

Multiband description of the upper critical field of bulk FeSeM. Bristow,¹ A. Gower^{1,*}, J. C. A. Prentice,² M. D. Watson,^{1,†} Z. Zajicek^{1,‡}, S. J. Blundell,¹
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The upper critical field of multiband superconductors can be an essential quantity to unravel the nature of superconducting pairing and its interplay with the electronic structure. Here we experimentally map out the complete upper critical field phase diagram of FeSe for different magnetic field orientations at temperatures down to 0.3 K using both resistivity and torque measurements. The temperature dependence of the upper critical field reflects that of a multiband superconductor and requires a two-band description in the clean limit with band coupling parameters favoring interband over intraband interactions. Despite the relatively small Maki parameter in FeSe of $\alpha \sim 1.6$, the multiband description of the upper critical field is consistent with the stabilization of a Fulde-Ferrell-Larkin-Ovchinnikov state below $T/T_c \sim 0.3$. We find that the anomalous behavior of the upper critical field is linked to a departure from the single-band picture, and FeSe provides a clear example of where multiband effects and the strong anisotropy of the superconducting gap need to be taken into account.

DOI: [10.1103/PhysRevB.108.184507](https://doi.org/10.1103/PhysRevB.108.184507)**I. INTRODUCTION**

The upper critical field of iron-based superconductors has unusually large values and reveals the interplay of orbital and paramagnetic pair-breaking effects in multiband superconductors with competing pairing channels and unconventional pairing symmetry [1]. These systems can provide ideal conditions to stabilize exotic superconducting phases like the Fulde-Ferrell-Larkin-Ovchinnikov (FFLO) state [2,3], in which the order parameter varies in space. This exotic superconducting phase can be stabilized in multiband clean materials due to the likely presence of shallow bands [4] and the consequent large Pauli paramagnetic effects [2]. Furthermore, iron-based superconductors have complex electronic structures formed of electron- and holelike bands with different orbital characters and highly anisotropic superconducting gaps. These effects are likely to manifest in the behavior of the temperature dependence of the upper critical field.

FeSe is a clean iron-based superconductor that offers us a platform on which to perform a detailed study of the up-

per critical fields down to the lowest temperature because it has a relatively low superconducting transition temperature T_c of ~ 9 K. FeSe exhibits a nematic electronic state below ~ 90 K, which leads to a small and strongly anisotropic Fermi surface driven by orbital degrees of freedom and interactions that trigger an orthorhombic-tetragonal structural transition in the absence of the long-range magnetic order [5–8]. The same interactions that affect the electronic structure are likely to influence superconductivity, leading to highly anisotropic superconducting gaps and potential orbital-dependent pairing interactions [9–11]. FeSe, due to the presence of its shallow bands, has been proposed to be a possible candidate for the BCS-BEC crossover [12,13], where the superconducting gap size and the superconducting transition temperature T_c are comparable to the Fermi energy. However, no evidence of a pseudogap of preformed pairs above T_c has been detected [14]. Instead, the multiband nature of the system and large anisotropies that develop inside the nematic state are likely to govern many of the features of this exotic superconductor. Recently, it was proposed that FeSe has unusual field-induced phases from an FFLO state, in which the formation of planar nodes gives rise to a segmentation of the flux-line lattice [15,16], or a field-induced magnetic phase transition to an in-plane magnetic field [17].

In this paper we study the upper critical fields of FeSe as a function of temperature down to ~ 0.33 K in magnetic fields up to 35 T for two magnetic field orientations with respect to the conducting planes using electrical transport and magnetic torque measurements. We find that the upper critical field of FeSe shows a clear deviation from a single-band description, with a strikingly linear behavior down to the lowest temperatures with the magnetic field perpendicular to the conducting planes. Furthermore, we find that a two-band model can

