

# On Preserving Secrecy in Mobile Social Networks

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Location-based services are one of the most important services offered by mobile social networks. Offering this kind of services requires accessing the physical position of users together with the access authorizations, i.e., who is authorized to access what information. However, these physical positions and authorizations are sensitive information which have to be kept secret from any adversary, including the service providers. As far as we know, the problem of offering location-based services in mobile social networks with a revocation feature under collusion assumption, i.e., an adversary colludes with the service provider, has not been studied. In this paper, we show how to solve this problem in the example of range queries. Specifically, we guarantee any adversary, including the service provider, is not able to learn (1) the physical position of the users, (2) the distance between his position and that of the users, and (3) whether two users are allowed to learn the distance between them. We propose two approaches namely two-layer symmetric encryption and two-layer attribute-based encryption. The main difference between them is that they use, among other encryption schemes, symmetric and attribute-based encryption, respectively. Next, we prove the secrecy guarantees of both approaches, analyze their complexity and provide experiments to evaluate their performance in practice.

CCS Concepts: • **Security and privacy** → **Social network security and privacy**; *Mobile and wireless security*.

Additional Key Words and Phrases: mobile social networks; access control; location-based services

## 1 INTRODUCTION

### 1.1 Motivation

Mobile Social Networks (mSNs) like Foursquare or Badoo have become popular in the last years. Similarly to traditional social networks, mSNs allow users to create virtual communities to share content, but they also let users share their physical position with other users. Having access to the physical position of the users, mSNs offer location-based services (LBS) such as querying friends within a given distance. In this kind of network, each user specifies who is authorized to learn information about his physical position, i.e., users establish authorization relationships with others. Next, given the dynamic relationships between users that are inherent to human behavior, revocation of such privileges is a fundamental feature of mSNs.

To deliver services in mSNs, one can consider different architectures with various components [15]. The three major components are service providers, mobile users, and network infrastructure. Depending on the features supported by mSNs, the service providers can be dedicated servers (e.g., location server or access control server) that give services to the users through the network infrastructure [15]. Mobile users (e.g., mobile phones, wearable devices) receive data or service results from the service providers. The network infrastructure transfers data from a source (e.g., service providers) to a destination (e.g., mobile users). A typical mSN architecture consists of users and two service providers: the LBS provider and the access control server (ACS). This architecture is enough to provide typical LBS and has been considered by existing work in the area [25, 26, 43]. The LBS provider stores the positions of the users, and the ACS stores the authorization relationships.

The physical positions of the users and authorization relationships are sensitive information that should be kept secret from any adversary, including the service providers. This information is particularly sensitive since it can be used to infer further personal information, e.g., one can use the position of the users to infer their state of health or personal preferences [3]. The number of users

of these services may indicate a lack of secrecy concerns. However, studies [33, 44] have shown that mobile users are not aware of various important characteristics of these systems: the data they collect, who is using the data, and how they use it. That is, issues regarding mobile secrecy remain poorly understood by end-users. We also argue that many users use these services without explicitly criticizing secrecy not because they are careless about their secrecy, but because they do not have a choice. Once the secrecy problems with LBS are solved, users may then switch to more secure systems when they become available. Consequently, the information stored by these systems has to be kept secret from unauthorized users, i.e., confidentiality.

Confidentiality is usually facilitated by trusting the entity in the system that manages the access policies, i.e., the ACS. However, recent privacy breaches on existing social networks, such as the Facebook–Cambridge Analytica scandal [12], have put this into question. In such attacks, the ACS has allowed unauthorized entities, intentionally or unintentionally, to access private information. Collusion attacks where adversaries, including malicious users, collude with the service provider to gain unauthorized access to information, are an important problem in mSNs.

This paper studies how to facilitate LBS in mSNs while providing secrecy guarantees to the users under collusion assumption. We focus on one specific service, namely querying friends within a given distance. As motivated earlier, we also cover revocation. Regarding collusion, we study the case of pairwise collusion in which a user colludes with either the LBS provider or the ACS to try accessing unauthorized information. In Section 2.2, we define our adversary model. Regarding secrecy guarantees, we provide users with the following guarantees:

$G_{position}$ : Given a user  $U$ , only authorized entities can learn the physical position of  $U$ .

$G_{distance}$ : Given a user  $U$ , only authorized entities can learn the distance between their physical position and the one of  $U$ .

$G_{authorization}$ : Given two users  $U$  and  $V$ , an adversary will not be able to learn whether  $U$  or  $V$  are allowed to learn the distance between them.

Existing work [25, 26, 48], either does not consider collusion attacks or their system architectures assume trusted entities, which does not solve the collusion problem but shifts it to the trusted entity. Besides, these approaches do not provide a rigorous specification of the collusion strategy as part of their adversary model, and they consider weaker adversaries, see Section 2.2. Next, none of the existing work we are aware of does protect  $G_{authorization}$  against both the LBS provider and ACS.

## 1.2 Challenges

Encryption techniques are an effective way to keep the information secret from all but those who are authorized to access it, without the presence of a trusted entity [29]. However, offering the secrecy guarantees  $G_{position}$ ,  $G_{distance}$  and  $G_{authorization}$  under our collusion assumption with a revocation feature in mSNs is challenging. First, the weak computing power of mobile devices requires mobile users to outsource any heavy computation task. This not only restricts the choice of encryption schemes that can be used but also the design alternatives for a solution.

Second, due to the collusion assumption, the typical encryption guarantee that only holders of the right key can decrypt the information does not hold anymore. If an entity  $A$  that is not authorized to decrypt a given ciphertext  $c$  colludes with an authorized entity  $B$ ,  $A$  can get the decryption key from  $B$  or send  $c$  to  $B$  to decrypt it and get back the plaintext. To solve this issue, one can add further entities in the system, use multi-layer encryption, and assign the keys of the encryption layers to the entities. Such an assignment has to ensure that in case of collusion, the entities cannot access to unauthorized information, i.e., they cannot access either the ciphertext or at least one key of a non-colluding entity to decrypt all encryption layers. Indeed, multi-layer encryption with an adequate key distribution among the entities of the system is the core idea

of our solution, as we explain in Section 4. Multi-layer encryption has been used previously in systems like CryptDB [38], but the context is different from ours. In CryptDB, each encryption layer gives a higher security level but reduces the capability of performing computation over the encrypted data. Users in CryptDB have all the keys to decrypt the encryption layers and use these keys during query processing.

Third, in a multi-user setting, such as our mSN scenario, several owners want to share information with authorized users. To this end, one can consider two main encryption schemes: symmetric and attribute-based encryption (ABE). Both schemes have advantages and disadvantages when comparing them to each other. The advantage of symmetric encryption schemes is the efficiency in the encryption/decryption operations. In the multi-user setting, however, key management and revocation are known problems of these schemes that could overcome their advantage if not implemented appropriately. Section 4.1 features an example illustrating that seemingly simple solutions based on symmetric encryption schemes are not adequate, i.e., the illustrated solution has a huge resource consumption in terms of storage and CPU usage, and users have to be online during revocation. In contrast, an approach that uses ABE has two advantages: One does not need to deal with multiple ciphertexts, and key management and revocation are straightforward. ABE generates a single ciphertext based on an access control policy so that only users whose attributes fulfill the policy can decrypt it. However, its encryption/decryption process involves bilinear pairing and exponentiation operations, which in general have a significant impact on performance [34]. We show that both approaches can solve the problem of sharing information in the multi-user setting if implemented appropriately. However, based on the pros and cons of both encryption schemes, it is not obvious to determine which one performs better in our specific scenario.

### 1.3 Contributions

This paper proposes two approaches, which combine existing encryption schemes, to allow users of mSNs to query friends within a given distance. Both approaches include a revocation feature and provide users with the secrecy guarantees  $G_{\text{position}}$ ,  $G_{\text{distance}}$  and  $G_{\text{authorization}}$  under the collusion assumption. We start by describing our problem and our adversary model. Next, we present our approaches, namely two-layer symmetric encryption (*2ISE*) and two-layer attribute-based encryption (*2LABE*). The main difference between them is that they use, among other encryption schemes, symmetric encryption and ABE, respectively. We prove that both approaches fulfill our secrecy guarantees and analyze their time complexity to evaluate their performance. Our analyses tell us which approach is better at each entity involved in the system. Finally, we conduct experiments to validate the results of our complexity analyses and to determine which approach performs better in practice. Next to other insights, despite the advantages of the *2LABE* approach compared to the *2ISE*—a more straightforward key-management and the storage of a single encrypted copy of each message at the service provider—, we have found that the *2ISE* approach is on average twice as efficient in our scenario. Therefore, we propose to consider the *2ISE* approach, which not only solves the secrecy problem existing in mSNs but also is more performant than the *2LABE* approach.

## 2 PROBLEM FORMULATION

### 2.1 System Architecture

To provide LBS, mSNs require for each user  $u$ : (1) the physical position of  $u$  denoted by  $p_u = \langle x_u, y_u \rangle$ , (2) the set of users who have allowed  $u$  to learn the distance between their position and the one of  $u$ ,  $Grantor_u$ , and (3) the set of users to whom  $u$  has allowed to learn the distance between his position  $p_u$  and their positions, called the set of grantees of  $u$ ,  $Grantee_u$ . We assume that an off-the-shelf positioning technology like GPS, GSM, or BLE inputs the physical position of the user in the system,

and we consider a periodic positioning update policy [47]. Our system takes the physical positions as delivered by the positioning technology used. We assume further that the positions of the users that are input to the system are real, i.e., users have honestly disclosed their location and have not manipulated it. We deem this assumption realistic – one can facilitate it by using technology such as hardware trusted sensors [40], which provide a signature to verify the validity of the position, or deep learning techniques, which detect abnormal traffic patterns to some extent [37].

As mentioned in Section 1, we consider a mSN system consisting of users and two service providers: the LBS provider and the ACS, which store the physical position and the sets of grantors and grantees of each user, respectively. In addition to these entities, there is a key-authority responsible for key issuing. Figure 1 illustrates our system architecture. We have omitted from the architecture illustration components related to the physical and network layers, such as physical transmission medium and routers, to focus on the essence of our work. One can integrate our system into other kinds of architectures like IoT by placing the physical devices of our system (positioning and smart devices) at the perception layer, the network technology at the communication layer, the cloud platform at the middleware layer, and the LBS application at the application layer.

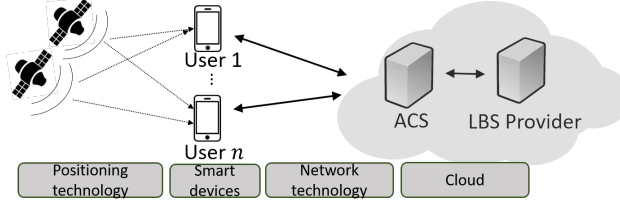


Fig. 1. mSN System Architecture

Users can update their position and allow or revoke access from users at any time. Users send access requests, Definition 2.1, to others to establish who can learn the distance between their physical positions. To avoid that the servers learn information from the stored data, the users must encrypt the information before outsourcing it. To obtain LBS, users send their queries to the ACS. The ACS and the LBS provider interact with each other to compute the query result, which the ACS sends to the user (see Section 4 for details). LBS support different types of queries. Here, we focus on range queries, one of the most important queries in mSNs [51]. Let  $U$  and  $dist^1 p_u; p^o$  denote the set of all users and the distance between the physical positions of users  $u$  and  $p^o$ , respectively.

*Definition 2.1 (Access request).* An **access request**  $accessReq : U \times U \rightarrow \{true, false\}$  is a function that takes as input two users  $u; p \in U$  and indicates that user  $u$  requests  $p$  for permission to *learn* the distance between their physical positions. The function  $accessReq^1 u; p^o$  outputs *true* if  $p^o$  authorizes the access request. Otherwise, it outputs *false*. We call a user who authorizes an access request and a user who receives an authorized access request, grantor and grantee, respectively.

*Definition 2.2 (Range query).* Given a user  $u$  and a distance  $d$ , a **range query**,  $Ran^e^1 u; d^o$ , is a query that returns the users who are located within a distance  $d$  from  $u$  and who have authorized  $u$  to learn the distance between their physical positions and the one of  $u$ . Formally,  $Ran^e^1 u; d^o = \{ p \in U \mid \exists Grantor_u \wedge dist^1 p_u; p^o \leq d \}$ .

## 2.2 Adversary Model and Secrecy Guarantees

To formally define an adversary model under a collusion assumption, one needs to specify four aspects [19]: (1) the collusion strategy, i.e., when or how entities come under the control of the adversary, (2) the computational strategy, i.e., the computational complexity the adversary is

assumed to have, (3) the adversarial behavior strategy, i.e., the actions that the colluding entities might take, and (4) the protocol execution strategy, i.e., how many times the adversary is allowed to execute the protocol. Next, we describe the main alternatives for each of these four aspects briefly and specify ours. We define our model based on a *just-strong-enough* principle, in which the selected alternatives for each of these aspects are just strong enough to model real-world adversaries under a collusion assumption with revocation capability, as we explain in the remaining of this section. Studying more complex settings that consider stronger adversary models is future work.

**Collusion strategy:** The main collusion strategies are: static and adaptive [19]. In the static strategy, the adversary is given a set of entities to collude with, and the honest entities remain honest during the protocol execution. In the adaptive strategy, the adversary can collude with any entity in the system during the protocol execution. Here, we consider the static strategy. Although the static strategy is weaker than the adaptive one, developing highly efficient schemes that are secure under the static strategy serves as an important step for constructing secure schemes under the adaptive one [19]. We refer to any entity that participates in a collusion as an adversary.

**Computational strategy:** The main computational strategies are: polynomial and unbound. In the first one, adversaries run in polynomial time, while in the second one, they do not have computational limits. Similar to existing works [19, 25], we consider the polynomial strategy.

