


# Challenges and current status of the TLEP lattice design

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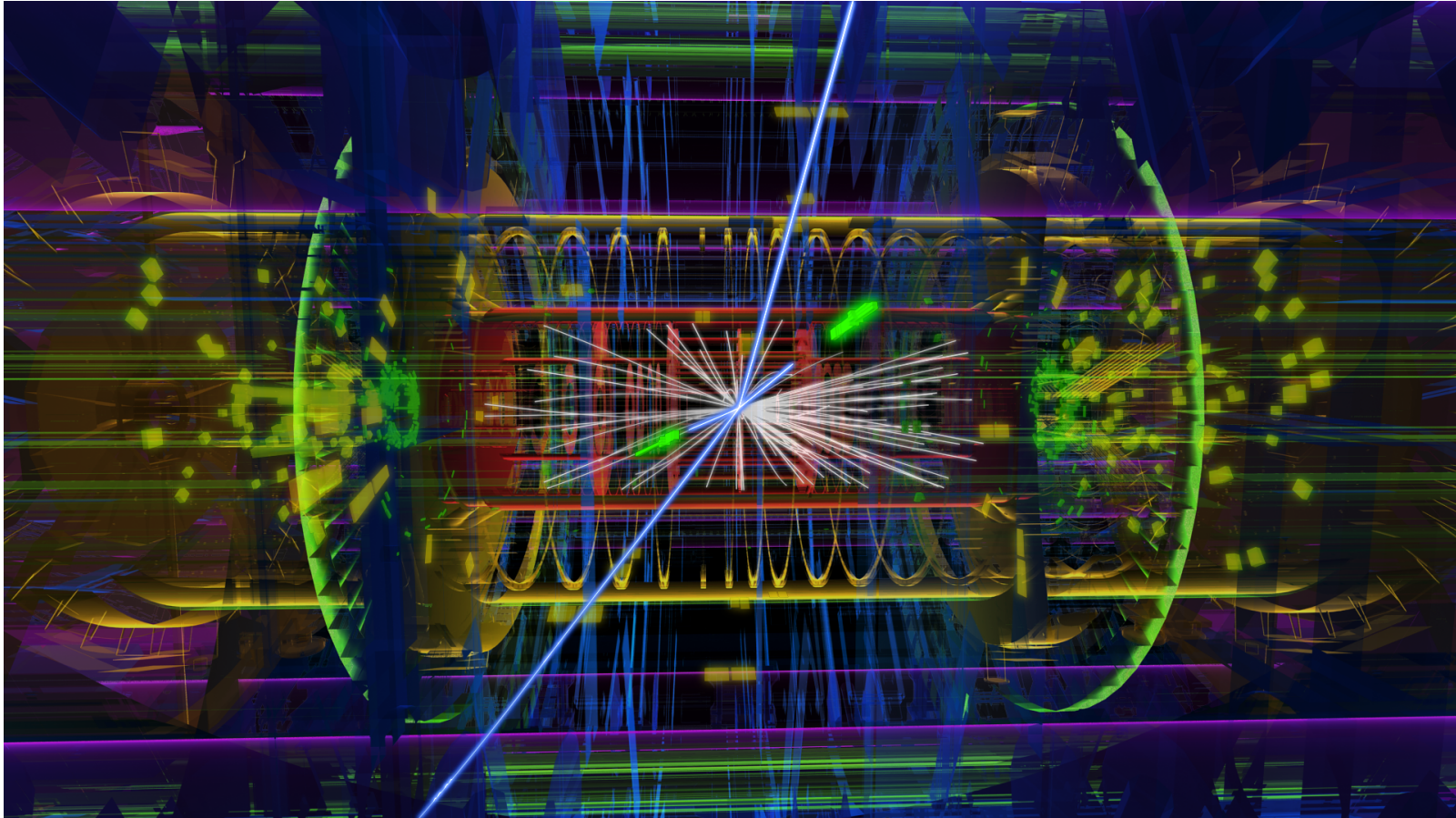
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# Outline

- Introduction
- 1) Lattice design for 175 GeV beam energy
- 2) Beam emittances
- 3) Lattice modifications for smaller energies
- 4) Interaction region lattice, mini-beta optics
- Résumé

# What do we have now?



■ ATLAS event display:  $H \rightarrow e^+ + e^- + \mu^+ + \mu^-$



# A bit of history

- In July 2011 a proposal was made to (re)install a 120 GeV / beam  $e^+e^-$  collider in the LEP-LHC tunnel – named LEP3. Work on LEP3 started in a series of workshops.
- The 80 km TLEP machine appeared in 2012 in parallel with the feasibility study for a 80 km ring for a future hadron collider around CERN. TLEP and LEP3 were presented in September 2012 at the European Strategy meeting in Krakow.
- In October 2013 TLEP was integrated into the FCC study and is now known as FCC-ee.

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# Future Circular Collider Study (FCC)



- New 80-100 km storage ring
- **FCC-hh** (=long-term goal):
  - High-energy hadron collider
  - Push the energy frontier to 100 TeV
- **FCC-ee (TLEP)**:
  - $e^+/e^-$ -collider as intermediate step
- **FCC-he**
  - Hadron-lepton collider option
  - Deep inelastic scattering




**Future Circular Collider Study  
Kick-off Meeting**

**12-15 February 2014,  
University of Geneva,  
Switzerland**

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University of Geneva  
C. Blanchard, A. Blondel,  
C. Doglioni, G. Iacobucci,  
M. Koratzinos

**CERN**  
M. Benedikt, E. Delucinge,  
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# Physics goals of TLEP

- Provide highest possible luminosity for a wide physics program ranging from the Z pole to the tt production threshold.
  - Beam energy range from 45 GeV to 175 GeV
- Main physics programs / energies (+ scan around central values):
  - Z (45.5 GeV): Z pole, high precision of  $M_Z$  and  $\Gamma_Z$ ,
  - W (80 GeV): W pair production threshold,
  - H (120 GeV): H production,
  - T (175 GeV): tt threshold.

All energies quoted refer to BEAM energies

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# Main challenge: the parameter list

|   | <b>Z</b> | <b>W</b> | <b>H</b> | <b>tt</b> |
|---|----------|----------|----------|-----------|
| <b>Beam energy [GeV]</b>                            | 45.5     | 80       | 120      | 175       |
| <b>Beam current [mA]</b>                            | 1450     | 152      | 30       | 6.6       |
| <b>Bunches / beam</b>                               | 16700    | 4490     | 1360     | 98        |
| <b>Bunch population [<math>10^{11}</math>]</b>      | 1.8      | 0.7      | 0.46     | 1.4       |
| <b>Transverse emittance <math>\epsilon</math></b>   |          |          |          |           |
| - Horizontal [nm]                                   | 29.2     | 3.3      | 0.94     | 2         |
| - Vertical [nm]                                     | 0.06     | 0.007    | 0.0019   | 0.002     |
| <b>Momentum comp. [<math>10^{-5}</math>]</b>        | 18       | 2        | 0.5      | 0.5       |
| <b>Betatron function at IP <math>\beta^*</math></b> |          |          |          |           |
| - Horizontal [mm]                                   | 500      | 500      | 500      | 1000      |
| - Vertical [mm]                                     | 1        | 1        | 1        | 1         |
| <b>Energy loss / turn [GeV]</b>                     | 0.03     | 0.33     | 1.67     | 7.55      |
| <b>Total RF voltage [GV]</b>                        | 2.5      | 4        | 5.5      | 11        |



# Main challenge: the parameter list

- Design & optimize a lattice for 4 different energies

|                                   | Z     | W     | H      | tt    |
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- Interaction region layout for a **large number of bunches**
- Horizontal emittance is **increasing** with reduced energy
- **Extremely small vert. beta\*** ( $\beta_y^* = 1 \text{ mm}$ )
  - High chromaticity
  - Challenging dynamic aperture

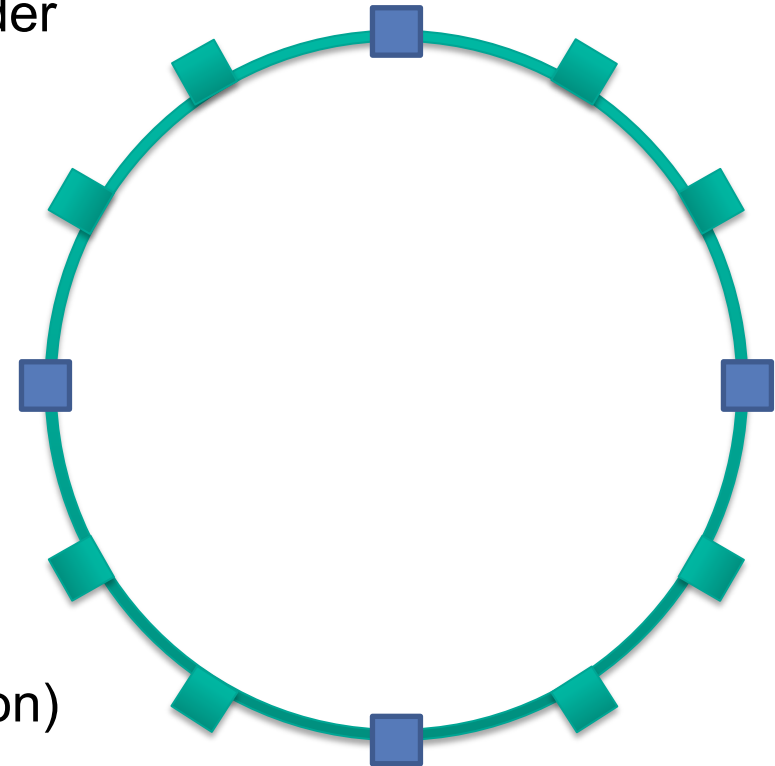
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- **High synchrotron radiation losses** include sophisticated absorber design in the lattice

# Current TLEP Layout

- Layout compatible with hadron collider
- Circumference: 80 km  
(will be increased to 100 km)
  
- 4 mini-beta insertions (blue)
- 8 long straight sections (green)  
(**1.5 km each!** for RF, injection, ...)
- 12 Arcs
  
- 12 RF sections (every straight section)
- Limit sawtooth effect
- 2 rings, side-by-side (polarization, vertical emittance)



