

Test of Lepton-Flavor Universality in $B \rightarrow K^* \ell^+ \ell^-$ Decays at Belle

S. Wehle,⁶ I. Adachi,^{14,11} K. Adamczyk,⁵⁶ H. Aihara,⁸¹ D. M. Asner,³ H. Atmacan,⁵ V. Aulchenko,^{4,59} T. Aushev,¹⁶ R. Ayad,⁷⁵ V. Babu,⁶ P. Behera,²² M. Berger,⁷² V. Bhardwaj,²⁰ J. Biswal,³⁰ A. Bozek,⁵⁶ M. Bračko,^{44,30} T. E. Browder,¹³ M. Campajola,^{27,51} L. Cao,² M.-C. Chang,⁸ A. Chen,⁵³ B. G. Cheon,¹² K. Chilikin,⁴⁰ K. Cho,³⁴ Y. Choi,⁷³ S. Choudhury,²¹ D. Cinabro,⁸⁵ S. Cunliffe,⁶ N. Dash,²² G. De Nardo,^{27,51} F. Di Capua,^{27,51} S. Dubey,¹³ S. Eidelman,^{4,59,40} D. Epifanov,^{4,59} T. Ferber,⁶ B. G. Fulsom,⁶¹ R. Garg,⁶² V. Gaur,⁸⁴ N. Gabyshev,^{4,59} A. Garmash,^{4,59} A. Giri,²¹ P. Goldenzweig,³¹ D. Greenwald,⁷⁷ Y. Guan,⁵ J. Haba,^{14,11} O. Hartbrich,¹³ K. Hayasaka,⁵⁸ H. Hayashii,⁵² M. T. Hedges,¹³ T. Higuchi,³² W.-S. Hou,⁵⁵ C.-L. Hsu,⁷⁴ T. Iijima,^{50,49} K. Inami,⁴⁹ G. Inguglia,²⁵ A. Ishikawa,^{14,11} R. Itoh,^{14,11} M. Iwasaki,⁶⁰ Y. Iwasaki,¹⁴ W. W. Jacobs,²³ S. Jia,⁹ Y. Jin,⁸¹ D. Joffe,³³ J. Kahn,³¹ A. B. Kaliyar,⁷⁶ G. Karyan,⁶ H. Kichimi,¹⁴ D. Y. Kim,⁷¹ K. T. Kim,³⁵ S. H. Kim,⁶⁸ Y.-K. Kim,⁸⁷ K. Kinoshita,⁵ I. Komarov,⁶ S. Korpar,^{44,30} D. Kotchetkov,¹³ R. Kroeger,⁴⁶ P. Krokovny,^{4,59} T. Kuhr,⁴² R. Kulasiri,³³ R. Kumar,⁶⁵ K. Kumara,⁸⁵ A. Kuzmin,^{4,59} Y.-J. Kwon,⁸⁷ J. S. Lange,¹⁰ J. Y. Lee,⁶⁸ S. C. Lee,³⁷ Y. B. Li,⁶³ J. Libby,²² Z. Liptak,¹⁸ D. Liventsev,^{85,14} T. Luo,⁹ J. MacNaughton,⁴⁷ M. Masuda,^{80,66} T. Matsuda,⁴⁷ J. T. McNeil,⁷ M. Merola,^{27,51} F. Metzner,³¹ H. Miyata,⁵⁸ R. Mizuk,^{40,16} G. B. Mohanty,⁷⁶ T. J. Moon,⁶⁸ R. Mussa,²⁸ M. Nakao,^{14,11} A. Natchii,¹³ M. Nayak,⁷⁸ C. Niebuhr,⁶ M. Niiyama,³⁶ N. K. Nisar,³ S. Nishida,^{14,11} K. Ogawa,⁵⁸ S. Ogawa,⁷⁹ H. Ono,^{57,58} Y. Onuki,⁸¹ P. Pakhlov,^{40,48} G. Pakhlova,^{16,40} H. Park,³⁷ S.-H. Park,⁸⁷ T. K. Pedlar,⁴³ R. Pestotnik,³⁰ L. E. Piilonen,⁸⁴ T. Podobnik,^{41,30} V. Popov,¹⁶ E. Prencipe,¹⁷ M. T. Prim,³¹ P. K. Resmi,²² M. Ritter,⁴² A. Rostomyan,⁶ N. Rout,²² G. Russo,⁵¹ D. Sahoo,⁷⁶ Y. Sakai,^{14,11} S. Sandilya,⁵ A. Sangal,⁵ L. Santelj,^{41,30} V. Savinov,⁶⁴ O. Schneider,³⁹ G. Schnell,^{1,19} J. Schueler,¹³ C. Schwanda,²⁵ A. J. Schwartz,⁵ Y. Seino,⁵⁸ K. Senyo,⁸⁶ M. E. Sevir,⁴⁵ M. Shapkin,²⁶ J.-G. Shiu,⁵⁵ B. Shwartz,^{4,59} E. Solovieva,⁴⁰ M. Starič,³⁰ J. F. Strube,⁶¹ T. Sumiyoshi,⁸³ W. Sutcliffe,² M. Takizawa,^{69,15} U. Tamponi,²⁸ K. Tanida,²⁹ Y. Tao,⁷ F. Tenchini,⁶ K. Trabelsi,³⁸ M. Uchida,⁸² T. Uglov,^{40,16} Y. Unno,¹² S. Uno,^{14,11} Y. Ushiroda,^{14,11} S. E. Vahsen,¹³ R. Van Tonder,² G. Varner,¹³ K. E. Varvell,⁷⁴ V. Vorobyev,^{4,59,40} C. H. Wang,⁵⁴ M.-Z. Wang,⁵⁵ P. Wang,²⁴ X. L. Wang,⁹ E. Won,³⁵ X. Xu,⁷⁰ S. B. Yang,³⁵ H. Ye,⁶ J. H. Yin,³⁵ C. Z. Yuan,²⁴ Z. P. Zhang,⁶⁷ V. Zhilich,^{4,59} V. Zhukova,⁴⁰ and V. Zhulanov^{4,59}