**Adversarial behavior strategy:** The main adversarial behavior strategies are: semi-honest, covert, and malicious [19]. In the semi-honest strategy, every colluding entity follows the protocol specification, i.e., each entity performs the tasks assigned to it correctly. Adversaries can access to the state of all colluding parties to try learning information from it. In the covert strategy, adversaries may deviate from the protocol specification if honest entities fail to detect them. This strategy represents many real-world scenarios like financial or political settings, where the involved entities, i.e., companies or individuals, cannot afford the embarrassment, loss of reputation, and law punishment associated with being caught cheating. In the malicious strategy, the colluding entities can deviate arbitrarily from the protocol specification, according to the instructions of the adversary. Since the security guarantees provided by schemes in the semi-honest strategy are weak, and schemes that offer security guarantees under the malicious strategy are inefficient to be implemented and used in practice [19], we opt for the covert strategy, which represents real-world adversaries. However, since we aim to cover realistic scenarios where unauthorized entities try to gain access to the information, we restrain the covert strategy further. Here, we limit adversaries to deviate from the protocol only to advantage themselves, but they will not disadvantage any entity in the system. Advantaging and disadvantaging an entity means to give the entity unauthorized access to the information and to prevent the entity from accessing authorized information, respectively.

**Protocol execution strategy:** The main protocol execution strategies are: stand-alone and concurrent-composition [9]. In the stand-alone strategy, the adversary is allowed to execute the protocol a single time, while in the concurrent-composition one, he can execute the protocol several times. Considering adversaries in the concurrent-composition strategy is a harder problem to solve, however, having a scheme for the stand-alone strategy can be used to design schemes for the concurrent-composition one [19]. Following our *just-strong-enough* principle for specifying the adversary model, we consider the stand-alone strategy, and we extend it to fulfill our needs. Here, we allow the execution of the protocol twice, which lets us evaluate the secrecy guarantees met after a revocation takes place. Before describing the extension, we explain the need for it. In a single protocol execution, the adversary can (1) collude with the entities of the system based on the defined collusion strategy, (2) send a set of queries, and (3) get their respective answers based on the information stored at each entity of the system at the moment of the protocol execution. In our scenario, the information stored by the entities includes, among others, the encrypted sets of

grantors and grantees of the users. This information stays unmodified during the protocol execution. To evaluate the secrecy guarantees of a scheme under revocation, one needs to change the authorizations, i.e., adjust the set of grantors and grantees of the users involved in the revocation. Therefore, after updating the information, we need to allow the adversary to execute the protocol a second time. In the second protocol execution, the adversary is allowed to repeat the steps (2)-(3) of the first execution, but it is forbidden to collude with any entity. The purpose of the second execution is to evaluate whether a revoked user can gain unauthorized access to information that he could access on the first execution. We call this extension the twofold-composition strategy.

In the remaining of the paper, when we refer to adversaries, we imply adversaries with the power specified in our adversary model. Note that, neither a user is an adversary of himself nor are the entities that a user has allowed them to access his data. Having specified our adversary model, it only remains to define the setting of the static strategy, i.e., specify the possible collusion scenarios.

**Static strategy setting:** Each execution of the protocol involves four entities: the key-authority, a user, the ACS, and the LBS provider. First, the key-authority is an honest entity. We note that the key-authority is only responsible for issuing keys during the registration of users in the system, it does not participate in any other phase of the protocol specification, and it does not store any information. Details of our protocol are in Section 4. Thus, considering the key-authority as an honest entity does not shift the collusion problem to it. Second, the LBS provider, ACS, and the user can be adversaries. However, we limit ourselves to the case of pairwise collusion, which is in line with the selected adversary behavior strategy, i.e., the covert strategy. Since three entities participate in the critical phases of the protocol execution, i.e., access request, query, and revocation phases, at least one honest entity is needed to detect the deviation from the protocol of the adversaries.

In line with existing approaches [26, 48, 53], we assume: the LBS provider and ACS do not collude with each other, and they cannot identify users by observing their IP addresses in the connections. Regarding the first assumption, we find it reasonable because we assume that different companies run the ACS, the LBS provider, and the internet provider. Regarding our second assumption, one can solve it by using hidden IP techniques that guarantee network intractability such as Virtual Private Network services [23], TOR encryption (The Onion Router) [14] or proxy servers [49].

**Secrecy Guarantees:** Based on our adversary model, we aim to offer the secrecy guarantees  $G_{\text{position}}$ ,  $G_{\text{distance}}$  and  $G_{\text{authorization}}$  stated in Section 1.

We note that given a resource  $r$ , an adversary is any entity that is not authorized to access  $r$ . Given a user  $u$ , authorized users, i.e., the grantors of  $u$ , can learn the distance between their position and the one of  $u$ , and the physical position of  $u$ .

### 3 CRYPTOGRAPHIC TECHNIQUES USED

In this section, we define the cryptographic techniques that we consider in our approaches. In Section 4, we explain how we apply them in our scenario. We write  $\text{Enc}^1k; m^\circ$  and  $\text{Dec}^1k; c^\circ$  for the operations of encrypting  $m$  under key  $k$  and decrypting  $c$  under key  $k$ , respectively.

*Definition 3.1 (Symmetric Encryption Scheme).* A **symmetric encryption scheme**  $\mathcal{SE} = \langle \text{KGen}; \text{Enc}; \text{Dec}^\circ \rangle$  consists of three algorithms: (1) A key generation algorithm  $\text{KGen}$  that returns a key  $k$ . (2) An encryption algorithm  $\text{Enc}$  which can be probabilistic or deterministic and takes as input the key  $k$  and a plaintext  $m$  to return a ciphertext  $c$ . (3) A deterministic decryption algorithm  $\text{Dec}$  that takes as input the key  $k$  and a ciphertext  $c$  to return a plaintext  $m$  such that  $\text{Dec}^1k; \text{Enc}^1k; m^\circ = m$ .

*Definition 3.2 (Asymmetric Encryption Scheme).* An **asymmetric encryption scheme**  $\mathcal{AE} = \langle \text{KGen}; \text{Enc}; \text{Dec}^\circ \rangle$  consists of three algorithms: (1) A key generation algorithm  $\text{KGen}$  that returns a pair of public and secret keys  $\langle \text{pk}; \text{sk}^\circ \rangle$ . (2) A probabilistic encryption algorithm  $\text{Enc}$  which takes as input the public key  $\text{pk}$  and a plaintext  $m$  to return a ciphertext  $c$ . (3) A deterministic decryption

algorithm  $\text{Dec}$  that takes as input the secret key  $sk$  and a ciphertext  $c$  to return a plaintext  $m$ , such that  $\text{Dec}^1sk; \text{Enc}^1pk; m^{oo} = m$ .

*Definition 3.3 (Somewhat Homomorphic Encryption Scheme).* A **somewhat homomorphic encryption scheme** (SHE) is an asymmetric encryption scheme in which the message space is a ring  $\langle R; +; \cdot \rangle$  and the ciphertext space is also a ring  $\langle R; +; \cdot \rangle$  such that for all messages  $m_1, m_2 \in R$ , and all pair of keys  $\langle pk; sk \rangle$ ,  $m_1 + m_2 = \text{Dec}^1sk; \text{Enc}^1pk; m_1 \oplus \text{Enc}^1pk; m_2^{oo}$ , and  $m_1 \cdot m_2 = \text{Dec}^1sk; \text{Enc}^1pk; m_1 \circ \text{Enc}^1pk; m_2^{oo}$ . A SHE supports limited computations on ciphertext, i.e., one can perform a limited number of addition and multiplication operations.

We also use Ciphertext-Policy attribute based encryption (CP-ABE) [7]. In CP-ABE, the data is encrypted based on an access policy, which itself consists of constraints on user attributes, like  $role = "student" \wedge memberOf = "Project1"$ . The encryption is done so that only users who fulfill the access policy can decrypt. Formally:

*Definition 3.4 (Ciphertext-Policy Attribute based Encryption Scheme).* A **CP-ABE scheme** consists of four algorithms  $\langle Setup; KGen; Enc; Dec \rangle$  (1) A setup algorithm, *Setup*, that selects two cyclic groups  $G$  and  $G_T$  and use them to generate and return a public key  $pk$  and a master key  $mk$ . (2) A key generation algorithm *KGen* that takes as input a set of attributes  $\mathcal{U}$  associated with a user  $u$  and the master key  $mk$ , to return a secret key  $sk_u$ . (3) A probabilistic encryption algorithm *Enc* that takes as input a message  $m$ , an access policy  $\mathcal{A}$  and the public key  $pk$  to return a ciphertext  $c$ . (4) A deterministic decryption algorithm *Dec* which takes as input the public key  $pk$ , a secret key  $sk_u$  associated with the set of attributes  $\mathcal{U}$  and a ciphertext  $c$  to return a message  $m$  if  $\mathcal{U}$  satisfies the access policy  $\mathcal{A}$ ; otherwise it returns an error message  $\perp$ . We write  $\text{Enc}^1pk; m^{\circ}$  for the operation of encrypting  $m$  under the access policy  $\mathcal{A}$  and key  $pk$ , and  $\text{Dec}^1pk; sk_u; c^{oo}$  for the operation of decrypting  $c$  under the pair of keys  $\langle pk; sk_u \rangle$ .

Note that general CP-ABE schemes do not guarantee the security of the access policy used to encrypt a given ciphertext  $c$ , i.e., an entity who has access to  $c$  can learn who is authorized to decrypt  $c$ . Learning this information is against the secrecy guarantee  $G_{authorization}$  that we aim to offer. However, we consider stronger CP-ABE schemes with *hidden policy* as proposed in [27].

Next, for key distribution, we use in Section 4.1 the Diffie-Hellman key exchange protocol [13].

*Definition 3.5 (Diffie-Hellman key exchange).* The **Diffie-Hellman** key exchange (DH) is a protocol which allows two parties,  $A$  and  $B$ , that have no prior knowledge of each other to establish a shared secret key jointly. The protocol is as follows: First, a trusted party chooses and publishes two integers  $p$  and  $g$ , where  $p$  is large, e.g., 512 bits, and  $g$  is a primitive root modulo  $p$ .<sup>1</sup> Second, the parties  $A$  and  $B$  choose the secret integers,  $a$  and  $b$ , respectively. Next,  $A$  computes  $Z_A = g^a \pmod{p}$  and sends  $Z_A$  to  $B$ .  $B$  computes  $Z_B = g^b \pmod{p}$  and sends  $Z_B$  to  $A$ . Finally,  $A$  computes the shared key  $k_{ba} = Z_B^a \pmod{p}$ .  $B$  computes the shared key  $k_{ab} = Z_A^b \pmod{p}$ . The shared key value is  $k_{ba} = Z_B^a \pmod{p} = g^{b \circ a} \pmod{p} = g^{a \circ b} \pmod{p} = Z_A^b \pmod{p} = k_{ab}$ .

Table 1 summarizes the encryption schemes and the encryption/decryption keys that we use.

## 4 OUR APPROACH

To fulfill the secrecy guarantees, users have to encrypt the information before outsourcing it to the ACS and the LBS provider. There are different possibilities to do so. Due to the decryption and revocation overhead at the users-side, we disregard naive solutions such as the one of Example 4.1. The illustrated solution has the following shortcomings: it affects the storage capacity and limited

<sup>1</sup>A primitive root modulo  $p$  is an integer  $g$  such that  $g \pmod{p}$  has multiplicative order  $p - 1$ .

| Encryption scheme                                     | Enc•Dec Keys                                 | Description  |
|---|--|--|
| Symmetric encryption ${}^1\mathcal{SE}^\circ$         | $k_U$<br>$k_U$                               | Key of user $U$<br>Shared key between users $U$ and  |
| Asymmetric encryption ${}^1\mathcal{AE}^\circ$        | $pk_{ACS}; sk_{ACS}$<br>$pk_{LBS}; sk_{LBS}$ | Public and secret keys of the ACS<br>Public and secret keys of the LBS provider                                      |
| Somewhat homomorphic encryption (SHE)                 | $pk_H; sk_H$                                 | Public and secret keys for SHE   |
| Ciphertext-policy attribute-based encryption (CP-ABE) | $mk_{ABE}; pk_{ABE}$<br>$sk_u$               | Master and public keys for CP-ABE<br>Secret key for CP-ABE of user $U$ , where $u$ is the set of attributes of $U$ , |

Table 1. Summary of Encryption Schemes and the corresponding keys used

processing resources of mobile devices, and revocation is not only inefficient for data owners, but it also requires authorized users to be online. Given a set  $S$ , let  $|S|$  denote the cardinality of  $S$ .

*Example 4.1.* Assume that each user  $U$  encrypts his name with a key  $k_U$ , stores his encrypted name at the LBS provider, and distributes  $k_U$  to all authorized users. Such a solution has several problems. First,  $U$  has to store as many keys as grantors. Second, during query processing,  $U$  receives, as a result, a set of encrypted names corresponding to users who fulfill the query condition. Since  $U$  stores one key for each of his grantors and  $U$  ignores which key to use to decrypt each ciphertext, the decryption process has a worst-case complexity of  $\mathcal{O}(|Grantor_U|)$ . Third, if  $U$  wants to revoke access from a user,  $U$  has to generate a new key  $k_{U'}$ , encrypt his name with  $k_{U'}$ , replace his encrypted name at the LBS provider with the new ciphertext and distribute  $k_{U'}$  to all still authorized users.

Next, we show how to use and combine existing cryptographic techniques to implement a scheme under our secrecy guarantees. We come up with two approaches. To ease the explanation of them, we first start by describing two basic schemes, called basic two-layer symmetric encryption, *basic 2ISE*, and basic two-layer attribute-based encryption, *basic 2IABE*. Our basic schemes meet our secrecy guarantees under a weaker adversary model than the one defined in Section 2.2. With it, we weaken the protocol execution strategy by considering the stand-alone strategy instead of the twofold-composition strategy, i.e., the protocol is executed only once. We then show how to extend the basic schemes to meet our secrecy guarantees under our actual adversary model, Section 2.2.

The main difference between our basic schemes lies on the cryptographic schemes used to encrypt the names which are sent as query answers. The basic schemes consist of four phases: initialization phase, registration phase, access request phase, and query phase. In Sections 4.1 and 4.2, we explain these phases for the *basic 2ISE* and the *basic 2IABE* schemes, respectively.