# 1) Lattice design for 175 GeV beam energy

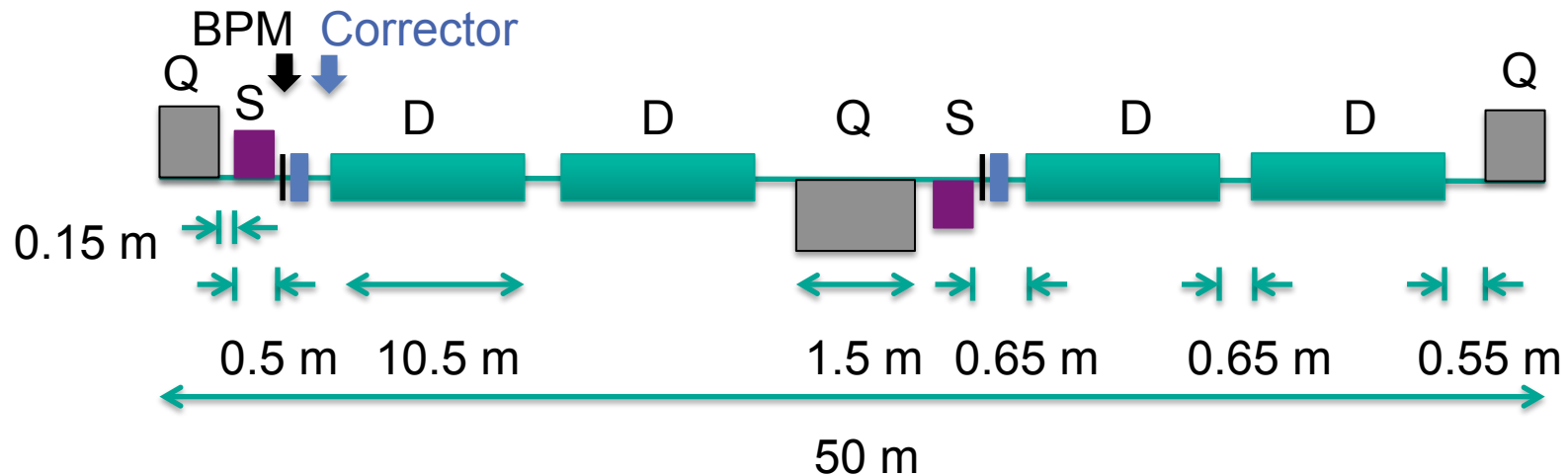
- Textbook like approach: start with FODO cells  
→ High dipole fill factor, easy to handle and optimize analytically
- Phase advance  $90^\circ / 60^\circ$  (LEP experience, to be discussed)
- Achieve horizontal emittance by selecting the cell length

$$\varepsilon = \left( \frac{\delta p}{p} \right)^2 \left( \gamma D^2 + 2\alpha D D' + \beta D'^2 \right)$$
$$\hat{D} = \frac{L_{cell}^2}{\rho} \cdot \frac{\left( 1 + \frac{1}{2} \sin\left( \frac{\psi_{cell}}{2} \right) \right)}{\sin^2\left( \frac{\psi_{cell}}{2} \right)}$$

- Use phase advance for fine tuning

# 1) TLEP FODO cell

- Cell length:  $L_{\text{cell}} = 50 \text{ m}$
- Layout already considers max. dipole length, drift spaces for absorbers, flanges etc.



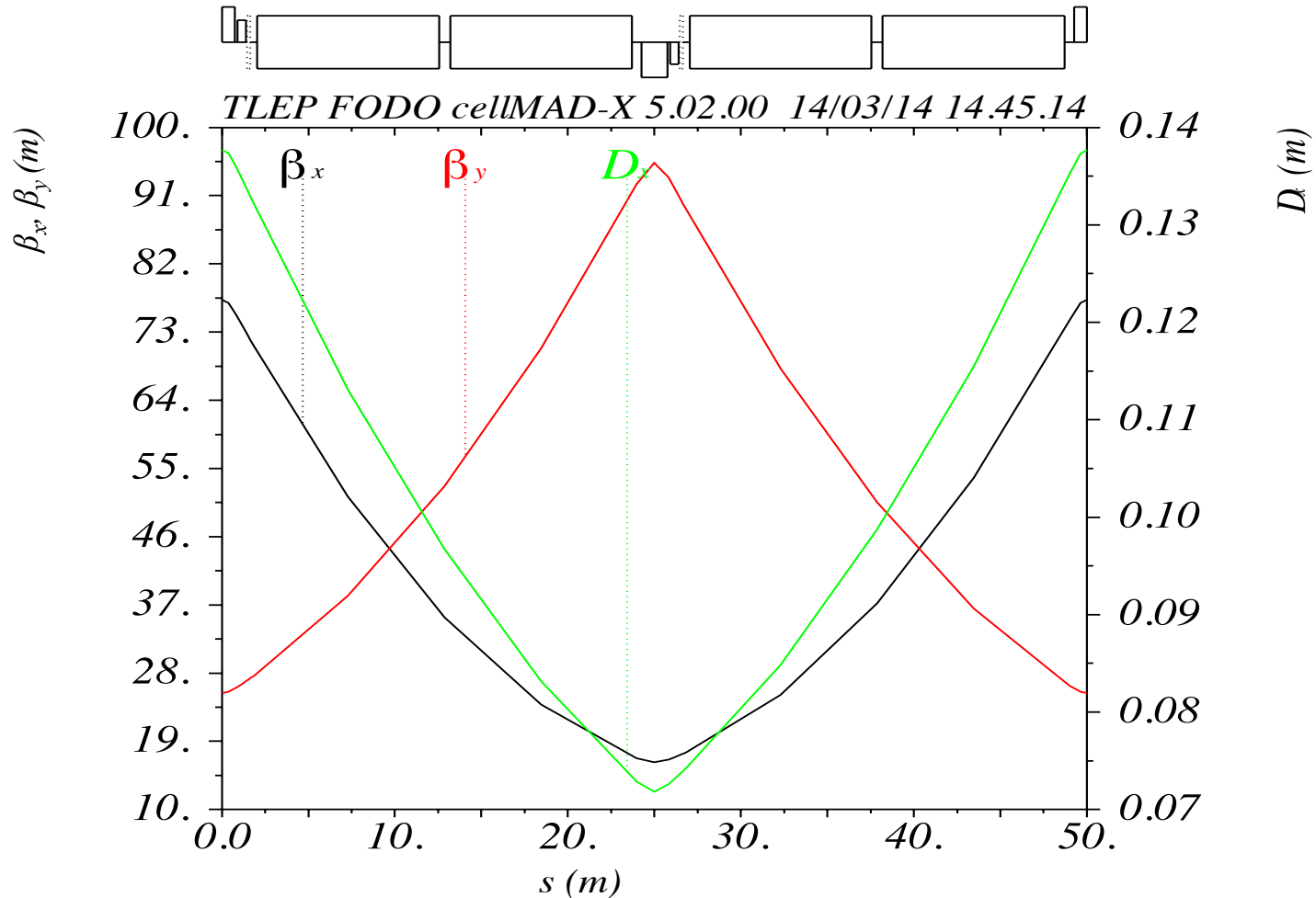
D = dipole, Q = quadrupole, S = sextupole

$N_{\text{dipoles}} = 6048$  (384 half bend) (LHC: 1232)  
 $N_{\text{quadrupoles}} = 3216$  (LHC: 478)

$\rho \approx 9.8 \text{ km}$   
 $\theta = 1.07 \text{ mrad}$   
 $B\rho = 583.3 \text{ Tm}$

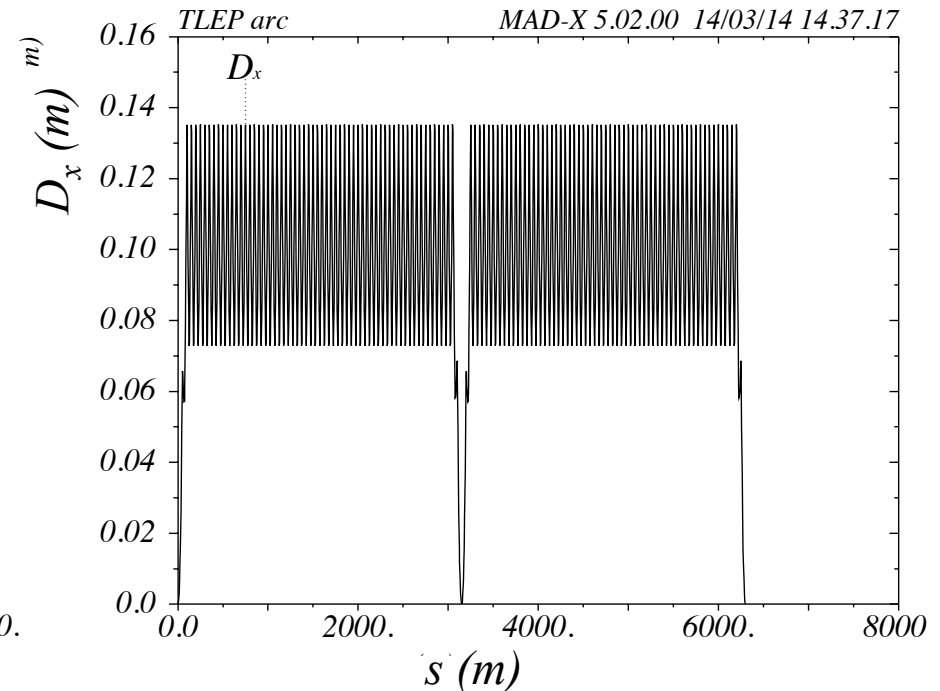
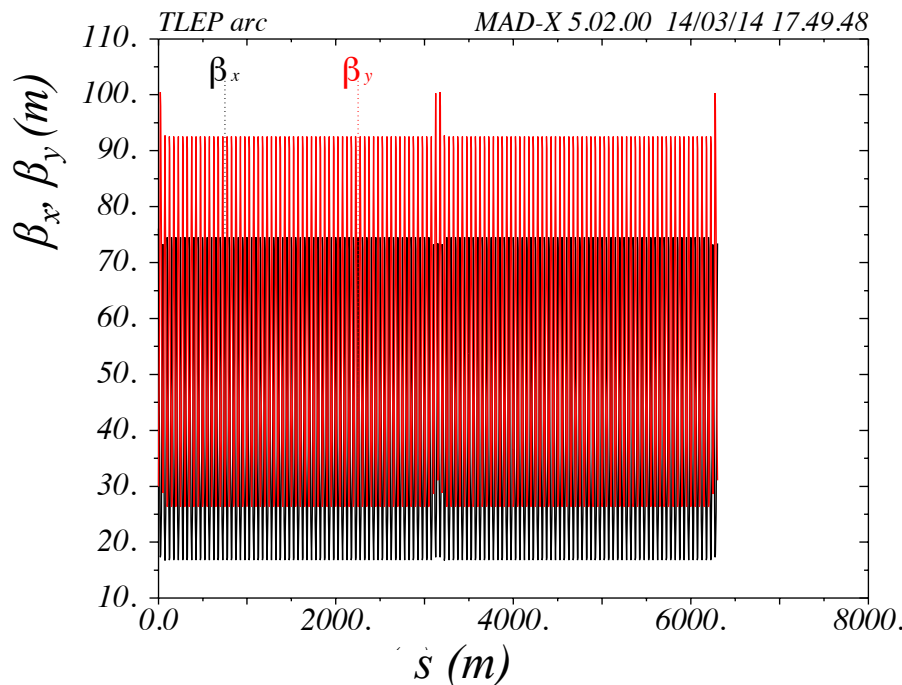


