

First principles simulation of resistivity recovery in irradiated beryllium

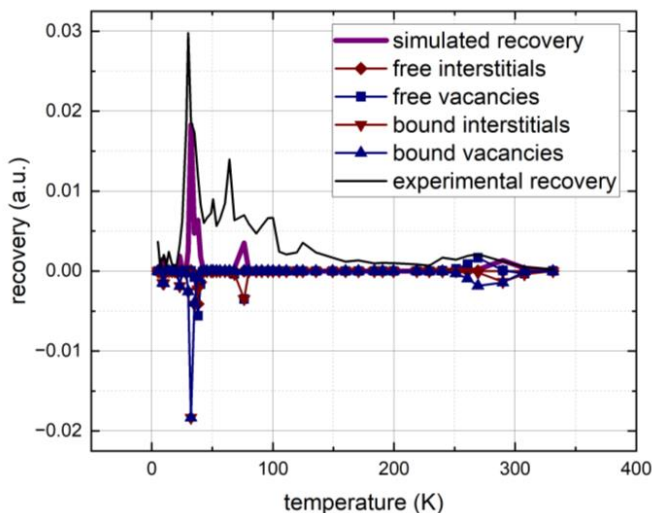
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Future fusion devices like ITER or DEMO require closed fuel cycles. These vitally depend on neutron multiplying materials as part of a breeding blanket module like beryllium pebbles in the European Helium-Cooled Pebble-Bed. During operation the beryllium pebbles will accumulate point defects, tritium, and helium due to inevitable exposure to highly energetic neutron irradiation as emitted by the fusion plasma. A detailed knowledge of the characteristics of point defects is decisive for reliable simulations of microstructure evolution in irradiated beryllium. Such models are a prerequisite for predicting tritium inventory during operation as well as after the blanket's end of life since tritium retention and release is the paramount safety concern.

A well-established experimental approach to assess the dynamics of relevant atomic defects consists in measuring electrical resistivity recovery (ERR) after irradiation during annealing. Within this approach, temperatures corresponding to electrical recovery steps are correlated with activation energies which are associated with different type of reactions between defects.

In this work, results of our ongoing efforts to model and understand the ERR of



beryllium are presented. To that end, we introduce a rate equation-based approach to model ERR spectra (see picture below) utilizing density functional theory results as input. Within this approach, electrical resistivity recovery models comprising the volume of spontaneous recombination of monovacancies and self-interstitial atoms in beryllium as well as various additional defects are considered. As a result, an intricate interplay between different defect dynamics is

uncovered, suggesting a clear route for further research to obtain systematically improved electrical resistivity recovery models.

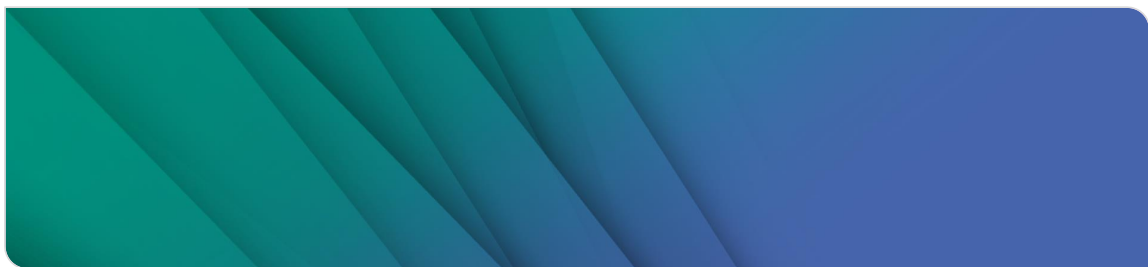
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Outline