#### 4.1 Basic two-layer symmetric encryption (*basic 2ISE*)

*4.1.1 Initialization phase.* In this phase, the key-authority generates and distributes keys. The initialization of the system happens once. The entities involved in this phase are the key-authority, the ACS, and the LBS provider. The key-authority generates three pairs of keys  ${}^1pk_{LBS}; sk_{LBS}^\circ$ ,  ${}^1pk_{ACS}; sk_{ACS}^\circ$ , and  ${}^1pk_H; sk_H^\circ$ . These keys are used during the registration, access request, and query phases. The key-authority sends the secret keys  $sk_H$  and  $sk_{ACS}$  to the ACS and the secret key  $sk_{LBS}$  to the LBS provider. It also chooses the integers  $p$  and  $q$  of the DH protocol, Definition 3.5, which is used to generate and share secret keys between a pair of users in the access request phase.



4.1.2 *Registration phase.* In this phase, new users register in the system. It involves four entities: the key-authority, the ACS, the LBS provider, and a user  $u$ . Figure 2 shows the steps of this phase.

First, the key-authority sends to  $u$  (1) two identifiers  $id_u^{ACS}$  and  $id_u^{LBS}$ , (2) a secret key  $k_u$ , (3) the public keys  $pk_{LBS}$  and  $pk_{ACS}$ , and (4) the integers  $p$  and  $q$ . Second,  $u$  selects an integer number  $x_u$  and compute the value  $Z_u = g^{x_u} \pmod{p^0}$ . We call  $x_u$  and  $Z_u$  the secret and public numbers of  $u$ , respectively. These two numbers are used as part of the DH protocol in the access request and query phases, as we explain in Sections 4.1.3 and 4.1.4. Next,  $u$  stores at the LBS provider his identifier  $id_u^{LBS}$ , his encrypted position  $Enc^1pk_H; \rho_u^0$ ,<sup>2</sup> and his encrypted public number  $Enc^1pk_{ACS}; Z_u^0$ . The use of SHE allows the LBS provider to compute the encrypted square distance between the encrypted positions of two users. The LBS provider cannot decrypt any of the ciphertexts because it does not have the secret keys. Finally,  $u$  stores at the ACS his identifier  $id_u^{ACS}$  and two empty sets  $Grantor_u$  and  $Grantee_u$ . Information is added to these two sets in the access request phase. We note that neither the LBS provider nor the ACS knows the link between users and their identifiers.

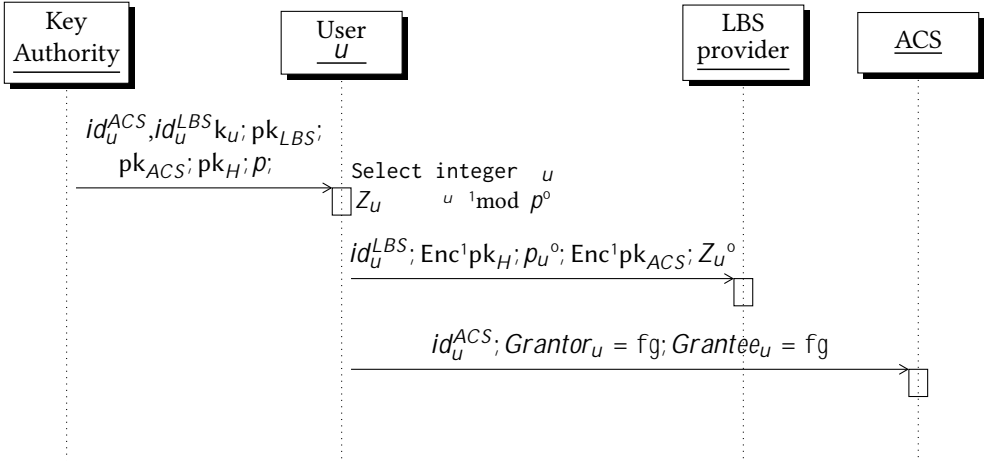


Fig. 2. User Registration Phase - basic 2ISE

4.1.3 *Access request phase.* In this phase, a user  $u$  calls the function  $accessReq^1u; \rho_u^0$ . If user authorizes the access request, i.e.,  $accessReq^1u; \rho_u^0 = true$ , stores encrypted information at the ACS and the LBS provider, as we will explain in this Section. The providers use this information to process queries sent by  $u$ . Before explaining the steps of this phase, let us analyze how query processing works to understand the information that  $u$  has to store. Example 4.2 illustrates two design alternatives, *querying-filtering* and *filtering-querying*, to answer a given range query.

*Example 4.2.* Think of an LBS provider and an ACS. Assume that for each user  $u$ , the LBS provider stores his encrypted physical position using SHE, and the ACS stores the set of grantors  $Grantor_u$ . Different design alternatives are conceivable to answer a given range query. In particular, one can consider two designs: *querying-filtering* and *filtering-querying*. With the first alternative, the LBS provider executes, first, the query and then sends the result to the ACS to filter it based on the set  $Grantor_u$ . With the second alternative, the ACS sends, first, the set  $Grantor_u$  to the LBS provider, and then the LBS provider executes the query using only the physical positions of users in  $Grantor_u$ . With both alternatives, since the LBS provider stores encrypted positions, it cannot

<sup>2</sup>In reality, we encrypt a given position  $\rho_u$  as  $Enc^1pk_H; x_u^0$  and  $Enc^1pk_H; y_u^0$ .

use indexing, like B-tree or R-tree, for spatial query processing. Then in terms of performance, the *querying-filtering* alternative is not a suitable option because

Due to performance reasons, as explained in Example 4.2, we opt for the *filtering-querying* approach. Then the set of grantors of each user  $u$  has to contain information that allows the LBS provider to reduce the computation cost during query execution. Specifically, if  $\text{accessReq}^u; \circ = \text{true}$ , has to add, among other information, his encrypted identifier  $id^{LBS}$  in the set  $Grantor_u$ , and to store his encrypted name at the LBS provider. The encrypted names of the users are sent as query answers, as we explain in Section 4.1.4. The access request phase involves the following entities: the users that are part of the access request,  $u$  and  $\circ$ , the LBS provider, and the ACS. Figure 3 illustrates the steps of this phase. We denote the concatenation of strings  $a$  and  $b$  by  $akb$ .

First, user  $u$  calls the function  $\text{accessReq}^u; \circ$  and sends to user  $\circ$  his identifier  $id_u^{ACS}$  and his public number  $Z_u$ . If  $\text{accessReq}^u; \circ = \text{true}$ ,  $\circ$  computes the shared key  $k_u = Z_u^{-1} \bmod p^\circ$  and selects two random numbers  $r_u^{ACS}, r_u^{LBS} \in \mathbb{Z}$ . Next,  $\circ$  encrypts his name using two layers of encryption.  $\circ$  uses the shared key  $k_u$  for the inner layer of encryption and the public key  $pk_{ACS}$  for the outer layer of encryption. Then,  $\circ$  stores at the LBS provider the resulting ciphertext,  $\text{Enc}^{pk_{ACS}}; \text{Enc}^{k_u}; \circ$ , together with the random number  $r_u^{LBS}$ . The LBS provider cannot decrypt the ciphertext, even if it colludes with any of the users, because none of them has the key to decrypt the outer layer of encryption. Secrecy proofs are in Section 5. Next,  $\circ$  sends to the ACS the identifier of  $u$ ,  $id_u^{ACS}$ , together with a tuple  $t$  which consists of two elements: the random number  $r_u^{ACS}$  and the ciphertext  $\text{Enc}^{pk_{LBS}}; id^{LBS} k r_u^{LBS \circ}$ . The ACS adds  $t$  to the set  $Grantor_u$ . The ACS uses the ciphertext that is part of tuple  $t$  during query processing, as we will explain in the query phase. Note that only  $\circ$  knows his identifier  $id^{LBS}$ , then he is the only one who can add his encrypted id to the set of grantors of other users. Finally, to revoke access,  $\circ$  stores in his set of grantees,  $Grantee$ , at the ACS, the ciphertext  $c = \text{Enc}^{k_u}; uk id_u^{ACS} k r_u^{ACS} k r_u^{LBS \circ}$ .  $c$  contains the name of  $u$  and index information that allows  $\circ$  to revoke access from  $u$ , i.e.,  $\circ$  can delete both the tuple  $t$  added in the set  $Grantor_u$  and the encrypted name stored at the LBS provider. Only  $\circ$  knows the key to decrypt  $c$ .

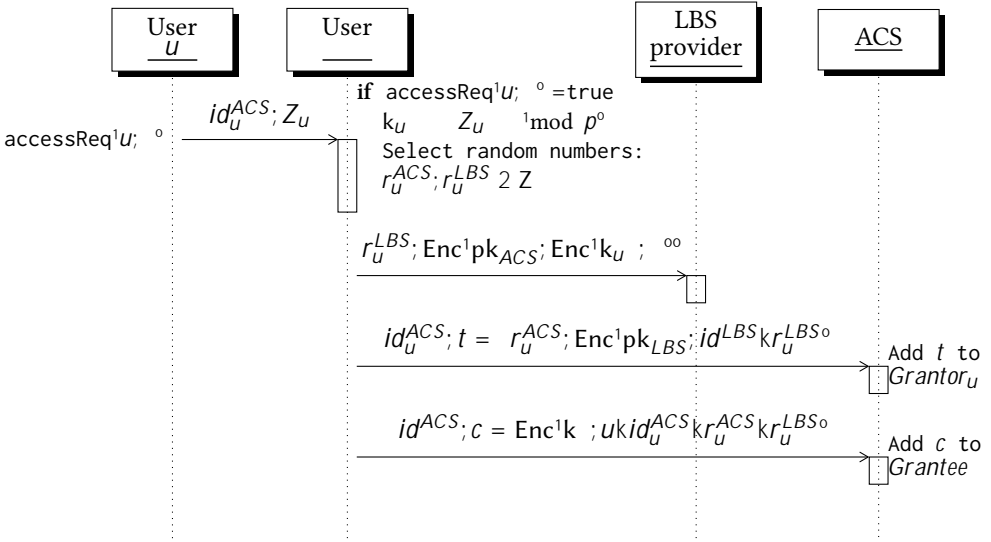


Fig. 3. Access Request Phase - basic 2ISE

**4.1.4 Query phase.** In this phase, users send range queries and get back query answers. This phase involves three entities: the querying user  $u$ , the ACS, and the LBS provider. We use the following notation: Given  $n$  strings,  $st_1; \dots; st_n$ , and the string  $st = st_1 \| \dots \| st_n$ , the function  $et^i(st; i^o$ , where  $1 \leq i \leq n$ , returns the  $i$ -th string in  $st$ . Given a tuple  $t$  which consist of  $n$  elements, we use  $t_i$ , where  $1 \leq i \leq n$ , to denote the  $i$ -th element of tuple  $t$ . Figure 4 illustrates the steps of this phase.

First, the querying user  $u$  sends his identifier  $id_u^{ACS}$ , the constraint  $d$  of the range query and his encrypted position  $Enc^{pk_{LBS}; sk_H}(p_u)$ .  $u$  encrypts his position using two layers of encryption because the encrypted position is sent through the ACS to the LBS provider, and the ACS knows the decryption key  $sk_H$ . The outer layer of encryption prevents the ACS from learning the position of  $u$ . Second, using the id  $id_u^{ACS}$ , the ACS retrieves the set of grantors of  $u$ ,  $Grantor_u$ . Recall that each tuple  $t$  in  $Grantor_u$  consists of two elements, a random number, and a ciphertext. The ACS constructs a set  $C$  that contains the ciphertext of each tuple  $t$  in  $Grantor_u$ , i.e.,  $t_2$ , and sends  $C$  and the encrypted position of  $u$  to the LBS provider. Third, the LBS provider decrypts each ciphertext  $c$  in  $C$  and obtains the plaintext  $st$ , which consists of an identifier  $id$  concatenated with a random number  $rand$ . The LBS provider searches and retrieves the encrypted position and the encrypted public number corresponding to the identifier  $id$ . We use  $p_{id}$  and  $Z_{id}$  to denote the retrieved encrypted position and the encrypted public number, respectively. Using  $p_{id}$  and the encrypted position of  $u$ , the LBS provider computes the encrypted square distance between them,  $Enc^{pk_H}(dist(p_{id}, p_u)^{2o})$ . It also searches and retrieves the encrypted name, corresponding to the number  $rand$ . We denote this ciphertext by  $name_{rand}$ . Then, it creates a tuple  $e$  that contains three elements:  $name_{rand}$ ,  $Z_{id}$ , and  $Enc^{pk_H}(dist(p_{id}, p_u)^{2o})$ . It adds  $e$  to the result set  $Res$  and sends  $Res$  to the ACS. Next, for each tuple  $e \in Res$ , the ACS decrypts the element  $e_3$ , i.e., the encrypted square distance. If the decrypted distance is less or equal than  $d^2$ , the ACS (1) decrypts  $e_1$  and  $e_2$ , i.e., the outer layer of the encrypted name and the encrypted public number, (2) creates a tuple  $l$  containing the decrypted information, and (3) adds  $l$  to the set of answers  $Ans$ . The ACS sends  $Ans$  to  $u$ . Finally, for each tuple  $l$  in  $Ans$ ,  $u$  (1) uses  $l_2$ , i.e., the public number, and his secret number  $s_u$  to compute the shared key  $k_{shared} = l_2^{s_u} \bmod p^o$ , and (2) decrypts  $l_1$ , i.e., the usernames, using  $k_{shared}$ . The decrypted names correspond to users that fulfill the query condition.

Next, we provide a working example to show how our *basic 2LSE* approach works step by step.

**Example 4.3.** Consider two users Alice and Bob. Suppose that Alice wants to query the set of users within a distance  $d$ . Assume further that Bob has allowed Alice to query the distance between their physical positions. Figure 5 illustrates the query processing steps (numbers within black circles). It also contains the information which each entity in the system stores. The data stored in the tables at the LBS provider and ACS is information about Alice and Bob.

