

First Search for Axionlike Particles in a Storage Ring Using a Polarized Deuteron Beam

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Based on the notion that the local dark-matter field of axions or axionlike particles (ALPs) in our Galaxy induces oscillating couplings to the spins of nucleons and nuclei (via the electric dipole moment of the latter and/or the paramagnetic axion-wind effect), we establish the feasibility of a new method to search for ALPs

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in storage rings. Based on previous work that allows us to maintain the in-plane polarization of a stored deuteron beam for a few hundred seconds, we perform a first proof-of-principle experiment at the Cooler Synchrotron (COSY) to scan momenta near 970 MeV/c. This entails a scan of the spin-precession frequency. At resonance between the spin-precession frequency of deuterons and the ALP-induced electric dipole moment (EDM) oscillation frequency, there is an accumulation of the polarization component out of the ring plane. Since the axion frequency is unknown, the momentum of the beam and, consequently, the spin-precession frequency are ramped to search for a vertical polarization change that occurs when the resonance is crossed. At COSY, four beam bunches with different polarization directions are used to make sure that no resonance is missed because of the unknown relative phase between the polarization precession and the axion or ALP field. A frequency window of 1.5 kHz width around the spin-precession frequency of 121 kHz is scanned. We describe the experimental procedure and a test of the methodology with the help of a radio-frequency Wien filter located on the COSY ring. No ALP resonance is observed. As a consequence, an upper limit of the oscillating EDM component of the deuteron as well as its axion coupling constants are provided.

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I. INTRODUCTION

In 1977, Peccei and Quinn proposed an extension of the Standard Model of particle physics to include a global chiral symmetry in order to explain the small if not vanishing magnitude of the CP violation in quantum chromodynamics (QCD) [1,2]. Since this so-called Peccei-Quinn (PQ) symmetry is necessarily spontaneously broken, the existence of the associated Nambu-Goldstone boson was conjectured by Weinberg [3] and Wilczek [4]—the latter coining the name axion for this pseudoscalar particle which acquires a small mass term via nonperturbative QCD effects. Since it was initially assumed that the order parameters of the spontaneous breaking of the PQ symmetry, f_a , would be the electroweak (Fermi) vacuum expectation value v_F [5], the original axion model by Peccei and Quinn could be rather quickly ruled out by beam-dump experiments; see, e.g., Ref. [6]. The focus then changed to the class of the so-called invisible axions with $f_a \gg v_F$, which are limited by two types of models, the KSVZ model due to Kim [7] and Shifman, Vainshtein, and Zakharov [8] and the DFSZ model due to Dine, Fischler, and Srednicki [9] and Zhitnitsky [10]. For the canonical QCD axion, which solves the strong CP problem, a relation between its mass m_a and the order parameter f_a can be determined [11], which to leading order reads

$$m_a = \frac{\sqrt{z}}{1+z} m_\pi f_\pi \frac{1}{f_a}. \quad (1)$$

Here, m_π and f_π are the mass and axial decay constant (chiral order parameter), respectively, of the pion, while $z = m_u/m_d \approx 0.474$ (see Ref. [12]) is the ratio of the u - and d -quark masses. For the so-called axionlike particles (ALPs) which are not related to the strong CP problem, there is not such a relation. Rather, for a given value of the decay constant f_a , any value of the mass m_a , in particular, a smaller one than that determined by the relation (1), is possible; see, e.g., Chap. 90 in Ref. [12].

Recently, however, a lighter type of axion field than the canonical one was proposed [13,14] that is based on the discrete $Z_{\mathcal{N}}$ shift symmetry suggested by Hook [13] for a dark world extension with \mathcal{N} mirror and degenerate worlds—one of which is ours. These worlds are linked by the so-called $Z_{\mathcal{N}}$ axion field. The latter still solves the strong CP problem if the integer \mathcal{N} is an odd positive number but has a (approximately $2^{-\mathcal{N}/2}$) smaller mass m_a versus $1/f_a$ relation than the canonical QCD axion, i.e.,

$$m_a \simeq \left(\frac{1-z}{\pi(1+z)} \right)^{1/4} m_\pi f_\pi \mathcal{N}^{3/4} z^{\mathcal{N}/2} \frac{1}{f_a}, \quad (2)$$

which, in principle, can be justified for $\mathcal{N} \gg 1$ but, in practice, already works for $\mathcal{N} \geq 3$ [14,15].

If sufficiently abundant, the canonical QCD axion, ALPs, or $Z_{\mathcal{N}}$ axions might be candidates for cold dark matter in the Universe; see, e.g., Refs. [12,16] for recent reviews. In Refs. [17–20], it is suggested that even axions and/or ALPs of mass from 10^{-7} eV/c² down to 10^{-22} eV/c² could be such candidates. This mass range is very challenging to reach with any established technique. For instance, the cavities of the microwave (haloscope) method, scanning for resonance frequencies due to the inverse Primakoff effect in strong magnetic fields, as suggested by Sikivie [21,22], would have to be unwieldy large [23]. Still, axions or ALPs of this mass range could be associated with cosmic dark matter created in the big bang via the so-called preinflationary PQ symmetry-breaking scenario [12]. In this case, these particles would be present now in sufficient concentrations to be regarded as an oscillating classical field that, established primordially, would still exist without losing most of its coherence. Locally within the Milky Way galaxy, the population of axions or ALPs would be dominated by those bound gravitationally to the Galaxy. Their speed is limited by the virial velocity of the stellar ensemble, or

roughly $v = 10^{-3}c$ (cf. Chap. 27 in Ref. [12]), which is similar to the orbital speed of the Solar System containing Earth with respect to the center of the Galaxy. This would result in a nonrelativistic distribution of the axion or ALP velocities, producing spatially coherent, but time-dependent oscillations summarized by the classical axion or ALP field

$$a(t) = a_0 \cos[\omega_a(t - t_0) + \phi_a(t_0)]. \quad (3)$$

Here, a_0 is the amplitude of the field, while ω_a is the pertinent angular frequency which, up to $\mathcal{O}(\{v/c\}^2) \sim 10^{-6}$ dispersive corrections, is determined by the axion or ALP mass m_a :

$$\hbar\omega_a = m_a c^2. \quad (4)$$

Finally, $\phi_a(t_0)$ is the local phase of the axion or ALP field, which not only is unknown but even changes depending on the respective starting point t_0 of any new measurement. The lifetime of validity of this phase can be deduced by the simple quantum estimate

$$\tau_a = \frac{h}{m_a v^2}, \quad (5)$$

while the spatial extent of the phase coherence is given by the length

$$l_a = \frac{h}{m_a v}. \quad (6)$$

Therefore, for axions or ALPs with mass less than $10^{-7} \text{ eV}/c^2$ considered here, any additional spatial dependence on the right-hand side of Eq. (3) can be safely neglected in laboratory experiments, e.g., also in axion searches in storage rings, since according to Eq. (6) and $v \approx 10^{-3}c$ the pertinent coherence length would be about 12 km and even proportionally larger for smaller masses.

Detection in the laboratory of the oscillating dark-matter field of axions or ALPs given in Eq. (3) has to overcome the extremely weak nature of the axion and ALP interactions with each other and other subatomic particles. Since their gravitational component can be safely neglected, these interactions scale with the inverse of the PQ order parameter f_a that empirically has to be much larger than the electroweak vacuum expectation value, as mentioned above. Nevertheless, the pseudoscalar nature of axions and ALPs allows—in accordance with the Wigner-Eckart theorem—for potential couplings to the *total* angular momentum (spin) of nucleons and nuclei and, therefore, opens up further avenues for the detection of the oscillating dark-matter field from Eq. (3)—in addition to utilizing the inverse Primakoff effect, astrophysical constraints, etc., as specified, e.g., in Refs. [12,16]. This holds especially for the mass region specified above, as the Primakoff-based

methods do not apply there. In fact, these spin couplings can occur in two different ways, either by a coupling to the electric dipole moment (EDM) of a non-self-conjugate matter particle carrying nonzero spin (see, e.g., Ref. [24]) or via the pseudomagnetic direct coupling of the gradient of the axion field to the spin of the matter particle, the so-called axion-wind effect. There can be further *CP*-allowed and even *CP*-violating couplings of axions or ALPs to nucleons (or nuclei); see, e.g., the second term in Eq. (8) and the first and third terms in Eq. (9) in Ref. [16]. These interactions are not discussed here, since either they are sensitive only to the (in the considered mass region) suppressed spatial variation of the axion field (3) or they couple only to scalar nucleon or nuclear densities which are *spin independent* to leading order.

The first of these couplings to the nucleon or nuclear spin (see Refs. [17,18]) is based on the introduction of an oscillating component d_{ac} to the total EDM of the pertinent matter particle:

$$d(t) = d_{dc} + d_{ac} \cos[\omega_a(t - t_0) + \phi_a(t_0)], \quad (7)$$

pointing parallel to the spin direction, by the oscillating axion or ALP field $a(t)$. Here, d_{dc} is the permanent (static) component of the pertinent EDM, while the other parameters follow from Eq. (3). In addition to astrophysical constraints (see Ref. [12]), there are first limits reported in Ref. [25] based on the upper bounds on the neutron EDM measurements (see also Ref. [26]). These limits, however, apply only to oscillations of frequency f_{ac} below 10^{-2} Hz , i.e., axion and ALP masses below $10^{-17} \text{ eV}/c^2$ (below $10^{-15} \text{ eV}/c^2$ in the case of Ref. [26]). To search for oscillating EDM components of higher frequency, other methods have to be utilized.

It has been proposed to search for oscillating EDMs with the help of electric, hybrid, or magnetic storage rings [27–30]. Especially in the last case, the charged particles in the comoving beam frame are subject to a large electric field ($c\vec{\beta} \times \vec{B}$) due to their relativistic motion $c\vec{\beta}$ in the magnetic field \vec{B} in the laboratory system. This (effective) electric field closes the orbit such that the resulting force always points toward the center of the ring. The EDM of the charged particle, which is aligned with the spin, feels a torque from this electric field. This causes the spin to rotate about the electric field direction. If the EDM is static, this rotation only wobbles the polarization about its starting point, as the polarization precession in the ring plane continually reverses the torque. If, however, the EDM oscillates at the same rate as the torque reversal, then the rotations accumulate, eventually creating a measurable polarization component perpendicular to the ring plane. Note that the action of an oscillating EDM on the spin can be mimicked by a radio-frequency (rf) Wien filter when its magnetic field, pointing horizontally, acts on the corresponding magnetic dipole moment; cf. Eq. (13).

The second coupling of the axion or ALP field to matter particles is based on the “axion-wind” or “pseudomagnetic” effect [3,31–38], causing a rotation of the spin of a nucleon or nucleus around the gradient of the axion field which acts analogously to a magnetic field [31,37–39]. The term “axion wind” was coined in Ref. [39] (see Ref. [18] for the extension to “ALP dark-matter wind” and, e.g., Refs. [40–42]) for the same pseudomagnetic field—this time manifestly proportional to the velocity of the Earth-bound spins with respect to the galactic axion or ALP field. In that case, the actual velocity is a superposition of the motion of the Solar System with respect to the axion field plus the rotation of Earth around the Sun plus the rotation of Earth around its axis plus the movement of the particle inside the pertinent sample or experiment in the laboratory. All the above complexity with the time-dependent orientation of the pseudomagnetic field becomes entirely irrelevant to the in-flight spins of the beam particles in a storage ring when the velocity is close to the speed of light. Most remarkably, the corresponding pseudomagnetic field is then always tangential to the beam orbit [43,44]; i.e., it plays the role of an rf solenoid uniformly distributed along the ring circumference [44,45].

The two spin-dependent axion or ALP couplings (EDM and axion wind) can be expressed in the Lagrangian formalism. The Lagrangian for the EDM coupling to nucleons is given by the generic expression of Ref. [12] in terms of the axion coupling $g_{aN\gamma}$ to the EDM operator:

$$\begin{aligned}\mathcal{L}_{aN\gamma} &= -\frac{i}{2}g_{aN\gamma}a\bar{\Psi}_N\sigma_{\mu\nu}\gamma_5\Psi_N F^{\mu\nu} \\ &= -\frac{i}{2}\frac{d_{ac}}{a_0}a\bar{\Psi}_N\sigma_{\mu\nu}\gamma_5\Psi_N F^{\mu\nu},\end{aligned}\quad (8)$$

where $N = n, p$ denotes neutron or proton, respectively. Note that the first line in Eq. (8) refers to $\hbar = c = 1$ units, while the second line is given in SI units. After the Dirac spinors Ψ_N are reduced to standard spinors, χ_N , and $a(t)$ of Eq. (3) is inserted for the generic ALP field $a(t, \vec{x})$, the pertinent Hamiltonian assumes the structure

$$\begin{aligned}H_{aN\gamma} &= -\frac{d_{ac}}{a_0}a(t)\left(\chi_N^\dagger\frac{1}{S}\vec{S}\chi_N\right)\cdot\vec{E} \\ &\equiv\vec{\Omega}_{\text{EDM}}\cdot(\chi_N^\dagger\hbar\vec{S}\chi_N),\end{aligned}\quad (9)$$

defining the angular velocity $\vec{\Omega}_{\text{EDM}}$ for the axion-EDM coupling. In fact, χ_N can be extended to apply even for the $(2S+1)$ -dimensional representations of nuclei, especially for the three-dimensional one of the deuteron d ; cf. Refs. [44,46,47]. In the following, the electric field is interpreted as the effective field $\vec{E} = c\vec{\beta} \times \vec{B}$.

The axion-wind case can be derived from the generic interaction Lagrangian of the pseudomagnetic coupling of an axion or ALP field $a(t, \vec{x})$ to an arbitrary fermion

field Ψ_f (where f can stand for the nucleon N , proton p , neutron n , etc.). In the notation of Ref. [12], this Lagrangian reads

$$\mathcal{L}_{aff} = \frac{C_f}{2f_a}\partial_\mu a\bar{\Psi}_f\gamma^\mu\gamma_5\Psi_f\quad (10)$$

in terms of the dimensionless coupling constant C_f and the generic axion or ALP decay constant f_a which is independent of the fermion (Dirac) field Ψ_f . If the latter is reduced to standard spinors (cf. Ref. [44]) and the ALP field $a(t)$ of Eq. (3) is inserted for the generic field $a(t, \vec{x})$, the corresponding Hamiltonian in SI units has the structure

$$\begin{aligned}H_{aNN} &= -\frac{C_N}{2f_a}\hbar\partial_0 a(t)\left(\chi_N^\dagger\frac{1}{S}\vec{S}\chi_N\right)\cdot\vec{\beta} \\ &\equiv\vec{\Omega}_{\text{wind}}\cdot(\chi_N^\dagger\hbar\vec{S}\chi_N),\end{aligned}\quad (11)$$

which is the axion-wind analog of the axion-EDM Hamiltonian (9).

