# Experimental observation of the $v_{2}+4 v_{3}$ bands of $\mathrm{HD}^{16} \mathrm{O}$ and $\mathrm{HD}^{18} \mathrm{O}$ between 14975 and $15275 \mathrm{~cm}^{-1}$ 

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#### Abstract

The $\mathrm{v}_{2}+4 \mathrm{v}_{3}$ combination bands of $\mathrm{HD}^{16} \mathrm{O}$ and $\mathrm{HD}^{18} \mathrm{O}$ were measured using Fourier transform-incoherent broadband cavity-enhanced absorption spectroscopy (FT-IBBCEAS) with a spectral resolution of $0.08 \mathrm{~cm}^{-1}$. The ro-vibrational lines of these bands were assigned through comparison with ab-initio molecular lines from the Tomsk variational calculation database (http://spectra.iao.ru/). For $\mathrm{HD}^{18} \mathrm{O}$ and $\mathrm{HD}^{16} \mathrm{O}$ in total 114 and 141 strong lines were assigned in the region between $14975.3 \mathrm{~cm}^{-1}$ and $15243.3 \mathrm{~cm}^{-1}$ and between $14998.5 \mathrm{~cm}^{-1}$ and $15274.7 \mathrm{~cm}^{-1}$, respectively. While the very satisfactory agreement of line intensities was used for line assignments, a systematic average discrepancy of $\sim 0.305 \mathrm{~cm}^{-1}$ in line positions was identified between the measured lines of $\mathrm{HD}^{18} \mathrm{O}$ and the theoretically predicted lines from the Tomsk database. Similarly for $\mathrm{HD}^{16} \mathrm{O}$, an approximate wavenumber difference of $\sim 0.361 \mathrm{~cm}^{-1}$ was observed. The wavenumber accuracy of the Fourier transform cavity enhanced absorption spectrometer was confirmed on basis of concurrently measured $\mathrm{H}_{2}^{16} \mathrm{O}$ spectra in the region between $15254.2 \mathrm{~cm}^{-1}$ and $15376.9 \mathrm{~cm}^{-1}$ and corroborated the systematic shifts of the $a b$ initio data. A few lines of the $v_{1}+4 v_{2}+2 v_{3}$ bands of $\mathrm{HD}^{16} \mathrm{O}$ and $\mathrm{HD}^{18} \mathrm{O}$ were also identified. The data are compared and discussed on basis of existing literature data.


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## 1. Introduction

One reason for water vapor being the most important greenhouse gas in the Earth's atmosphere is its ubiquity. Hence, not only the most dominant isotopologue, $\mathrm{H}_{2}^{16} \mathrm{O}$ (relative abundance 0.997317), is of high relevance for atmospheric sciences, but also its deuterated isotopologues, such as $\mathrm{HD}^{16} \mathrm{O}$ or $\mathrm{HD}^{18} \mathrm{O}$ (relative abundances $3.10693 \times 10^{-4}$ and $6.23003 \times 10^{-7}$, respectively) [1]. In the analysis of trace gas measurements, be it from in situ spectrometers or remote sensing instruments, the occurrence of absorption features of water isotopologues, affecting the retrieval of number densities of target species, is very common in many spectral regions. Thus, the knowledge of weak water absorption lines including isotopologues is important to enable the unambiguous identification of other trace species. The high relevance of the

[^0]isotopic composition of water vapour for climatic and hydrological studies has been illustrated recently in the publication of a global database on stable water vapor isotope ratios ( $\delta^{18} \mathrm{O}$ and $\delta \mathrm{D}$ ) with high temporal resolution [2]. Furthermore, new experimental data on water isotopologues, in conjunction with $a b$ initio calculations [ 3,4 ] enable the improvement of the ground state potential energy surface (as well as wavefunctions for intensity calculations) of water and hence a more accurate prediction of rotation-vibration line positions for spectral regions where experimental data are either sparse or unreliable, or do not exist.

Singly deuterated water, HDO, has been the subject of many previous theoretical studies (see e.g. Refs. [1,5-9]). $\mathrm{HD}^{16} \mathrm{O}$ has been widely experimentally addressed at lower energies ( $<14115 \mathrm{~cm}^{-1}$ ) [10-26], but above $14115 \mathrm{~cm}^{-1}$ a more limited number of experimental investigation exists to our knowledge [26-31].
$\mathrm{HD}^{18} \mathrm{O}$ in comparison has been much less focused on [32-34], not least because of its lower natural abundance, and experimental data in the visible region do not seem to be available in the literature.

Here we report experimental observations of the $v_{2}+4 v_{3}$ bands of the deuterated water isotopologues $\mathrm{HD}^{16} \mathrm{O}$ and $\mathrm{HD}^{18} \mathrm{O}$ and their (partial) rotational assignments. The spectra were measured in the
spectral range from 14975 to $15275 \mathrm{~cm}^{-1}$ using Fourier transformincoherent broadband cavity-enhanced absorption spectroscopy (FT-IBBCEAS). The spectral analysis focused on the line positions' accuracy in the measured spectra and on assignments based on the line intensities and positions from the Tomsk abinitio variational calculation database (http://spectra.iao.ru/) [35] (this database will be referred to as "Tomsk database" from here on). The accuracy of absolute line intensities was not investigated in this study. The spectral resolution was moderately high ( $\sim 0.08 \mathrm{~cm}^{-1}$ ), hence strong lines in the spectral region of the $v_{2}+4 v_{3}$ band are sufficiently isolated and well separated from the corresponding band of the most abundant water isotopologue $\left(\mathrm{H}_{2}^{16} \mathrm{O}\right)$ to enable unambiguous assignments. A few lines in the spectral region of concern were assigned to the $v_{1}+4 v_{2}+2 v_{3}$ combination bands of singly deuterated water. Our findings for $\mathrm{HD}^{16} \mathrm{O}$ are compared with available literature data $[9,27,28,35]$ and give confidence for the assignment of the new lines in $\mathrm{HD}^{18} \mathrm{O}$.

The new data presented here will be useful for new theoretical modelling of the ground state potential energy surface of the water molecule. Moreover, the data will be also helpful for the interpretation of observation and retrieval of data from satellite based remote sensing applications such as the Global Ozone Monitoring Experiment 2 (GOME-2) onboard the MetOp satellites [36] or the TROPOspheric Monitoring Instrument (TROPOMI) onboard the Copernicus Sentinel-5 precursor probe [37,38].

After outlining some experimental details in the next section, we will present the main results and assignments in Section 3, and discuss the data on basis of a comparison with database and literature data in Section 4, before the work reported here is concluded.

## 2. Experiment

### 2.1. Measurement method, components and parameters

The near IR spectra of the deuterated water isotopologues $\mathrm{HD}^{16} \mathrm{O}$ and $\mathrm{HD}^{18} \mathrm{O}$ were measured using Fourier transformincoherent broadband cavity-enhanced absorption spectroscopy (FT-IBBCEAS) [39-41]. The general experimental setup has been reported previously [42-45] and specifics of the measurement arrangement are only briefly outlined here. The light source was a 6 W supercontinuum source (Fianium SC450-6) operating at a repetition rate of 50 MHz delivering pulses of $\sim 5 \mathrm{ps}$ duration. The broadband radiation ( $\sim 500-1800 \mathrm{~nm}$ ) was passed through a long-pass filter with a cut-on wavelength at 642 nm ( $15600 \mathrm{~cm}^{-1}$ ). The light was spatially filtered and collimated before entering the optical cavity of length $d \sim 644 \mathrm{~cm}$. The optical cavity was formed by two di-electric plano-concave mirrors (Layertec GmbH , Germany) with a high reflectivity between 14200 and $15600 \mathrm{~cm}^{-1}$. The experiment was carried out with a static cell; no mirror purge was applied. An IR optimized achromatic doublet was used for coupling the light exiting the cavity into a multimode fiber ( $\sim 0.8 \mathrm{~nm}$ ), which was connected to the entrance port (aperture size 0.5 mm ) of a Fourier transform spectrometer (FTS; Bruker Vertex 80). On basis of a low pressure $\mathrm{CO}_{2}$ spectrum the instrumental line shape was determined, and a spectral resolution of $\sim 0.08 \mathrm{~cm}^{-1}$ was established employing Norton-Beer weak apodization (see also next section). The integration time used for measuring the spectrum was 120 min . For this acquisition time a signal-to-noise ratio of >35 was achieved, which was evaluated on basis of the strong $\mathrm{HD}^{16} \mathrm{O}$ absorption line at $\sim 15126 \mathrm{~cm}^{-1}$.

