



# Search for a critical point of strongly-interacting matter in central $^{40}\text{Ar} + ^{45}\text{Sc}$ collisions at 13A–75A GeV/c beam momentum

NA61/SHINE Collaboration\*

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**Abstract** The critical point of strongly interacting matter is searched for at the CERN SPS by the NA61/SHINE experiment in central  $^{40}\text{Ar} + ^{45}\text{Sc}$  collisions at 13A, 19A, 30A, 40A, and 75A GeV/c. The dependence of the second-order scaled factorial moments of proton multiplicity distributions on the number of subdivisions in transverse momentum space is measured. The intermittency analysis uses statistically independent data sets for every subdivision in transverse and cumulative-transverse momentum variables. The results obtained do not indicate the searched intermittent pattern. An upper limit on the fraction of correlated protons and the intermittency index is obtained based on a comparison with the Power-law Model.

## 1 Introduction

The experimental results are presented on intermittency analysis using second-order scaled factorial moments of mid-rapidity protons produced in central  $^{40}\text{Ar} + ^{45}\text{Sc}$  collisions at 13A, 19A, 30A, 40A, and 75A GeV/c beam momentum ( $\sqrt{s_{\text{NN}}} \approx 5.1\text{--}11.9$  GeV). The measurements were performed by the multi-purpose NA61/SHINE [1] apparatus being operated at the CERN Super Proton Synchrotron (SPS). They are part of the strong interactions program of NA61/SHINE devoted to studying the properties of strongly interacting matter, such as the onset of deconfinement and critical endpoint (CP). Within this program, a two-dimensional scan of collision energy and colliding nuclei size was conducted [2].

In the QCD phase diagram, CP is a hypothetical endpoint of the first-order phase transition line with properties of second-order phase transition. In the proximity of CP, self-similar dynamics [3] is expected to lead to the corresponding fluctuations of the chiral order parameter, belonging to the 3D-Ising universality class [4] and can be detected in

transverse momentum space within the framework of intermittency analysis of proton density fluctuations using scaled factorial moments.

The idea of “intermittency”, which was first introduced to the study of turbulent flow [5], later became important in the physics of particle production, especially as a way to study fluctuations. In the pioneering article of Bialas and Peschanski [6] introducing intermittency analysis to high-energy physics, it was proposed to study the scaled factorial moments of the multiplicity of particles produced in high-energy collisions as a function of the resolution size of rapidity interval.

Over the past decade, there has been significant experimental exploration into intermittency and fractality within high-energy collisions. The initial findings from NA49 [7,8] and NA61/SHINE [9] Collaborations have been reported, inspiring further investigation by the NA61/SHINE Collaboration through an Ar+Sc energy scan aimed at searching for the critical point of strongly interacting matter via intermittency analysis. Additionally, recent intermittency studies by STAR [10] and ALICE [11] Collaborations have been reported.

In the meantime, various model studies have been conducted to understand the experimental data. It includes studies reported in Refs. [12–18] along with the Critical Monte-Carlo (CMC) [3] and Power-law Model [19].

This paper follows the proton intermittency analysis of  $^{40}\text{Ar} + ^{45}\text{Sc}$  collisions at 150A GeV/c [9] by the NA61/SHINE Collaboration. This analysis was performed in intervals of transverse momentum and cumulative transverse momentum distributions. Using the approach of intermittency analysis introduced in Ref. [9], statistically independent data sets were used to obtain results for the different numbers of intervals.

The paper is organized as follows. Section 2 introduces quantities exploited for the CP search using the intermittency analysis. In Sect. 3, the characteristics of the NA61/SHINE detector, relevant for the current study, are briefly presented. The details of data selection and the analysis procedure are

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Collision energy per nucleon pair in the center-of-mass system.

presented in Sect. 4. Results obtained are shown in Sect. 5 and compared with models in Sect. 6. A summary in Sect. 7 closes the paper.

Throughout this paper, the rapidity,  $y = \text{atanh}(\beta_L)$ , is calculated in the nucleon-nucleon center-of-mass frame by shifting rapidity in laboratory frame by rapidity of the nucleon-nucleon center-of-mass, assuming proton mass. The  $\beta_L = p_L/E$  ( $c \equiv 1$ ) is the longitudinal (z) component of the velocity, while  $p_L$  and  $E$  are particle longitudinal momentum and energy in the collision center-of-mass system. The transverse component of the momentum is denoted as  $p_T = \sqrt{p_x^2 + p_y^2}$ , where  $p_x$  and  $p_y$  are its horizontal and vertical components. The azimuthal angle is the angle between the transverse momentum vector and the horizontal (x) axis. Total momentum in the laboratory system is denoted as  $p_{lab}$ .

