \text{FT}^{-1}\left[\text{FT}\left(\Phi(r) \cdot \exp\left(-\frac{T(r)}{\lambda_{\text{mfp}}}\right)\right) \cdot \exp(-i\pi\lambda d_{\text{eff}}k^2)\right] \quad (6)$$

with the spatial frequency at the PM plane  $k$ . We calculated  $I_{\text{OP}}$  without consideration of a demagnifying lens using  $d_{\text{eff}}$  and then demagnified the simulated beam by the experimentally determined  $M(I_{\text{Cl}})$ . Additionally, we included a slight PM tilt which leads to an elliptical deformation of the rings (figure 10). We then varied  $\phi_a$ ,  $\lambda_{\text{mfp}}$  and  $d_{\text{phys}}$  from which we calculated the different  $d_{\text{eff}}$  for each image using the applied  $I_{\text{Cl}}$  and equations (4) and (6). The simulated images were then compared to the experiment and the optimum values of  $\phi_a$ ,  $\lambda_{\text{mfp}}$  and  $d_{\text{phys}}$  were obtained by least-square fitting.

Figure 10 shows the comparison between five experimental BBs (left) acquired with a PM ( $k_r = 0.4 \mu\text{m}^{-1}$ ,  $D = 50 \mu\text{m}$ ) and corresponding simulations (right). We chose BBs obtained in the near field of the PM with effective propagation distances of below 500 mm ( $< 0.02 \cdot z_{\text{max}}$ ) where the demagnification is still small.

Simulation and experiment agree very well except for minor point defects in the experiment which stem from local imperfections of the PM. We obtained a phase amplitude of  $2\phi_a = 2.3 \cdot \pi$  which leads to  $V_{\text{MIP}} = 14\text{--}15 \text{ V}$  for the used  $\text{Si}_3\text{N}_4$  which agrees very well with the value of  $V_{\text{MIP}} = 13.5 \pm 0.5 \text{ V}$  determined by electron holography. The total mean free path for the best fit is  $\lambda_{\text{mfp}} = 180 \text{ nm}$ .

To find an optimum value for the phase amplitude  $\phi_a$  of the PM regarding a potential application, we conducted simulations of the BB evolution. Figure 11 shows a result with the intensity of the central maximum  $I_{\text{CM}}$  being the evaluation criterion. The simulations were conducted with PM parameters of  $D = 10 \mu\text{m}$  and  $k_r = 5 \mu\text{m}^{-1}$  and with an electron energy of 300 keV. Figure 11 shows the value of  $I_{\text{CM}}$  of a BB propagated



432 mm ( $0.86 \cdot z_{\max}$  after transmission through the PM in dependence of the phase shift  $2\phi_a$  and the amplitude modulation  $2A_a$  induced by the PM. The highest intensity (red) is reached for a pure phase shift of  $1.2\pi$  and decreases with both de- and increasing amount of phase shift as well as with increasing amplitude modulation.

The simulations suggest that  $\phi_a = 2.3\pi$  of the PM implemented in the Hitachi HF-3300 is not ideal as it differs from a phase shift of  $1.2\pi$ . A more detailed analysis of the simulations show that the propagation distance at which the maximum value for  $I_{CM}$  is obtained, decreases with increasing  $2\phi_a$  above  $1.2\pi$ . Above this propagation distance, the BB gets distorted which is in agreement with the experimental finding of the distorted appearance of the BB for larger propagation distances (figure 8(c)). The effect of a focusing lens is neglected in the simulations and is responsible for the further increasing  $I_{CM}$  for higher effective propagation distances in the experiment (figure 9(c)) as it demagnifies the BB and thus increases the beam current density.

## 5. Potential applications of BB

We succeeded to generate BBs with an Å-sized central maximum in the sample plane of a transmission electron microscope. In addition, our experimental results agree very well with theory and with simulations. Nevertheless, STEM imaging with the presented BBs is not beneficial compared to conventional STEM probes. Here we discuss the limitations and propose further optimization to be considered in order to exploit the beneficial characteristics of BBs and to be able to compete with existing conventional STEM probes. We finally present a range of techniques in which such optimized BBs could be applied.