### 2.2. Calibration aspects

## (A) Extinction coefficients

In order to measure absolute extinction coefficients (in $\left[\mathrm{cm}^{-1}\right]$ ) with FT-IBBCEAS, the broadband mirror reflectivity must be known. The mirror reflectivity was calibrated by filling a well evacuated cavity ( $P<10^{-3}$ mbar) with a known amount of $\mathrm{CO}_{2}$ (purity $>99.9 \%$ ) at a pressure of $\sim 6$ mbar $[40,41]$. The reflectivity was then determined from the measured $\mathrm{CO}_{2}$ extinction coefficients using the HITRAN absorption cross-sections of $\mathrm{CO}_{2}$ in the wavenumber region between 14200 and $15600 \mathrm{~cm}^{-1}$ [1]. The reflectivity was found to be $R=0.9975 \pm 0.0002$ between $14975 \mathrm{~cm}^{-1}$ and $15275 \mathrm{~cm}^{-1}$. The uncertainty of the reflectivity represents the largest contribution ( $\sim 10 \%$ ) to the systematic error of the measured water isotopologue absorption coefficients. Other uncertainties arise from the pressure measurement ( $\sim 5 \%$ ) and from intensity fluctuations of the SC light source ( $\sim 4 \%$ ) [43]. The total systematic mean square uncertainty contributing to the measured absorption coefficients was estimated to be $\sim 12 \%$.
(B) Wavenumber scale

Wavenumber calibration of the FTS is crucially important when new line positions are reported. For the purpose of minimizing the error in line positions, spectra of the most abundant water isotopologue ( $\mathrm{H}_{2}^{16} \mathrm{O}$, doubly distilled) were measured using FT-IBBCEAS in the region between 14200 and $15600 \mathrm{~cm}^{-1}$. The $\mathrm{H}_{2} \mathrm{O}$ vapor was filled into the optical cavity at a pressure of 7.1 mbar. The wavenumber accuracy was evaluated by comparing the line positions of 30 measured isolated ro-vibrational lines with reasonable intensities $S(\lambda)$ to those in the Tomsk database in the region from 15250 to $15380 \mathrm{~cm}^{-1}$ (see Table 1), which is adjacent to the region where the $v_{2}+4 v_{3}$ bands of $\mathrm{HD}^{16} \mathrm{O}$ and $\mathrm{HD}^{18} \mathrm{O}$ are located. Fig. 1 is essentially a graphical representation of Table 1. The inset in Fig. 1 illustrates the excellent center wavenumber match between the measured FT-IBBCEAS spectrum (black trace) and the position from the Tomsk database, represented as a stick spectrum based on values for $S(\lambda)$. The average absolute discrepancy between the measured and literature line positions is $0.004 \pm 0.002 \mathrm{~cm}^{-1}$. This discrepancy is $\sim 20$ times smaller than the instrumental resolution of $0.08 \mathrm{~cm}^{-1}$. We assume the reported wavenumber accuracy of $\mathrm{HD}^{16} \mathrm{O}$ and $\mathrm{HD}^{18} \mathrm{O}$ lines to be about $0.006 \mathrm{~cm}^{-1}$. Therefore the wavenumber scale accuracy is sufficient to record accurate spectral line positions with a spectral resolution of $0.08 \mathrm{~cm}^{-1}$.

### 2.3. Materials and gas preparations

$\mathrm{H}_{2}^{18} \mathrm{O}$ was purchased from Taiyo Nippon Sanso Corporation (purity $>98 \%$ ) and the $\mathrm{D}_{2}^{16} \mathrm{O}$ was purchased from Sigma Aldrich (purity $>99.994 \%$ ). The water samples were degassed by a sufficient number of "freeze pump-thaw" cycles before injection into the cavity. No further purification was applied. First the evacuated optical cavity was primed with $\mathrm{H}_{2}^{18} \mathrm{O}$ vapor at a pressure of $\sim 4.0$ mbar. Then $\mathrm{D}_{2}^{16} \mathrm{O}$ was injected (partial pressure $\sim 4.0 \mathrm{mbar}$ ) to the chamber and left to equilibrate for ca. 16 h at room temperature. Hence the initial concentrations of $\mathrm{D}_{2}^{16} \mathrm{O}$ and $\mathrm{H}_{2}^{18} \mathrm{O}$ were approximately equal ( $50: 50$ ) before the commencement of deuterium exchange reactions. The total mixture pressure before the start of the actual measurement was observed to have reduced to $\sim 7.7$ mbar, probably due to adsorption on the cell wall surfaces.

## 3. Results and discussion

### 3.1. Spectral features in the region between $14975 \mathrm{~cm}^{-1}$ and

 $15275 \mathrm{~cm}^{-1}$Following the outlined preparation method (section 2.2), overview absorption spectra of the isotopologue mixture were recorded in the region between $\sim 14200$ and $15600 \mathrm{~cm}^{-1}$. The spectra are dominated by ro-vibrational features of $\mathrm{H}_{2}^{16} \mathrm{O}$ and $\mathrm{H}_{2}^{18} \mathrm{O}$,

Table 1
Comparison of spectral line positions of $\mathrm{H}_{2}^{16} \mathrm{O}$ measured using FT-IBBCEAS and from the Tomsk database between 15254 and $15377 \mathrm{~cm}^{-1}$.

| FT-IBBCEAS | Tomsk database [35] | Difference <br> $v_{\text {exp }}\left[\mathrm{cm}^{-1}\right]$ |
| :--- | :--- | ---: |
| 15254.168 | $v_{\mathrm{T}}\left[\mathrm{cm}^{-1}\right]$ | $\Delta v=v_{\mathrm{T}}-v_{\mathrm{exp}}\left[\mathrm{cm}^{-1}\right]$ |

however between 14975 and $15275 \mathrm{~cm}^{-1}$ strong lines of the $v_{2}+4 v_{3}$ combination bands of $\mathrm{HD}^{16} \mathrm{O}$ and $\mathrm{HD}^{18} \mathrm{O}$ are clearly discernible. It turned out that this region is sufficiently isolated and exhibited merely weak interferences from $\mathrm{H}_{2}^{16} \mathrm{O}$ and $\mathrm{H}_{2}^{18} \mathrm{O}$ (see Fig. 2), thus allowing for ro-vibrational line assignments through comparison with the existing literature. Individual line assignments were established by comparing the measured $\mathrm{HD}^{16} \mathrm{O}$ and $\mathrm{HD}^{18} \mathrm{O}$ spectra with data reported in the Tomsk database. For that purpose, the line intensities of the two water isotopologues were calculated for the pertinent experimental conditions using the 'Tomsk' abinito variational database [35,46], and then visually inspected for recognizable patterns starting with the strongest ro-vibrational absorption features. In order to obtain unambiguous line-by-line assignments the cut off intensity for weaker lines was suitably adjusted for the spectral simulations using the Tomsk database. The minimal cut off intensities used were $10^{-29} \mathrm{~cm} /-$ molecule and $10^{-32} \mathrm{~cm} /$ molecule for $\mathrm{HD}^{16} \mathrm{O}$ and $\mathrm{HD}^{18} \mathrm{O}$ respectively (note that the values in the database are weighted with the natural abundances of the different isotopologues).

Fig. 2 shows the measured absorption coefficients (Panel (a)) and the approximated absorption coefficient based on the (abundance-weighted) theoretical line intensities from the Tomsk database (Panel (b)) of the $v_{2}+4 v_{3}$ bands of $\mathrm{HD}^{16} \mathrm{O}$ and $\mathrm{HD}^{18} \mathrm{O}$ between 14975 and $15275 \mathrm{~cm}^{-1}$. As mentioned earlier, the $v_{2}+4 v_{3}$ bands of the different isotopologues are not spectrally isolated. On the one hand, there are some discernable features of the isotoplogues $\mathrm{H}_{2}^{16} \mathrm{O}$ and $\mathrm{H}_{2}^{18} \mathrm{O}$ in the R branch of the $\mathrm{HD}^{16} \mathrm{O} \mathrm{v}_{2}+4 \mathrm{v}_{3}$ band, while the P branch appears less prone to those interferences (see Fig. 2a). On the other hand, the spectra of $\mathrm{HD}^{16} \mathrm{O}$ and $\mathrm{HD}^{18} \mathrm{O}$ are also not separated, however, rotational lines of both target isotopologues could nevertheless be readily distinguished.

After the assignment of individual lines (see Sections 3.2 and 3.3) the relative abundances of the four relevant isotopologues in


Fig. 1. Wavenumber calibration using the most abundant water isotopologue, $\mathrm{H}_{2}^{16} \mathrm{O}$. The black trace is the FT-IBBCEAS spectrum (left axis) of $\mathrm{H}_{2}^{16} \mathrm{O}$ at 7.1 mbar in the region from 15250 to $15380 \mathrm{~cm}^{-1}$ measured at a resolution of $0.08 \mathrm{~cm}^{-1}$. The red trace represents the line positions and absorption strength, $S$, of $\mathrm{H}_{2}^{16} \mathrm{O}$ as reported in the Tomsk database (right axis). The inset shows a magnified view of the line at $15277.2 \mathrm{~cm}^{-1}$ in the dashed rectangle. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)