(Belle Collaboration)

¹University of the Basque Country UPV/EHU, 48080 Bilbao²University of Bonn, 53115 Bonn³Brookhaven National Laboratory, Upton, New York 11973⁴Budker Institute of Nuclear Physics SB RAS, Novosibirsk 630090⁵University of Cincinnati, Cincinnati, Ohio 45221⁶Deutsches Elektronen-Synchrotron, 22607 Hamburg⁷University of Florida, Gainesville, Florida 32611⁸Department of Physics, Fu Jen Catholic University, Taipei 24205⁹Key Laboratory of Nuclear Physics and Ion-beam Application (MOE) and Institute of Modern Physics, Fudan University, Shanghai 200443¹⁰Justus-Liebig-Universität Gießen, 35392 Gießen¹¹SOKENDAI (The Graduate University for Advanced Studies), Hayama 240-0193¹²Department of Physics and Institute of Natural Sciences, Hanyang University, Seoul 04763¹³University of Hawaii, Honolulu, Hawaii 96822¹⁴High Energy Accelerator Research Organization (KEK), Tsukuba 305-0801¹⁵J-PARC Branch, KEK Theory Center, High Energy Accelerator Research Organization (KEK), Tsukuba 305-0801¹⁶Higher School of Economics (HSE), Moscow 101000¹⁷Forschungszentrum Jülich, 52425 Jülich¹⁸Hiroshima Institute of Technology, Hiroshima 731-5193¹⁹IKERBASQUE, Basque Foundation for Science, 48013 Bilbao²⁰Indian Institute of Science Education and Research Mohali, SAS Nagar, 140306²¹Indian Institute of Technology Hyderabad, Telangana 502285²²Indian Institute of Technology Madras, Chennai 600036²³Indiana University, Bloomington, Indiana 47408²⁴Institute of High Energy Physics, Chinese Academy of Sciences, Beijing 100049²⁵Institute of High Energy Physics, Vienna 1050²⁶Institute for High Energy Physics, Provnino 142281