# 1) TLEP FODO cell

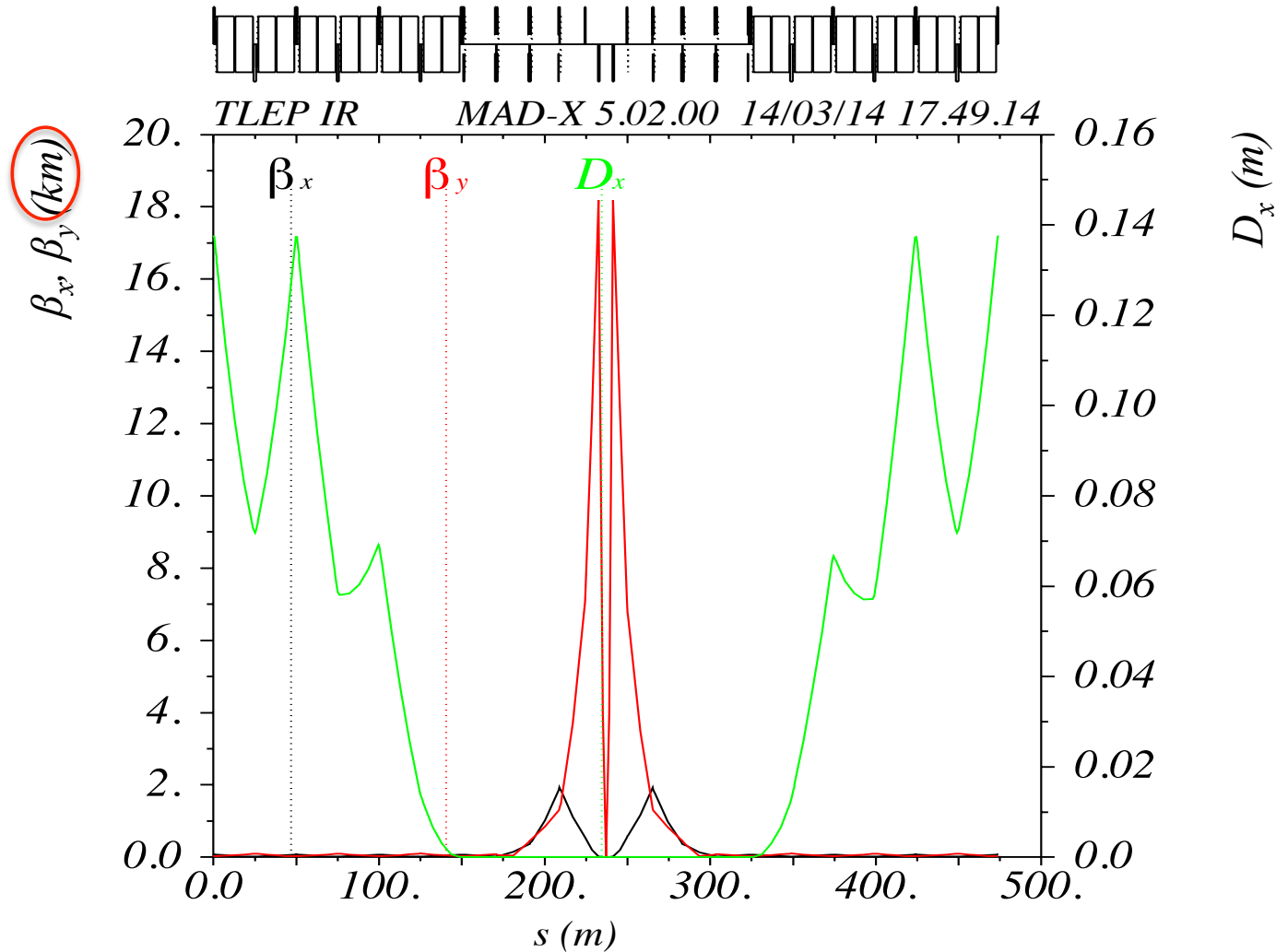


# 1) TLEP Arc

- 2\*63 FODO cells
- Each arc is embedded in dispersion free region
  - 2 half bend cells as dispersion suppressor at beginning and end
- Arc length:  $\approx 6$  km



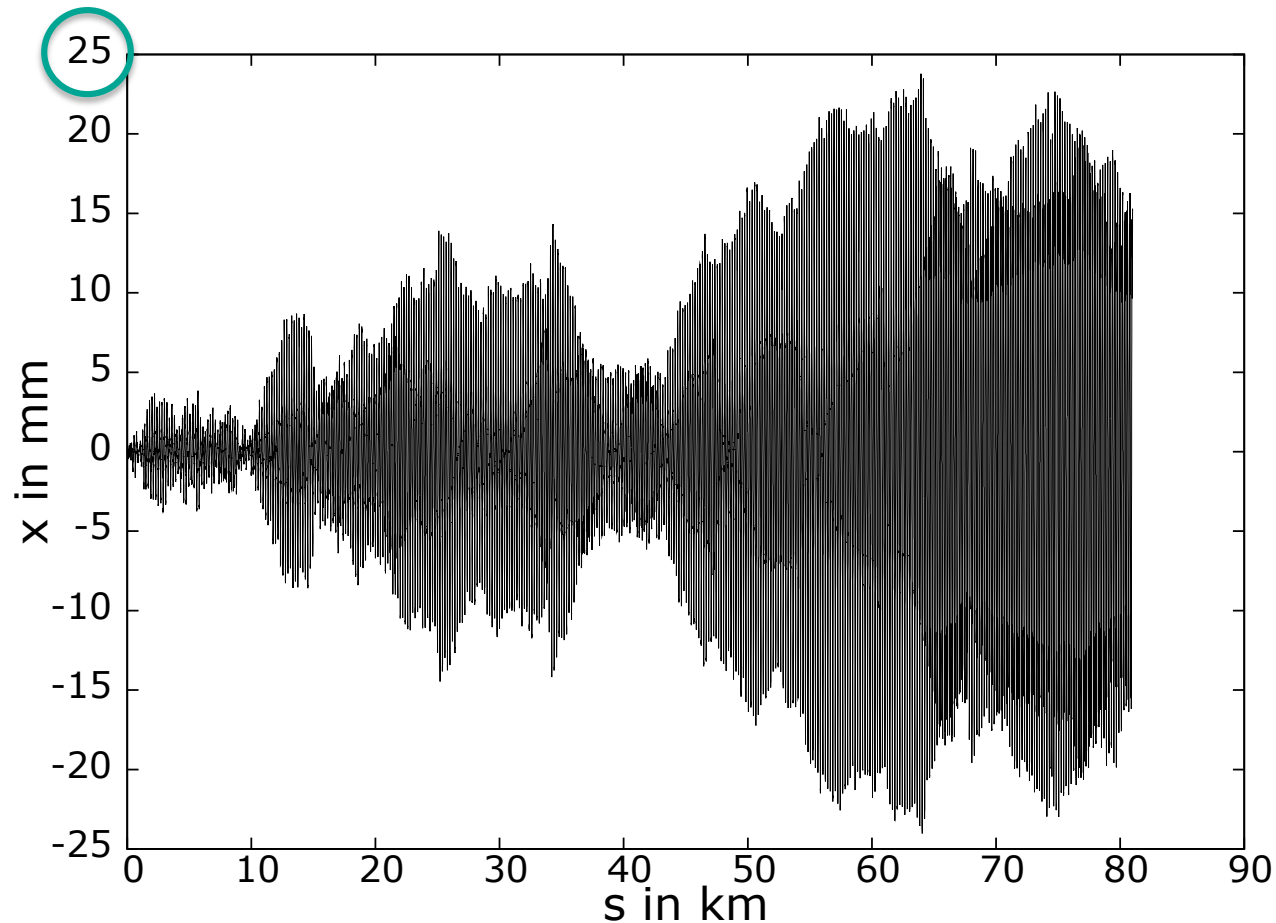
# 1) TLEP Interaction region



## 2) Beam emittances

- Required ratio:  $\varepsilon_y/\varepsilon_x = 0.001$
- Horizontal emittance is defined by energy, cell length and focusing properties. ✓
- Vertical emittance is defined by orbit tolerances (misalignments & coupling).
- Assumed magnet alignment tolerance (D. Missiaen):  
$$\Delta x = \Delta y = 150 \mu m$$
- Orbit tolerances add up to very large distortions and are amplified by the extreme minibeta concept.

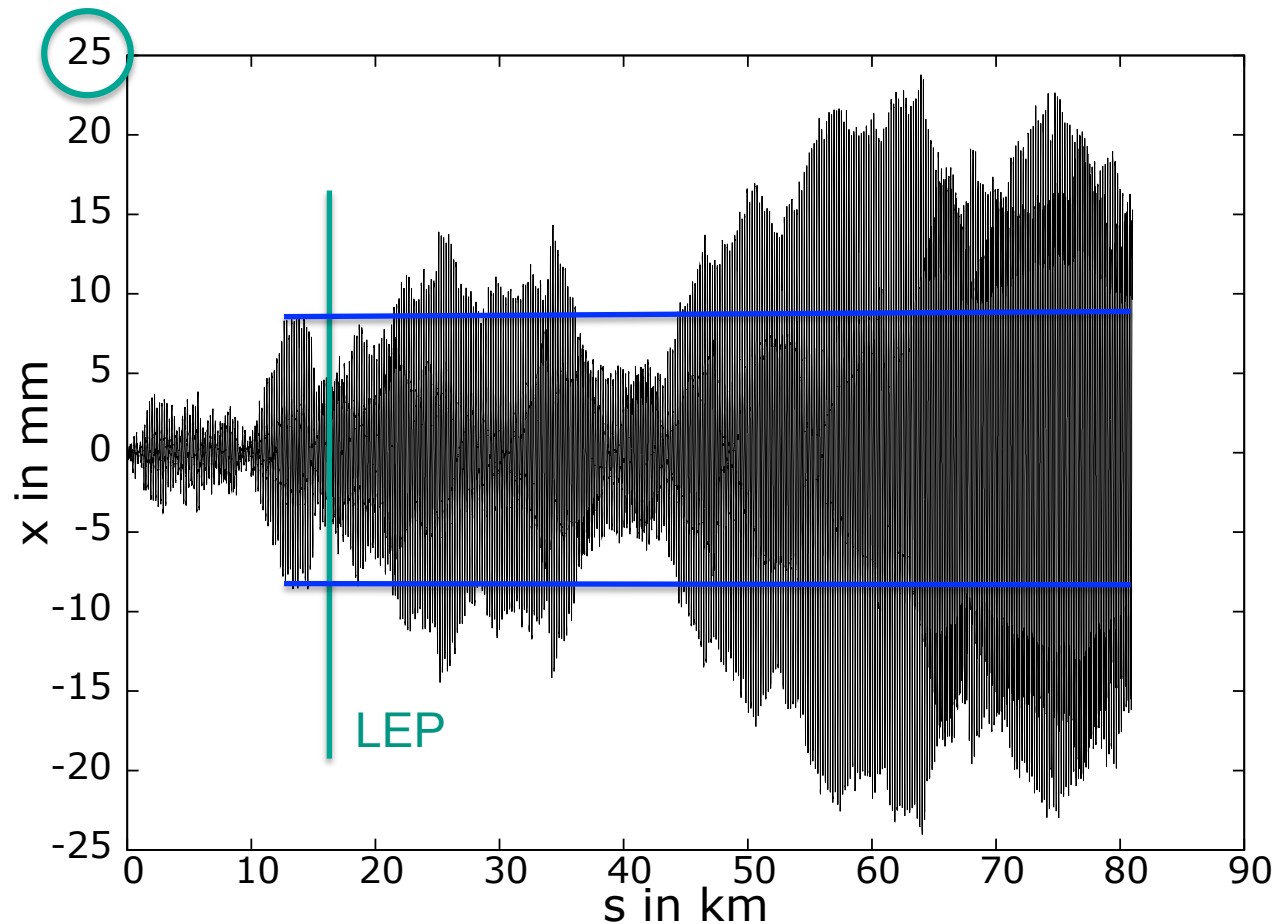
## 2) Horizontal distorted orbit



- Due to transversal misalignments of quadrupoles
- Calculated as transfer line

Without minibetas!