Fig. 2. (a) Upper panel: Stick spectrum of the ro-vibrational line absorption coefficient, $A=S_{\text {Tomsk }}$ [ $\mathrm{cm} /$ molecule] / FWHM [ $\mathrm{cm}^{-1}$ ] / (natural relative abundance) $\times n$ [molecule $\mathrm{cm}^{-3}$ ], of the $\mathrm{v}_{2}+4 \mathrm{v}_{3}$ bands of $\mathrm{HD}^{16} \mathrm{O}$ (blue trace) and $\mathrm{HD}^{18} \mathrm{O}$ (red trace) from the Tomsk database [35] between 14970 and $15280 \mathrm{~cm}^{-1}$, that best matches the measured spectrum. The magenta and green traces show the corresponding stick spectra of $\mathrm{H}_{2}^{18} \mathrm{O}$ and $\mathrm{H}_{2}^{16} \mathrm{O}$ in that region. Values of (natural relative abundance) $\times n: \mathrm{HD}^{16} \mathrm{O}\left(3.10693 \times 10^{-4}\right) \times 6.7 \times 10^{16} \mathrm{~cm}^{-3}, \mathrm{HD}^{18} \mathrm{O}$ $\left(6.23003 \times 10^{-7}\right) \times 5.5 \times 10^{16} \mathrm{~cm}^{-3}, \mathrm{H}_{2}^{16} \mathrm{O}(0.997317) \times 3.8 \times 10^{16} \mathrm{~cm}^{-3}, \mathrm{H}_{2}^{18} \mathrm{O}$ $\left(1.99983 \times 10^{-3}\right) \times 3.1 \times 10^{16} \mathrm{~cm}^{-3} ;$ FWHM $=0.1 \mathrm{~cm}^{-1}$. The wavenumber scale of line intensities of $\mathrm{HD}^{16} \mathrm{O}$ was shifted by $-0.361 \mathrm{~cm}^{-1}$ and the wavenumber scale of $\mathrm{H}^{18} \mathrm{OD}$ was shifted by $-0.305 \mathrm{~cm}^{-1}$. (b) Lower panel: main measured spectrum (absorption coefficient $\alpha$, black trace) using FT-IBBCEAS. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)
the experiment were estimated by scaling the theoretical spectra [35] until a best match was found with the measured data as shown in Fig. 2 (see the figure caption for details). The partial pressures (and number densities) turned out to be $\sim 2.20$ mbar $\left(\approx 5.5 \times 10^{16} \mathrm{~cm}^{-3}\right)$ for $\mathrm{HD}^{18} \mathrm{O}, \sim 2.68 \mathrm{mbar}\left(\approx 6.7 \times 10^{16} \mathrm{~cm}^{-3}\right)$ for $\mathrm{HD}^{16} \mathrm{O}, \sim 1.24 \mathrm{mbar}\left(\approx 3.1 \times 10^{16} \mathrm{~cm}^{-3}\right.$ ) for $\mathrm{H}_{2}^{18} \mathrm{O}$, and $\sim 1.52 \mathrm{mbar}$ $\left(\approx 3.8 \times 10^{16} \mathrm{~cm}^{-3}\right)$ for $\mathrm{H}_{2}^{16} \mathrm{O}$. The sum of partial pressures agrees well with the overall pressure of 7.7 mbar after ${ }^{18} \mathrm{O}$ and D exchange (see previous section). The relative abundances of $\mathrm{HD}^{18} \mathrm{O}, \mathrm{HD}^{16} \mathrm{O}$, and $\mathrm{H}_{2}^{18} \mathrm{O}$ in the experiment were hence larger than their natural
abundances by factors of $\sim 462227, \sim 113$, and $\sim 81$, respectively, while the abundance of $\mathrm{H}_{2}^{16} \mathrm{O}$ was reduced by a factor of $\sim 5$.

### 3.2. Ro-vibrational assignments for $H D^{16} \mathrm{O}$

The $\mathrm{HD}^{16} \mathrm{O}$ ro-vibrational lines in the $v_{2}+4 v_{3}$ band ( 014 ) were identified in comparison with the corresponding experimental line positions reported in Naumenko and Campargue [27], who used intracavity laser absorption spectroscopy to study $\mathrm{HD}^{16} \mathrm{O}$ at a resolution of $0.03 \mathrm{~cm}^{-1}$, as well as with Bach et al. [28] who studied this isotopologue with a long path Fourier transform setup with a resolution of $0.06 \mathrm{~cm}^{-1}$. (Note: Doppler FWHM at room temperature is $\sim 0.05 \mathrm{~cm}^{-1}$ ). In comparison with Ref. [27] and Ref. [28] the median absolute wavenumber discrepancy was merely $\sim 0.010 \mathrm{~cm}^{-1}$ and $\sim 0.008 \mathrm{~cm}^{-1}$, respectively, which is approximately 10 times smaller than our instrumental spectral resolution. This good agreement of $\sim 150$ strong ro-vibrational lines (see column 3 of Table 2a) inspires confidence in our wavenumber calibration and at the same time corroborates the data in Refs. [27,28]. The assignment of the $\mathrm{HD}^{16} \mathrm{O}$ lines were then made on basis of the Tomsk database for our measurement conditions (see Table 2a). The large majority of lines in the Tomsk database was found to be systematically shifted to larger wavenumbers. An average absolute discrepancy of $0.361 \pm 0.052 \mathrm{~cm}^{-1}(1 \sigma)$ between the theoretical [35] and measured $v_{2}+4 v_{3}$ line positions for $\mathrm{HD}^{16} \mathrm{O}$ was established. 141 assigned lines were also compared with the corresponding theoretical line list reported by Kyuberis et al. [9]. Here the absolute value of the median wavenumber discrepancy was again only $\sim 0.008 \mathrm{~cm}^{-1}$ (see Table 2a). The fact that the wavenumber accuracy of the line positions of $\mathrm{HD}^{16} \mathrm{O}$ agrees really well with literature data implies the same can be expected for the line positions of $\mathrm{HD}^{18} \mathrm{O}$. In addition to lines from the $v_{2}+4 v_{3}$ band of $\mathrm{HD}^{16} \mathrm{O}$, seven significantly strong lines from the overlapping $v_{1}+4 v_{2}+2 v_{3}$ band were identified in the spectrum (see Table 2b). For this small number of lines, the average absolute discrepancy with regard to the Tomsk database was systematically less than half on average, i.e. $0.160 \pm 0.036 \mathrm{~cm}^{-1}(1 \sigma$, student $t$-distribution assumed for small sample size). Several more line observations and alternative (ambiguous) assignments are listed in the supplementary material.

### 3.3. Ro-vibrational assignments for $H D^{18} O$

The instrument's well calibrated wavenumber scale with an overall uncertainty of $0.006 \mathrm{~cm}^{-1}$ (using $\mathrm{H}_{2}^{16} \mathrm{O}$ lines, see Section 2.1) and the good match with $\mathrm{HD}^{16} \mathrm{O}$ line position data from Refs. [9,28] enabled the assignment of $\mathrm{HD}^{18} \mathrm{O}$ lines on basis of the Tomsk database, using characteristic intensity patterns of the lines. 114 new ro-vibrational lines in the $v_{2}+4 v_{3}$ band were identified and assigned for $\mathrm{HD}^{18} \mathrm{O}$; they are listed in Table 3a. The lower and upper rotational quantum numbers ( $J K_{\mathrm{a}} K_{\mathrm{c}}$ ) are given for each rotational line; the assignments in Table 3a are taken from Ref. [35]. As in the case of $\mathrm{HD}^{16} \mathrm{O}$, the line positions for $\mathrm{HD}^{18} \mathrm{O}$ from the Tomsk database [35] were systematically shifted to larger wavenumbers. The average discrepancy of experimental $\mathrm{HD}^{18} \mathrm{O}$ lines with the predicted line positions was observed to be $\sim 0.305 \pm 0.064 \mathrm{~cm}^{-1}(1 \sigma)$. In the case of $\mathrm{HD}^{18} \mathrm{O}$, only three lines in the $v_{1}+4 v_{2}+2 v_{3}$ band were unambiguously identified (see Table 3b), with observed systematic shifts of ca. $0.122 \mathrm{~cm}^{-1}$. Even though this latter systematic shift is rather uncertain due to the small sample size, the trend of a smaller systematic difference in the $v_{1}+4 v_{2}+2 v_{3}$ combination band is the same as for $\mathrm{HD}^{16} \mathrm{O}$. It is interesting to note that the predictions from the Tomsk database appear to depend on two factors: (a) on the vibrational mode (mean shifts of $0.361 \mathrm{~cm}^{-1}$ for ( 014 ) versus $0.160 \mathrm{~cm}^{-1}$ for (142) in $\mathrm{HD}^{16} \mathrm{O}$ ), and (b) on the relevant isotopologue (shifts of $0.361 \mathrm{~cm}^{-1}$ and $0.160 \mathrm{~cm}^{-1}$ for $\mathrm{HD}^{16} \mathrm{O}$ versus
$0.305 \mathrm{~cm}^{-1}$ and $0.122 \mathrm{~cm}^{-1}$ for $\mathrm{HD}^{18} \mathrm{O}$ )), see also the captions of Tables 2 and 3 ).

It was also observed that the shifts are not symmetrically distributed around the stated average, which is also implied by the significant difference between the median and the mean in the observed shifts (see Figs. S1 and S2 in the supplementary material). The median may be a better measure for the expected discrepancy.

Fig. 3 shows a magnified view of the $v_{2}+4 v_{3}$ band's $P$ branch, i.e. the region between 15060 and $15080 \mathrm{~cm}^{-1}$. The measured spectrum is compared with the line intensities from the Tomsk database after the latter were shifted by the average values of $-0.305 \mathrm{~cm}^{-1}$ for $\mathrm{HD}^{18} \mathrm{O}$ and $-0.361 \mathrm{~cm}^{-1}$ for $\mathrm{HD}^{16} \mathrm{O}$ (Tables 2a and 3a). The inset in Fig. 3 illustrates the quality of the match of center wavenumbers of lines after the shift of all lines by an average value. The dashed line in the inset shows an example of the good match with the data by Naumenko and Campargue [27], as well as Bach et al. [28] (see also Table 2a). The lines of the P branch of $\mathrm{HD}^{16} \mathrm{O}$ start at $14998.5 \mathrm{~cm}^{-1}$ and the lines of R branch ends at $15274.7 \mathrm{~cm}^{-1}$, whereas the lines of the P branch of $\mathrm{HD}^{18} \mathrm{O}$ start at $14975.3 \mathrm{~cm}^{-1}$ and those of the R branch end at $15243.3 \mathrm{~cm}^{-1}$. The P branch portion for Fig. 3 was selected in such a way that the line assignments of both $\mathrm{HD}^{16} \mathrm{O}$ and $\mathrm{HD}^{18} \mathrm{O}$ are clearly discernable (see the inset in Fig. 3).

