

Highly efficient energy and mass transfer in bcc metals by supersonic 2-crowdions

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Abstract

During irradiation, bombardment with energetic particles, or plasma treatment, structural transformations occur in materials, in which point defects play a very important role. Highly mobile crowdions contribute to the transfer of mass and energy in the crystal lattice. Static and slowly moving crowdions are well studied, in contrast to crowdions moving at a speed exceeding the speed of sound. Here, for the first time, dynamics of supersonic N -crowdions ($N = 1, 2$) is investigated in bcc metals (tungsten and vanadium) with the help of molecular dynamics simulations. N -crowdions are excited by imparting sufficiently high initial velocities to N neighboring atoms located in the same close-packed atomic row along this row. Both supersonic 1- and 2-crowdions carry one interstitial atom each. Modeling shows that much less energy is required to excite a 2-crowdion compared to a 1-crowdion. Energy dissipation for a 2-crowdion is much slower than for a 1-crowdion suggesting that the supersonic 2-crowdion is an efficient mass transfer mechanism in bcc metals. The distance traveled by the supersonic 1- and 2-crowdions in W is much greater than in V. The supersonic crowdion in W transforms into a moving subsonic crowdion, and in V it transforms into a standing subsonic crowdion carrying a localized high-amplitude oscillation mode. These differences can be explained by the features of interatomic interactions in W and V.

Keywords: lattice defects, subsonic crowdion, supersonic crowdion, mass transfer, molecular dynamics simulations

I. INTRODUCTION

Extreme influences, such as laser treatment¹, severe plastic deformation², ultrafast loading^{3,4}, irradiation^{5–10}, plasma treatment¹¹, etc., cause irreversible changes in the crystal structure and lead to the transition of the lattice to a non-equilibrium state. In these processes, the atoms strongly deviate from their equilibrium lattice sites, and the nonlinear nature of the interatomic bonds begins to play a significant role. Such extreme impacts cause the appearance of an abnormally high concentration of point defects, called Frenkel pairs (vacancy and interstitial).

An interstitial atom can exist in many configurations, including the crowdion configuration, when it is located in a close-packed atomic row^{12–14}. The migration ability of crowdions is much greater as compared to vacancies^{2,15,16}, which makes them efficient in mass transfer in materials. The high migration ability of crowdions leads to their rapid annihilation, hindering experimental analysis of their structure and movement¹⁷. Therefore, computer simulation methods are widely used, including methods of molecular dynamics^{18–24}, Monte Carlo^{25,26}, first-principles^{27,28} and multiscale modelling^{13,29–31}.

If an atom in a close-packed row receives a large enough momentum along the row, it can replace a neighboring atom and initiate a replacement collision sequence (RCS) produced by a moving crowdion³². In this case, a Frenkel pair is formed, and the moving interstitial atom transfers mass. If the initial energy is below the threshold displacement energy, then a focuson sequence (FS) is realized³². After the focuson relaxation, the ideal crystal structure is restored.

Most of the studies analyze static or slowly moving crowdions and the elastic stress fields produced by them^{27,31,33,34}. However, the interstitials produced under the above-mentioned extreme influences can propagate along close-packed atomic rows with the speed exceeding the speed of longitudinal sound. The supersonic motion of crowdions was studied in the two-dimensional triangular lattices^{35–37}, fcc lattices^{28,38,39} and intermetallic compound Ni₃Al⁴⁰. For bcc metals, as far as we know, the supersonic motion of crowdions has not yet been studied.

Metals with bcc lattice, such as tungsten and vanadium, are of particular interest due to the fact that they are planned to be widely used in the International Thermonuclear Experimental Reactor (ITER)⁴¹. Tungsten is considered as divertor material^{42,43} and vanadium

alloys are promising materials for the first-wall and breeding blanket due to their outstanding thermal properties^{44,45}. This is the reason for active studies on the defects in W^{7-10,18,46-50} and V^{44,51-54}. In order to demonstrate the difference between 1- and 2-crowdions, we provide two Supplemental files named 1_crowdion.gif and 2_crowdion.gif. Atoms are colored according to their kinetic energy. It can be seen that in the 2-crowdion two atoms move simultaneously at a high speed, while in the 1-crowdion one atom has a high speed. It is well-known that atomic collisions are focusing only if the collision velocity is below a critical value. The 2-crowdion with the fastest focusing speed carries twice as much energy as the 1-crowdion and therefore travels a longer distance.

Along with the supersonic 1-crowdions, the mass transfer by the supersonic N -crowdions, which were excited by giving an initial velocity to N neighboring atoms along the chosen close-packed atomic row, has been studied^{35,38,39}. It turned out that supersonic N -crowdions can be excited with a lower energy and travel much longer distances than supersonic 1-crowdions. This is related to the fact that motion of supersonic N -crowdions for $N > 1$ is more self-focusing than that for $N = 1$ ^{38,55}.

Atomic collisions in a close-packed row with a velocity above a threshold level are defocusing, i.e., any small deviation of the velocity vector from the direction of the row will increase exponentially from atom to atom^{38,55}. Collisions with speeds below the threshold are self-focusing, and the direction of the velocity vector in successive collisions will exponentially approach the direction of the atomic row. It follows from this that there is an upper limit on the energy that can be imparted to an atom to excite a supersonic 1-crowdion. This energy can be increased without increasing the speed of atoms, if not one, but N neighboring atoms are excited, creating a supersonic N -crowdion. Having more energy, an N -crowdion with $N > 1$ propagates to a longer distance than a 1-crowdion.

Simultaneous excitation of two atoms in an atomic row can be easily achieved by bombardment of crystal surface by biatomic molecules³⁹. This fact is important for such applications as deposition, sputtering and ion implantation. We do not know whether supersonic 2-crowdions are formed in the collision cascades in metals under irradiation. Both supersonic 1- and 2-crowdions carry single interstitial and when they transform to subsonic crowdions they become indistinguishable.

The present work is aimed to study the energy and mass transfer in bcc metals (tungsten and vanadium) via supersonic N -crowdions by means of molecular dynamics simulations.

The emphasis is mainly on the physics of the observed process. The temperature effect is analyzed, while the influence of various imperfections (impurity atoms, point or extended defects, strain fields, etc.) is not considered here.

II. METHODOLOGY

The molecular dynamics method is ideally suited for the analysis of mass transfer by supersonic crowdions, taking into account the small spatial and temporal scales of the phenomenon under study. This method has established itself as a powerful tool in modern materials science with numerous applications to materials under extreme conditions, including the analysis of defect dynamics in various crystal lattices, both model and real^{51,56–62}, nonlinear dynamics of the crystal lattice^{63–65}, and exposure to radiation^{57,66}.

The molecular dynamics method is based on phenomenological interatomic potentials, which should be chosen taking into account the specific problem being solved. In materials under high-energy impacts, atoms collide with high velocities, and at short interatomic distances the repulsive part of the potentials becomes important. For this purpose, many-body interatomic potentials have been developed that describe well the behavior of metals under extreme conditions. In particular, the embedded atom method potentials have been adapted for bcc tungsten⁶⁷ and vanadium⁵², which are widely used in fusion and fission reactors. Both the potentials are of Finnis-Sinclair type and are fitted to both the experimental and first principles calculation data. The total energy E_i of the i -th atom is given by:

$$E_i = F_\alpha \left(\sum_{j \neq i} \rho_{\alpha\beta}(r_{ij}) \right) + \frac{1}{2} \sum_{j \neq i} \phi_{\alpha\beta}(r_{ij}), \quad (1)$$

where $\rho_{\alpha\beta}$ refers to the electron density contributed by a neighboring j -th atom of element β at the site of i -th atom of element α . ρ is a functional specific to the elements of both i -th and j -th atoms, so that different elements can contribute differently to the total electron density at an atomic site depending on the element at this atomic site. These potentials are incorporated into the Large-scale Atomic/Molecular Massively Parallel Simulator (LAMMPS), which is used for molecular dynamics simulations.

