

The Study of $\gamma\gamma \rightarrow \gamma\psi(2S)$ at Belle

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Abstract

Using 980 fb^{-1} of data at and around the $\Upsilon(nS)$ ($n = 1, 2, 3, 4, 5$) resonances collected with the Belle detector at the KEKB asymmetric-energy e^+e^- collider, the two-photon process $\gamma\gamma \rightarrow \gamma\psi(2S)$ is studied from the threshold to 4.2 GeV for the first time. Two structures are seen in the invariant mass distribution of $\gamma\psi(2S)$: one at $M_{R_1} = 3922.4 \pm 6.5 \pm 2.0 \text{ MeV}/c^2$ with a width of $\Gamma_{R_1} = 22 \pm 17 \pm 4 \text{ MeV}$, and another at $M_{R_2} = 4014.3 \pm 4.0 \pm 1.5 \text{ MeV}/c^2$ with a width of $\Gamma_{R_2} = 4 \pm 11 \pm 6 \text{ MeV}$; the signals are parametrized with the incoherent sum of two Breit-Wigner functions. The first structure is consistent with the $X(3915)$ or the $\chi_{c2}(3930)$, and the local statistical significance is determined to be 3.1σ with the systematic uncertainties included. The second matches none of the known charmonium or charmoniumlike states, and its global significance is determined to be 2.8σ including the look-elsewhere effect. The production rates are $\Gamma_{\gamma\gamma}\mathcal{B}(R_1 \rightarrow \gamma\psi(2S)) = 9.8 \pm 3.6 \pm 1.2 \text{ eV}$ assuming $(J^{PC}, |\lambda|) = (0^{++}, 0)$ or $2.0 \pm 0.7 \pm 0.2 \text{ eV}$ with $(2^{++}, 2)$ for the first structure and $\Gamma_{\gamma\gamma}\mathcal{B}(R_2 \rightarrow \gamma\psi(2S)) = 6.2 \pm 2.2 \pm 0.8 \text{ eV}$ with $(0^{++}, 0)$ or $1.2 \pm 0.4 \pm 0.2 \text{ eV}$ with $(2^{++}, 2)$ for the second one. Here, the first errors are statistical and the second systematic, and λ is the helicity.

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I. INTRODUCTION

More than two dozen new resonances that are dubbed as X , Y and/or Z states have been found above the $D\bar{D}$ threshold since Belle observed the $X(3872)$ (now labeled the $\chi_{c1}(3872)$ [1]) in $B \rightarrow K\pi^+\pi^-J/\psi$ [2], and this number is much larger than the expectation from predictions of conventional quark-antiquark models. Among these, candidates for both conventional and exotic charmonium-like states are discussed widely [3]. Many puzzles arise from these XYZ states, and one of them concerns the candidates for P -wave triplet states near $3.9 \text{ GeV}/c^2$, including the $X(3872)$, $Z(3930) \rightarrow D\bar{D}$ and $X(3915) \rightarrow \omega J/\psi$ observed in two-photon collisions [4–8], and $X^*(3860) \rightarrow D\bar{D}$ observed in a full amplitude analysis of the process $e^+e^- \rightarrow J/\psi D\bar{D}$ [9].

One of the most interesting XYZ states is the $X(3872)$, which lies very near the $D\bar{D}^* + c.c.$ mass threshold and is conjectured to have a large $D\bar{D}^* + c.c.$ molecular component [10]. Its large production rates in pp and $p\bar{p}$ collision experiments [11–14] and the determination of its quantum number by LHCb [15] suggest that there is a conventional charmonium $\chi_{c1}(2P)$ core in its wave function. This is supported by another study of $X(3872) \rightarrow \gamma\psi(2S)$ by LHCb [16]. A study of the lineshape of this state by LHCb reveals a pole structure that is compatible with a quasibound state of $D^0\bar{D}^{*0}$ but allowing a quasivirtual state at the level of 2σ [17]. Partners of the $X(3872)$ are suggested, and one of them is a $D^*\bar{D}^*$ loosely bound state with quantum numbers $J^{PC} = 2^{++}$ [18, 19]. Belle found evidence for $X(3872)$ production in two-photon collisions [20], thus motivating the search for the possible 2^{++} partner of the $X(3872)$ in such collisions. Such a study can provide essential information to understand the nature of the $X(3872)$.

Concurrently, there have been many studies related to the $\chi_{cJ}(2P)$ triplet states. The $Z(3930)$ was discovered by Belle in the process $\gamma\gamma \rightarrow D\bar{D}$, and the angular distribution was used to identify it as the $\chi_{c2}(2P)$ state [4]. The existence of $Z(3930)$ and its angular distribution were confirmed by BaBar [5]. The $X(3915)$ was discovered by Belle [7] and a spin-parity analysis of this state by BaBar favored the $J^{PC} = 0^{++}$ quantum numbers [8]. The $X(3915)$ is a candidate of the $\chi_{c0}(2P)$ state [21–24]. In a recent amplitude analysis of the $B^+ \rightarrow K^+D^+D^-$ decay by LHCb [25], there are both 0^{++} and 2^{++} states at $m(D^+D^-) \approx 3930 \text{ MeV}/c^2$. Their parameters are determined to be $M = 3923.8 \pm 1.5 \pm 0.4 \text{ MeV}/c^2$ and $\Gamma = 17.4 \pm 5.1 \pm 0.8 \text{ MeV}$ for $\chi_{c0}(3930)$ and $M = 3926.8 \pm 2.4 \pm 0.8 \text{ MeV}/c^2$ and $\Gamma = 34.2 \pm 6.6 \pm 1.1 \text{ MeV}$ for $\chi_{c2}(3930)$. (Here and hereinafter, the first errors are statistical and the second are systematic.) The $\chi_{c2}(3930)$ state is a good candidate of $\chi_{c2}(2P)$, but this would imply that the hyperfine splitting of $12 \text{ MeV}/c^2$ between $\chi_{c2}(2P)$ and $X(3915)$ would be only 6% of that between $\chi_{c2}(1P)$ and $\chi_{c0}(1P)$ [26]. In contrast, an early calculation [27] utilizing the Godfrey-Isgur relativistic potential model [28] predicts a much larger mass difference of about $60 \text{ MeV}/c^2$ [27]. The $X^*(3860)$ observed by Belle is another candidate of $\chi_{c0}(2P)$ but it was not seen in LHCb’s study of the $B^+ \rightarrow K^+D^+D^-$ decay [25]. One interpretation of the $X^*(3860)$ is a $D\bar{D}$ bound state close to the threshold with isospin $I = 0$ [29]. Therefore, additional studies of the P -wave triplet states near $3.9 \text{ GeV}/c^2$ are needed for a more comprehensive understanding of the XYZ states and, in particular, of the $X(3872)$.

