MulT_predict - An optimised comprehensive multicomponent geothermometer

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Abstract

In this study, we introduce MulT_predict as a fully integrated solute multicomponent geothermometer, combining numerical optimisation processes for sensitive parameters to back-calculate on chemical reservoir conditions. This results in a state of the art geothermometer, providing accurate reservoir temperature estimation validated at geothermal borehole measurements on a worldwide scale. In addition, a universally valid mineral assemblage for unknown reservoir composition is developed, focusing on worldwide applicability. Using the evolved methodology, the limits of the optimisation processes are determined by using a synthetic brine (150°C, pH 6, aluminium concentration 0.003 mmol/l) and successively perturbing its geochemical equilibrium state. Individual back-calculation of reservoir conditions lead to valid temperature estimations of 145°C, 3.4% lower than the initial temperature while simultaneously and interdependently optimisation reconstructs the sensitive parameters even more precise with a deviation of 0.056 for the initial pH value, and 0.164 µmol/l for the aluminium concentration.

Keywords

MulT_predict, multicomponent geothermometry, reservoir temperature estimation, universally valid mineral set, benchmarking

1. Introduction

Evaluating the quantity of energy in a reservoir is essential for economical geothermal energy production. Therefore, the accurate determination of the reservoir temperature is one key factor of geothermal exploration besides flow rate. Geothermometry is a common technique to predict the reservoir temperatures from the geochemical composition of geothermal fluids. Temperature-dependent cation ratios, as well as saturation of mineral phases, can be the basis for temperature estimation, assuming an in-situ chemical equilibrium of reservoir rock and fluid (Ellis and Mahon, 1964). As a result, the first conventional solute geothermometers were introduced around 60 years
ago by Fournier and Rowe (1966). In an ongoing development, new solute geothermometers were continuously developed but led to high uncertainties due to changes in fluid chemistry regarding different geothermal locations (Nitschke et al., 2018). In 1984, Reed and Spycher plotted saturation indices of mineral phases calculated from thermodynamic data against temperature. The resulting saturation curves illustrate the temperature-dependent solubility of the reservoir mineral assemblage in the geothermal fluid. Spycher et al. (2014) took up this methodology and presented a multicomponent geothermometer, which evaluates the geochemical equilibria of mineral phases and fluid for reservoir temperature estimation. Nitschke et al. (2017) analysed temperature predictions from conventional and multicomponent geothermometers, showing a large reduction in uncertainties for this modelling approach. Thus, multiple mineral phases lead to statistically more robust temperature estimations. Therefore in 2011, Spycher et al. introduced the multicomponent geothermometer GeoT, followed by RTEst by Palmer (2014). Also, software for chemical reconstruction of downhole and reservoir conditions like WATCH (Bjarnason, 2010) improved the results of solute geothermometry. Developing MulT_predict, Ystroem et al. (2020) combined the multicomponent temperature estimation with a numerical reconstruction of the reservoir conditions. Sensitive parameters such as the aluminium concentration and pH value are back-calculated to their original in-situ values (Ystroem et al., 2021). In addition, effects from secondary processes such as dilution and boiling are corrected. These parameters are prone to geochemical changes of the fluid during the ascent to the surface or while sampling (Giggenbach, 1981, 1988). The major advantage of MulT_predict, unlike other solutes multicomponent geothermometers, is that a standard fluid analysis is sufficient and a sophisticated gas analysis is not required. Previously, MulT_predict was developed, applied, and validated for the basaltic setting of Krafla and Reykjanes fields in Iceland (Ystroem et al., 2020). The emphasis of this study is the development of a comprehensive multicomponent geothermometer for greenfield exploration. In such an early stage, little reservoir knowledge and no borehole data is available. The reservoir rock mineralogy as the basis of multicomponent geothermometrical temperature estimation is typically lacking. To still facilitate the application of MulT_predict, as an early-stage exploration tool, on a broad range of geothermal sites, geological settings, and play types, the focus of the study is the development of a universally valid mineral set. Based on this, a general procedure of statistical outlier removal is introduced to acquire more precise temperature estimations and simplify the practicality of MulT_predict.

First, the applicability of the tool is transferred to a broad range of geothermal settings around the world including saline crystalline basements, marine, and continental basin facies as well as volcanic rock. In a first step, individual mineral sets are evolved for each geothermal setting. Afterwards, mineralogical coherences within the mineral sets are combined in a universally valid mineral set for general applicability. The subsequent outlier removal increases the precision of the temperature
estimation. The results of the validation are shown for exemplary boreholes. Furthermore, the characteristics of the site-specific brine are discussed to identify clustering and similarities concerning geochemical key parameters, providing insights into why a universally valid mineral set provides precise temperature predictions and where the limits of its application are. In the last part, MulT_predict’s optimisation processes are benchmarked and discussed. Therefore, a predefined synthetic brine, initially in full equilibrium, is increasingly perturbed stepwise. This perturbation is then reconstructed using two different approaches. Firstly, each optimisation process is evaluated individually regarding the back-calculation of each sensitive parameter (boiling/dilution, pH value, and aluminium concentration). Secondly, the performance of the interdependent optimisation processes is evaluated by reconstructing all sensitive parameters together. Further, the results of both reconstructions of reservoir conditions are discussed.