- ²⁷*INFN—Sezione di Napoli, 80126 Napoli*
²⁸*INFN—Sezione di Torino, 10125 Torino*
²⁹*Advanced Science Research Center, Japan Atomic Energy Agency, Naka 319-1195*
³⁰*J. Stefan Institute, 1000 Ljubljana*
³¹*Institut für Experimentelle Teilchenphysik, Karlsruher Institut für Technologie, 76131 Karlsruhe*
³²*Kavli Institute for the Physics and Mathematics of the Universe (WPI), University of Tokyo, Kashiwa 277-8583*
³³*Kennesaw State University, Kennesaw, Georgia 30144*
³⁴*Korea Institute of Science and Technology Information, Daejeon 34141*
³⁵*Korea University, Seoul 02841*
³⁶*Kyoto Sangyo University, Kyoto 603-8555*
³⁷*Kyungpook National University, Daegu 41566*
³⁸*Université Paris-Saclay, CNRS/IN2P3, IJCLab, 91405 Orsay*
³⁹*École Polytechnique Fédérale de Lausanne (EPFL), Lausanne 1015*
⁴⁰*P. N. Lebedev Physical Institute of the Russian Academy of Sciences, Moscow 119991*
⁴¹*Faculty of Mathematics and Physics, University of Ljubljana, 1000 Ljubljana*
⁴²*Ludwig Maximilians University, 80539 Munich*
⁴³*Luther College, Decorah, Iowa 52101*
⁴⁴*University of Maribor, 2000 Maribor*
⁴⁵*School of Physics, University of Melbourne, Victoria 3010*
⁴⁶*University of Mississippi, University, Mississippi 38677*
⁴⁷*University of Miyazaki, Miyazaki 889-2192*
⁴⁸*Moscow Physical Engineering Institute, Moscow 115409*
⁴⁹*Graduate School of Science, Nagoya University, Nagoya 464-8602*
⁵⁰*Kobayashi-Maskawa Institute, Nagoya University, Nagoya 464-8602*
⁵¹*Università di Napoli Federico II, 80126 Napoli*
⁵²*Nara Women's University, Nara 630-8506*
⁵³*National Central University, Chung-li 32054*
⁵⁴*National United University, Miao Li 36003*
⁵⁵*Department of Physics, National Taiwan University, Taipei 10617*
⁵⁶*H. Niewodniczanski Institute of Nuclear Physics, Krakow 31-342*
⁵⁷*Nippon Dental University, Niigata 951-8580*
⁵⁸*Niigata University, Niigata 950-2181*
⁵⁹*Novosibirsk State University, Novosibirsk 630090*
⁶⁰*Osaka City University, Osaka 558-8585*
⁶¹*Pacific Northwest National Laboratory, Richland, Washington 99352*
⁶²*Panjab University, Chandigarh 160014*
⁶³*Peking University, Beijing 100871*
⁶⁴*University of Pittsburgh, Pittsburgh, Pennsylvania 15260*
⁶⁵*Punjab Agricultural University, Ludhiana 141004*
⁶⁶*Research Center for Nuclear Physics, Osaka University, Osaka 567-0047*
⁶⁷*Department of Modern Physics and State Key Laboratory of Particle Detection and Electronics, University of Science and Technology of China, Hefei 230026*
⁶⁸*Seoul National University, Seoul 08826*
⁶⁹*Showa Pharmaceutical University, Tokyo 194-8543*
⁷⁰*Soochow University, Suzhou 215006*
⁷¹*Soongsil University, Seoul 06978*
⁷²*Stefan Meyer Institute for Subatomic Physics, Vienna 1090*
⁷³*Sungkyunkwan University, Suwon 16419*
⁷⁴*School of Physics, University of Sydney, New South Wales 2006*
⁷⁵*Department of Physics, Faculty of Science, University of Tabuk, Tabuk 71451*
⁷⁶*Tata Institute of Fundamental Research, Mumbai 400005*
⁷⁷*Department of Physics, Technische Universität München, 85748 Garching*
⁷⁸*School of Physics and Astronomy, Tel Aviv University, Tel Aviv 69978*
⁷⁹*Toho University, Funabashi 274-8510*
⁸⁰*Earthquake Research Institute, University of Tokyo, Tokyo 113-0032*
⁸¹*Department of Physics, University of Tokyo, Tokyo 113-0033*
⁸²*Tokyo Institute of Technology, Tokyo 152-8550*
⁸³*Tokyo Metropolitan University, Tokyo 192-0397*
⁸⁴*Virginia Polytechnic Institute and State University, Blacksburg, Virginia 24061*
⁸⁵*Wayne State University, Detroit, Michigan 48202*

⁸⁶Yamagata University, Yamagata 990-8560
⁸⁷Yonsei University, Seoul 03722

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We present a measurement of R_{K^*} , the branching fraction ratio $\mathcal{B}(B \rightarrow K^* \mu^+ \mu^-) / \mathcal{B}(B \rightarrow K^* e^+ e^-)$, for both charged and neutral B mesons. The ratio for the charged case $R_{K^{*+}}$ is the first measurement ever performed. In addition, we report absolute branching fractions for the individual modes in bins of the squared dilepton invariant mass q^2 . The analysis is based on a data sample of 711 fb^{-1} , containing $772 \times 10^6 B\bar{B}$ events, recorded at the $\Upsilon(4S)$ resonance with the Belle detector at the KEKB asymmetric-energy e^+e^- collider. The obtained results are consistent with standard model expectations.

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In the standard model (SM), the coupling of gauge bosons to leptons is independent of lepton flavor, a concept known as lepton-flavor universality (LFU). Therefore, experimental tests of LFU are excellent probes for new physics (NP). In this Letter, we present a test of LFU in $B \rightarrow K^* \ell^+ \ell^-$ decays, where ℓ is either e or μ . These decays have been studied by several experiments, and some results suggest an intriguing possibility that the underlying $b \rightarrow s \ell^+ \ell^-$ transition may be affected by physics beyond the SM in modes involving muons [1–6]. The ratio of branching fractions

$$R_{K^*} = \frac{\mathcal{B}(B \rightarrow K^* \mu^+ \mu^-)}{\mathcal{B}(B \rightarrow K^* e^+ e^-)} \quad (1)$$

is well suited to test LFU [7]. The theoretical predictions for R_{K^*} are robust [7–9], as uncertainties related to form factors cancel out in the ratio. This observable is expected to be close to unity in the SM.

