Gas permeation through single-crystal ZIF-8 membranes
Chen Chen¹, Aydin Ozcan², A. Ozgur Yazaydin², and Bradley P. Ladewig¹,³*

¹Barrer Centre, Department of Chemical Engineering, Imperial College London, SW7 2AZ, United Kingdom
²Department of Chemical Engineering, University College London, WC1E 7JE, United Kingdom
³Institute for Micro Process Engineering, Karlsruhe Institute of Technology, Hermann-von-Helmholtz-Platz 1, Eggenstein-Leopoldshafen, 76344, Germany
*e-mail: b.ladewig@imperial.ac.uk

Abstract
Grain boundaries are an unavoidable microstructural feature in intergrown polycrystalline metal-organic framework (MOF) membranes. They have been suspected to be less size-selective than a MOF’s micropores, resulting in suboptimal separation performances – a speculation recently confirmed by transmission electron microscopy of MOF ZIF-8. Single-crystal membranes, without grain boundaries, should confine mass transport to micropores and reflect the intrinsic selectivity of the porous material. Here, we demonstrate the feasibility of fabricating single-crystal MOF membranes and directly measuring gas permeability through such a membrane using ZIF-8 as an exemplary MOF. Our single-crystal ZIF-8 membranes achieved ideal selectivities up to 28.9, 10.0, 40.1 and 3.6 for gas pairs CO₂/N₂, CO₂/CH₄, He/CH₄ and CH₄/N₂ respectively, much higher than or reversely selective to over 20 polycrystalline ZIF-8 membranes, unequivocally proving the non-selectivity of grain boundaries. The permeability trend obtained in single-crystal membranes aligned with a force field that had been validated against multiple empirical adsorption isotherms.

Keywords: metal-organic framework, single crystal, ZIF-8, gas permeation, ideal selectivity
1. Introduction

Metal-organic frameworks (MOFs) are commonly defined as potentially porous coordination polymers made of metal nodes and organic ligands extending in two or three dimensions [1]. Reticular syntheses [2] afforded MOFs a wide range of tailorable pore apertures from 3.0 Å in ZIF-11 [3] to 98 Å in IRMOF-74-XI [4], corresponding to diverse molecular sizes from those of small gases (e.g. hydrogen) to natural proteins. Post-synthetic modifications can usually alter the reactivity of a MOF through its linkers [5]. These two developments have made MOFs strong contenders in adsorption- and membrane-based separations [6, 7]. In the domain of membrane-based gas separations, MOFs are typically used as either the selective layer in polycrystalline pure-MOF membranes [8], or the stability- and permeability-enhancing filler in mixed-matrix membranes (MMMs) [7, 9]; a few MOFs even simultaneously increase permeability and selectivity of MMMs [10, 11].

From a design point of view, polycrystalline pure-MOF membranes are theoretically advantageous over MMMs because a pure-MOF membrane’s selectivity should be predictable – close to the optimal, molecular-sieving selectivity of the MOF’s pore aperture size [7] – as long as the membrane is properly intergrown and crack-free. Many endeavours have been dedicated to fabricating a crack-free polycrystalline MOF membrane over a substrate by optimising a) chemistry of the precursor solutions [12], b) chemistry of the substrate [13, 14], c) membrane growth method or set-up [15-17], or d) a combination of the aforementioned three [18, 19]. One of such well-engineered polycrystalline ZIF-8 (Zn(MeIM)_2, MeIM = 2-methylimidazole) membranes used the pore aperture of ZIF-8 (3.4 Å) to score an exceptional separation factor of 105 for propene (kinetic diameter: 4.0 Å) over propane (kinetic diameter: 4.3 Å) [12].

Despite these remarkable developments, polycrystalline membranes, by their very nature, always contain grain boundaries that have been suspected to be non-size-selective thus undermining separation performances [6, 20-23] (Fig. 1). A recent breakthrough in
transmission electron microscopy (TEM) imaging by Zhu et al revealed for the first time the grain boundary structure in a MOF [24]. They recreated the self-assembly process of the interface between two ZIF-8 crystals joint via the (110) plane by molecular dynamics simulation, Two of the three interconnected channels at the grain boundary (~8.2 Å and ~3.8 Å in diameter) were larger than the six-membered-ring channels (3.4 Å in diameter) of ZIF-8; self- and transport-diffusivities of guest molecules were higher in samples with grain boundaries.

**Fig. 1.** A schematic diagram showing the possible grain boundary structure in a polycrystalline ZIF-8 membrane. A molecule, such as propane, that is too large to go through the six-membered-ring channel of ZIF-8 may be able to permeate through the larger grain boundary structure (red dotted rectangle).
Single-crystal membranes (SCMs) are widely recognised as the ideal tool to study a material's intrinsic permeation selectivities [6, 20, 21, 25], and are the assumed model in computational predictions of MOF-membranes' separation performances [26-28]. Single crystals have proved useful for studying intrinsic diffusion properties – infra-red imaging monitored the CO$_2$ uptake and revealed the concentration evolution within a ZIF-8 crystal [29] and at the crystal-polymer interface [30]. However, there are very limited attempts at using single crystals in a membrane configuration to investigate the intrinsic permeation properties because of lack of practical applications of these membranes [31] and fabrication difficulties [32, 33]. Since single-crystal zeolite membranes fabricated more than three decades ago [32, 34, 35], only one one-dimensional coordination polymer (i.e. by definition, not a MOF [1]) [Cu$_2$(bza)$_4$(pyz)$_n$ (bza = benzoate; pyz = pyrazine)$_{21}$] and its analogues [36, 37] have been made into SCMs. There was, regrettably, no comparison between these SCMs and polycrystalline membranes of the same materials in terms of permeance or selectivity. In our proof-of-concept study of gas permeation through a single-crystal MOF membrane, ZIF-8 was chosen as a representative material because of the readily available data on ceramic-supported polycrystalline ZIF-8 membranes for comparison.

A large crystal is a prerequisite for single-crystal membranes for practical reasons – it would be prohibitively difficult to manually pick up and orient the crystal in the subsequent stage of membrane fabrication. Based on our experience, crystals of at least 100 micrometres are worth being considered for further processing. In order for the downstream pressure to be measured with better accuracy, we needed crystals of a few hundred micrometres – a demanding size as most crystallisation studies aimed to make nanosized crystals [38]; this is also pushing the upper limit of ZIF-8 size reported to date (around 300 µm) – first synthesised by Chmelik et al [39] and reproduced or adapted in many other studies [31, 40-45]. Crystal growth is a highly complex and intractable process [46]. It is impossible and beyond the capacity of this work to predict a complete set of parameters that will guarantee
the unusually large crystals; instead, we built upon methods that have produced the largest ZIF-8 crystals reported.

Here we report permeabilities of light gases (helium, carbon dioxide, nitrogen and methane) through a single-crystal membrane of ZIF-8, and compare the single-crystal ideal selectivities with polycrystalline ZIF-8 membranes. These light gases constitute industrially relevant separations. Carbon dioxide and nitrogen are the main impurities in natural gas [47], which is also an important source of the increasingly demanded helium [26, 48]. Separating CO$_2$ from N$_2$, the largest component of flue gas, is essential to curbing CO$_2$ emission [49]. To the best of our knowledge, this is the first direct measurement of gas permeation through a single-crystal MOF membrane. Without interference from non-selective grain boundaries or inter-crystalline defects, the single-crystal ideal selectivities can be considered intrinsic to ZIF-8 as permeation occurs through micropores only. We believe that intrinsic selectivities are of great interest to the microporous membrane community as these values could provide a benchmark for polycrystalline ZIF-8 membranes' performance.