Quantitatively, the spin motion relative to the momentum vector in purely magnetic fields is governed by the subtracted, EDM-, and axion-wind extended Thomas-Bargmann-Michel-Telegdi equation of Refs. [48,49] and [44], respectively:

$$\frac{d\vec{S}}{dt} = (\vec{\Omega}_{\text{MDM}} - \vec{\Omega}_{\text{rev}} + \vec{\Omega}_{\text{EDM}} + \vec{\Omega}_{\text{wind}}) \times \vec{S},\quad (12)$$

defined in terms of the angular velocities for the magnetic dipole moment (MDM) including the Thomas precession, the revolution of the beam (rev), the electric dipole moment (EDM), and the axion-wind effect (wind):

$$\vec{\Omega}_{\text{MDM}} = -\frac{q}{m}\left(G + \frac{1}{\gamma}\right)\vec{B},\quad (13)$$

$$\vec{\Omega}_{\text{rev}} = -\frac{q}{\gamma m}\vec{B},\quad (14)$$

$$\vec{\Omega}_{\text{EDM}} = -\frac{1}{S\hbar}d(t)c\vec{\beta} \times \vec{B},\quad (15)$$

$$\vec{\Omega}_{\text{wind}} = -\frac{1}{S\hbar}\frac{C_N}{2f_a}[\hbar\partial_0 a(t)]\vec{\beta},\quad (16)$$

where, to simplify the notation, terms including $\vec{\beta} \cdot \vec{B}$ are omitted. \vec{S} in the above equations denotes the spin vector in the particle rest frame, t the time in the laboratory system, β and γ the relativistic Lorentz factors of a particle of rest mass m , and \vec{B} the magnetic field in the laboratory system pointing perpendicular to the ring plane. The magnetic dipole moment $\vec{\mu}$ and electric dipole moment \vec{d} are both pointing along the axis of the particle’s spin \vec{S} . The

dimensionless quantity G (magnetic anomaly) is related to the magnetic moment as follows:

$$\vec{\mu} = g \frac{q\hbar}{2m} \vec{S} = (1 + G) \frac{q\hbar}{m} \vec{S}. \quad (17)$$

The oscillating axion or ALP field $a(t)$ [see Eq. (3)] generates the oscillating (ac) term in the electric dipole moment $d(t)$; cf. Eqs. (7) and (9). Through the time derivative $\partial_0 a(t)$, a second oscillating contribution in the term $\vec{\Omega}_{\text{wind}}$ [43–45] is present; cf. Eq. (11). It depends on the specific coupling strength C_N , while f_a is the generic axion or ALP decay constant, namely, the order parameter of PQ breaking mentioned above. By just measuring a vertical buildup of a polarization component perpendicular to the ring plane, the EDM-induced axion coupling and the axion-wind pseudomagnetic coupling cannot be distinguished, since they have the same effect on vertical polarization. Moreover, for axion or ALP masses below 10^{-7} eV/ c^2 , the sensitivity in any foreseeable search is not expected to extend to the scale where the pseudoscalar bosons determining the $a(t)$ field would appear as a result of known QCD processes; thus, if the possibility of Z_N axions is ignored here, these particles should be referred to as ALPs rather than axions.

At COSY, which belongs to the class of purely magnetic storage rings, we store in-plane beams of deuterons of approximately 970 MeV/ c beam momenta with a spin-precession frequency of $f_{\text{spin}} = f_{\text{rev}} |G\gamma| \approx 120$ kHz (where $G = -0.142\,987\,542\,4$ is the deuteron magnetic anomaly and f_{rev} and γ the revolution frequency and the relativistic factor of the circulating deuterons, respectively) [50]. This corresponds to an ALP mass of about 5×10^{-10} eV/ c^2 . Then, the simple quantum estimate of the lifetime in Eq. (5) gives $\tau_a \approx 8$ s. The time for the frequency scan to cross the ALP resonance should not be much greater than this, or else the size of the polarization jump will be attenuated. In fact, the crossing times are less in this experiment. At the same time, the ALP field must be able to act on all the particles in the beam simultaneously. A similar estimate of the spatial extent of phase coherence as in Eq. (6) gives the length $l_a \approx 2500$ km. This coherence length well exceeds the size of the storage ring (183.6 m circumference). All parts of the beam and their particles should, therefore, be exposed to the same ALP field as given in Eq. (3).

Since the ALP oscillation frequency ω_a in Eq. (3) is unknown, it is necessary to slowly ramp the beam energy and, thus, the spin-precession rate while continually monitoring the vertical polarization with the hope of detecting its sudden change (to which we refer as a *polarization jump* in the following) as the resonance is crossed. For this, it is crucial to be able to maintain the in-plane polarization over the entire measurement cycle [51] and to continuously monitor the spin-precession frequency with high

precision [52]. The phase of the EDM oscillation relative to the polarization precession is also unknown [cf. $\phi_a(t_0)$ in Eqs. (3) and (7)], so four beam bunches are stored simultaneously in the ring with different polarization directions in order that all possible phases are adequately sampled. A novel waveguide rf Wien filter designed for EDM searches at COSY is successfully used to generate a test signal in the beam polarization as a confirmation of the method.

This paper describes the details of the first search for ALPs using a storage ring. Section II provides a description of the experiment with a polarized beam. This includes the properties of the beam and the requirements for the search. Subsections deal with the problem of using multiple beam bunches to ensure that all phase possibilities are covered and describe the management of the scanning process in detail. Section II C describes how the rf Wien filter installed in the COSY ring is used to create a resonance that confirms our model for the process of generating a polarization jump. The analysis of the data is covered in Sec. III, and Sec. III E discusses how we handle a systematic problem with false positive signals. There is also a description of the model used for the calibration of any polarization jump in terms of an oscillating EDM. The various upper limits of the ALP-deuteron couplings are discussed in Sec. IV. Conclusions and an outlook are pursued in Sec. V. Details about the four-bunch procedure and the calibration of the sensitivity of the measurement are relegated to Appendixes A and B.

II. THE EXPERIMENT

The search for ALPs was performed at the Cooler Synchrotron (COSY) located at Forschungszentrum Jülich, Germany [53] in the spring of 2019 [50]. The polarized deuteron beam (\vec{D}^-) is generated in an atomic beam polarized ion source [54]. A single polarized state is made using a weak field transition unit. The beam is then preaccelerated in the JULIC cyclotron. The beam polarization is measured in the transfer line between the cyclotron and the COSY ring using a dedicated low-energy polarimeter (see Ref. [55]). Deuterons are scattered from a carbon target at a kinetic energy of 75.6 MeV [55]. The quantization axis for the spins of the beam particles is vertical, a direction imposed by the cyclotron fields. Elastically scattered deuterons are detected at 40° in the lab on either side of the beam using plastic scintillator detectors. A description of deuteron spin polarization is given by Tanifuji [56] and is consistent with the Madison convention [57]. The analyzing power in this configuration is $A_y = 0.61 \pm 0.04$ [55]. A left-right asymmetry $(L - R)/(L + R) = (3p_y A_y/2)$ of -0.508 ± 0.007 is recorded. Repeating this measurement with the polarized source rf transition turned off produces an asymmetry of -0.159 ± 0.008 . This is a measure of the geometrical

errors in the detector and data acquisition setup. The difference, -0.349 ± 0.011 , results in a polarization of $p_y = -0.38 \pm 0.03$.

The deuteron beam is injected into the COSY synchrotron at 75.6 MeV by stripping off the electrons in a thin foil and ramped to an energy of 236 MeV (0.97 GeV/*c* momentum). At this energy, the polarization of the stored beam is measured using the forward detector from the Wide Angle Shower Apparatus (WASA) facility [58], as shown in Fig. 1.

A 2-cm-thick carbon block is inserted from above the beam and brought into position with the bottom edge aligned along the center of the WASA detector. This requires that the beam be locally lowered by about 3 mm as it passes the carbon target. At the start of data acquisition, the beam is heated vertically using rf white noise generated in a band about one of the harmonics of the vertical tune. This brings beam particles to the front face of the target. From there, deuterons pass through the target. Some are scattered into the WASA detector system. The observed event rate is dominated by elastic scattering which has a forward-peaked angular distribution. The relevant analyzing powers for elastic scattering are shown in Ref. [58]. The detector acceptance is divided by software into four quadrants (left, right, down, and up). The sum of these four detector rates is fed back to control the power level

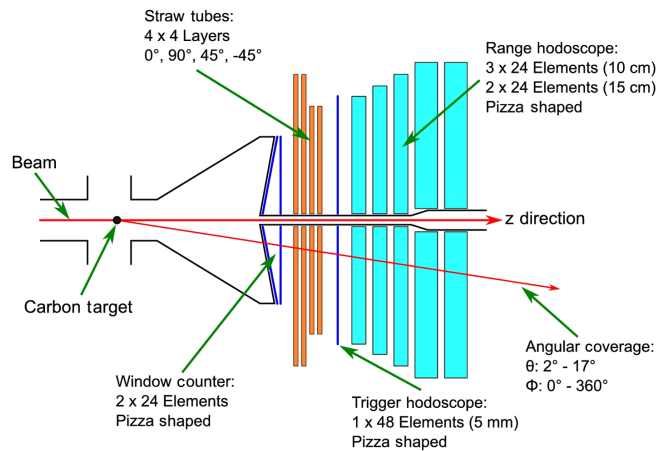


FIG. 1. Cross-sectional diagram showing the layout of the WASA forward detector, reprinted from Ref. [58]. The beam travels from left to right (horizontal red arrow), closely passing a 2-cm-thick carbon block target along the way. The beam is heated vertically to bring beam particles to the front face of the target. Scattered particles moving forward exit the vacuum through a stainless steel window at angles between 2° and 17° . They then pass through two plastic scintillator window counters cut into pie-shaped segments, an array of straw tubes for position and angle tracking, a segmented trigger hodoscope, and five layers (light blue) of plastic scintillator calorimeter detectors. The trigger counter and calorimeter detectors are also divided into pie-shaped segments. All the scintillator counters are read out using photomultiplier tubes mounted at the outer edge of each pie segment.

of the white noise and maintain a constant event rate. Left-right and down-up asymmetries are computed in real time in four-second time intervals and made available for inspection as each beam store progresses. The down-up data stream is unfolded [59] based on the spin tune frequency in order to generate a value of the magnitude of the rotating in-plane component of the beam polarization.

A typical left-right asymmetry with the vertically polarized beam running is 0.12 ± 0.02 , where the error indicates the variation in this value during the experiment. This means that the cross section weighted average of the analyzing power over the WASA detector acceptance is 0.210 ± 0.035 .

The beam is accelerated in less than a second to full energy. Then electron cooling is applied for 71 s. This reduces the phase space of the beam to a point where the polarization lifetime in the horizontal plane could become long [51]. Once electron cooling is complete, the operating conditions for the beam are set. This requires minimizing orbit deviations that would take the beam away from the centers of quadrupole lenses and reducing other unnecessary deviations. Finally, the polarization, which begins in the vertical direction, is rotated into the horizontal plane using an rf solenoid.

The timing list for a machine beam cycle is given in Table I.

In order to precess the deuteron polarization into the ring plane, the rf solenoid is operated for 3 s on the $(1 + G\gamma)f_{\text{rev}}$ harmonic, where $f_{\text{rev}} = 750\,602.6$ Hz. At this frequency, the relativistic factor is $\gamma = 1.126$. A search, made either as a scan or in fine steps, shows that the $(1 + G\gamma)$ resonance for the rf solenoid occurs at $f_{\text{sol}} = 629\,755.3$ Hz. The difference of these two frequencies, $f_{\text{rev}} - f_{\text{sol}} = 120\,847.3$ Hz, is the spin tune frequency f_{spin} . The frequency generators are synchronized with the 10 MHz signal from the Global Positioning System; thus, the set values are precise and stable out to several millihertz. From these two frequencies and the assumption that the

TABLE I. Times for various COSY operations during the beam cycle.

Event in the cycle	Time (s)
Acceleration off	0.674
E-cooling on	4–75
Carbon target moved in	75
White noise extraction on	77
WASA flag (DAQ on)	78
rf solenoid on (rotate p_y)	83–86
Quick ramp to start of scan	90.0–90.1
Constant frequency hold	90.1–120.1
Ramp to search for ALP	120.1–255.1
Constant frequency hold	255.1–285.1
COSY rf stop	287
End of data taking	288

TABLE II. Beam parameters.

Parameter	Symbol (unit)	Value
Revolution frequency	f_{rev} (Hz)	750 602.6
Spin resonance frequency	f_{sol} (Hz)	629 755.3
Spin tune frequency	f_{spin} (Hz)	120 847.3
Lorentz factor	γ [1]	1.126
Beam velocity $/c$	β [1]	0.460
Orbit circumference	l (m)	183.57
Number of deuterons per cycle	N_d [1]	$\approx 10^9$

COSY ring is purely magnetic, it is possible to deduce the kinematic parameters of the beam given in Table II. This parameter list is shown without errors, since they lie beyond the range shown in the table. The values are typical of the initial conditions of the deuteron beam in the storage ring before ramping. The setup of the Wien filter in Sec. II C contains the results of the scan used to determine the $(1 - G\gamma)f_{\text{rev}}$ spin resonance frequency. In that case, the resonance shape is measured as part of the matching process and found to have a fractional full width of about 2×10^{-9} which represents one estimate of its precision.

As for the spin tune frequency f_{spin} , the analysis of the polarization data allows us to measure it with a 10^{-10} precision [52], and the cycle-to-cycle variations are driven by the stability of the power supplies and the resulting orbit variations rather than by the precision of frequency setting.

It is important that the orbit does not deviate during the course of a ramp. This requirement is tracked with the use of beam position monitors.

The strategy for making the ALP search contains the steps shown in Fig. 2. Because of the necessity to maintain reproducible conditions for the rotation of the polarization from the vertical into the horizontal plane, all machine cycles begin at the same beam energy or revolution frequency, as indicated by the blue horizontal axis in the figure. Once the polarization rotation is complete, a quick ramp is made to take the machine to the starting point for the scan. This removes the necessity to search for a new resonance frequency before every new scan. The scans, indicated by the long sloping lines in Fig. 2, last for 135 s. Before and after, there is a 30-s period with no ramp. This is meant to provide extra data to characterize the starting and ending points under stable conditions. The ramps are planned to overlap at the ends, as shown in the figure. Since it is possible that an ALP-induced resonance might occur near the start or end, the overlap with the neighboring ramp is planned so that the resonance can be correctly characterized.

Altogether, there are 103 ramps covering a range from 119.997 to 121.457 kHz, or an axion mass range of 4.95–5.02 neV/ c^2 .

In detail, after completing the initial preparatory phase of the machine cycle, the beam is brought to an interaction

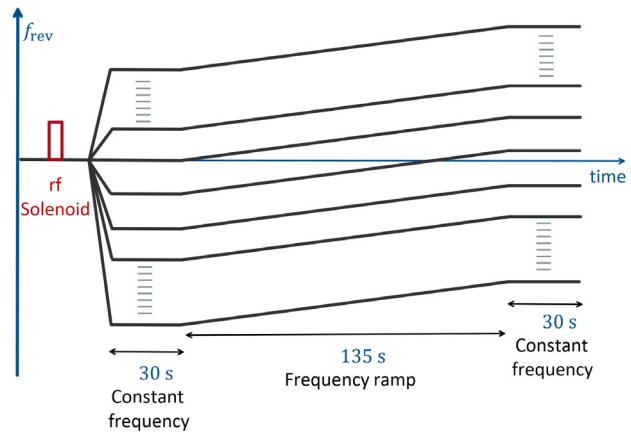


FIG. 2. Diagram of revolution frequency as a function of time (black lines) showing how scans for axions are organized. The diagram includes an early time (marked in red) when the rf solenoid rotates the polarization into the horizontal plane. Then, quick ramps take the machine to the start point for each ramp. Flat parts are included at the beginning and end of each scanning ramp to allow checks of the polarization with enhanced statistical precision. The resonance jump is expected to appear at some time during the scanning ramp.

with the polarimeter target by moving the target into the correct position, turning on the rf white noise, and initiating the feedback used to maintain the polarimeter count rate. At this stage, the data acquisition (DAQ) is turned on. After a short period that is used to check the vertical polarization, the rf solenoid is activated to rotate the polarization into the horizontal plane. For each scan, the machine is first set to the starting conditions. Then, the first 30-s holding time takes place, followed by the ramp and the second 30-s holding time.

The rf solenoid, whose magnetic axis is along the beam axis, operates by giving a series of small kicks to the rotation of the polarization. The magnetic field, except for some mild focusing effects, does not steer the beam. It, thus, maintains the constant orbit length constraint. The rf solenoid is kept running for 3 s. If allowed to continue, it would drive the vertical polarization into an oscillating pattern [60]. The solenoid strength is adjusted until the vertical polarization component observed after the rotation is brought to zero. See the beginning of Appendix A for more details.

If the beam, once in the plane of the ring, remains polarized, then the down-up asymmetry in the WASA forward detector oscillates with the precession frequency. However, this frequency is much too large to be able to observe even a single polarimeter event per oscillation; thus, a different technique has been developed [52]. Namely, a value of the spin tune ($\nu = G\gamma$) is assumed and the data sorted among nine bins according to where the spin tune would predict it would lie along a single oscillation of the asymmetry. At the end of a preset time interval of 4 s, the data accumulated in each of the time bins are used to calculate a down-up asymmetry for that bin.