The Cartesian coordinate axes are chosen so that the x axis is oriented along the $\langle 111 \rangle$ close-packed crystallographic direction. The translational cell has the shape of a parallelepiped and contains 8 atoms. The equilibrium bcc lattice parameters are $a_0 = 3.14 \text{ \AA}$ for

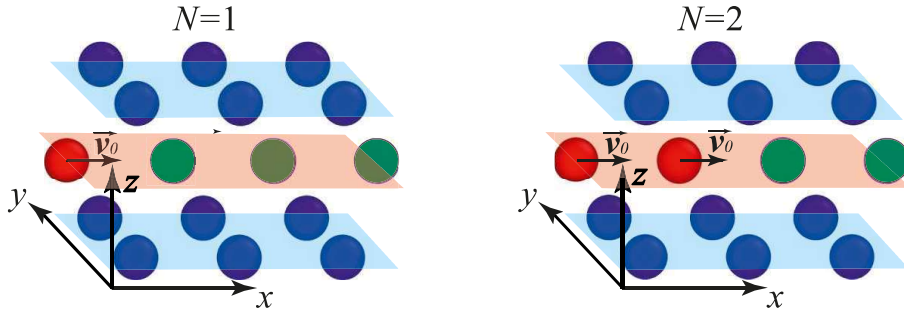


Figure 1. Illustration of the initial conditions for excitation of 1-crowdion (left panel) and 2-crowdion (right panel) by imposing initial velocities to the selected atoms along the $\langle 111 \rangle$ close-packed atomic row in bcc lattice. Only part of the computation cell is shown. The initial velocity v_0 along the x -axis is given to the atoms colored in red. Atoms colored in green are in the close-packed row, where the soliton/crowdion propagates. All other atoms are colored in blue.

W and $a_0 = 3.03 \text{ \AA}$ for V. The interatomic distance is $h = a_0\sqrt{3}/2$. One has $h = 2.72 \text{ \AA}$ for W and $h = 2.62 \text{ \AA}$ for V. The computational cells of W and V contain 82944 atoms and are of the sizes of $391.58 \times 61.53 \times 53.29 \text{ \AA}$ and $377.87 \times 59.38 \times 51.42 \text{ \AA}$, respectively. All molecular dynamics simulations are performed at zero initial temperature $T=0 \text{ K}$ using the NVE (constant number of atoms, volume, and energy) thermodynamic ensemble. The equations of motion are integrated using the Verlet integration scheme with the time step of 0.5 fs .

Excitation of 1- or 2-crowdions is performed by setting an initial directed momentum along the $\langle 111 \rangle$ close-packed direction to one or two neighboring atoms, respectively, according to the scheme illustrated in Fig. 1. The atoms to which the initial momentum is transferred are colored in red. All other atoms in the computational cell have zero initial velocities. Initial displacements of all atoms are equal to zero.

The kinetic energy that is imparted to the crystal at $t = 0$ is

$$T_0 = N \frac{mv_0^2}{2}, \quad (2)$$

where $N = 1$ or 2 is the number of excited atoms, m is the atom mass, v_0 is the initial velocity of the excited atom. In the present study, $m = 183.84 \text{ u}$ for W and $m = 50.941 \text{ u}$ for V.

III. NUMERICAL RESULTS

If the energy of the initial excitation is insufficient to overcome the potential barrier, then the Frenkel pair is not formed and the compressive soliton (focuson) propagates. This localized excitation only transfers energy, but not a mass. Gradually, the energy of the initial excitation dissipates in the lattice, and all atoms return to their equilibrium lattice positions. Usually, the threshold level of an atomic displacement corresponds to a half of the interatomic distance, $h/2 = a_0\sqrt{3}/4$. When the displacement of the excited atom exceeds $h/2$, it does not return to its original equilibrium position, but moves to the next one. This corresponds to crowdion motion, i.e., wave propagation with relay-race motion of interstitial atom in a close-packed atomic rows. Note that both supersonic 1- and 2-crowdions transfer the mass of one interstitial atom and some energy.

In the following sections, we present the results of excitation of focusons or supersonic 1- and 2-crowdions in bcc W and V. Atomic displacements, radiation of energy and crowdion path lengths are analyzed.

A. 1-crowdion

An excitation of one atom in W and V lattices with relatively low initial velocity results in a formation of localized compressive soliton also called focuson. The soliton propagation is illustrated in Figs. 2(a,c) for W and in Figs. 2(b,d) for V, by showing the normalized atomic displacements in the close-packed row, where the soliton moves. When the initial energy is relatively low (top row in Fig. 2), the maximal displacement of atoms is approximately $\Delta x/h \approx 0.5$, and the atoms move back into their initial equilibrium lattice sites. The Frenkel pair is not formed in this case. The soliton moves with supersonic velocity and intensively dissipates its energy into the lattice via phonons. For this reason, the soliton stops after a while, and the traveled distance is rather short. It should be noted that the dynamics of solitons in W and V is noticeably different. Comparison of Figs. 2 (a) and (b) reveals that in V, the atoms return to their equilibrium positions faster, while the atoms in W stay longer at $\Delta x/h \approx 0.5$, which corresponds to the top of the potential barrier. The reason for this difference in the dynamics of solitons in two metals will be explained below.

If the initial velocity is slightly below the threshold level, that is $v_0 = 110 \text{ \AA}/\text{ps}$