Both 0^{++} and 2^{++} states can be produced in two-photon collisions and can decay to $\gamma\psi(2S)$ via an E1 transition. For example, the partial widths are expected to be $\Gamma(\chi_{c0}(2P) \rightarrow \gamma\psi(2S)) \approx 135 \text{ keV}$ and $\Gamma(\chi_{c2}(2P) \rightarrow \gamma\psi(2S)) \approx 207 \text{ keV}$ according to the aforementioned calculation [27]. In this Article, we report an investigation of the

$\gamma\psi(2S)$ final state produced in two-photon collisions ($e^+e^- \rightarrow e^+e^-\gamma\gamma \rightarrow e^+e^-\gamma\psi(2S)$ or $\gamma\gamma \rightarrow \gamma\psi(2S)$ for brevity), using data collected with the Belle detector [30] at the KEKB asymmetric-energy e^+e^- collider [31]. The $\psi(2S)$ is reconstructed from its hadronic final state $\pi^+\pi^-J/\psi$ with J/ψ reconstructed from a lepton pair $\ell^+\ell^-$ ($\ell = e, \mu$).

II. DETECTOR, DATA SAMPLE, AND MONTE CARLO (MC) SIMULATION

The Belle detector is a large-solid-angle magnetic spectrometer that consists of a silicon vertex detector, a 50-layer central drift chamber, an array of aerogel threshold Cherenkov counters, a barrel-like arrangement of time-of-flight scintillation counters, and an electromagnetic calorimeter (ECL) comprised of CsI(Tl) crystals located inside a superconducting solenoid coil that provides a 1.5T magnetic field. An iron flux return located outside of the coil is instrumented to detect K_L^0 mesons and to identify muons. The origin of the coordinate system is defined as the position of the nominal interaction point (IP). The z axis is aligned with the direction opposite the e^+ beam and is parallel to the direction of the magnetic field within the solenoid. The x axis is horizontal and points toward the outside of the storage ring; the y axis is vertical upward. The polar angle θ and azimuthal angle ϕ are measured relative to the positive z and x axes, respectively.

The integrated luminosity of Belle data used in this analysis is 980 fb^{-1} . About 70% of the data are collected at the $\Upsilon(4S)$ resonance, and the rest are taken at other $\Upsilon(nS)$ ($n = 1, 2, 3, \text{ or } 5$) states or center-of-mass energies a few tens of MeV below the Υ states. The TREPS event generator [33] is used to simulate the signals of $\gamma\gamma \rightarrow X \rightarrow \gamma\psi(2S)$ for optimization of selection criteria, efficiency determination and calculation of the luminosity function $L_{\gamma\gamma}$ of two-photon collisions in Belle data. The major background is found to be the initial-state radiation (ISR) process $e^+e^- \rightarrow \psi(2S)$, which has a cross section of $15.42 \pm 0.12 \pm 0.89 \text{ pb}$ in the Belle data sample [34]. There are 0.6×10^6 events with a $\pi^+\pi^-\ell^+\ell^-$ final state in data, and an MC sample containing 3.8×10^6 such events is simulated with the PHOKHARA generator, which has a precision better than 0.5% [35]. An MC simulation using GEANT3 [36] is used to model the performance of the Belle detector.

III. SELECTION CRITERIA AND SIGNAL RECONSTRUCTIONS

Photon candidates are reconstructed from ECL clusters that do not match any charged tracks; the candidate with the highest energy is selected to form the $\gamma\psi(2S)$ final state. This energy is required to be larger than 100 MeV to suppress the background from fake photons. A candidate of $\psi(2S) \rightarrow \pi^+\pi^-J/\psi$ with $J/\psi \rightarrow e^+e^-$ or $\mu^+\mu^-$ is reconstructed from four well-measured charged tracks, each having impact parameters with respect to the IP of $|dz| < 5 \text{ cm}$ along the z (positron-beam) axis and $dr < 0.5 \text{ cm}$ in the transverse r - ϕ plane. For a charged track, information from the detector subsystems is combined to form a likelihood \mathcal{L}_i for a particle species of $i \in \{e, \mu, \pi, K \text{ or proton}\}$ [37]. Tracks with $\mathcal{R}_K = \mathcal{L}_K/(\mathcal{L}_K + \mathcal{L}_\pi) < 0.4$ are identified as pions with an efficiency of about 95%, while 6% of kaons misidentified as pions. Similar likelihood ratios are formed for electron and muon identification [38, 39]. Both lepton candidates are required to have $\mathcal{R}_e > 0.1$ for the $J/\psi \rightarrow e^+e^-$ mode; at least one candidate is required to have $\mathcal{R}_\mu > 0.1$ for the $J/\psi \rightarrow \mu^+\mu^-$ mode. For the first mode, any bremsstrahlung photons detected in the ECL within 0.05 radians of the original lepton direction are included in the calculation of the

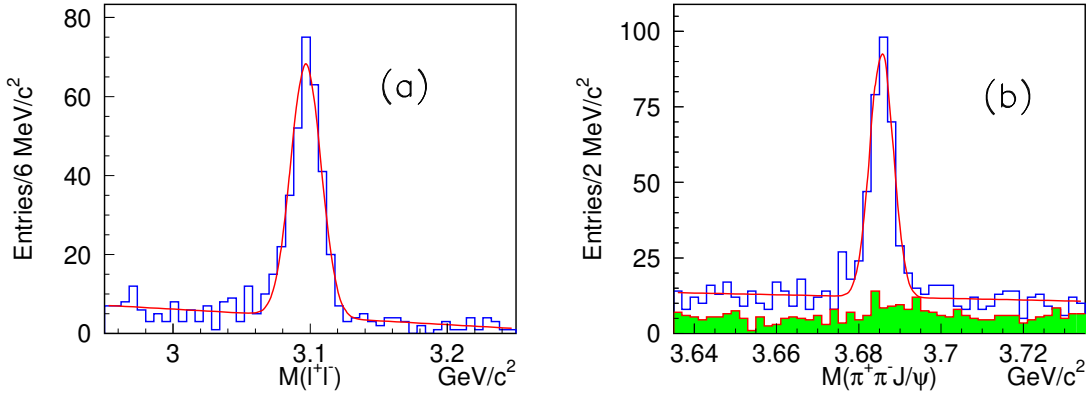


FIG. 1. Invariant mass distributions of (a) $\ell^+\ell^-$ ($\ell = e, \mu$) for the J/ψ signal and (b) $\pi^+\pi^-J/\psi$ for the $\psi(2S)$ signal in data. The shaded histogram is the background estimated from the J/ψ mass sidebands. The curves show the best fit results.

e^+e^- invariant mass.