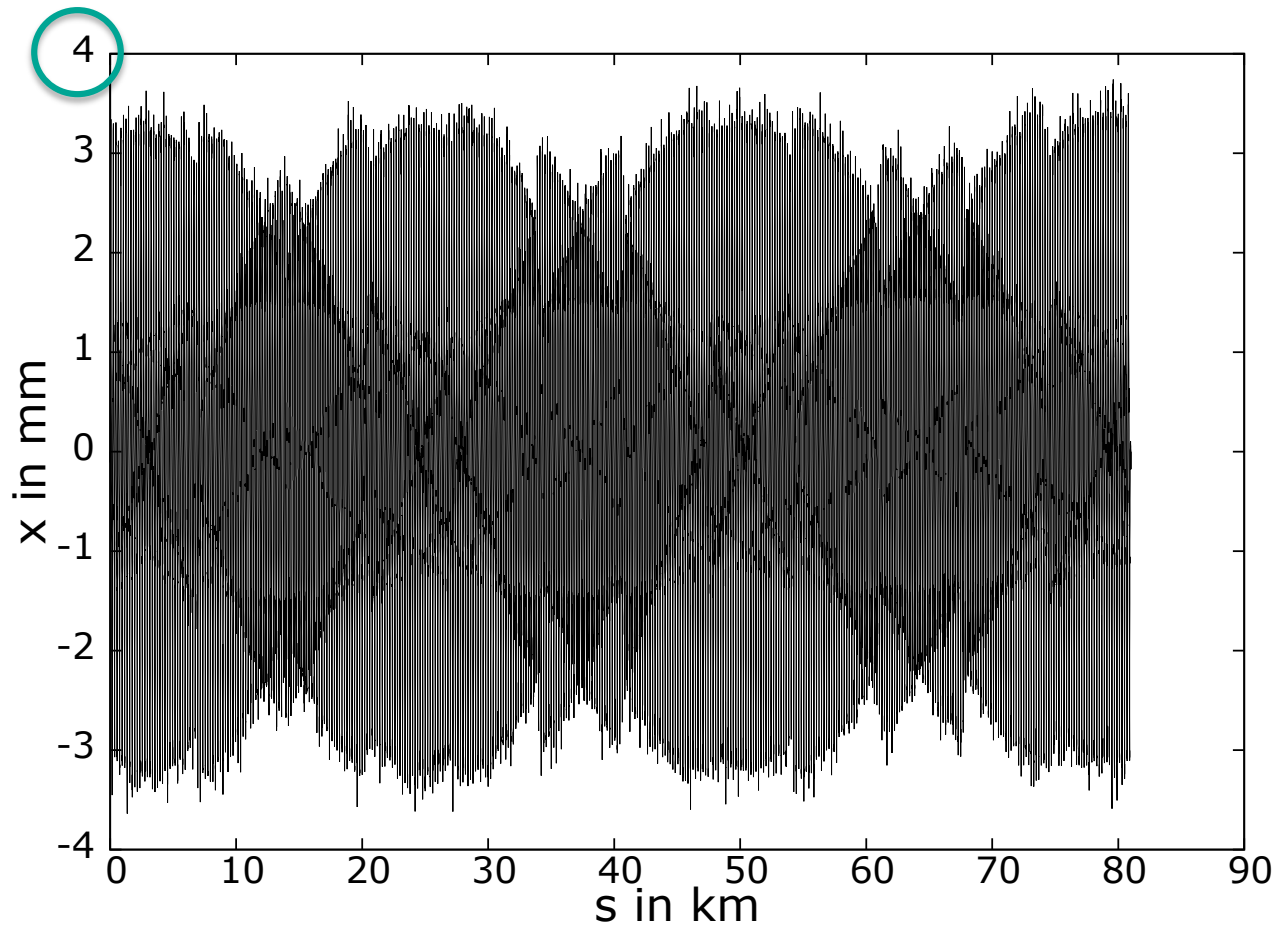
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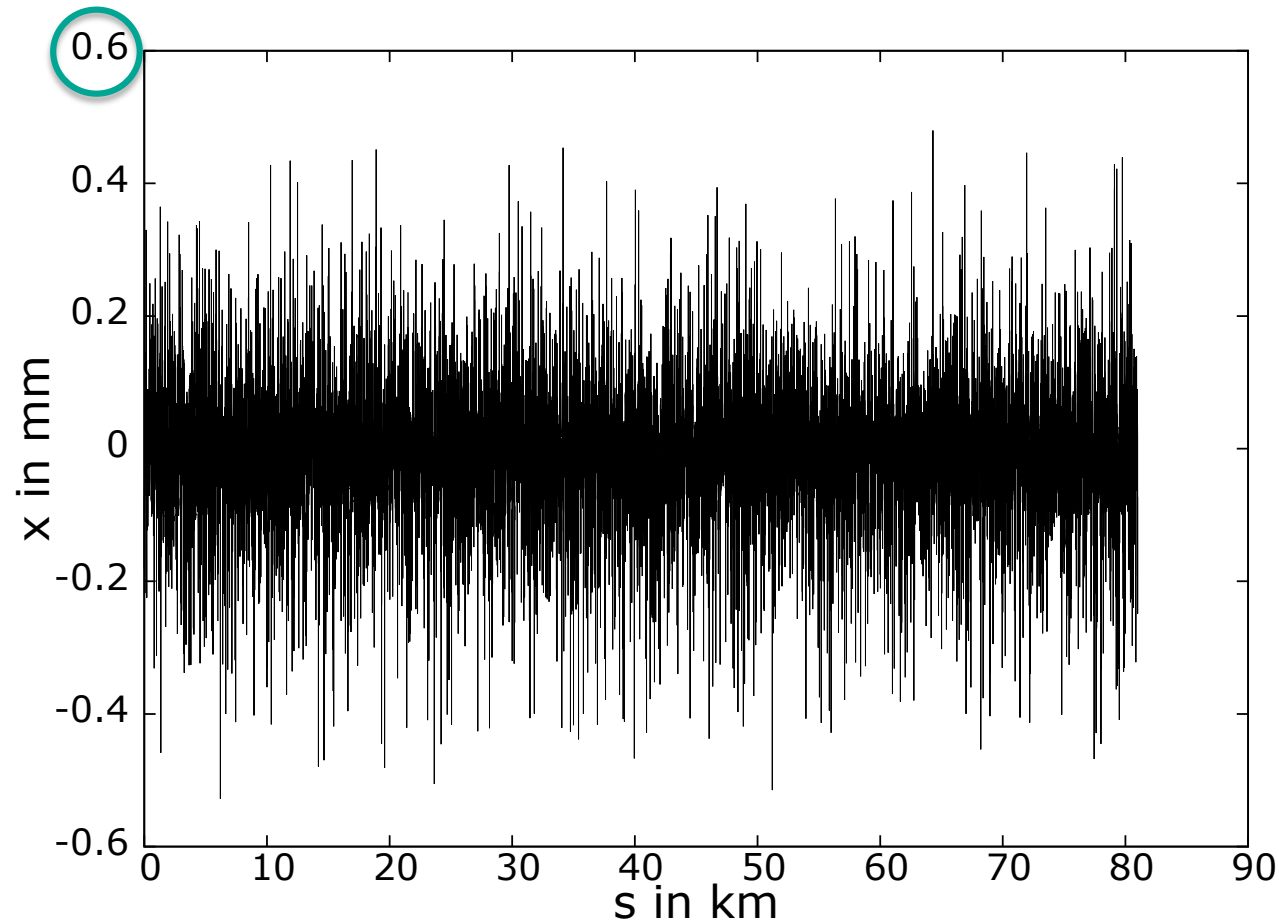
Without minibetas!

## 2) Horizontal distorted orbit



■ ... after 3 orbit correction iterations

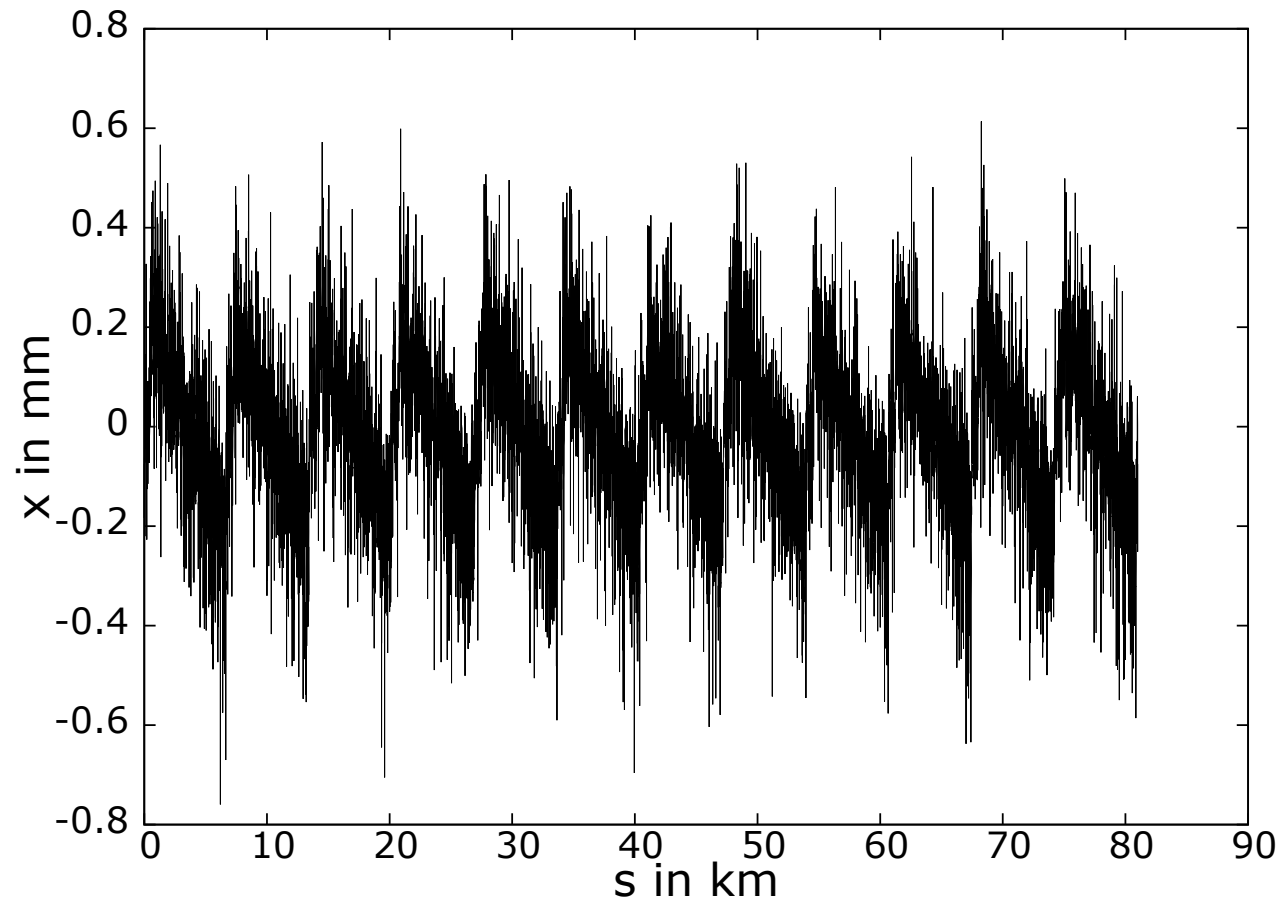
## 2) Horizontal distorted orbit



- ... after closing the ring, final correction and switching on sextupoles



## 2) Horizontal distorted orbit



$$x_D(s) = D(s) \cdot \frac{\Delta p}{p}$$

- ... including synchrotron radiation and RF structures

## 2) Beam emittances

- Equilibrium emittances calculated by MAD-X:

$$\varepsilon_x = 1.23 \text{ nm}, \quad \varepsilon_y = 1.05 \text{ pm} \quad \checkmark$$

Without minibetas!