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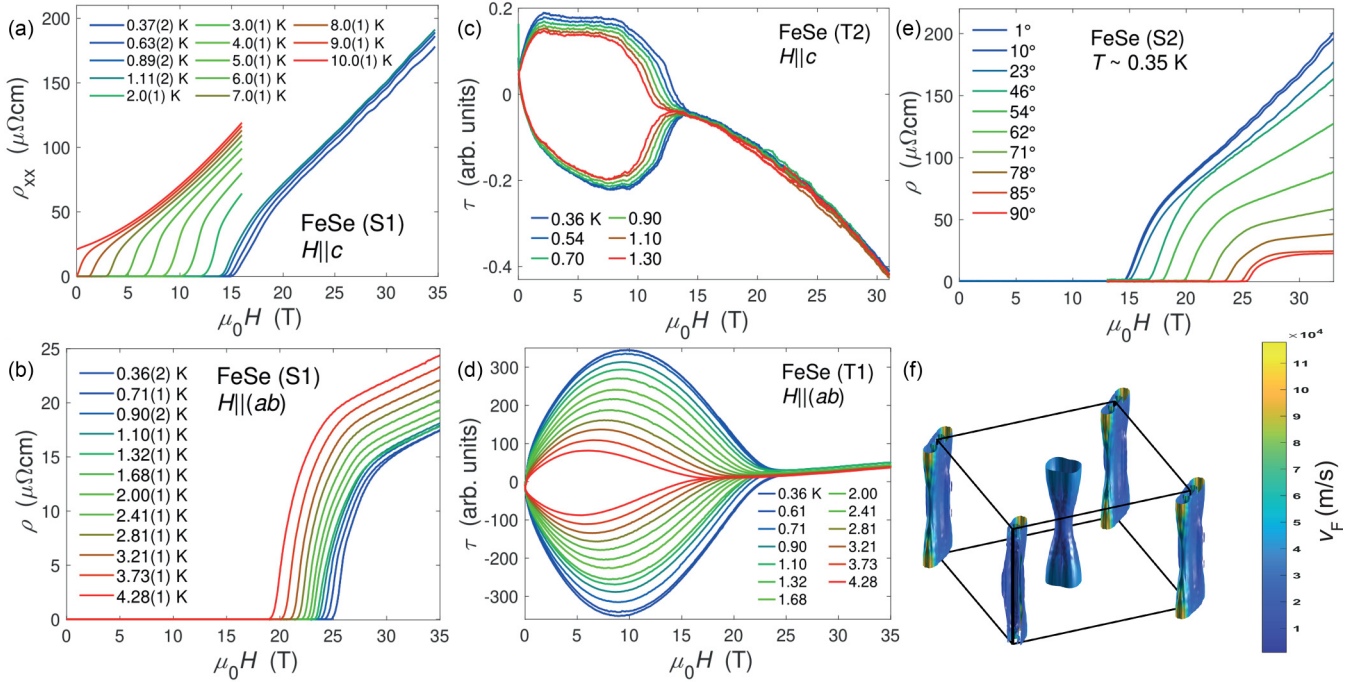


FIG. 1. (a) and (b) Resistivity versus applied magnetic field for FeSe (S1) at different constant temperatures for $H||c$ and $H||(ab)$, respectively. (c) and (d) Torque versus magnetic field at constant temperatures for $H||c$ (T2) and $H||(ab)$ (T1), respectively. The torque has arbitrary units. (e) Resistivity against applied magnetic field for FeSe (S2) at ~ 0.35 K at different angles in magnetic field. (f) Calculated Fermi surface of FeSe with experimental lattice parameters, shifted to match quantum oscillations data (as detailed in Fig. S3 in the SM) [6,20,21]. The colors in (f) reflect the variation of the Fermi velocity from 200 meV \AA for an in-plane electron pocket to 23 meV \AA for its related out-of-plane value. The corresponding anisotropy is $\Gamma = \lambda_c/\lambda_{ab} \sim 4.5$.

describe the temperature dependence of the upper critical field for both orientations. The band coupling parameters indicate the dominance of the interband pairing channels. At low temperatures, below ~ 2 K, when the magnetic field is aligned parallel to the conducting planes, the upper critical field of FeSe does not saturate but displays a characteristic upturn, consistent with the emergence of an FFLO state that can be stabilized in the presence of Pauli-paramagnetic effects.

II. EXPERIMENTAL METHODS

Single crystals of FeSe were grown using the KCl/AlCl₃ chemical vapor transport method [18] and were from the same batches reported previously in Refs. [6,19]. Electrical transport was measured using the low-frequency four- or five-point contact method. Low-resistance contacts ($< 1 \Omega$) were made using indium solder to reduce heating at low temperatures. Typically, a current of 1 mA was used for electrical transport. Quantum oscillations are observed in these samples, indicating high-quality single crystals, as described in Refs. [6,19]. Torque measurements were performed using two cantilevers, one with a sample and a dummy lever in a Wheatstone bridge configuration, and small ac currents of $\sim 70 \mu\text{A}$ at a low frequency (~ 72 Hz). Low magnetic field measurements (up to 16 T) were performed using a Quantum Design physical properties measurements system. Both field sweeps at fixed temperature and temperature sweeps in constant field were used to build the upper critical field phase diagrams. High field measurements were performed at the High Field Magnetic Laboratory, Nijmegen, up to 38 T at temperatures down to

~ 0.3 K. The upper critical fields were identified from magnetic field sweeps at constant temperature, and the angular dependence was measured using a single-axis rotator.