## 4.2 Basic two-layer attribute-based encryption (*basic 2LABE*)

To facilitate the understanding, before describing the *basic 2LABE* approach, we specify the differences between our two approaches. With the *basic 2LSE*, the LBS provider stores, for each user  $u$ ,  $|Grantee_u|$  copies of the encrypted name of  $u$ . Each ciphertext is generated using a shared key between  $u$  and each  $g$  in  $Grantee_u$ . The DH protocol is used to generate shared keys. In contrast, with the *basic 2LABE* there is no need to store multiple copies of the encrypted name or to share keys. Instead, each user encrypts his name using CP-ABE, Definition 3.4. Because of the properties of CP-ABE, each user receives a secret key based on his set of attributes, and only users who fulfill the access policy can decrypt a given ciphertext. In Sections 4.2.2 and 4.2.3, we specify the access policy and the set of attributes used for the encryption and decryption process.

Next, we describe the initialization, registration, access request, and query phases of the *basic 2LABE*. For brevity, we only describe the differences between the *basic 2LABE* and *basic 2LSE* schemes.

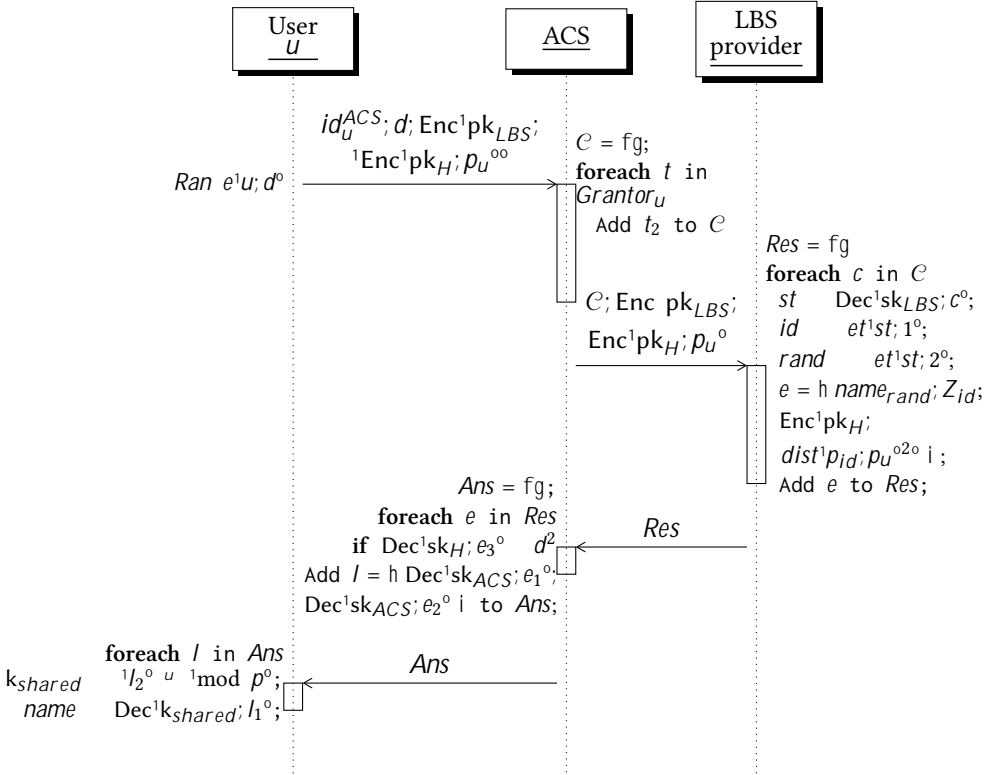


Fig. 4. Query Phase - basic 2ISE

**4.2.1 Initialization phase.** This phase differs from that of the *basic 2ISE*, Section 4.1.1, only in the selection of the parameters  $p$  and  $q$  of the DH protocol. Since the *basic 2IABE* uses CP-ABE, it does not need the DH protocol for generating and sharing keys. The key-authority generates a public key  $pk_{ABE}$  and a master key  $mk_{ABE}$ . It uses these keys during the registration phase (Section 4.2.2). The key-authority keeps  $mk_{ABE}$  secret from all entities.

**4.2.2 Registration phase.** Before explaining the steps of this phase, let us analyze how CP-ABE works in our scenario. The key-authority has to generate a secret key for each user  $u$  using attributes associated with  $u$ . In our scenario, we consider only the attribute *name* of the users. That is because the access policy used in this work considers the names of the users to establish who can decrypt a given ciphertext. If one needs to use other attributes, one has to include them in the set of attributes associated with the users. Given a user  $u$ , the access policy defined by  $u$ ,  $\mathcal{A}_u$ , is a disjunction of terms of the form  $1\text{name}=\text{value}^0$ , where *name* is a user attribute, and *value* refers to an atomic value.

*Example 4.4.* Consider a user  $u$ , the set  $\text{Grantee}_u = \{w\}$ , and a message  $m$ . User  $u$  wants to encrypt  $m$  and allow the users in  $\text{Grantee}_u$  to decrypt it.  $u$  can use the usernames to identify the users in  $\text{Grantee}_u$ , and to generate the access policy  $\mathcal{A}_u$  needed to encrypt  $m$ .  $u$  can specify the access policy  $\mathcal{A}_u = 1\text{name} = w^0$  and generate the ciphertext  $C = \text{Enc}^1pk_{ABE}; m_{\mathcal{A}_u}^0$ .  $u$  indicates that  $C$  can be decrypted by users with name  $w$ . The secret keys of users  $u$  and  $w$  are generated based on their attributes, e.g., the secret key of  $u$ ,  $sk_u$ , is generated based on the set of attributes  $\mathcal{A}_u = 1\text{name} = w^0$ . Only users whose secret key fulfill the access policy  $\mathcal{A}_u$  can decrypt  $C$ .

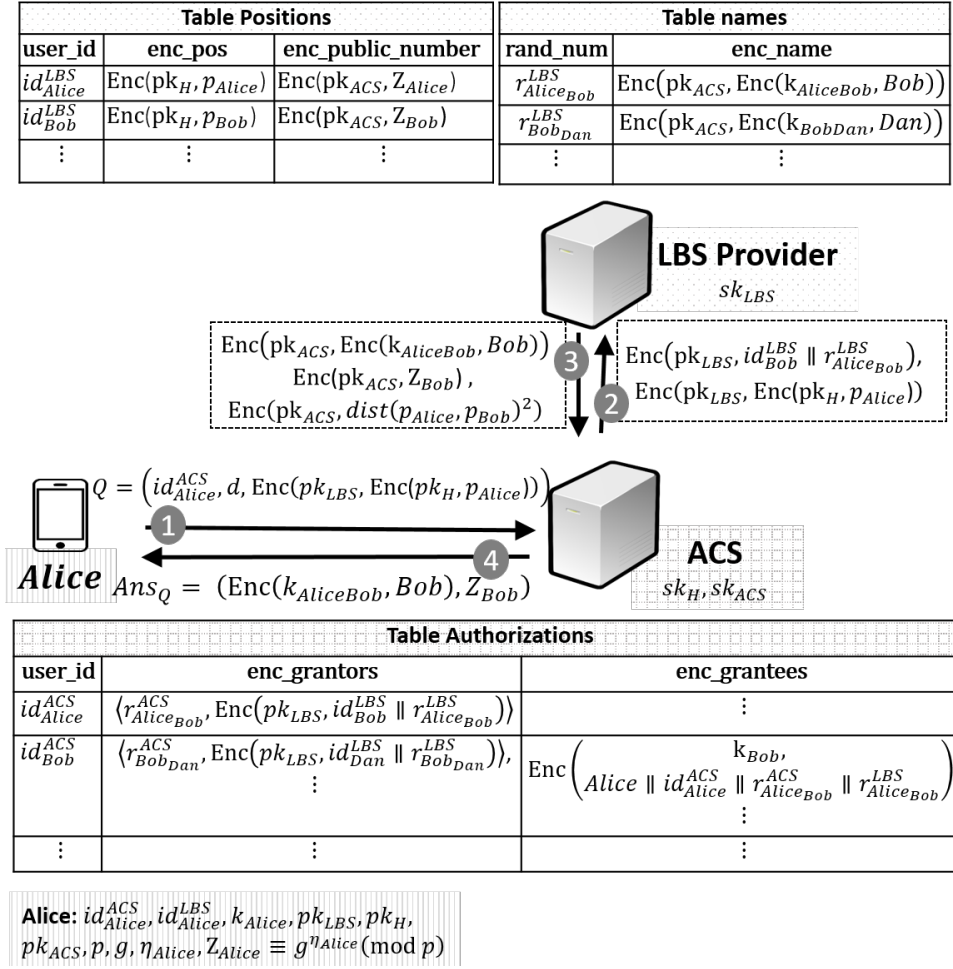


Fig. 5. 2ISE Approach - Example

This phase differs from that of the *basic 2ISE*, Section 4.1.2, in the following: First, the key-authority uses the master key  $mk_{ABE}$  and the set of attributes of the registering user  $u$ ,  $u = fname = ug$  to generate the secret key  $sk_u$ . Second, the key-authority, instead of sending to  $u$  the parameters  $p$  and  $g$ , sends the keys  $pk_{ABE}$  and  $sk_u$ . Third,  $u$  does not follow the DH protocol. Instead,  $u$  stores at the LBS provider, apart from his identifier  $id_u^{LBS}$  and his encrypted position, his encrypted name  $Enc^1pk_{ACS}; Enc^1pk_{ABE}; u$ , with access policy  $u = 'name = u^o$ . Note that, since  $u$  has not authorized any access request, yet,  $u$  specifies that only  $u$  can decrypt his encrypted name.

**4.2.3 Access request phase.** This phase differs from that of the *basic 2IABE*, Section 4.1.3, in the following: First, since the *basic 2IABE* does not use the DH protocol, users  $u$  and  $u'$  do not compute the shared key  $k_u$ . Instead,  $u$  has to update his access policy by adding to the disjunction the term " $name = u^o$ ". Second,  $u$  does not generate the random number  $r_u^{LBS}$ . That is because, the LBS provider stores, together with the identifier  $id_u^{LBS}$ , a single ciphertext containing the encrypted name of  $u$ , which can be decrypted by all his grantors. Then,  $u$  selects only one random number,  $r_u^{ACS} \in \mathbb{Z}$ , instead of two. As a consequence, the tuple  $t$  added to the set  $Grantor_u$  is  $t =$

$r_U^{ACS}, \text{Enc}^1 \text{pk}_{LBS}; id^{LBS\circ}$ , instead of  $t = r_U^{ACS}, \text{Enc}^1 \text{pk}_{LBS}; id^{LBS} \text{kr}_U^{LBS\circ}$ , and the ciphertext added to the set *Grantee* is  $c = \text{Enc}^1 \text{k}; uk id_U^{ACS} \text{kr}_U^{ACS\circ}$ , instead of  $c = \text{Enc}^1 \text{k}; uk id_U^{ACS} \text{kr}_U^{ACS} \text{kr}_U^{LBS\circ}$ . Third,  $\mathcal{U}$  encrypts and updates at the LBS provider his name using, for the inner layer of encryption, the public key  $\text{pk}_{ABE}$ , and the access policy  $\mathcal{A}$ , instead of using the shared key  $k_U$ .

**4.2.4 Query phase.** This phase differs from that of the *basic 2ISE*, Section 4.1.4, in the following: First, the set of ciphertexts  $C$  that the LBS provider receives from the ACS contains only encrypted identifiers, instead of encrypted identifiers concatenated with random numbers. Second, the LBS provider neither retrieves public numbers nor uses the decrypted random numbers to retrieve encrypted names. Instead, it only uses the decrypted identifiers to retrieve the encrypted positions and encrypted names. Third, the set of tuples that the ACS receives from the LBS provider does not contain encrypted public numbers. Fourth, the querying user  $u$  does not need to compute shared keys to decrypt the ciphertexts received as query answer. Instead,  $u$  uses his secret key  $sk_u$ .

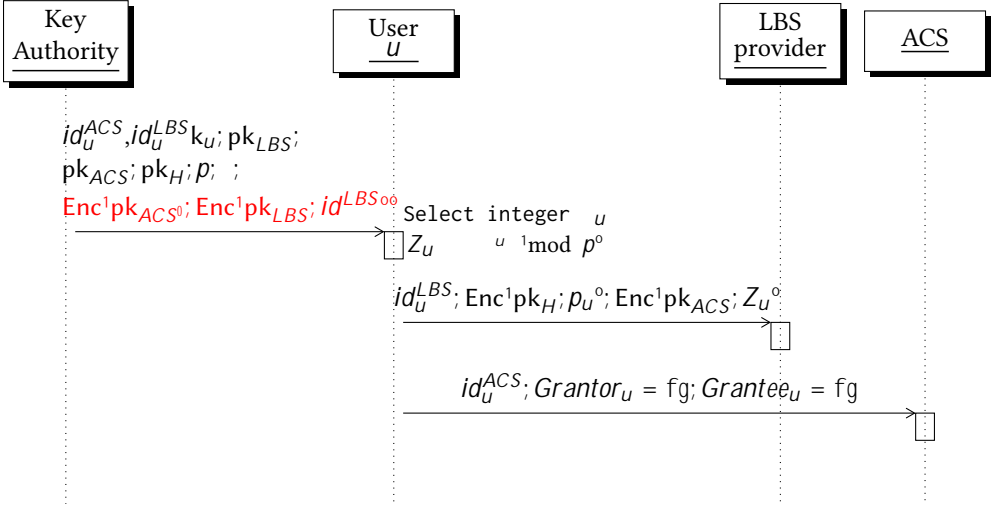
### 4.3 Extending the basic schemes

Having the basic schemes, *basic 2ISE* and *basic 2LABE*, we now show how to extend them to meet our secrecy guarantees  $G_{\text{position}}$ ,  $G_{\text{distance}}$  and  $G_{\text{authorization}}$  under our actual adversary model defined in Section 2.2. That is, we consider the twofold-composition strategy in which the protocol is executed twice. The only problem of the basic schemes under the twofold-composition strategy relies on the revocation process. With both approaches, a revoked user, in case of collusion with the LBS provider, could gain access to unauthorized information, as explained in Example 4.5. In the case of collusion with the ACS, there is no information leakage, as we prove in Section 5.