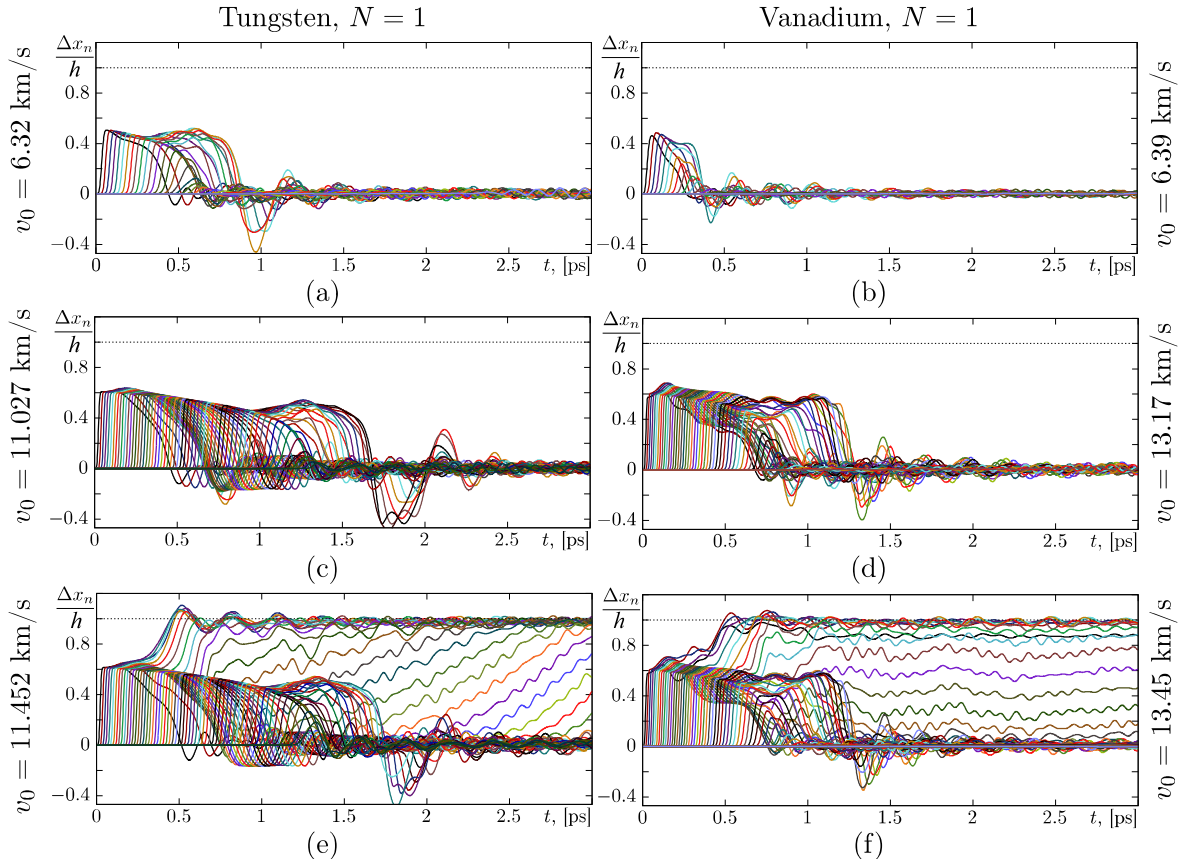


Figure 2. (Color online) The relative atomic displacements $\Delta x/h$ as functions of time illustrating propagation of 1-soliton (a)-(d) and 1-crowdion (e)-(f) in W (left column) and V (right column) at different initial velocities v_0 (kinetic energy T_0): (a) 6.32 km/s (38.9 eV), (b) 6.39 km/s (10.8 eV), (c) 11.0 km/s (119 eV), (d) 13.2 km/s (45.8 eV), (e) 11.5 km/s (128 eV), (f) 13.5 km/s (47.8 eV).

$=11.0$ km/s ($T_0 = 119$ eV) for W and $v_0 = 132 \text{ \AA/ps} = 13.2$ km/s ($T_0 = 45.8$ eV) for V, the distance travelled by the solitons becomes noticeably longer. However, the mass transfer does not occur. This is clearly illustrated in Figs. 2(c) and (d) for both bcc metals. In this case, atoms remain close to their saddle point between the two neighboring lattice sites, which is at $\Delta x/h = 0.5$, during relatively long time. It is worth noting that at a certain time atomic displacements can even exceed $h/2$, but atoms still move back into the initial lattice sites. However, this occurs only when the soliton energy is relatively low and the number of atoms with displacements greater than $h/2$ is relatively small.

An increase of the initial excitation velocity up to $v_0 = 11.5$ km/s for W and up to $v_0 = 13.5$ km/s for V results in a formation of a supersonic crowdion. The threshold

value of the excitation energy is $T_0 = 128$ eV for W and $T_0 = 47.8$ eV for V. As clearly seen in Figs. 2(e) and (f), atomic displacements exceed the saddle point (the potential barrier) and atoms start to move into the neighboring lattice sites at $\Delta x/h = 1$. Supersonic crowdion constantly radiates energy and slows down³⁶. When the crowdion energy becomes insufficient for supersonic propagation, it evolves into a subsonic crowdion. Supersonic crowdion is localized on one or two atoms, while subsonic crowdion is considerably wider (half a dozen to a dozen atoms) and it can carry the localized mode oscillating at frequency above the phonon spectrum of the lattice⁶⁸. In both W and V, the transition from super- to subsonic regime occurs at the time instant of about $t = 0.6$ ps, see Figs. 2(e) and (f). For $t > 0.6$ ps, propagation of subsonic crowdions is accompanied by the oscillation of atoms' trajectories at the frequency of 11 THz for W and 13 THz for V. Note that these frequencies are considerably higher than the maximal phonon frequency, which is 6.8 THz for W⁶⁹ and 8.1 THz for V⁵³. Since the vibrational mode localized on subsonic crowdions does not resonate with phonons and does not lose energy to excite them, it has a very long lifetime⁶⁸. The subsonic crowdion in W propagates from left to right, moving atoms from their initial positions into neighboring lattice sites, Fig. 2(e); while in V the subsonic crowdion does not move as demonstrated in Fig. 2(f), since the trajectories of the atoms remain parallel to the abscissa, showing the vibrations mentioned above. In the subsonic regime of motion crowdion in W transfers to the adjacent sites about 5 atoms in 1 ps. The latter means that the propagation velocity is of about $5h/\text{ps} = 13.6 \text{ \AA}/\text{ps} = 1.36 \text{ km/s}$. The velocity of sound in W is 5.2 km/s.

It can be concluded that the threshold values of the initial velocity v_0 , when the external excitation creates a supersonic 1-crowdion, are $v_0 \approx 11.5 \text{ km/s}$ ($T_0 = 128$ eV) for W and $v_0 \approx 13.5 \text{ km/s}$ ($T_0 = 47.8$ eV) for V. Deceleration of a supersonic crowdion produces a moving subsonic crowdion in W and standing subsonic crowdion in V. Subsonic crowdions, produced by slowing down supersonic crowdions, carry a localized vibrational mode with a frequency above the phonon spectrum⁶⁸.

B. 2-crowdion

A focuson or supersonic 2-crowdion is excited by setting initial velocities v_0 for two neighboring atoms in a close-packed atomic row, as shown in Fig. 1(b). If v_0 is below a

threshold value, a compressive soliton (focuson) is excited. Examples are given in Figs. 3(a) and (b) by applying $v_0 = 3.16$ km/s ($T_0 = 19.5$ eV) for W and $v_0 = 4.46$ km/s ($T_0 = 10.5$ eV) for V, respectively. A few atoms have a maximum displacement greater than $\Delta x/h = 0.5$, but this is not enough to create a Frenkel pair. After the energy transferred to the crystal is dissipated through the lattice, all atoms return to their original lattice sites. The atomic displacement curves have a specific 'two-step' shape stipulated by the excitation of 2 adjacent atoms.

An increase of the initial velocity up to $v_0 = 3.61$ km/s ($T_0 = 25.4$ eV) for W and $v_0 = 4.91$ km/s ($T_0 = 12.7$ eV) for V results in an overcoming of the potential barrier and in the formation of a supersonic 2-crowdion. This case is represented in Figs. 3(c) and (d) for W and V, respectively. It is seen that the atoms shift in two steps by $\Delta x/h \approx 0.75$ and thereafter slowly move towards adjacent lattice sites. At the same time, the supersonic stage in these cases is rather short; it ends approximately at $t = 0.5$ ps for both metals. For $t > 0.5$ ps energy of the crowdion becomes lower than a certain threshold level, and the supersonic crowdion transforms into a subsonic one. In W the subsonic crowdion continues its motion from the left to the right bearing a localized vibrational mode of relatively small amplitude. In V the subsonic crowdion does not move, since the curves $\Delta x_n(t)$ are parallel to the time axis, see Fig. 3(d). These curves show oscillations at a relatively large amplitude. The frequency of these oscillations can be estimated as 14 THz, which is above the upper edge of the phonon spectrum of V (8.1 THz). This explains why the oscillations decay very slowly: they do not resonate with phonons and do not waste energy on their excitation.