These asymmetries are reproduced with a sinusoidal curve from which the magnitude and phase of the oscillating horizontal asymmetry are obtained. The value of the spin tune is varied in small steps until a maximum in the amplitude of the sine wave is found [59]. The resulting magnitude and phase are recorded for that time bin. Data from the in-plane polarization measurement are recorded every 4 s in order to provide the statistics to complete this search. The processing time is quick enough that values of the horizontal asymmetry are made available in real time during the experiment.

The horizontal polarization is subject to depolarization, because betatron oscillations of the beam particles lead to variations in their spin tunes. It has been shown that the addition of sextupole fields to the ring allows for the compensation of this depolarizing effect [51,61]. Thus, a part of the setup for this search involves optimizing these fields for the particular running conditions present in COSY at the time of this search. Online data are used to determine the horizontal polarization loss. Values for the strength of the three families of sextupole magnets are adjusted until the maximum polarization lifetime is obtained. During this experiment, the lifetime continues to vary, because it is very sensitive to running conditions. At all times, the slope of the horizontal polarization with time is maintained with a half-life greater than 300 s. Thus, no more than a quarter of the polarization is lost during a typical scan.

A. Dealing with ALP phase

During the scan, the phase of the oscillating EDM with respect to the rotating in-plane polarization (with reference to the beam-frame electric field) is not known. With only a single beam bunch in the machine at one time, the amplitude of a jump is modulated by a sine function of this relative phase. This situation could easily allow an ALP to be missed during a single scan. To avoid this, our strategy is to use more than one beam bunch at the same time, since the same ALP phase is shared among all of these bunches. With the equipment available at COSY, bunching the beam up through harmonic 4 was already available.

A model study is performed to see if this change would satisfy the requirement with no further additions to the COSY ring. The details of this calculation are described in Appendix A. Assuming a round rather than a racetrack-shaped ring, it is found that four equally spaced bunches offered four mutually perpendicular orientations of the polarization direction relative to the beam-frame electric field (see Fig. 23). As the beam circulates in the ring, these four polarization directions rotate synchronously.

The COSY ring is racetrack shaped, with arcs and straight sections of approximately the same length. This breaks the simple rotation pattern. Two bunches on opposite sides of the ring have a rotating polarization, while the two bunches in between have a stationary phase

without any electric field. This pattern swaps four times during each beam rotation. The sensitivity to all possible ALP phases comes from the comparison between neighboring bunches. During a single turn, the angle between polarization vectors of two subsequent bunches oscillates from 90° to 61.2° and back again. In this case, the actual sensitivity must be averaged over the range of angles covered in this oscillation. This results in a reduction of the signal by 4.2%, and the presented results are corrected for this effect.

B. Scan management

The approach to managing the scanning process is described in Sec. II above and is shown in Fig. 2. In preparing this scheme, one of the most crucial parts is the precession of the polarization from the vertical to the horizontal. To do this, the resonant frequency for the rf solenoid on a harmonic of the revolution frequency must be located experimentally to within about 0.1 Hz. This level of precision requires several tests that demonstrate an efficient precession process and the vanishing of the vertical polarization component at the end. This procedure is usually time consuming, taking longer than the series of scans themselves at one frequency setting. It was decided to separate the rf-solenoid-driven spin rotation from the rest of the scan procedure in order to save time and effort. After the rf-solenoid-driven spin precession is complete, the COSY operating frequency is ramped to the starting point for the scan and the scanning process begins. In this way, the same resonance frequency is kept for all scans.

The ramping process itself must obey the constraint of preserving the orbit circumference while maintaining the optical properties of the beam. Even small variations can alter the way that sextupole corrections affect the beam. The resulting changes in the cancellation of depolarizing effects would make the lifetime of the horizontal polarization significantly smaller. For ramping, the two adjustable parameters on the machine are the magnetic field in the arcs and the frequency of the rf cavity that bunches (and accelerates) the beam. We choose to create a linear ramp in momentum. The field of the ring magnets is usually characterized by rigidity $B\rho$ which itself is proportional to the momentum. Thus, this requirement for the magnetic field is met straightforwardly using

$$B\rho = \frac{pc}{q}, \quad (18)$$

where ρ is the curvature radius of a particle track in field B , c is the speed of light, and q is the electric charge of the nucleus. The bunching or accelerating cavity frequency must obey the same constraints and should follow

$$f_{\text{rev}} = \frac{p}{\sqrt{m^2c^4 + p^2c^2} \Lambda}, \quad (19)$$

where m is the deuteron mass and Λ is the orbit circumference. The value of f_{rev} used in the scan must be recalculated at each step of the ramp. The quality of the orbit control is checked by computing the root mean square (rms) deviation of the orbit summed over all of the beam position monitors in the ring. Control is adequate when this deviation is less than 1 mm.

The ramps are controlled by providing continuously changing momentum values to the COSY control system. The ramps are calculated from a common starting point of 970 MeV/c, the same momentum used for the rf solenoid on resonance. Then, the machine settings are moved to the starting point for an ALP scan. Two speeds are employed during the experiment. For the faster ramps, the initial and final momenta are calculated according to

$$p_0 = 970(1 + 1.173 \times 10^{-4}n) \text{ MeV}/c, \quad (20)$$

$$p_f = p_0 + \Delta p, \quad (21)$$

where n is the number of the scan (see Fig. 2), either positive or negative, away from 970 MeV/c and Δp is the momentum change in 135 s. Table III gives the momentum change Δp which is entered into the COSY control system and the corresponding change in f_{spin} and f_{rev} calculated from the read back from the rf cavity frequency. For the faster of the two ramps, the overlap between ramps is about 2.6 Hz.

For the slower ramps (second row), the same formula is used for p_0 , but Δp is decreased. In this case, there is a small coverage gap between adjacent ramps. The original plan was to have the ramps overlap so that resonances near the beginning or end of a scan would not be missed because of reduced time near the center of the resonance. As it is, they barely touch for the slow scans. There are 85 of the faster scans made with n ranging from -42 to 42 . For the 18 slow scans, n ranges from -60 to -43 .

Each run usually consists of ten separate beam fills. One out of five of the fills is deliberately unpolarized in order to provide a baseline for no polarization effect. Thus, each run usually consists of eight polarized fills. The results from these fills are combined, as explained in more detail in the analysis section below, to yield sensitivity results for the range of the scan.

The goal for each fill is to begin with 10^9 polarized deuterons. Because of changes in source and machine operation efficiency over time, this value could vary up or

TABLE III. Change in beam parameters during the ramp.

Δp (MeV/c)	Δf_{rev} (Hz)	$\Delta \dot{f}_{\text{rev}}$ (Hz/s)	Δf_{spin} (Hz)	$\Delta \dot{f}_{\text{spin}}$ (Hz/s)
0.138	81.0	0.600	16.8	0.124
0.112	66.15	0.490	13.5	0.100

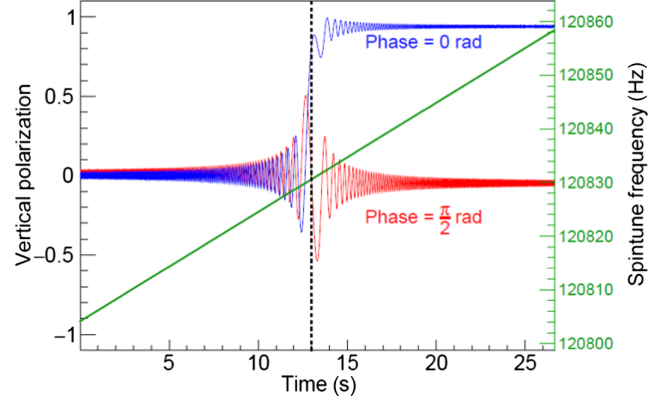


FIG. 3. Graph of the vertical component of the polarization for a hypothetical resonance between the polarization rotation and the frequency of the ALP. Three quantities are shown as a function of time during a scan. The green line illustrates the changing spin-precession frequency as time passes and the momentum of the beam is ramped up. At 13 s, the spin tune frequency and the ALP frequency in this model are the same. The blue and red curves show the time dependence of the vertical polarization component for two different choices of the ALP phase. In this case, initial conditions are such that a large jump is seen for a phase of zero and a much smaller, negative jump is seen for a phase of $\pi/2$. These two cases sample the ALP phase along perpendicular axes; thus, the sum in quadrature of the jumps represents the strength of the ALP coupling to the deuteron.

down by a factor of 2. These changes are reflected in the final sensitivity as a function of the ALP frequency.

The calibration of the jump size in terms of the size of the oscillating EDM is presented in Appendix B. Here, in the description of the experiment, it is useful to illustrate an example of the signal as it might appear for one bunch during the experiment. This is shown in Fig. 3.

In the analysis of the scans, the data are rebinned into 2-s bins, but the details of the resonance crossing as shown in Fig. 3 are not apparent in the data. This same feature also applies to the Wien filter test described in the next section. If the scanning speed is slower, then more time is available to make a polarization jump. Calibration calculations discussed in Appendix B show that the jump size scales as the square root of the reciprocal of the ramp rate.

C. Wien filter test

The COSY ring has been recently equipped with a spin manipulation tool that allows for spin rotations with minimal orbit disturbance, namely, a waveguide rf Wien filter [62–65]. It is especially designed for precision experiments including the measurements of permanent EDMs in a magnetic storage ring, which are performed at COSY in the framework of the JEDI Collaboration. The electric field is generated in sync with a perpendicular magnetic field so that the beam orbit is not perturbed. The Wien filter can be rotated 90° around the beam axis without breaking the vacuum to adjust the field directions to the

experimental needs. We choose to use this device to test the ability of our system to detect a vertical polarization jump when passing a resonance. For this, it is operated at a fixed frequency on the $(1 - G\gamma)f_{\text{rev}}$ resonance with the magnetic field horizontal, such that the polarization is rotated about a sideways axis. By scanning the Wien filter frequency in small steps, the resonant frequency is found to be $871\,450.039 \pm 0.002$ Hz. The scan of the rf frequency is done in the way established for the ALP scans. In this setup, the phase between the Wien filter oscillation and the rotation of the in-plane polarization is arbitrary for each fill of the machine. Thus, jumps are expected to be of variable sign and magnitude in consecutive cycles. Nevertheless, the result of a random distribution of phases should be a series of jumps between a positive and negative limit of the same size with more cases located near the limits (projection of a sinusoidal function on the y axis). As is the case for the ALP scans, the ramp operates between 120 and 255 s in the machine cycle, producing a ramping time of 135 s. Ramps are made with the resonance in the middle of the ramp. The ramps go in both directions. There are two different ramp speeds, based on a total momentum change of either 0.056 or 0.112 MeV/ c during the ramp.

As an initial calibration of the strength of the Wien filter magnetic field, the beam injected with a vertical polarization (no rf solenoid) is subjected to continuous operation of the Wien filter from 88 to 285 s in the machine cycle. Thus, time that is normally not a part of the scan in the machine cycle is added to the time to observe oscillations. This extra time comes mostly from the two 30-s periods used previously for the nonramp data. This setup should produce a continuous oscillation of the vertical polarization component. Four different power levels are used for the Wien filter, each differing from the previous by a factor of 2 in magnetic field. In Fig. 4, data are shown between 81 and 287 s. The Wien filter is turned on at $t_0 = 88$ s.

For the fits to the driven oscillations, the raw asymmetry data from the measurements are averaged across all four bunches and rebinned in 1-s intervals. Because of a slow depolarization arising from synchrotron oscillations [60], the oscillations are damped with time. These patterns are reproduced using the function

$$A_{\text{LR}}(t) = A \{ e^{-(t-t_0)/\tau} \cos[2\pi f_{\text{drv}}(t - t_0) + \phi] \} + k, \quad (22)$$

where $A_{\text{LR}}(t)$ is the shape of the data, A is the amplitude, τ is the decay constant, f_{drv} is the driven oscillation frequency, ϕ is the phase, and k is the zero offset of the asymmetry data. The results for the frequency f_{drv} , which is a measure of the strength of the Wien filter magnetic field, are given in Table IV. The right-hand column shows the ratio between the frequency on that row and the previous row. Given the power settings, this ratio should be two. Within a few percent, this ratio is realized. Variations are due to the properties of the control system of the Wien filter.

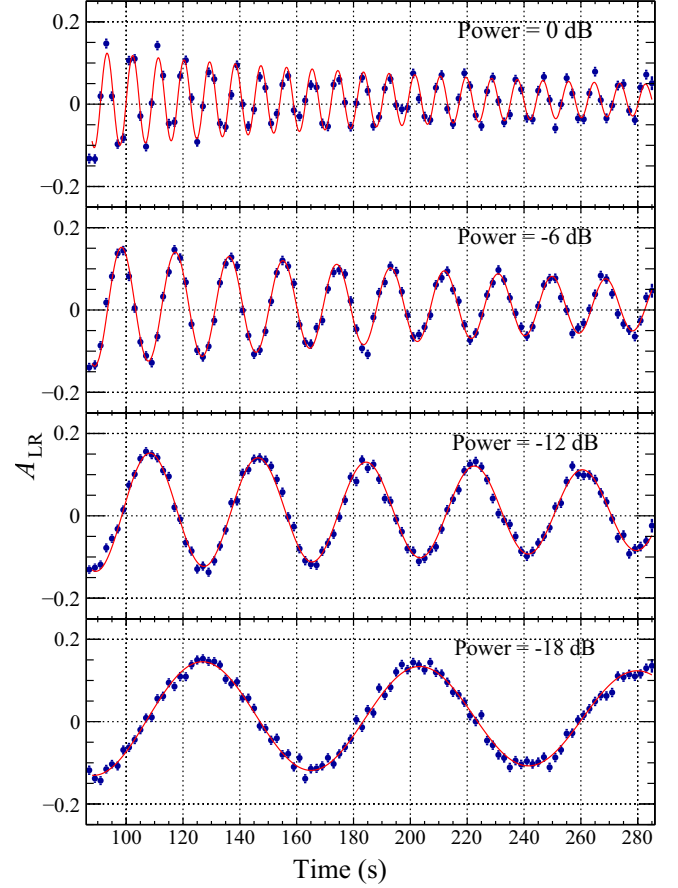


FIG. 4. Measurements of the oscillating left-right asymmetry proportional to the vertical polarization produced by the continuous operation of the Wien filter at various power levels (noted in the figure). The horizontal axis is time in seconds. The Wien filter is on continuously. Data from all four bunches are combined into a single asymmetry.

When scans are recorded for the size of their jumps, a power level of 0 db is used.

III. DATA ANALYSIS

The data available from each run consist of the left-right asymmetry and the unfolded down-up asymmetry as functions of time before, during, and after each scan. These measurements are available from each of the four beam bunches. Since the initial vertical polarization has already been precessed into the ring plane, the left-right

TABLE IV. Driven oscillation frequencies. The third column contains the ratio of the current row frequency to the one in the preceding row.

Power (db)	Frequency (Hz)	Ratio
-18	0.013 084(19)	
-12	0.026 326(21)	2.0122(33)
-6	0.0528 16(25)	2.0062(19)
0	0.110 848(345)	2.0988(66)

asymmetry where the jump may appear is initially close to zero. Meanwhile, the down-up asymmetry, which is subject to depolarization due to spin tune spread, declines slowly with time. This behavior is usually linear. For each fill and bunch, a linear fit to these data provides values of the in-plane asymmetry (A_{IP}) as a function of time during the scan. Results from different bunches in the same fill are consistent. Jumps are observed only for the test case using the Wien filter to rotate the spins of the deuterons.

In line with the open science policy, the collected semiraw experimental data are available in the Jülich DATA repository [66]. Two independent analyses are performed using somewhat different analysis algorithms to define confidence intervals. As they yield consistent results, in the following, we present only one of the approaches based on the well-known Feldman-Cousins [67] procedure, while the other can be found in Ref. [68].

Models, as described in the appendixes, are used to relate the sizes of the jumps to the case where the beam polarization is unity and the effects are generated by the presence of an oscillating EDM. Subsequent examples of left-right asymmetries in this section show the original measurements; any jumps recorded are then normalized by dividing by the linear fit to $A_{\text{IP}}(t)$ appropriate for the time of the observation.