For this measurement, we reconstruct the decay channels $B^0 \rightarrow K^{*0} \mu^+ \mu^-$, $B^+ \rightarrow K^{*+} \mu^+ \mu^-$, $B^0 \rightarrow K^{*0} e^+ e^-$, and $B^+ \rightarrow K^{*+} e^+ e^-$. The K^* meson is reconstructed in the $K^+ \pi^-$, $K^+ \pi^0$, and $K_S^0 \pi^+$ decay modes. The inclusion of charge-conjugate states is implied throughout this Letter. Compared to the previous analysis [6], the full $\Upsilon(4S)$ data sample containing $772 \times 10^6 B\bar{B}$ events, recorded with the Belle detector [10] at the KEKB asymmetric-energy e^+e^- collider [11], is used.

Belle is a large-solid-angle magnetic spectrometer that consists of a silicon vertex detector, a 50-layer central drift chamber (CDC), an array of aerogel threshold Cherenkov counters (ACC), a barrel-like arrangement of time-of-flight scintillation counters (TOF), and an electromagnetic calorimeter (ECL) comprised of CsI(Tl) crystals. All these components are located inside a superconducting solenoid

coil that provides a 1.5 T magnetic field. An iron flux return placed outside of the coil is instrumented with resistive plate chambers to detect K_L^0 mesons and muons (KLM).

The analysis is validated and optimized with simulated Monte Carlo (MC) data samples, from which the selection efficiencies are also derived. The EvtGen [12] and PYTHIA [13] packages are used to generate decay chains, where final state radiation is incorporated with PHOTOS [14]. The detector response is simulated with GEANT3 [15].

All tracks, except for those from K_S^0 decays, need to satisfy requirements on their impact parameter with respect to the interaction point along the z axis ($|dz| < 5.0 \text{ cm}$) and in the transverse x - y plane ($|dr| < 1.0 \text{ cm}$). The z axis is in the direction opposite to that of the e^+ beam. We calculate a particle identification (PID) likelihood for each track using energy loss in the CDC, information from the TOF, number of photoelectrons from the ACC, the transverse shower shape and energy in the ECL, and hit information from the KLM. Electrons are identified using the likelihood ratio $\mathcal{P}_e = L_e / (L_e + L_\pi)$, where L_i is the PID likelihood for the particle type i . Charged tracks satisfying $\mathcal{P}_e > 0.9$ are accepted as electron candidates. Energy losses due to bremsstrahlung are recovered by adding the momenta of photons to that of the electron's momentum if they lie within 0.05 rad of the initial track direction. Tracks are selected as muon candidates if they satisfy $\mathcal{P}_\mu > 0.9$, where \mathcal{P}_μ is the analogous likelihood ratio for muons. For electron (muon) candidates, we require the momentum to be greater than 0.4 (0.7) GeV/ c so that they can reach the ECL (KLM), which improves the PID. These requirements select electron (muon) candidates with an efficiency greater than 86% (92%), while rejecting more than 99% of pions. Charged kaons are distinguished from pions (and vice versa) by requiring the likelihood ratio $\mathcal{P}_K = L_K / (L_K + L_\pi)$ to be greater than 0.1 (smaller than 0.9). This requirement retains more than 99% of kaons (pions), while reducing the misidentification rate of pions (kaons) by 94% (86%).

The K_S^0 candidates are reconstructed with an efficiency of 74% from two oppositely charged tracks (treated as pions) by applying selection criteria on their invariant mass and vertex-fit quality [16]. We reconstruct π^0 candidates

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TABLE I. Systematic uncertainties in R_{K^*} for different q^2 regions.

q^2 (GeV $^2/c^4$)	Signal shape	Peaking backgrounds	Charmonium backgrounds	e, μ efficiency	Classifier	MC size	Total
All modes							
[0.045, 1.1]	0.017	0.026	0.001	0.027	0.030	0.006	0.051
[1.1, 6]	0.020	0.070	0.013	0.065	0.038	0.008	0.106
[0.1, 8]	0.023	0.054	0.051	0.058	0.024	0.005	0.101
[15, 19]	0.019	0.003	0.003	0.090	0.047	0.012	0.104
[0.045, 19]	0.025	0.031	0.023	0.061	0.026	0.004	0.080
B^0 modes							
[0.045, 1.1]	0.010	0.049	0.001	0.024	0.112	0.007	0.126
[1.1, 6]	0.014	0.070	0.012	0.082	0.062	0.010	0.126
[0.1, 8]	0.013	0.033	0.018	0.058	0.049	0.006	0.086
[15, 19]	0.006	0.007	0.001	0.091	0.032	0.013	0.098
[0.045, 19]	0.012	0.031	0.021	0.073	0.033	0.006	0.090
B^+ modes							
[0.045, 1.1]	0.011	0.006	0.000	0.033	0.060	0.013	0.071
[1.1, 6]	0.017	0.086	0.009	0.045	0.092	0.010	0.135
[0.1, 8]	0.013	0.048	0.107	0.060	0.023	0.010	0.135
[15, 19]	0.007	0.008	0.002	0.089	0.052	0.028	0.108
[0.045, 19]	0.011	0.025	0.023	0.044	0.015	0.005	0.059