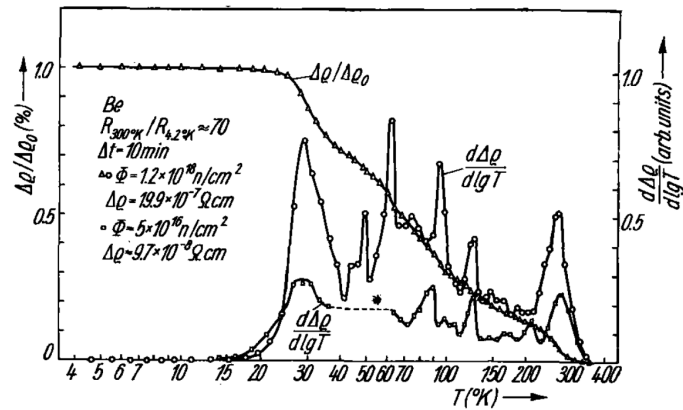


- Resistivity Recovery Experiments
- Resistivity Recovery Modelling
 - Relevant Be properties
 - Model derivation
 - Various models
- Conclusions & outlook

Resistivity recovery experiment(s by example)



- sample preparation
 - cool to 4.2 K
 - measure resistivity
 - irradiate
 - measure resistivity
- measurements
 - do annealing cycle
 - heat
 - hold
 - cool
 - measure resistivity
 - repeat at higher T
- process spectrum



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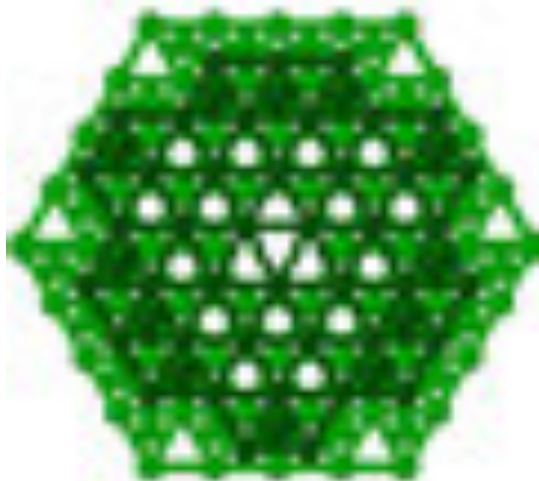
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Model-relevant Be properties (from DFT)



- HCP structure
- **AB**-stacked layers
- mono vacancies
 - immobile (0.8 eV)
- basal interstitials
 - mobile (0.12 eV)
- spontaneous recombination hull
 - oblate spheroid
 - with (very) fast recombination



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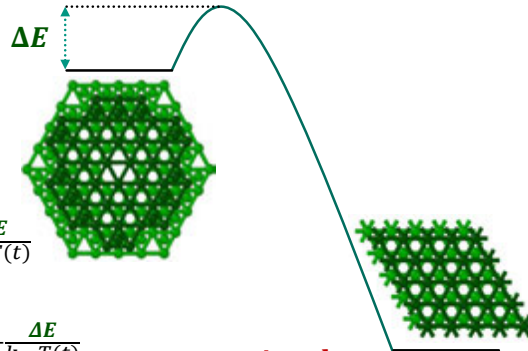
Deriving a hull-only recovery model ...

... as an initial value problem (IVP):

- recombination from hull
 - various small barriers $\Delta E < 0.12 \text{ eV}$
 - $c_0 \approx 1 \%$ per hull defect pair
 - ordinary differential equations (ODEs)

$$\frac{d}{dt} c \left(\text{hull} \right) = -c \left(\text{hull} \right) \cdot \nu \cdot e^{-\frac{\Delta E}{k_B \cdot T(t)}}$$

$$\frac{d}{dt} c \left(\text{defect} \right) = + \sum c \left(\text{hull} \right) \cdot \nu \cdot e^{-\frac{\Delta E}{k_B \cdot T(t)}} \propto \text{recovery signal}$$



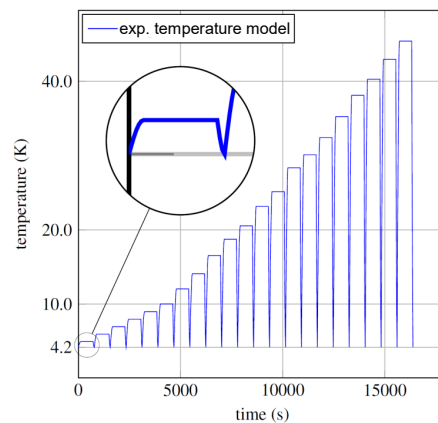
Solving the hull-only recovery model's IVP