This section addresses, in turn, the calculation of A_{IP} in the presence of ramping, the general treatment of possible jumps, and results for the Wien filter scans and the ALP scans. The jumps for the four bunches are then combined into a single result by fitting them to a sinusoid as a

function of the relative phase between the beam rotation and the ALP oscillation. This process produces nonvanishing amplitudes for the sine wave even in cases where no effect is expected. This leads to a more complicated interpretation, as explained in Sec. III E.

A. Calculation of the in-plane polarization

The analysis of the down-up in-plane asymmetry A_{IP} is described in Ref. [59]. Data consisting of down-up events are gathered into 2-s time bins. As a function of time, the angle of the polarization α is given by

$$\alpha = \omega t = 2\pi\nu f_{\text{rev}}(t - t_0), \quad (23)$$

where the spin tune $\nu = G\gamma$ and the revolution frequency f_{rev} are assumed to be constant and t is measured relative to t_0 at the beginning of the time bin. The events are divided into 12 angular bins according to the value of α modulo 2π . The down-up asymmetry A_{DU} is calculated for the events in each bin. Finally, a sinusoidal curve is fit to $A_{\text{DU}}(\alpha)$. The amplitude of the sine curve becomes the measure of A_{IP} , the in-plane asymmetry. The phase of the fit is tracked as a function of the time bin. A constant value is interpreted as a validation that the initial choice of spin tune is correct.

In the case of a scan, the spin tune undergoes a linear ramp from time t_1 to t_2 , as depicted in Fig. 3. At the same time, the machine revolution frequency also ramps. This gives

$$\omega(t) = \begin{cases} 2\pi\nu_0 f_{\text{rev},0} & \text{for } t_0 < t < t_1, \\ 2\pi[\nu_0 + \dot{\nu}(t - t_1)][f_{\text{rev},0} + \dot{f}_{\text{rev}}(t - t_1)] & \text{for } t_1 < t < t_2, \\ 2\pi\nu_f f_{\text{rev},f} & \text{for } t > t_2, \end{cases} \quad (24)$$

$$\alpha(t) = \int_{t_0}^t \omega(t') dt', \quad (25)$$

where the subscripts 0 and f correspond to the initial and final values, respectively. Dotted symbols denote time derivatives. Once the spin phase $\alpha(t)$ is known, the calculation of A_{IP} proceeds as in the no-ramp case mentioned above.

B. Calculation of polarization jump

The data to be used in the analysis come from the left-right asymmetries recorded during the scanning process as a function of time. An illustration based on data taken with the Wien filter is shown in Fig. 5. With the level of time binning used in this experiment, the jump appears to be instantaneous. We represent this process using the step function:

$$f(t) = \begin{cases} A_{\text{LR},0} & \text{if } t < t_{\text{step}}, \\ A_{\text{LR},0} + \Delta A_{\text{LR}} & \text{if } t \geq t_{\text{step}}. \end{cases} \quad (26)$$

In this equation, $A_{\text{LR},0}$ represents the left-right asymmetry before the scan as well as the asymmetry before the jump. The jump value ΔA_{LR} is the size of the change in the asymmetry. In Fig. 5, the black curve uses $t_{\text{step}} = 187$ s, the time when the in-plane polarization rotation frequency and the Wien filter frequency are the same. The step function is a good representation of these data.

In the case of normal scans for an ALP, we do not know *a priori* when the jump may have occurred, if at all. In this case, the fit is repeated as t_{step} is given the time of each bin from 121 to 257 s. When this is done for the Wien filter data in Fig. 5, the fits away from the resonance, as shown by sample red and green curves, display a smaller value of ΔA_{LR} . There is also a larger value of the fit χ^2 , as seen in

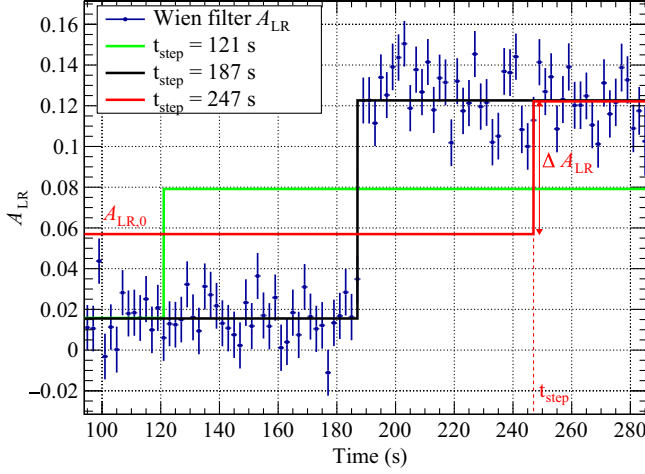


FIG. 5. Examples of step function fits for the Wien filter scan data for a single bunch from one cycle. The black line is fit with the jump (t_{step}) at the resonance crossing. The red and green curves show the results for other choices of the jump time. In both cases, the jump size is smaller and the reduced chi square of the fit is increased (see Fig. 6).

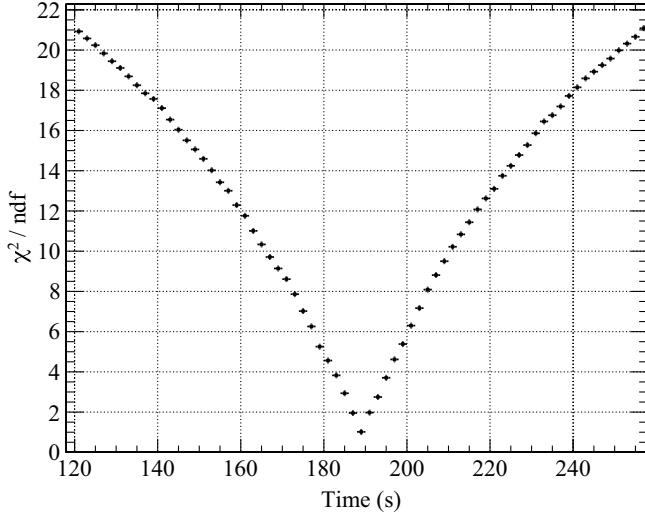


FIG. 6. Reduced chi-squared plot of the step function fits for a Wien filter scan from one cycle as a function of the time assumed for the jump. The calculations are based on the data from Fig. 5. The minimum corresponds to the time when the resonance takes place.

Fig. 6 when t_{step} is away from the resonant frequency. Each cycle and bunch of the ALP search data is scanned for such a feature. The results are discussed in Sec. III D.

C. Wien filter scan analysis

The Wien filter scan data consist of 48 separate machine cycles. The four bunches within each cycle display oscillating jumps of the opposite sign. In each different cycle, the phase between the Wien filter and the rotating in-plane polarization is random. This results in variations in the

TABLE V. Comparison of the maximum polarization jump Δp_y from simulation and experiment for the Wien filter test.

Δp (MeV/c)	Simulation	Experiment
0.112	0.75	0.796(15)
0.056	0.93	0.892(18)

jump size from cycle to cycle that span the range of possibilities. Statistical variations in the recorded asymmetries lead to errors in the jump of about 2%. In addition, the phase uncertainty multiplies this size by the cosine of the unknown relative phase. This acts to reduce all jump sizes. But the peak of the distribution should be close to the maximum value of one for the cosine.

To get a better estimate of the maximum, the absolute values of the jumps for the two ramp speeds are placed into separate distributions. In each case, there is a clear maximum. The jump amplitude is found by interpolating halfway between the bin with the maximum number of cases in the upper 20% of the distribution and the maximum in the distribution. This, in part, allows the downward bias of the cosine effect to be corrected by the possible upward bias of the jump statistical distribution. An evaluation of this procedure using a Monte Carlo model shows that the scatter of the answers is 2% given the number of jumps recorded, roughly the same as the statistical error in the jump size. The 2% error overlaps with the model value of the maximum jump.

The experimental values obtained using this procedure are presented in Table V along with the values from a dedicated simulation. This simulation is performed similarly to the one for the sensitivity calibration presented in Appendix B, only using the actual working parameters of the Wien filter and probing various relative phases. In addition, as the Wien filter is a localized device, the rotations are not combined but executed subsequently as described for the rf solenoid simulation in Appendix A. The resonance strength of the Wien filter is derived from the ratio of the driven oscillation frequency (see Sec. II C) to the revolution frequency in the storage ring at resonance:

$$\epsilon_{\text{WF}} = \frac{0.110848 \text{ Hz}}{750602.6 \text{ Hz}} = 1.4768 \times 10^{-7}. \quad (27)$$

This converts to an oscillation amplitude of the spin rotation per turn by the Wien filter of $\psi_{\text{WF}} = 4\pi\epsilon_{\text{WF}}$ (see, e.g., Ref. [64]). Note that at this large resonance strength the linear dependence between rotation amplitude and polarization jump (see Appendix B) no longer holds, and, thus, the ratio of the polarization signals for the two ramp rates does not reflect the discussed scaling behavior.

While neither pair of values agrees within errors, taken together there is a confirmation that the simulation program correctly models the sensitivity of the

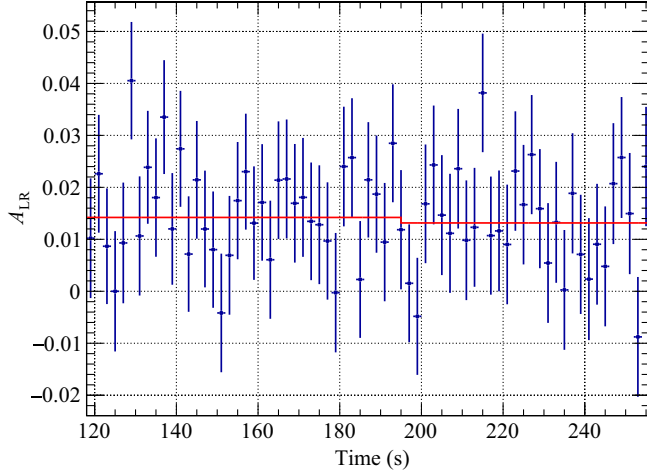


FIG. 7. Example step function fit for an axion scan for a single bunch from one cycle. There is no jump in asymmetry since $\Delta A_{LR} = -0.001(2)$ is consistent with zero.

experiment. We, therefore, assume that the calibration described in Appendix B may be used to determine our sensitivity to ALPs.

D. ALP scan analysis

For the data generated during scanning for an ALP, the process just described to locate the most probable time and size for a jump is repeated for each machine cycle and bunch. A typical example is shown in Fig. 7. Unlike the Wien filter case, there is no apparent jump. The red curve shows the largest possible jump found. This result is consistent with the lack of a minimum in the associated chi-square versus time plot presented in Fig. 8. Together, these results point to the absence of a resonance between

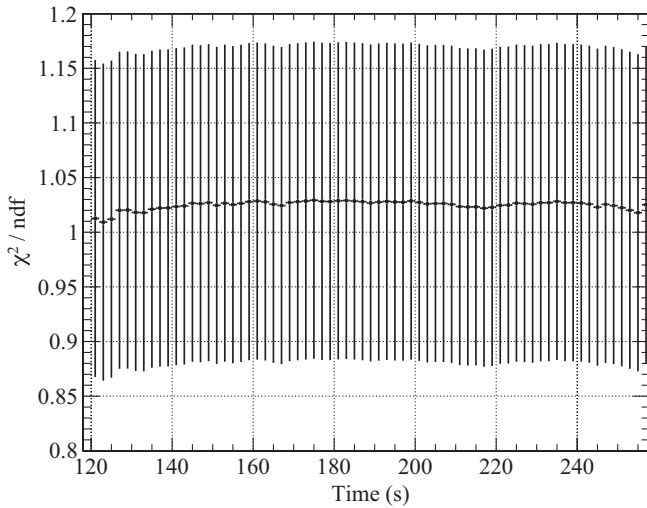


FIG. 8. Reduced chi-squared plot of the step function fits for an axion scan from one cycle. The absence of a minimum indicates no resonance. The vertical bar shows the standard deviation of the chi-square values based on the number of degrees of freedom.

the spin tune frequency and any ALP frequency within the range of the scan. The vertical bars in Fig. 8 indicate the standard deviation of the reduced χ^2 distribution given by $\sqrt{2/\text{ndf}}$, where ndf indicates the number of degrees of freedom in the fit with $\text{ndf} = 2 \times 15$ flat region points + 68 scan region points — 3 fit variables = 95. (This corresponds to a standard deviation of 0.145.) Figures 7 and 8 are for the scan data what Figs. 5 and 6 are for the Wien filter data.

To avoid missing an ALP due to a phase mismatch, the search results from all four bunches in each time bin of a scan are combined to produce a single sinusoidal curve as a function of possible phase using the formula

$$f(\phi_m) = C_1 \sin \phi_m + C_2 \cos \phi_m, \quad (28)$$

$$\hat{A} = \sqrt{C_1^2 + C_2^2}, \quad (29)$$

where m denotes the bunch number. The y axis is renormalized and shows the amplitude of each jump analysis divided by the in-plane asymmetry A_{IP} at the time of the tentative jump. The amplitude of the sinusoidal fit is given by Eq. (29). The spacing between the bunches on the ϕ_m axis is $\pi/2$ in Fig. 9. As discussed at the end of Sec. II A, the spacing is not always equal but oscillates between two extreme values. A correction is made for this effect.

The jump amplitude \hat{A} (29) from the sinusoidal fit is calculated for each time bin, and Fig. 10 shows the time distribution of that amplitude for one cycle. For multiple cycles covering the same frequency region, the mean amplitude is calculated for each time bin as a weighted average of amplitudes from the individual cycles. That

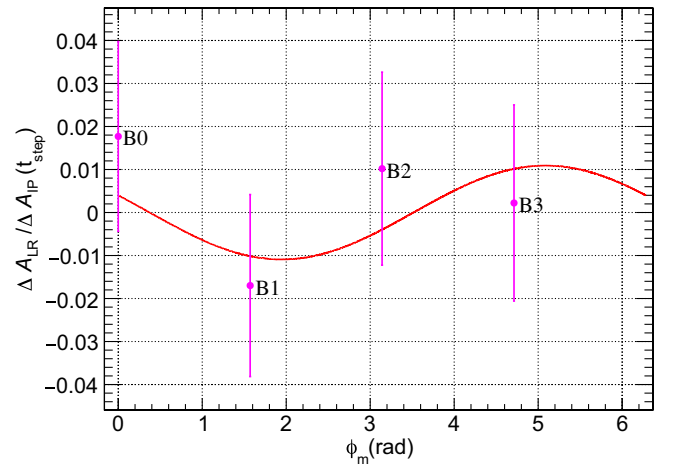
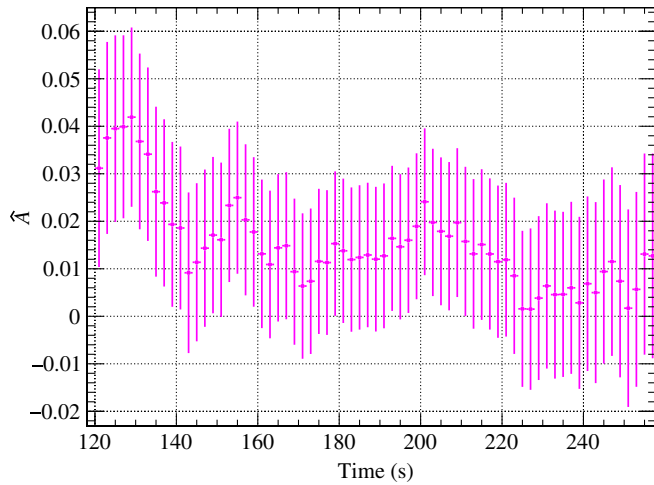


FIG. 9. Left-right asymmetry jump for all four bunches, from one cycle, as a function of the angle between the bunch polarization and the axion phase ϕ_m for a single time bin. The red curve is the sinusoidal fit from which the jump amplitude \hat{A} is calculated.

FIG. 10. Amplitude \hat{A} from sinusoidal fit for a single cycle.

mean and its uncertainty enter the next stage of the calculation of the confidence limit.