Supersonic 2-crowdions propagating longer distances can be seen in Figs. 3(e) and (f). They were excited in W and V with $v_0 = 5.83$ km/s ($T_0 = 66.2$ eV) and $v_0 = 6.39$ km/s ($T_0 = 21.6$ eV), respectively. In this case, the atoms in two steps move to the adjacent lattice sites at $\Delta x_n/h = 1.0$. Let the time interval between the neighboring $\Delta x_n/h$ curves is Δt . Then the crowdion speed is $h/\Delta t$. The sound velocity in W, as mentioned above, is $52 \text{ \AA}/\text{ps}$. For this velocity $\Delta t = 0.052$ ps. As can be seen in Fig. 3(e), the supersonic stage of crowdion propagation in W is relatively long and lasts till 1.5 ps. Similar calculations for V give the supersonic regime of motion till 0.5 ps.

Comparison of Figs. 3(e) and (f) reveals that in W the transition from supersonic to subsonic propagation is smooth, while it is abrupt in V. This explains why the just born subsonic crowdion moves in W, but not in V, as well as why the oscillation mode localized

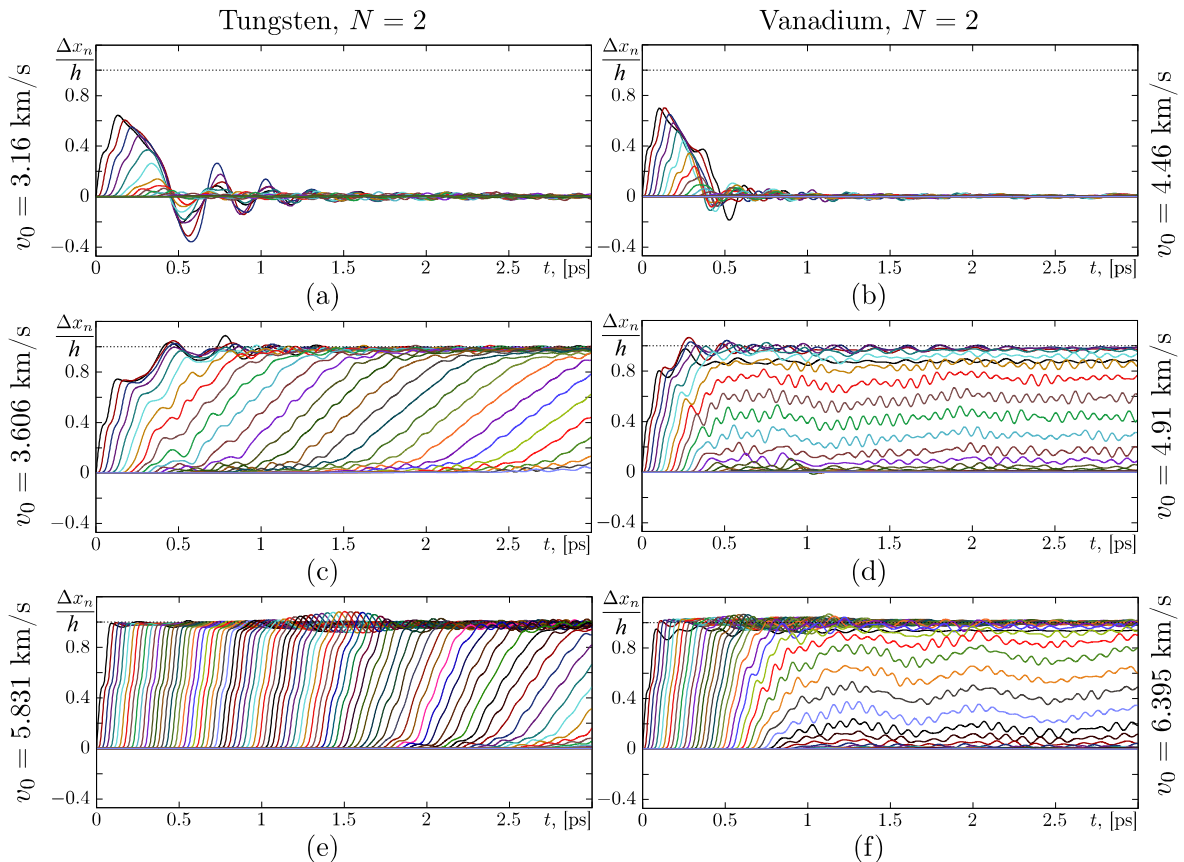


Figure 3. (Color online) The relative atomic displacements $\Delta x/h$ as functions of time illustrating propagation of 2-soliton (a)-(b) and 2-crowdion (c)-(f) in W (left column) and V (right column) at different velocities v_0 (kinetic energy T_0): (a) 3.16 km/s (19.5 eV), (b) 4.46 km/s (10.5 eV), (c) 3.61 km/s (25.4 eV), (d) 4.91 km/s (12.7 eV), (e) 5.83 km/s (66.2 eV), (f) 6.39 km/s (21.6 eV).

on subsonic crowdion in V has much higher amplitude than in W. A smooth transition from supersonic to subsonic motion in W ensures the transfer of momentum of the directed motion to the atoms moving along the close-packed row in the subsonic regime. A sharp transition in V leads to the transfer of the energy of the directed motion of the supersonic crowdion to a large-amplitude vibrational mode localized on the subsonic crowdion.

An excitation of supersonic 2-crowdion needs noticeably lower initial energy as compared to supersonic 1-crowdion. Recall that the minimal energy required for excitation of a supersonic 1-crowdion is 128 eV in W and 47.8 eV in V. On the other hand, for excitation of supersonic 2-crowdions it is sufficient to spend 25.4 eV in W and 12.7 eV in V. The energy gain is 5 times for W and 3.8 times for V. Since both the supersonic 1- and 2-crowdions

each carry one interstitial atom, it can be concluded that the supersonic 2-crowdion in bcc crystals is a much more efficient mass transfer mechanism in comparison with the supersonic 1-crowdion.

This effect is described here for the first time for bcc metals. Despite the fact that similar results were obtained earlier for the two-dimensional triangular lattice modeled with the pair-wise Morse interatomic potential³⁸. In particular, it was established that the excitation energies of supersonic 2-crowdion are two times less than that for supersonic 1-crowdion. Note that similar results have been obtained in Ref.³⁶, where the authors have found that excitation of 2×1 supersonic crowdion cluster costs 2.4 and 3 times more energy than that for 2×2 and 2×4 supersonic crowdion clusters, respectively.

C. Evolution of crowdion energy

In Fig. 4, temporal evolution of the kinetic energy $T_n(t)$ of the n -th atom in the close-packed row in W is plotted for (a) 1-crowdion and (b) 2-crowdion. The crowdions were excited with $v_0 = 11.5$ km/s ($T_0 = 128$ eV) in (a) and $v_0 = 5.83$ km/s ($T_0 = 66.2$ eV) in (b). The maximal value of the kinetic energy of atoms can be regarded as the maximal kinetic energy of crowdion. For 1-crowdion, the maxima of the energies are well fitted by a cubic polynomial with inaccuracy less than 1%. In 2-crowdion, two atoms simultaneously have a high kinetic energy. The envelop function for the maximal kinetic energy of atoms decreases in time for the 2-crowdion almost linearly (the envelopes are shown in Fig. 4 as solid red lines).

The result presented in Fig. 4 demonstrates that the energy of the 1-crowdion decreases with time faster than the energy of the 2-crowdion. This can be explained by the fact that collisions of atoms in a 1-crowdion occur at higher energies, which leads to a greater energy dissipation by the lattice. In a 2-crowdion, the energy is shared between two atoms, and the collisions of the atoms occur at a lower energy, resulting in a slower loss of energy by the crowdion.