- Can we maintain these values including coupling and beam-beam effects?
- How do we deal with the extreme sensitivity of the minibeta sections?

$$(\beta_y \approx 18 \text{ km})$$

$$x_{rms}(s) \propto \sqrt{\beta(s)} \cdot \sqrt{\beta(s_0)}$$

→ Active alignment feature with piezos?

### 3) Lattice modifications for smaller energies



|                                 | Z     | W     | H      | tt    |
|---------------------------------|-------|-------|--------|-------|
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■ At 45.5 GeV the emittance is a factor 15 higher compared to 175 GeV!

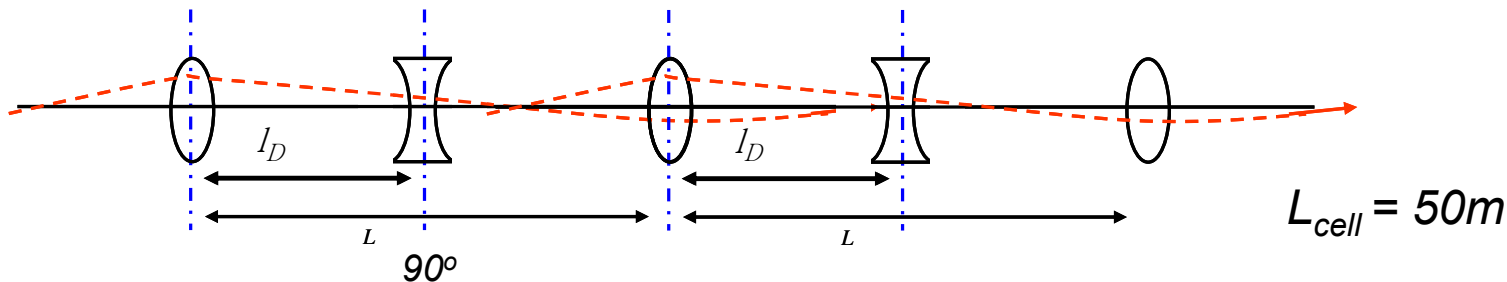
■ BUT:  $\epsilon_0 \propto \gamma^2$

→ How can we counteract the natural emittance shrinking for lower energies?

### 3) Lattice modifications for smaller energies



- Increase the FODO cell length to adjust the emittance!

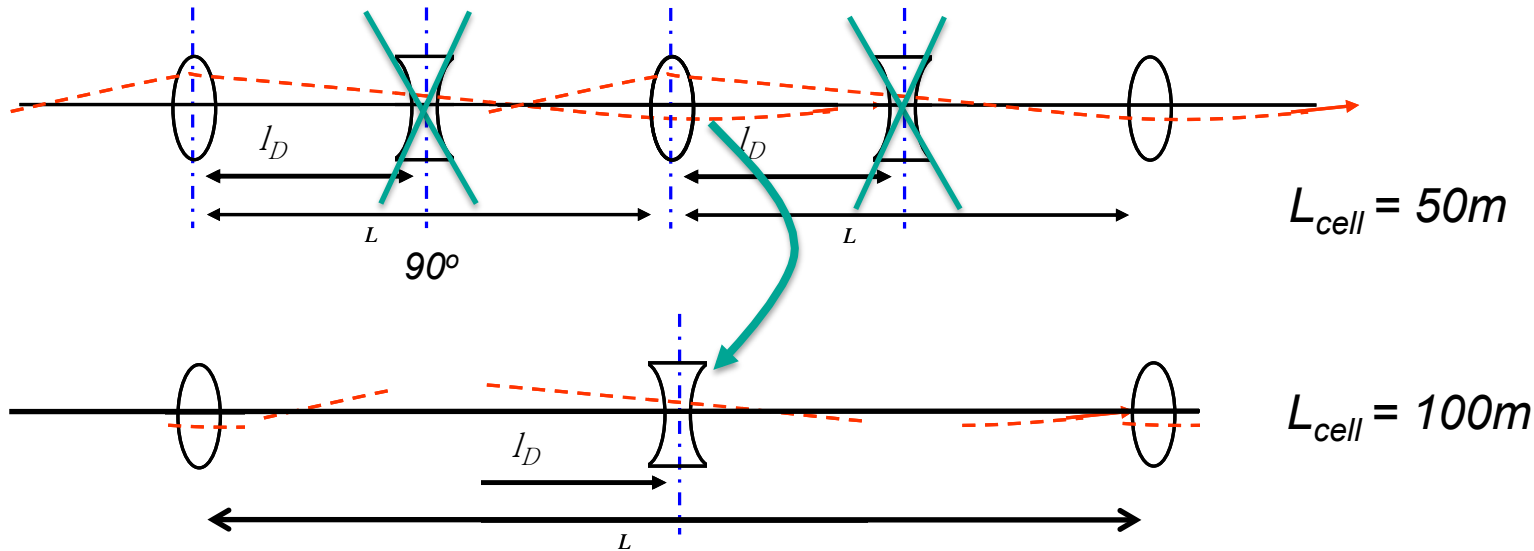


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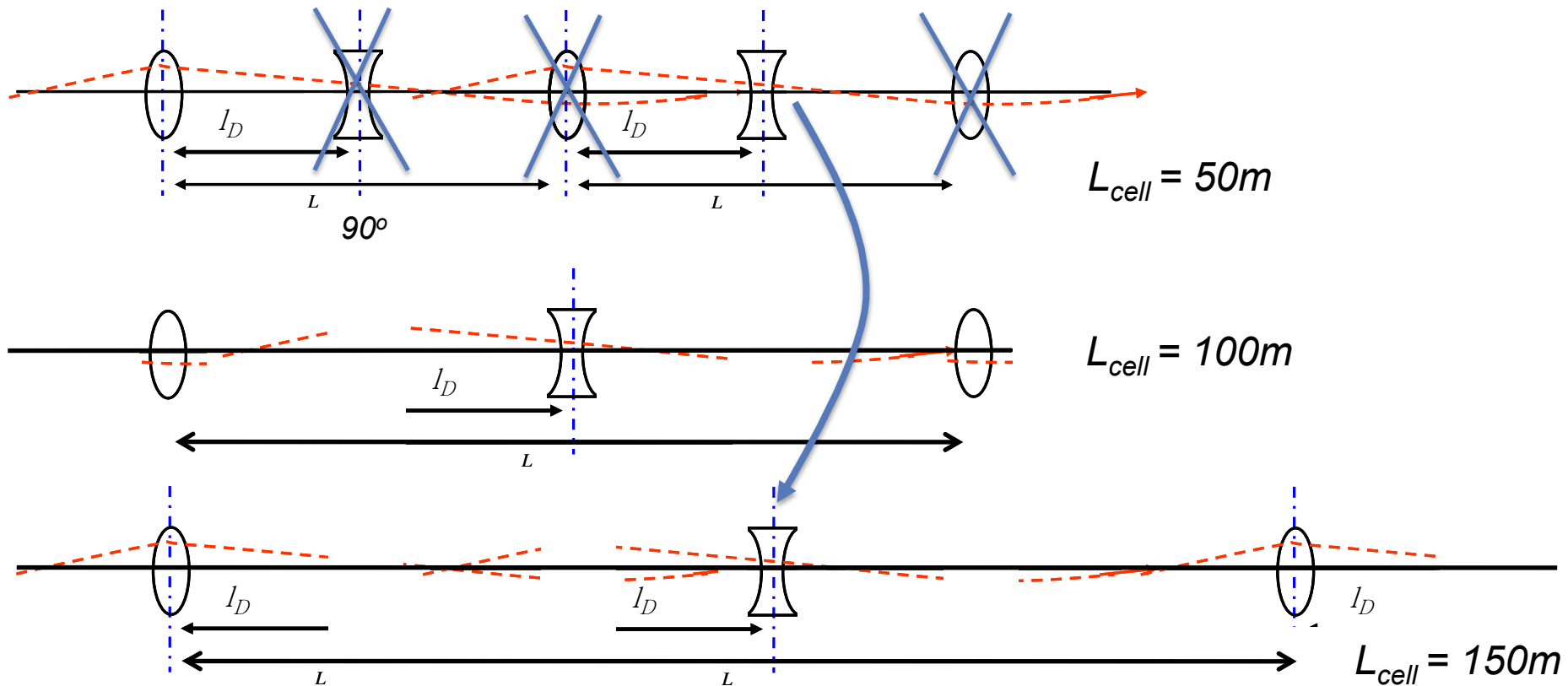


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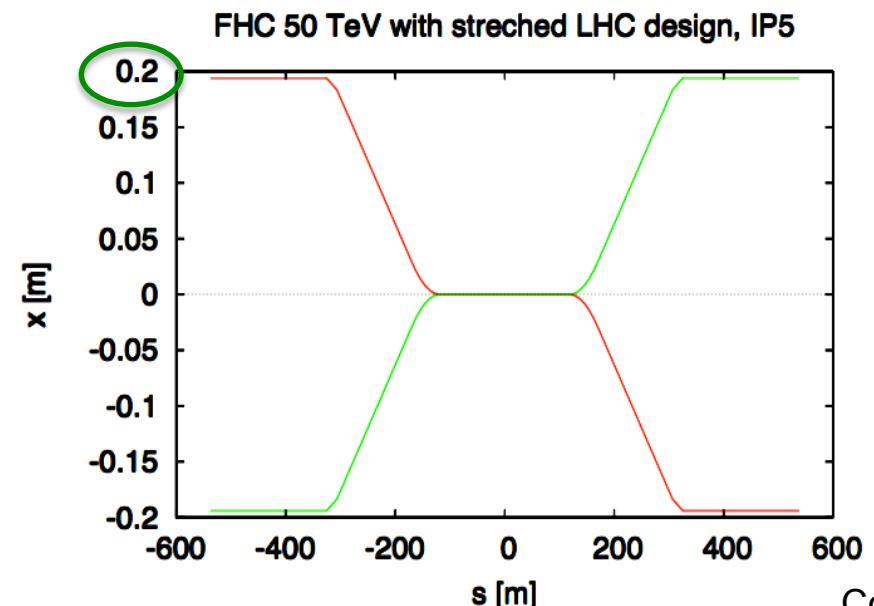
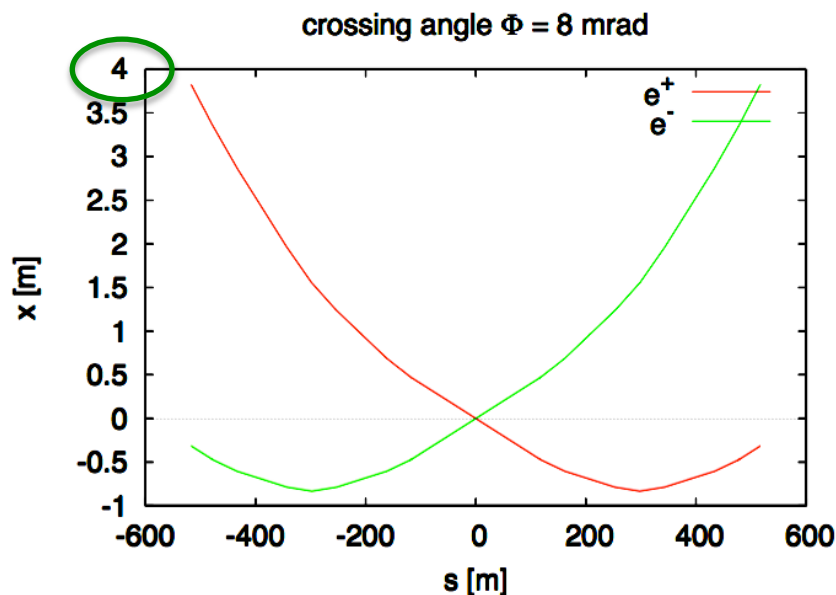
- Increase the FODO cell length to adjust the emittance!