from photon pairs, where each photon is required to have an energy greater than 30 MeV. Furthermore, the invariant mass of the photon pair is required to be in the [115, 153] MeV/ c^2 range, which corresponds to approximately ± 4 times the π^0 mass resolution. We form K^* candidates from $K^+\pi^-$, $K^+\pi^0$, and $K_S^0\pi^+$ combinations with an invariant mass lying in the range [0.6, 1.4] GeV/ c^2 . We also apply a requirement on the K^* vertex-fit quality to reduce background. The K^* candidates are combined with two oppositely charged leptons to form B meson candidates.

The dominant background is due to incorrect combinations of tracks. This combinatorial background is suppressed by applying requirements on the beam-energy-constrained mass, $M_{bc} = \sqrt{E_{\text{beam}}^2/c^4 - |\vec{p}_B|^2/c^2}$, and the energy difference, $\Delta E = E_B - E_{\text{beam}}$, where E_{beam} is the beam energy, and E_B and \vec{p}_B are the energy and momentum, respectively, of the reconstructed B -meson candidate. All of these quantities are calculated in the center-of-mass frame. Correctly reconstructed signal events peak near the B -meson mass [17] in M_{bc} and at zero in ΔE . The ΔE distribution is wider for electron modes, as some bremsstrahlung photons are not reconstructed. We retain B -decay candidates that satisfy $5.22 < M_{bc} < 5.30$ GeV/ c^2 and $-0.10(-0.05) < \Delta E < 0.05$ GeV in the electron (muon) mode.

Large irreducible background contributions arise in the ΔE and M_{bc} distributions from the decays $B \rightarrow J/\psi K^*$ and $B \rightarrow \psi(2S)K^*$, where the charmonium states further decay into two leptons. We veto these backgrounds by rejecting candidates with $-0.25(-0.15) < M_{\ell\ell} - m_{J/\psi} < 0.08$ GeV/ c^2 and $-0.20(-0.10) < M_{\ell\ell} - m_{\psi(2S)} < 0.08$ GeV/ c^2 for the electron (muon) channel. In the electron case, the veto is

applied twice: before and after the bremsstrahlung-recovery treatment. This is done to prevent charmonium backgrounds from shifting out of the veto region when an incorrect photon is combined with the electron.

A multivariate analysis technique is developed to suppress combinatorial background. A dedicated neural-network classifier is trained with MC samples to identify each particle type used in the decay chain, from which a signal probability is calculated for each candidate. The neural networks dedicated to identifying the particles e^\pm , μ^\pm , K^\pm , K_S^0 , π^0 , and π^\pm are identical to those used in Ref. [18]. The networks for K^* selection use input variables related to the K^* -decay products. Most of the discrimination of the K^* selection comes from vertex-fit information, decay-product neural-network outputs, and momenta of the decay products. The final signal selection is performed with a dedicated neural network for each B -decay channel. The inputs to these B -decay classifiers include event-shape variables (modified Fox-Wolfman moments [19]), vertex-fit information, and kinematic variables, such as the reconstructed mass of the K^* and the angle between its momentum vector and the initial direction extracted from the vertex fit. The most discriminating of these input variables are ΔE , the reconstructed K^* mass, the product of the network outputs for all final state particles, and the distance between the two leptons projected onto the z axis as derived from a fit to the B -decay vertex. The final selection requirement on the B -decay classifier output value is optimized by maximizing a figure of merit, $n_s/\sqrt{n_s + n_b}$, where n_s (n_b) is the expected number of signal (background) events calculated from MC samples in the region $M_{bc} > 5.27$ GeV/ c^2 .

Less than 2% of events contain multiple B candidates. In such cases, we choose the one with the highest signal probability, estimated from the neural-network output values. This procedure selects the correct B candidate with an efficiency between 82% and 92%, depending on the channel.

We extract signal yields in various regions of the squared dilepton invariant mass q^2 , using an unbinned extended maximum-likelihood fit to the M_{bc} distribution of $B \rightarrow K^* \ell^+ \ell^-$ candidates. We consider four different components in the likelihood fit. First, a signal component is parametrized by a Crystal Ball function [20], with the shape parameters determined from $B \rightarrow J/\psi K^*$ candidates that fail the J/ψ veto in data. Second, a combinatorial background component is described by an ARGUS function [21]. Third, there is a component from events in which charmonium decays pass the veto when they are misreconstructed; for example, when the bremsstrahlung recovery fails to detect photons. This background component is studied using an MC sample with 100 times higher statistics than that expected from the charmonium decays in the data sample. The shape of the charmonium background is determined via kernel density estimation (KDE) [22]. Finally, a peaking background component in which two particles have been assigned the wrong hypothesis, such as $B \rightarrow K^* \pi^+ \pi^-$, $B \rightarrow KK\pi$, or $B \rightarrow D^* \pi$, is studied using MC samples, with the shape parametrized via KDE. As the expected yields of charmonium and double-misidentification backgrounds are small, their yields are fixed in the fit to values obtained from MC simulation.