2. Experimental

2.1. Synthesis of ZIF-8 (Optimised protocol)

1.764 g (5.93 mmol) of zinc nitrate hexahydrate (≥98%, Sigma-Aldrich) was dissolved in 15 ml of methanol (≥99.8% HiPerSolv CHROMANORM® grade, VWR UK). 0.9739 g (11.86 mmol) of 2-methylimidazole (99%, Sigma-Aldrich) and 0.4034 g (5.93 mmol) of sodium formate (99%, Sigma-Aldrich) were dissolved in 25 ml of methanol. The two solutions were combined and mixed briefly for 5 minutes on a stirring plate. Meanwhile, 3 new 20-ml crimp-cap glass vials (Kinesis UK) were rinsed with methanol and set aside with their caps loosely placed over them to prevent dust or any particulates from entering the vials. 13 ml of the combined precursor solution was drawn by a syringe and passed to each glass vial through a 0.2-µm polytetrafluoroethylene (PTFE) syringe filter (VWR UK). The vials were sealed by a manual crimper (Kinesis UK) and placed in a 90-°C oven for 24 hours. The vials were left to
cool naturally in the oven until they were safe to touch. Large crystals on the wall of vials (Fig. S7) were carefully picked up by PTFE tweezers with fine, pointed ends and released into a small snap-cap vial of fresh methanol. Both the manually selected crystals and the leftover crystals were soaked in fresh methanol replaced every 24 hours for 2 days – the extensive solvent exchange was to increase the chance of removing unreacted precursor chemicals. The crystals were dried in a vacuum oven at 25 °C for 6 hours. The manually selected crystals were inspected under an optical microscope. Single, visually defect- and crack-free crystals with the characteristic dodecahedron shape of ZIF-8 were kept for membrane fabrication and single-crystal XRD. The leftover crystals were kept in another container for powder XRD, nitrogen adsorption and other characterisation studies.

2.2. PXRD studies

Powder X-ray diffraction spectra were collected by an PANalytical X’Pert Pro diffractometer with a CuKα X-ray source (40 kV, 20 mA) and a reflection-transmission spinner sample stage at ambient conditions. Large crystals were ground before pressed onto the sample holder to obtain a flat surface.

2.3. Nitrogen sorption

Nitrogen sorption measurement was performed on a Micromeritics 3Flex volumetric instrument at 77 K. The sample was evacuated at 100 °C under vacuum overnight, followed by 2 hours of in situ degassing at 100 °C under vacuum prior to the start of nitrogen sorption analysis. BET surface area was estimated from the quantities adsorbed at relative pressures between 0.045 and 0.299.

2.4. Construction of single-crystal membranes

We adapted the single-crystal zeolite membrane model designed by Geus et al [35] because of its simplicity and compatibility with a commercially available membrane holder (Merck Millipore, XX4404700). Steel plates (47 mm in diameter, 0.37 mm in thickness) with a 400-
µm-diameter hole drilled in the centre were made in-house and cleaned with acetone. The construction was carried out under an optical microscope. Epoxy (Araldite, rapid 2-component epoxy) was spread around the hole and pushed to the rim of the hole as closely as possible without going over the rim. Five minutes later, a ZIF-8 crystal, held by high-precision plastic tweezers (ideal-tek, 707A.DG), was placed over the epoxy with its large flat base parallel to the steel plate, and secured in place by a gentle push. We allowed the first layer of epoxy to partially set so that it would not overflow the rim of the hole and cover the bottom of the crystal. A fresh batch of epoxy was made and spread around the crystal to ensure a gas-tight seal. The membrane assembly was left at ambient conditions overnight for the epoxy to cure.

2.5. Gas permeation measurements

The constant-volume, pressure-rise apparatus (Fig. S5) was used to measure gas permeation. After the membrane was placed in the permeation cell and sealed by a Viton O-ring, each segment of the rig was evacuated for 5 to 30 minutes depending on the size of the segment. Gas was introduced to the upstream tank until the pressure stabilised at around 2.1 bar absolute (or 31 psia). The system was left in this state for 2 days, which we observed was enough for the downstream air ingress to reach a steady-state, whilst the pressure gauges 1 and 2 (Fig. S5) were recording continuously. The valve V-2 was then opened; the upstream and downstream pressures were recorded for another 2 days.

3. Results

3.1. Synthesis of large, single crystals of ZIF-8

The plethora of chemical and process variables used to synthesise the same MOF makes it challenging to systemically and extensively investigate crystallisation processes. For example, ZIF-8 have been made from various Zn\(^{2+}\) salts (nitrate, acetate, sulfate, chloride, bromide, iodide, perchlorate etc) [12, 50, 51], with or without [52, 53] a modulator, in different solvents (water, alcohols, dimethylformamide, dimethyl sulfoxide, acetone etc) [52-54] with
different molar ratios of reactants at a range of temperatures [55]. To further complicate the matter, the variables may not be independent from each other – one could behave differently when combined with different sets of other variables. For example, sodium formate, a common modulator in ZIF-8 syntheses, was observed to accelerate nucleation and result in smaller ZIF-8 crystals in a solvothermal synthesis [41]; the same modulator served the opposite purpose (i.e. slowing down nucleation and facilitating the formation of bigger ZIF-8 crystals) in an ambient-condition synthesis with stirring [40]. Some studies have tried to control the crystal size of ZIF-8 by adjusting a few variables [50, 56]; however, the large array of variables means our understanding of crystal size engineering is merely fragments of the whole picture. In view of these challenges, it is more realistic to fine-tune existing protocols than designing the optimal one ab initio.

On the basis of the largest-to-date ZIF-8 [31, 39], we formulated a reproducible synthesis protocol that made large single crystals of ZIF-8 up to 1 mm (Fig. 2a). Most of the crystals that appeared to be single, crack-free under the microscope were above 500 µm (Fig. S2a). The optimal protocol was finalised after varying the zinc salt, synthesis temperature and the modulator concentration (Supplementary Information 1.1); the observations did not always agree with what previous studies suggested, highlighting limitations of the current knowledge of crystal size engineering. For example, we consistently obtained larger crystals from zinc nitrate than from zinc chloride, whilst the opposite was reported in the literature [12, 50]. Also, we postulated that two opposing roles – deprotonation agent and competitive ligand – of the modulator were present instead of just one (Supplementary Information 1.1). Connecting the fragments of existing insights to form the complete picture of ZIF-8 size control is well beyond the capacity of this work; nonetheless, we found that a few simple steps of removing undesired nucleation sites (filtering the precursor solution, using high-purity solvent and rinsing new glass vials with high-purity solvent) helped achieve bigger crystals than the original methods [31, 39] and ensure the reproducibility of our protocol.
Fig. 2. (a) A micrograph of a millimetre-sized single crystal ZIF-8 viewed along [110] axis. (b) Powder X-ray diffraction (PXRD) pattern of two batches of ZIF-8 from which large, single crystals were selected to make membranes. The two batches were made with the same conditions (in methanol at 90 °C for 24 hours, i.e. the optimised protocol in Section 2.1). After large, single crystals were isolated, the remaining product was used for PXRD. The simulated pattern was from Park et al [3].

Single-crystal X-ray diffraction (Table S3) and powder X-ray diffraction spectra (Fig. 2b) were collected to confirm that the product was indeed high-quality ZIF-8. A Type 1 adsorption isotherm characteristic of microporous materials [57] was obtained from nitrogen sorption at 77 K (Fig. S1), from which the Brunauer–Emmett–Teller surface area was calculated to be 1,490 m² g⁻¹, within the range of literature values from 960 to 1,918 m² g⁻¹ compiled by Huang et al [58].

3.2. Single-crystal membrane fabrication

In order to test gas permeation through a SCM in a commercially available permeation test cell (Merck Millipore, XX4404700), we glued the selected single crystal to a steel plate (47 mm in diameter, 0.37 mm in thickness) with a 400-µm-diameter hole drilled in the centre. Two single-crystal ZIF-8 membranes, ZIF8-SCM-1 and ZIF8-SCM-2 (Figs. 3a and 3b) containing single crystals ZIF8-1 and ZIF8-2 respectively, were fabricated and tested. ZIF8-1
and ZIF8-2 were perfect-looking single crystals of ZIF-8 selected from two identical syntheses detailed in Methods.