Finally, it is worth noting that the spectral region studied here (14975-15275 $\mathrm{cm}^{-1}$ corresponding to the wavelength range of $654.7-667.8 \mathrm{~nm}$ ) is highly relevant for $\mathrm{NO}_{3}$ detection by spectroscopic methods, which use the origin of the strong $B \mathrm{E}^{\prime}(00000) \leftarrow X$ $\mathrm{A}_{2}{ }^{\prime}(00000)$ transition of $\mathrm{NO}_{3}$ with maximum at $\sim 662 \mathrm{~nm}$. In this region, water vapor is known to be the most important interfering species in the measurement and retrieval of $\mathrm{NO}_{3}$ mixing ratios in ambient air samples. In "single wavelength" cavity ring-down approaches the position and absorption strength of lines is important and should be avoided or taken into account [47]. In broadband cavity enhanced absorption approaches to multiple absorber retrieval [39], small errors in modelling the water absorption can mask the $\mathrm{NO}_{3}$ absorption features and lead to spurious $\mathrm{NO}_{3}$ signals [48,49]. Thus the accurate knowledge of the position and absorption strength of even the less abundant water isotopologues, such as $\mathrm{HD}^{16} \mathrm{O}$ and $\mathrm{HD}^{18} \mathrm{O}$, may contribute to accurate quantitative retrieval procedures.

## 4. Conclusions

In this publication, the first observation of the $v_{2}+4 v_{3}$ combination band of $\mathrm{HD}^{18} \mathrm{O}$ is reported using FT-IBBCEAS, illustrating the high suitability of this method for measurements of trace species isotopologues for which small sample volumes and high absorption sensitivity are required. 114 strong ro-vibrational lines for $\mathrm{HD}^{18} \mathrm{O}$ were assigned in the region between 14975.3 and $15243.3 \mathrm{~cm}^{-1}$ in comparison with line intensities and positions from the Tomsk database. The $v_{2}+4 v_{3}$ band of $\mathrm{HD}^{16} \mathrm{O}$ has also been observed and fully agree with the results published by Naumenko and Camargue [27], Bach et al. [28], and Kyuberis et al. [9]. 141 strong lines were assigned for $\mathrm{HD}^{16} \mathrm{O}$ in the region between $15058.8 \mathrm{~cm}^{-1}$ and $15274.7 \mathrm{~cm}^{-1}$. Systematic discrepancies in the line positions of $0.361 \pm 0.052 \mathrm{~cm}^{-1}(1 \sigma)$ and of $0.305 \pm 0.064 \mathrm{~cm}^{-1}$ $(1 \sigma)$ were found for $\mathrm{HD}^{16} \mathrm{O}$ and $\mathrm{HD}^{18} \mathrm{O}$ respectively, in comparison with the Tomsk database. The presented data may be useful for future detection of atmospheric $\mathrm{HD}^{16} \mathrm{O}$ and $\mathrm{HD}^{18} \mathrm{O}$ in remote sensing applications. More high-resolution measurements of the $v_{2}+4 v_{3}$ combination bands of these water isotopologues as well as new theoretical modelling of data in this spectral region are merited by this study.



 15181.286 and $15185.994 \mathrm{~cm}^{-1}, 15195.516$ and $15199.667 \mathrm{~cm}^{-1}, 15208.043,15210.717$ and $15214.092 \mathrm{~cm}^{-1}$.

| $\begin{aligned} & \hline \mathrm{HD}^{16} \mathrm{O} \\ & \text { FT-IBBCEAS } \end{aligned}$ | Tomsk data [35] | Ref. [27] | Ref. [28] | Ref. [9] | Difference ( $\Delta v$ ) |  |  |  | Rotat. quantum number [35] |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $v_{\text {exp }}\left[\mathrm{cm}^{-1}\right]$ | $\mathrm{V}_{\mathrm{T}}\left[\mathrm{cm}^{-1}\right]$ | $v_{\mathrm{N}}\left[\mathrm{cm}^{-1}\right]$ | $\nu_{B}\left[\mathrm{~cm}^{-1}\right]$ | $v_{\mathrm{K}}\left[\mathrm{cm}^{-1}\right]$ | $v_{T}-v_{\text {exp }}\left[\mathrm{cm}^{-1}\right]$ | $v_{N}-v_{\exp }\left[\mathrm{cm}^{-1}\right]$ | $v_{B}-v_{\exp }\left[\mathrm{cm}^{-1}\right]$ | $v_{\mathrm{K}}-v_{\exp }\left[\mathrm{cm}^{-1}\right]$ | Upper $\left(J K_{\mathrm{a}} K_{\mathrm{c}}\right)$ | Lower $\left(J K_{\mathrm{a}} K_{\mathrm{c}}\right)$ |
| 14980.652 | - | - | 14980.6566 | - | - | - | 0.005 | - | - | - |
| 14998.460 | 14998.790640 | 14998.482 | 14998.4526 | 14998.445948 | 0.331 | 0.022 | -0.007 | -0.014 | (919) | (10010) ${ }^{\text {a }}$ |
| 14998.595 | 14998.859730 | 14998.482 | 14998.5781 | 14998.588736 | 0.265 | -0.113 | -0.017 | -0.006 | (744) | (845) ${ }^{\text {a }}$ |
| 14999.288 | 14999.643670 | 14999.278 | 14999.2604 | 14999.259860 | 0.356 | -0.010 | -0.028 | -0.028 | (835) | (936) |
| 15007.763 | 15008.142890 | 15007.750 | 15007.7492 | 15007.750207 | 0.380 | -0.013 | -0.014 | -0.013 | (826) | (927) |
| 15009.036 | 15009.440770 | 15009.080 | 15009.0553 | 15009.055569 | 0.405 | 0.044 | 0.019 | 0.020 | (827) | (928) |
| 15009.812 | - | - | 15009.8058 | - | - | - | -0.006 | - | - | - |
| 15011.560 | 15011.956180 | 15011.573 | 15011.5664 | 15011.566883 | 0.397 | 0.013 | 0.006 | 0.007 | (817) | (918) |
| 15015.206 | 15015.573510 | 15015.223 | 15015.2195 | 15015.211553 | 0.368 | 0.017 | 0.014 | 0.006 | (642) | (743) |
| 15015.552 | 15015.882190 | 15015.494 | 15015.5701 | 15015.492908 | 0.330 | -0.058 | 0.018 | -0.059 | (734) | (835) |
| 15018.151 | 15018.495480 | 15018.137 | 15018.1408 | 15018.140773 | 0.344 | -0.014 | -0.010 | -0.010 | (808) | (909) |
| 15018.309 | 15018.661020 | 15018.279 | 15018.2877 | 15018.287719 | 0.352 | -0.030 | -0.021 | -0.021 | (818) | (919) |
| 15025.187 | 15025.567510 | 15025.156 | 15025.1710 | 15025.170528 | 0.381 | -0.031 | -0.016 | -0.016 | (725) | (826) |
| 15027.311 | 15027.691500 | 15027.297 | 15027.3017 | 15027.301748 | 0.381 | -0.014 | -0.009 | -0.009 | (726) | (827) |
| 15030.302 | 15030.682620 | 15030.288 | 15030.2877 | 15030.287709 | 0.381 | -0.014 | -0.014 | -0.014 | (716) | (817) |
| 15031.854 | 15032.231200 | 15031.862 | 15031.8481 | 15031.840302 | 0.377 | 0.008 | -0.006 | -0.014 | (633) | (734) |
| 15032.223 | 15032.615690 | 15032.240 | 15032.2228 | 15032.222510 | 0.393 | 0.017 | 0.000 | 0.000 | (634) | (735) |
| 15036.938 | 15037.272430 | 15036.922 | 15036.9230 | 15036.923018 | 0.334 | -0.016 | -0.015 | -0.015 | (707) | (808) |
| 15037.210 | 15037.582210 | 15037.202 | 15037.2007 | 15037.200696 | 0.372 | -0.008 | -0.009 | -0.009 | (717) | (818) |
| 15042.099 | 15042.487830 | 15042.096 | 15042.0904 | 15042.090184 | 0.389 | -0.003 | -0.009 | -0.009 | (624) | (725) |
| 15044.803 | 15045.180270 | 15044.806 | 15044.7972 | 15044.797231 | 0.377 | 0.003 | -0.006 | -0.006 | (625) | (726) |
| 15048.072 | 15048.464640 | 15048.065 | 15048.0650 | 15048.065029 | 0.393 | -0.007 | -0.007 | -0.007 | (615) | (716) |
| 15048.471 | 15048.863090 | 15048.468 | 15048.4724 | 15048.472464 | 0.392 | -0.003 | 0.001 | 0.001 | (532) | (633) |
| 15048.946 | 15049.321790 | 15048.933 | 15048.9295 | 15048.929423 | 0.376 | -0.013 | -0.017 | -0.017 | (533) | (634) |
| 15055.462 | 15055.834340 | 15055.459 | 15055.4577 | 15055.457843 | 0.372 | -0.003 | -0.004 | -0.004 | (616) | (717) |
| 15056.517 | 15056.881050 | 15056.506 | 15056.5045 | 15056.504454 | 0.364 | -0.011 | -0.013 | -0.013 | (606) | (707) |
| 15058.792 | 15059.181610 | 15058.780 | 15058.7814 | 15058.781397 | 0.390 | -0.012 | -0.011 | -0.011 | (523) | (624) |
| 15061.873 | 15062.257800 | 15061.861 | 15061.8620 | 15061.861994 | 0.385 | -0.012 | -0.011 | -0.011 | (524) | (625) |
| 15065.067 | 15065.458120 | 15065.055 | 15065.0558 | 15065.055815 | 0.391 | -0.012 | -0.011 | -0.011 | (514) | (615) |
| 15065.195 | 15065.580410 | 15065.194 | 15065.1888 | 15065.188531 | 0.385 | -0.001 | -0.006 | -0.006 | (431) | (532) |
| 15065.496 | 15065.881820 | 15065.496 | 15065.4902 | 15065.490114 | 0.386 | 0.000 | -0.006 | -0.006 | (432) | (533) |
| 15072.133 | 15072.381000 | 15072.114 | 15072.1184 | 15072.119566 | 0.248 | -0.019 | -0.015 | -0.013 | (505) | (616) ${ }^{\text {a }}$ |
| 15072.871 | 15073.239710 | 15072.862 | 15072.8711 | 15072.876602 | 0.369 | -0.009 | 0.000 | -0.006 | (515) | (616) |
| 15074.453 | 15074.681280 | 15074.434 | 15074.4247 | 15074.420511 | 0.228 | -0.019 | -0.028 | -0.032 | (505) | (606) ${ }^{\text {a }}$ |
| 15075.176 | 15075.540000 | 15075.166 | 15075.1775 | 15075.177547 | 0.364 | -0.010 | 0.002 | 0.002 | (515) | (606) |
| 15075.605 | 15075.999520 | 15075.583 | 15075.5992 | 15075.599196 | 0.395 | -0.022 | -0.006 | -0.006 | (422) | (523) |
| 15078.415 | 15078.804000 | 15078.397 | 15078.4061 | 15078.405628 | 0.389 | -0.018 | -0.009 | -0.009 | (423) | (524) |
| 15080.457 | - | 15080.473 | 15080.4797 | - | - | 0.016 | 0.023 | - | - |  |
| $15081.572^{\text {b }}$ | 15081.997230 | 15081.594 | 15081.5937 | 15081.593588 | 0.425 | 0.022 | 0.022 | 0.022 | (413) | (514) |
| 15081.805 | 15082.179800 | 15081.788 | 15081.7874 | 15081.793278 | 0.375 | -0.017 | -0.018 | -0.012 | (330) | (431) |
| 15081.926 | 15082.305390 | 15081.918 | 15081.9134 | 15081.913512 | 0.380 | -0.008 | -0.013 | -0.012 | (331) | (432) |
| 15089.300 | 15089.668880 | 15089.281 | 15089.2947 | 15089.294702 | 0.369 | -0.019 | -0.005 | -0.005 | (414) | (515) |
| 15090.280 | 15090.554910 | 15090.266 | 15090.2736 | 15090.275102 | 0.275 | -0.014 | -0.006 | -0.005 | (404) | (505) |
| 15092.585 | 15092.982560 | 15092.586 | 15092.5814 | 15092.581376 | 0.398 | 0.001 | -0.004 | -0.004 | (321) | (422) |
| 15093.202 | 15093.586700 | 15093.218 | 15093.2152 | 15093.213371 | 0.384 | 0.016 | 0.013 | 0.011 | (414) | (505) |
| 15093.346 | - | 15093.363 | 15093.3554 | - |  | 0.017 | 0.009 | - |  | - |
| 15094.641 | 15095.040630 | 15094.637 | 15094.6406 | 15094.640611 | 0.400 | -0.004 | 0.000 | 0.000 | (322) | (423) |
| 15097.986 | 15098.378760 | 15097.978 | 15097.9775 | 15097.976957 | 0.393 | -0.008 | -0.009 | -0.009 | (312) | (413) |