III. RESULTS AND DISCUSSION

Transport and torque measurements. Figures 1(a)–1(d) show resistivity (S1) and torque data (T1 and T2) for FeSe against magnetic field for different sample orientations in relation to the applied magnetic field. The superconducting transition temperature for the transport sample S1 is $T_c \sim 9.08$ K, which is defined by the offset temperature. As the magnetic field increases, the superconducting transition becomes broader and is suppressed at $\sim 14.6(1)$ T for $H||c$ at 0.36 K [Fig. 1(a)], whereas the value is above 25 T for $H||(ab)$, as the orbital effects are less effective in destroying superconductivity in this orientation. These values are in good agreement with previous reports [15,17]. Furthermore, significant broadening of the superconducting transition for $H||(ab)$ was observed in other systems, such as CaKFe₄As₄ [22] and FeSe_{0.5}Te_{0.5} [23], where it was attributed to strong anisotropic superconducting fluctuations. In our transport data, the upper critical field $\mu_0 H_{c2}$ is defined as the offset magnetic field, as shown in Fig. S1 in the Supplemental Material (SM) [24]. Additionally, we use torque magnetometry, as a thermodynamic probe, to detect the irreversible magnetic field H_{irr} for additional single crystals (T2 and T3) for different magnetic field orientations, as shown in Fig. 1(d) and Fig. S1 in the SM.

Single-band description. From the transport and torque data we have constructed a complete upper critical field phase

diagram of FeSe down to ~ 0.35 K in magnetic fields up to 35 T. This is shown in reduced units for the two orientations in Fig. 2(a). In order to assess the role of orbital and Pauli paramagnetic effects on the upper critical field of FeSe we first describe the temperature dependence using the three-dimensional (3D) Werthamer-Helfand-Hohenberg (WHH) model for a single-band weakly coupled superconductor with an ellipsoidal Fermi surface [26,27]. The slope close to T_c ($H'_{c2} = -|\mu_0 dH_{c2}/dT|_{T_c}$) can be used to estimate the zero-temperature orbital upper critical field using $\mu_0 H_{\text{orb}}(0) = 0.73 T_c H'_{c2}$ in the clean limit [26]. This gives ~ 11.1 T for $H||c$ [using a slope of $-1.7(1)$ T/K and $T_c \sim 9$ K], which is smaller than the measured value of ~ 14.6 T at 0.3 K, whereas $\mu_0 H_{\text{orb}}(0) \sim 42.7$ T for $H||(ab)$ [using a slope of $\mu_0 H'_{c2} \sim -6.5(1)$ T/K]. Furthermore, the upper critical field of FeSe for $H||c$ in Fig. 2(a) has a striking linear dependence, similar to that in other reports on FeSe [13,15]. This has also been observed in LiFeAs [28]. This is a significant deviation from single-band behavior [Fig. 2(a), blue and red lines] and suggests that a multiband model needs to be considered [29].

Besides the orbital-limiting effects, the BCS Pauli paramagnetic limit, determined by the magnetic field at which Zeeman splitting breaks the spin-singlet Cooper pair, is defined for a single gap in the weak coupling limit as $\mu_0 H_P^{\text{BCS}}(0) = 1.85 T_c$ [30] and reaches a value of 16.6 T. However, FeSe is not a single-gap superconductor, and the Pauli limit can be estimated using the value of the superconducting gap with $\mu_0 H_P^{\Delta_i}(0) = \sqrt{2} \Delta_i / g \mu_B$, where μ_B is the Bohr magneton and g is the Landé factor [26]. Measured values of the superconducting gaps Δ_i vary between 2.3 meV for the hole pocket near the Γ point and 1.5 meV for the electron pocket at the M point [11], with another potential small gap of 0.39 meV suggested from specific heat data [31] (values of 1.8 and 0.7 meV are also extracted from superfluid density [32]). Using these values, the Pauli paramagnetic field $\mu_0 H_P^{\Delta_i}(0)$ would vary between 28, 18.3, and 4.8 T (assuming $g = 2$). The Pauli limiting field can also be enhanced by either strong coupling effects (from electron-boson coupling or correlations) or significant spin-orbit scattering (where finite λ_{SO} would reduce g below 2). Thus, Pauli limiting could exceed the single-band estimate since FeSe is a multiband system with several anisotropic superconducting gaps [11] and the largest gap is expected to determine the Pauli limit [2,33].