The envelop functions of the maximal kinetic energy $T(t)$ for (a) W and (b) V are shown in Fig. 5. Initial parameters are specified for each curve in the legends. Curves 1 to 3 are for $N = 1$, while curves 4 and 5 are for $N = 2$. In particular, curves 1 in Fig. 5 correspond to the 1-solitons excited with the low initial energy, see Figs. 2(a) and (b). Curves 2 and 3 in Fig. 5

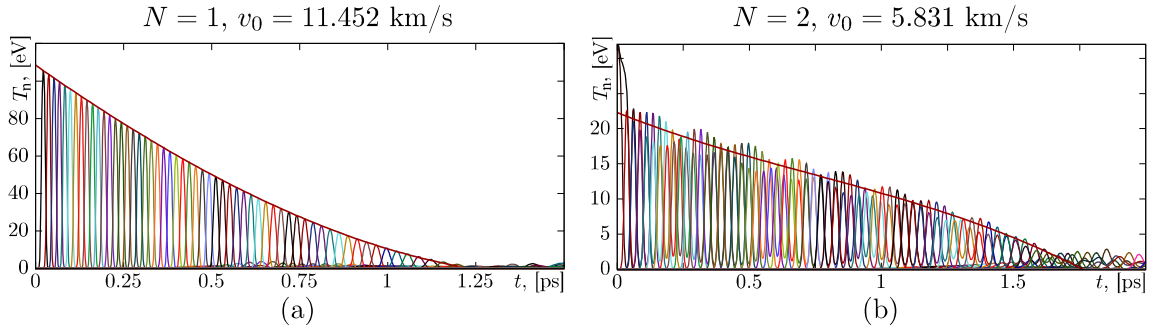


Figure 4. (Color online) Temporal evolution of the kinetic energy $T_n(t)$ of the n -th atom in the close-packed row in W for (a) $N = 1$, $v_0 = 11.5$ km/s ($T_0 = 128$ eV), and (b) $N = 2$, $v_0 = 5.83$ km/s ($T_0 = 66.2$ eV). The envelope lines are shown in red. In (a), it is a cubic polynomial, and in (b) the envelope is almost a linear function.

are for the 1-solitons excited with the sub- and over-threshold energies, see Figs. 2(c),(d) and (e),(f), respectively. Dependencies $T(t)$ for 2-crowdions are noticeably different from those for 1-crowdions. The energy evolution for 2-crowdion induced with the initial energy slightly above the threshold level is shown in Fig. 5 by the curves 4, see Figs. 3(c) and (d). The case of the long-lived 2-crowdion is illustrated in Fig. 5 by the curves 5, see Figs. 3(e) and (f).

As seen in Figs. 5(a) and (b) that curves 1 for 1-solitons in both bcc metals start at relatively low energy level and decay quickly. Curves 2 and 3 start at considerably higher energy level, and then they also decay quickly. Curves 4 for the 2-crowdion excited with the energy slightly above the threshold level have two maxima. The second maximum appears after the transition from the supersonic to subsonic crowdion. The slowly decaying curves 5 in Fig. 5 show $T(t)$ for the long-lived 2-crowdions. The energy level for these curves is relatively low.

Time derivatives of the maximal kinetic energy envelopes, dT/dt , characterizing the energy dissipation rate are depicted in Fig. 5 for W (c) and V (d). The energy loss for 2-crowdion is significantly lower than that for 1-crowdion. Moreover, the energy dissipation of 2-crowdion excited with the larger momentum (curves 5) is lower than that for 2-crowdion excited with smaller momentum (curves 4). Curve 5 in Fig. 5(c) is almost horizontal, showing that, as mentioned above, the maximum kinetic energy for a supersonic 2-crowdion in W decreases almost linearly with time.

D. Propagation of supersonic crowdions

Further an analysis of the distance L_s travelled by 1- and 2-crowdions during their supersonic motion as well as the duration of the supersonic stage t_s as functions of the initial velocity v_0 and the initial energy T_0 are presented in Fig. 6. It is clearly seen that in both bcc metals supersonic 2-crowdion covers larger distance and moves longer time as compared to supersonic 1-crowdion excited with the same initial velocity or energy. For comparison, a supersonic 2-crowdion induced in W with $T_0 \approx 70$ eV passes the distance of $L_s = 100$ Å in

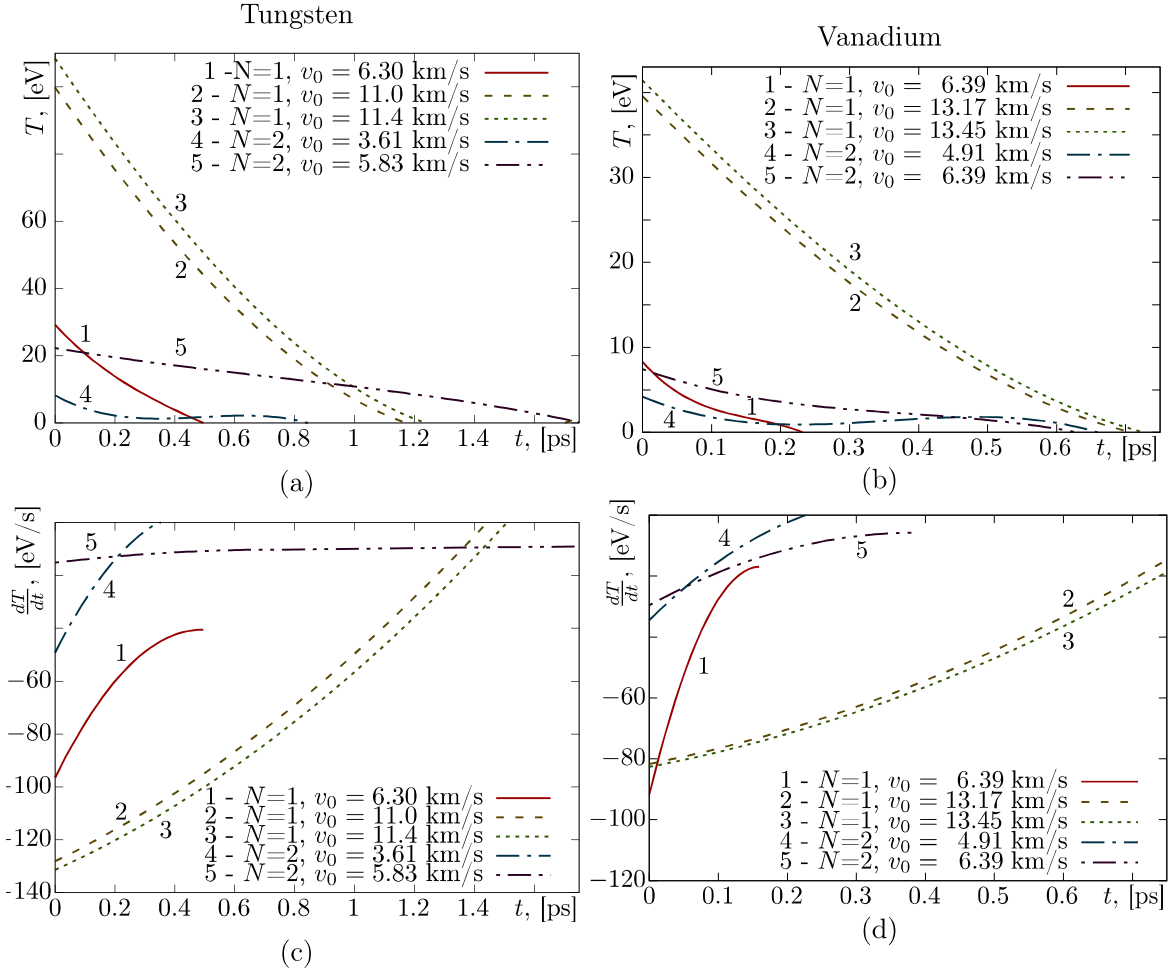


Figure 5. (Color online) (a,b) Envelop functions, $T(t)$, approximating evolution of the maximal kinetic energy of atoms; (c,d) the energy dissipation rate, dT/dt , of the solitons/crowdions as the function of time for W (c) and V (d). Initial parameters are specified for each curve in the corresponding legends.