2. Method

In solute multicomponent geothermometry, the base assumption is the geochemical equilibrium between the geothermal fluid and the hosted reservoir rock (Fournier and Truesdell, 1974). Thus, in the temperature-dependent reaction mineral phases are dissolved until an equilibrium within the fluid is reached. The geochemical equilibrium of each mineral phase is attained when the measured ion activity product IAP of the fluid equals the temperature-dependent thermodynamic constant $K(T)$ (Equation 1). As a result, the temperature-dependent saturation index $SI(T)$ of a mineral phase is zero.

$$SI(T) = \log \left( \frac{IAP}{K(T)} \right)$$

$SI$ saturation index; $T$ temperature; $IAP$ ion activity product; $K$ thermodynamic equilibrium constant

For reservoir temperature estimation, the saturation indices of several mineral phases are plotted over the temperature. The resulting equilibrium temperatures (at $SI = 0$) serve as part of the geothermometer. Basing the temperature estimation on the $SI$s of several minerals has proven to be a robust geothermometric tool. As input parameters for MulT_predict, a standard geochemical fluid analysis covering the major cations and anions, the pH value, as well as silica and aluminium concentration is needed to account for the chemical elements being the components of the reservoir rock mineral assemblage. Nevertheless, the geochemical equilibrium is still prone to uncertainties when the chemistry of the fluid changes. Divergences from the chemical equilibrium state are due to a) an immature fluid has not yet reached equilibrium or b) secondary processes while the fluid ascends to the surface or while sampling. Such processes are referring to phase segregation, boiling, mixing or dilution, as well as complex building and precipitation of mineral phases (Arnórsson et al., 1990)
In a previous study, numerical optimisation processes are introduced to MulT_predict correcting sensitive parameters such as pH value, aluminium concentration, as well as changes in the fluid concentration from these effects (Ystroem et al., 2021). The goal is to reconstruct the true in-situ chemical system as a basis to compute the equilibrium temperatures. Assuming the temperature estimations of multiple mineral phases converge to an equal temperature. For these saturation index determinations, MulT_predict is coupling MATLAB to an IPhreeqcCOM server introduced by Charlton and Parkhurst (2011). The current IPhreeqc version (3.7.0 – 15749) is used to calculate the equilibrium state of a chosen mineral set serving as a multicomponent geothermometer. Thermodynamic data of mineral phases is taken from Lawrence Livermore National Laboratory (llnl.dat) database. The major cations (Na, K, Ca, and Mg), and major anions (Cl, SO₄, H₂S, and HCO₃⁻) as well as SiO₂, Fe, and Al concentrations are used as input data. In addition, to calculate the saturation indices of the mineral phases, the physicochemical parameters of the geothermal brine has to be defined. Therefore, the sampling pressure, temperature, as well as pH value are essential input data. MulT_predict distributes the input data to IPhreeqc to calculate the saturation indices $SI(T)$ over a predefined temperature range $i$ for previously selected mineral phases $j$ (e.g. universally valid mineral set). To identify the equilibrium temperatures for the mineral phases ($SI = 0$), the $SI(T)$ returned from IPhreeqc are stored in a $i \times j$ matrix $A_{ij}$ and evaluated by the signum function in matrix $B_{ij}$ (Equation 2).

$$B_{ij} = \text{sign}(A_{ij}) := \lim_{k \to \infty} \frac{1 - (-1)^{k}A_{ij}}{1 + (-1)^{k}A_{ij}} = \begin{cases} -1 & \text{if } A_{ij} < 0 \\ 0 & \text{if } A_{ij} = 0 \\ 1 & \text{if } A_{ij} > 0 \end{cases}$$ (2)

Performing differences and approximate derivatives (Equation 3) upon the data returns the zero crossing of the saturation indices (Equation 1) of the chosen mineral set $j$ over their defined temperature range $i$, which are stored in a new matrix $C$.

$$C = \text{diff}(B_{ij}) = \begin{bmatrix} B(1,0) - B(0,0) & \cdots & B(1,j) - B(0,j) \\ \vdots & \ddots & \vdots \\ B(i,0) - B(i-1,0) & \cdots & B(i,j) - B(i-1,j) \end{bmatrix}$$ (3)

To find the equilibrium temperature, the data of matrix $C$ are indexed by Equation 4 and transferred into an array $D$.