The orbital pair breaking dominates the temperature dependence for $H||c$ only down to $0.6 T_c$, and afterwards, it deviates significantly, as shown in Fig. 2(a). Similarly, for $H||(ab)$ the deviation from the single-band WHH model is obvious below $0.25 T_c$. The parameter used to quantify the Pauli pair breaking contribution to the upper critical field, when the magnetic field is aligned along the conducting (ab) plane, is the Maki parameter, $\alpha = \sqrt{2} H_{\text{orb}}(0) / H_P(0)$. This varies strongly depending on the Pauli paramagnetic limiting field considered, with values ranging from $\alpha \sim 3.6$, in the BCS limit, to ~ 2.15 – 3.3 using $H_P^{\Delta_{1,2}}(0)$. Using the measured lowest-temperature value of $\mu_0 H_{c2}(0) \sim 26$ T, the standard form $\mu_0 H_{c2}(0) = \mu_0 H^{\text{orb}}(0) / \sqrt{1 + \alpha^2}$ would give $\alpha \sim 1.3$.

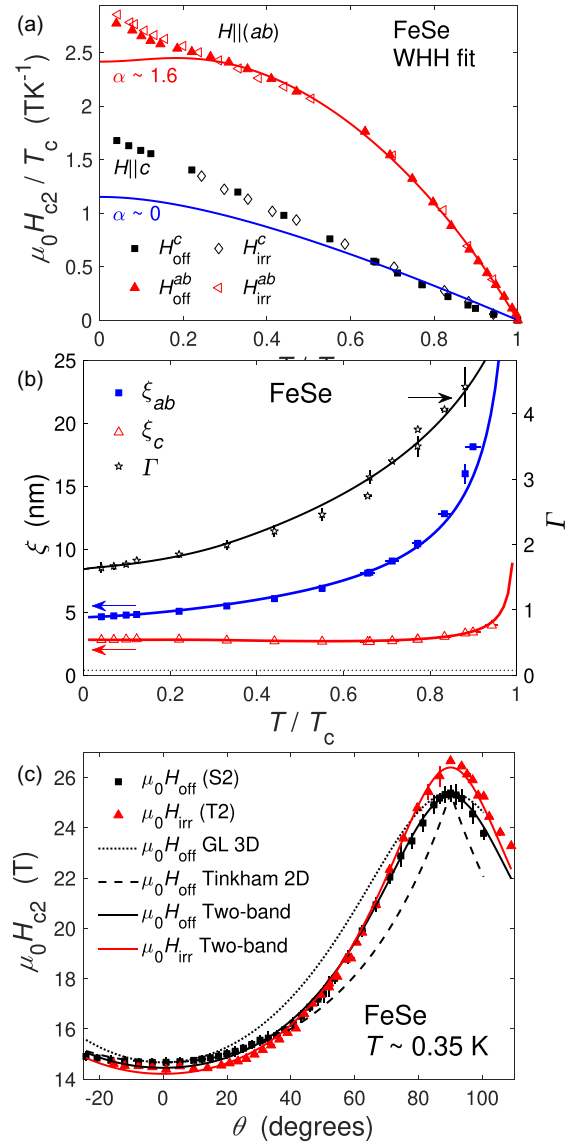


FIG. 2. (a) Upper critical fields of FeSe for $H||c$ and $H||(ab)$ obtained from transport (solid symbols) and torque measurements (open symbols) scaled against reduced temperature T/T_c , where the superconducting transition temperature T_c is 9.08 and 8.5 K, respectively. The blue and red lines are WHH fits for $H||c$ and $H||(ab)$, respectively, using different α values. (b) The temperature dependence of coherence lengths (left axis, blue and red) and anisotropy of the upper critical field (right axis, black). The $H_{c2}(T \rightarrow 0)$ values were used to find the zero-temperature coherence lengths. The horizontal dashed line represents the 3D-2D crossover length of $\sim c/\sqrt{2}$, where c is the c -axis lattice constant. Solid lines are a guide to the eye using the two-band model (described later). (c) Angular dependence of the superconducting upper critical field, $\mu_0 H_{c2}(\theta)$ at 0.35 K for different single crystals of FeSe (raw data are shown in Fig. S2 in the SM). The dotted black line is a fit to the 3D Ginzburg-Landau (GL) model, and the dashed black line represents a fit to the 2D Tinkham model [25], both for upper critical fields from resistivity data. The solid black and red lines are two-band fits to upper critical fields from resistivity and torque, respectively.