- ODEs

$$\frac{d}{dt} c \left(\text{hull} \right) = -c \left(\text{hull} \right) \cdot \nu \cdot e^{-\frac{-\Delta E}{k_B \cdot T(t)}}$$

$$\frac{d}{dt} c \left(\text{defect} \right) = \sum c \left(\text{hull} \right) \cdot \nu \cdot e^{-\frac{-\Delta E}{k_B \cdot T(t)}}$$

- $T(t)$ from experiment
- initial values of $\approx 1\%$ per defect



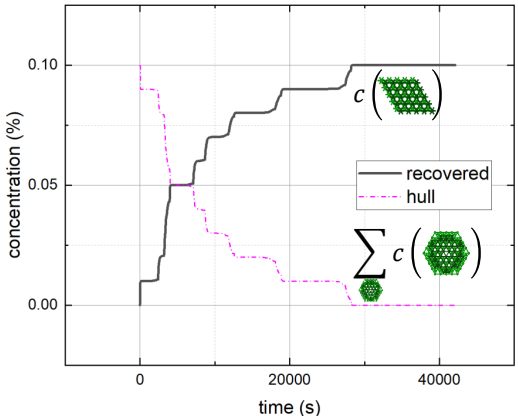


Solving the hull-only recovery model's IVP


- ODEs

$$\frac{d}{dt} c(\text{hex}) = -c(\text{hex}) \cdot \nu \cdot e^{\frac{-\Delta E}{k_B \cdot T(t)}}$$

$$\frac{d}{dt} c(\text{hull}) = \sum c(\text{hex}) \cdot \nu \cdot e^{\frac{-\Delta E}{k_B \cdot T(t)}}$$
- $T(t)$ from experiment
- initial values of $\approx 1\%$ per defect
- symmetric hull and recovery evolution
- sloped step patterns from annealing cycles



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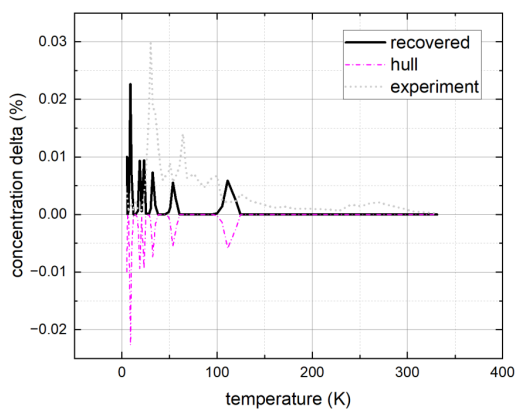


Solving the hull-only recovery model's IVP


- ODEs

$$\frac{d}{dt} c(\text{hex}) = -c(\text{hex}) \cdot \nu \cdot e^{\frac{-\Delta E}{k_B \cdot T(t)}}$$

$$\frac{d}{dt} c(\text{hull}) = \sum c(\text{hex}) \cdot \nu \cdot e^{\frac{-\Delta E}{k_B \cdot T(t)}}$$
- $T(t)$ from experiment
- initial values of $\approx 1\%$ per defect
- symmetric hull and recovery evolution
- sloped step patterns from annealing cycles
- +/- peaks show in/decreasing concentration
- lowest-energy hull pairs decay early
- initial values are important free parameter



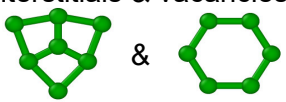
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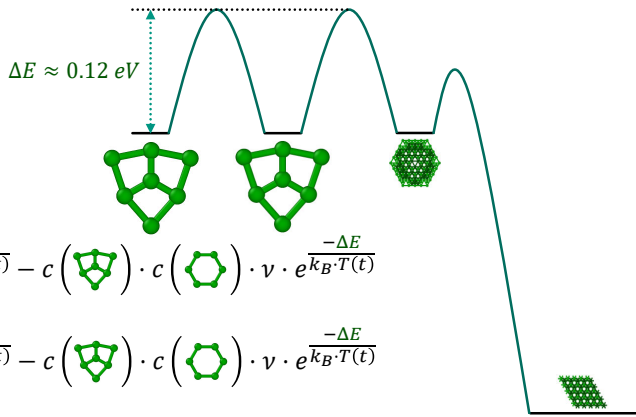


Defect mobility-enhanced recovery model ...