The determination of signal efficiency is verified by measuring the well-known $B \rightarrow J/\psi K^*$ branching fractions, which are found to be compatible with world averages [17]. As a cross-check, the LFU ratio of $\mathcal{B}[B \rightarrow J/\psi(\rightarrow \mu^+ \mu^-) K^*]$ and $\mathcal{B}[B \rightarrow J/\psi(\rightarrow e^+ e^-) K^*]$ is measured to be $1.015 \pm 0.025 \pm 0.038$, where the first error is statistical and the second due to uncertainty in data-MC corrections for lepton identification. This cross-check neglects contributions from the $B \rightarrow K^* \ell \ell$ channel in the J/ψ control region.

The reconstruction procedure for this analysis is optimized for maximal statistical sensitivity to R_{K^*} , at the cost of systematic uncertainties due to the use of multivariate selections in particle identification. Systematic uncertainties arise from the determination of the signal yield and reconstruction efficiency. All considered systematic uncertainties for R_{K^*} are listed in Table I. The uncertainty in the signal yield is evaluated by propagating the uncertainties in all Crystal Ball shape parameters, including their correlations. The normalizations of peaking and charmonium backgrounds are varied in the fit by $\pm 50\%$ and $\pm 25\%$; these ranges are chosen according to the maximum uncertainties in the respective branching fractions. The resulting signal-yield deviations are included as part of the systematic uncertainty. We correct for differences in the

lepton identification efficiency between data and MC by using the results obtained from a control sample of two-photon $e^+ e^- \rightarrow e^+ e^- e^+ e^- / e^+ e^- \mu^+ \mu^-$ events. The input distributions used by the top-level classifiers are compared between data and simulation, and no significant differences are found. In order to estimate the resulting uncertainty, the ratio of $B \rightarrow J/\psi K^*$ branching fractions between data and MC is obtained in bins of the classifier output. The obtained ratio is propagated as classifier output-dependent weights to candidates in all fits to M_{bc} distributions, and changes in the resulting signal yields are taken as systematic uncertainties. The statistical uncertainty of this reweighting procedure is evaluated in simulations on signal MC samples, and this adds 1%–2% additional uncertainty. Further uncertainties arise from limited MC statistics. Effects due to migration of events between different q^2

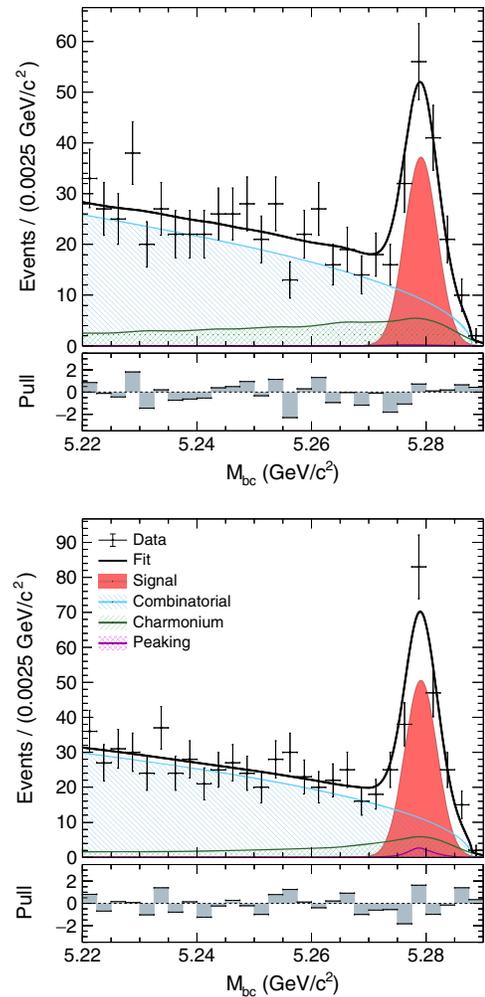


FIG. 1. Results of the combined B^+ and B^0 signal yield fit to the M_{bc} distributions for the electron (top) and muon (bottom) modes for $q^2 > 0.045 \text{ GeV}^2/c^4$. Combinatorial (dashed blue), signal (red filled), charmonium (dashed green), peaking (purple dotted), and total (solid) fit distributions are superimposed on data (points with error bars).