| $\begin{aligned} & \hline \mathrm{HD}^{16} \mathrm{O} \\ & \text { FT-IBBCEAS } \end{aligned}$ | Tomsk data [35] | Ref. [27] | Ref. [28] | Ref. [9] | Difference ( $\Delta v$ ) |  |  |  | Rotat. quantum number [35] |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $v_{\text {exp }}\left[\mathrm{cm}^{-1}\right]$ | $\mathrm{v}_{\mathrm{T}}\left[\mathrm{cm}^{-1}\right]$ | $v_{\mathrm{N}}\left[\mathrm{cm}^{-1}\right]$ | $\nu_{B}\left[\mathrm{~cm}^{-1}\right]$ | $\mathrm{v}_{\mathrm{K}}\left[\mathrm{cm}^{-1}\right]$ | $v_{T}-v_{\text {exp }}\left[\mathrm{cm}^{-1}\right]$ | $v_{N}-v_{\exp }\left[\mathrm{cm}^{-1}\right]$ | $v_{B}-v_{\exp }\left[\mathrm{cm}^{-1}\right]$ | $v_{\mathrm{K}}-v_{\exp }\left[\mathrm{cm}^{-1}\right]$ | Upper $\left(J K_{\mathrm{a}} K_{\mathrm{c}}\right)$ | Lower $\left(J K_{\mathrm{a}} K_{\mathrm{c}}\right)$ |
| 15210.717 | 15210.941370 | 15210.720 | 15210.7219 | 15210.722149 | 0.224 | 0.003 | 0.005 | 0.005 | (303) | (202) ${ }^{\text {a }}$ |
| 15214.092 | 15214.280150 | 15214.093 | 15214.0913 | 15214.091271 | 0.188 | 0.001 | -0.001 | -0.001 | (303) | (202) ${ }^{\text {a }}$ |
| 15214.778 | 15215.149530 | 15214.778 | 15214.7726 | 15214.768682 | 0.372 | 0.000 | -0.005 | -0.009 | (414) | (313) |
| 15216.653 | 15217.059490 | 15216.646 | 15216.6529 | 15216.653144 | 0.406 | -0.007 | 0.000 | 0.000 | (423) | (322) |
| 15218.310 | 15218.696800 | 15218.312 | 15218.3201 | 15218.320118 | 0.386 | 0.002 | 0.010 | 0.010 | (643) | (542) |
| 15220.917 | 15221.177070 | 15220.885 | 15220.8915 | 15220.891067 | 0.260 | -0.032 | -0.026 | -0.026 | (404) | (303) |
| 15222.514 | 15222.939060 | 15222.505 | 15222.5321 | 15222.529302 | 0.425 | -0.009 | 0.018 | 0.015 | (422) | (321) |
| 15224.367 | 15224.622410 | 15224.343 | 15224.3530 | 15224.352995 | 0.255 | -0.024 | -0.014 | -0.014 | (505) | $(414)^{\text {a }}$ |
| 15224.789 | 15225.113050 | 15224.760 | 15224.7656 | 15224.758722 | 0.324 | -0.029 | -0.023 | -0.030 | (854) | (753) |
| 15225.113 | 15225.481130 | 15225.108 | 15225.1104 | 15225.110031 | 0.368 | -0.005 | -0.003 | -0.003 | (515) | (414) |
| 15228.887 | - | 15228.898 | 15228.9024 | - | - | 0.011 | 0.015 | - | (625) | $(606)^{\text {f }}$ |
| 15229.693 | 15230.100870 | 15229.690 | 15229.6956 | 15229.695612 | 0.408 | -0.003 | 0.003 | 0.003 | (524) | (423) |
| 15230.364 | 15230.780240 | 15230.352 | 15230.3681 | 15230.368493 | 0.416 | -0.012 | 0.004 | 0.004 | (413) | (312) |
| 15230.574 | 15230.847210 | 15230.564 | 15230.5777 | 15230.578949 | 0.273 | -0.010 | 0.004 | 0.005 | (505) | $(404)^{\text {a }}$ |
| 15233.143 | 15233.547710 | 15233.116 | 15233.1304 | 15233.130459 | 0.405 | -0.027 | -0.013 | -0.013 | (744) | (643) |
| 15233.806 | 15234.187300 | 15233.782 | 15233.8007 | 15233.801028 | 0.381 | -0.024 | -0.005 | -0.005 | (606) | (515) |
| 15234.032 | 15234.424370 | 15234.011 | 15234.0341 | 15234.038611 | 0.392 | -0.021 | 0.002 | 0.007 | (616) | (515) |
| 15235.471 | 15235.866970 | 15235.450 | 15235.4610 | 15235.461313 | 0.396 | -0.021 | -0.010 | -0.010 | (634) | (533) |
| 15237.723 | 15238.105120 | 15237.724 | 15237.7196 | 15237.719697 | 0.382 | 0.001 | -0.003 | -0.003 | (606) | (505) |
| $15237.957^{\text {c }}$ | 15238.342190 | 15237.959 | 15237.9573 | 15237.957280 | 0.385 | 0.002 | 0.000 | 0.000 | (616) | (505) |
| 15239.403 | 15239.796960 | 15239.408 | 15239.3902 | 15239.392372 | 0.394 | 0.005 | -0.013 | -0.011 | (633) | (532) |
| 15240.495 | 15240.905830 | 15240.507 | 15240.4945 | 15240.494258 | 0.411 | 0.012 | -0.001 | -0.001 | (523) | (422) |
| 15241.595 | 15241.981800 | 15241.599 | 15241.5881 | 15241.588073 | 0.387 | 0.004 | -0.007 | -0.007 | (625) | (524) |
| 15241.799 | 15242.184180 | 15241.807 | 15241.7921 | 15241.792162 | 0.385 | 0.008 | -0.007 | -0.007 | (717) | (616) |
| 15243.132 | 15243.483550 | 15243.134 | 15243.1244 | 15243.124062 | 0.352 | 0.002 | -0.008 | -0.008 | (707) | (606) |
| 15244.578 | 15244.991000 | 15244.585 | 15244.5795 | 15244.579491 | 0.413 | 0.007 | 0.002 | 0.001 | (514) | (413) |
| 15248.639 | 15249.018050 | 15248.632 | 15248.6330 | 15248.632994 | 0.379 | -0.007 | -0.006 | -0.006 | (818) | (717) |
| 15248.827 | - | 15248.800 | 15248.8029 | - | - | -0.027 | -0.024 | - | (1019) | $(10110)^{\text {f }}$ |
| 15249.414 | 15249.773630 | 15249.404 | 15249.4071 | 15249.407455 | 0.360 | -0.010 | -0.007 | -0.007 | (808) | (707) |
| 15249.686 | 15250.007450 | 15249.670 | 15249.6676 | 15249.667657 | 0.321 | -0.016 | -0.018 | -0.018 | (735) | (634) |
| 15249.927 | 15250.301830 | 15249.916 | 15249.9188 | 15249.917188 | 0.375 | -0.011 | -0.008 | -0.010 | (818) | (707) |
| 15252.375 | 15252.774300 | 15252.374 | 15252.3727 | 15252.372695 | 0.399 | -0.001 | -0.002 | -0.002 | (726) | (625) |
| 15254.507 | 15254.874770 | 15254.499 | 15254.5008 | 15254.498377 | 0.368 | -0.008 | -0.006 | -0.009 | (909) | (818) ${ }^{\text {a }}$ |
| $15256.857^{\text {d }}$ | 15257.156160 | 15256.743 | 15256.7465 | 15256.746421 | 0.299 | -0.114 | -0.111 | -0.111 | (615) | (514) |
| 15257.633 | 15258.029670 | 15257.619 | 15257.6246 | 15257.624617 | 0.397 | -0.014 | -0.008 | -0.008 | (734) | (633) |
| $15258.258^{\text {e }}$ | 15258.629280 | 15258.213 | 15258.2185 | 15258.218845 | 0.371 | -0.045 | -0.040 | -0.039 | (624) | (523) |
| 15259.162 | 15259.479270 | 15259.132 | 15259.1391 | 15259.139193 | 0.317 | -0.030 | -0.023 | -0.023 | (10110) | (919) ${ }^{\text {a }}$ |
| 15259.516 | 15259.858860 | 15259.497 | 15259.5049 | 15259.501958 | 0.343 | -0.019 | -0.011 | -0.014 | (10010) | (919) ${ }^{\text {a }}$ |
| 15259.870 | 15260.221510 | 15259.856 | 15259.8644 | 15259.864745 | 0.351 | -0.014 | -0.006 | -0.005 | (10010) | (909) ${ }^{\text {a }}$ |
| 15261.723 | 15262.123640 | 15261.714 | 15261.7265 | 15261.725505 | 0.401 | -0.009 | 0.004 | 0.003 | (827) | (726) |
| 15262.288 | 15262.583520 | 15262.281 | 15262.2884 | 15262.299987 | 0.295 | -0.007 | 0.000 | 0.012 | (836) | (735) |
| 15263.049 | 15263.397670 | 15263.088 | 15263.0906 | 15263.090585 | 0.349 | 0.039 | 0.042 | 0.042 | (11111) | (10110) ${ }^{\text {a }}$ |
| 15266.349 | 15266.749240 | 15266.347 | 15266.3437 | 15266.343575 | 0.400 | -0.002 | -0.005 | -0.005 | (716) | (615) |
| 15267.464 | 15267.825700 | 15267.446 | 15267.4435 | 15267.443558 | 0.362 | -0.018 | -0.021 | -0.020 | (945) | (844) |
| 15269.739 | 15270.119200 | 15269.723 | 15269.7243 | 15269.724214 | 0.381 | -0.016 | -0.015 | -0.015 | (928) | (827) |
| 15273.392 | 15273.785090 | 15273.382 | 15273.3848 | 15273.384311 | 0.393 | -0.010 | -0.007 | -0.008 | (817) | (716) |
| 15273.950 | 15274.341470 | 15273.956 | 15273.9586 | 15273.958611 | 0.392 | 0.006 | 0.009 | 0.009 | (937) | (836) |
| 15274.718 | 15275.121000 | 15274.715 | 15274.7098 | 15274.710160 | 0.403 | -0.003 | -0.008 | -0.008 | (725) | (624) |