The invariant mass distributions of the lepton pair ($M_{\ell^+\ell^-}$) from data are shown in Fig. 1(a), where clear J/ψ signals are seen. By fitting the $M_{\ell^+\ell^-}$ distributions with a Gaussian function for the J/ψ signal and a first-order polynomial function for background, we obtain the J/ψ mass resolutions of $\sigma_{\ell^+\ell^-}^{\text{data}} = 11.0 \pm 0.6 \text{ MeV}/c^2$ from data and $\sigma_{\ell^+\ell^-}^{\text{MC}} = 9.4 \pm 0.1 \text{ MeV}/c^2$ from signal MC simulation. A lepton pair is regarded as a J/ψ candidate if $|M_{\ell^+\ell^-} - m_{J/\psi}| < 4\sigma_{\ell^+\ell^-}$, where $m_{J/\psi}$ is the nominal mass of J/ψ [1] and $\sigma_{\ell^+\ell^-} = 11.0 \text{ MeV}/c^2$. Events in the J/ψ mass sidebands, defined as $M_{\ell^+\ell^-} \in [m_{J/\psi} - 13\sigma_{\ell^+\ell^-}, m_{J/\psi} - 5\sigma_{\ell^+\ell^-}] \cup [m_{J/\psi} + 5\sigma_{\ell^+\ell^-}, m_{J/\psi} + 13\sigma_{\ell^+\ell^-}]$, are used to study the background in the $\psi(2S)$ reconstruction. Figure 1(b) shows the distributions of $M_{\pi^+\pi^-J/\psi} \equiv M_{\pi^+\pi^-\ell^+\ell^-} - M_{\ell^+\ell^-} + m_{J/\psi}$ from data, where $M_{\pi^+\pi^-\ell^+\ell^-}$ is the invariant mass of $\pi^+\pi^-\ell^+\ell^-$. Fitting the $M_{\pi^+\pi^-J/\psi}$ distributions with a Gaussian function for $\psi(2S)$ signal and a second-order polynomial function for the background, we obtain the $\psi(2S)$ mass resolutions of $\sigma_{\pi^+\pi^-J/\psi}^{\text{data}} = 2.80 \pm 0.21 \text{ MeV}/c^2$ from data and $\sigma_{\pi^+\pi^-J/\psi}^{\text{MC}} = 2.52 \pm 0.04 \text{ MeV}/c^2$ from the signal MC simulation. The $\psi(2S)$ signal window is defined to be $|M_{\pi^+\pi^-J/\psi} - m_{\psi(2S)}| < 2.5\sigma_{\pi^+\pi^-J/\psi}$, where $m_{\psi(2S)}$ is the nominal mass of $\psi(2S)$ [1] and $\sigma_{\pi^+\pi^-J/\psi} = 2.80 \text{ MeV}/c^2$. To estimate the background in the $\psi(2S)$ reconstruction, the sideband region is defined to be $|M_{\pi^+\pi^-J/\psi} - m_{\psi(2S)}| \pm 9\sigma_{\pi^+\pi^-J/\psi} < 3.75\sigma_{\pi^+\pi^-J/\psi}$.

The background is dominated by $e^+e^- \rightarrow \psi(2S)$ via ISR, where $\psi(2S)$ is combined with a fake photon. Figure 2 shows the distributions of the recoil mass squared $M_{\text{rec}}^2(\gamma\psi(2S))$ of $\gamma\psi(2S)$. For two-photon collision events, there may be an outgoing e^+e^- pair traveling back-to-back along the e^+e^- beams so that $M_{\text{rec}}^2(\gamma\psi(2S))$, corresponding to the mass squared of the outgoing e^+e^- pair, tends to be large. For ISR events, the recoil of $\gamma\psi(2S)$ is dominated by one energetic ISR photon with $E(\gamma_{\text{ISR}}) > 1.5 \text{ GeV}$, so $M_{\text{rec}}^2(\gamma\psi(2S))$ is around zero. We apply $M_{\text{rec}}^2(\gamma\psi(2S)) > 10 (\text{GeV}/c^2)^2$ to remove most ISR events. Nevertheless, there still remain events with two ISR photons traveling back-to-back along the e^+e^- collision beams; such events have a topology similar to two-photon collisions.

To suppress the ISR background further, the transverse momenta of $\psi(2S)$ and $\gamma\psi(2S)$, i.e., $P_t^*(\psi(2S))$ and $P_t^*(\gamma\psi(2S))$, calculated in the center-of-mass system (c.m.s.) and shown in Fig. 3 (a) and (c), are used. $P_t^*(\gamma\psi(2S))$ is small for most of the signal events, in which

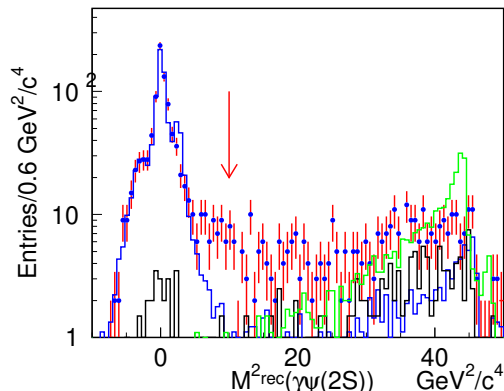


FIG. 2. The distributions of recoil mass square of $\gamma\psi(2S)$. The dots with error bars are data, the black blank histogram is the background estimated from the $\psi(2S)$ mass sidebands, the blue histogram is the ISR MC simulation and the green histogram is the signal MC simulation. The normalization of ISR MC simulation is according the region $M_{\text{rec}}^2(\gamma\psi(2S)) < 10$ $(\text{GeV}/c^2)^2$, and the one of the signal MC simulation is arbitrary. The arrow shows the position of $M_{\text{rec}}^2(\gamma\psi(2S)) = 10$ $(\text{GeV}/c^2)^2$.