A more reliable method of extracting the α value is to fit $H_{c2}(T)$ to the WHH model, which gives $\alpha = 1.6$ for $H||c$ (solid blue line) and $H||(ab)$ (red line). In estimating the value of α the spin-orbit constant λ_{SO} was close to zero, different from those found for thin flakes of FeSe, where $\lambda_{SO} \sim 0.2$ and $\alpha \sim 2.4$ [34]. Interestingly, a relatively low value of α would also imply an important role is played by the largest gap on the hole band dominating the Pauli paramagnetic effects. For a clean isotropic single-band system, the Maki parameter is given by $\alpha = \pi^2 \Delta / (4E_F)$, and thus, one can estimate the Fermi energy to be ~ 3.5 meV, which would suggest the presence of a shallow band of a size similar to the smallest pocket observed in quantum oscillations [6,20]. The α value for FeSe is similar to that of other systems, such as LiFeAs [28], but much smaller than that of FeTe_{0.6}Se_{0.4} single crystals, for which $\alpha \sim 5.5$ [35], and CaKFe₄As₄, with $\alpha \sim 4.2$ [22], where the upper critical field is strongly dominated by Pauli paramagnetic effects. Strong paramagnetic effects seem to be an important signature of optimally doped iron-based superconductors [22,36–39]. It is worth emphasizing that in the related isoelectronic compounds Fe_{1+y}Se_xTe_{1-x} ($x = 0.4$), where the BEC-BCS crossover has been invoked to be present due to a hole band very close to the Fermi level [40], upper critical field studies have found much larger values of α than those extracted here for FeSe.

Figure 2(b) shows that the anisotropy of the upper critical field of FeSe, defined as the ratio of the upper critical field for different orientations, $\Gamma = H_{c2}^{ab}/H_{c2}^c$, drops dramatically with decreasing temperature from ~ 4 to ~ 1.7 , in good agreement with heat capacity data [41] and similar to other iron-based superconductors like LiFeAs [28]. The Fermi surface of FeSe has significant warping on the outer electron and hole bands that can potentially allow circulating currents out of plane [see Fig. 1(f)]. Furthermore, the calculated anisotropy of the penetration depth based on plasma frequencies (as in Ref. [42]) is $\Gamma = \lambda_c/\lambda_{ab} \sim 4.5$ (see Fig. S3 in the SM for the shifted Fermi surface). This is similar to the measured anisotropy of ~ 4 close to T_c [Fig. 2(b)], suggesting that the Fermi surface details play an important role in understanding its superconducting properties. The upper critical fields for the two orientations do not cross at low temperatures like in optimally doped iron-based superconductors, for which Pauli paramagnetic effects are significant, such as FeSe_{0.5}Te_{0.5} [23,43] and CaKFe₄As₄ [22].

Using the experimental values of the upper critical fields for different orientations in magnetic field, we can extract the coherence lengths for FeSe in different temperature regimes, as shown in Fig. 2(b). The coherence lengths at low temperature reach values of $\xi_{ab} = 4.57(4)$ nm and $\xi_c = 2.78(6)$ nm for FeSe and are well above the $c/\sqrt{2} \sim 0.388$ nm limit, where a 3D-2D crossover can occur, as was observed in the thinnest flakes of FeSe [34]. The mean free path due to elastic scattering from impurities of FeSe was found to vary between $\ell \sim 712$ Å [44] and 850 nm [15] using the ℓ -isotropic approximation. This approach assumes that at the lowest temperatures, where the transport properties are dominated by large-angle scattering from impurities (rather than the quantum scattering time [45]), the in-plane mean free path is limited only by the separation between the scattering

impurities, and it is not sensitive to the Fermi velocity across the Fermi surface or on different sheets in the case of a multi-band metal [46]. Thus, the mean free path depends only on the averaged Fermi surface formed of two-dimensional (2D) cylinders with compensated hole and two-electron pockets, approximated by $k_F \sim 0.1$ Å⁻¹. These values are much larger than the coherence length, $\xi(0) \ll \ell$, and as a result, FeSe is in the clean limit. Furthermore, the carrier density of this compensated metal, $n \sim 2 \times 3.6 \times 10^{20}$ cm⁻³ [47], is close to the density of paired electrons n_s estimated from muon spin rotation (using a penetration depth of $\lambda \sim 391$ nm) [32], suggesting that all carriers condense at low temperatures.