E. Construction of confidence interval

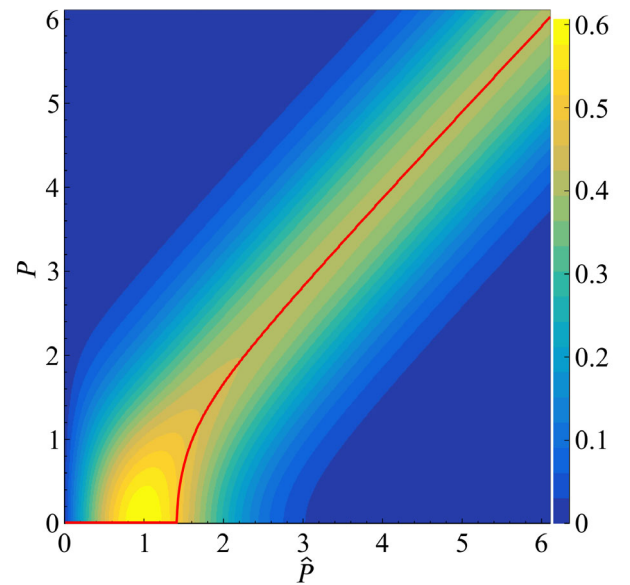
The use of Eqs. (28) and (29) is designed to capture any possible ALP regardless of the ALP phase at the time of resonance crossing. The cost of using these equations is that near zero amplitude, where most of the results will be, there is a systematic tendency to overestimate the size of the jump. Equation (29) always generates a positive definite value. There is no distribution about zero that would allow zero as a mean. If \hat{A} would happen to be large compared to its error, this effect would fade. To account for this positive bias and calculate a meaningful upper limit, the Feldman-Cousins procedure [67] is used to construct the confidence interval. References [69,70] contain a detailed discussion on how the procedure is used for these cases.

In these references, the discussion describes how to interpret the estimated amplitude (\hat{A}) in terms of a true amplitude (A). In order to facilitate the application to a large number of time bins as a function of ALP frequency, we switch to the amplitude normalized by the statistical error. This gives the normalized estimated value ($\hat{P} = \hat{A}/\sigma_{\text{exp}}$) and true value ($P = A/\sigma_{\text{exp}}$). The advantage is that we do not need to regenerate the interpretation for each time bin.

The probability density function (PDF) for data distributed according to $\hat{A} = \sqrt{C_1^2 + C_2^2}$ is given in Eq. (2.2) in Ref. [70]. Modifying this for the P quantity, we obtain

$$f(\hat{P}|P)d\hat{P} = e^{-(\hat{P}^2 + P^2)/2} \hat{P} I_0(\hat{P}P) d\hat{P}, \quad (30)$$

where I_0 is the modified Bessel function of the first kind. Equation (30) is called the Rice distribution. A two-dimensional graphical representation of this distribution for $0 \leq P \leq 6$ is shown in Fig. 11. The red line denotes

FIG. 11. A two-dimensional Rice plot for one cycle. The red line represents the value of P for which Eq. (30) is maximum for a given value of \hat{P} .

P_{best} , which is the value of P for which $f(\hat{P}|P)$ has the maximum probability in the physically allowed region for P .

The distortion of the distribution away from a typical Gaussian shape where $P \approx \hat{P}$ becomes clear below $\hat{P} = 2.5$. For quantities that are near zero, the estimated or experimental value is about one. This means that the experiment seems to produce evidence of an effect even though it is significant only at the one standard deviation statistical level.

Next, a likelihood ratio R is calculated using the following definition:

$$R = \frac{f(\hat{P}|P)}{f(\hat{P}|P_{\text{best}})}. \quad (31)$$

Two examples of the likelihood curve for $P = 1.0$ and 2.8 are shown, in blue, in the top row in Fig. 12. The Feldman-Cousins confidence interval is constructed by determining the bounds within which the integral of $f(\hat{P}|P)$ reaches the desired confidence interval, e.g., 90%. The bottom row in Fig. 12 shows the PDF for $P = 1.0$ and 2.8 along with the gray shaded region denoting the 90% confidence limit for the two cases above.

The confidence limit bounds on \hat{P} are determined by starting with the largest value of R where it is one and following the two limit points given by the intersection of a straight horizontal line with the likelihood ratio curve as the line moves down the plot. In the upper left case, where the curve ends at $\hat{P} = 0$ as the horizontal line crosses $R = 0.6$, the left axis where $\hat{P} = 0$ replaces the lower limit

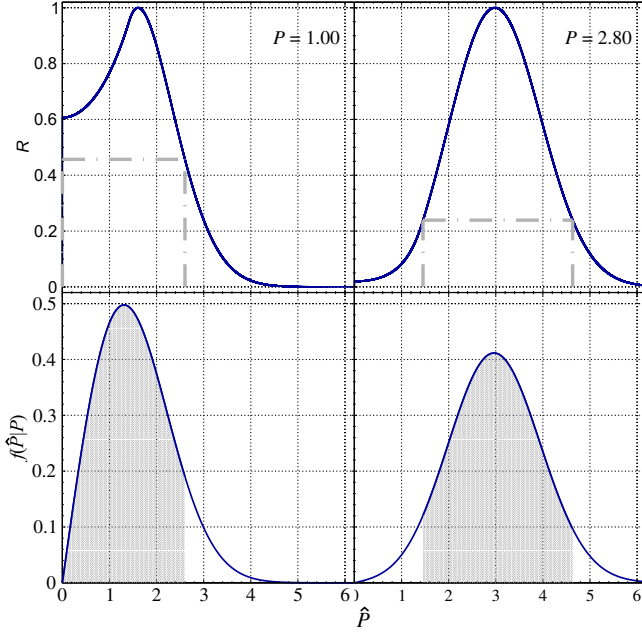


FIG. 12. Two examples, (left) $P = 1.0$ and (right) $P = 2.8$, for the calculation of 90% confidence limits using the likelihood ratio given by Eq. (31) (top row) and PDF given by Eq. (30) (bottom row). The gray horizontal dashed line in the likelihood ratio curves denotes the R value for which the corresponding \hat{P} values (gray vertical dashed lines) forms the 90% integral in the PDF curves. The gray shaded region marks the 90% integral region.

of the R curve. This process continues until the integral (gray shading) of the lower curve between the two limits reaches the desired confidence level. For the right-hand “Gaussian” case, both limits are still on the R curve and are roughly symmetric about the peak of R . The lower and upper limits of approximately 1.5 and approximately 4.6 represent the bounds of the 90% confidence interval. For the “left-hand” case, there is only an upper limit at approximately 2.6. Most of the data points in this experiment follow this example.

A summary of all of the limits for P may be found in Fig. 13. Inside the blue band, the confidence is 68%. The gray band outside the blue band shows the edges for the 90% limit. For a given value of \hat{P} , trace a line upward until it crosses the appropriate boundary. The case shown is for an upper limit only where there is no lower limit other than zero. These limits correspond to a single beam fill in the experiment with only one scan.

Since most scans comprise eight cycles, the confidence interval needs to be constructed taking this into account. A few scans comprise seven, nine, or 16 cycles. According to the central limit theorem, for n cycles, \hat{P} follows a Gaussian distribution, the mean amplitude remains at the same A value, and the uncertainty is $\sigma_n = \sigma_{\text{exp}}/\sqrt{n}$. It is assumed that this is approximately true, since, once set up, the beam current reproduces well from cycle to cycle for any particular scan. All σ_{exp} are the same for cycles being

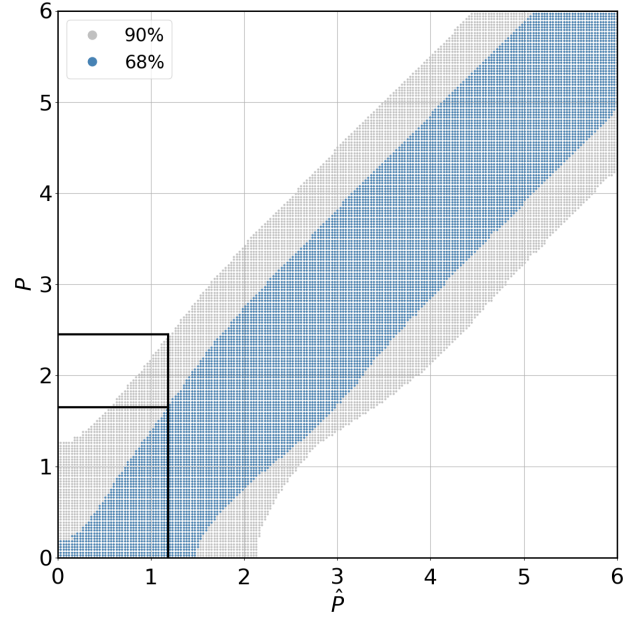


FIG. 13. A 68% (blue) and 90% (gray) confidence interval for one-cycle analysis. On the x axis we have the estimated value \hat{P} , and on the y axis is the true value P .

averaged this way. The PDF for n cycles is a Gaussian with $P = A/\sigma_n$:

$$f(\hat{P}|P) = \frac{1}{\sqrt{2\pi}\sigma_{\text{Rice}}} e^{-(\hat{P}-\mu_{\text{Rice}})^2/2\sigma_{\text{Rice}}^2}, \quad (32)$$

$$\mu_{\text{Rice}} = \sqrt{\frac{\pi}{2}}\sqrt{n}L_{1/2}\left(-\frac{1}{2}\frac{P^2}{n}\right), \quad (33)$$

$$\sigma_{\text{Rice}}^2 = 2 + \frac{P^2}{n} - \frac{\pi}{2}L_{1/2}^2\left(-\frac{1}{2}\frac{P^2}{n}\right), \quad (34)$$

where $L_{1/2}$ is the generalized Laguerre function.

Figure 14 is the two-dimensional plot for $n = 8$ calculated using Eq. (32). The construction of confidence interval follows the one-cycle case. The confidence interval for $n = 8$ is shown in Fig. 15. The edges of the blue and gray bands represent the 68% and 90% confidence levels, respectively.

Care must be taken if the observed \hat{P} is less than the expected value μ_{Rice} . These are considered to be from downward statistical fluctuations, and P is calculated at μ_{Rice} as explained in Ref. [67]. For each experimentally obtained value of \hat{P} , the corresponding boundary values of P are determined. This value is multiplied by the experimental uncertainty σ_n to give the true amplitude A . In the frequency range or axion mass range covered by the experiment, no signal is observed that could not be explained by a statistical fluctuation. Note that, in setting a 90% confidence interval, one expects in 10% of the cases a lower limit larger than zero even if no signal is

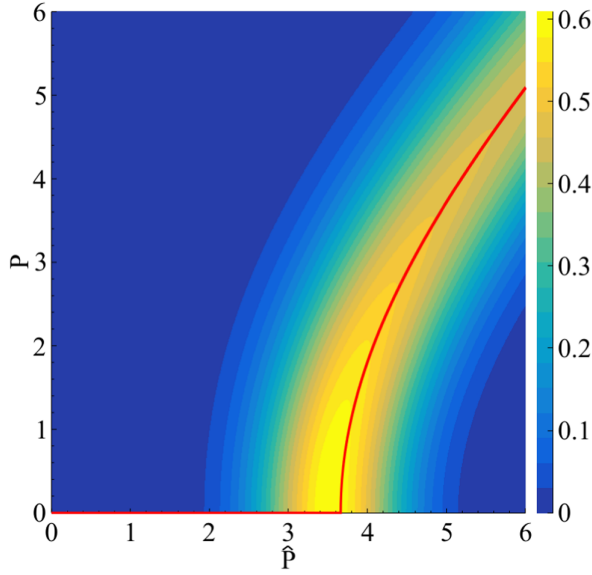


FIG. 14. A two-dimensional Rice plot for eight cycles. The red line represents the value of P for which Eq. (32) is maximum for a given value of \hat{P} .

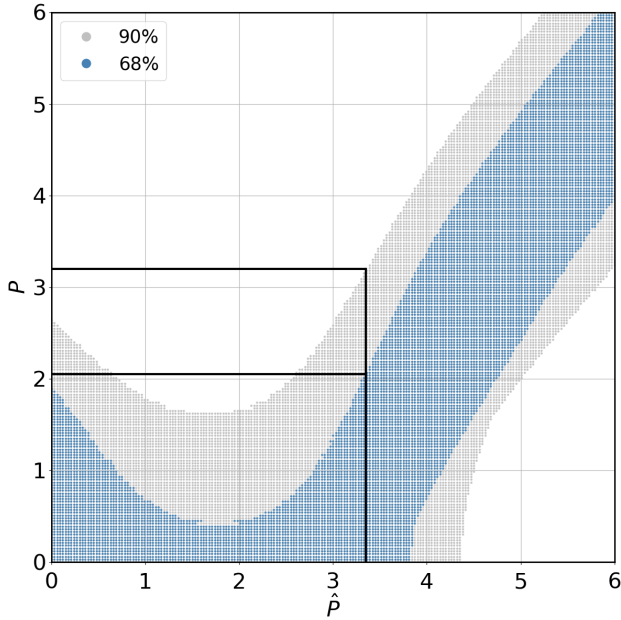


FIG. 15. A 68% (blue) and 90% (gray) confidence interval for the multicycle analysis ($n = 8$). On the x axis we have the estimated experimental value \hat{P} , and on the y axis is the true value P . For an experimental value of $\hat{P} = 3.3$, the true value P can be found between 0 and 3.15 with a confidence of 90%.

present. This corresponds to our observation, as shown in Fig. 16. From this, we also conclude that at this level of precision there is no systematic effect resulting in a fake signal.

The conversion into a limit of the oscillating EDM of the deuteron is done through the equation

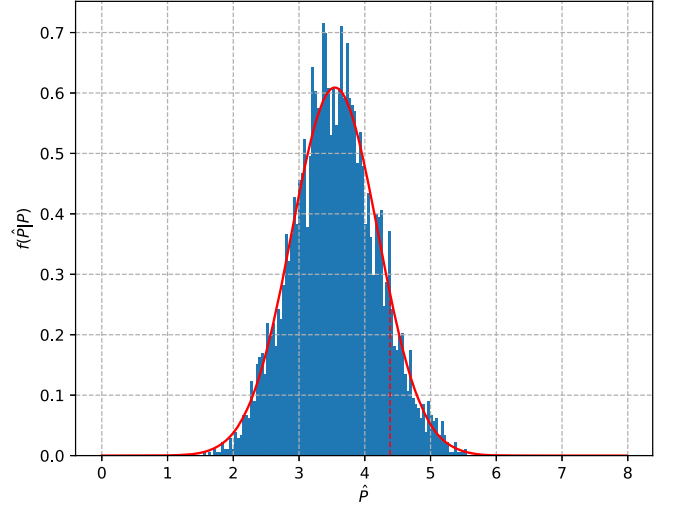


FIG. 16. The blue histogram is the distribution of \hat{P} , normalized such that the integral is one. The experimental data are in good agreement with the probability density function for $P = 0$ [Eq. (32)] drawn in red. In both cases, there are $n = 8$ cycles. The vertical red line at $\hat{P} = 4.38$ corresponds to the lower limit of the 90% confidence interval being greater than zero. This is the case for 9.63% of the contributing data points.

$$|d_{ac}^d| = \lambda A \times 10^{-23} \text{ e} \cdot \text{cm}, \quad (35)$$

where here and in the following we use the convention that the unit of electric charge e is defined to be positive. The coefficient $\lambda = 316$ for the fast ramps and 286 for the slow ramps, respectively. λ is based on a model of the polarization jump size for a particular ramp rate. The derivation of Eq. (35) is given in Appendix B; see Eq. (B7).

IV. RESULT AND DISCUSSION

A. Limits of ALP signals

According to Refs. [44,45], the angular velocity $\vec{\Omega}$ of the extended Thomas-BMT equation (12) of a beam with particles of mass m , charge q , spin S , Lorentz factor γ , and velocity $\vec{v} = c\vec{\beta}$ acquires the following oscillating term:

$$\begin{aligned} \vec{\Omega}_{a(t)} &= -\frac{1}{S\hbar} \frac{d_{ac}}{a_0} a(t) c\vec{\beta} \times \vec{B} - \frac{1}{S\hbar} \frac{C_N}{2f_a} \hbar \partial_0 a(t) \vec{\beta} \\ &= d_{ac} \frac{c\gamma m}{q\hbar S} \cos[\omega_a(t - t_0) + \phi_a(t_0)] \vec{\beta} \times \vec{\Omega}_{\text{rev}} \\ &\quad + \frac{C_N}{2f_a S} \omega_a a_0 \sin[\omega_a(t - t_0) + \phi_a(t_0)] \vec{\beta}, \end{aligned} \quad (36)$$

whenever a classical ALP field, as in Eq. (3), couples to the particles stored in the beam; cf. Eqs. (8)–(11). Note that the magnetic field in the laboratory system can be expressed as $\vec{B} = (-m\gamma/q)\vec{\Omega}_{\text{rev}}$ in terms of the angular revolution velocity of the particle beam, $\vec{\Omega}_{\text{rev}}$, as shown in Eq. (14).