the outgoing e^+e^- travel along the accelerator beamline. However, $P_t^*(\psi(2S))$ could be large if $\psi(2S)$ originates from the decay of a resonance such as $\chi_{c0}(2P)$ or $\chi_{c2}(2P)$. For the ISR events, $P_t^*(\psi(2S))$ is small since the ISR photon(s) always travel along the accelerator beamline. We optimize the selections of $P_t^*(\psi(2S))$ and $P_t^*(\gamma\psi(2S))$ based on the Punzi figure of merit (FOM), defined as

$$\text{FOM} \equiv \frac{\varepsilon(t)}{a/2 + \sqrt{N_{\text{bkg}}(t)}} \quad (1)$$

according to Eq.(7) in Ref. [32]. Here, $\varepsilon(t)$ is the signal efficiency based on the selection criterion t , a is the number of sigmas corresponding to one-side Gaussian tests — we take $a = 5$ — and $N_{\text{bkg}}(t)$ is the background estimated from the ISR events and the $\psi(2S)$ mass sidebands. The FOM and $\varepsilon(t)$ versus P_t^* selections are shown in Figs. 3(b) and 3(d). We apply $P_t^*(\psi(2S)) > 0.1$ GeV/c and $P_t^*(\gamma\psi(2S)) < 0.2$ GeV/c with selection efficiencies of $\varepsilon^{\text{MC}}(t) = (97.1 \pm 0.3)\%$ and $\varepsilon^{\text{MC}}(t) = (67.8 \pm 0.7)\%$, respectively. There are about 150 ISR events surviving these selection criteria with an efficiency of about 0.02%.

IV. INVARIANT MASS DISTRIBUTION OF $\gamma\psi(2S)$ AND TWO STRUCTURES

Figure 4 shows the invariant mass distributions for data of $\gamma\psi(2S)$ ($M_{\gamma\psi(2S)}$) in the $J/\psi \rightarrow e^+e^-$ and $\mu^+\mu^-$ modes. The distributions of the backgrounds estimated from the scaled $\psi(2S)$ mass sidebands and ISR events simulated by PHOKHARA [35] are also shown in Fig. 4. The ratio between data and ISR MC simulation is 0.147 ± 0.012 from the distributions in the region $M_{\gamma\psi(2S)} < 3.9$ GeV/c^2 , while the expected ratio is 0.156 ± 0.009 according to the cross section and the size of the ISR MC sample. Figure 5 shows the signal selection efficiency and the two-photon luminosity function $L_{\gamma\gamma}(\sqrt{s})$, which is defined as the probability of a two-photon emission with $\gamma\gamma$ c.m.s. energy \sqrt{s} in the Belle experiment [33]. The efficiencies

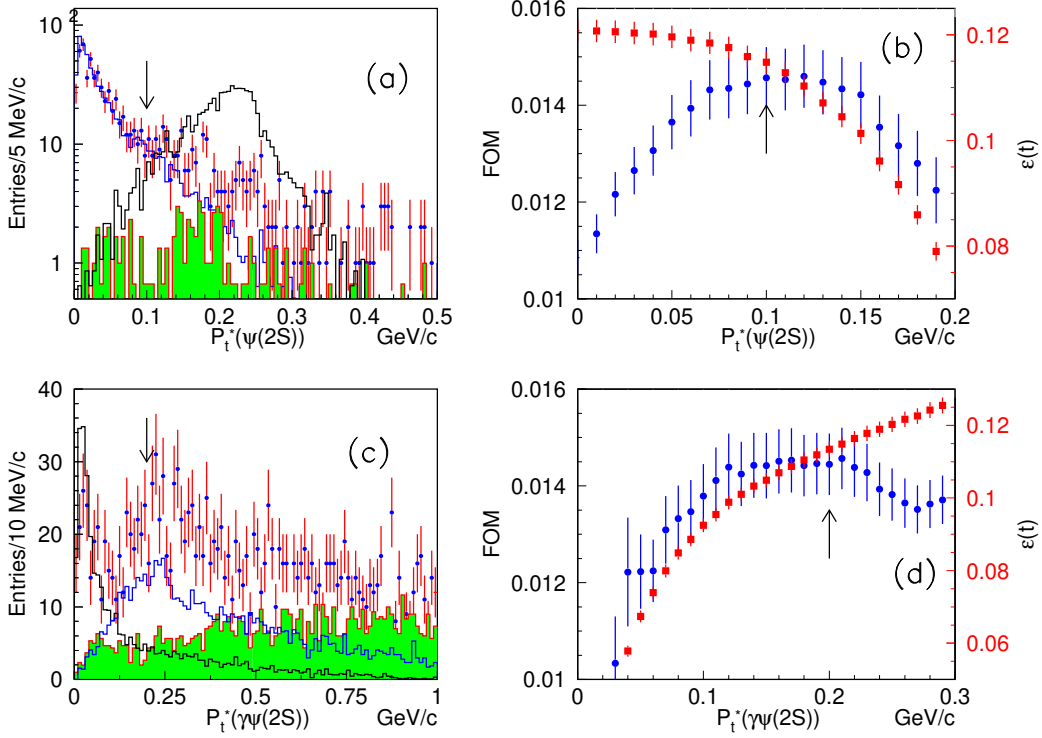


FIG. 3. The distributions of transverse momenta of $\psi(2S)$ (top row) and $\gamma\psi(2S)$ (bottom row) in the c.m.s of e^+e^- collision. In the left panel, the dots with error bars are from the signal region, the shaded histograms are the backgrounds estimated from the $\psi(2S)$ mass sidebands, the black blank histograms are signal MC simulation with arbitrary normalizations, and the blue blank histograms are ISR MC simulation. The normalization of ISR MC simulation in (a) is according to data with $P_t^*(\psi(2S)) < 0.1$ GeV/ c^2 , and the one in (c) is according to the size of ISR MC simulation sample. The right panel shows the Punzi FOMs in dots and efficiencies in diamonds versus (b) $P_t^*(\psi(2S))$ and (d) $P_t^*(\gamma\psi(2S))$. The arrows show the selections applied.

for $J^{PC} = 0^{++}$ and 2^{++} ($|\lambda| = 0$ or 2) range from $\sim 10\%$ to $\sim 15\%$ for $M_{\gamma\psi(2S)}$ between 3.85 GeV/ c^2 and 4.20 GeV/ c^2 . The difference of $L_{\gamma\gamma}$ between 0^{++} and 2^{++} is very small and thus ignored.