$$D = \text{for} \text{ diff } (C) \neq 0$$ (4)

The resulting equilibrium temperatures $D$ and their mineral phases are both stored as cell entries in $E$. When the optimisation process is enabled, the selected sensitive parameters (boiling/dilution, pH value, and aluminium concentration) are iterated interdependently in their predefined range. After each computation, the result is also stored in the cell array $E$. Depending on the number of selected
parameters \( n \), the cell array \( E \) is stocked up in \( n \)-dimensions. To get a consistent, statistically evaluable dataset, the mineral phases and their associated equilibrium temperatures are validated in each entry. Therefore, the cell entries of \( E \) have to be cleaned up. An \( n \)-dimensional loop compares all resulting mineral phases and their temperatures from beginning to end. Missing temperature data is filled up with NaN while the names of \( j \) are added as the associated phases. Simultaneously, redundant and excess information are removed. After the completion, the procedure is executed vice versa starting at the end to check for inconsistency within the updated array \( E \). Then, the cell array \( E \) is analysed by comparing the 0.25 and 0.75 quantiles, the interquartile range IQR, as well as the 1.5*IQR outliers within each entry stored in an array \( F \) (Equation 5).

\[
F_n = [(q_{0.75} + 1.5 \cdot IQR) - (q_{0.25} - 1.5 \cdot IQR)] \; \text{for all entries in} \; E
\] (5)

Afterwards, MulT_predict statistically evaluates all \( n \)-dimensional cell entries of \( F_n \) for the minimum element of the array excluding NaN values. The global minimum represents the maximal convergence of the equilibrium temperatures of the considered mineral phases (Equation 6).

\[
\min\{f(x_0)\}, \; F_n \subseteq \mathbb{R}^+ \; \text{, } x_0 \in F_n, \; f : F_n \rightarrow \mathbb{R}^+, \; \text{if } (\forall x \in F_n) f(x_0) \leq f(x)
\] (6)

Determining the position of the global minima in the array \( F_n \), the back-calculated in-situ values of the reservoir parameters are extracted. In the last step, MulT_predict re-evaluates the in-situ reservoir parameters and re-calculates the final temperature estimation. The final results are outputted graphically and tabular.

3. Data & Results

To develop a comprehensive multicomponent geothermometer and a universally valid mineral assemblage MulT_predict has to be validated for a variety of geothermal sites. A thorough validation is only possible with datasets, where geochemical fluid analyses, as well as borehole temperatures, are available. Geothermal sites were intentionally selected in a way, that the data covers a broad range of different lithologies, temperatures, and geochemical characteristics to evolve a comprehensive tool. The geothermal fluid samples from different geothermal sites are mostly compiled from literature. In sum, eight geothermal settings were evaluated (Table 1). To validate MulT_predict, geochemical data, as well as in-situ reservoir temperature measurements of the reservoir, must be available for each site. The sites are categorised by their geology and tectonic setting: crystalline basement of a rift basin, sedimentary back-arc basin dominated by continental facies, foreland basin dominated by marine facies, sedimentary basin dominated by marine facies, volcanic facies dominated by andesite to rhyolite at subduction zones, and basaltic facies on the mid-ocean ridge induced by a hotspot.
Table 1: Collocation of the lithology, geological setting, location, and references of the geothermal wells for the validation of MulT_predict.

<table>
<thead>
<tr>
<th>Lithology</th>
<th>Setting</th>
<th>Location</th>
<th>Reference</th>
</tr>
</thead>
<tbody>
<tr>
<td>Granite</td>
<td>Basement (rift basin)</td>
<td>Upper Rhine Graben</td>
<td>Sanjuan et al. (2001) Schindler et al. (2010)</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>Dezayes et al. (2013) Sanjuan et al. (2016)</td>
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<td></td>
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<td>Vidal et al. (2019) Vidal and Genter (2018)</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>Dezayes et al. (2013) Sanjuan et al. (2016)</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>Vidal et al. (2019) Vidal and Genter (2018)</td>
</tr>
<tr>
<td>Lacustrine facies</td>
<td>Back-arc basin</td>
<td>Pannonian Basin</td>
<td>Varsányi et al. (1997)</td>
</tr>
<tr>
<td>Marine facies, Malm</td>
<td>Foreland basin</td>
<td>German Molasse Basin</td>
<td>Internal communication</td>
</tr>
<tr>
<td>Rhyolite, Andesite</td>
<td>Subduction zone</td>
<td>Waiotapu</td>
<td>Banwell (1959)</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>Ellis and Mahon (1977) Giggenbach et al. (1994)</td>
</tr>
<tr>
<td>Andesite</td>
<td>Subduction zone</td>
<td>Miravalles</td>
<td>Dennis et al. (1989) Gherardi et al. (2002)</td>
</tr>
<tr>
<td>Dacite</td>
<td>Subduction zone</td>
<td>El Tatio</td>
<td>Ellis and Mahon (1977) Giggenbach (1978)</td>
</tr>
<tr>
<td>Basalt, hyaloclastite</td>
<td>Hotspot</td>
<td>Iceland</td>
<td>Guðmundsson and Arnórsson (2002)</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>Óskarsson et al. (2015)</td>
</tr>
</tbody>
</table>