Although ZIF-8 is isotropic and has identical six-membered channels along the [111] direction, it has another set of inaccessible four-membered channels in the [100] direction [18, 59]. Therefore, having the pressure gradient in the [111] direction makes the ideal orientation; and [100] direction, the most unfavourable because of a more torturous permeation path. We did not engineer the growth direction of ZIF-8 crystals. Serendipitously, most of the single crystals harvested from the wall of a glass vial grew along similar directions – somewhat between [111] and [110] – as seen by comparing the Figs. 3a and 3b with Fig. S4. Conveniently, they were ‘half crystals’ – half of a whole rhombic dodecahedron – with a large, flat surface (Fig. 3b inset) originally in contact with the wall. This large, flat surface became the base parallel to the steel plate and perpendicular to the pressure gradient direction (Fig. 3c). Therefore, harvesting single crystals from the wall of glass vials proved beneficial in two ways – a) it reduced the chance of picking up intergrown crystals, and b) it helped ensure a rather consistent orientation of the embedded crystal in the membrane assembly.
Fig. 3. (a) Micrographs of the top and bottom views of ZIF8-SCM-1. (b) Micrographs of the top and bottom views of ZIF8-SCM-2, inset: the crystal that was embedded in ZIF8-SCM-2.
Our SCM assembly has its limitations. Firstly, the embedded crystal does not have a set of parallel surfaces (Fig. 3c), resulting in uneven thickness – the average thickness was used in permeability calculations. There are errors associated with averaging and even the method of using the average thickness (Supplementary Information 1.4.4); however, they will not affect the ideal selectivities of each membrane because when taking the ratio of two permeabilities, the thickness term disappears (Supplementary information 1.4.1). Secondly, the thickness far exceeds what is conventionally acceptable for a membrane. This is the side effect of using a large ZIF-8 crystal as the crystal grows in all three dimensions. We decided not to polish the brittle crystal to protect its integrity. Future work may consider polishing methods that do not damage the crystal, or using MOFs that naturally have a plate-like morphology. Lastly, the extremely small permeation area (i.e. the area of the hole on the steel plate) presents a challenge to the downstream pressure measurement. We kept the downstream volume of the rig (Fig. S5) is kept to the minimum – just the internal volume of the necessary tubing – so that the pressure transducer can pick up any change caused by the small amount of permeate.

3.3. Single-gas permeation and ideal selectivities

Single-gas permeabilities of both single-crystal membranes agree with the trend reported by other ZIF-8 membranes – permeability is generally inversely proportional to the kinetic diameter of the permeant, and framework flexibility [31, 60] allows transport of molecules larger than the aperture size (Table S1 and Fig. S6). We compared our SCMs’ ideal selectivities of four industrially important separations (CO₂/N₂, CO₂/CH₄, He/CH₄ and CH₄/N₂) with over 20 polycrystalline ZIF-8 membranes that measured single-gas permeation of common small gases at room temperature (Fig. 4 and Table S2). Some polycrystalline ZIF-8 membranes such as the those reported by Brown et al [61] and Marti et al [62] were not included in the comparison because the Torlon polymer substrate showed an ideal CO₂/N₂
selectivity of 0.90 [63] – higher than the Knudsen value of 0.8. The macroporous substrate might have affected permeation through adsorption.

Despite the disparity in our two SCMs’ ideal selectivities, they are almost always well above the Knudsen selectivities and polycrystalline ZIF-8 membranes’ selectivities for all four gas pairs. Most of the polycrystalline selectivities do not reflect a remarkable improvement from – some were even below – Knudsen selectivities, suggesting that the molecular sieving potential of ZIF-8 was not fully achieved in those membranes. Interestingly, both SCMs were CH₄-selective whereas most polycrystalline ZIF-8 membranes had ideal CH₄/N₂ selectivities fluctuating around unity, showing no selectivity or marginal N₂-selectivity (Fig. 4d). Two membranes [64, 65] showed superior or similar CO₂/CH₄ selectivity to ours (Fig. 4b), but neither membrane could match our results in other gas pairs. Thus, their exceptional CO₂/CH₄ selectivities should not be generalised to indicate superior membrane performance.
Fig. 4. Single-crystal ZIF-8 membranes’ ideal separation performance in (a) CO₂/N₂, (b) CO₂/CH₄, (c) He/CH₄, and (d) CH₄/N₂ at room temperature (20 – 25 °C). The ideal selectivities are compared with polycrystalline ZIF-8 membranes (Table S2) and Knudsen selectivity. Knudsen selectivity is commonly used to benchmark a membrane’s performance – molecular sieving if membrane’s selectivity is above the Knudsen selectivity; containing pinholes or mesopores otherwise. There are fewer literature values available for helium as it has not been as extensively tested as other small gases. The effective/average thicknesses of ZIF8-SCM-1 and ZIF8-SCM-2 were around 382 µm and 292 µm respectively. The method of calculating the average thickness is explained in Supplementary Information 1.4.4 and Fig. S10.

Unlike polycrystalline ZIF-8 membranes that are mostly non-selective or N₂-selective over CH₄ (Fig. 4d), our SCMs showed reverse selectivity for CH₄ over N₂. Experimental single-component adsorption isotherms at 25 – 30 °C revealed that ZIF-8’s uptake of CH₄ almost double that of N₂ between 0 and 1 bar [66], i.e. the adsorptive CH₄/N₂ selectivity is around 2. The linear isotherms suggest that we can expect the adsorptive selectivity to continue being 2 at our upstream pressure of 2 bar. On the other hand, the small difference in the two molecules kinetic diameters (N₂: 3.64 Å, CH₄: 3.8 Å), coupled with ZIF-8 framework flexibility, means the diffusive selectivity of N₂ over CH₄ should be marginal. Indeed, the ratio of total diffusion coefficients N₂/CH₄ in ZIF-8 was predicted to be 1.38 computationally by Battisti et al [67], giving a diffusive CH₄/N₂ selectivity of 1/1.38 = 0.724. The adsorption-diffusion model suggests that the permeability (or membrane) selectivity is approximately the product of adsorptive and diffusive selectivities [68, 69], the permeability selectivity should therefore be approximately 2 × 0.724 = 1.45, making ZIF-8 CH₄-selective over N₂, in line with our SCMs’ performances.

We also compared our ideal selectivities with four sets of in silico results based on four widely used flexible force fields [70-74] for molecular simulations of ZIF-8 (Supplementary
Information 1.5). Helium was not modelled because of its nearly non-adsorbing nature at room temperature. We believe the force field proposed by Wu et al [71] is more accurate than the other three because it was validated against the experimental adsorption isotherms of N₂, CO₂ and CH₄ at 298 K whereas others were only compared with one of the gases. The ideal selectivities obtained from Wu et al’s force field (Table S7) agree with our permeability trend of CO₂ > CH₄ > N₂ (Table S1) – an additional validation of their force field. The grain boundary structure may provide an explanation on why polycrystalline ZIF-8 membranes tend to be N₂ selective over CH₄. There is an extra layer of the 2-methylimidazolate ligands at the grain boundary [24] which are the binding sites for N₂ [72]. Therefore, with additional imidazolate rings at grain boundaries, a polycrystalline membrane may have higher N₂ adsorption capacity than that in a single crystal, giving a lower and even reverse CH₄/N₂ membrane selectivity.

We do not know with absolute certainty what caused the disparities in the two SCMs' selectivities. The disparity is larger when the gas pair involves a slow-permeating gas such as N₂ and CH₄. A small quantity of ingress air could not be avoided during the extended test period – a method to correct for this is described in the Supplementary Information 1.3. As only a small amount of N₂ or CH₄ will accumulate in the downstream over the duration of a measurement, it is much more crucial to account for air ingress when testing N₂ and CH₄ than a fast-permeating species like He. Our method of background subtraction may not be robust enough for N₂ and CH₄; a high-vacuum set-up in the downstream or a sweep gas in conjunction with a gas chromatography may improve the consistency across different membranes. Having said that, we are aware that it is common to observe nonuniformity among single crystals because of variations in crystal quality [34].