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## 4) Interaction region lattice

- Large number of bunches: → 2 rings and crossing angles
- How do we get sufficient separation to avoid beam-beam-effect?
- How do we separate the beams without large synchrotron radiation background?



- How do we get a proton and an electron geometry together?

Court.  
Roman  
Martin

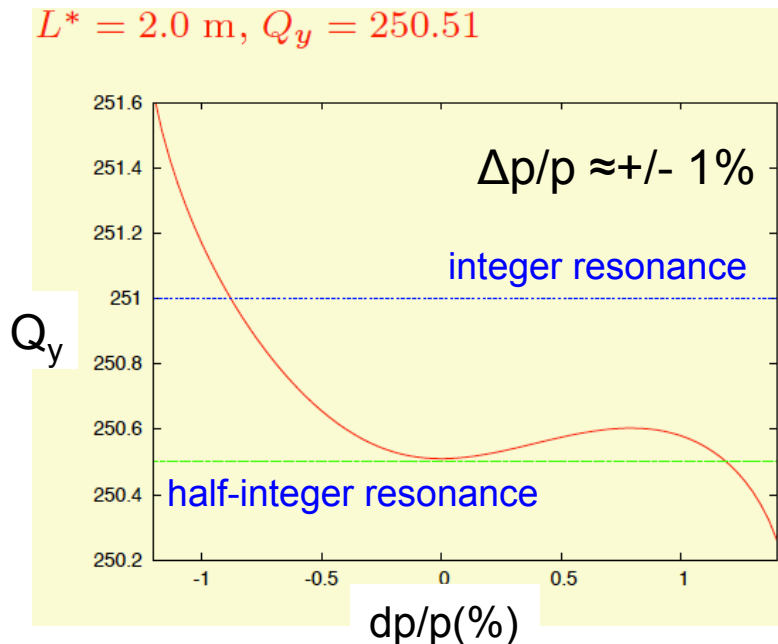
# 4) Mini-beta optics

- Extreme small  $\beta_y^* = 1$  mm drives chromaticity to extreme values

without mini-beta:  $Q'_x = -399$   
 $Q'_y = -332$

with mini-beta:  $Q'_x = -483$   
 $Q'_y = -3066$

- Tune shift drives off-momentum particles to strong resonances



→ Linear Collider like interaction region with quasi local chromaticity control?

→ How to distribute the correction load in IR and arc?

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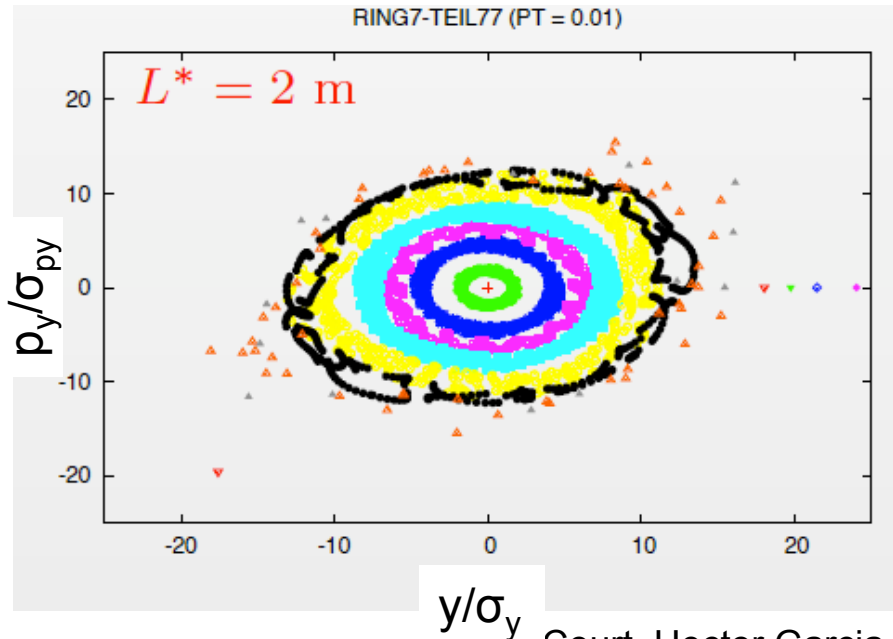
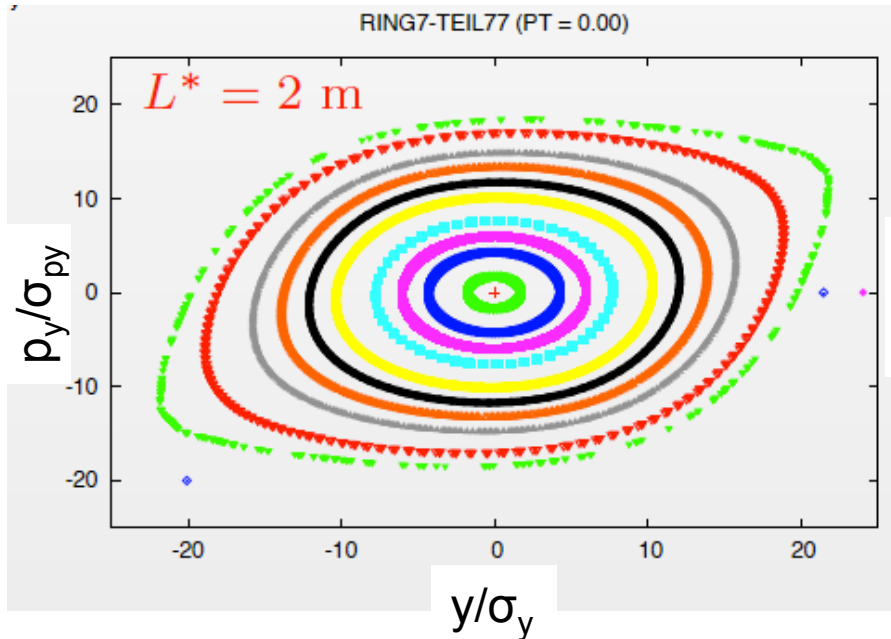


# 4) Dynamic aperture

- Very first dynamic aperture calculations

Ideal momentum  $\Delta p/p = 0$

Off momentum  $\Delta p/p = \pm 1 \%$



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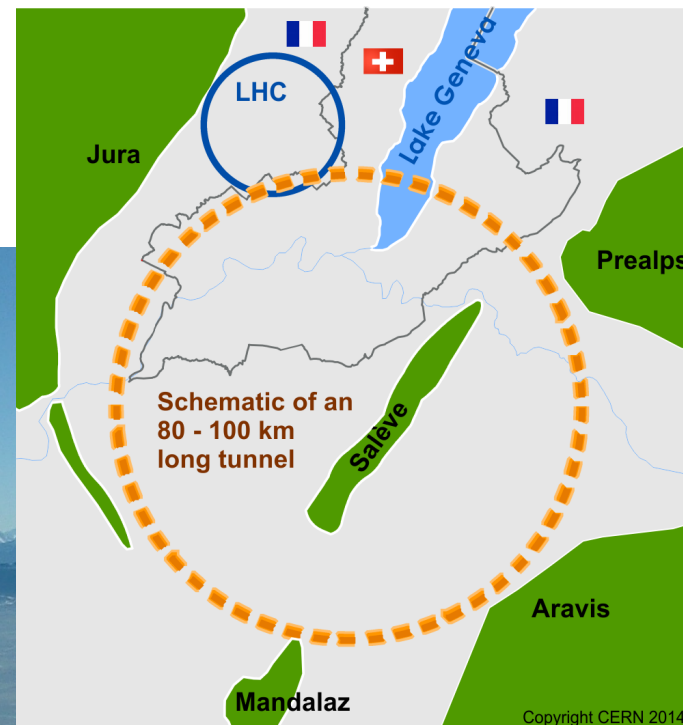
- How do we improve the dynamic aperture for  $\Delta p/p = \pm 2 \%$ ?

# Résumé

- We need a lattice design with highest flexibility.
  - Is a FODO cell the best solution? **Light source lattices?**
- We have to determine different beam optics to obtain the required emittances for all 4 energies.
- We have many **challenges for the design of the interaction region:**
  - Separation scheme with tolerable amount of synchrotron radiation
  - Large number of bunches
  - Minibeta insertions with  $\beta_y^* = 1$  mm
- And still **control and compensate the chromaticity.**
- We have to obtain a **momentum acceptance of  $\Delta p/p = \pm 2$  %.**



Thank you for your attention!



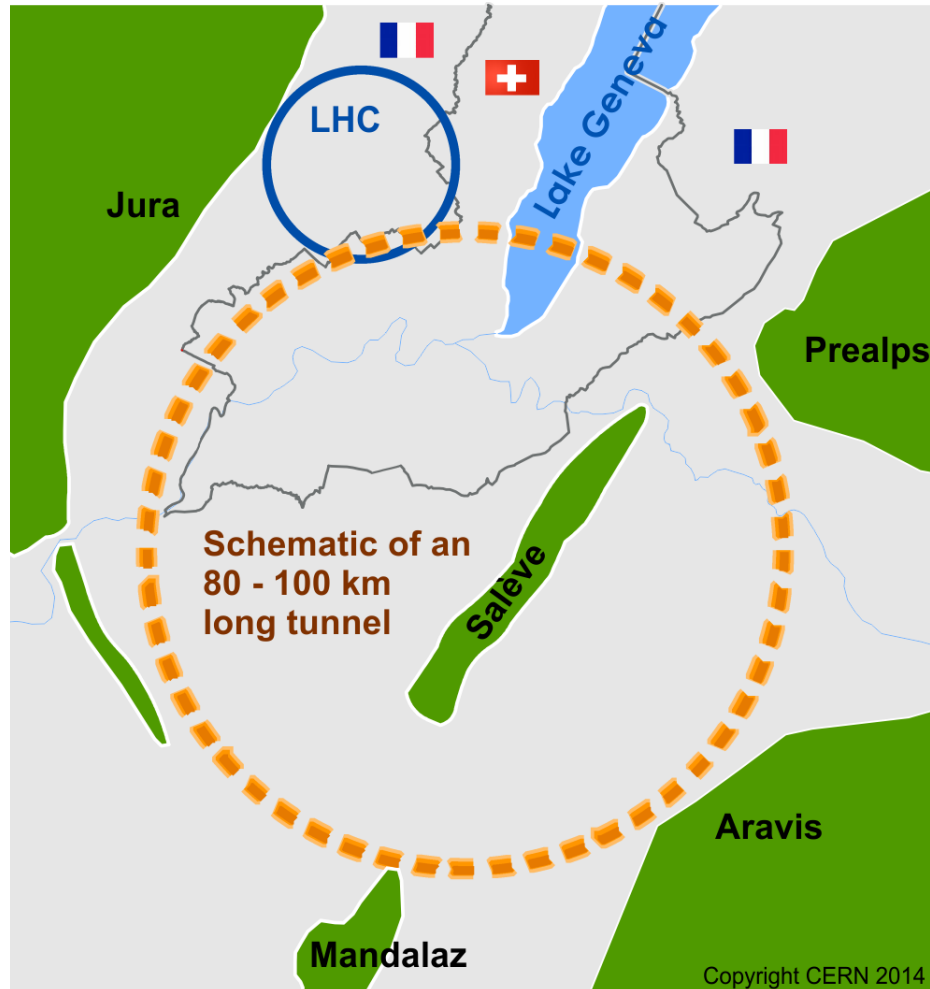
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# Potential location for TLEP/FCC-hh



court. Michael Benedikt

# FCC motivation: pushing energy frontier

## High-energy hadron collider *FCC-hh* as long-term goal

- Seems only approach to get to 100 TeV range in the coming decades
- High energy and luminosity at affordable power consumption
- Lead time design & construction > 20 years (LHC study started 1983!)  
→ Must start studying now to be ready for 2035/2040