The $M_{\gamma\psi(2S)}$ distribution of data after combining the e^+e^- and $\mu^+\mu^-$ modes are shown in Fig. 6. Excesses around 3.92 GeV/ c^2 and 4.02 GeV/ c^2 are seen. To study the excesses, a binned extended maximum-likelihood fit is performed to the $M_{\gamma\psi(2S)}$ mass spectra. The function used for the fit is characterized by the sum:

$$f_{\text{sum}} = f_{R_1} + f_{R_2} + f_{\text{ISR}} + f_{\text{bkg}} + f_{\text{SB}}. \quad (2)$$

Here, f_{R_1} (f_{R_2}) is for the structure R_1 (R_2) near 3.92 GeV/ c^2 (4.02 GeV/ c^2), f_{ISR} for the ISR events, f_{SB} for the background in $\psi(2S)$ reconstruction, and f_{bkg} for the possible additional backgrounds. The f_{SB} distribution is estimated from the $\psi(2S)$ mass sidebands, and its yield is fixed in the fits. The function f_{R_1} (f_{R_2}) contains the convolution of a relativistic Breit-Wigner (BW) function with a form of $12\pi\Gamma_{\gamma\gamma}\Gamma_X/((s - M^2)^2 + M^2\Gamma^2)$ and a Crystal Ball (CB) function [40] with a mass resolution of about 7.2 MeV/ c^2 (8.0 MeV/ c^2), and the parameters of CB function are fixed according to the signal MC simulation of a resonance

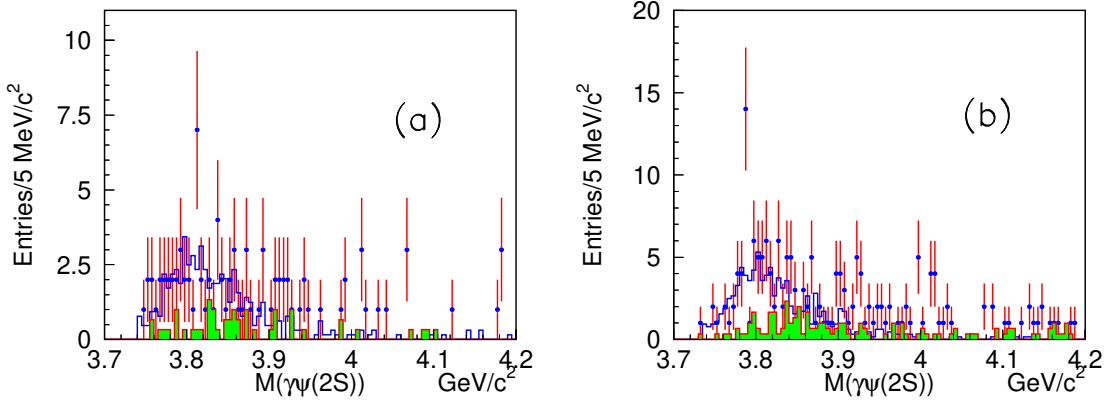


FIG. 4. The invariant mass distributions of $\gamma\psi(2S)$ from (a) e^+e^- mode and (b) $\mu^+\mu^-$ mode. The dots with error bars are data, and the shaded histograms are backgrounds estimated from the $\psi(2S)$ mass sidebands. The blank histograms are ISR events simulated and scaled to the size of the Belle data sample.

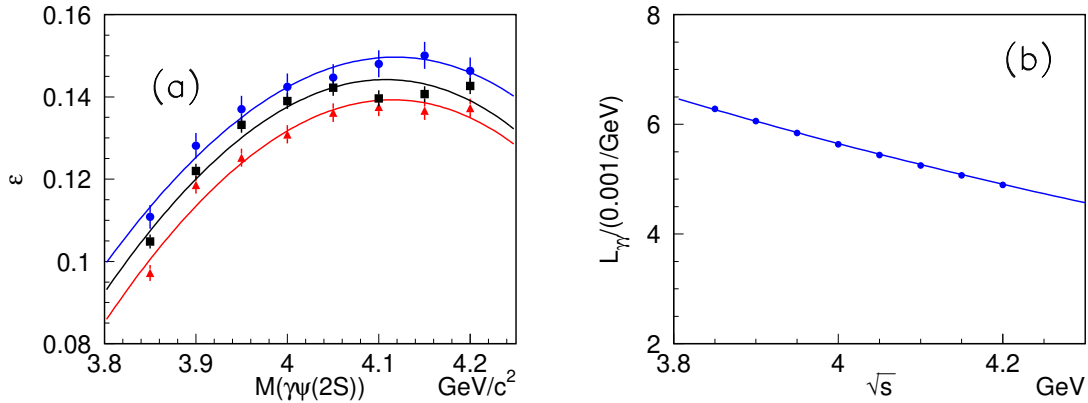


FIG. 5. (a) The efficiencies at different $M_{\gamma\psi(2S)}$ from MC simulation, and (b) the two-photon luminosity function $L_{\gamma\gamma}(\sqrt{s})$. In (a), the blue dots are the efficiencies for $J^{PC} = 0^{++}$, and the black (red) dots are the efficiencies for 2^{++} with helicity $|\lambda| = 0$ ($|\lambda| = 2$). The curves show the best fits with polynomial functions.