4. Discussion

Our work is a proof of concept that direct measurements of gas permeabilities through a single-crystal MOF membrane can be achieved. More importantly, it provided like-for-like
comparisons between polycrystalline and single-crystal MOF selectivities. The postulation that a single-crystal zeolite membrane may have higher separation factors than the polycrystalline version is not new [32]; however, there was no direct comparison in any SCMs [21, 32, 34, 35] prior to our work. Such comparison was either not part of the objectives of those studies, or unachievable due to the lack of polycrystalline membranes or the lack of data under similar test conditions. By choosing an extensively studied MOF ZIF-8, we showed that by eliminating grain boundaries and constraining gas transport to intracrystalline pores, single-crystal ZIF-8 offered consistently higher ideal selectivities than polycrystalline ZIF-8 membranes for all gas pairs of interest.

This implies that grain boundaries indeed provide a less-selective route than ZIF-8’s 6-membered-ring channels. With better-engineered synthetic protocols, it is possible to fabricate intergrown, macroscopic-defect-free polycrystalline membranes; but the corollary of a polycrystalline membrane is the presence of grain boundaries. Our results corroborated Zhu et al’s conclusion from molecular dynamics simulations of small gases and kinetic vapour adsorption of toluene and 1,3,5-trimethylbenzene in ZIF-8 structures with and without interfacial structures – that the larger interfacial openings in ZIF-8 increase the transport diffusivities of guest molecules. The discovery that larger molecules’ mass transport is increased by a greater extent [24] means the diffusive selectivity $D_i/D_j$ where $D$ is diffusion coefficient, $i$ is the smaller molecule and $j$ the larger, is reduced by grain boundaries. Since permeability selectivity is the product of adsorptive and diffusive selectivities, polycrystalline ZIF-8 membranes will exhibit lower permeability selectivity than a SCM.

5. Conclusions
We measured single-gas permeabilities of He, CO$_2$, N$_2$ and CH$_4$ through two single-crystal ZIF-8 membranes and obtained ideal selectivities that are intrinsic to the chemistry and porous structure of ZIF-8 in the absence of other transport routes such as less selective grain boundaries. Our single-crystal membranes displayed consistently higher ideal CO$_2$/N$_2$,
CO\(_2/\text{CH}_4\) and He/\text{CH}_4 selectivities of than an overwhelming majority of ceramic-supported polycrystalline membranes reported in the literature, and reverse \text{CH}_4/N\text{_2} selectivity compared with most polycrystalline membranes. The reverse \text{CH}_4/N\text{_2} selectivity was supported by simulation and could be explained by the extra imidazole rings, where N\text{_2} interacts with strongly, at grain boundaries. It is not our slightest intention to trivialise the breakthroughs in the field of polycrystalline membranes; they are, after all, a beacon of hope for the commercialisation of MOF membranes. What we want to demonstrate through our work is that grain boundaries in ZIF-8 contribute to mass transport and reduce ideal selectivity. With the accuracy of single-crystal membrane measurements improved in the future, they could provide useful empirical results for validation of new force fields.

**Acknowledgements**

C.C. thanks Nicholaus Prasetya for assistance with the gas permeation rig. We thank Dr Andrew White for collecting and refining single-crystal X-ray diffraction data, and staff at the Imperial Chemical Engineering Department Workshop for making the steel plates.

**Appendix A. Supporting information**

Supplementary data associated with this article can be found in the online version at:

The simulations are available from the repository located at:

https://doi.org/10.5281/zenodo.1435643
References


Supplementary Information

Gas permeation through single-crystal ZIF-8 membranes

Chen Chen¹, Aydin Ozcan², A. Ozgur Yazaydin², and Bradley P. Ladewig¹,³*

¹Barrer Centre, Department of Chemical Engineering, Imperial College London, SW7 2AZ, United Kingdom

²Department of Chemical Engineering, University College London, WC1E 7JE, United Kingdom

³Institute for Micro Process Engineering, Karlsruhe Institute of Technology, Hermann-von-Helmholtz-Platz 1, Eggenstein-Leopoldshafen, 76344, Germany

*e-mail: b.ladewig@imperial.ac.uk
1. Supplementary Text

1.1. Variations in ZIF-8 synthesis protocol
1.2. Epoxy non-permeability check
1.3. Method to account for downstream air ingress
1.4. Calculation details
1.5. Self-diffusion coefficients of CH₄, CO₂ and N₂ in ZIF-8 from molecular simulations

2. Supplementary Figures

Figure S1: Nitrogen isotherms at 77 K.
Figure S2. Micrographs of ZIF-8 crystals made with various changes in precursors at 90 °C.
Figure S3. A micrograph of ZIF-8 crystals made from zinc nitrate hexahydrate at 70 °C.
Figure S4. ZIF-8 from different perspectives.
Figure S5. A schematic diagram of the permeation rig.
Figure S6. Single-gas permeabilities of ZIF-8 single-crystal membranes.
Figure S7. Single crystals of ZIF-8 grown on the wall of a synthesis vial in their mother liquor.
Figure S8. A schematic side-view of the pure-epoxy membrane.
Figure S9. Downstream pressure evolution due to air ingress.
Figure S10. Method of estimating the average crystal thickness.

3. Supplementary Tables

Table S1: Single-gas permeabilities and ideal selectivities.
Table S2: Ceramic-supported polycrystalline ZIF-8 membranes reported in the literature and their single-gas permeances at room temperature.
Table S3: Crystallographic data of ZIF-8 from single-crystal X-ray diffraction.
Table S4. Lennard-Jones parameters for CH₄, CO₂ and N₂ molecules.
Table S5. Predicted number of CH₄, CO₂ and N₂ molecules adsorbed per 2 × 2 × 2 ZIF-8 system at 2 bars and 298 K for different ZIF-8 force fields from GCMC simulations.

Table S6. Self-diffusion coefficients of CH₄, CO₂ and N₂ in ZIF-8 calculated for loadings obtained at 2 bars and 298 K from MD simulations using different ZIF-8 force fields.

Table S7. Simulated ideal selectivities of CO₂/N₂, CO₂/CH₄ and CH₄/N₂ mixtures in ZIF-8.
1. Supplementary text

1.1. Variations in ZIF-8 synthesis protocol

1.1.1. Zinc chloride as the zinc source

We replaced zinc nitrate hexahydrate with the same molar amount of zinc chloride (≥ 98%, Sigma-Aldrich), that is, 5.93 mmol or 0.808 g of zinc chloride, whilst keeping everything else the same as described in the Method section of the main manuscript. There was no isolated, large crystal on the wall of glass vials; many smaller crystals were rather evenly distributed all over the wall, with the bulk of the product at the bottom. We could not see particularly large single crystals when examining the product under an optical microscope. As seen on the micrograph (Fig. S2), most of the ZIF-8 crystals made from zinc chloride are in the range of 50 – 100 µm. The absence of large crystals and the generally smaller crystal sizes than those made from zinc nitrate hexahydrate did not agree the observations in other methanol-based solvothermal or room-temperature syntheses of ZIF-8 [1, 2] where the authors suggested that nitrate, being a more reactive salt than chloride, led to a faster coordination reaction between zinc ions and ligands (i.e. faster nucleation) and smaller crystals.

1.1.2. Synthesis various amounts of modulator

Apart from the optimised protocol where the molar ratios of Zn:MeIM:formate:methanol = 1:2:1:167, we attempted syntheses with molar ratios of 1:2:0:167, 1:2:0.5:167 and 1:2:2:167 whilst keeping everything else the same as described in the Method section of the main manuscript. Without sodium formate, the precursor solution remained clear and no product was formed even after a week. The same was observed in an unmodulated synthesis using zinc chloride as the zinc source.