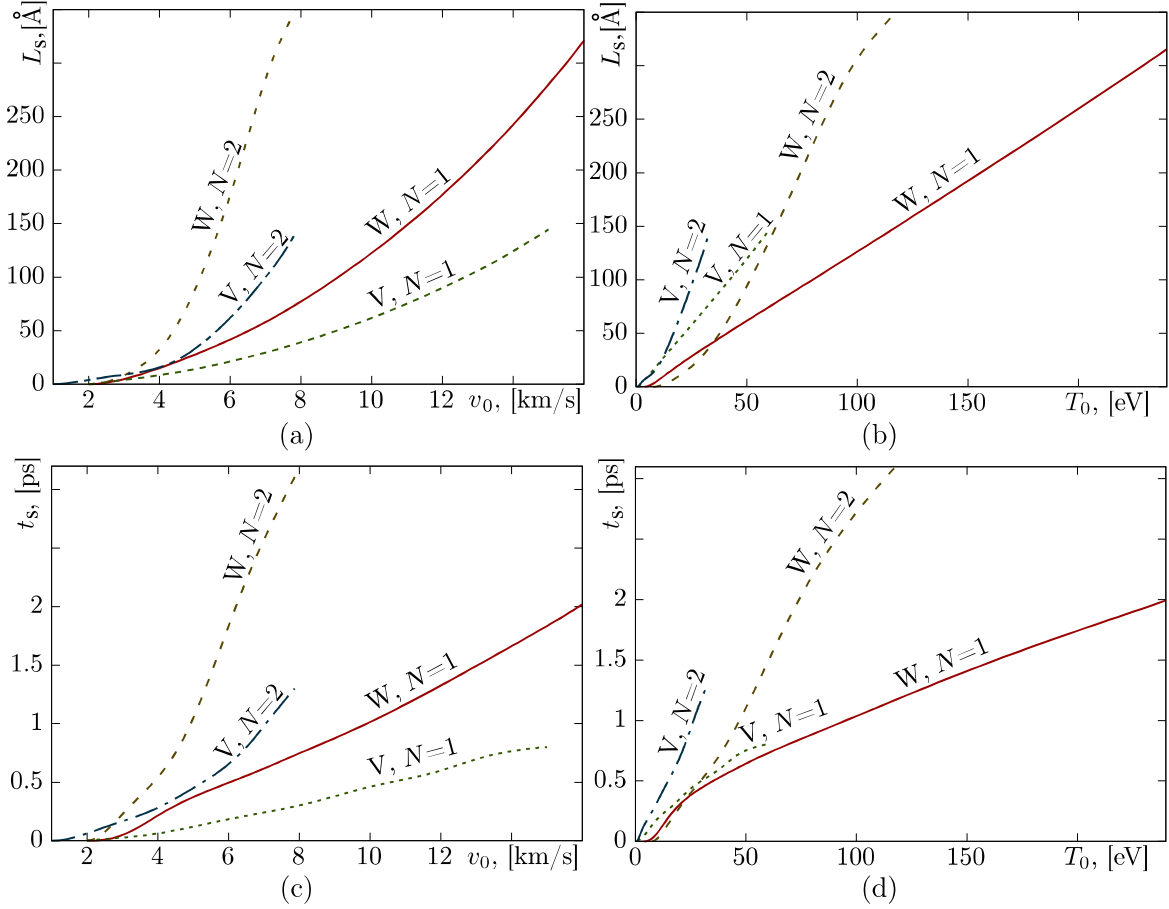


Figure 6. (Color online) (a,b) Propagation distance L_s and (c,d) propagation time t_s of 1- and 2-crowdions with the supersonic velocity in W and V as the functions of the initial velocity v_0 (a,c) and the initial energy T_0 (b,d). The metal and the type of crowdion are indicated in each curve.

$t_s \approx 2$ ps. A supersonic 1-crowdion travels the same distance in $t_s \approx 1.3$ ps being excited at a much higher energy of $T_0 \approx 155$ eV. It should be noted that the dependence $L_s(T_0)$ is almost linear for 1-crowdion and it increases much faster than for 2-crowdion in both studied bcc metals suggesting that 2-crowdions are more efficient at transferring mass. Interestingly, the distance and duration of supersonic propagation of both 1- and 2-crowdions are significantly longer in W than in V.

E. Comparison of interatomic potentials for W and V

It follows from the presented results that supersonic 1- and 2-crowdions propagate much longer distances and need for their excitation lower energies in W than in V. There is also

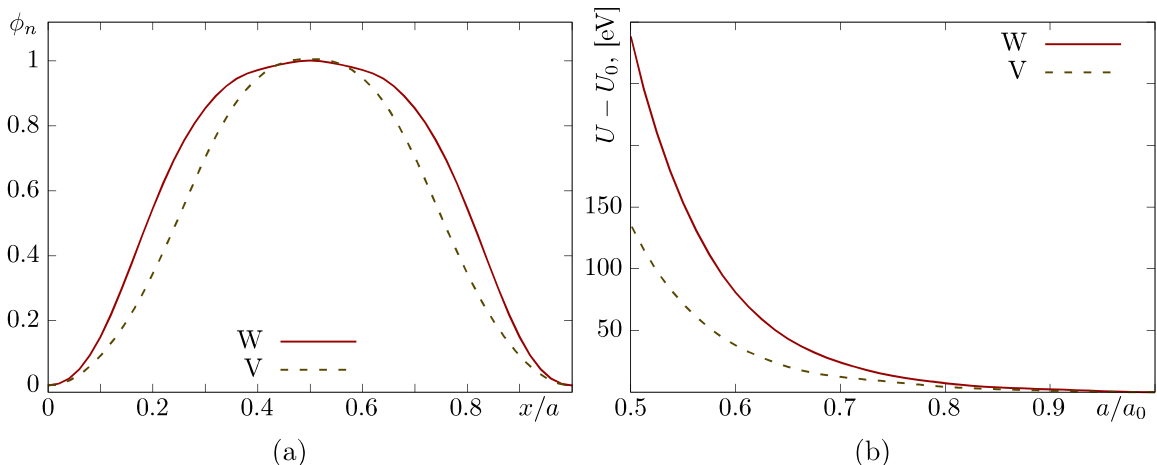


Figure 7. (Color online) (a) Normalized potential function, $\phi_n(x/h)$, defined by Eq. (3); (b) sublimation energy per atom U relative to its equilibrium value, U_0 , as the function of the bcc lattice parameter a normalized to its equilibrium value a_0 . Results for W are shown by the solid red line and for V by the dashed black line.

a qualitative difference in the transition from supersonic to subsonic crowdion motion in W and V.