BBs develop in the Fresnel regime of a direct PM. As the electron optics of the condenser lens system of transmission electron microscopes is designed to create either an image or a diffraction pattern of a condenser aperture in the sample plane, they are not ideally suited for BB generation. Figure 12 shows a sketch of a potential lens setup with two transfer lens doublets. The PM with periodicity  $k_r$  is illuminated with an electron wave with a very low convergence (plane wave) and the following transfer lens doublet demagnifies the PM by a factor of  $M1$  which simultaneously decreases  $z_{\max}$  and increases  $k_r$ . In the following free space with length  $d_1$ , the BB can evolve. Finally, the second transfer lens doublet further demagnifies the BB ( $M2$ ) on the sample. Fresnel diffraction at the edge of the PM, as well as the outer rings of the BB can be blocked by an obstructing aperture shortly before the second transfer lens doublet without destroying the non-diffractive property in the necessary range of working distance ( $d_2$ ). Two pairs of scan coils located below the aperture allow to scan the beam over the sample. If designed appropriately, the setup allows PMs with different properties ( $D, k_r$ ) as the physical propagation distances  $d_1$  and  $d_2$  can be tuned to the necessary effective propagation distances by adjusting the lens currents.

There are two main fields of potential applications for BBs: first, in imaging modes where a large focal depth is required. Large focal depths would be highly beneficial in scanning EM, where large differences in working distances ( $=d_2$ ) are very common. Focused imaging of samples located at different working distances would be possible with BBs. In STEM conducted in a TEM, BBs are promising in tomography where high sample tilts are applied and a high DOF is necessary to image the whole sample area in focus [27].

As already stated above, the non-diffractive property of the electron beams comes at the expense of a reduced intensity in the central maximum. To keep the reduction of the signal-to-noise ratio at a tolerable value, the

number of rings should be chosen adequately. A value of  $n_{\text{rings}} = 5$ , which implies that roughly 20% of the intensity is allocated in the central maximum, has already been successfully applied in light microscopy [22].

The second field of application are dose-dependent processes. The central maximum of the BB only represents a fraction of the total intensity in the beam which decreases the signal-to-noise ratio if the BB is used for imaging. However, the areal dose in the central maximum is tremendously larger than in the surrounding rings. If BBs are applied in dose-dependent processes such as lithography or electron-beam manipulation [28], the surrounding rings only represent a small dose which could potentially be tolerated.

## 6. Conclusions

Direct PMs are well suited to generate quasi non-diffractive electron BBs for application in EM. The following conclusions can be drawn from our results obtained by experiment and simulation:

- We optimized the fabrication process of direct PMs by applying a lift-off process to create Pt apertures and custom circular scan routines for FIB milling of the necessary thickness profile. This leads to an enhanced homogeneity of the PM and to an improved quality of the generated electron beams.
- The electron-beam evolution of BBs can be analyzed in great detail by using the PM as specimen in a transmission electron microscope. The experiments reveal, e.g. the quasi non-diffractive behavior, the Bessel-type beam shape and the oscillating increase of the intensity of the central maximum which is predicted by theory.
- The implementation of a PM in the condenser aperture allows the generation of BBs in the specimen plane and their control by the condenser lens system. A high demagnification of the PM in the order of  $10^4$  is achieved in a Hitachi HF-3300.
- Simulations show good qualitative agreement with the experimental results and can be used to derive PM parameters for generation of optimum BBs.
- To find an optimum design of the PM, three parameters have to be considered: the diameter  $D$ , the Bessel frequency  $k_r$ , and the phase amplitude  $\phi_a$  of the PM. While  $D$  should be chosen similar to conventional EM apertures for high-resolution application,  $k_r$  may be defined by the desired number of rings  $N$  from the relation  $N = D \cdot k_r$ . Simulations show that  $2\phi_a = 1.2\pi$  leads to a BB with the highest intensity.
- We propose a four lens condenser system with which the application of BBs could be optimized and which would allow the beneficial application of BBs in, e.g. scanning electron microscopy.

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