The data representing the granitic crystalline basement in the Upper Rhine Graben (URG) is presented by Sanjuan et al. (2001) and Schindler et al. (2010) for GPK 1 and 2 in Soultz-sous-Forêts, Dezayes et al. (2013) and Vidal et al. (2019) for GRT-1 in Rittershoffen, and Sanjuan et al. (2016) as well as Vidal and Genter (2018) for GTLA-1 in Landau and INSH in Insheim. The continental sedimentary facies is represented by lacustrine to fluvial sedimentary sequences in the Pannonian Basin published by Varsányi et al. (1997). Malm layers in the German Molasse Basin represent marine facies in a foreland basin (internal communication with power plant operators, Appendix A). Marine sedimentary facies from Dogger layers in the Paris Basin were published by Michard and Bastide (1988), Marty et al. (1988), and Criaud et al. (1989). The volcanic facies are summing up different types of reservoir rock around the Pacific Ring of Fire. For Waiotapu in New Zealand, rhyolite and andesite reservoir formations are hosting the geothermal wells published by Banwell (1959), Ellis and Mahon (1977), and Giggenbach et al. (1994). Further, data from the wells of the andesite reservoir formation in Miravalles, Costa Rica, are presented by Dennis et al. (1989), and Gherardi et al. (2002). Lastly, the geochemical data presented by Ellis and Mahon (1977), and Giggenbach (1978) of a dacite reservoir in an ignimbrite formation at El Tatio, Chile, are used. The basalt and hyaloclastite facies are visualised by data from
Krafla (Guðmundsson and Arnórsson, 2002), and Reykjanes (Óskarsson et al., 2015). For reference, the artificial standard of ocean water is illustrated (D19 Committee).

To establish the new procedure for unknown temperature estimations three steps had to be passed. First, setting-specific mineral sets were developed for known mineralogical and temperature data. Second, coinciding mineral phases of setting-specific mineral sets are combined into a universally valid set. Third, to refine the general temperature estimation, a procedure of outlier removal has to be implemented. The results of the three steps are visualised in Figure 1.

For each geothermal setting, the mineral set for reservoir temperature estimation is compiled individually (Appendix B). Creating these unique sets is time-consuming. Therefore, if known, the observed mineral composition of the reservoir rock should be transferred into a mineral set. Hence, the main mineral phases of the reservoir rock, as well as secondary and accessory minerals, have to be considered. The resulting mineral assemblages have to be refined until the optimised saturation curves converge on each other, minimising the uncertainty of the temperature estimation (c.f. Equation 5, 6).

Therefore, mineralogical foreknowledge of the reservoir rock composition and its secondary mineralisation is preferable in general. Nevertheless, in some cases this information is not available or unknown, thus, a predefined universal mineral set is presented. This universally valid mineral set consists of the most common rock-forming minerals as well as secondary and accessory minerals. The focus of the universal set is its comprehensive applicability while providing still reasonable temperature estimations. Together with the upcoming procedure of outlier removal, the temperature estimations get more precise. Thus, all evolved setting-specific mineral sets were compared among themselves. As a result, in most of the sets, an overlap of mineral phases is repeatedly equilibrated.

Combining them, a universally valid mineral set has been established, which can be applied on a worldwide scale independently of reservoir mineralogy and setting. This universally valid set consists of quartz, K-feldspar, microcline, albite, muscovite, illite, diaspore, analcime, scolecite, anhydrite, kaolinite, and pyrophyllite (Appendix B). Figure 1 illustrates the outlier removal procedure to obtain the most reasonable temperature estimation. In the diagram, three temperature estimations per geothermal setting are shown. The orange box indicates the measured in-situ temperature corresponding to the open hole section within the example. The first boxplot (magenta) illustrates the temperature estimation by just applying the universally valid mineral set. In the next step, for the second boxplot in green, two statistical outliers of the universal set are removed. This corresponds to mineral phases \( M \), which are exceeding 1.5 times the interquartile range (IQR) the most (Equation 7).

\[
M \subseteq \mathbb{R}^+, y \in M, \begin{cases} 
\text{if } y > y_{\text{median}} + 1.5 \times IQR \\
\text{if } y < y_{\text{median}} - 1.5 \times IQR 
\end{cases}
\]

This outlier removal represents the procedure, which is used to evaluate new geochemical data with unknown mineralogy. The third boxplot in blue visualises the best fitting result obtained by developing
an individual mineral set for each setting, as mentioned in Appendix B. After the universally valid mineral set for reservoir temperature estimation has been introduced, it can be compared to the results of the outlier removal and each setting-specific mineral set (Appendix B). Comparing the three boxplots in Figure 1, the shift of temperature estimation towards the measured in-situ temperature is evident. In each case, the overall spread of the plot is decreasing as well as a decreasing or steady IQR. Only for the carbonate facies of the Paris Basin and the Molasse Basin, calcite and dolomite have to be added to the universally valid mineral set to reconstruct reservoir conditions and temperature estimations more precisely.