These effects cannot be explained by the greater mass and, consequently, the greater kinetic energy of W atoms as compared to V atoms. This is so because the mass of an atom can be taken as a unit for any pure metal with an appropriate choice of the unit of time. Then the explanation of the qualitative difference in the dynamics of crowdions in the two studied bcc metals should be related to the difference in their interatomic interactions.

In order to compare the potentials for W and V, we consider a close-packed atomic row oriented along the x -axis and calculate the potential energy per atom of the row, $\tilde{\phi}_n$, as the function of the rigid shift along the x -axis in the rigid crystal matrix. The function $\tilde{\phi}_n(x)$ has period equal to the interatomic distance h and its minimal and maximal values are ϕ_{\min} and ϕ_{\max} . For quantitative comparison, the potential functions for W and V are presented in Fig. 7(a) in the following normalized form:

$$\phi_n(x/h) = \frac{\tilde{\phi}(x/h) - \phi_{\min}}{\phi_{\max} - \phi_{\min}}. \quad (3)$$

When an atom is moved by a supersonic crowdion along a close-packed row, it overcomes a potential barrier with a height close to $\phi_{\max} - \phi_{\min}$ because the surrounding atoms of the matrix have a very short time to relax and to modify this potential.

It is seen in Fig. 7(a) that the potential profiles are noticeably different. The potential for W, compared to the potential for V, has a narrower minimum and a wider maximum. This difference in potential energy profiles probably explains why the transition from supersonic to subsonic motion is smooth in W and abrupt in V. This leads to the transformation of supersonic crowdions into moving subsonic crowdions in W and standing subsonic crowdions in V. A sharp transition to the subsonic regime in V creates a high-amplitude vibrational mode localized on the subsonic crowdion.

An interesting insight into the structure of the dislocation core in bcc metals can be obtained within the framework of the multi-string Frenkel-Kontorova model⁷⁰.

Effect of interatomic potentials on mass transfer by supersonic 2-crowdions was studied in a triangular two-dimensional lattice with Morse and Born-Mayer potentials³⁷. It was shown that the potential with a stronger repulsive part promotes self-focusing collisions of atoms and, consequently, the propagation of supersonic crowdions.

In order to compare the repulsive parts of the potentials for W and V we calculate the sublimation energy per atom U as the function of the lattice parameter a . In Fig. 7(b) the difference $U - U_0$ as the function of a/a_0 is plotted, where U_0 is the sublimation energy at $a = a_0$, where a_0 is the equilibrium lattice parameter. The result is presented in Fig. 7(b) for the range of $0.5 < a/a_0 < 1.0$, since this is the range of self-focusing atomic collisions³⁸. If the distance between colliding atoms becomes smaller than the half of the equilibrium interatomic distance, then the collisions are defocusing and propagation of a supersonic crowdion is impossible. That is why stable (self-focusing) propagation of supersonic crowdions is possible only if the collision velocity of the atoms is not too high. Besides, this is the reason why the supersonic 2-crowdions are much more efficient in mass transfer in comparison with the supersonic 1-crowdions. In 2-crowdion the energy is shared by the two atoms moving simultaneously with the high velocity and collision velocities are smaller than that in 1-crowdion with the same energy.

The result presented in Fig. 7(b) shows that the compressive part of the potential in W is much stronger than in V. This explains the fact that the supersonic motion of crowdions in W is noticeably longer in duration and distance in comparison with V. Indeed, self-focusing propagation in W is possible for higher energy atoms, and they can travel longer distances. In addition to that, it should be noted that a detailed analysis of large statistics of molecular dynamics simulations was performed with different embedded atom method potentials for

Fe and W in Refs.^{71,72}.

F. Effect of temperature

Temperature is an important parameter when discussing the motion of interstitial atoms^{6,71}. Figure 8 shows the effect of temperature on the propagation distance of a supersonic 2-crowdion in W. The propagation distance is normalized to the interatomic distance. Two initial velocities of the excited atoms $v_0 = 5.7$ and 7.8 km/s (blue and black lines, respectively) are considered. The temperature range from 300 to 1300 K covers temperatures that are important for the application of W. Each point on the plot is the result of averaging over five realizations.

As seen in Fig. 8, an increase in temperature leads to a decrease in the crowdion propagation distance. The decrease is fast at low temperatures and becomes slower as temperature increases. At high temperatures, the propagation distance of a supersonic 2-crowdion is about ten interatomic distances. Then the structure of the supersonic 2-crowdion is destroyed, and its energy is given to the formation of supersonic 1-crowdions moving in directions different from the direction of the initial momentum.

G. Effect of interatomic potentials for W

It is well-known that interatomic potentials influence the results of molecular dynamics simulations, especially for simulations of high-energy interatomic collisions. So far, the results for the interatomic potential by Marinica *et al.*⁶⁷ were reported. Recently, Mason *et al.* have developed interatomic potential for W that is particularly well suited for modeling vacancy-type defects⁷³. Figure 9 shows the result of application of this potential for simulation of supersonic 1- and 2-crowdions. The left (right) column is for $N = 1$ ($N = 2$). For each panel, the initial velocity of the atoms is indicated.

Panels (a) and (c) of Fig. 9 should be compared to Fig. 2, panels (c) and (e) respectively, since they are plotted for 1-crowdion ($N = 1$) and for the same initial velocities. Similarly, panels (b) and (d) of Fig. 9 are plotted for 2-crowdion ($N = 2$) and the same initial velocities as in Fig. 3, panels (c) and (e), respectively. Comparison reveals that the potential by Mason *et al.*⁷³ predicts even greater propagation distances for supersonic crowdions than the

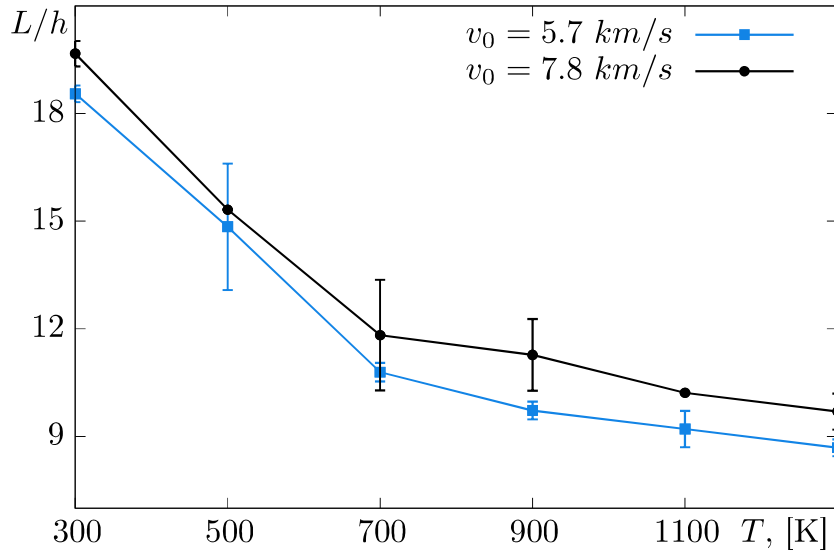


Figure 8. The effect of temperature on the propagation distance of the supersonic 2-crowdion in W. The 2-crowdions are excited with the initial velocities of 5.7 km/s (blue line, blue square dots) and 7.8 km/s (black line, route dots). Each point is the result of averaging over five realizations. Error bars represent the variability of travelled distances. Lines connecting the data points are visual guides.

potential by Marinica *et al.*⁶⁷. This result confirms that the repulsive part of the potentials must be carefully adjusted to better describe collisions of high-energy atoms⁷¹.