Experimental line (at $15081.572 \mathrm{~cm}^{-1}$ ) is also listed in Table 3a, since a $\mathrm{HD}^{16} \mathrm{O}$ line and a $\mathrm{HD}^{18} \mathrm{O}$ line from Ref. [35] overlap at this position within the experimental resolution.
${ }^{\text {E }}$ Experimental line (at $15237.957 \mathrm{~cm}^{-1}$ ) overlaps with a $\mathrm{H}_{2}^{18} \mathrm{O}$ line predicted in the Tomsk database [35]
Experimental line (at $15256.857 \mathrm{~cm}^{-1}$ ) overlaps with a $\mathrm{H}_{2}^{16} \mathrm{O}$ line from the Tomsk database [35].
Experimental line (at $15258.258 \mathrm{~cm}^{-1}$ ) overlaps with a $\mathrm{H}_{2}^{18} \mathrm{O}$ and a $\mathrm{H}_{2}^{16} \mathrm{O}$ absorption line [35].
${ }^{\mathrm{f}}$ Assignments from Naumenko and Campargue [27].

Table 2b
Measured rotational line positions (col 1) in the vibrational transition (142) $\leftarrow(000)$ of $\mathbf{H D} \mathbf{D}^{\mathbf{1 6}} \mathbf{O}$, which were assigned on basis of positions in the Tomsk database [35] (col 2) are compared with reported experimental line positions [27,28] (col 3 \& 4), and theoretical line lists [9] (col 5). The assignments (col 10, 11) are established by comparing the measured spectra with the theoretical line intensities from the 'Tomsk' database. The average difference of the measured (col 1 ) and predicted line positions from the Tomsk database [35] (col 2) is $0.160 \pm 0.036 \mathrm{~cm}^{-1}\left(1 \sigma\right.$, Student's $t$-distribution assumed) - Median $0.153 \mathrm{~cm}^{-1}$ (min. $0.109 \mathrm{~cm}^{-1}$, max. $0.203 \mathrm{~cm}^{-1}$ ). The differences, $\Delta v$, between the experimental data in this work and theoretical/measured line positions are listed in col (6-9). In total 9 ro-vibrational (142) lines were confirmed.

| $\mathrm{HD}^{16}$ <br> O FT- <br> IBBCEAS <br> $v_{\text {exp }}$ <br> [ $\mathrm{cm}^{-1}$ ] | Tomsk data [35]$\begin{aligned} & V_{\mathrm{T}} \\ & {\left[\mathrm{~cm}^{-1}\right]} \end{aligned}$ | Ref. [27]$\begin{aligned} & v_{\mathrm{N}} \\ & {\left[\mathrm{~cm}^{-1}\right]} \end{aligned}$ | Ref. [28]$\begin{aligned} & V_{\mathrm{B}} \\ & {\left[\mathrm{~cm}^{-1}\right]} \end{aligned}$ | Ref. [9] Difference ( $\Delta v$ ) |  |  |  |  | Rotat. Quantum number [35] |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | $\begin{aligned} & v_{\mathrm{K}} \\ & {\left[\mathrm{~cm}^{-1}\right]} \end{aligned}$ | $\begin{aligned} & v_{\mathrm{T}}-v_{\mathrm{exp}} \\ & {\left[\mathrm{~cm}^{-1}\right]} \end{aligned}$ | $\begin{aligned} & v_{\mathrm{N}}-v_{\text {exp }} \\ & {\left[\mathrm{cm}^{-1}\right]} \end{aligned}$ | $\begin{aligned} & v_{\mathrm{B}}-v_{\mathrm{exp}} \\ & {\left[\mathrm{~cm}^{-1}\right]} \end{aligned}$ | $\begin{aligned} & v_{\mathrm{K}}-v_{\mathrm{exp}} \\ & {\left[\mathrm{~cm}^{-1}\right]} \end{aligned}$ | Upper $\left(J K_{\mathrm{a}} K_{\mathrm{c}}\right)$ | $\begin{aligned} & \text { Lower } \\ & \left(J K_{\mathrm{a}} K_{\mathrm{c}}\right) \end{aligned}$ |
| 15041.760 | 15041.959390 | 15041.774 | 15041.7649 | 15041.764675 | 0.199 | 0.014 | 0.005 | 0.005 | (707) | (808) |
| 15080.246 | - | 15080.258 | 15080.2574 | - | - | 0.012 | 0.011 | - | (505) | (606) ${ }^{\text {a }}$ |
| 15091.545 | 15091.713390 | 15091.550 | 15091.5528 | 15091.552977 | 0.168 | 0.005 | 0.008 | 0.008 | (404) | (515) |
| 15095.485 | 15095.631210 | 15095.468 | 15095.4736 | 15095.471646 | 0.146 | -0.017 | -0.011 | -0.013 | (404) | (505) |
| 15217.053 | 15217.194040 | 15217.029 | 15217.0270 | 15217.026957 | 0.141 | -0.024 | -0.026 | -0.026 | (404) | (313) |
| 15226.100 | 15226.253360 | 15226.086 | 15226.0876 | 15226.087611 | 0.153 | -0.014 | -0.012 | -0.012 | (404) | (303) |
| 15236.428 | 15236.537110 | 15236.408 | 15236.4142 | 15236.414343 | 0.109 | -0.020 | -0.014 | -0.014 | (505) | (404) |
| 15247.968 | 15248.170500 | 15247.958 | 15247.9657 | 15247.965719 | 0.203 | -0.010 | -0.002 | -0.002 | (707) | (606) |
| 15267.629 | - | 15267.626 | 15267.6208 | - | - | -0.003 | -0.008 | - | (11011) | $(10110)^{\text {a }}$ |