*Example 4.5.* Consider Example 4.3 and assume that Alice colludes with the LBS provider and sends a range query. The ACS sends to the LBS provider, during query processing, a message containing, among others, the identifier  $id_{Bob}^{LBS}$ . If the system does not receive other queries while it computes the query of Alice, the LBS provider and Alice can learn that  $id_{Bob}^{LBS}$  is the identifier of Bob. Assume now that Bob revokes access to Alice. Alice can regain this access by following herself the steps of the access request phase. Specifically, with the *basic 2ISE*, Alice can follow all the steps of the access request phase that Bob, i.e., the grantor, should execute (Section 4.1.3). With the *basic 2LABE*, Alice can follow the steps of the access request phase and store information at the ACS (Section 4.2.3). But she cannot update the ciphertext  $C$  containing the name of Bob, stored at the LBS provider, because she does not know the access policy  $\mathcal{A}_{Bob}$  that Bob used to generate  $C$ . Nevertheless, during querying processing, with the information added at the ACS, Alice will receive the encrypted name of Bob, which she cannot decrypt, but she knows it corresponds to Bob.

**4.3.1 Extended two-layer symmetric encryption (2ISE).** If a revoked user colludes with the LBS provider, we need the ACS to detect the attack and raise an alarm. To do so, we extend the *basic 2ISE* as follows: First, in the initialization phase, in addition to the steps of the *basic 2ISE*, Section 4.1.1, the key-authority generates a pair of keys  $^1 \text{pk}_{ACS^0}; sk_{ACS^0}$ , and sends  $sk_{ACS^0}$  to the ACS. The key-authority keeps for itself the key  $\text{pk}_{ACS^0}$ . Second, in the registration phase, the key-authority sends to each registering user  $u$ , in addition to the information sent with the *basic 2ISE*, Section 4.1.2, a ciphertext containing his identifier encrypted using two layers of encryption. The key for the inner layer is  $\text{pk}_{LBS}$  and the one for the outer layer is  $\text{pk}_{ACS^0}$ . That is, each user  $u$  receives, additionally, the ciphertext  $\text{Enc}^1 \text{pk}_{ACS^0}; \text{Enc}^1 \text{pk}_{LBS}; id^{LBS\circ}$ . Third, in the access request phase, the tuple  $t$  that the grantor  $\mathcal{U}$  sends to the ACS changes from  $t = r_U^{ACS}; \text{Enc}^1 \text{pk}_{LBS}; id^{LBS} \text{kr}_U^{LBS\circ}$  to  $t = r_U^{ACS}; \text{Enc}^1 \text{pk}_{ACS^0}; \text{Enc}^1 \text{pk}_{LBS}; id^{LBS\circ}; \text{Enc}^1 \text{pk}_{LBS}; r_U^{LBS\circ}$ . Next, the ACS uses the key  $sk_{ACS^0}$  to decrypt the element  $t_2$ , replaces  $t_2$  with the decrypted information and adds  $t$  to the set *Grantor $_u$* . Since  $u$  is the only user who knows the ciphertext  $\text{Enc}^1 \text{pk}_{ACS^0}; \text{Enc}^1 \text{pk}_{LBS}; id^{LBS\circ}$ , the ACS knows

that the access request has been registered by the actual grantor and not by a revoked user who has colluded with the LBS provider. In other words, even if a user  $u$  learns the identifier of one of his grantors, in case of revocation,  $u$  cannot regain access because only  $\text{Key Authority}$  knows his ciphertext  $c = \text{Enc}^1 \text{pk}_{\text{ACS}^0}; \text{Enc}^1 \text{pk}_{\text{LBS}}; id^{\text{LBS}00}$  and only the key-authority knows the key  $\text{pk}_{\text{ACS}^0}$  to generate  $c$ . We assume that the ACS uses a decryption algorithm  $\text{Dec}$  that indicates successful decryption. That is, the decryption  $\text{Dec}^1 \text{sk}_{\text{ACS}^0}; \text{Enc}^1 k^0; c^{00}$ , where  $c$  is a ciphertext, is called successful if  $\text{sk}_{\text{ACS}^0} = k^0$ . One can implement a successful decryption algorithm by concatenating the hash value  $H^1 c^0$  to the encryption  $\text{Enc}^1 k^0; c; H^1 c^0$  and checking this relation in the decryption algorithm [18]. Fourth, in the query phase, the set of ciphertexts  $C$  that the ACS sends to the LBS provider is different from that of the *basic 2ISE*, Section 4.1.4. Here,  $C$  is a set of tuples, where each tuple contains two ciphertexts. Specifically, for each tuple  $t$  in the set  $\text{Grantor}_u$ , the ACS adds to  $C$  a tuple consisting of the elements  $t_2$  and  $t_3$ , i.e., the encrypted identifier and the encrypted random number. The LBS provider decrypts both ciphertexts and processes the query as with the *basic 2ISE*. Figures 6, 7, and 8 illustrate the steps of the user registration, access request and query phases, respectively. The changes compared to the basic scheme are highlighted in red.


 Fig. 6. User Registration Phase - *basic 2ISE*

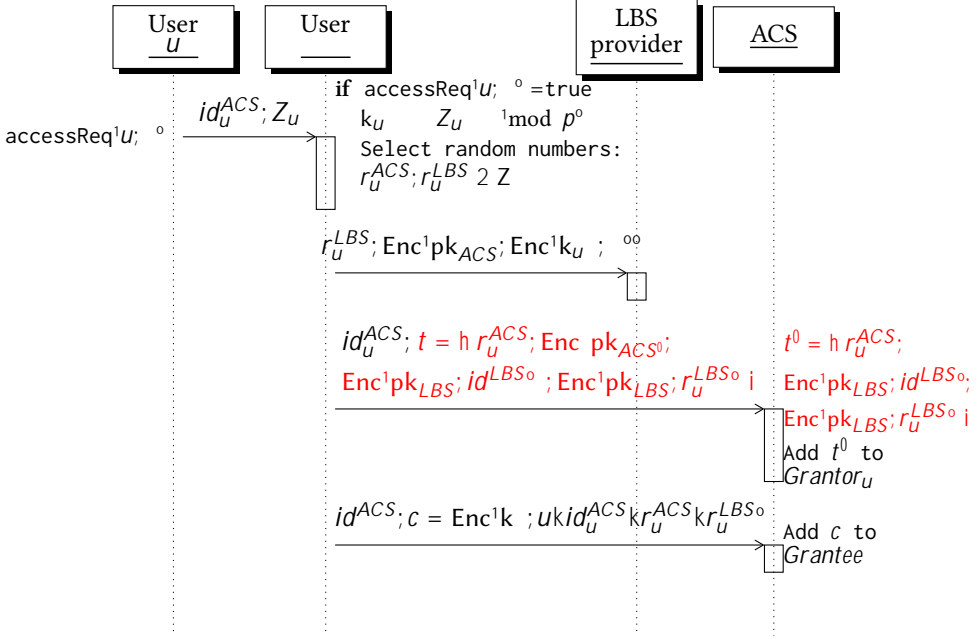
**4.3.2 Extended two-layer attribute-based encryption (2LABE).** To solve the existing problems when a revoked user colludes with the LBS provider, we use the same technique as that of the *2ISE*, Section 4.3.1. That is, the ACS, during the access request phase, receives the following ciphertext:  $\text{Enc}^1 \text{pk}_{\text{ACS}^0}; \text{Enc}^1 \text{pk}_{\text{LBS}}; id^{\text{LBS}00}$ , and verifies that the actual grantor has sent the received ciphertext. The query processing phase is similar to that of the *basic 2LABE*, Section 4.2.4.

## 5 SECURITY PROOFS

This section provides the secrecy analysis of our proposed approaches. The proofs are organized as follows: For each approach, we first prove that, under our adversary model defined in Section 2.2, the approach provides the secrecy guarantee  $G_{\text{position}}$ , then  $G_{\text{distance}}$ , and finally  $G_{\text{authorization}}$ .

### 5.1 Secrecy Proofs of the *2ISE* approach

For each of the proofs in this section, we first consider the case that a user colludes with the LBS provider and then the case that a user colludes with the ACS, during the first execution of the

Fig. 7. Access Request Phase - *basic 2ISE*

protocol. During the second execution of the protocol, the user is not allowed to collude anymore (twofold-composition strategy). The case where each party individually acts as an adversary is straightforward and therefore omitted. Given two entities  $A$  and  $B$ , we study the case where entity  $A$  colludes with  $B$ , and omit the case where  $B$  colludes with  $A$ . In the case of collusion of two entities  $A$  and  $B$ , we assume that either  $A$  or  $B$  has access to all information and functionality of  $A$  and  $B$  together.

Before starting with the proofs, let us recall the information that the users, LBS provider, and ACS have. We use this information in the proofs. First, each user  $s$  knows: his identifiers  $id_s^{LBS}$ ,  $id_s^{ACS}$ , the keys  $k_s$ ,  $pk_H$  and  $pk_{ACS}$ , his encrypted identifier  $Enc^1pk_{ACS^0}$ ,  $Enc^1pk_{LBS}$ ,  $id_s^{LBS_0}$ , and the parameters  $p$ ,  $\rho$ ,  $\gamma_s$ . Second, the LBS provider stores: the user identifiers, the encrypted positions, the encrypted public numbers, the encrypted names together with the random numbers, and the secret key  $sk_{LBS}$ . Additionally, the LBS provider knows the relations existing between the information that it stores, e.g., the encrypted position that corresponds to a given identifier. Third, the ACS stores: the encrypted sets of grantors and grantees of all the users, and the keys  $sk_H$ ,  $sk_{ACS}$  and  $sk_{ACS^0}$ . Additionally, the ACS knows the relations existing between the stored information

**LEMMA 5.1.** *Given a user  $u$ , the 2ISE approach guarantees that, in the presence of adversaries with the characteristics defined in our adversary model, Section 2.2, only authorized entities can learn the physical position of  $u$ .*

**PROOF.** *Case 1: A user  $s$  colludes with the LBS provider.* During the first protocol execution,  $s$  has access to the information that he owns and the one stored at the LBS provider. However, none of the information that  $s$  has can be used to decrypt the encrypted positions. The decryption key  $sk_H$  is known only by the ACS, but according to our adversary model,  $s$  cannot collude with both entities at the same time. Furthermore, SHE, which is used to encrypt the physical positions of



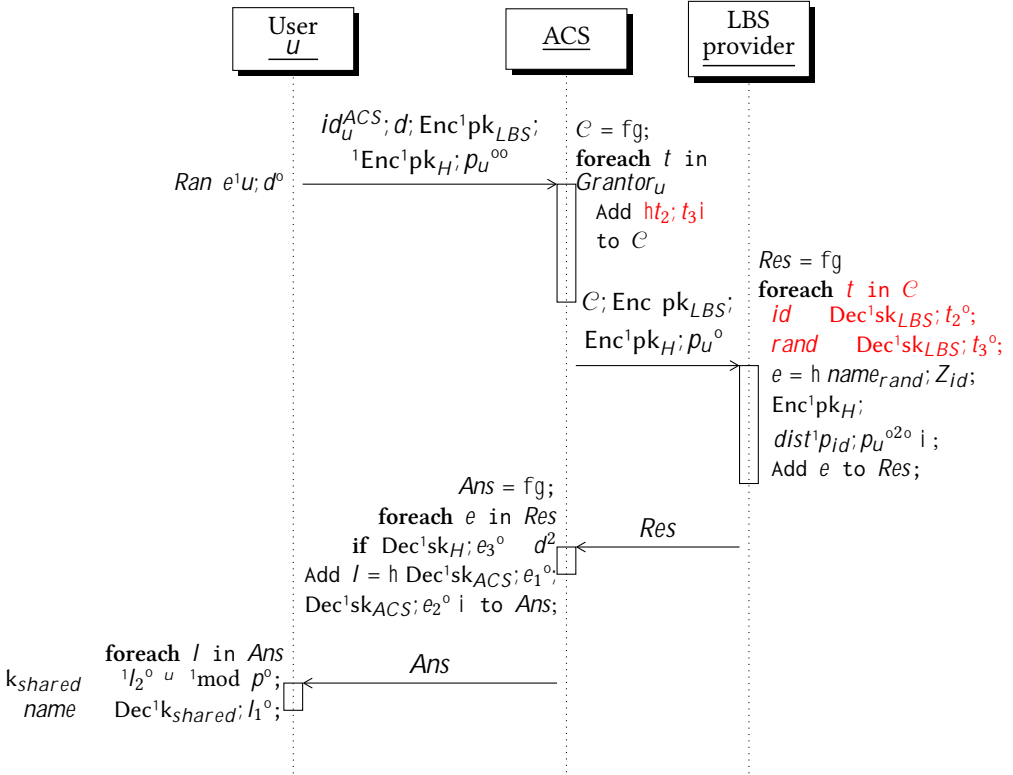


Fig. 8. Query Phase - basic 2ISE

the users, is secure against indistinguishability chosen-plaintext attacks (IND-CPA) [31], i.e., an adversary cannot learn any useful information from the encrypted data.