When using the molar ratio of Zn:MeIM:formate:methanol = 1:2:0.5:167, the precursor solution remained clear after 24 hours; the final product was harvested at the 43rd hour mark. Most of the crystals were too small for our microscope to resolve; a few larger crystals
between 100 and 200 µm were also observed (Fig. S2c). On the other hand, with more formate than in the optimised protocol, product was formed after 24 hours (Fig. S2d) but appeared much smaller than what was achieved by the optimised protocol (Fig. S2a).

The observation that using no formate and 0.5-part formate resulted in no crystallisation and a longer lag phase than using 1- or 2-part formate, respectively, suggests that the modulator acts as a base that deprotonates the ligand, accelerating nucleation and growth rates and leading to small crystals [3]. However, the fact that the crystal size went through a maximum at 1-part formate when the amount of formate was varied from 0 to 2 parts made us doubt the role of formate was just to increase nucleation and growth rates. It is possible that the other role of formate – a competitive ligand [3, 4] – was in force simultaneously and generating the opposing effect, i.e. slowing down nucleation and growth and facilitating the formation of larger crystals. We postulate under our synthetic conditions, the modulator formate acts as both a deprotonation agent and a competitive ligand; the crystal size can be maximised when a fine balance is achieved between the two opposing roles. Direct experimental evidence is needed to validate or disprove our postulation.

1.1.3. Synthesis at other temperatures

The protocol described in the Method section of the main manuscript was also carried out at 70 °C and 110 °C. ZIF-8 made at 70 °C are small and highly intergrown (Fig. S3). Multiple attempts at 110 °C were unsuccessful because the vapour pressure of methanol at 110 °C compromised the seal of the crimp caps, and methanol evaporated completely.
1.2. Epoxy non-permeability check

A membrane without a ZIF-8 crystal was constructed (Fig. S8) to check the non-permeability of the epoxy. Freshly mixed epoxy was allowed to partially cure for 3 minutes before spread over the hole of a steel plate. The semi-hardened epoxy was still able to bond to the steel plate, yet viscous enough not to seep through the hole to the other side. Helium, the fastest permeating gas of the four, had a permeability of 26 barrer through the pure epoxy membrane at 24 °C, merely 1.3% and 1.1% of the helium permeabilities through ZIF8-SCM-1 and ZIF8-SCM-2 respectively (Table S1). It was therefore established that the epoxy resin did not provide an alternative transport route for permeants at our experimental conditions.
1.3. Method to account for downstream air ingress

We observed a continuous rise in the downstream pressure after the downstream and the segment between membrane and Valve V-2 (Fig. S5) were evacuated. Since no leaks were picked up by a helium leak detector, we postulated that the pressure rise was air ingress through fittings that were not rated to attain vacuum sealing. The small downstream volume of 1.2 cm$^3$ made the pressure gauge sensitive to small amounts of gases.

The rate of ingress to the downstream became approximately constant after 1.5 days and remained so at the end of the 4th day, as indicated by the linear pressure-time curve (Fig. S9). We therefore assumed that by keeping the duration of each permeation under 4 days (2 days of stabilising downstream ingress + 2 days of gas permeation), the downstream ingress rate could be regarded constant. The actual rate of pressure rise caused by gas permeation $(dP/dt)_{actual}$ was calculated by:

$$
\left( \frac{dP}{dt} \right)_{actual} = \left( \frac{dP}{dt} \right)_{observed} - \left( \frac{dP}{dt} \right)_{ingress}
$$

where

$(dP/dt)_{actual} = $ the rate of pressure rise caused by permeant accumulated in the downstream

$(dP/dt)_{observed} = $ the apparent gradient from the pressure-time curve collected during gas permeation, which is the result of both gas permeation and air ingress to the downstream
1.4. Calculation details

1.4.1. Permeability

Gas permeability was calculated by the following equation [5]:

\[
p = \frac{VL}{A} \frac{T_0}{(\Delta P)_{avg}} \frac{T P_0}{(dP)}_{actual}
\]

where \( p \) is the permeability in barrer (1 barrer = \(10^{-10}\) cm\(^3\) (STP) cm cm\(^{-2}\) s\(^{-1}\) cmHg\(^{-1}\)), \( V \) is the downstream volume in cm\(^3\), \( L \) is the membrane thickness in cm, \( A \) is the permeation area in cm\(^2\) which, in our case, is the area of the hole in the centre of a steel plate, \((\Delta P)_{avg}\) is the average trans-membrane pressure difference in cmHg, \( T \) is operating temperature in K, \(((dP/dt)_{actual})\) is the rate of downstream pressure rise in cmHg s\(^{-1}\) after accounting for the air ingress rate, \( T_0 \) and \( P_0 \) are the standard state temperature (273 K) and pressure (76 cmHg) respectively. In our experiments, the downstream pressure was two-orders-of-magnitude smaller than the upstream, therefore we assumed the trans-membrane pressure difference to be constant \(((\Delta P)_{avg})\) for the duration of each permeation test.

1.4.2. Ideal selectivity

The ideal selectivity of gas \( i \) over gas \( j \) \( (\alpha_{ij}) \) is the ratio of their permeatilities:

\[
\alpha_{ij} = \frac{p_i}{p_j} = \frac{(\Delta P)_{avg,i}}{(\Delta P)_{avg,j}} \times \frac{T_i}{T_j} \times \frac{(dP)_{actual,i}}{(dP)_{actual,j}}
\]

When taking the ratio of two permeabilities, downstream volume, permeation area and membrane thickness disappear. The uncertainties associated with each quantity do not affect the accuracy of the ideal selectivity. Therefore, despite not having the most accurate downstream volume or membrane thickness, we are reasonably confident about the accuracy of our SCMs’ ideal selectivities.

1.4.3. Knudsen selectivity
Knudsen selectivity, calculated from the ratio of Knudsen diffusion fluxes\cite{6}, is:

\[
\left( \alpha_{i/j} \right)_{Knudsen} = \sqrt{\frac{M_i}{M_j}}
\]

where \( M_i \) and \( M_j \) are the formula masses of \( i \) and \( j \) respectively.

1.4.4. Membrane thickness

Since the embedded ZIF-8 crystal does not have a set of parallel surfaces along the direction of pressure gradient, we estimated the average thickness along this direction by using a microscope image processing software (Motic) to trace the boundary of the side-view of the crystal as if it was embedded in the membrane assembly (Fig. S10). After the correct calibration and magnification settings were given to the software, it automatically calculated the cross-sectional area. To measure the length as seen on the crystal side-view that corresponded to the large, flat base glued to the steel plate, we drew a parallel line of the same length. The average crystal thickness in the direction of pressure gradient was estimated by cross-sectional area/length of the base.

1.4.5. Downstream volume

The downstream volume is the sum of the internal volumes of downstream fittings. The internal volumes were calculated from the computer-aided design drawings available on the Swagelok website.
1.5. Self-diffusion Coefficients of CH₄, CO₂ and N₂ in ZIF-8 from Molecular Simulations

Self-diffusivities of CH₄, CO₂ and N₂ at 298 K in ZIF-8 were calculated by running equilibrium molecular dynamics (MD) simulations in the NVT ensemble using the DL_POLY CLASSIC software. Prior to running the MD simulations the numbers of molecules of CH₄, CO₂ and N₂ adsorbed in ZIF-8 at 298 K and 2 bars, which is the experimental feed pressure, were predicted by performing grand canonical Monte Carlo (GCMC) simulations using the RASPA molecular simulation package. The predicted loadings were then used in the MD simulations.

For both GCMC and MD simulations, a simulation box consisting of ZIF-8 unit cell replicated by 2 × 2 × 2 in the x, y and z directions, respectively, was used. The short-range interactions between the atoms in the system were calculated using the Lennard-Jones (LJ) potential and the long-range electrostatic interactions were computed using the Ewald sum method. Cut-off distance for the LJ interactions and the real part of Ewald sum was set to 13 Å. Transferable potentials for phase equilibria (TraPPE) force field was used for modelling the CH₄, N₂ and CO₂ gas molecules (Table S4) [7, 8]. To model the ZIF-8 structure we considered flexible force fields developed by Krokidas et al. [9], Wu et al. [10], Zhang et al. [11], and Zheng et al. [12, 13], all of which have been widely used in the literature in molecular simulation studies of ZIF-8.