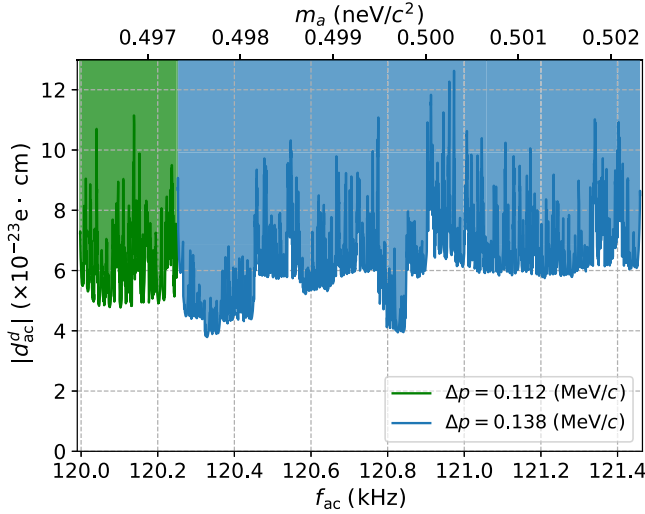


FIG. 17. 90% confidence level sensitivity for excluding the ALP-induced oscillating EDM ($e \cdot \text{cm}$) in the frequency range 120.0–121.4 kHz ($m_a = 0.495\text{--}0.502$ neV/c^2). More explanation may be found in the text.

According to Eq. (36), the spin rotation around the axis $\vec{\beta} \times \vec{\Omega}_{\text{rev}}$ (the latter always points radially outward, regardless of whether the beam is rotating clockwise or counter-clockwise) is generated by the ac part of the electric dipole moment of the beam particle [see Eq. (7)] which, in turn, is induced by the ALP field, while the spin rotation with respect to the longitudinal axis $\vec{\beta}$ of the beam (see Refs. [44,45]) follows from the pseudomagnetic (axion-wind) effect [18,39] of strength C_N/f_a in terms of the axion decay constant f_a [12]. In the experiment, we cannot distinguish these two rotation types around two orthogonal axes which both induce—on resonance—a polarization shift in the vertical direction but are $\pi/2$ out of phase with each other, so that the two rotation amplitudes add up coherently.

Thus, to obtain an upper limit on d_{ac} or C_N/f_a , one has to assume that the other term vanishes, such that the bound is saturated by one term only.

First, we assume that only the EDM term is present, i.e., $C_N/f_a = 0$. Figure 17 provides the 90% confidence level sensitivity for excluding the ALP-induced oscillating EDM of the deuteron, d_{ac}^d , in the frequency range of 120.0–121.4 kHz and the corresponding axion mass range of 0.495–0.502 neV/c^2 represented on the upper axis. The darker lines indicate the upper limit of the oscillating EDM, and the lighter filled region above is the exclusion region. The green and blue colors differentiate the two different ramp rates mentioned in Sec. II B. The green indicates a momentum change $\Delta p = 0.112$ MeV/c and the blue $\Delta p = 0.138$ MeV/c .

The fluctuations in the exclusion plot result mainly from two beam properties, intensity and polarization, as well as the clock time during the scan. Good beam properties mean better sensitivity. The dependency of intensity is seen in a

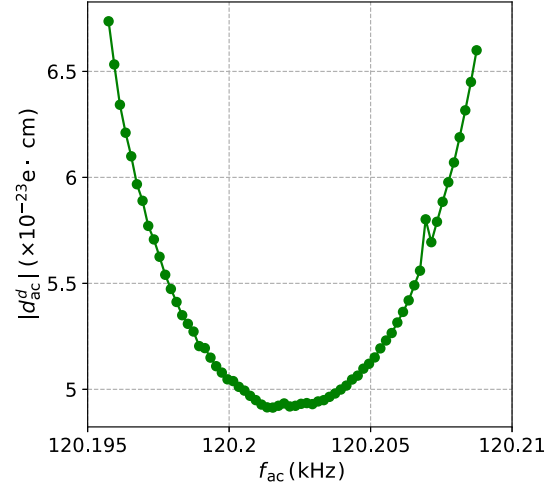


FIG. 18. Sensitivity of a single scan including eight cycles. The sensitivity decreases and the curve gets larger as one moves away from the center of the scan. There is no overlap between the scans in this example.

larger scale over multiple scans. If, for a particular frequency range, a larger number of scans are performed, the obtained sensitivity is better. This can be observed in Fig. 17 around frequency 120.8 kHz, for example. The decline in sensitivity within a cycle is mainly due to beam depolarization.

A small contribution to these fluctuations arises from the way ΔA_{LR} is calculated in Eq. (26). As a consequence, the sensitivity becomes worse as one moves further from the middle of the scan, because the imbalance in the number of points on both sides of the anticipated jump in the calculation of ΔA_{LR} leads to a larger uncertainty in the jump. An example of how this sensitivity appears for a single scan region comprising eight cycles is shown in Fig. 18. However, the intensity of the beam and the polarization have the greatest influence, and their combination is the reason for the higher values ($|d_{\text{ac}}^d| > 8 \times 10^{-23}$ $e \cdot \text{cm}$).

This experiment to search for ALPs in the storage ring provides a 90% confidence level upper bound of

$$|d_{\text{ac}}^d| < 6.4 \times 10^{-23} \text{ e} \cdot \text{cm}. \quad (37)$$

This value is used to calculate ALP coupling constants in the next subsection and is based on the average of the individual limit points in Fig. 17. These data are available online in Ref. [71].

B. Limits of various ALP couplings

In this paper, we focus on the coupling of ALPs to the deuteron spin via the oscillating part of the deuteron EDM d_{ac}^d and/or via the axion-wind effect proportional to C_d/f_a . For all these calculations, it is assumed that the local dark-matter density $\rho_{\text{LDM}} = (0.55 \pm 0.17)$ GeV/cm^3 (see, e.g., Chap. 27 in Ref. [12]) contains only ALPs.

The bound on the amplitude of the oscillating deuteron EDM d_{ac}^d [cf. Eq. (37)] can be interpreted as a bound on the axion coupling to the deuteron EDM operator [in analogy to the axion coupling to the nucleon EDM operator $g_{aN\gamma}$ of Eq. 90.38 in Ref. [12]; see also Eqs. (8) and (9) in terms of the electromagnetic fine-structure constant α :

$$|g_{ad\gamma}| = \frac{|d_{ac}^d|}{a_0} \frac{\sqrt{4\pi\alpha}}{e\hbar c} < 1.7 \times 10^{-7} \text{ GeV}^2. \quad (38)$$

Here, we assume that $a_0 = \sqrt{2\rho_{\text{LDM}}(\hbar c)^3}/(m_a c^2) = 5.8 \text{ MeV}$. The occurrence of the axion or ALP amplitude a_0 in the denominator of Eq. (38) is typical when the calculation is based on axions or ALPs as candidates for (local) dark-matter particles. The inverse proportionality of a_0 and m_a implies that the exclusion limits derived from oscillating EDM measurements at similar experimental sensitivity have to be linearly increasing functions of the ALP mass m_a .

Figure 19 shows the limit on $|g_{ad\gamma}|$ from this experiment in cyan along with bounds for $|g_{aN\gamma}|$ from the nEDM [25], CASPER-electric [72], and Beam EDM [73] experiments. In addition, the figure presents the $|g_{aN\gamma}|$ exclusion region

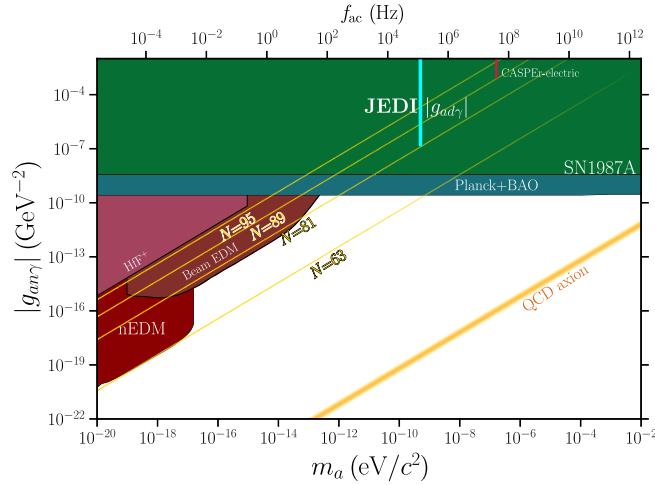


FIG. 19. The 90% upper bound on $|g_{ad\gamma}|$ from this experiment (in cyan) is shown along with the bound on $|g_{aN\gamma}|$ from experiments such as nEDM [25], CASPER-electric [72], HfF^+ [26], and Beam EDM [73] (as presented in Ref. [74]), in different shades of red. Also, seen in green is the constraint, calculated in Ref. [18] from the SN1987A supernova energy loss, which might be model dependent [75]. In blue, a further constraint calculated in Ref. [76] from the combined Planck 2018 and baryon acoustic oscillation cosmological data is displayed (as presented in Ref. [74]). Finally, the yellow lines $\mathcal{N} = n$, parallel to the QCD axion band and plotted according to Eqs. (2) and (90.5) in Ref. [12], indicate that $Z_{\mathcal{N}}$ axions with $\mathcal{N} > n$ are excluded by the above-mentioned *measured* bounds in their respective mass ranges. Figure courtesy of Refs. [12,74].

as tabulated in Ref. [74] via reformulating the limits of the electron-EDM HfF^+ experiment (see Fig. 3 in Ref. [26]). Furthermore, a constraint on $|g_{aN\gamma}|$ is shown that is derived in Ref. [18] from assuming $N + \gamma \rightarrow N + a$ cooling in SN1987A. Thus, the latter bound is based on the strength of the coupling constant in the axion or ALP interaction with the nucleon EDM and is, therefore, independent of m_a . Note, however, that Ref. [75] suggests an alternative collapse mechanism for supernovae SN1987A that would not place limits on the emission of ALPs or axions. Moreover, following Ref. [74], an exclusion region is shown that is based on a new constraint on the coupling of thermally produced ALPs as calculated in Ref. [76] from combined data of cosmic microwave background spectra and baryon acoustic oscillations. However, according to Ref. [76], these bounds are derived only for the mass range $10^{-4} \text{ eV}/c^2 \lesssim m_a \lesssim 100 \text{ eV}/c^2$. Our *directly measured* upper bound (38) at $m_a = 0.5 \text{ neV}/c^2$ falls within the model-dependent constraint obtained from SN1987A but is stronger than the CASPER-electric result at $m_a \approx 100 \text{ neV}/c^2$.

Finally, in Fig. 19, $|g_{aN\gamma}(m_a)|_{\mathcal{N}}$ lines of the $Z_{\mathcal{N}}$ -axion model are plotted which follow from the exclusion limits of the presented EDM-based experiments and which run parallel to the displayed QCD axion band. Each \mathcal{N} must be an odd-valued positive integer, as otherwise the pertinent model would not solve the strong CP problem (see Refs. [13,14]) and one would be back at the ALP case. In detail, according to Eq. (2) combined with Eq. (90.5) in Ref. [12], i.e.,

$$g_{aN\gamma} = (3.7 \pm 1.5) \times 10^{-3} \text{ GeV} \frac{1}{f_a(m_a)|_{\mathcal{N}}}, \quad (39)$$

$Z_{\mathcal{N}}$ axions with $\mathcal{N} > 81$ are excluded by our bound (38) at $m_a \approx 5 \times 10^{-10} \text{ eV}/c^2$. Even if the canonical QCD axion or ALP scenario prevails, the straight lines (proportional to m_a) that can be derived from Eq. (39) can still serve as excellent guides for “extrapolating” exclusion limits to different ALP masses and, therefore, comparing the experimental sensitivities of the underlying measurements of hadron (neutron, proton, deuteron, etc.) electric dipole moments. For instance, the line $\mathcal{N} = 63$ shows that the pertinent experimental sensitivity of the nEDM limits is approximately a factor of 10^3 better than in our experiment. This is compatible with a factor of approximately 10^{-3} between the oscillating neutron EDM bounds between $5.0 \times 10^{-26} \text{ e} \cdot \text{cm}$ and $7.0 \times 10^{-26} \text{ e} \cdot \text{cm}$ as shown in Fig. 2 in Ref. [25] and our upper bound $|d_{ac}^d| < 6.4 \times 10^{-23} \text{ e} \cdot \text{cm}$; see Eq. (37). The line $\mathcal{N} = 89$ indicates that the CASPER-electric limit [72] is roughly a factor of 20 less sensitive than that of our experiment, while the sensitivity of the Beam EDM

experiment [73] is slightly better than ours. Finally, the HfF⁺ limits [26] exclude $Z_{\mathcal{N}}$ axions with $\mathcal{N} > 95$ in the specified mass range. The corresponding $\mathcal{N} = 95$ line implies that the sensitivity of this *electron*-EDM-based experiment to constrain oscillating *hadronic* EDMs is about 10^2 times worse than in our case.

The second coupling we consider is the ALP-gluon coupling C_G/f_a , generated from the $\bar{\Theta}$ term for the permanent EDM case, where the use of C_G/f_a instead of just $1/f_a$ takes into account that the ALP coupling strength might differ from the axion one. The coupling is given by [17,25,77]

$$\begin{aligned} d_{\text{ac}}^{\mathcal{N}}(t) &= S \cdot \kappa_a \frac{e\hbar c}{2mc^2} \cdot \frac{C_G}{f_a} \cdot a_0 \cos[\omega_a(t-t_0) + \phi_a(t_0)] \\ &\approx 2.4 \times 10^{-16} \text{ e} \cdot \text{cm} \cdot \frac{C_G}{f_a} \cdot a_0 \cos[\omega_a(t-t_0) + \phi_a(t_0)], \end{aligned} \quad (40)$$

where S and m are the spin and mass of the nucleon, respectively, and κ_a is the chiral suppression factor of the $\bar{\Theta}$ term. Here, the loop-enhanced value $\kappa_a \approx 0.046$ of Refs. [12,25,77] is used. Note that the numerical factor $2.4 \times 10^{-16} \text{ e} \cdot \text{cm}$ is the same for proton (or neutron) and deuteron, because the ratio $S/m = (1/2)/m_p \approx 1/m_d$ is approximately the same for these particle species. Compared to the direct determination of C_G/f_a in the case of the nucleon, however, corrections are expected in the deuteron scenario. From the isoscalar nature of the deuteron nucleus and the isovector nature of the leading low-energy pion-loop contribution to the nucleon EDM [78–80], a severe cancellation between the contributions of its proton and neutron components is anticipated; see, e.g., Ref. [12]. Moreover, the small D -wave admixture of the deuteron wave function affects the weights of these individual nucleon components [81,82]. Finally, P - and T -breaking meson-exchange terms contribute already at leading tree-level order [83,84]. The latter contributions to the permanent EDM of the deuteron, induced by the QCD-theta term or more generalized chromoelectric EDMs of quarks, are shown to be of similar magnitude as the single nucleon ones; see, e.g., Refs. [81–90]. The ALP-gluon coupling in the deuteron case is, therefore, denoted in the following by an upper index d , i.e., C_G^d , to signal that this coefficient is likely to contain corrections of order one relative to the coupling C_G in the nucleon scenario.