${ }^{\text {a }}$ Assignments from Naumenko and Campargue [27].

Table 3a
Measured rotational line positions (col 2) in the vibrational transition ( 014 ) $\leftarrow(000)$ of $\mathbf{H} \mathbf{D}^{\mathbf{1 8}} \mathbf{O}$. The vibrational and rotational quantum number assignments (col 5,6 ) were established on basis of positions in the Tomsk database [35] (col 3). The differences, $\Delta v$, between the experimental data of this work (col 2) and those in the Tomsk database [35] ( $\operatorname{col} 3$ ) are listed in col 4 . The average difference is $0.305 \pm 0.064 \mathrm{~cm}^{-1}(1 \sigma)-$ median $0.331 \mathrm{~cm}^{-1}$ ( $\mathrm{min} .0 .130 \mathrm{~cm}^{-1}$, max. $0.388 \mathrm{~cm}^{-1}$ ). In total 114 ro-vibrational ( 014 ) lines were confirmed. Rotational quantum number assignments set in italics in rows 26/27, 32/33, 39/40, 63/64, 68/70 are ambiguous in [35].

| \# | $\mathrm{HD}^{18} \mathrm{O}$ <br> FT-IBBCEAS [this work] $\begin{aligned} & v_{\exp } \\ & {\left[\mathrm{cm}^{-1}\right]} \end{aligned}$ | Tomsk database [35]$v_{T}$$\left[\mathrm{cm}^{-1}\right]$ | Difference ( $\Delta v$ )$\begin{aligned} & v_{\mathrm{T}}-\mathrm{V}_{\mathrm{exp}} \\ & {\left[\mathrm{~cm}^{-1}\right]} \end{aligned}$ | Rotational quantum number[35] |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | Upper $\left(J K_{\mathrm{a}} K_{\mathrm{c}}\right)$ | Lower $\left(J K_{\mathrm{a}} K_{\mathrm{c}}\right)$ |
| 1 | 14975.288 | 14975.597870 | 0.310 | (808) | (909) |
| 2 | 14980.652 | 14981.000310 | 0.348 | (725) | (826) |
| 3 | 14982.957 | 14983.299160 | 0.342 | (726) | (827) |
| 4 | 14985.247 | 14985.560670 | 0.314 | (716) | (817) |
| 5 | 14987.499 | 14987.846860 | 0.348 | (633) | (734) |
| 6 | 14987.657 | 14987.967100 | 0.310 | (541) | (642) |
| 7 | 14987.838 | 14988.188090 | 0.350 | (634) | (735) |
| 8 | 14994.113 | 14994.405230 | 0.292 | (717) | (818) |
| 9 | 14994.264 | 14994.570690 | 0.307 | (707) | (808) |
| 10 | 14997.450 | 14997.807970 | 0.358 | (624) | (725) |
| 11 | 15000.343 | 15000.695300 | 0.352 | (625) | (726) |
| 12 | 15001.963 | 15002.176370 | 0.213 | (615) | (716) |
| 13 | 15004.019 | 15004.349280 | 0.330 | (532) | (633) |
| 14 | 15004.464 | 15004.813060 | 0.349 | (533) | (634) |
| 15 | 15012.162 | 15012.459800 | 0.298 | (616) | (717) |
| 16 | 15012.479 | 15012.752540 | 0.274 | (606) | (707) |
| 17 | 15014.136 | 15014.484850 | 0.349 | (523) | (624) |
| 18 | 15017.209 | 15017.555650 | 0.347 | (524) | (625) |
| 19 | 15020.358 | 15020.629750 | 0.272 | (514) | (615) |
| 20 | 15020.614 | 15020.951350 | 0.337 | (431) | (532) |
| 21 | 15020.923 | 15021.261830 | 0.339 | (432) | (533) |
| 22 | 15029.488 | 15029.772960 | 0.285 | (515) | (616) |
| 23 | 15029.593 | 15029.913440 | 0.320 | (505) | (606) |
| 24 | 15030.761 | 15031.118450 | 0.357 | (422) | (523) |
| 25 | 15033.640 | 15033.986970 | 0.347 | (423) | (524) |
| 26 | 15035.213 | 15035.391430 | 0.178 | (413) | (514) |
| 27 | 15039.341 | 15039.485640 | 0.145 | (413) | (514) |
| 28 | 15046.106 | 15046.392600 | 0.287 | (404) | (505) |
| 29 | 15046.106 | 15046.415150 | 0.309 | (414) | (515) |
| 30 | 15047.658 | 15048.015380 | 0.357 | (321) | (422) |
| 31 | 15049.752 | 15050.110330 | 0.358 | (322) | (423) |
| 32 | 15051.025 | 15051.177940 | 0.153 | (312) | (413) |
| 33 | 15055.304 | 15055.496210 | 0.192 | (312) | (413) |
| 34 | 15058.551 | 15058.858850 | 0.308 | (550) | (551) |
| 35 | 15061.526 | 15061.857000 | 0.331 | (303) | (404) |
| 36 | 15062.197 | 15062.455150 | 0.258 | (313) | (414) |
| 37 | 15064.539 | 15064.899580 | 0.361 | (220) | (321) |
| 38 | 15065.662 | 15066.023750 | 0.362 | (221) | (322) |
| 39 | 15067.214 | 15067.374110 | 0.160 | (211) | (312) |
| 40 | 15071.583 | 15071.784630 | 0.202 | (211) | (312) |
| 41 | 15076.841 | 15077.178770 | 0.338 | (202) | (303) |

Table 3a (continued)