Figure 1: Comparison of three temperature estimations for an exemplary well of individual geothermal settings around the world (Krafla on Iceland, Soultz-sous-Forêts in the Upper Rhine Graben, Waiotapu in New Zealand, El Tatio in Chile, Miravalle in Costa Rica, Makó in the Pannonian Basin, Unterhaching in the German Molasse Basin, and Evry in the Paris Basin). Straight lines separate different reservoir rock compositions (basaltic, crystalline, volcanic, clastic, and marine facies). The orange box indicates the measured in-situ temperature in the open hole section of the well. The first boxplot (magenta) visualises the temperature estimation with the original universally valid set. The secondary boxplot is obtained by reducing the outermost mineral phases within the universal set and recalculating the temperature estimation (outlier reduction in green). In comparison, the third boxplot (blue) is the best-fitting mineral set individually developed for each setting (cf. Appendix B).
For Iceland, the outlier removal reduces the IQR by 50% to 7 K, while the median temperature remains at 235°C, fitting the best-fit temperature and the temperature log. For URG, the overall uncertainty decreases by 12% due to the outlier removal, but further refinement of the mineral set is necessary to reach best-fit conditions at 166°C. At Waiotapu, the necessity of outlier removal for the magenta boxplot is vivid. The removal reduces the spread by 59 K and emphasises the median temperature at 207°C within the measured temperature. In addition, the IQR (4 K) of the adjusted universally valid mineral set equals the best-fitting result. For El Tatio, the overall spread reduces by 50% due to the outlier removal and increases the median temperature to its final result at 228 °C, matching the measured in-situ temperature. The outlier removal for Miravalles reduces the spread by 62 K and the IQR by 45%. Likewise, the adjusted universally valid mineral set resembles the best-fitting plot. For the Pannonian Basin, the procedure shifts the median temperature by 22 K into the measured temperature range. Compared to the best-fitting plot, the mineral assemblage can be further refined to increase accuracy. For both marine facies, the outlier removal reduces the uncertainties but the temperature estimation does not fit the in-situ temperature. For the Molasse Basin, the spread minimises by 79%, while for the Paris Basin its halves. Due to the lack of carbonate mineral phases within the universally valid mineral set, the median of the temperature estimation in the Molasse is 20 K beneath the best fit and in the case of Paris Basin 16 K.

4. Discussion

For the illustration of coherences of the properties of brines from different geothermal settings, geochemical key parameters are analysed. These parameters are relevant to multicomponent geothermometry and can explain the plausibility of a generally valid mineral set. For this purpose, the major chemical components are used (Na, K, Ca, Mg, Cl, SO₄, HCO₃, and additionally pH). To graphically cluster the brines according to the surrounding lithology, strongly temperature-sensitive components such as SiO₂ were omitted. Thus, the major chemical components of dissolved mineral phases used in geothermometry are evaluated. Thus, the graphical single-point method by Langelier and Ludwig (1942) is modified. In the original two-dimensional plot, the pH value of the fluid is added as the z-axis. Furthermore, the total dissolved solids TDS are projected as sphere sizes

\[ s = \log (\text{TDS} \times 10) \]  

(8)

To display the differences in sphere sizes homogenously, the TDS is multiplied by ten and then the decadic logarithm is applied. Hence, standard fluid analysis of the geothermal brines are plotted in the modified Langelier-Ludwig diagram (Figure 2).
Figure 2: Modified Langelier-Ludwig diagram for classification of geothermal settings in different facies. The pH value was added as a third dimension (z-axis) as well as the total dissolved solids (TDS) visualised in sphere size.