So, substituting $S = 1$ and m_d for the deuteron, we get the bound on the coupling constant:

$$\begin{aligned} \left| \frac{C_G^d}{f_a} \right| &= \left| \frac{d_{\text{ac}}^d}{2.4 \times 10^{-16} \text{ e} \cdot \text{cm} \times a_0} \right| \\ &< 0.46 \times 10^{-4} \text{ GeV}^{-1}. \end{aligned} \quad (41)$$

Note again the a_0 dependence in the denominator which implies a linear dependence of the bound on ALP mass m_a and is a signal that the calculation is based on axions or ALPs as dark-matter candidates.

Figure 20 shows the upper bound on $|C_G^d/f_a|$ in comparison with the results on $|C_G/f_a|$ from the nEDM experiment [25], the HfF⁺ electron EDM [26], and the Beam EDM [73] experiments as well as the limits obtained from astrophysical calculations such as big bang nucleosynthesis, solar core, and supernova SN1987A [18]—the latter based on the $N + \gamma \rightarrow N + a$ cooling mechanism. Details can be found in Refs. [12,74]. Our result is within the limits obtained from the supernova emission. In addition, three $Z_{\mathcal{N}}$ lines are plotted, given directly by $1/f_a(m_a, \mathcal{N})$, as calculated in Eq. (2). They show that $Z_{\mathcal{N}}$ axions with $\mathcal{N} > 81$ and $\mathcal{N} > 63$ are again excluded by the JEDI and nEDM [25] experiments in their respective mass regions, while the eEDM-based HfF⁺ exclusion region (see Ref. [26]) vetoes $Z_{\mathcal{N}}$ axions with $N > 95$ in the specified mass range. Note that the apparently better fitting line $\mathcal{N} = 96$ can be excluded for another reason, since $Z_{\mathcal{N}}$ axions with even \mathcal{N} do not solve the strong CP problem.

Next, we consider the axion-wind case. By ignoring the EDM term in Eq. (36), we can provide a bound on the ALP (pseudomagnetic) coupling to the deuteron spin, $|C_d/f_a|$. On resonance and using Eq. (36), this limit can simply be expressed in terms of the limit on the oscillating EDM (37), $|d_{\text{ac}}^d| < 6.4 \times 10^{-23} \text{ e} \cdot \text{cm}$, as

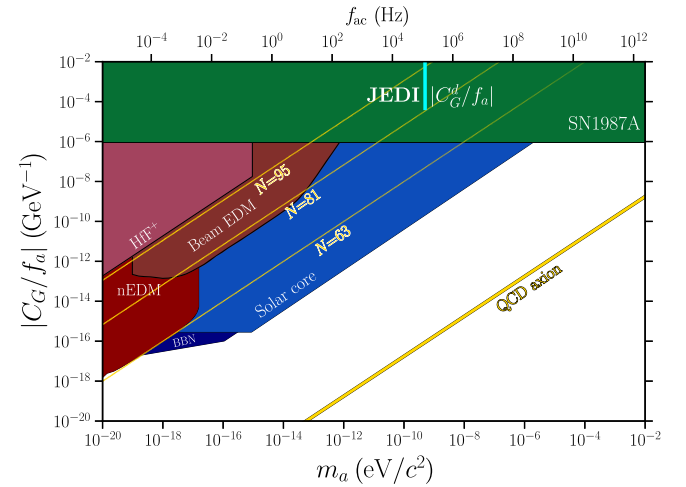


FIG. 20. Figure showing the 90% upper bound on $|C_G^d/f_a|$, in cyan, in comparison with the $|C_G/f_a|$ nEDM [25], HfF⁺ [26], and Beam EDM [73] results in various shades of red. Also shown are the limits from supernova SN1987A, as calculated in Ref. [18] in green, solar core [14,91] in lighter blue, and big bang nucleosynthesis [92] in darker blue. The three yellow lines $\mathcal{N} = n$, which are parallel to the QCD axion band, are calculated directly from Eq. (2) and indicate that $Z_{\mathcal{N}}$ axions with $\mathcal{N} > n$ are excluded by the above-mentioned *measured* bounds in their respective mass regions. Figure courtesy of Refs. [12,74].

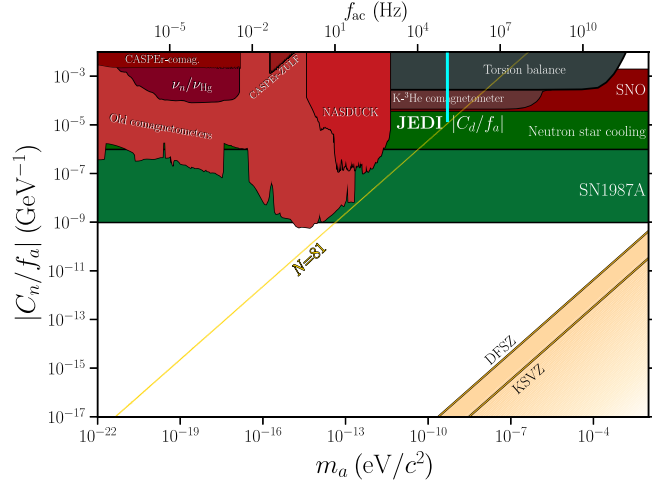


FIG. 21. Figure displaying the ALP-neutron coupling $|C_n/f_a|$ from various experimental results (CASPER-comag [93], ν_n/ν_{Hg} [25], CASPER-Zulf [94], old comagnetometers [95], NASTRUCK [96], torsion balance [97], K^3He comagnetometer [98], SNO [99], neutron star cooling [100], and SN1987A [101]). The 90% upper bound on the ALP-deuteron coupling, $|C_d/f_a|$ from the JEDI experiment, is shown in cyan, and the corresponding $Z_{\mathcal{N}}$ axion line, labeled $\mathcal{N} = 81$ and parallel to the DFSZ and KSVZ axion lines, is displayed in yellow. The limits from supernova SN1987A, as calculated in Ref. [101] (see also Ref. [102]), are presented in green. Figure courtesy of Refs. [12,74].

$$\begin{aligned} \left| \frac{C_d}{f_a} \right| &= \left| \frac{2\gamma m_d c}{e\hbar\omega_a a_0} \right| \cdot |\vec{\Omega}_{\text{rev}}| \cdot |d_{ac}^d| \\ &= \left| \frac{2m_d c}{e\hbar G a_0} \right| \cdot |d_{ac}^d| < 1.5 \times 10^{-5} \text{ GeV}^{-1}. \quad (42) \end{aligned}$$

In the second line, the ALP-resonance condition is applied, i.e., $\omega_a = \gamma|G\vec{\Omega}_{\text{rev}}|$, where G is here the magnetic anomaly of the deuteron. Thus, this limit also shows a linear dependence on the ALP mass m_a indicating axions and ALPs as dark-matter candidates.

The bound on the ALP-deuteron coupling $|C_d/f_a|$ is shown in Fig. 21. Other limits shown in this figure are bounds on ALP-neutron coupling.

Moreover, constraints from supernova SN1987A on $|C_n/f_a|$ are shown in green that are calculated in Ref. [102] and recently updated in Ref. [101]. Here, the underlying cooling mechanism is assumed to be of bremsstrahlung type, i.e., $NN \rightarrow NN a$. The result is, therefore, based on the strength of the coupling constant in the axion or ALP wind effect and is independent of m_a . Remember, however, that Ref. [75] suggests an alternative collapse mechanism for supernova SN1987A that would not place limits on the emission of ALPs or axions.

In addition, the displayed $Z_{\mathcal{N}} = 81$ line indicates that $Z_{\mathcal{N}}$ axions with $\mathcal{N} > 81$ at $m_a \simeq 5 \times 10^{-10} \text{ eV}/c^2$ are excluded. Here, $1/f_a(m_a, \mathcal{N})$ of Eq. (2) is now rescaled by a factor of approximately 1/3 in order to follow the

KSVZ axion line. The $\mathcal{N} = 81$ line shows that the underlying experimental sensitivity of the JEDI measurement is compatible with, if not better than, that of the old comagnetometers [95] and NASTRUCK [96] experiments.

This underlines the statement made earlier that the axion-wind effect in storage ring experiments is greatly enhanced relative to other laboratory measurements because it depends on the relative velocity of the axions with respect to the particle under study [see Eq. (36)]. In storage rings, one has $v \approx c$, whereas for particles at rest in the laboratory system [25,72], the relative velocity is given by the velocity of Earth with respect to the center of our Galaxy, i.e., $v \approx 250 \text{ km/s} \sim 10^{-3}c$. Since the latter contribution can be safely neglected in relativistic storage rings, the pertinent pseudomagnetic field of the axion wind always points tangentially to the beam trajectory. Therefore, the direction of \vec{v} is uniquely determined, while in laboratory experiments it depends in a complicated way on a time-dependent superposition of a considerable number of non-negligible motions.

It should be noted that Ref. [25] assumes $\rho_{\text{LDM}} = 0.4 \text{ GeV}/\text{cm}^3$ in contrast to $\rho_{\text{LDM}} = 0.55 \text{ GeV}/\text{cm}^3$ assumed in this paper. Thus, quoted coupling constants in this paper are approximately 0.85 times smaller compared to Ref. [25].

V. CONCLUSIONS AND OUTLOOK

This paper presents an experiment conducted to demonstrate a new method to search for ALPs using an in-plane polarized deuteron beam in a storage ring. The polarization vector of the deuteron beam is influenced by ALPs due to two effects. First, ALPs introduce an oscillating EDM, causing a spin rotation around a radial axis in the storage ring. Second, ALPs introduce the so-called axion-wind or pseudomagnetic effect resulting in a spin rotation around the longitudinal axis. Storage ring experiments are specifically sensitive to the second effect, because it scales with the velocity of the particles with respect to the axion field which moreover always points tangentially to the beam, i.e., in the same direction in the comoving (rest) frame of the beam particle.

The experiment did not see any ALP signal within the achieved sensitivity. An upper limit on the deuteron oscillating EDM is quoted for the first time. In the mass range $m_a = 0.495\text{--}0.502 \text{ neV}/c^2$, oscillating EDM values above approximately $10^{-22} \text{ e} \cdot \text{cm}$ are excluded by this experiment at least at a 90% level, assuming a direct EDM coupling. Constraints on other axion and ALP coupling strengths, like the ALP coupling to the EDM operator of the deuteron, $g_{ad\gamma}$, the ALP-gluon coupling of the deuteron, C_G^d/f_a , and the ALP (pseudomagnetic) coupling to the deuteron spin C_d/f_a , are estimated as well.

As a proof of principle for ALP searches in storage rings, this experiment was just an exploratory study where the actual data taking period for the axion search was only four

days. In future experiments with extended beam times and higher beam intensities, the sensitivity can be increased by at least an order of magnitude. Systematic effects are not expected to play an important role, since one is looking for an ac effect at a particular frequency.

In the future, new types of storage rings to measure the permanent EDM of charged hadrons are planned [29]. This would allow the search for axions essentially in the whole mass range displayed in Figs. 19–21. For this kind of storage ring, it is proposed to use a combination of radial electric and vertical magnetic bending fields. In this case, the spin-precession frequency $\vec{\Omega}_{\text{MDM}} - \vec{\Omega}_{\text{rev}}$ is given by

$$\vec{\Omega}_{\text{MDM}} - \vec{\Omega}_{\text{rev}} = -\frac{q}{m} \left[G\vec{B} - \left(G - \frac{1}{\gamma^2 - 1} \right) \frac{\vec{\beta} \times \vec{E}}{c} \right]. \quad (43)$$

By using appropriate combinations of the electric and magnetic field, the amplitude of $\vec{\Omega}_{\text{MDM}} - \vec{\Omega}_{\text{rev}}$ can be varied from 0 to the values corresponding to $\omega_a = m_a c^2 / \hbar \simeq 10^{-9} \text{ eV} / \hbar$ as described in Ref. [103]. In that case, the relation of the EDM angular velocity [cf. Eq. (15)] becomes

$$\vec{\Omega}_{\text{EDM}} = -\frac{1}{S\hbar} d(t)(\vec{E} + c\vec{\beta} \times \vec{B}) \quad (44)$$

but still agrees with the second line in Eq. (36) when expressed as a function of the angular velocity of beam revolution. Also, the relation of the axion-wind angular velocity remains unchanged; see Eq. (16) and the third line in Eq. (36).

Recently, various ideas have been discussed in the literature to extend the here presented and established storage ring searches for axions and ALPs: namely, by applying, e.g., *static* Wien filters or modulating radio-frequency *cavities* (see Ref. [44]) or by using radio-frequency Wien filters operating at the *sidebands* of the axion frequency ω_a and Ω_{MDM} as discussed in Ref. [30].

This kind of experiment can be further explored at facilities like RHIC, NICA, or GSI/FAIR where polarized hadrons beams are either available or planned or could be added to the physics program. Using different particles (protons, deuterons, nuclei, and even leptons) would allow one to study the influence of spin and isospin on various couplings. Moreover, it offers the possibility to perform measurements with different G factors.

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APPENDIX A: CALCULATION OF THE RELATIVE IN-PLANE POLARIZATION DIRECTIONS USING FOUR BUNCHES

The signal of an ALP in a storage ring requires that the oscillation of the EDM be in phase with the rotation of the deuteron polarization in the ring plane. Specifically, the maximum value of the EDM must occur when the polarization is oriented perpendicular to the direction of the electric field in the particle frame of reference. During the search, the phase of the ALP is unknown. In order to make the effect visible for any phase, we choose to operate the COSY rf on the fourth harmonic ($h = 4$) of the revolution frequency and store four beam bunches. This appendix demonstrates that this choice provides beams with different phases between the oscillating EDM and the direction of the rotating beam polarization. Since the wavelength of the axion field is much larger than the physical size of the COSY ring, this allows the ALP signal to be observed regardless of the ALP phase.

The beam is loaded into COSY with the polarization oriented in the vertical direction. Rotation of the polarization into the ring plane is accomplished by operating an rf solenoid for a brief period of time. If the solenoid rf operates at the same frequency as the in-plane rotation of the polarization, then the small rotation induced by the solenoid accumulates. Continuous running of the solenoid produces an oscillation of the vertical polarization component. If the solenoid is stopped when the polarization reaches the in-plane orientation, then the beam is prepared for the experiment.

This result may be calculated using a simple series of classical rotations, each associated with one turn of the beam around COSY. For this, a comoving coordinate system is used with the z axis pointing in momentum direction, the y axis upward parallel to the magnetic field, and, consequently, the x axis from the center of the ring outward as the beam is rotating clockwise. In the model, the polarization is described by a vector $[p_x, p_y, p_z]$ with the initial polarization $[0, 1, 0]$. One turn around the ring is described by two rotations, one (θ)

for the precession in the ring magnets and another (α) for the precession in the rf solenoid, as shown in Eq. (A1):

$$\begin{bmatrix} p'_x \\ p'_y \\ p'_z \end{bmatrix} = \begin{bmatrix} \cos \alpha & -\sin \alpha & 0 \\ \sin \alpha & \cos \alpha & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \cos \theta & 0 & \sin \theta \\ 0 & 1 & 0 \\ -\sin \theta & 0 & \cos \theta \end{bmatrix} \begin{bmatrix} p_x \\ p_y \\ p_z \end{bmatrix}. \quad (\text{A1})$$

The primed spin vector is the result of one revolution of the beam around the ring. The rotations may be treated separately, since the length of the rf solenoid is very short compared with the circumference of the ring. For the purposes of a computer-based calculation, the precession of the spins about the y axis in the ring magnets per turn is given by $\theta = -2\pi G\gamma$, where $G = -0.1429875424$ is the deuteron magnetic anomaly and $\gamma = 1.1259762$ is the relativistic factor at the initial beam energy. This rotation is the same for every turn. The rf solenoid operates on a harmonic of the revolution frequency and with an adjustable strength $4\pi\epsilon_{\text{sol}}$, such that $\epsilon_{\text{sol}} = f_{\text{sol}}/f_{\text{rev}}$ with f_{sol} being the frequency of the resulting driven spin oscillations. Thus, $\alpha = 4\pi\epsilon_{\text{sol}} \cos[2\pi n(1 + G\gamma) + \phi]$, where n is the turn count (or the number of times the two rotations are applied) and ϕ is a phase that is described later. For each turn of the beam, the operation shown in Eq. (A1) is repeated based on the result of the previous series of rotations. The solenoid rotation α is cumulative, adding another $4\pi\epsilon_{\text{sol}} \cos[2\pi n(1 + G\gamma)]$ to the previous value on each turn.