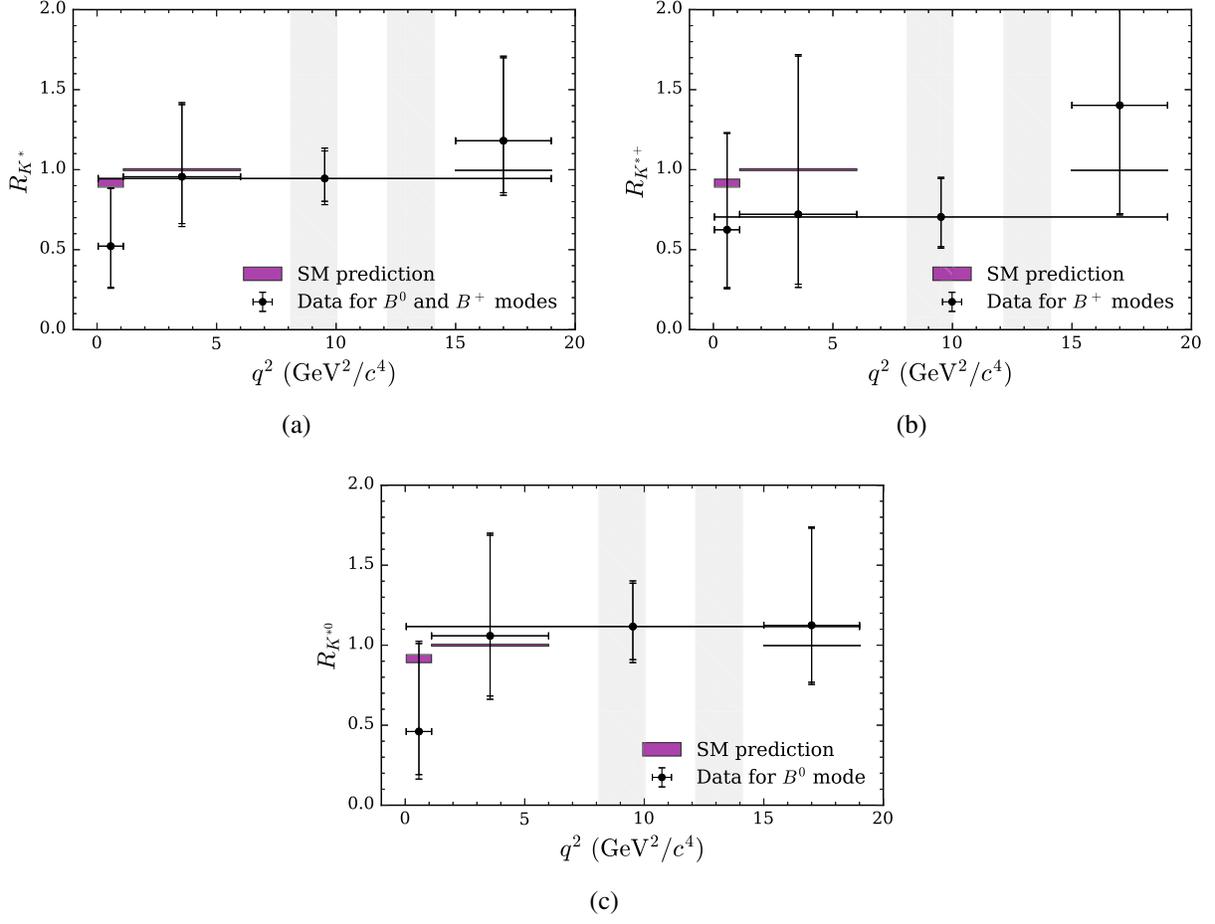


FIG. 2. Results for R_{K^*} (a), $R_{K^{*+}}$ (b), and $R_{K^{*0}}$ (c) compared to SM predictions from Refs. [26,27]. The separate vertical error bars indicate the statistical and total uncertainty. Shaded bands indicate the charmonium vetoes.

bins are studied using MC events and found to be negligible. In the case of results for the full region of $q^2 > 0.045 \text{ GeV}^2/c^4$, the different veto regions for the electron and muon channels need to be accounted for in the determination of reconstruction efficiency. This introduces model dependence to our signal simulation, which uses form factors from Ref. [23]. We estimate the systematic uncertainty due to this model dependence using different signal MC samples generated with form factors from QCD sum rules [24] and quark models [25]. The maximum difference in selection efficiency with respect to the nominal model, in each q^2 region, is taken as our estimate

for the size of this effect. This results, on average, in a difference of $0.4 \pm 2.4\%$ with a maximum of 6.5%, depending on the mode and q^2 region. As discussed in the beginning, this uncertainty only applies to the branching fractions, not to the LFU ratios. The systematic uncertainty for hadron identification and K^* selection is covered in the uncertainty for the top-level classifiers due to the multivariate selection approach. For the branching fraction measurements, additional uncertainties from tracking (0.35% per track) and the total number of $B\bar{B}$ events in data are taken into account. The dominant uncertainty originates from lepton identification, ranging