with a mass near the one of R_1 (R_2) states and with no width. The resonant parameters in the BW function, M , Γ , and $\Gamma_X\Gamma_{\gamma\gamma}$ are the mass, the width, and the product of partial widths of the decays to the final state X ($= \gamma\psi(2S)$ here) and $\gamma\gamma$, respectively. The product $\Gamma_X\Gamma_{\gamma\gamma}$ is treated as one parameter, since it is impossible to separate Γ_X and $\Gamma_{\gamma\gamma}$ in the fits. The efficiency curve ε is shown in Fig. 5(a) and is incorporated into f_{R_1} and f_{R_2} , i.e., $f_R \propto \varepsilon \cdot (\text{BW} \otimes \text{CB})$. The widths Γ_{R_1} and Γ_{R_2} are found to be small and thus the possible interference between R_1 and R_2 is expected to be small and is ignored in the fit. The histogram of $M_{\gamma\psi(2S)}$ distribution from the ISR MC simulation is used for f_{ISR} . There may be more subdominant sources of background, such as high order QED processes and continuum production of $\gamma\gamma \rightarrow \gamma\psi(2S)$, but their individual and collective contributions are not clearly distinguishable with the current limited statistics. A second-order polynomial function is used for f_{bkg} , and polynomial functions with different order are considered to

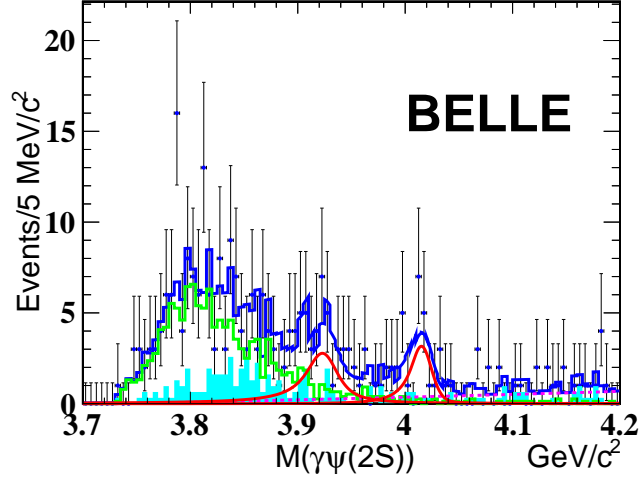


FIG. 6. The $\gamma\psi(2S)$ invariant mass distribution and the fit result. The points with error bars show the data while the shaded histogram is the normalized background from the $\psi(2S)$ mass sidebands. The solid blue curve shows the best fit results. The red signal curves from the convolutions of BW and CB functions show the contributions from the two structures. The green blank histogram shows the component of ISR events of $e^+e^- \rightarrow \psi(2S) \rightarrow \pi^+\pi^-J/\psi$. The pink dashed line shows the possible additional background, modeled by a second-order polynomial.

Resonant parameters	$J = 0$	$J = 2$
M_{R_1}	$3922.4 \pm 6.5 \pm 2.0$	
Γ_{R_1}	$22 \pm 17 \pm 4$	
$\Gamma_{\gamma\gamma}\mathcal{B}(R_1 \rightarrow \gamma\psi(2S))$	$9.8 \pm 3.6 \pm 1.2$	$2.0 \pm 0.7 \pm 0.2$
M_{R_2}	$4014.3 \pm 4.0 \pm 1.5$	
Γ_{R_2}	$4 \pm 11 \pm 6$	
$\Gamma_{\gamma\gamma}\mathcal{B}(R_2 \rightarrow \gamma\psi(2S))$	$6.2 \pm 2.2 \pm 0.8$	$1.2 \pm 0.4 \pm 0.2$

TABLE I. Summary of the resonant parameters determined. The units of mass (M), width (Γ), product of partial width and branching fraction $\Gamma_{\gamma\gamma}\mathcal{B}$ are MeV/c^2 , MeV and eV , respectively. The first errors are statistical and the second are systematic.

estimate the systematic uncertainty.

The result from a fit in which all parameters are floated except the yield of the f_{SB} component is shown Fig. 6 and Table I. The reduced chi-squared of the fit to the $M_{\gamma\psi(2S)}$ spectrum is $\chi^2/ndf = 0.69$. The signal yields are $N_{R_1} = 31 \pm 11$ events for R_1 with $M_{R_1} = 3922.4 \pm 6.5 \text{ MeV}/c^2$ and $\Gamma_{R_1} = 22 \pm 17 \text{ MeV}$, and $N_{R_2} = 19 \pm 7$ events for R_2 with $M_{R_2} = 4014.3 \pm 4.0 \text{ MeV}/c^2$ and $\Gamma_{R_2} = 4 \pm 11 \text{ MeV}$.

The production of R_1 and R_2 in two-photon collisions are studied by determining the parameter $\mathcal{B} \cdot \Gamma_{\gamma\gamma} \equiv \Gamma_{\gamma\psi(2S)}\Gamma_{\gamma\gamma}/\Gamma$ with the formula [33]:

$$\mathcal{B} \cdot \Gamma_{\gamma\gamma} = \frac{n_{\text{fit}}^{\text{sig}}}{L_{\text{tot}} \cdot \mathcal{B}^{\text{prod}} \cdot \varepsilon \cdot F(\sqrt{s}, J)}, \quad (3)$$

where $n_{\text{fit}}^{\text{sig}}$ is the signal yield from the fit, $L_{\text{tot}} = 980 \text{ fb}^{-1}$ is the integrated luminosity of the

Belle data sample, J is the spin of a structure, and $\mathcal{B}^{\text{prod}}$ is the product of branching fractions $\mathcal{B}(\psi(2S) \rightarrow \pi^+\pi^- J/\psi) \cdot \mathcal{B}(J/\psi \rightarrow e^+e^-/\mu^+\mu^-)$. Since Γ_{R_1} and Γ_{R_2} are small compared to the available kinetic energy in the decays, the spin-dependent factor is $F(\sqrt{s}, J) = 4\pi^2(2J+1)L_{\gamma\gamma}(\sqrt{s})/s$. The best fit gives $\Gamma_{\gamma\gamma}\mathcal{B}(R_1 \rightarrow \gamma\psi(2S)) = (8.2 \pm 3.4)$ eV if $J = 0$ and (1.6 ± 0.7) eV if $J = 2$ for structure R_1 , and $\Gamma_{\gamma\gamma}\mathcal{B}(R_2 \rightarrow \gamma\psi(2S)) = (6.8 \pm 2.8)$ eV if $J = 0$ and (1.4 ± 0.6) eV if $J = 2$ for structure R_2 . The ISR yield of 134 ± 15 is consistent with the estimate from the ISR MC simulation of 154 ± 10 . The mass of R_1 indicates that it is a good candidate for $X(3915)$, $\chi_{c2}(3930)$ or an admixture of them. An alternate fit with both structures included and M_{R_1} and Γ_{R_1} fixed to the nominal $X(3915)$ parameters yields $\Gamma_{\gamma\gamma}\mathcal{B}(X(3915) \rightarrow \gamma\psi(2S)) = 9.6 \pm 2.9 \pm 1.0$ eV if $J^{PC} = 0^{++}$ of 1.9 ± 0.6 eV if $J^{PC} = 2^{++}$. Another alternative fit with the mass and width of R_1 fixed to those of $\chi_{c2}(3930)$ yields $\Gamma_{\gamma\gamma}\mathcal{B}(\chi_{c2}(3930) \rightarrow \gamma\psi(2S)) = 2.2 \pm 0.6 \pm 0.4$ eV if $J^{PC} = 2^{++}$. A third alternate fit with R_1 being an admixture of $X(3915)$ and $\chi_{c2}(3930)$ shows no notable change in the fit quality.