A program is written to complete the numerical sum of all rotations. In the model, 2×10^6 turns are used, and a value of $4\pi\epsilon_{\text{sol}} = 1.5708 \times 10^{-6}$ brings the vertical polarization very close to zero.

To simulate what happens for each of the four beam bunches, we need to repeat the calculation described above but with an initial phase added to the rf solenoid angle α to describe the delay in the phase for each bunch. For the first bunch, denoted as B0, $\phi = 0$. For the three subsequent bunches, the starting phase is $U(1 + G\gamma)$, where $U = \pi/2, \pi$, and $3\pi/2$ for bunches B1, B2, and B3, respectively.

The orientation of the polarization at the end of this process can be described using the x and z coordinates as follows.

The angle starts at the z axis. The first four columns in Table VI show the results at the end of 2×10^6 turns. The last column shows the differences in the polarization directions between adjacent bunches, as predicted by the rotation model. The phase angles in the next to last column apply at the time that the bunch lands in the ring plane, which is different for each bunch. There is also a polarimeter in the COSY ring that is capable of measuring the phase at the beginning of each 4-s time interval. It is worth noting that the spacing between the bunches is not equal

TABLE VI. Model calculation of bunch spin directions as measured at a fixed point in the ring, e.g., at the polarimeter.

Bunch	x	z	Angle (rad)	Angle B($n-1$)-B(n)
B0	-0.639 562	0.768 740	-0.693 928	
B1	-0.904 313	-0.426 870	-2.011 825	1.317 897
B2	0.187 022	-0.982 356	-3.328 722	1.317 897
B3	0.997 903	-0.064 724	-4.647 619	1.317 897
B0 (again)				2.329 493

across the break from B3 to B0. Thus, we should be able to tell from the relative phases which bunch is the first. Sample results are given in Fig. 22.

The match of the phase differences in Fig. 22 with the predictions in Table VI (column 5) shows that the process of using an rf solenoid to rotate the spins into the horizontal plane matches the model.

Using the model results as a starting point, we can extrapolate forward in the calculation to the same point in time for each bunch. If we choose the moment when the rotation of B3 to the horizontal plane is complete, then the in-plane rotation of bunches B0, B1, and B2 moves forward by $3\pi/2, \pi$, and $\pi/2$, respectively. This produces a final orientation of the polarization given by Table VII.

An inspection of the x and z columns shows that these four polarization directions form right angles to each other in the beam coordinate system, thus mapping out a space in all directions. The rotation of the ALP EDM is generated

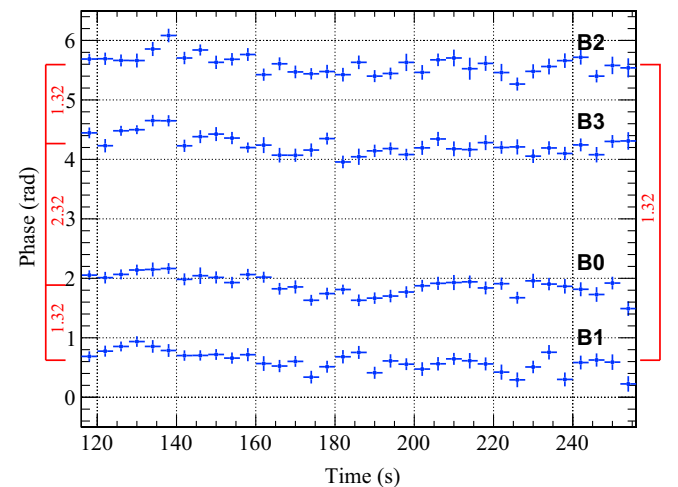


FIG. 22. Measurements of the phase of the in-plane polarization of a four-bunch beam as a function of the time in the store after the rf solenoid is turned off. The four bunches are B0, B1, B2, and B3. The differences in phase angle are indicated by the red diagram that includes the relative bunch angles in radians. A fixed value of the spin tune $G\gamma$ is assumed during the analysis in order to freeze any phase drift with time.

TABLE VII. Model calculation of bunch spin directions as measured at a fixed point in time, i.e., when bunch B3 is completely rotated into the horizontal plane.

Bunch	x	z
B0	0.064 724	0.997 903
B1	-0.997 903	0.064 724
B2	-0.064 724	-0.997 903
B3 (no change)	0.997 903	-0.064 724

by the presence of an electric field in the rest frame of the deuterons as they pass through the ring magnets and are subject to a vertical lab magnetic field. This induces a force on the deuterons, $\vec{F} = ec\vec{\beta} \times \vec{B}$, that bends them into the closed orbit around the ring. The resulting electric field in the comoving frame also creates a torque on the oscillating EDM to the extent that the latter is perpendicular to the field at the time that the EDM is at an extreme point in its oscillation. Note that the electric field points toward the center of the ring. With this assortment of polarization directions, all phases (represented by sine and cosine functions) generate a measurable change in the vertical polarization, and no ALP field goes undetected due to phase mismatch. In addition, the presence of polarizations of opposite sign ensures that any nonzero offset in the polarimeter that measures the size of the resonant jump is offset by a jump on the opposite bunch that is of equal and opposite sign.

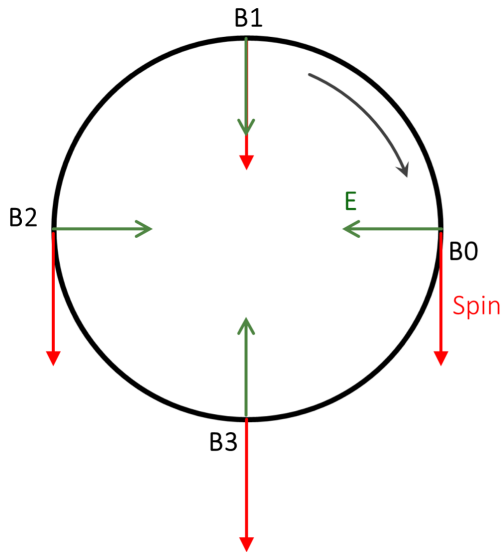


FIG. 23. Diagram showing the orientations of the polarization relative to the electric field for the four bunches circulating in the storage ring, as given in Table VII. The black arrow shows the direction of the clockwise rotating beam, while the rotation of the spins of the deuterons in the comoving frame and the order of the bunches on the ring (B_i , $i = 0, 1, 2, 3$) are counterclockwise (all viewed from above).

The orientations of the polarization relative to the electric field are illustrated by the diagram in Fig. 23. It then becomes clear that the polarization direction for each of the bunches relative to the local electric field is perpendicular to the bunch preceding it. All the polarizations are either parallel or perpendicular to their respective electric fields. This figure assumes a circular ring without straight sections and a clockwise rotating beam viewed from above.

These calculations may be repeated for the case of the $1 - G\gamma$ harmonic. Here, the resulting phase gaps have a different pattern, which is also confirmed experimentally using the phase measurements. The modeling shows that a good polarization distribution among the four bunches is possible using either harmonic for the rf solenoid. There is a sort of symmetry between the two possibilities. The sets of phases as measured by a fixed polarimeter looking at the bunches one at a time are distinctive and allow one to pick out the “first” bunch in each group from its location next to the single gap that is different from all the rest. This result is impervious to a number of potential issues, including whether or not the rf solenoid switching time is gradual (as is the case experimentally) or instantaneous (as it is in the model).

APPENDIX B: CALCULATION OF THE SENSITIVITY CALIBRATION

Previous calculations of the response of the COSY storage ring have been made using a “no-lattice” model [60] of successive rotations without a breakdown for each element of the ring. While the rotations in the bending magnets are continuous in this model, other devices such as the rf solenoid (see Appendix A) and the Wien filter are relatively short and may be treated as having zero length. The spin rotation per turn due to the bending magnet is about the vertical axis and given by the rotation vector $\vec{\theta} = -2\pi G\gamma\vec{e}_y$ ($=\theta\vec{e}_y$). When we include the EDM, this introduces another continuous effect with a rotation about the radial [pointing outward from the center of the bend assuming $d > 0$ in Eq. (15)] axis given by $\vec{\psi} = 2\pi\vec{\Omega}_{\text{EDM}}/|\vec{\Omega}_{\text{rev}}|$ ($=\psi\vec{e}_x$). As a result, one gets a new, combined rotation about a new axis $\vec{\chi}$:

$$\vec{\chi} = \vec{\theta} + \vec{\psi}. \quad (\text{B1})$$

The situation is depicted in Fig. 24.

To calculate the result within the no-lattice model, we choose to tilt the reference frame about the z axis so that the new y axis lies along the total rotation vector $\vec{\chi}$. The angle of tilt becomes

$$\xi = \arctan \frac{\psi}{\theta}. \quad (\text{B2})$$

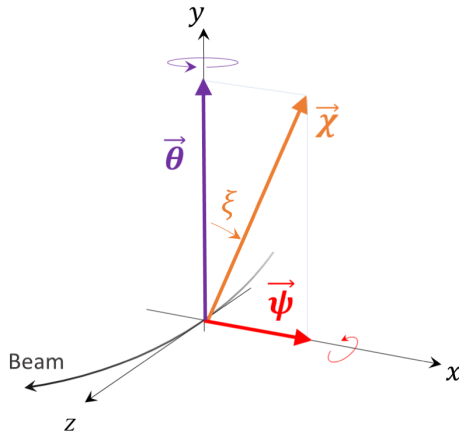


FIG. 24. Diagram showing the orientation of the rotation vectors associated with an EDM precession in the presence of bending in a storage ring. Coordinates and the bent particle path are shown. The total rotation $\vec{\chi}$ is the vector sum of $\vec{\theta}$ and $\vec{\psi}$. The angle between $\vec{\theta}$ and $\vec{\chi}$, denoted by ξ , is the angle of the coordinate system rotation (see the text). The size of $\vec{\psi}$ in this figure is exaggerated to make it visible to the reader.

One turn through the storage ring is represented by

$$\begin{bmatrix} p'_x \\ p'_y \\ p'_z \end{bmatrix} = \begin{bmatrix} \cos \xi & -\sin \xi & 0 \\ \sin \xi & \cos \xi & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \cos \chi & 0 & \sin \chi \\ 0 & 1 & 0 \\ -\sin \chi & 0 & \cos \chi \end{bmatrix} \times \begin{bmatrix} \cos \xi & \sin \xi & 0 \\ -\sin \xi & \cos \xi & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} p_x \\ p_y \\ p_z \end{bmatrix}, \quad (\text{B3})$$

where the vector $[p_x, p_y, p_z]$ represents the initial projection of the polarization along the axes shown in Fig. 24 and $[p'_x, p'_y, p'_z]$ represents the resulting polarization. The first and third square matrices handle the transformation of the coordinate system, while the main rotation is described by the middle matrix.

In the simulation used to calibrate the response of the system to an axion, the revolution frequency of the deuteron is ramped. The ramp is centered at the nominal beam frequency of $f_{\text{rev}} = 750\,602.6$ Hz, with a 100 Hz scanning range. The ramp rate for f_{rev} in the calculation is 1 Hz/s. As the ramp is followed, the small changes to the relativistic factor γ and the elapsed time of a single turn $1/f_{\text{rev}}$ are followed as discussed in the main text.

In Eq. (7), the oscillating part of the EDM is described by

$$d_{\text{osc}}(t) = d_{\text{ac}} \cos[\omega_a(t - t_0) + \phi_a(t_0)]. \quad (\text{B4})$$

This can be expressed in terms of the EDM rotation angle $\psi_{\text{osc}}(t)$ as

$$\psi_{\text{osc}}(t) = \psi_{\text{ac}} \cos[\omega_a(t - t_0) + \phi_a(t_0)]. \quad (\text{B5})$$

In this equation, t_0 is assumed to be the time at the start of the scan. Thus, time accumulates with an ever-decreasing time step for each turn as the scan slowly ramps up the revolution frequency. This causes the EDM oscillation, initially out of step with the polarization rotation, to fall in step and then out of step as the scan proceeds. Depending on the exact conditions at the beginning, the individual accumulation of the vertical polarization y' as the resonance is crossed may be any value between its positive and negative limits. Thus, the size of the calculated jump varies similarly. In order to know the maximum jump possible, the calculation must be run with two orthogonal phases such as $\phi_a = 0$ and $\pi/2$. Then, the sizes of the jumps are added in quadrature to obtain the final value of the jump size.

The numerical simulation used in the calibration of the sensitivity begins with a particular size of the oscillating EDM and scanning rate to calculate the expected polarization jump. For jumps that are much less than one (assuming complete polarization), the relationship between the EDM size and the jump is nearly linear. This allows us to use just the slope given by the calibration. One example of such a calculation begins with an EDM rotation of $\psi_{\text{ac}} = 8 \times 10^{-9}$ rad/turn and a scanning rate of 1 Hz/s. After calculating the jump for two orthogonal choices of the axion phase, the results are combined and give a jump of $\Delta p_y = 0.0066$, which is normalized to a beam polarization of one. Tests with the calibration program demonstrate that the jump scales with the reciprocal of the square root of the ramping rate in the linear region. The ratio of EDM rotation to total polarization jump must be scaled by $w = \sqrt{\text{ramp}(\text{actual})/\text{ramp}(\text{calib})} = 0.775$ for the faster scans and 0.700 for the slower scans.

The value of $\text{ramp}(\text{calib})$ is 1.00, and the values of $\text{ramp}(\text{actual})$ are found in column 3 in Table III where the rates are 0.600 Hz/s for the fast scans and 0.490 Hz/s for the slow scans. The ratio or slope between ψ_{ac} and Δp_y then becomes 9.35×10^{-7} rad/turn for the fast scans and 8.48×10^{-7} rad/turn for the slow scans.

Using the first (radially pointing) term in Eq. (36), we can describe the amplitude of the contribution to the determination of the oscillating EDM in terms of $\psi_{\text{ac}} = 2\pi\Omega_a/|\vec{\Omega}_{\text{rev}}|$, where Ω_a is the amplitude of the oscillating angular velocity $\vec{\Omega}_a(t)$, by

$$d_{\text{ac}} = \frac{1}{2\pi} \frac{S\hbar q}{\beta\gamma m_d c} \frac{w}{0.958} \psi_{\text{ac}}, \quad (\text{B6})$$

where the spin S is equal to one. The factor w corrects for the ramp rate, and 0.958 corrects for the alternating straight and curved sections in the COSY ring (see the end of Sec. II A). For ease of connecting with the parameters of the COSY ring, the charge q and the denominator of the second fraction may be swapped for the beam momentum expressed as $(B\rho)$. Then, in the usual EDM units of

$e \cdot \text{cm}$ and expressed in terms of the above quoted slope between ψ_{ac} and the jump Δp_y , we have

$$|d_{ac}| = \frac{1}{2\pi} \frac{\hbar}{B\rho} \frac{w}{0.958} \left| \frac{\psi_{ac}}{\Delta p_y} \right|_{\text{calib}} A, \quad (\text{B7})$$

where A is the true value of the upper limit on the magnitude of the jump. The second fraction in this expression has the value of $\hbar/B\rho = 3.26 \times 10^{-35} \text{ J} \cdot \text{s} \cdot (\text{T} \cdot \text{m})^{-1} = 2.03 \times 10^{-14} e \cdot \text{cm}$, while the rest of the expression is dimensionless. In this way, Eq. (35) is derived—including the values 316 and 286, respectively, of the coefficient λ . For typical values of the true A , values for d_{ac} usually lie below $10^{-22} e \cdot \text{cm}$.

The oscillating EDM has a period that is comparable in size to the revolution frequency. We make the approximation that the size of the EDM could be represented at any moment by its average value during a time interval that is chosen to be a fraction of a turn as the beam circulates in the storage ring. The three-matrix formula shown above in Eq. (B3) is repeated N times during each turn. For the calculations reported here, we choose $N = 15$ for which the calculations converge to a precision of 0.1%.

The calculations are repeated for spin rotation with respect to the longitudinal axis of the beam arising from the axion-wind effect, and the calibration matches the rotation along radial axis as explained in this appendix.

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