## Lepton collider *FCC-ee* as potential intermediate step

- Would provide/share part of infrastructure
- Important precision measurements indicating the energy scale at which new physics is expected
- Search for new physics in rare decays of  $Z$ ,  $W$ ,  $H$ ,  $t$  and rare processes

## Lepton-hadron collider *FCC-he* as option

- High precision deep inelastic scattering and Higgs physics

**Most aspects of collider designs and R&D non-site specific.  
Tunnel and site study in Geneva area as ESU requests.**

**(court. Michael Benedikt)**

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| Beam current [mA]              | 1450  | 152  | 30    | 6.6   |
| Bunches / beam                 | 16700 | 4490 | 1360  | 98    |
| Bunch population [ $10^{11}$ ] | 1.8   | 0.7  | 0.46  | 1.4   |
| Transverse emittance e         |       |      |       |       |
| - Horizontal [nm]              | 29.2  | 3.3  | 0.94  | 2     |
| - Vertical [pm]                | 60    | 7    | 1.9   | 2     |
| Momentum comp. [ $10^{-5}$ ]   | 18    | 2    | 0.5   | 0.5   |
| Betatron function at IP $b^*$  |       |      |       |       |
| - Horizontal [m]               | 0.5   | 0.5  | 0.5   | 1     |
| - Vertical [mm]                | 1     | 1    | 1     | 1     |
| Beam size at IP $s^*$ [mm]     |       |      |       |       |
| - Horizontal                   | 121   | 26   | 22    | 45    |
| - Vertical                     | 0.25  | 0.13 | 0.044 | 0.045 |
| Bunch length [mm]              |       |      |       |       |
| - Synchrotron radiation        | 1.64  | 1.01 | 0.81  | 1.16  |
| - Total                        | 2.56  | 1.49 | 1.17  | 1.49  |
| Energy loss / turn [GeV]       | 0.03  | 0.33 | 1.67  | 7.55  |
| Total RF voltage [GV]          | 2.5   | 4    | 5.5   | 11    |

- Design & optimize a lattice for **4 different energies**
- Interaction region layout for a **large number of bunches**
- Horizontal emittance is **increasing** with reduced energy
- **Extremely small vert. beta\*** ( $\beta_y^* = 1 \text{ mm}$ )
  - High chromaticity
  - Challenging dynamic aperture
- **High synchrotron radiation losses** include sophisticated absorber design in the lattice

# Interconnection types and naming convention



IC BB

IC  
BQ

QB



Assumptions:

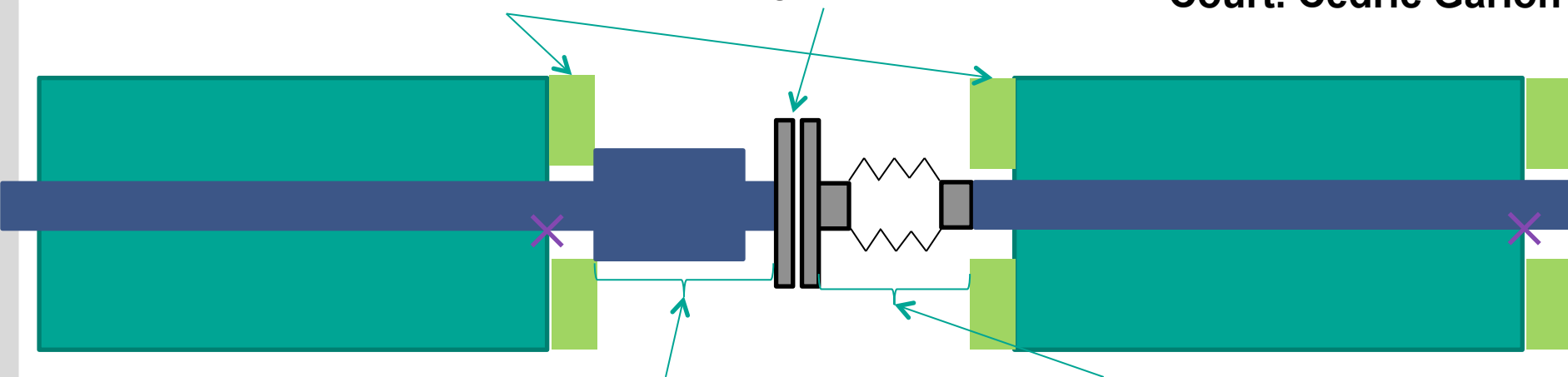
Quadrupoles and sextupoles with the same chamber and on same girder (two halves?)

Interconnection BB

Coils: 10 cm

Flanges : 5 cm

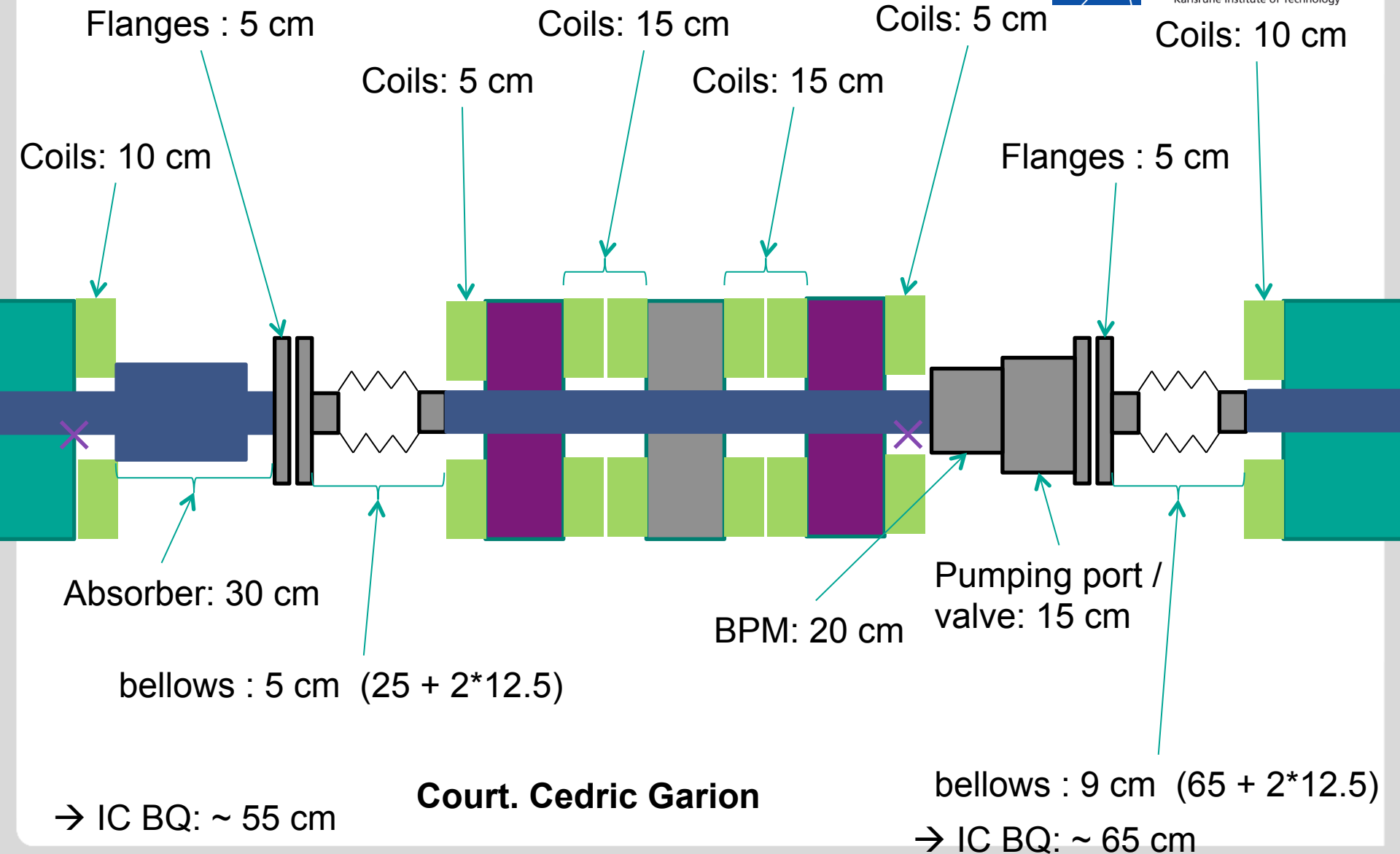
Court. Cedric Garion



→ IC BB: ~ 65 cm

Absorber: 30 cm    bellows : 9 cm (65 + 2\*12.5)

# Interconnections BQ and QB





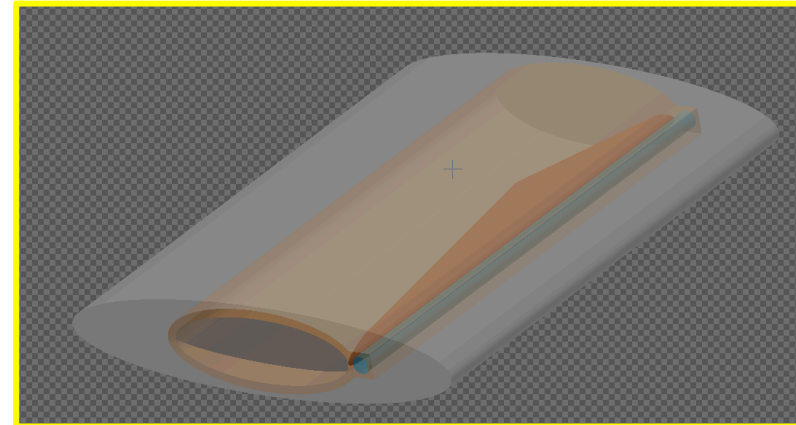
# Challenge 2: Lattice Design ... Layout of the Magnets