The local signal significance is determined to be 3.5σ for R_1 and 3.4σ for R_2 by comparing the value of $\Delta(-2 \ln \mathcal{L}) = -2 \ln(\mathcal{L}_{\text{max}}/\mathcal{L}_0)$ and the change of the number of free parameters (N_{par}) in the fits, where \mathcal{L}_{max} is the likelihood with both R_1 and R_2 included in Eq. 2, and \mathcal{L}_0 is the likelihood with only one of R_1 or R_2 excluded. The values of $-2 \ln \mathcal{L}$, χ^2/ndf , and N_{par} of all these fits are summarized in Table II. Taking into account the systematic uncertainties, described in Section V, the lowest values of the local significance of R_1 is 3.1σ . Since R_2 has never been seen before, the look-elsewhere effect is assessed for it with pseudo-experiments to check its global significance. The function for generating pseudo-experiments is $f_{\text{toyMC}} = f_{R_1} + f_{\text{ISR}} + f_{\text{bkg}} + f_{\text{SB}}$ with the parameters from the nominal fit. The fit in each pseudo-experiment is performed with the same procedures as for the nominal fit to the actual data sample, except that the mass range of R_2 is limited to $M_{R_2} > 3.95$ GeV/ c^2 because the region $M_{\gamma\psi(2S)} < 3.95$ GeV/ c^2 is dominated by R_1 and ISR backgrounds. Among the 5.0×10^4 pseudo-experiments, the number of experiments with $\Delta(-2 \ln \mathcal{L})$ of R_2 signal larger than the one from data is 137. Therefore, the probability considering the look-elsewhere effect is about $(2.74 \pm 0.23) \times 10^{-3}$, corresponding to a global significance of 2.8σ .

TABLE II. The values of $-2 \ln \mathcal{L}$, χ^2/ndf and number of free parameters (N_{par}) in the different fits. From left to right, the rows are the fits with no resonance included, only R_1 included, only R_2 included, both R_1 and R_2 included (nominal fit), both resonances included and the mass and width of R_1 fixed to those of $X(3915)$, and both resonances included and the mass and width of R_1 fixed to those of $\chi_{c2}(3930)$. Only the differences among $-2 \ln \mathcal{L}$ are meaningful in studying the statistical significance of R_1 and R_2 .

—	no resonance	R_1 only	R_2 only	$R_1 + R_2$	$X(3915) + R_2$	$\chi_{c2}(3930) + R_2$
$-2 \ln \mathcal{L}$	-2932.2	-2946.5	-2946.3	-2965.4	-2964.8	-2963.0
χ^2/ndf	0.76	0.74	0.78	0.70	0.68	0.68
N_{par}	5	8	8	11	9	9

V. SYSTEMATIC UNCERTAINTIES

There are systematic uncertainties in determining the resonant parameters of the two structures. The masses and widths are determined from fitting to the invariant mass distribution of $\gamma\psi(2S)$. In determining $\mathcal{B} \cdot \Gamma_{\gamma\gamma}$ with Eq. (3), additional systematic uncertainties

from the selection efficiency, the luminosity of Belle data sample and the branching fractions of J/ψ and $\psi(2S)$ decays are taken into account.

The uncertainties due to the fits are estimated by changing the fit range, the number and the f_{SB} shape of the background in the $\psi(2S)$ reconstruction, the f_{bkg} shape, the bin width of the $M_{\gamma\psi(2S)}$ distribution, the parametrization of the BW function, and the resonant parameters of $X(3915)$ and $\chi_{c2}(3930)$. The fit range is changed from $[3.70, 4.20]$ GeV/ c^2 to $[3.725, 4.15]$ GeV/ c^2 . The number of $\psi(2S)$ mass sideband events is changed by 1σ , and the sideband region is changed from $|M_{\pi^+\pi^-J/\psi} - m_{\psi(2S)} \pm 9\sigma_{\pi^+\pi^-J/\psi}| < 3.75\sigma_{\pi^+\pi^-J/\psi}$ to $|M_{\pi^+\pi^-J/\psi} - m_{\psi(2S)} \pm 8\sigma_{\pi^+\pi^-J/\psi}| < 3.75\sigma_{\pi^+\pi^-J/\psi}$ to estimate the uncertainty due to the f_{SB} component. Another ISR MC sample is simulated to estimate the uncertainty from the shape of f_{ISR} . The alternative polynomial function for f_{bkg} is first-order or third-order. The bin width is changed from 5 MeV/ c^2 to 4 MeV/ c^2 . The alternative formula of the resonant shape is $\text{BW} \propto (M^2/s) \cdot 12\pi\Gamma_{\gamma\gamma}\Gamma_X / ((s-M^2)^2 + M^2\Gamma^2)$. The uncertainty from the resolution of $M_{\gamma\psi(2S)}$ is mainly related to the reconstructed γ , and it is estimated with a sample of about 4,000 $\gamma\gamma \rightarrow \chi_{c2} \rightarrow \gamma J/\psi$ events selected in the Belle data sample. Fitting to χ_{c2} signals in the $M_{\gamma J/\psi}$ distributions from data and MC simulation results in the consistent value of 10.84 ± 0.26 MeV/ c^2 and 10.77 ± 0.22 MeV/ c^2 , respectively. Thus, the uncertainty due to the mass resolution of $\gamma\psi(2S)$ is expected to be very small and so is ignored. When M_{R_1} and Γ_{R_1} are fixed to those of $X(3915)$ or $\chi_{c2}(3930)$, their values are changed by 1σ to estimate the related systematic uncertainties [1]. The largest differences between the nominal fit results and those from these various fits are taken as the systematic uncertainties of the mass, the width and the product $\Gamma_{\gamma\gamma}\mathcal{B}(R \rightarrow \gamma\psi(2S))$.