To further assess the changes in the superconducting anisotropy at the lowest experimental temperature, we performed an angle-dependent study of the upper critical field $\mu_0 H_{c2}(\theta)$ for different samples of FeSe measured by transport and torque at 0.35 K, as presented in Fig. 2(c) (raw data are shown in Fig. S1 in the SM). The angular dependence of the upper critical field can normally be described by the anisotropic single-band Ginzburg-Landau (GL) theory [48]. However, we observe a deviation from this model, along with the 2D Tinkham model, while trying to describe transport and torque data of FeSe [Fig. 2(c)]. Instead, the observed behavior is described by accounting for the contribution of a second band to the angular dependence that can be strongly temperature dependent and vary with the strength of the square of Fermi velocities, as detailed in Ref. [29].

Two-band description. In order to describe the complete temperature dependence of $H_{c2}(T)$ for FeSe in the two magnetic field orientations, a two-band isotropic model in the clean limit is considered, as detailed in Ref. [2] and previously applied to CaKFe₄As₄ in Ref. [22]. This model accounts for the presence of two different bands, with intraband ($\lambda_{11}, \lambda_{22}$) and interband ($\lambda_{12}, \lambda_{21}$) scattering and includes paramagnetic effects. It allows for the presence of an FFLO inhomogeneous state at high-fields and low temperatures [2]. In many iron-based superconductors, the pairing is expected to be mediated by spin fluctuations, leading to a sign-changing s^\pm order parameter described by dominant interband coupling parameters with $\lambda_{11}\lambda_{22} \ll \lambda_{12}\lambda_{21}$ (here the coupling constants are reported to be positive, but the signs of the products are unaffected even if the signs are negative and correspond to the expected repulsive interactions) [1,36,37]. Extensive simulations have established that the shape of the upper critical field is strongly sensitive to the values of $\eta = v_2^2/v_1^2$, which can change for different field orientations due to the variation of velocities on the Fermi surface, as shown in Ref. [22] and Fig. S4 in the SM. We find that the temperature dependences of $H_{c2}(T)$ for FeSe in both orientations is best described by parameters that consider interband pairing and an intraband scattering on a single band, using $\lambda_{11} = 0.81$, $\lambda_{22} = 0$, and $\lambda_{12} = \lambda_{21} = 0.5$, as shown in Fig. 3 and Fig. S6 in the SM. For $H||c$ we use $\alpha = 0$ and $\eta \sim 0.01$, while for $H||(ab)$, $\alpha_1 = 1.6$, $\alpha_2 = 0$ (Pauli paramagnetic effects only on the dominant band), and $\eta \sim 0.02$. These η values reflect strong anisotropy of the Fermi velocity between the two bands. Interestingly, the value of the Fermi velocity (expressed in units of \hbar^{-1}) for the dominant band for $H||c$ has $v_1 \sim 315$ meV Å, which is remarkably similar to the value of ~ 360 meV Å associated with the hole band β orbit in previous angle-resolved