In addition to the information that  $S$  has learned,  $S$  can execute queries and get their respective answers. We now show that  $S$  cannot use this information to learn the physical positions of users who have not authorized him to do so. During query processing, the LBS provider receives from the ACS a set containing the encrypted identifiers of the grantors of  $s$ . So,  $S$  knows that the set of identifiers used by the LBS provider to process his query corresponds to his grantors. The identifiers are random numbers, so  $S$  cannot link the identifiers with their owners, except if  $|Grantor_s| = 1$ . In this last case,  $S$  can learn the identifier of his unique grantor, namely  $u$ ,  $id_u^{LBS}$ , see Example 4.5. However,  $id_u^{LBS}$  does not leak any information about the position of  $u$  or cannot be used to decrypt his encrypted position. Next, during query processing,  $S$  receives a set of encrypted names and public numbers corresponding to the grantors of  $s$  that fulfill the query condition. Since the information received belongs to the grantors of  $s$ ,  $S$  is allowed to learn such information. Next, assume that the LBS provider deviates from the query processing protocol, as part of the collusion. That is, the LBS provider processes the query with different identifiers from the ones sent by the ACS. So, instead of using the information that belongs to the grantors of  $s$ , the LBS provider selects different identifiers and random numbers to give  $S$  information that he is not authorized to access. However, the identifiers are random numbers, and neither  $S$  nor the LBS provider knows the relationship between identifier and users. Next, if the LBS provider processes the query with identifiers selected at random,  $S$  receives as query result a set of encrypted names and public numbers. However, the

names are encrypted using probabilistic symmetric encryption, which is secure against IND-CPA [21], and  $s$  does not know the key to decrypt them. Next, by using the received public numbers, and the parameters  $p$  and  $g$ ,  $s$  cannot compute the decryption key because of the security offered by the DH problem, which has been proven to be computationally infeasible in [8]. Then,  $s$  cannot learn, in the first protocol execution, the physical position of users that he is not authorized.

During the second protocol execution, since  $s$  is not allowed to collude anymore with any entity,  $s$  only has access to information that he owns, information that he has learned during the first protocol execution, and the one that he will obtain during the second protocol execution. However, during the second protocol execution,  $s$  does not learn any new information. Then, as in the first execution, this information is not enough to decrypt and learn the physical positions of other users. *Case 2: A user  $s$  colludes with the ACS.* During the first protocol execution,  $s$  has access to the information that he owns and the one stored at the ACS. Although  $s$  knows the key  $sk_H$  to decrypt the encrypted positions,  $s$  does not have the ciphertext to decrypt them because they are stored at the LBS provider. Since, according to our adversary model,  $s$  cannot collude with both entities at the same time,  $s$  cannot use the key  $sk_H$  to decrypt the physical positions of other users.

In addition to the information that  $s$  has learned,  $s$  can execute queries and get their respective answers. We now show that  $s$  cannot use this information to learn the physical positions of other users.

By following the query processing protocol,  $s$  receives a set of encrypted names and public numbers corresponding to the grantors of  $s$  that fulfill the query condition. Since the information received belongs to the grantors of  $s$ ,  $s$  is allowed to learn that information. Next, assume that the ACS deviates from the query processing protocol, as part of the collusion. That is, the ACS includes in the set  $Grantor_s$ , information from the other sets of grantors to give access to  $s$  to information that he is not authorized to access. So,  $s$  receives as query answer, a set of encrypted names and public numbers. Based on the same arguments as the ones presented in the Case 1,  $s$  cannot compute the decryption key and cannot learn any information from the encrypted names. Then, during the first protocol execution,  $s$  cannot learn the physical position of users who have not authorized him.

During the second protocol execution, since  $s$  is not allowed to collude anymore with any entity,  $s$  only has access to information that he owns, information that he has learned during the first execution, and the one that he will obtain during the second protocol execution. Different from the case 1, after query processing,  $s$  cannot learn any extra information, i.e.,  $s$  has access to the same information as in the first protocol execution. Using the same arguments as in the first execution,  $s$  cannot learn the physical positions of users that he is not authorized.

Consequently, given a user  $u$ , the 2LSE approach guarantees that, in the presence of adversaries with the power defined in our adversary model, only authorized entities can learn the physical position of  $u$ .

**LEMMA 5.2.** *Given a user  $u$ , the 2LSE approach guarantees that, in the presence of adversaries with the characteristics defined in our adversary model, Section 2.2, only entities they themselves have authorized can learn the distance between their physical position and the one of  $u$ .*

**PROOF.** *Case 1: A user  $s$  colludes with the LBS provider.* During the first protocol execution,  $s$  has access to the information that he owns and the one stored at the LBS provider. Using this data, as proved in Lemma 5.1,  $s$  cannot learn any useful information from the encrypted data.

In addition to the information that  $s$  has learned,  $s$  can execute queries and get their respective answers. We now show that  $s$  cannot use this information to learn the distance between his position and the one of the users who have not authorized him to do so. As explained in the proof of Lemma 5.1, during query processing, if  $|Grantor_s| = 1$ ,  $s$  can learn the identifier of his

unique grantor, namely  $u$ ,  $id_u^{LBS}$ . However,  $id_u^{LBS}$  does not leak any information about the physical positions or the distance between users. Additionally, as proved in Lemma 5.1, by following the query processing protocol,  $s$  receives as query answer only information that he is authorized to access. Next, assume that the LBS provider deviates from the query processing protocol, as part of the collusion. That is, the LBS provider processes the query with different identifiers from the ones sent by the ACS. So, instead of using the information that belongs to the grantors of  $s$ , the LBS provider selects different identifiers and random numbers to give  $s$  information that he is not authorized to access. As proved in Lemma 5.1, since  $s$  cannot compute the encryption key and probabilistic encryption is secure against IND-CPA [21],  $s$  cannot learn any useful information from the encrypted data received during query processing. Then,  $s$  cannot learn, in the first protocol execution, the distance between his position and the one of users that he is not authorized.

Next, during the second protocol execution, since  $s$  is not allowed to collude anymore with any entity,  $s$  only has access to information that he owns, information that he has learned during the first protocol execution, and the one that he will obtain during the second protocol execution. Assume that in the second protocol execution,  $u$  revokes access to  $s$ . Then  $s$  can try himself to add  $id_u^{LBS}$  to his set  $Grantor_s$  following the steps of the access request phase. However,  $s$  needs to send the ciphertext  $c = \text{Enc}^{pk_{ACS^0}}; \text{Enc}^{pk_{LBS}}; id_u^{LBS\infty}$  to the ACS. Since  $s$  does not know  $c$  or the key  $pk_{ACS^0}$  to generate  $c$ ,  $s$  cannot add  $id_u^{LBS}$  in his set  $Grantor_s$ . Therefore, in the case of revocation,  $s$  cannot regain access.

*Case 2: A user  $s$  colludes with the ACS.* During the first protocol execution,  $s$  has access to the information that he owns and the one stored at the ACS. Knowing all this information, as proved in Lemma 5.1,  $s$  cannot obtain the ciphertexts corresponding to the encrypted positions of other users. So  $s$  cannot learn any useful information in this step.

In addition to the information that  $s$  has learned,  $s$  can execute queries and get their respective answers. As proved in Lemma 5.1, by following the query processing protocol,  $s$  receives as query answer only information that he is authorized to access. Next, assume that the ACS deviates from the query processing protocol, as part of the collusion. That is, the ACS includes in the set  $Grantor_s$ , information from the other sets of grantors to give access to  $s$  to information that he is not authorized to access. As proved in Lemma 5.1, and similar to Case 1, since  $s$  cannot compute the encryption key and probabilistic encryption is secure against IND-CPA [21],  $s$  cannot learn any useful information from the encrypted data received during query processing. Then,  $s$  cannot learn, in the first protocol execution, the distance between his position and the one of users that he is not authorized.

During the second protocol execution, since  $s$  is not allowed to collude anymore with any entity,  $s$  only has access to information that he owns, information that he has learned during the first execution, and the one that he will obtain during the second protocol execution. Different from Case 1, after query processing,  $s$  cannot learn any extra information, i.e.,  $s$  has access to the same information as in the first protocol execution. Using the same arguments as in the first execution,  $s$  cannot learn the distance between his position and the one of the users who have not authorized him. So, in the case of revocation, by using the information that  $s$  knows,  $s$  cannot regain access.

Consequently, given a user  $u$ , the *2ISE* approach guarantees that, in the presence of adversaries with the power defined in our adversary model, only entities they themselves have authorized can learn the distance between their physical position and the one of  $u$ .

We note that although users do not receive as part of the query answers the physical position of authorized users, they could submit fake positions and check the results of the query to infer the real position of a target. However, as proved in Lemma 5.2, if a user  $u$  submits a query, the query result contains only users who have authorized  $u$  to learn the distance between their physical position

and the one of  $u$ . That is, only authorized users could infer the real position of a target. However, these users are authorized to access such information with respect to our secrecy guarantees.

**LEMMA 5.3.** *Given two users  $u$  and  $v$ , the 2ISE approach guarantees that, in the presence of adversaries with the characteristics defined in our adversary model, Section 2.2, an adversary will not be able to learn whether  $u$  or  $v$  are allowed to learn the distance between them.*

**PROOF.** *Case 1: A user  $s$  colludes with the LBS provider.* During the first protocol execution,  $s$  has access to the information that he owns and the one stored at the LBS provider. First, the user identifiers are random numbers, and by using all the known information, neither the LBS provider nor  $s$  can determine the link between users and identifiers. Second, the information that  $s$  knows does not contain any link between grantees and grantors. Then,  $s$  cannot determine whether two given users  $u$  and  $v$  are allowed to learn the distance between them.

In addition to the information that  $s$  has learned,  $s$  can execute queries and get their respective answers. We now show that  $s$  cannot use this information to learn whether two given users  $u$  and  $v$  are allowed to learn the distance between them. As explained in the proof of Lemma 5.1, during query processing, if  $|Grantors_s| = 1$ ,  $s$  can learn the identifier of his unique grantor, namely  $u$ ,  $id_u^{LBS}$ . However, given a set of queries, neither  $s$  nor the LBS provider knows who are the querying users. Therefore, if the identifier  $id_u^{LBS}$  is used during query processing,  $s$  cannot determine who are the grantees of  $u$ . Additionally, during query processing,  $s$  receives a set of encrypted names and public numbers corresponding to the grantors of  $s$  that fulfill the query condition. However, the received information does not reveal any data about the grantees and grantors of other users. Then, given two users  $u$  and  $v$ , during the first protocol execution,  $s$  is not able to learn whether  $u$  or  $v$  are allowed to learn the distance between them.

During the second protocol execution, since  $s$  is not allowed to collude anymore with any entity,  $s$  only has access to information that he owns, the one that he has learned during the first execution, and the one that he will obtain during the second protocol execution. Since the information that  $s$  gets in the second protocol execution is similar to the one of the first execution, this information is not enough to learn whether  $u$  or  $v$  are allowed to learn the distance between them.

*Case 2: A user  $s$  colludes with the ACS.* During the first protocol execution,  $s$  has access to the information that he owns and the one stored at the ACS. First, the set of grantors is encrypted using asymmetric encryption and the key  $pk_{LBS}$ . Since  $s$  does not know  $pk_{LBS}$  and asymmetric encryption is secure against IND-CPA [21],  $s$  cannot learn any useful information from the encrypted data. Second, the set of grantees are encrypted using probabilistic encryption and the key of its owner. Since  $s$  knows only the key to decrypt his set of grantees, and probabilistic encryption is secure against IND-CPA [21],  $s$  cannot learn any useful information from the encrypted data.

In addition to the information that  $s$  has learned,  $s$  can execute queries and get their respective answers. Similar to the case 1, the information that  $s$  received during query processing does not reveal any data about the grantees and grantors of other users. Next, during the second protocol execution, since  $s$  is not allowed to collude anymore with any entity,  $s$  only has access to information that he owns, the one that he has learned during the first protocol execution, and the one that he will obtain during the second execution. Similar to the case 1,  $s$  has access to the same information as in the first protocol execution. Therefore, using the same arguments as in the first protocol execution,  $s$  cannot learn whether  $u$  or  $v$  are allowed to learn the distance between them.

Consequently, given two users  $u$  and  $v$ , the 2ISE approach guarantees that, in the presence of adversaries with the power defined in our adversary model, an adversary will not be able to learn whether  $u$  or  $v$  are allowed to learn the distance between them.

## 5.2 Secrecy Proofs of the 2LABE approach

LEMMA 5.4. *Given a user  $u$ , the 2LABE approach guarantees that, in the presence of adversaries with the characteristics defined in our adversary model, Section 2.2, only authorized entities can learn the physical position of  $u$ .*

LEMMA 5.5. *Given a user  $u$ , the 2LABE approach guarantees that, in the presence of adversaries with the characteristics defined in our adversary model, Section 2.2, only entities they themselves have authorized can learn the distance between their physical position and the one of  $u$ .*

LEMMA 5.6. *Given two users  $u$  and  $v$ , the 2LABE approach guarantees that, in the presence of adversaries with the characteristics defined in our adversary model, Section 2.2, an adversary will not be able to learn whether  $u$  or  $v$  are allowed to learn the distance between them.*

The proofs of Lemmas 5.4 - 5.6 are analogous to the proofs of Lemmas 5.1 - 5.3, respectively. Although the 2ISE and the 2LABE approaches have some differences, the properties of the 2ISE used for the proofs also hold for 2LABE. First, both approaches differ in the encryption scheme used to encrypt the usernames. The 2LABE uses CP-ABE. Since CP-ABE is IND-CPA secure [7], adversaries cannot learn any useful information from the encrypted names. Second, different from the 2ISE, the 2LABE does not use the DH protocol to share keys between users. Instead, each user receives, as part of the CP-ABE, a secret key for decryption. A user can decrypt a ciphertext  $c$  only if the attributes used to generate his secret key satisfies the access policy used to generate  $c$ . That is, a user can decrypt only usernames that belong to his grantors.

## 6 TIME COMPLEXITY ANALYSIS

A complexity analysis is helpful to predict the behavior of the 2ISE and 2LABE approaches and to facilitate meaningful comparisons. An average complexity analysis depends on the internal behavior of the database, which is specific to the product and is not openly available. Furthermore, if there are changes in the system settings, the average analysis is void. So our complexity analysis is a worst case analysis. Here, we focus on the complexity of the query phase because this is the most frequently used phase in our scenario.

### 6.1 Time Complexity Analysis of the 2ISE and 2LABE approaches

The number of operations at the user-side depends on the number of grantors of the querying user  $u$  that are inside the query range. Then, our worst-case complexity analysis considers that all the users in the set of grantors of  $u$  are located within the query range. To perform the complexity analysis of our approaches, one needs to specify the complexity of the encryption/decryption process, which depends on the type of encryption/decryption algorithm used. We select the following well-known algorithms from the literature: For symmetric and asymmetric encryption schemes, we use AES and RSA, respectively. For SHE, we use algorithms based on the learning with errors problem over rings, such as the ones presented in [32]. For CP-ABE, we select the algorithm presented in [27].