Several sources of non-fit-related systematic uncertainties are considered. The particle identification uncertainty is 2.8% [37–39]; the uncertainty of the tracking efficiency is 0.35% per track and is additive; the uncertainty of the photon reconstruction is 2% per photon. The efficiency for the tracks in the extreme forward and backward regions obtained from MC simulation is found to be higher than that obtained in data according to the study of $e^+e^- \rightarrow \psi(2S) \rightarrow \pi^+\pi^-J/\psi$ via ISR [34], and appropriate corrections have been applied. The uncertainty in the $\psi(2S)$ mass window requirement is measured to be 0.6%, while the one of J/ψ mass window is ignored. The efficiencies of the selection criteria on $P_t^*(\psi(2S))$ and $P_t^*(\gamma\psi(2S))$ are strongly related to the boost transformation from the lab system to the c.m.s. of e^+e^- collisions. However, the related uncertainty is very small, and 1% is taken to be a conservative estimation for the uncertainty due to the P_t^* selections. The uncertainty due to the $M_{\text{rec}}^2(\gamma\psi(2S))$ requirement is less than 0.5%. The uncertainty due to the momentum and angular distributions of helicities 0 and 2 for $J = 2$ is estimated to be 4.3% from the TREPS generator [33], while the one of $J = 0$ is ignored with the decay to $\gamma\psi(2S)$ isotropic and no uncertainty in helicity. Belle measures the luminosity with 1.4% precision. The trigger efficiency for the events surviving the selection criteria exceeds 99.4%, and so the uncertainty is ignored. The uncertainties of the J/ψ and $\psi(2S)$ decay branching fractions taken from Ref. [1] contribute a systematic uncertainty of 1.3%. The statistical error in the MC determination of the efficiency is less than 0.7%.

The non-fit-related systematic uncertainties are listed in Table III. Assuming all the sources are independent, we add them in quadrature to obtain a total systematic uncertainty of 6.2% (4.4%) of $J = 2$ ($J = 0$) in determining $\mathcal{B} \cdot \Gamma_{\gamma\gamma}$, in addition to the uncertainties from the fits.

Source	Relative error (%)	
	$J = 0$	$J = 2$
—		
Particle identification	2.8	
Tracking efficiency	1.4	
Photon reconstruction	2.0	
$\psi(2S)$ mass window	0.6	
$P_t^*(\psi(2S))$ and $P_t^*(\gamma\psi(2S))$	1.0	
$M_{\text{rec}}^2(\gamma\psi(2S))$	0.5	
Luminosity	1.4	
Generator	—	4.3
Branching fractions	1.3	
Statistics of MC samples	0.7	
Sum in quadrature	4.4	6.2

TABLE III. The summary of systematic uncertainties besides the fits in $\gamma\gamma \rightarrow \gamma\psi(2S)$ measurement.

VI. DISCUSSION ON THE TWO STRUCTURES

We find evidence for the structure R_1 near $3.92 \text{ GeV}/c^2$, which may be $X(3915)$, $\chi_{c2}(3930)$, or an admixture of them. Assuming R_1 is $\chi_{c2}(3930)$ and taking into account $\Gamma_{\gamma\gamma}\mathcal{B}(\chi_{c2}(3930) \rightarrow D\bar{D}) = 210 \pm 40 \text{ eV}$, the ratio $R = \mathcal{B}(\chi_{c2}(3930) \rightarrow \gamma\psi(2S))/\mathcal{B}(\chi_{c2}(3930) \rightarrow D\bar{D}) = 0.010 \pm 0.003$ is obtained. A rough estimation shows the partial width $\Gamma(\chi_{c2}(3930) \rightarrow \gamma\psi(2S)) = (200 \sim 300) \text{ keV}$, which is close to the predicted value of 207 keV from Godfrey-Isgur relativistic potential model [27].

It is interesting to see that the mass of R_2 agrees with the HQSS-predicted mass ($\approx 4013 \text{ MeV}/c^2$) of the 2^{++} partner of $X(3872)$ [18]. The mass difference between R_2 and $X(3872)$ is $142.6 \pm 4.2 \text{ MeV}/c^2$, while that between $D^{*0}(2007)$ and D^0 is $142.01 \text{ MeV}/c^2$. Meanwhile, the width of R_2 from the fit coincides with the predicted width of $2 - 8 \text{ MeV}/c^2$ for the 2^{++} partner of $X(3872)$ [19]. Thus, R_2 may provide important information for understanding the nature of the $X(3872)$. However, the global significance of R_2 is only 2.8σ . A much larger data sample that will be collected by Belle II may resolve this in the near future.

VII. SUMMARY

The two-photon process $\gamma\gamma \rightarrow \gamma\psi(2S)$ is studied in the $\gamma\gamma$ mass range from the threshold to $4.2 \text{ GeV}/c^2$ for the first time with the full Belle data sample, and two structures are seen in the invariant mass distribution of $\gamma\psi(2S)$. The first has a mass of $M_{R_1} = 3922.4 \pm 6.5 \pm 2.0 \text{ MeV}/c^2$ and a width of $\Gamma_{R_1} = 22 \pm 17 \pm 4 \text{ MeV}$ with a local statistical significance of 3.1σ when the systematic uncertainties are included. This is close to the mass of $X(3915)$ and $\chi_{c2}(3930)$. The second has a mass of $M_{R_2} = 4014.3 \pm 4.0 \pm 1.5 \text{ MeV}/c^2$ and a width of $\Gamma_{R_2} = 4 \pm 11 \pm 6 \text{ MeV}$, with a global statistical significance of 2.8σ . The values of $\Gamma_{\gamma\gamma}\mathcal{B}(R \rightarrow \gamma\psi(2S))$ are of the order of several eV.

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