| \# | $\mathrm{HD}^{18} \mathrm{O}$ <br> FT-IBBCEAS [this work] | Tomsk database [35] | Difference ( $\Delta v$ ) | Rotational quantum number [35] |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\begin{aligned} & V_{\exp } \\ & {\left[\mathrm{cm}^{-1}\right]} \end{aligned}$ | $\begin{aligned} & \mathrm{V}_{\mathrm{T}} \\ & {\left[\mathrm{~cm}^{-1}\right]} \end{aligned}$ | $\begin{aligned} & v_{\mathrm{T}}-v_{\mathrm{exp}} \\ & {\left[\mathrm{~cm}^{-1}\right]} \end{aligned}$ | Upper $\left(J K_{\mathrm{a}} K_{\mathrm{c}}\right)$ | Lower $\left(J K_{\mathrm{a}} K_{\mathrm{c}}\right)$ |
| 42 | 15077.737 | 15077.977960 | 0.241 | (212) | (313) |
| 43 | 15080.781 | 15081.094670 | 0.314 | (542) | (541) |
| 44 | 15080.781 | 15081.168660 | 0.388 | (541) | (542) |
| 45 | $15081.572^{\text {a }}$ | 15081.871860 | 0.300 | (441) | (440) |
| 46 | 15092.020 | 15092.366710 | 0.347 | (101) | (202) |
| 47 | 15092.803 | 15093.044860 | 0.242 | (111) | (212) |
| 48 | 15097.014 | 15097.364430 | 0.350 | (533) | (532) |
| 49 | 15098.461 | 15098.804090 | 0.343 | (432) | (431) |
| 50 | 15099.108 | 15099.460760 | 0.353 | (431) | (432) |
| 51 | 15099.334 | 15099.664130 | 0.330 | (331) | (330) |
| 52 | 15099.402 | 15099.759960 | 0.358 | (330) | (331) |
| 53 | 15099.545 | 15099.893250 | 0.348 | (532) | (533) |
| 54 | 15104.901 | 15105.252120 | 0.351 | (423) | (422) |
| 55 | 15107.365 | 15107.709570 | 0.345 | (000) | (101) |
| 56 | 15109.331 | 15109.696290 | 0.365 | (322) | (321) |
| 57 | 15111.515 | 15111.868530 | 0.354 | (221) | (220) |
| 58 | 15111.673 | 15111.907220 | 0.234 | (212) | (211) |
| 59 | 15112.442 | 15112.797820 | 0.356 | (220) | (221) |
| 60 | 15113.813 | 15114.176430 | 0.363 | (321) | (322) |
| 61 | 15117.399 | 15117.758820 | 0.360 | (422) | (423) |
| 62 | 15118.265 | 15118.494230 | 0.229 | (111) | (110) |
| 63 | 15119.892 | 15120.054670 | 0.163 | (110) | (111) |
| 64 | 15124.276 | 15124.488800 | 0.213 | (110) | (111) |
| 65 | 15129.655 | 15129.855110 | 0.200 | (211) | (212) |
| 66 | 15137.918 | 15138.267250 | 0.349 | (101) | (000) |
| 67 | 15147.862 | 15148.108060 | 0.246 | (212) | (111) |
| 68 | 15150.717 | 15150.893970 | 0.177 | (211) | (110) |
| 69 | 15152.186 | 15152.528470 | 0.342 | (202) | (101) |
| 70 | 15155.101 | 15155.304490 | 0.203 | (211) | (110) |
| 71 | 15157.233 | 15157.594530 | 0.362 | (322) | (221) |
| 72 | 15159.659 | 15160.021220 | 0.362 | (321) | (220) |
| 73 | 15159.802 | 15160.069930 | 0.268 | (313) | (212) |
| 74 | 15160.751 | 15161.111250 | 0.360 | (432) | (331) |
| 75 | 15161.195 | 15161.542470 | 0.347 | (431) | (330) |
| 76 | 15164.819 | 15165.150100 | 0.331 | (303) | (202) |
| 77 | 15167.169 | 15167.342040 | 0.173 | (312) | (211) |
| 78 | 15170.777 | 15171.055790 | 0.279 | (414) | (313) |
| 79 | 15171.056 | 15171.413180 | 0.357 | (423) | (322) |
| 80 | 15171.470 | 15171.660310 | 0.190 | (312) | (211) |
| 81 | 15175.523 | 15175.873830 | 0.351 | (533) | (432) |
| 82 | 15175.779 | 15176.095530 | 0.317 | (404) | (303) |
| 83 | 15177.007 | 15177.344780 | 0.338 | (422) | (321) |
| 84 | $15177.067^{\text {b }}$ | 15177.435510 | 0.369 | (532) | (431) |
| 85 | 15180.683 | 15180.977910 | 0.295 | (515) | (414) |
| 86 | 15183.139 | 15183.325560 | 0.187 | (413) | (312) |
| 87 | 15184.020 | 15184.371530 | 0.352 | (524) | (423) |
| 88 | 15184.631 | 15184.949840 | 0.319 | (505) | (404) |
| 89 | 15187.290 | 15187.419770 | 0.130 | (413) | (312) |
| 90 | 15189.512 | 15189.817040 | 0.305 | (616) | (515) |
| 91 | 15189.926 | 15190.281390 | 0.355 | (634) | (533) |
| 92 | 15192.367 | 15192.657680 | 0.291 | (606) | (505) |
| 93 | 15194.039 | 15194.391280 | 0.352 | (633) | (532) |
| 94 | 15194.966 | 15195.330180 | 0.364 | (523) | (422) |
| 95 | 15195.908 | 15196.264830 | 0.357 | (625) | (524) |
| 96 | 15197.271 | 15197.580400 | 0.309 | (717) | (616) |
| 97 | 15198.800 | 15199.082460 | 0.282 | (514) | (413) |
| 98 | 15198.981 | 15199.287810 | 0.307 | (707) | (606) |
| 99 | 15203.734 | 15204.084530 | 0.351 | (735) | (634) |
| 100 | $15204.066^{\text {c }}$ | 15204.334970 | 0.269 | (818) | (717) |
| 101 | 15204.887 | 15205.212040 | 0.325 | (808) | (707) |
| 102 | 15206.574 | 15206.939080 | 0.365 | (726) | (625) |
| 103 | 15209.316 | 15209.528370 | 0.212 | (615) | (514) |
| 104 | $15209.859^{\text {d }}$ | 15210.184250 | 0.325 | (919) | (818) |
| 105 | 15210.356 | 15210.685230 | 0.329 | (909) | (808) |
| 106 | 15212.299 | 15212.655620 | 0.357 | (734) | (633) |
| 107 | 15212.503 | 15212.872190 | 0.369 | (624) | (523) |
| 108 | $15213.362^{\text {e }}$ | 15213.507650 | 0.146 | (615) | (514) |
| 109 | 15215.817 | 15216.159430 | 0.342 | (827) | (726) |
| 110 | 15219.697 | 15220.010760 | 0.314 | (716) | (615) |
| 111 | 15226.921 | 15227.255310 | 0.334 | (817) | (716) |
| 112 | $15228.887^{\text {c }}$ | 15229.245090 | 0.358 | (725) | (624) |
| 113 | 15232.058 | 15232.392350 | 0.334 | (918) | (817) |
| 114 | 15243.283 | 15243.621020 | 0.338 | (826) | (725) |

${ }^{\text {a }}$ Experimental line 45 (at $15081.572 \mathrm{~cm}^{-1}$ ) is also listed in Table 2a, since a $\mathrm{HD}^{16} \mathrm{O}$ line and a $\mathrm{HD}^{18} \mathrm{O}$ line from Ref. [35] overlap at this position within the resolution of the setup.
${ }^{\text {b }}$ Experimental line 84 (at $15177.067 \mathrm{~cm}^{-1}$ ) overlaps with a $\mathrm{H}_{2}^{18} \mathrm{O}$ line predicted in the Tomsk database [35].
${ }^{\text {c }}$ Experimental line 100 (at $15204.066 \mathrm{~cm}^{-1}$ ) overlaps with a $\mathrm{H}_{2}^{18} \mathrm{O}$ and $\mathrm{HD}^{16} \mathrm{O}$ line from [35].
${ }^{\text {d }}$ Experimental lines 104 and 112 (at 15209.859 and $15228.887 \mathrm{~cm}^{-1}$ ) overlap with individual $\mathrm{HD}^{16} \mathrm{O}$ absorption lines reported in [28].
${ }^{e}$ Experimental line 108 (at $15213.362 \mathrm{~cm}^{-1}$ ) overlaps with a $\mathrm{HD}^{16} \mathrm{O}$ line reported in Refs. [9,28].

Table 3b
Measured rotational line positions (col 2) in the vibrational transition (142) $\leftarrow(000)$ of $\mathbf{H D}^{\mathbf{1 8}} \mathbf{O}$. The vibrational and rotational quantum number assignments (col 5 , 6 ) were established on basis of positions in the Tomsk database [35] (col 3). The differences, $\Delta v$, between the experimental data ( $\operatorname{col} 2$ ) in this work and those in the Tomsk database [35] ( col 3 ) are listed in col 4. The average difference is $0.122 \mathrm{~cm}^{-1}$.

| $\#$ | $\mathrm{HD}^{18} \mathrm{O}$ | Tomsk database | Difference $(\Delta v)$ | Rotational quantum number |
| :--- | :--- | :--- | :--- | :--- |
|  | FT-IBBCEAS [this work] | $[35]$ |  | [35] |
|  | $v_{\exp }$ | $v_{\mathrm{T}}$ | $v_{\mathrm{T}}-v_{\exp }$ | Upper |
|  | $\left[\mathrm{cm}^{-1}\right]$ | 15057.423900 | $\left[\mathrm{~cm}^{-1}\right]$ | 0.116 |
| $\left(J K_{\mathrm{a}} K_{\mathrm{c}}\right)$ |  |  |  |  |
| 1 | 15057.308 | 15073.221850 | $(313)$ |  |
| 2 | 15073.097 | 15155.038680 | 0.125 | $(212)$ |
| 3 | 15154.913 | 0.126 | $(313)$ |  |



Fig. 3. Magnified view of Fig. 2; a section of the $P$ branch of the $v_{2}+4 v_{3}$ band of $\mathrm{HD}^{18} \mathrm{O}$ and $\mathrm{HD}^{16} \mathrm{O}$. Black trace: measured FT-IBBCEAS spectrum. Red trace: line intensities of $\mathrm{HD}^{18} \mathrm{O}$. Blue trace: line intensities of $\mathrm{HD}^{16} \mathrm{O}$. Inset (the shaded region in the black dashed rectangle): magnified view of the region between $15061.3 \mathrm{~cm}^{-1}$ and $15062.5 \mathrm{~cm}^{-1}$. The line at $15061.9 \mathrm{~cm}^{-1}$ belongs to $\mathrm{HD}^{16} \mathrm{O}$, whereas the other two peaks at $15061.5 \mathrm{~cm}^{-1}$ and $15062.2 \mathrm{~cm}^{-1}$ are assigned to $\mathrm{HD}^{18} \mathrm{O}$. The dashed vertical line in the inset indicates the position of the corresponding line listed in Refs. [27,28]. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

## CRediT authorship contribution statement

S. Chandran: Formal analysis, Writing - review \& editing, Methodology. S. Dixneuf: Investigation, Data curation, Funding acquisition. J. Orphal: Conceptualization, Writing - review \& editing. A.A. Ruth: Writing - original draft, Supervision, Conceptualization, Project administration.

## Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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## Appendix A. Supplementary material

Supplementary data to this article can be found online at https://doi.org/10.1016/j.jms.2020.111395.

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