During the GCMC simulations, the ZIF-8 atoms were held fixed at their crystallographically determined positions. Translation, rotation and insertion/deletion of the gas molecules were sampled with equal probability. Each GCMC simulation was equilibrated for 10⁵ cycles followed by a 10⁵-cycle production run. A cycle is N steps where N is either 20 or the number of molecules in the system, whichever is greater. The predicted average numbers of molecules adsorbed in ZIF-8 for each force field type are given in Table S5. These were rounded off to the nearest integer and then used in the MD simulations.
During the MD simulations, ZIF-8 framework was treated fully flexible. A Nose-Hoover thermostat was used to keep the temperature at 298 K. The time step was set to 1 fs and each simulation was equilibrated for 5 ns and then run for another 40 ns. Trajectories were saved every 1000 steps. Self-diffusivities of CH₄, CO₂ and N₂ were then calculated by mean squared displacement method using the Einstein relation:

\[ D_s = \lim_{t \to \infty} \frac{1}{6t} \left\langle \frac{1}{N} \sum_i^N (r_i(t) - r_i(t_0))^2 \right\rangle \]

where \( N \) is the number of gas molecules in the system, \( r_i(t) \) is the instantaneous position of the \( i \)th gas molecule and \( r_i(t_0) \) is the initial position of the same molecule. To improve the statistics, multiple origins were used and self-diffusion coefficients were calculated over 30 ns trajectories which are reported for each ZIF-8 force field type in Table S6.
2. Supplementary figures

Fig. S1. Nitrogen isotherms at 77 K. The Type 1 adsorption isotherm confirmed the microporous nature of ZIF-8. The inset reveals several adsorption sub-steps at low relative pressures (i.e. micropore region) that were also observed in previous studies [14-16]. Possible reasons for the sub-steps include rearrangement of adsorbed nitrogen molecules [15] and structural changes to ZIF-8 caused by adsorbed nitrogen molecules [16].
**Fig. S2.** Micrographs of ZIF-8 crystals made with various changes in precursors at 90 °C. (a) Crystals made by the optimised protocol appear to be high-quality, single crystals above 500 µm. (b) Crystals made from zinc chloride are mostly in the range of 50 – 150 µm, smaller than those made from zinc nitrate hexahydrate in the optimised protocol. (c) Crystals made using molar ratio Zn:MeIM:formate:methanol = 1:2:0.5:167 (i.e. the amount of sodium formate is half of the optimised protocol’s) are too small to be examined by our microscope except a few crystals that are between 100 and 200 µm. (d) Crystals made using molar ratio Zn:MeIM:formate:methanol = 1:2:2:167 (i.e. the amount of sodium formate is twice of the optimised protocol’s) are small and intergrown.
**Fig. S3.** A micrograph of ZIF-8 crystals made from zinc nitrate hexahydrate at 70 °C. The crystals are small, highly intergrown, or have no well-defined morphology.
Fig. S4. ZIF-8 from different perspectives. (a) A rhombic dodecahedron, the morphology of ZIF-8. This file, ‘Rhombicdodecahedron.jpg’ by Cyp is licensed under the Creative Commons Attribution-Share Alike 3.0 Unported (CC BY-SA 3.0) license. (b) An illustration of the 2-dimensional top view when a ZIF-8 crystal is viewed along [111], [110] and [100] directions. (c) Top views of three ZIF-8 ‘half crystals’ grown on the wall of a glass vial with different growth directions. When they lie on their large, flat surface, the top views correspond to the shapes of a rhombic dodecahedron viewed in directions (shown in b) equal to their respective growth directions.
**Fig. S5.** A schematic diagram of the permeation rig. The downstream of the rig has a constant volume and variable pressure as permeant accumulates in the downstream.
Fig. S6. Single-gas permeabilities of ZIF-8 single-crystal membranes. Experiments were conducted at room temperatures between 20 and 25 °C. 1 barrer = 10⁻¹⁰ cm³(STP) cm cm⁻² s⁻¹ cmHg⁻¹.
Fig. S7. Single crystals of ZIF-8 grown on the wall of a synthesis vial in their mother liquor. Using the optimised protocol, we had many high-quality, large, single crystals on the wall. Most of the product was inter-grown crystals aggregating at the bottom of the vial; these products were used for PXRD and N\textsubscript{2} sorption. For size comparison, the outer diameter of the vial is 23 mm.
**Fig. S8.** A schematic side-view of the pure-epoxy membrane. \( L_P \) and \( L_{P+E} \) denote the thickness of steel plate and the combined thickness and steel plate and epoxy respectively. We approximated the thickness of the epoxy membrane by \((L_{P+E} - L_P)\), neglecting the thickness of epoxy that seeped through the hole.
Fig. S9. Downstream pressure evolution due to air ingress. The air ingress for both ZIF8-SCM-1 and ZIF8-SCM-2 reached steady-state after approximately 1.5 days (indicated by the linear portions of the two curves). We regarded the gradients of the linear portions as the ingress rate \((dP/dt)_{\text{ingress}}\) of the two membranes, and subtracted \((dP/dt)_{\text{ingress}}\) from the observed gradients during gas permeations \((dP/dt)_{\text{observed}}\) to obtain the rate of pressure rise actually caused by gas permeation.
Fig. S10. Method of estimating the average crystal thickness. The crystal is the same as Fig. 3b inset.
3. Supplementary tables

Table S1. Single-gas permeabilities and ideal selectivities. Single-gas permeabilities $P$ of two single-crystal ZIF-8 membranes tested at room temperature (20 – 25 °C), and ideal permselectivities $\alpha(i/j)$ calculated as $P_i/P_j$. The transmembrane pressure difference was approximately constant at 2 bar.

<table>
<thead>
<tr>
<th></th>
<th>ZIF8-SCM-1</th>
<th>ZIF8-SCM-2</th>
</tr>
</thead>
<tbody>
<tr>
<td>Single-gas permeability (barrer)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>He</td>
<td>1935</td>
<td>2309</td>
</tr>
<tr>
<td>CO$_2$</td>
<td>750.7</td>
<td>577.1</td>
</tr>
<tr>
<td>N$_2$</td>
<td>26.0</td>
<td>29.7</td>
</tr>
<tr>
<td>CH$_4$</td>
<td>93.4</td>
<td>57.5</td>
</tr>
<tr>
<td>Ideal selectivity</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\alpha$(He/CO$_2$)</td>
<td>2.6</td>
<td>4.0</td>
</tr>
<tr>
<td>$\alpha$(He/N$_2$)</td>
<td>74.5</td>
<td>77.7</td>
</tr>
<tr>
<td>$\alpha$(He/CH$_4$)</td>
<td>20.7</td>
<td>40.1</td>
</tr>
<tr>
<td>$\alpha$(CO$_2$/N$_2$)</td>
<td>28.9</td>
<td>19.4</td>
</tr>
<tr>
<td>$\alpha$(CO$_2$/CH$_4$)</td>
<td>8.0</td>
<td>10.0</td>
</tr>
<tr>
<td>$\alpha$(CH$_4$/N$_2$)</td>
<td>3.6</td>
<td>1.9</td>
</tr>
</tbody>
</table>
**Table S2.** Ceramic-supported polycrystalline ZIF-8 membranes reported in the literature and their single-gas permeances at room temperature. Permeabilities were calculated from permeances and membrane thicknesses.