Let  $A$  be the total number of authorized access requests, i.e.,  $A = \sum_{u \in U} |Grantor_u|$ ,  $B^l p_u^o$  be the bit string representation of the physical position  $p_u$ , and  $|B^l p_u^o|$  its length. Further, let  $TC_{user}$ ,  $TC_{ACS}$ , and  $TC_{LBS}$  denote the time complexity at the user-side, the ACS and the LBS provider, respectively. A ciphertext generated using SHE is represented as a matrix  $M$ . We use  $|M|$  to denote the size of the matrix. Next, the initialization of the RSA algorithm requires to select at random two large primes. We use  $N$  to denote the product of the selected primes. Next, note that  $p$  and  $d_u$  are the integer and the secret number of a given user  $u$ , respectively, that are part of the DH protocol.

LEMMA 6.1. *Given a range query  $Ran_e = [u; d]^\circ$ , the time complexities of the 2ISE approach at the user-side, the ACS, and the LBS provider are:*

$$\begin{aligned} TC_{user} &= \mathcal{O}(|Grantor_u| \log^1 p^{02} \log^1 u^\circ) \\ TC_{ACS} &= \mathcal{O}(|Grantor_u| |jB^1 p_u^\circ| \log^1 |jB^1 p_u^\circ|^\circ + \log^1 N^{03^\circ}) \\ TC_{LBS} &= \mathcal{O}(|Grantor_u| |jM|^3) \end{aligned} \quad (1)$$

PROOF. We start by analyzing the complexity of the encryption/decryption process of each of the encryption schemes used in the 2ISE approach, i.e., symmetric, asymmetric encryption, and SHE. First, the complexity of symmetric encryption schemes, specifically AES, depends on the length of the message  $m$  to be encrypted,  $|m|$ , [36]. Then, the complexity of the encryption/decryption process is  $\mathcal{O}(|m|^\circ)$ . In our scenario, we use symmetric encryption to encrypt the usernames. We consider that the length of the string that represents a username has a constant size of 12 bytes. Therefore, the complexity of the encryption/decryption process using symmetric encryption reduces to  $\mathcal{O}^1$ .

Second, the complexity of asymmetric encryption schemes, specifically RSA, is based on the complexity of modular exponentiation. Using RSA, given a message  $m$ , the resulting ciphertext is  $c = m^e \bmod N^\circ$ , and the decryption of  $c$  is  $m = c^d \bmod N^\circ$ , where  $e$  is the public key and  $d$  is the secret key. Given the integer numbers  $B; C; N$ , the complexity of the modular exponentiation  $B^C \bmod N^\circ$  is  $\mathcal{O}^1 \log^1 N^{02} \log^1 C^{00}$ . We consider that the exponent  $e$  in the RSA algorithm, i.e., the public key, is fixed, as specified in FIPS-186-3 [30]. So the encryption complexity using RSA is  $\mathcal{O}^1 \log^1 N^{02^\circ}$ . Using standard RSA assumptions, the exponent  $d$  in the RSA algorithm, i.e., the secret key, has size in bits close to that of  $N$ . Then, the decryption complexity using RSA is  $\mathcal{O}^1 \log^1 N^{03^\circ}$ .

Third, in SHE schemes [32], the encryption/decryption process depends on modular multiplication and addition of vectors. Given a message  $m$ , using SHE, the complexity of encrypting/decrypting  $m$  is  $\log^1 |jB^1 m^\circ|$  per bit [11], assuming the use of the Montgomery multiplication, which is one of the fastest methods available for performing modular multiplication. Then, the encryption/decryption complexity of SHE schemes is  $\mathcal{O}^1 |jB^1 m^\circ| \log^1 |jB^1 m^\circ|^\circ$ . The following steps are required to compute a given range query with the 2ISE approach.

- (1) Encrypt using SHE the position of the querying user  $u$ . The user executes this step. The complexity of this step is  $\mathcal{O}^1 |jB^1 p_u^\circ| \log^1 |jB^1 p_u^\circ|^\circ$ .
- (2) Use the identifier of the querying user  $u$ ,  $id_u^{ACS}$  to retrieve the set of grantors  $Grantor_u$ . The ACS executes this step. We assume the ACS uses B-tree indexing. Then, the complexity of this step is  $\mathcal{O}^1 \log^1 |jU|^\circ$ .
- (3) Decrypt the set of encrypted identifiers and the set of encrypted random numbers sent by the ACS. Since both sets have a size of  $|jGrantor_u|$  and each element of these sets is encrypted using the asymmetric encryption, the LBS provider has to execute  $2 |jGrantor_u|$  asymmetric decryptions. The complexity of this step is  $\mathcal{O}^1 |jGrantor_u| \log^1 N^{03^\circ}$ .
- (4) For each decrypted identifier in step 3, retrieve the corresponding encrypted position and encrypted public value. The LBS provider does this step. We assume the LBS provider uses B-tree indexing. Then, the complexity of this step is  $\mathcal{O}^1 |jGrantor_u| \log^1 |jU|^\circ$ .
- (5) Compute the encrypted square distances between the querying user and the ones retrieved in step 4. The LBS provider executes this step. This operation requires three homomorphic additions and two multiplications. A ciphertext generated using SHE is represented as a matrix. So adding and multiplying two ciphertexts imply addition and multiplication of two matrices [45]. The addition and multiplication operations have a complexity of  $\mathcal{O}^1 |jM|^2^\circ$  and  $\mathcal{O}^1 |jM|^3^\circ$ , respectively. Since  $\mathcal{O}^1 |jM|^3^\circ$  dominates  $\mathcal{O}^1 |jM|^2^\circ$ , the complexity of computing one encrypted square distance is  $\mathcal{O}^1 |jM|^3^\circ$ . The complexity of this step is  $\mathcal{O}^1 |jGrantor_u| |jM|^3^\circ$ .

- (6) Retrieve from the set of encrypted names stored at the LBS provider the encrypted names corresponding to each of the random numbers decrypted in step 3. The LBS provider executes this step. The complexity of this step is  $\mathcal{O}(|Grantor_U| \log^1 A^{00})$ .
- (7) Decrypt the information sent by the LBS provider: the encrypted square distances, the second layer of encryption of the encrypted names, and the encrypted public numbers. The ACS executes this step. It decrypts in total  $3 |Grantor_U|$  ciphertexts. The square distances are encrypted using SHE, and the names and public numbers are encrypted using asymmetric encryption. Then, the ACS performs  $|Grantor_U|$  SHE decryptions and  $2 |Grantor_U|$  asymmetric decryptions. The complexity of this step is  $\mathcal{O}(|Grantor_U| |jB^1 p_U^0| \log^1 |jB^1 p_U^0| + \log^1 N^{0300})$ .
- (8) Compute the shared keys and decrypt the encrypted names corresponding to users that fulfill the query condition. The user does this step.  $u$  computes in total  $|Grantor_U|$  shared keys. The shared keys are generated using the DH protocol, which requires modular exponentiation. Given a public number of a user  $Z$ ,  $u$ , and the secret number of  $u$ ,  $u$ , the complexity of the modular exponentiation  $Z^u \pmod{p}$  is  $\mathcal{O}(\log^1 p^{02} \log^1 u^{00})$ , where  $p$  is the parameter of the DH protocol. The number of decryptions performed are  $|Grantor_U|$ , where each decryption has a complexity of  $\mathcal{O}^1$ . The complexity of this step is  $\mathcal{O}(|Grantor_U| \log^1 p^{02} \log^1 u^{00})$ .

By considering the step with the highest complexity that is performed by each entity of the system, one can easily construct the terms of Equation 1.

We introduce further notation: Let  $G$  and  $G_T$  be two cyclic groups of the same order, where  $G$  and  $G_T$  are the groups selected during the initialization of the CP-ABE scheme. Further, let  $e$  be a bilinear map of the form  $e : G \times G \rightarrow G_T$ . The encryption/decryption process using CP-ABE is based on bilinear mappings and operations in the groups  $G$  and  $G_T$ . We use  $C_e$  and  $C_{G_T}$  to denote the complexity of computing  $e$ , and the complexity of performing an operation in the group  $G_T$ , respectively.

LEMMA 6.2. *Given a range query  $Ran_e = [u; d^0]$ , the time complexities of the 2LABE approach at the user-side, the ACS, and the LBS provider are:*

$$\begin{aligned}
 TC_{user} &= \mathcal{O}(|Grantor_U| C_e + C_{G_T}) \\
 TC_{ACS} &= \mathcal{O}(|Grantor_U| |jB^1 p_U^0| \log^1 |jB^1 p_U^0| + \log^1 N^{0300}) \\
 TC_{LBS} &= \mathcal{O}(|Grantor_U| |jM|^3)
 \end{aligned} \tag{2}$$

PROOF. We start by analyzing the complexity of the encryption/decryption process of each of the encryption schemes used in the 2LABE approach, i.e., asymmetric encryption, SHE, and CP-ABE. First, as shown in the proof of Lemma 6.1, the encryption and decryption complexity of asymmetric encryption schemes are  $\mathcal{O}(\log^1 N^{020})$  and  $\mathcal{O}(\log^1 N^{030})$ , respectively, and given a message  $m$ , the encryption/decryption complexity of SHE is  $\mathcal{O}(|jB^1 m^0| \log^1 |jB^1 m^0|)$ . Third, the encryption complexity of CP-ABE schemes [27] depends on the size of the access policy and the cyclic groups  $G$  and  $G_T$ . The encryption costs using CP-ABE is  $(n + 3) C_G + 2 C_{G_T}$ , where  $n$  is the size of the access policy and  $C_G$  is the complexity of performing an operation in the group  $G$  [50]. In our scenario, the size of the access policy depends on the size of the set of grantees of each user. Then, the encryption complexity of CP-ABE is  $\mathcal{O}(|jGrantor_U| C_G + C_{G_T})$ . The decryption cost using CP-ABE is  $2 C_e + 2 C_{G_T}$  [50]. Then, the decryption complexity of CP-ABE is  $\mathcal{O}(C_e + C_{G_T})$ .

The following steps are required to compute a given range query with the 2LABE approach.

- (1)-(3) Similar to the step 1-3 of the 2ISE.
- (4) Retrieve the encrypted position and encrypted name corresponding to each decrypted identifier in step 3. The LBS provider executes this step. The complexity of this step is  $\mathcal{O}(|Grantor_U| \log^1 |jU|)$ .

- (5) Similar to the step 5 of the *2ISE*.
- (6) Decrypt the encrypted square distances and the second layer of encryption of the encrypted names sent by the LBS provider. The total number of ciphertexts that the ACS has to decrypt is  $2 \cdot |Grantor_U|$ , where the square distances are encrypted using SHE and the names are encrypted using asymmetric encryption. This step is done by the ACS. The complexity of this step is  $\mathcal{O}(|Grantor_U| \cdot |B^1 p_U^0| \cdot \log^1 |B^1 p_U^0| + \log^1 N^{0300})$ .
- (7) Decrypt the encrypted names corresponding to users that fulfill the query condition. The user executes this step. The number of decryptions performed are  $|Grantor_U|$ . Then the complexity of this step is  $\mathcal{O}(|Grantor_U| \cdot C_e + C_{G_T}^{00})$ .

By considering the step with the highest complexity that is performed by each entity of the system, one can easily construct the terms of Equation 2.

## 6.2 Discussion

From our worst-case analysis, Lemmas 6.1 and 6.2, we observe that both approaches differ only at one entity: the user-side. The main difference relies on the decryption process, which is related to the encryption scheme used. With the *2ISE*, the encryption/decryption complexity of symmetric schemes is  $\mathcal{O}^1$ . However, the querying user has to perform a total of  $|Grantor_U|$  exponentiations module  $p$  to calculate the shared key. In contrast, with the *2LABE*, each user uses a single key to decrypt the received ciphertexts. However, the encryption/decryption complexity of CP-ABE schemes depends on the size of the access policy used to generate a given ciphertext and bilinear pairing operations, which are computationally expensive [50]. In fact, both schemes have a trade-off between secrecy and efficiency, as we explain in the following. Our *2ISE* approach uses the DH protocol to build a shared secret key between two users. The secrecy of this protocol relies on the Computational DH problem (CDH) [13]. Our *2LABE* approach uses CP-ABE to encrypt the name of the users. CP-ABE schemes are built based on bilinear pairing functions, which themselves rely on the CDH problem. The secrecy and efficiency of both approaches rely, among others, on the hardness of the CDH problem, and the algebraic operations in the cyclic group that is being used. The CDH problem has a trade-off between secrecy and performance. A large order of a cyclic group implies higher secrecy [16], i.e., less success probability of an adversary solving the CDH problem. However, the efficiency of computing algebraic operations is affected. Then one has to make a trade-off between the secrecy level needed and the efficiency of the approach.

Since a complexity analysis considers only the dominating operations, a worst-case analysis is insufficient to determine the performance of an algorithm in practice. For instance, for the complexity at the LBS provider, one can observe that both approaches have the same time complexity. However, one can find significant differences between both approaches in the less dominant steps. With the *2ISE* approach, the LBS provider has to perform  $|Grantor_U|$  extra searches with complexity  $\log^1 A^0$ , which will affect its performance. Therefore, we additionally perform experiments to validate our complexity analysis, evaluate how the differences between both approaches impact on their performance and determine at the end which approach performs better in practice.

## 7 EXPERIMENTS

This section presents an experimental analysis of the performance of the *2ISE* and *2LABE* approaches.

### 7.1 Experiment Setup

**7.1.1 Dataset and Query Sample.** We use the Tokyo dataset [52] in our experiments. This dataset contains 573703 real check-ins, i.e., positions. We choose a sample of 1000 users at random. Next, we divide the users into ten equally classes. We generate authorized access requests such that all



the users in each class have the same number of grantors. Specifically, we selected at random from the dataset the following grantors sizes: 10, 25, 50, 100, 250, 500, 750, 1000, 2500, and 5000.