IV. CONCLUSIONS AND FUTURE WORK

In the present study, for the first time, the dynamics of N -solitons/ N -crowdions (N is a number of initially excited neighboring atoms in one close-packed atomic row) were investigated in bcc metals W and V via molecular dynamics simulations. The main conclusions can be drawn as follows.

- In order to initiate mass transfer by a supersonic 1-crowdion, an energy of 128 eV in W and 47.8 eV in V is required. On the other hand, to initiate mass transfer by a supersonic 2-crowdion, it is sufficient to expend an energy of 25.4 eV in W and 12.7 eV in V, i.e., 5 and 3.8 times less, respectively. Less energy is not enough to create a Frenkel pair and a compressive soliton (focuson) is formed, which does not transfer mass.

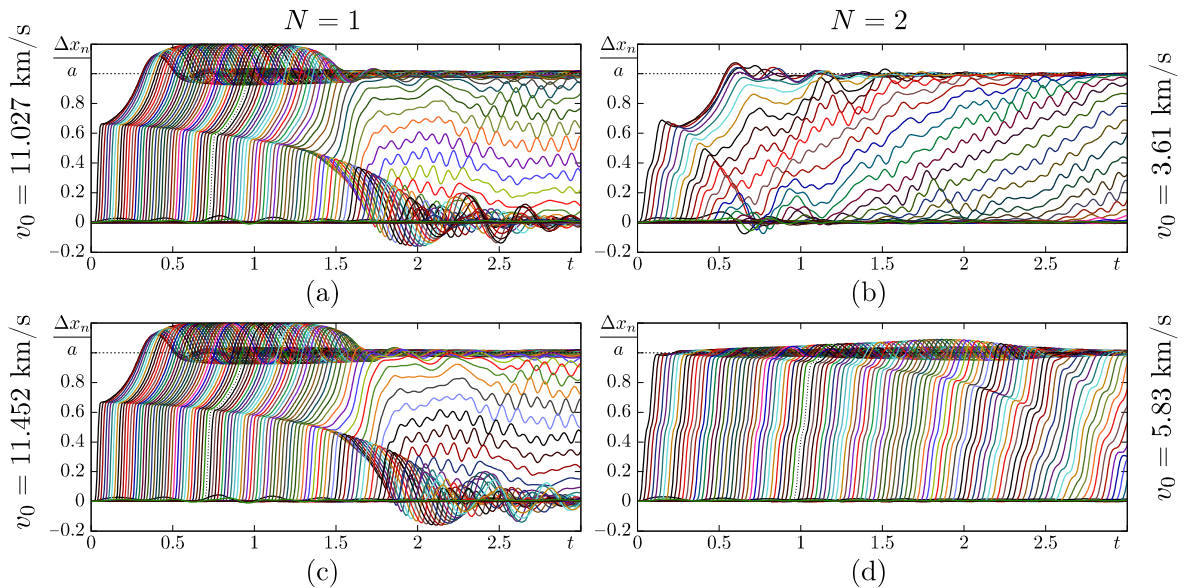


Figure 9. (Color online) The relative atomic displacements $\Delta x/h$ as the functions of time illustrating propagation of 1-crowdion (a), (c) and 2-crowdion (b), (d) in W calculated for a new interatomic potential by Mason *et al.*⁷³ at different initial velocities v_0 (kinetic energy T_0): (a) 11.027 km/s (119 eV) (compare with Fig. 2(c)), (b) 3.61 km/s (25.4 eV) (Fig. 3(c)), (c) 11.452 km/s (128 eV) (Fig. 2(e)), (d) 5.83 km/s (66.2 eV) (Fig. 3(e)).

- Energy dissipation rate for supersonic 2-crowdion is significantly lower than that for supersonic 1-crowdion. This can be explained by the fact that collisions of atoms in a supersonic 1-crowdion, having the same energy as supersonic 2-crowdion, occur at higher velocities, which leads to a greater energy dissipation by the lattice. In a supersonic 2-crowdion, the energy is shared between two atoms, and the collisions of the atoms occur at a lower velocity, resulting in a slower loss of energy by the crowdion.
- Deceleration of a supersonic crowdion produces a moving subsonic crowdion in W and standing subsonic crowdion in V. Subsonic crowdions, produced by slowing down supersonic crowdions, carry a localized vibrational mode with a frequency above the phonon spectrum.
- In W the transition from supersonic to subsonic regime is smooth, while it is abrupt in V. This explains why the just born subsonic crowdion moves in W, but not in V. A smooth transition from supersonic to subsonic motion in W ensures the transfer of

momentum of the directed motion to the atoms moving along the close-packed row in the subsonic regime. A sharp transition in V leads to the transfer of the energy of the directed motion of the supersonic crowdion to a large-amplitude vibrational mode localized on the subsonic crowdion. This explains why the oscillation mode localized on subsonic crowdion in V has much higher amplitude than in W.

- The potential for W, compared to the potential for V, has a narrower minimum and a wider maximum. This difference in potential energy profiles probably explains the reason why the transition from supersonic to subsonic motion is smooth in W and abrupt in V.
- Interatomic interactions in W have a much stronger repulsive part as compared to V, which facilitates the self-focusing propagation of supersonic crowdions in W.

In this work, we mainly discussed the supersonic stage of crowdion motion, since only in the supersonic regime 1- and 2-crowdions are different. Both of them carry one interstitial atom each and after the transition to the subsonic regime they become indistinguishable. However, interstitial atoms continue their directed motion after the transition from supersonic to subsonic regime. An open question stands: do supersonic 2-crowdions form in collision cascades, and if so, how many of them compared to the number of supersonic 1-crowdions? Since, as already noted, both types of supersonic crowdions carry a single interstitial atom, their dynamics must be carefully analyzed to distinguish them.

Starting with the work of Heinisch and Singh⁷⁴, the object kinetic Monte Carlo (OKMC) method has been developed⁷⁵⁻⁷⁷ to understand the evolution of microstructure in materials under irradiation. The main advantage of this method is that it allows one to analyze time and space scales that are inaccessible to the molecular dynamics method. In OKMC method, defects and defect clusters perform random walks imitating their diffusion motion and interact with each other, simulating the transformation and relaxation of the structure. In the present work, we have analyzed the supersonic rather than diffusive motion of self-interstitial atoms. This type of motion of point defects can be incorporated in the OKMC method to describe the collisional stage of cascade development.

The results of our study contribute to a better understanding of the supersonic motion of crowdions in metals and pose new problems that should be solved in future work. A comparative analysis of the dynamics of supersonic crowdions should be carried out for

other metals which are planned to be operated under extreme conditions and which are important for nuclear power engineering. In order to verify the results obtained by molecular dynamics, it is necessary to analyze the supersonic motion of 1- and 2-crowdions in bcc metals using more accurate *ab initio* methods, as was done for fcc Al²⁸. A recent study of supersonic $M \times N$ -crowdions in a two-dimensional triangular Morse lattice, where $M \times N$ is a block of excited atoms, showed that the distances traveled at supersonic speed significantly exceed those for supersonic 1-crowdions³⁶. For bcc and fcc metals, the class of supersonic $M \times N \times K$ -crowdions has not yet been investigated at all and therefore should be analysed. Propagation of supersonic crowdion clusters can produce in the lattice delocalized vacancies (voidions) moving along a close-packed atomic row at subsonic or supersonic speed^{36,78–83}. These objects deserve further study in various metals and alloys. **In addition, real materials have various kinds of defects and are characterized by an increased concentration of vacancies upon irradiation. In our future work, we are going to study the influence of various types of crystal lattice defects on the dynamics of crowdions.**

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