TABLE II. Results for R_{K^*} , $R_{K^{*0}}$, and $R_{K^{*+}}$. The first uncertainty is statistical and the second is systematic.

q^2 (GeV^2/c^4)	All modes	B^0 modes	B^+ modes
[0.045, 1.1]	$0.52^{+0.36}_{-0.26} \pm 0.05$	$0.46^{+0.55}_{-0.27} \pm 0.13$	$0.62^{+0.60}_{-0.36} \pm 0.07$
[1.1, 6]	$0.96^{+0.45}_{-0.29} \pm 0.11$	$1.06^{+0.63}_{-0.38} \pm 0.13$	$0.72^{+0.99}_{-0.44} \pm 0.14$
[0.1, 8]	$0.90^{+0.27}_{-0.21} \pm 0.10$	$0.86^{+0.33}_{-0.24} \pm 0.09$	$0.96^{+0.56}_{-0.35} \pm 0.13$
[15, 19]	$1.18^{+0.52}_{-0.32} \pm 0.10$	$1.12^{+0.61}_{-0.36} \pm 0.10$	$1.40^{+1.99}_{-0.68} \pm 0.11$
[0.045, 19]	$0.94^{+0.17}_{-0.14} \pm 0.08$	$1.12^{+0.27}_{-0.21} \pm 0.09$	$0.70^{+0.24}_{-0.19} \pm 0.06$

TABLE III. Results for the branching fractions in $[10^{-7}]$ in the corresponding q^2 range in GeV^2/c^4 . The first uncertainty is statistical and the second is systematic.

Mode	$q^2 \in [1.1, 6]$	$q^2 \in [0.1, 8]$	$q^2 \in [15, 19]$	$q^2 > 0.045$
$\mathcal{B}(B^0 \rightarrow K^{*0} e^+ e^-)$	$1.8^{+0.6}_{-0.6} \pm 0.2$	$3.7^{+0.9}_{-0.9} \pm 0.4$	$2.0^{+0.6}_{-0.5} \pm 0.2$	$9.2^{+1.6}_{-1.6} \pm 0.8$
$\mathcal{B}(B^0 \rightarrow K^{*0} \mu^+ \mu^-)$	$1.9^{+0.6}_{-0.5} \pm 0.3$	$3.2^{+0.8}_{-0.8} \pm 0.4$	$2.2^{+0.5}_{-0.4} \pm 0.2$	$10.3^{+1.3}_{-1.3} \pm 1.1$
$\mathcal{B}(B^+ \rightarrow K^{*+} e^+ e^-)$	$1.7^{+1.0}_{-1.0} \pm 0.2$	$4.6^{+1.6}_{-1.5} \pm 0.7$	$2.1^{+1.2}_{-1.0} \pm 0.2$	$14.1^{+3.1}_{-2.8} \pm 1.8$
$\mathcal{B}(B^+ \rightarrow K^{*+} \mu^+ \mu^-)$	$1.2^{+0.9}_{-0.7} \pm 0.2$	$4.4^{+1.6}_{-1.4} \pm 0.5$	$2.9^{+1.0}_{-0.8} \pm 0.3$	$9.9^{+2.4}_{-2.3} \pm 1.1$

between 5% and 10% depending on the mode and q^2 region, as also here a more conservative estimation of uncertainty is performed to account for residual correlations with the top-level classifiers.

In the range $q^2 > 0.045 \text{ GeV}^2/c^4$ we find $103.0^{+13.4}_{-12.7}$ ($139.9^{+16.0}_{-15.4}$) events in the electron (muon) channels. Example fits are presented in Fig. 1. Using the fitted signal yields, we construct the LFU ratio R_{K^*} for all signal channels combined, as well as separate ratios for the B^0 and B^+ decays, $R_{K^{*0}}$ and $R_{K^{*+}}$. The results are shown in Table II and Fig. 2. Our measurement of $R_{K^{*+}}$ is the first ever performed. The branching fractions are calculated assuming equal production of B^+ and B^0 mesons and the results are presented in Table III.

In summary, all our results are consistent with the SM expectations [26,27]. Global analyses of measurements of $b \rightarrow s\ell^+\ell^-$ mediated decays prefer NP models that predict R_{K^*} values smaller than unity [27]. The largest deviation along this direction is observed in the lowest q^2 bin, in the same region where LHCb reports a measurement deviating from the SM [4]. Our separate results for the B -meson isospin partners $R_{K^{*+}}$ and $R_{K^{*0}}$ are statistically compatible, which would also be expected if contributions from NP arise from the $b \rightarrow s\ell^+\ell^-$ transition. The Belle II experiment [28,29] is expected to record a 50 times larger data sample than Belle, providing ideal conditions to precisely study lepton flavor universality in these modes.

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