<table>
<thead>
<tr>
<th>First author (year)</th>
<th>Temperature (°C)*</th>
<th>Thickness (µm)</th>
<th>Single-gas permeance (×10^-8 mol m⁻² s⁻¹ Pa⁻¹)</th>
<th>Single-gas permeability (barrer)**</th>
<th>Ideal selectivity</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td>He</td>
<td>CO₂</td>
<td>N₂</td>
</tr>
<tr>
<td>Tanaka (2017)[17]</td>
<td>25</td>
<td>1</td>
<td>3.71</td>
<td>1.69</td>
<td>1.55</td>
</tr>
<tr>
<td>Huang (2013)[18]</td>
<td>unknown</td>
<td>2</td>
<td>12.20</td>
<td>3.52</td>
<td>3.22</td>
</tr>
<tr>
<td>Liu (2014)[19]</td>
<td>35</td>
<td>2.5</td>
<td>19.10</td>
<td>12.20</td>
<td>4.46</td>
</tr>
<tr>
<td>Pan (2011)[20]</td>
<td>23</td>
<td>2.5</td>
<td>-</td>
<td>13.00</td>
<td>9.00</td>
</tr>
<tr>
<td>Pan (2012)[21]</td>
<td>22</td>
<td>2</td>
<td>-</td>
<td>40.00</td>
<td>14.00</td>
</tr>
<tr>
<td>Tao (2013)[22]</td>
<td>30</td>
<td>5</td>
<td>21.15</td>
<td>15.07</td>
<td>16.18</td>
</tr>
<tr>
<td>Tao (2013)[23]</td>
<td>25</td>
<td>20</td>
<td>-</td>
<td>13.50</td>
<td>7.92</td>
</tr>
<tr>
<td>Xu (2011)[24]</td>
<td>25</td>
<td>6</td>
<td>-</td>
<td>1.70</td>
<td>31.00</td>
</tr>
<tr>
<td>Shekhah (2014)[25]</td>
<td>35</td>
<td>0.5</td>
<td>0.89</td>
<td>0.41</td>
<td>0.19</td>
</tr>
<tr>
<td>Hu (2016)[26]</td>
<td>25</td>
<td>0.1</td>
<td>-</td>
<td>3.44</td>
<td>0.49</td>
</tr>
<tr>
<td>Drobek (2015)[27]</td>
<td>25</td>
<td>17.5</td>
<td>6.00</td>
<td>2.80</td>
<td>1.10</td>
</tr>
<tr>
<td>Zhang (2013)[28]</td>
<td>25</td>
<td>8</td>
<td>-</td>
<td>5.12</td>
<td>2.02</td>
</tr>
<tr>
<td>Fan (2012)[29]</td>
<td>25</td>
<td>60</td>
<td>-</td>
<td>9.56</td>
<td>14.70</td>
</tr>
<tr>
<td>First author (year)</td>
<td>Temperature (°C)</td>
<td>Thickness (µm)</td>
<td>Single-gas permeance ($\times 10^{-3}$ mol m$^{-2}$ s$^{-1}$ Pa$^{-1}$)</td>
<td>Single-gas permeability (barrer)</td>
<td>Ideal selectivity</td>
</tr>
<tr>
<td>---------------------</td>
<td>------------------</td>
<td>----------------</td>
<td>-------------------------------------------------</td>
<td>-------------------------------</td>
<td>------------------</td>
</tr>
<tr>
<td>Yu (2016)[30]</td>
<td>25</td>
<td>2.5</td>
<td>- 12.00 7.00 6.10</td>
<td>- 896.4 522.9 455.7</td>
<td>1.71</td>
</tr>
<tr>
<td>Hara (2015)[31]</td>
<td>25</td>
<td>20</td>
<td>19.00 10.00 4.50 5.00</td>
<td>11354 5976 2689 2988</td>
<td>2.22</td>
</tr>
<tr>
<td>Hara (2014)[32]</td>
<td>25</td>
<td>80</td>
<td>4.50 2.70 0.95 1.10</td>
<td>10757 6454 2271 2629</td>
<td>2.84</td>
</tr>
<tr>
<td>Wang (2016)[33]</td>
<td>unspecified</td>
<td>5</td>
<td>- 31.75 17.40 15.47</td>
<td>- 4744 2600 2311</td>
<td>1.82</td>
</tr>
<tr>
<td>McCarthy (2010)[34]</td>
<td>25</td>
<td>20</td>
<td>- 4.45 1.49 1.33</td>
<td>- 2659 890.4 794.8</td>
<td>2.99</td>
</tr>
<tr>
<td>Zhang (2017)[35]</td>
<td>25</td>
<td>0.55</td>
<td>- 1.47 3.16 1.66</td>
<td>- 24.1 51.8 27.3</td>
<td>0.47</td>
</tr>
<tr>
<td>Liu (2015)[36]</td>
<td>30</td>
<td>0.16</td>
<td>- 0.19 0.06 0.02</td>
<td>- 0.9 0.3 0.1</td>
<td>3.09</td>
</tr>
<tr>
<td>Bux (2009)[37]</td>
<td>25</td>
<td>30</td>
<td>- 1.33 0.52 0.48</td>
<td>- 1192 466.1 430.3</td>
<td>2.56</td>
</tr>
<tr>
<td>Kong (2014)[38]</td>
<td>30</td>
<td>2.5</td>
<td>- 38.50 14.70 12.10</td>
<td>- 2876 1098 903.9</td>
<td>2.62</td>
</tr>
<tr>
<td>Xie (2012)[39]</td>
<td>25</td>
<td>2</td>
<td>- 327.4 371.1 -</td>
<td>- 19567 22178 -</td>
<td>0.88</td>
</tr>
<tr>
<td>Shah (2013)[40]</td>
<td>25</td>
<td>25</td>
<td>- 4.50 2.00 1.90</td>
<td>- 3362 1494 1419</td>
<td>2.25</td>
</tr>
</tbody>
</table>

*: unless specified by authors, ‘room temperature’ is assumed to be 25 °C

**: 1 barrer = $10^{-10}$ cm$^3$(STP) cm cm$^{-2}$ s$^{-1}$ cmHg$^{-1}$. Permeability is calculated by the following equation:

Permeability (barrer) = permeance (mol m$^{-2}$ s$^{-1}$ Pa$^{-1}$) × thickness (µm) × 29.88
Table S3. Crystallographic data of ZIF-8 from single-crystal X-ray diffraction.