**7.1.2 Encryption Algorithms.** We use the following libraries for the implementation: Microsoft SEAL [42] for the SHE and the Java Pairing-Based Cryptography Library together with the Cryptographic Packages `javax.crypto` and `java.security` for symmetric, asymmetric encryption and CP-ABE.

**7.1.3 Evaluation Measures.** For our evaluation, we considered the access request and query phases. All other phases are executed only once, at least with respect to one of the entities of the systems. In this sense, we consider six measures: the storage size, the access request time, the query processing time at the user-side, the query processing at the LBS provider, the query processing time at the ACS, and the total query processing time. The total query processing time is the sum of the query processing time at each of the entities.

Note that positioning and query processing are two separate activities. So, in our experiments, we do not study the time that a positioning technology needs to provide the physical position of the users and its accuracy. The level of position accuracy and its computational time depend on the underlying technology and on factors such as receiver noise and satellite geometry. For instance, under open sky conditions, GPS-based solutions have an accuracy of 3 - 5 meters and a computational time of 3.6 seconds [54]. In the case of GSM-based solutions, they have an accuracy of 65 - 134 meters [10] and a computation time of 7.04 milliseconds [20]. Improving the accuracy and computational time of the positioning technology technologies is not a topic of this paper.

## 7.2 Results

We now present our experiment results, which evaluate the performance of our schemes using the metrics defined in Section 7.1.3. Note that we do not consider the network-communication time.

**Storage-Size:** Figure 9(a) shows the total storage size occupied by each of the approaches. The blue and red colors represent the storage size at the ACS and LBS provider, respectively. The 2IABE approach requires more storage capacity. However, the difference between the storage capacity of both approaches is minimal (2 percent in our scenario).

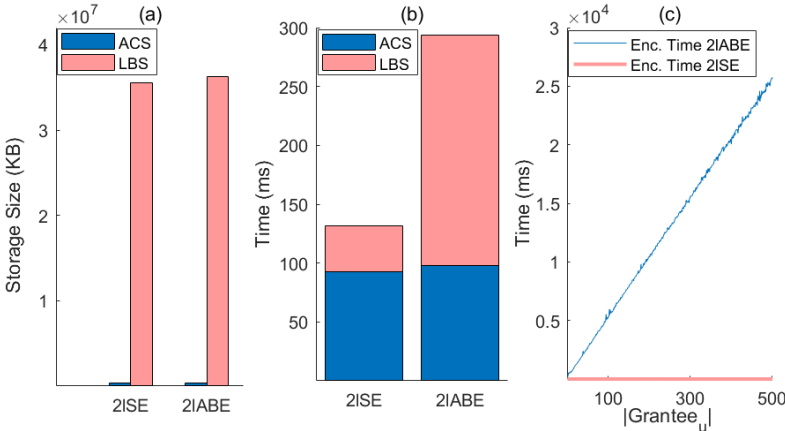


Fig. 9. Storage size(a), Access request time (b) and Encryption time (c)

**Access request time:** Given an authorized access request  $accessReq(u,v)=true$ , we measure the time required by the grantor  $u$  to generate and add the information needed at the ACS and the LBS provider, with each approach. Figure 9(b) shows the average access request time with both

approaches for our sample. Both approaches require the same amount of time to generate and store the corresponding information at the ACS (blue color). With the *2LABE* approach, the grantors require more time to generate and store the information at the LBS provider. That is because of the different encryption scheme used to encrypt the usernames stored at the LBS provider. One could think that our results are specific to the number of grantees of the users in our sample. Next, we show that our results apply to any number of grantees. Lemma 6.2 shows that the encryption complexity using CP-ABE, which is used by the *2LABE* approach, depends, among others, on the number of grantees that a user has. To analyze in-depth, the effect of each encryption scheme, we select a user and increase his number of grantees, starting from 1 up to 500. Next, we measure the time required by the user to encrypt his username against the size of his set of grantees. Figure 9(c) shows the encryption time with both approaches. One can observe that even for a set of grantees with cardinality one, the *2ISE* approach performs better than the *2LABE*. Moreover, as expected from our complexity analysis, the encryption time with the *2LABE* grows linearly with the number of grantees. With the *2ISE* the encryption time is constant because each grantor generates a different ciphertext for each of his grantees. Consequently, with the *2ISE*, the encryption time of each ciphertext is independent of the number of grantees of a user. With the *2LABE*, although each grantor generates only one ciphertext, which can be accessed by all of his grantees, the number of operations required to encrypt a ciphertext depends, among others, on the number of grantees.

*Query time:* Figures 10(a), 10(b), and 10(c) show the average query processing time for each of the ten classes at the ACS, the LBS provider, and the user, respectively. The query processing times of the LBS provider and ACS with the *2ISE* approach are greater than that of the ones with the *2LABE*. In contrast, the query processing time of the user with the *2ISE* approach is less than the one with the *2LABE*. We explain this as follows: First, with the *2ISE*, the LBS provider performs an additional search to recover the encrypted version of the name, which can be decrypted by the querying user. The LBS provider does not perform this search with the *2LABE* because it stores one encrypted version of the name for each user. Second, with the *2ISE* approach, the ACS decrypts three ciphertexts for each user in the query answer: the second layer of the encrypted name of  $u$ , the encrypted square distance, and the encrypted public number  $Z$ . With the *2LABE* approach, it decrypts only the encrypted square distances and the second layer of the encrypted names. Third, with the *2ISE* approach, the user has to compute the shared key and decrypt the names encrypted with symmetric encryption. With the *2LABE* the user decrypts the names encrypted with CP-ABE. The encryption/decryption process using CP-ABE is computationally more expensive than the one using symmetric encryption and even more expensive than computing the shared keys and decrypting. In the end, the query processing time of the *2LABE* at the LBS provider and the ACS is less than the one with the *2ISE*. However, the user-side performance of the *2ISE* is that much high that it compensates the advantages of the *2LABE*. Figure 10(d) shows that the total average query processing time, i.e., the sum of the times required by the LBS provider, the ACS, and the user, with the *2ISE* approach is much less (approximately by a factor of 2) than the one with the *2LABE*.

*Discussion:* One important difference between both approaches that affect query performance is the encryption scheme used to encrypt the usernames. In general, in our scenario, as our experimental results show, having multiple encrypted copies of a message (*2ISE*) is more efficient in terms of query performance. The additional search process needed with the *2ISE* approximately doubles the query processing time at the LBS provider side compare to the one with the *2LABE* approach. The opposite happens at the user-side, where the decryption time, with the *2LABE*, increases by more than twice compared to the one with the *2ISE*. However, the time contribution to the total query processing time of the LBS provider is less in comparison to that of the user. These differences are reflected in the total query processing time, where the *2ISE* approach is twice more efficient than the *2LABE*, which is impressive. Therefore, one can say that the 2 percent extra storage

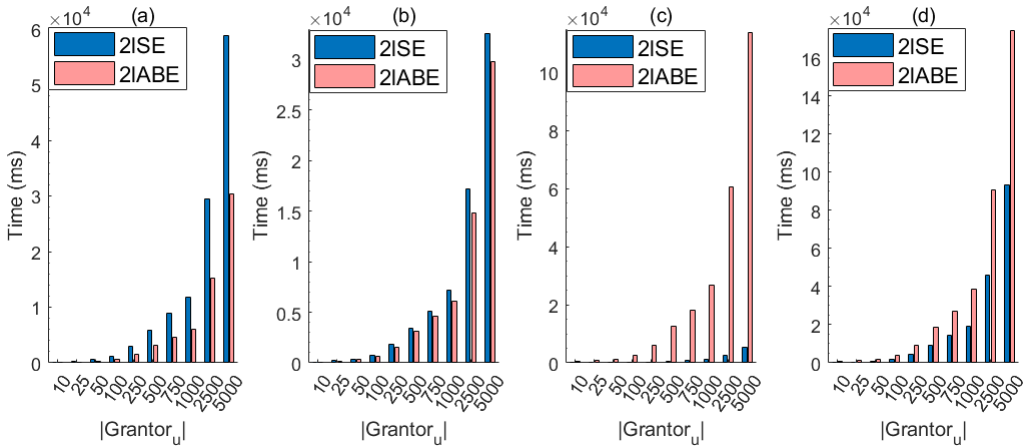


Fig. 10. Average query processing time at the ACS (a), the LBS provider (b) and the user-side (c). Total average query processing time (d)

required by the *2ISE* pays off with better query performance. Our results not only apply to real online social networks like Facebook and LiveJournal, where the average number of connections of a person, i.e., the size of the set of grantors, is 322 [41] and 520.04 [24], respectively, but also to unrealistic scenarios where the size of the set of grantors is 5000. These results are in line with our complexity analysis, and one may interpret them as an indication that our analysis also holds for the average case. Consequently, the *2ISE* approach is the most feasible option in our scenario.

## 8 RELATED WORK

We categorize exiting works aiming to preserve location secrecy in two groups: location secrecy in LBS and location secrecy in mSNs. The difference between these groups is that approaches in the first one do not consider access policies, i.e., users can access the location of any user in the system.

**Location secrecy in LBS:** Existing techniques that achieve location secrecy in LBS are:

**Mix zones:** The key idea of these approaches is to prevent adversaries from tracking long-term user movements [5]. A mix zone is a spatial region with a predetermined size, inside which users do not report their position to the LBS provider. These approaches focus on data anonymization and replace the user identity with a pseudonym. They offer anonymity guarantees by changing the pseudonyms of users inside a mix zone such that an adversary is unable to link users that go inside a zone with those leaving it. The position of users outside the mix zones is disclosed. Then queries are executed on plaintext data. Users inside the mix zones do not communicate with the LBS provider; so they cannot get any service. This lack of communication affects functionality.

**Coordinates transformation:** Approaches in this area aim to guarantee that an adversary does not learn the position of the users. These approaches map the location of users to another space coordinate and address the query on the transformed space. In the approach presented in [17], users use a transformation function over their physical position before sending it to the LBS provider. The transformation function consists of shifts and rotations. Each user sets the parameters of the transformation function and distributes these parameters among the rest of users to allow them to recover the original position. This approach is subject to data reconstruction attacks [22]. To avoid this kind of attacks, the authors in [28] use agents to transform the physical positions of users. Agents are trusted third parties servers that act as middleware between the users and the LBS provider. Agents periodically change their transformation functions, which prevents the adversaries

from analyzing the data. These approaches allow users to query for one specific user at each time, i.e., point queries. The secrecy of this approach relies on trusted third servers.

**Cryptography:** Approaches like [35, 55] keep the position of users secret from adversaries including the service provider. They use encryption techniques and hash functions to compute proximity between two users privately. The authors in [55] use, besides hash functions, location tags to prevent users from announcing unreal locations. Location tags are pieces of information obtained from the network protocol like 802.11 frames in WiFi networks. These approaches allow users to query for the proximity of one specific user at each time, i.e., point queries.

**Location secrecy in mSNs:** Approaches in this area restrict access to the position of users based on access control policies. Each user defines a set of users who are authorized to read his position. The scheme proposed in [39] guarantees location secrecy by using encryption and coordinate transformation techniques. The LBS provider stores the transformed data. Querying requires that users distribute among their friends the transformation parameters and the corresponding decryption keys. This scheme focuses on dealing with point and nearest neighbor queries. Wei et al. [48] proposed an approach called Mobishare. The architecture of Mobishare consists of a trusted central tower, an untrusted LBS provider, and an untrusted Access Control Server (ACS). Mobishare uses dummy techniques to prevent the LBS provider and the ACS from learning the users identities and their positions. Before outsourcing the data to the LBS provider, Mobishare replaces users identities with pseudonyms and adds dummy pseudonyms together with dummy locations. The position of users is stored in plaintext; so the LBS provider can compute any query. Before sending the final query answer to the user, the ACS filters the data based on the access policies, and the central tower replaces pseudonyms with user identities. However, an adversary who can observe query executions will be able to identify real pseudonyms from dummy ones. An adversary could use such information to link a pseudonym with a user identity and therefore learn the position of the user. The adversary could also learn the access policies, i.e., the set of users that have allowed a given user to access their position. To avoid these issues, the authors in [25] extended Mobishare by adding dummy queries and using a private set intersection protocol. The authors in [26] extended the latter approach by introducing a new architecture with multiple LBS providers. Their approach aims to prevent an adversary from identifying queries coming from the same user, which could be used to learn the users identities. To conclude, approaches in this area focus on point or nearest neighbor queries, or they rely on trusted central towers. Furthermore, their adversary model is weaker than ours, as explained in Section 2.2.

Besides the works discussed in this section, there are works that propose solutions to interesting problems related to mobile devices and location services, such as user authentication [2], location tracking techniques [1], and congestion problems in mobile device clouds [4]. However, they are examples of work that does not solve our specific problem—secrecy guarantees in LBS.

## 9 CONCLUSION

Location-based services are an important feature provided by mSNs. However, users usually are reluctant to share their position with others due to privacy reasons. In this paper, we have shown how to offer LBS, in the example of range queries, in mSNs with a revocation feature while providing to the users the secrecy guarantees  $G_{position}$ ,  $G_{distance}$ , and  $G_{authorization}$  under collusion assumption. We introduced two approaches namely two-layer symmetric encryption, *2ISE*, and two-layer attribute-based encryption, *2IABE*. The main differences between them is that they use, among other encryption schemes, symmetric and attribute-based encryption, respectively. A complexity analysis of the query phase tells us that both approaches differ only at one entity—the user-side. Their differences rely on the decryption process, which is related to the encryption scheme used. We have further compared our approaches experimentally. Although with the *2IABE*,

the key management is more straightforward than with the *2ISE*, and the LBS provider stores a single encrypted copy for each message, we found that our former solution is on average twice more efficient in our scenario.

In the future, it will be interesting to study how to offer location-based services in mSNs with different kind access policies while providing secrecy guarantees. For instance, one can consider integrating mutual authorizations [46], where users grant access to their resources, i.e., physical positions, to users that allow them the same, or location constraints [6], where users restrict access to their resources based on the location of the accessing user.

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