By plotting the geochemistry of the different geothermal sites clustering can be observed. High saline brines from the Dogger formation in the Paris Basin, the saltwater intrusion in the wells of the Reykjanes Peninsular, as well as the samples from the Upper Rhine Graben, are clustering beneath the salinity of seawater at Na+K 40% and SO$_4$+Cl 50%. The shift in pH value is a function of temperature and salinity (Ellis, 1970). Increasing temperature and salinity causes the pH value to decrease. The marine facies samples cluster near-neutral pH values. This corresponds to buffering reaction within the carbonates (Malm, Dogger) due to calcite solubility equilibrium and temperature-dependent auto-dissociation within the fluid (Ellis, 1963). Therefore, the brines in the URG (TDS ~ 100 g/L) and high-temperature settings in Rekjanes (exceeding 300°C) have lower pH values. For the volcanic facies, Miravalles and El Tatio are forming the main cluster around Na+K 47% and SO$_4$+Cl 50% with a pH of 7.5. The samples of Waiotapu have a shift to higher pH values. For Waiotapu, Giggenbach et al. (1994) proposed a low content of CO$_2$ within the parent magma and removal of CO$_2$ as calcite through Ca-Al-silica interaction. In addition, there is degassing and dilution of the fluid before reaching the wells. The
wells in Kafla and Námafjall are clustering at the highest pH values. These waters are low mineralised and of meteoric origin. Due to degassing of CO₂ and H₂S the pH is increased as well as a bicarbonate trend up to 15% of HCO₃ corresponding to an increase in magmatic activity underneath the well K-20 (Guðmundsson and Amóðsson, 2002). For samples from the Pannonian Basin, the TDS is low. The fluid chemistry is clustering next to Waiotapu samples. Similar to the bicarbonate trend in Icelandic samples, the Pannonian chemistry shows HCO₃ influences increasing with temperature and depth corresponding to lacustrine carbonates within the formations (Varsányi et al., 1997). The clustering of samples in the Langelier-Ludwig diagram (Figure 2) visualises similarities within the unique signature of each geothermal setting. In addition, the influence of evaporates and seawater can clearly be distinguished from samples of meteoric origin. The distribution of pH values represents a variety of geochemical processes coupled to the individual settings. The pH value sums up buffer reactions, degassing processes, and the impact of salinity and temperature. Therefore, the geochemistry of the geothermal fluid is an indicator of the mineral composition leached out of the reservoir rock. Thus, these similarities in the clustering are reflected in the universally valid mineral assemblage presented for reservoir temperature estimations.

Further, the optimisation process within MulT_predict is evaluated. Therefore, a synthetic brine is set up and processed by MulT_predict to back-calculate the initial brine temperature. In the next step, all parameters of the optimisation processes are tested individually. In this case, the influence of salinity, steam loss and dilution, the pH value as well as the Al concentration are examined. Therefore, the synthetic brine is increasingly perturbed stepwise for one of these parameters at once. This is resumed until the numerical limits of the optimisation of MulT_predict are reached. Thus, the individual optimisation processes can be evaluated. Lastly, the synthetic brine is perturbed for all parameters at once. The steam loss and dilution is increased stepwise, while random pH values and element concentrations in a predefined range are added. In this case, MulT_predict’s optimisation process is used interdependently to back-calculate reservoir conditions.

The synthetic mineral assemblage is equilibrated at 150°C and has a pH value of six. The mineral assemblage composes of phases of the universally valid set: quartz, microcline, albite, calcite, anhydrite, muscovite, illite, and stilbite. The resulting equilibrated fluid lost some mass while reacting with stilbite (0.899 kg remaining) as well as the pH value increased to 6.743 due to changes in the activity of hydrogen ions. To revered initial conditions, the fluid mass is set back to 1 kg. In the next step, each parameter is varied individually and stepwise around its initial value to perturb the equilibrium between mineral phases. Then, MulT_predict’s optimisation process is used to reconstruct the equilibrium conditions of the fluid and determine the initial equilibrium temperature. First, the salinity is increased in 100 steps from zero molar up to five molar by adding NaCl to the solution. In Figure 3, for each increment, the MulT_predict computes the temperature estimations which are
plotted in the diagram. The computed temperature estimation is constantly at 148°C close to the initial conditions of 150°C, thus Mult_predict temperature estimations show virtually no sensitivity to increasing salinity.

Figure 3: Temperature estimations corresponding to salinity changes from zero to five molar by adding NaCl to the solution. The red line is indicating the initial equilibrium temperature of the synthetic fluid. The red line indicates the equilibrium temperature of 150°C.

The assessment of the sensitivity of changes by steam loss and dilution in the fluid is displayed in Figure 4. Therefore, the moles of the fluid is altered by 1% per step. For dilution, 0.555 moles of pure water is added per increment. Contrary, 0.555 moles of pure water is subtracted mimicking steam loss.

In Mult_predict’s optimisation process, these changes are back-calculated. On the left side a) of Figure 4, Mult_predict’s computed concentration error is plotted over the percentage of changes to the fluid concentration as well as the resulting temperature estimation on the right side b).