<table>
<thead>
<tr>
<th>Crystal data and structure refinement</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Formula</td>
<td>C_{8}H_{10}N_{4}Zn, 0.33(C H_{4}O)</td>
</tr>
<tr>
<td>Formula weight</td>
<td>238.25</td>
</tr>
<tr>
<td>Temperature</td>
<td>173(2) K</td>
</tr>
<tr>
<td>Diffractometer, wavelength</td>
<td>Agilent Xcalibur 3 E, 0.71073 Å</td>
</tr>
<tr>
<td>Crystal system, space group</td>
<td>Cubic, I-43m</td>
</tr>
<tr>
<td>Unit cell dimensions</td>
<td>a = 16.9853(4) Å  (\alpha = 90^\circ)</td>
</tr>
<tr>
<td></td>
<td>b = 16.9853(4) Å  (\beta = 90^\circ)</td>
</tr>
<tr>
<td></td>
<td>c = 16.9853(4) Å  (\gamma = 90^\circ)</td>
</tr>
<tr>
<td>Volume, Z</td>
<td>4900.2(4) Å(^3), 12</td>
</tr>
<tr>
<td>Density (calculated)</td>
<td>0.969 mg/m(^3)</td>
</tr>
<tr>
<td>Absorption coefficient</td>
<td>1.482 mm(^{-1})</td>
</tr>
<tr>
<td>F(000)</td>
<td>1464</td>
</tr>
<tr>
<td>Crystal colour / morphology</td>
<td>Colourless blocks</td>
</tr>
<tr>
<td>Crystal size</td>
<td>0.66 \times 0.60 \times 0.55 mm(^3)</td>
</tr>
<tr>
<td>(\theta) range for data collection</td>
<td>3.393 to 28.075°</td>
</tr>
<tr>
<td>Index ranges</td>
<td>-14 \leq h \leq 12, -19 \leq k \leq 4, -11 \leq l \leq 21</td>
</tr>
<tr>
<td>Reflections collected / unique</td>
<td>2076 / 873 [R(int) = 0.0213]</td>
</tr>
<tr>
<td>Reflections observed [F &gt; 4(\sigma)(F)]</td>
<td>838</td>
</tr>
<tr>
<td>Absorption correction</td>
<td>Analytical</td>
</tr>
<tr>
<td>Max. and min. transmission</td>
<td>0.587 and 0.537</td>
</tr>
<tr>
<td>Refinement method</td>
<td>Full-matrix least-squares on (F^2)</td>
</tr>
<tr>
<td>Data / restraints / parameters</td>
<td>873 / 0 / 35</td>
</tr>
<tr>
<td>Goodness-of-fit on (F^2)</td>
<td>1.037</td>
</tr>
<tr>
<td>Final R indices [F &gt; 4(\sigma)(F)]</td>
<td>R(_1) = 0.0218, wR(_2) = 0.0510</td>
</tr>
<tr>
<td>R indices (all data)</td>
<td>R(_1) = 0.0237, wR(_2) = 0.0517</td>
</tr>
<tr>
<td>Absolute structure parameter</td>
<td>-0.028(15)</td>
</tr>
<tr>
<td>Largest diff. peak, hole</td>
<td>0.158, -0.241 eÅ(^{-3})</td>
</tr>
<tr>
<td>Mean and maximum shift/error</td>
<td>0.000 and 0.000</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Bond lengths (Å)</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Zn(1)-N(2)</td>
<td>1.9913(18)</td>
</tr>
<tr>
<td>Zn(1)-N(2)#1</td>
<td>1.9913(18)</td>
</tr>
<tr>
<td>Zn(1)-N(2)#2</td>
<td>1.9913(18)</td>
</tr>
<tr>
<td>Zn(1)-N(2)#3</td>
<td>1.9913(18)</td>
</tr>
<tr>
<td>C(1)-N(2)#4</td>
<td>1.336(3)</td>
</tr>
<tr>
<td>C(1)-N(2)</td>
<td>1.336(3)</td>
</tr>
<tr>
<td>C(1)-C(4)</td>
<td>1.497(6)</td>
</tr>
<tr>
<td>N(2)-C(3)</td>
<td>1.375(3)</td>
</tr>
<tr>
<td>Bond angles (°)</td>
<td></td>
</tr>
<tr>
<td>--------------------------------------------------</td>
<td></td>
</tr>
<tr>
<td>N(2)-Zn(1)-N(2)#1</td>
<td>109.47(6)</td>
</tr>
<tr>
<td>N(2)-Zn(1)-N(2)#2</td>
<td>109.48(6)</td>
</tr>
<tr>
<td>N(2)#1-Zn(1)-N(2)#2</td>
<td>109.46(12)</td>
</tr>
<tr>
<td>N(2)-Zn(1)-N(2)#3</td>
<td>109.46(12)</td>
</tr>
<tr>
<td>N(2)#1-Zn(1)-N(2)#3</td>
<td>109.48(6)</td>
</tr>
<tr>
<td>N(2)#2-Zn(1)-N(2)#3</td>
<td>109.48(6)</td>
</tr>
<tr>
<td>N(2)#4-C(1)-N(2)</td>
<td>112.0(4)</td>
</tr>
<tr>
<td>N(2)#4-C(1)-C(4)</td>
<td>123.98(19)</td>
</tr>
<tr>
<td>N(2)-C(1)-C(4)</td>
<td>123.98(19)</td>
</tr>
<tr>
<td>C(1)-N(2)-C(3)</td>
<td>105.3(3)</td>
</tr>
<tr>
<td>C(1)-N(2)-Zn(1)</td>
<td>128.1(2)</td>
</tr>
<tr>
<td>C(3)-N(2)-Zn(1)</td>
<td>126.63(16)</td>
</tr>
<tr>
<td>C(3)#4-C(3)-N(2)</td>
<td>108.73(14)</td>
</tr>
</tbody>
</table>
Table S4. Lennard-Jones parameters for CH₄, CO₂ and N₂ molecules.*

<table>
<thead>
<tr>
<th>Molecule</th>
<th>Atom</th>
<th>ε/k_B (K)</th>
<th>σ (Å)</th>
<th>Charge</th>
</tr>
</thead>
<tbody>
<tr>
<td>CH₄</td>
<td>CH₄</td>
<td>148.0</td>
<td>3.73</td>
<td>N/A</td>
</tr>
<tr>
<td>CO₂</td>
<td>C</td>
<td>27.0</td>
<td>2.80</td>
<td>0.7</td>
</tr>
<tr>
<td></td>
<td>O</td>
<td>79.0</td>
<td>3.05</td>
<td>-0.35</td>
</tr>
<tr>
<td>N₂</td>
<td>N</td>
<td>36.0</td>
<td>3.31</td>
<td>-0.482</td>
</tr>
<tr>
<td></td>
<td>N_com</td>
<td>N/A</td>
<td>N/A</td>
<td>0.964</td>
</tr>
</tbody>
</table>

* The Lorentz-Berthelot mixing rules were used to calculate the interaction parameters between unlike atoms.

Table S5. Predicted number of CH₄, CO₂ and N₂ molecules adsorbed per 2 × 2 × 2 ZIF-8 system at 2 bars and 298 K for different ZIF-8 force fields from GCMC simulations.

<table>
<thead>
<tr>
<th>Force field used</th>
<th>CH₄</th>
<th>CO₂</th>
<th>N₂</th>
</tr>
</thead>
<tbody>
<tr>
<td>Krokidas et al.</td>
<td>21.14</td>
<td>45.72</td>
<td>7.42</td>
</tr>
<tr>
<td>Wu et al.</td>
<td>12.07</td>
<td>20.71</td>
<td>4.77</td>
</tr>
<tr>
<td>Zhang et al.</td>
<td>9.04</td>
<td>15.27</td>
<td>3.88</td>
</tr>
<tr>
<td>Zheng et al.</td>
<td>20.88</td>
<td>48.88</td>
<td>7.42</td>
</tr>
</tbody>
</table>

Table S6. Self-diffusion coefficients of CH₄, CO₂ and N₂ in ZIF-8 calculated for loadings obtained at 2 bars and 298 K from MD simulations using different ZIF-8 force fields.

<table>
<thead>
<tr>
<th>Force field used</th>
<th>CH₄ (10⁻¹⁰ m²/s)</th>
<th>CO₂ (10⁻¹⁰ m²/s)</th>
<th>N₂ (10⁻¹⁰ m²/s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Krokidas et al.</td>
<td>2.00</td>
<td>11.7</td>
<td>8.38</td>
</tr>
<tr>
<td>Wu et al.</td>
<td>23.7</td>
<td>20.9</td>
<td>37.5</td>
</tr>
<tr>
<td>Zhang et al.</td>
<td>0.37</td>
<td>3.31</td>
<td>1.53</td>
</tr>
<tr>
<td>Zheng et al.</td>
<td>0.15</td>
<td>2.17</td>
<td>1.71</td>
</tr>
</tbody>
</table>
Table S7. Simulated ideal selectivities of CO$_2$/N$_2$, CO$_2$/CH$_4$ and CH$_4$/N$_2$ mixtures in ZIF-8. Here the ideal selectivity is defined as $(q_i/q_j) \times (D_i/D_j)$, where $q$ is the adsorbed amount and $D$ is the self-diffusion coefficient.

<table>
<thead>
<tr>
<th>Ideal Selectivity</th>
<th>CO$_2$/N$_2$</th>
<th>CO$_2$/CH$_4$</th>
<th>CH$_4$/N$_2$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Krokidas et al.</td>
<td>8.61</td>
<td>12.65</td>
<td>0.68</td>
</tr>
<tr>
<td>Wu et al.</td>
<td>2.42</td>
<td>1.51</td>
<td>1.60</td>
</tr>
<tr>
<td>Zhang et al.</td>
<td>8.52</td>
<td>15.12</td>
<td>0.56</td>
</tr>
<tr>
<td>Zheng et al.</td>
<td>8.36</td>
<td>33.87</td>
<td>0.25</td>
</tr>
</tbody>
</table>
References