... by adding:

- free interstitials & vacancies


&




- new corresponding ODEs

$$\frac{d}{dt} c(\text{int}) = \sum_{\text{vac}} c(\text{vac}) \cdot \nu \cdot e^{\frac{-\Delta E}{k_B \cdot T(t)}} - c(\text{int}) \cdot c(\text{vac}) \cdot \nu \cdot e^{\frac{-\Delta E}{k_B \cdot T(t)}}$$

$$\frac{d}{dt} c(\text{vac}) = \sum_{\text{int}} c(\text{int}) \cdot \nu \cdot e^{\frac{-\Delta E}{k_B \cdot T(t)}} - c(\text{int}) \cdot c(\text{vac}) \cdot \nu \cdot e^{\frac{-\Delta E}{k_B \cdot T(t)}}$$

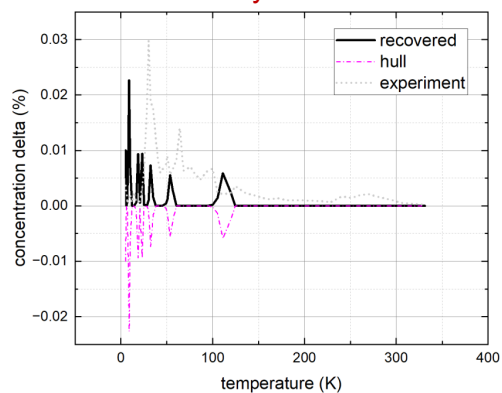
- additional terms in existing ODEs

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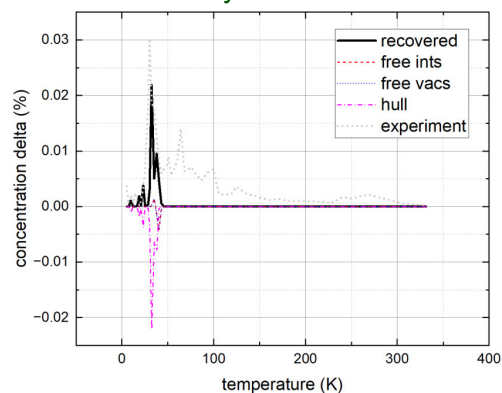


Defect mobility-enhanced recovery spectrum


hull-only model



defect mobility-enhanced model

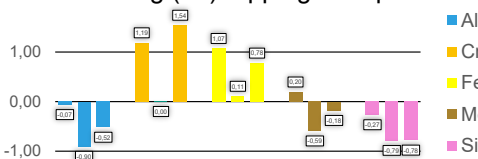


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Impurity-enhanced recovery models ...

... from adding (de)trapping at impurities

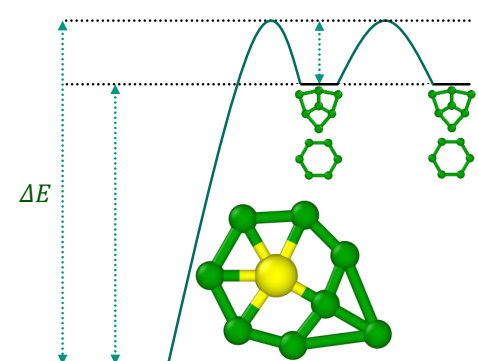


- Al
- Cr
- Fe
- Mg
- Si

■ interstitials (de)trapping at Fe adds ODEs


$$\frac{d}{dt} c(\text{int}) = + c(\text{vac}) \cdot c(\text{int}) \cdot v \cdot e^{\frac{-0.12 \text{ eV}}{k_B \cdot T(t)}} - c(\text{int}) \cdot v \cdot e^{\frac{-\Delta E}{k_B \cdot T(t)}}$$

$$\frac{d}{dt} c(\text{vac}) = - c(\text{int}) \cdot c(\text{vac}) \cdot v \cdot e^{\frac{-0.12 \text{ eV}}{k_B \cdot T(t)}} + c(\text{int}) \cdot v \cdot e^{\frac{-\Delta E}{k_B \cdot T(t)}}$$