Figure 4: On the left side a), the error of the reconstructed fluid concentration is plotted over the changes to the mass of water within the fluid. The dashed red line indicates the targeted error. In the right graph b), the corresponding temperature estimations are visualised, while the solid red line indicates the targeted temperature of 150°C.
For perturbations within ±20% of dilution or steam loss, the optimisation process reconstructs the fluid with small errors of 3 percentage points on average (cf. dashed, red line in Figure 4). Regardless of whether steam loss or dilution, at higher changes MuLT_predict starts to underestimate these perturbations. Thus, the difference between the synthetic changes in the fluid and the reconstruction is rising. This curve shape corresponds to the geochemistry in the fluid. Reducing 50% of water doubles the element concentration. In contrast, dilution of 100% is halving the concentration. Comparing the resulting element concentration leads to a continuous increase in error. Nevertheless, the temperature estimations on the right side of Figure 4 have a maximum spread of five Kelvin (144°C to 149°C) and are on average 145°C. The red line indicates the equilibrium temperature of the synthetic set.

Further, changes in the pH value are evaluated in Figure 5. The pH value is perturbed between a value of five and seven in 200 increments. The resulting pH value of the optimisation process is plotted in a) over the synthetic pH variation. In b), the resulting pH value is illustrated over the temperature estimation.

Figure 5: On the left side a), the reconstructed pH value of the fluid is plotted over its variation between five and seven. The dashed red line indicates the initial equilibrium pH at 6.743. In the right graph b), the corresponding temperature estimations are visualised, while the solid red line indicates the targeted temperature of 150°C.

Figure 5 a) visualises the difference between the resulting optimised pH value and the initial equilibrate pH (6.743) indicated by the dashed, red line. pH values increasing 6.743 cannot be back-calculated by IPhreeqc because of a thermodynamic equilibrium gap for the aluminium concentration at higher pH. Therefore, MuLT_predict is also capped at this level, not allowing interdependent optimisation yet. The estimations of the pH value show a pattern corresponding to geochemical adaptations of IPhreeqc iteration steps. Because of the loss in precision due to no redox buffering, IPhreeqc alters parameters automatically. Therefore, the redox potential is varied so the balance equations can be solved to obtain a chemical equilibrium (Parkhurst and Appelo, 2013). This leads to a recommencement at pH 6.443 and a steady decline of the optimised pH value towards the initial value while the redox potential is
adjusted. In Figure 5 b), optimised pH values in the range of 7.303 to 7.193 reach a temperature estimation of 144°C. For values from 7.183 to 6.883 the estimation is 145°C and for smaller pH, a temperature of 147°C is calculated.

Finally, variations in the aluminium concentration are examined. In 160 steps, 80% of the initial aluminium concentration is added and subtracted. Figure 6 illustrates the optimised aluminium concentration over the shift in concentration as well as the resulting temperature estimation.

Figure 6: On the left side a), the reconstructed aluminium concentration is plotted over its variation between -80% and +80%. The dashed red line indicates the initial aluminium concentration of 0.00303 mmol/l. In the right graph b), the corresponding temperature estimations are visualised, while the solid red line indicates the targeted temperature of 150°C.

Figure 6 a) shows a steady back-calculated aluminium concentration around 0.00267 mmol/l (11% less the initial 0.00303 mmol/l) for raising concentrations. With decreasing aluminium concentration, IPhreeqc starts to iterate the equilibrium calculation to converge the chemistry. Due to the variation in the overall small aluminium concentration, errors accumulate while running the simulation. Thus, the program automatically attempts to solve the calculation by altering and combining tolerances and step sizes to fit the solution (Parkhurst and Appelo, 2013). Similarly, the redox potential is adjusted. Therefore, the aluminium concentration is fluctuating from 0.00245 mmol/l to 0.00269 mmol/l and reaches the maximum of 0.00304 mmol/l at -80%. However, the temperature estimation is steady at 145°C once rising to 147°C at -80%.

Comprising all cases, MulT_predict is underestimating the temperature estimations, anyhow not exceeding 6 K (4% error). Only optimising individual parameters does not take chemical interactions into account. As mentioned in the methodology, these sensitive parameters are coupled due to secondary processes. Therefore, in a second step, the back-calculation process is tested by optimising the parameters interdependently. Therefore, in 5%-steps the fluid concentration was perturbed again between -45% to 70%, as well as the values for the pH and Al concentration have been randomised. For the pH, random values between pH 5 and 7 and for the aluminium concentration values between
0.001 mmol/l and 0.006 mmol/l were generated. Currently, MuIT_predict is allowed to simultaneously optimise all sensitive parameters interdependently.

In Figure 7, the fluid concentration, pH value, and aluminium concentration are optimised simultaneously. The interdependent estimations from test step 1 were plotted into the results of the individual optimisation processes, which were paled out. In a), the average concentration error decreases by 2 percentage points compared to the independent back-calculation. The pH values in b) and the aluminium concentrations in c) are fitting the target values more accurate than the individual
optimisation process. For the pH value, the maximum deviation is 0.3 less than the targeted pH. On average, the variance of the interdependent pH optimisation is 0.056, which is negligible compared to the mean deviation of 0.32 for the independent calculation. For the aluminium concentration, the average deviation is 0.164 µmol/L about 5% of the target concentration. Therefore, interdependent optimisation is circa 50% more precise than independent optimisation. In addition, the temperature estimations in d) improved to a mean value of 147°C. Especially the reconstruction of the pH value and the aluminium concentration shows the importance of an interdependent optimisation process to reflect geochemical changes within the fluid.