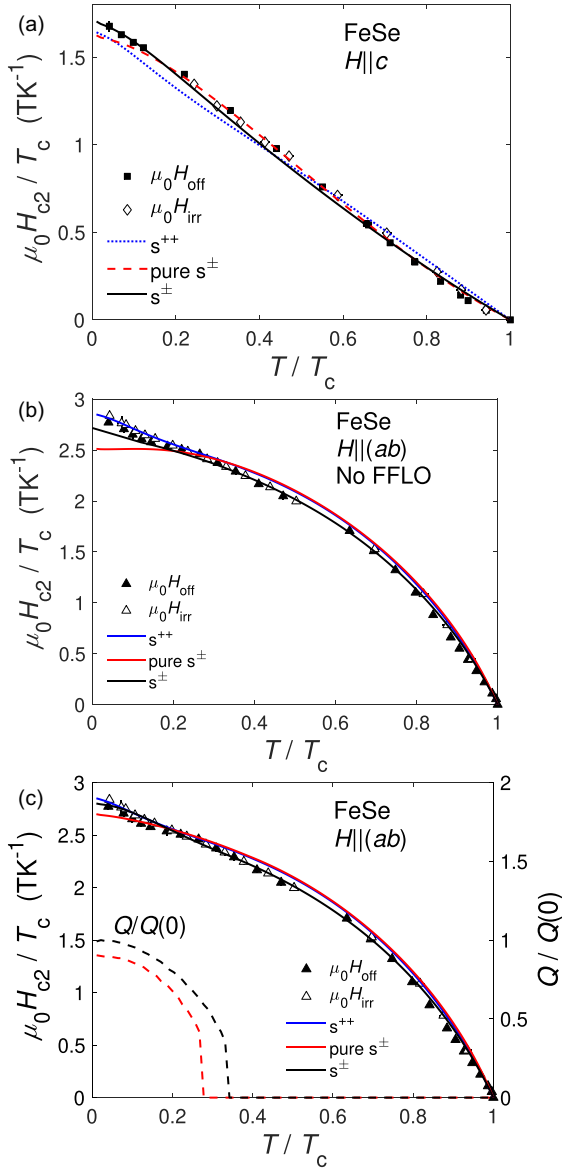


FIG. 3. Upper critical fields of FeSe for (a) $H||c$ (squares) and (b) and (c) $H||(ab)$ (triangles). In (a) the dotted blue line corresponds to s^{++} intraband pairing ($\lambda_{11} = 0.81$, $\lambda_{22} = 0.29$, and $\lambda_{12} = \lambda_{21} = 0.1$), the dashed red line corresponds to s^{\pm} pure interband pairing ($\lambda_{11} = \lambda_{22} = 0$, $\lambda_{12} = \lambda_{21} = 0.5$), and the solid black line corresponds to interband s^{\pm} pairing with a dominant band ($\lambda_{11} = 0.81$, $\lambda_{22} = 0$, and $\lambda_{12} = \lambda_{21} = 0.5$). Here the s^{\pm} interband model is best, with $\alpha = 0$ and $\eta \sim 0.01$. (b) Two-band models of the upper critical field when $H||(ab)$ for the case where no FFLO state is present. The solid blue curve represents the s^{++} case, the solid red curve represents the pure s^{\pm} case, and the solid black curve represents the s^{\pm} case with a dominant band [same band coupling parameters as in (a)]. (c) Two-band models when $H||(ab)$ with the inclusion of an FFLO modulation. The curves represent the same cases as in (b), and the dashed lines of the same color are the FFLO modulation $Q/Q(0)$ (right axis) for each case. Again, the s^{\pm} case with a dominant band offers the best description using $\alpha = 1.6$ and $\eta \sim 0.02$.

photoemission spectroscopy (ARPES) studies [49,50]. The second band has a velocity of $v_2 \sim 36 \text{ meV \AA}$, which is much lower than that expected for the outer electron band, which is

$\sim 450 \text{ meV \AA}$ [49,50]. Additionally, we can compare these values of velocities using the Pippard coherence length ξ_0 , which quantifies the size of Cooper pairs. Using coherence lengths of $\xi \sim 4.6 \text{ nm}$ and $\xi = \hbar v_F / \pi \Delta(0)$, we find that v_F varies from 332 to 216 to 56 meV \AA (assuming the presence of the three different superconducting gaps in FeSe mentioned above). Thus, based on these values, one could suggest that the two-band model used here reveals the role played by the hole band and another band with a small gap and low velocity. Alternatively, the extracted velocities could reflect the behavior of a dominant band involved in pairing, and the two values of velocities would correspond to the in-plane and out-of-plane averaged components [see Fig. 1(f)].

The in-plane model for FeSe [$H||(ab)$] uses the same coupling parameters, a slightly larger η value, and lower velocities of $v_1 \sim 140 \text{ meV \AA}$ and $v_2 \sim 20 \text{ meV \AA}$. For this field orientation we use a coherence length of $\xi \sim 2.8 \text{ nm}$ along with the same values of Δ as above, which gives predicted velocities of 132 and 34 meV \AA . Additionally due to a finite Maki parameter of $\alpha \sim 1.6$, the model allows for the stabilization of an FFLO state below $T_{\text{FFLO}} \sim 0.3T_c \sim 2.5 \text{ K}$, as shown in Fig. 3(c). The formation of the FFLO state in a system with a cylindrical Fermi surface requires a large Zeeman energy and a critical Maki parameter of $\alpha_c = 4.76$ [3], compared to $\alpha_c = 1.8$ [51] for a 3D ellipsoidal Fermi surface. An FFLO state can be realized in clean materials with weak scattering of quasiparticles. It manifests as a change in slope in the upper critical field at low temperatures [2], and it has been suggested to occur in FeSe [15]. Bands which could be involved in this effect are expected to be associated with shallow Fermi surface pockets with small Fermi energies which can be spin polarized in large magnetic fields. At low temperatures possible candidates are the inner hole pocket centered at the Z point, which is pushed down below the Fermi level inside the nematic electronic phase, and the electron pocket centered at the zone corner, which is lifted close to the Fermi level ($\sim 3 \text{ meV}$), as detected by ARPES [5].