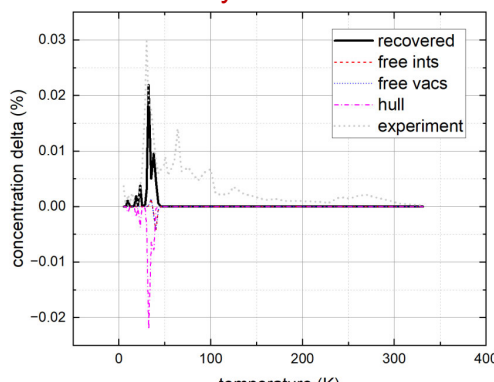
- analogous vacancy (de)trapping ODEs
- additional terms in existing ODEs

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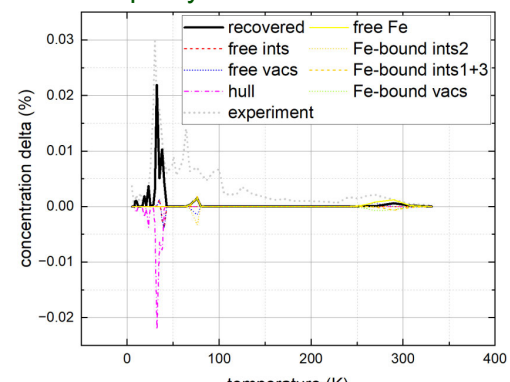


Fe impurity-enhanced recovery spectrum

defect mobility-enhanced model



impurity-enhanced model

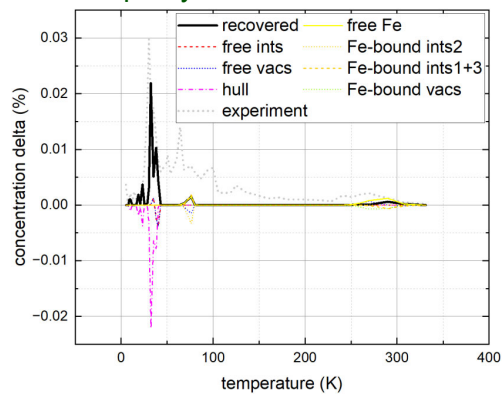


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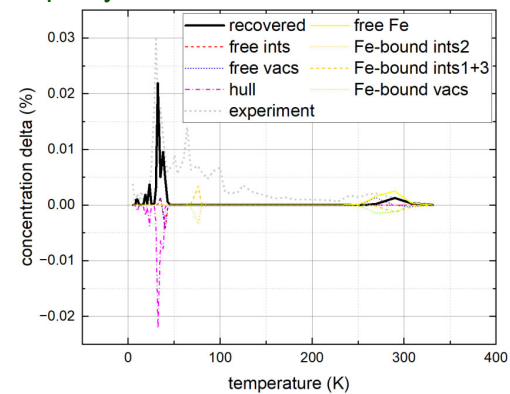
Fe impurity-enhanced recovery spectra



impurity-enhanced model



impurity-enhanced, vac-starved model



Conclusions & outlook



- first peaks due to closely correlated pairs
 - reasonable defect concentrations sufficient
 - gaps likely due to non-exhaustive set of pairs
- diffusion onset decisive for later spectrum
- last peaks due to mobile vacancies
 - here from vacs weakly bound to Fe
- interdependent dynamics of different traps
 - e.g. different traps at Fe (and additional ones ...)
- intermediate peaks *likely not* due to impurities
 - concentrations *too low*
 - might still contribute some peaks
- additional Be-only defects to be considered
- model can be extended to calorimetry signals