5. Conclusion

MulT_predict is a robust multicomponent geothermometer with a build-in optimisation process to reconstruct the initial in-situ reservoir conditions and temperature from a chemically perturbed geothermal fluid sample. The temperature estimations are based on a standard chemical analysis of the geothermal fluid composition. No sophisticated sampling methods nor analyses are needed. A numerical reconstruction process of the in-situ chemical conditions is implemented to correct secondary perturbation of the fluid sample. The joint optimisation of coupled key parameters (boiling/dilution, pH value, and aluminium concentration) allows for the determination of precise reservoir temperatures. A universally valid mineral set is deduced allowing the calculation of reservoir temperatures. Regardless of the setting and the reservoir mineralogy, the universally valid mineral set provides a great advantage when only little or no knowledge of the subsurface mineralogy is available. The implementation of a statistical outlier removal refines the mineral assemblage and improves the temperature estimation further. Therefore, MulT_predict can be used as an early phase greenfield exploration tool, which was validated at multiple geothermal sites worldwide.

The emphasis of the study was the enhancement of the applicability of MulT_predict on a worldwide scale, as well as the focus on the performance of the optimisation processes and its validation. The newly developed universally valid mineral set allows a first temperature estimation for geothermal systems of unknown subsurface. The set contains twelve mineral phases (quartz, K-feldspar, microcline, albite, muscovite, illite, diaspore, analcime, scolecite, anhydrite, kaolinite, and pyrophyllite). These mineral phases are selected according to their common appearance in geothermal systems worldwide causing similar chemical signatures (in terms of key parameters for multicomponent geothermometry) to fluids of very different settings. They consist of key mineral phases of major rock types, accessory minerals, secondary mineral phases, as well as polymorphic mineral phases. The developed universally valid mineral set is tested and validated at eight different geothermal sites (Iceland, Upper Rhine Graben, German Molasse Basin, Paris Basin, Pannonian Basin,
Waiotapu, Miravalles, and El Tatio). This mineral set combines mineral phases of the associated geology of the settings (basaltic, volcanic, marine, and continental facies as well as crystalline basement).

The functionality of the optimisation processes is tested by perturbing an equilibrated synthetic mineral assemblage. Thus, four critical parameters are investigated: the salinity of the fluid, changes in the mass of water (steam loss and dilution), as well as alterations in the pH value, and the aluminium concentration. First, each optimisation process is performed individually. Perturbation of the salinity does not affect the temperature estimation of MulT_predict. Perturbation in the mass of water, the pH value, and aluminium concentration leads to an average temperature estimation of 145°C and therefore, a reasonable error of 3.4%. For the interdependent optimisation process, the back-calculations for pH value and aluminium concentration resemble the initial conditions. The average temperature estimation is 147°C, 3 K less than the initial equilibrium temperature of 150°C. Considering all cases, MulT_predict and its build-in optimisation processes provide precise temperature estimation. Thereby, the interdependent optimisation process can back-calculate reservoir conditions more accurately than an individual parameter optimisation. Thought, the calculation of the interdependent optimisation process is more computation-intensive. Therefore, the number of coupled sensitive parameters should be optimised jointly. Overall, the introduced universally valid mineral set expands the usability of MulT_predict and its applicability for the user. In addition, the effectiveness of interdependent optimisation processes is verified, resulting in improved temperature estimations. Eventually MulT_predict, as a fully integrated comprehensive multicomponent geothermometer.

6. Data Availability

Upper Rhine Graben: Sanjuan et al. (2001); Schindler et al. (2010); Dezayes et al. (2013), Sanjuan et al. (2016); Vidal and Genter (2018); Vidal et al. (2019). Pannonian Basin: Varsányi et al. (1997).
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**Competing interest**
The authors declare that they have no competing interests.

**Authors’ contributions**
**Lars Ystroem**: Conceptualisation, Data curation, Investigation, Methodology, Software, Writing - Original Draft. **Fabian Nitschke**: Conceptualisation, Investigation, Writing - Review & Editing, Supervision. **Thomas Kohl**: Writing - Review & Editing, Supervision, Funding acquisition.

**Funding**
See section “Acknowledgements”.
Appendices

Appendix A: Anonymised data from power plant operators from the German Molasse Basin. Element concentrations are presented in mg/l.

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Appendix B: Individual setting-specific minerals sets for reservoir temperature estimation.

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