Besides the model described above for FeSe, we consider coupling parameters that could be related to s^{++} pairing in the presence of the orbital fluctuations and spin-orbit coupling, as suggested for LiFeAs [52]. By investigating different combinations of the band coupling parameters we find that intraband pairing with $\lambda_{11} = 0.81$, $\lambda_{22} = 0.29$, and $\lambda_{12} = \lambda_{21} = 0.1$ reasonably describes the temperature dependence of the upper critical field data in FeSe for both orientations in magnetic field. However, after we assess the best fit, it appears that interband scattering promoted by spin fluctuations could dominate over intraband scattering (see Fig. 3 and Fig. S6 and Table S1 in the SM). The s^{\pm} coupling parameters also describe well the upper critical field of thin flakes of FeSe [34] (see Fig. S7 in the SM) and Cu-FeSe [44], which are more sensitive to disorder and in which the degree of anisotropy is suppressed ($\eta \sim 0.2$). As in other iron-based superconductors, the presence of several scattering channels in a multiband system, like FeSe, can increase the upper critical field far above the single-band limit, caused by the relative weight of different scattering channels. On the other hand, the shallow bands in FeSe are likely to be involved in the stabilization of the FFLO state, which is very fragile to disorder, as found for thin flakes of FeSe [34] (see Fig. S7 in the SM) and

Cu-FeSe [44]. The temperature dependence of the upper critical field of FeSe reflects either the behavior of two dominant superconducting gaps that reside on different sheets of the cylindrical Fermi surface (one on a large hole band and one on a shallow small band) or the strong gap anisotropy of the hole band, which may have nodes or deep minima on the long axis of the ellipse [11]. Furthermore, ARPES studies suggest that there is significant anisotropy of the superconducting gap in all momentum directions which needs to be taken into account [53].

The upper critical field values reported here are in good agreement with previous transport and torque studies on FeSe [15,17]. All these studies reveal a linear temperature dependence of the upper critical field for $H||c$, as shown in Fig. S5 in the SM, despite a small variation in the reported values of T_c . The precise definition of T_c for FeSe can vary slightly between thermodynamic and transport studies as a result of the growth process itself [54,55] and, potentially, any small applied strain if the crystals are glued during the experiments [56]. On the other hand, the upper critical field boundaries for $H||(ab)$ show additional features at low temperature which differ more between various studies (see Fig. S5) [13,17]. Furthermore, recent heat capacity data suggest that sizable field-induced Gaussian superconducting fluctuations could affect the precise upper boundaries of the upper critical field [41].

There has been a series of proposed field-induced magnetic transitions in FeSe. The nonsaturating behavior of H_{c2} for $H||c$ below 1.3 K was linked to unconventional pairing due to the spin splitting of the Fermi surface [13,57]. Furthermore, the thermal conductivity has a transition field $\mu_0 H^*$ that remains almost constant around 14 T, which is lower than $\mu_0 H_{\text{irr}}$ obtained from torque data [12,13]. Other studies proposed an in-plane field-induced phase transition originating from the inherent spin-density-wave instability of quasiparticles in FeSe [17]. Despite all these findings, the upper critical field of FeSe tuned by pressure or chemical pressure [58–60] displays an almost linear dependence as a function of temperature for $H||c$. This suggests that multiband effects are necessary to describe the upper critical field of iron chalcogenide superconductors. Similarly, most of the temperature dependence studies of the superfluid density and specific heat [32,61] also confirmed the relevance of multiband and anisotropic effects in FeSe.

IV. CONCLUSION

In summary, we experimentally mapped the temperature dependence of the upper critical fields of FeSe based on transport and torque measurements up to 35 T and down to 0.35 K for two orientations of magnetic field. Employing a two-band model in the clean limit, we estimated the band coupling constants, which suggest more dominant interband scattering promoted by spin fluctuations in FeSe. Additionally, for magnetic fields aligned in the conducting plane the temperature dependence of the upper critical field is consistent with the emergence of an FFLO state at low temperatures. Future theoretical studies need to take into account the exact details of the electronic structure as well as the gap anisotropy to explain the specific features of the upper critical field as well as other relevant temperature-dependent superconducting quantities of FeSe.

In accordance with the EPSRC policy framework on research data, access to the data will be made available from ORA (ORA - Oxford University Research Archive [62]).

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