Achieve **highest possible fill factor**

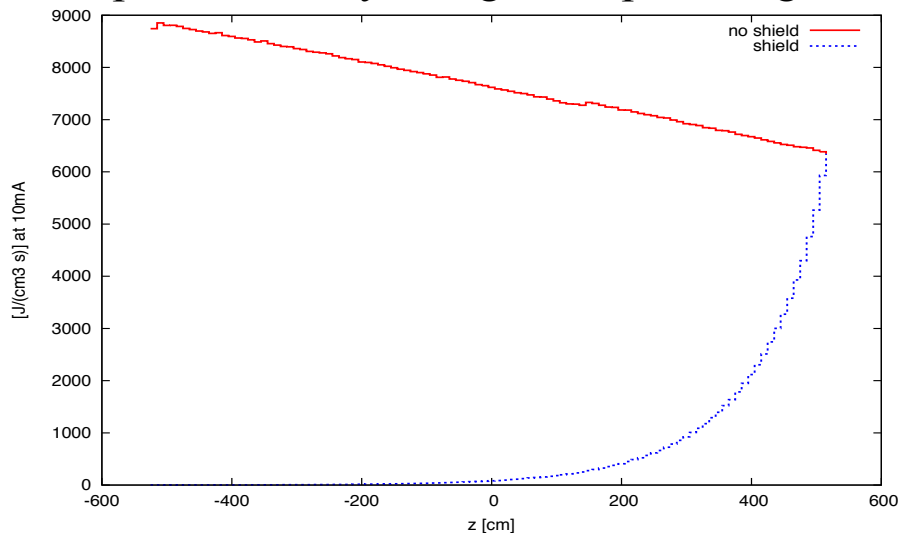
to limit synchrotron radiation losses

Include **Absorber Design** in the lattice layout

Distribute RF straights to **limit saw tooth effect**  
(dispersion suppressor layout)



power density along the dipole magnet



*Dipole length defined by  
synchrotron radiation load*

$$L_{\text{dipole}} < 11 \text{m}$$

*court. Luisella Lari et al*

## 2) Beam emittances

- Equilibrium emittances calculated by MAD-X:

$$\varepsilon_x = 1.23 \text{ nm}, \varepsilon_y = 1.05 \text{ pm} \quad \checkmark$$

Without minibetas!

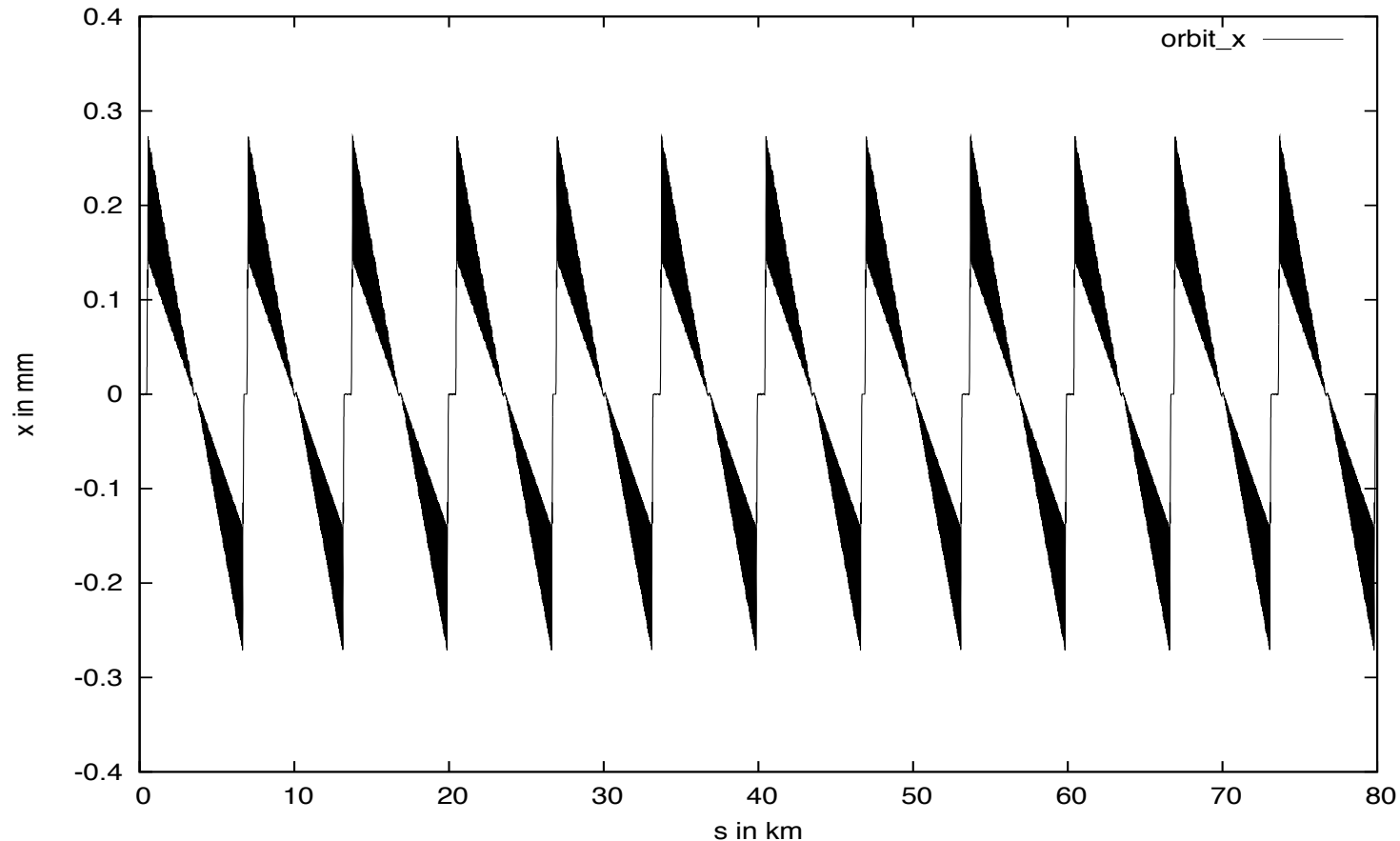
- Can we maintain these values including coupling and beam-beam effects?
- How do we deal with the extreme sensitivity of the minibeta sections?

$$(\beta_y \approx 18 \text{ km})$$

$$x_{rms}(s) = \frac{\sqrt{\beta(s)}}{2 \sin Q\pi} \Delta x' \sqrt{\beta(s_0)} \cos[\psi(s) - \psi(s_0) - Q\pi]$$

→ Active alignment feature with piezos?

# Sawtooth effect (no misalignments)



- RF equally distributed among minibetas and straight sections

### 3) Lattice modifications for smaller energies



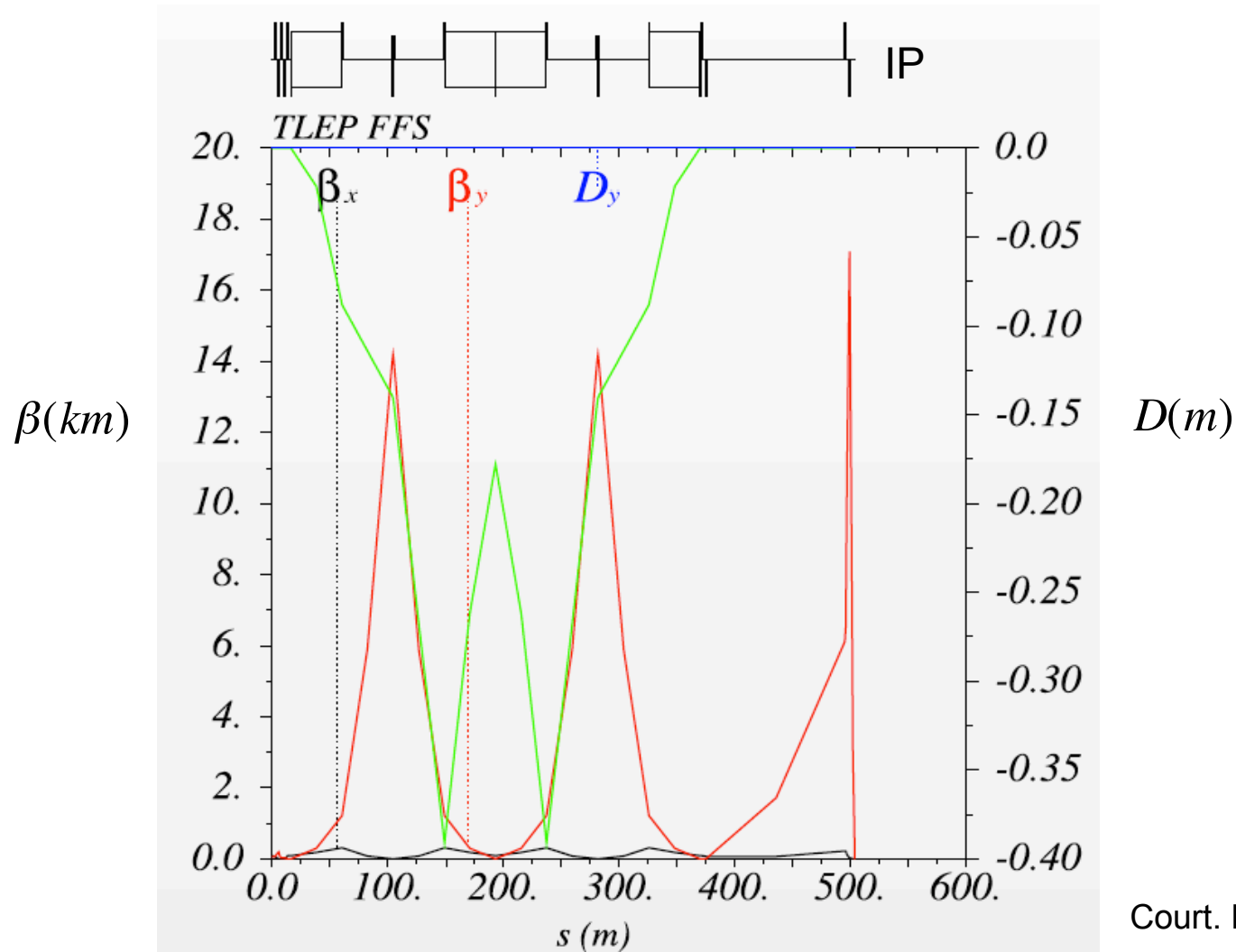
|                                 | Z    | W   | H    | tt  |
|---------------------------------|------|-----|------|-----|
| Beam energy [GeV]               | 45.5 | 80  | 120  | 175 |
| Transverse emittance $\epsilon$ |      |     |      |     |
| - Horizontal [nm]               | 29.2 | 3.3 | 0.94 | 2   |
| - Vertical [pm]                 | 60   | 7   | 1.9  | 2   |

- At 45.5 GeV the emittance is a factor 15 higher compared to 175 GeV!

BUT:  $\epsilon_0 = C_q \gamma^2 \frac{I_5}{J_x I_2}$ ,  $I_2 = \oint \frac{1}{\rho^2} ds$ ,  $I_5 = \oint \frac{\mathcal{H}_x}{|\rho|^3} ds$ ,  $\mathcal{H}_x = \gamma_x \eta_x^2 + 2\alpha_x \eta_x \eta_{px} + \beta_x \eta_{px}^2$

→ How can we counteract the natural emittance shrinking for lower energies?

# Minibeta with quasi-local correction scheme



Court. Hector Garcia