The  $^{40}\text{Ar} + ^{45}\text{Sc}$  collisions are selected by requiring a low energy value measured by the forward calorimeter, the Projectile Spectator Detector (PSD). This is the energy emitted into the region populated mostly by projectile spectators. These collisions are called PSD-central collisions, and a selection of collisions based on the PSD energy is called a PSD-centrality selection.

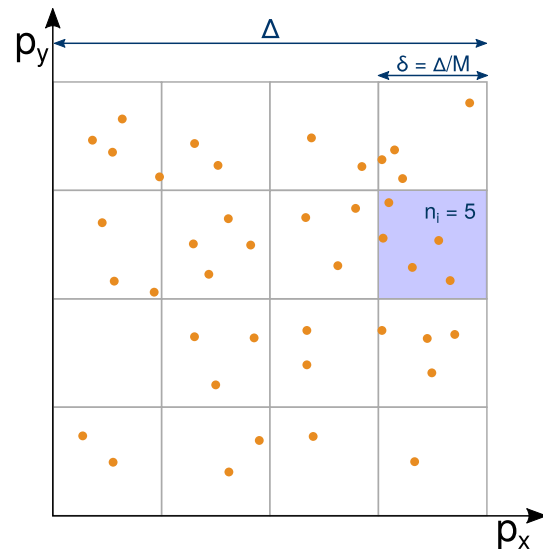
## 2 Scaled factorial moments

### 2.1 Critical point and intermittency in heavy-ion collisions

A second-order phase transition leads to the divergence of the correlation length ( $\xi$ ). The infinite system becomes scale-invariant with the particle density-density correlation function exhibiting power-law scaling, which induces intermittent behavior of particle multiplicity fluctuations [20].

The maximum critical signal is expected when the freeze-out occurs close to the CP. On the other hand, the energy density at the freeze-out is lower than at the early stage of the collision. Clearly, the critical point should be experimentally searched for in nuclear collisions at energies higher than that of the onset of deconfinement – when quark-gluon plasma creation sets in.

The intermittent multiplicity fluctuations [6] were discussed as the signal of CP by Satz [21], Antoniou et al. [22] and Bialas, Hwa [23]. This initiated experimental studies of the structure of the phase transition region via analyses of particle multiplicity fluctuations using scaled factorial moments [8]. Later, additional measures of fluctuations were also proposed as probes of the critical behavior [24, 25]. The NA61/SHINE experiment has performed a systematic scan of collision energy and system size. To date none of the anticipated signals have been observed for the critical behavior [26–28]. The new measurements may answer the



**Fig. 1** Two-dimensional transverse momentum space is subdivided into  $M \times M$  number of equally sized bins. The  $n_i$  is the particle multiplicity in a given subinterval,  $\Delta$  is the momentum region, and  $\delta$  is bin width (in this example  $n_i$  equals 5 in the (4,3) subinterval)

question about the nature of the transition region and, in particular, whether or not the critical point of strongly interacting matter exists.

The scaled factorial moments  $F_r(M)$  [6] of order  $r$  are defined as:

$$F_r(M) = \frac{\left\langle \frac{1}{M^D} \sum_{i=1}^{M^D} n_i \dots (n_i - r + 1) \right\rangle}{\left\langle \frac{1}{M^D} \sum_{i=1}^{M^D} n_i \right\rangle^r}, \quad (1)$$

where  $M$  is the number of subdivision intervals in each of the  $D$  dimensions of the selected range  $\Delta$  (see Fig. 1),  $n_i$  is the particle multiplicity in a given subinterval and angle brackets denote averaging over the analyzed events. In the presented analysis,  $\Delta$  is divided into two-dimensional ( $D = 2$ ) cells in  $p_x$  and  $p_y$ . In case the mean particle multiplicity,  $\langle n_i \rangle$ , is proportional to the subdivision interval size and for a Poissonian multiplicity distribution,  $F_r(M)$  is equal to 1 for all values of  $r$  and  $M^D$ . This condition is satisfied in the configuration space when the particle density is uniform. The momentum distribution is, in general, non-uniform, and thus in the momentum space, it is more convenient to use the cumulative variables [29] which, for a small cell size, leave a power-law behavior unaffected and at the same time lead to a uniformly distributed particle density.

If the system freezes out near CP, its properties are expected to be different from those of an ideal gas [30]. Such a system represents a simple fractal and  $F_r(M)$  follows a power-law dependence:

$$F_r(M) = F_r(\Delta) \cdot (M^D)^{\varphi_r}. \tag{2}$$

Moreover, the exponent (intermittency index)  $\varphi_r$  obeys the relation:

$$\varphi_r = (r - 1) \cdot (d_r/D), \tag{3}$$

where  $d_r$ , the anomalous fractal dimension, is independent of  $r$  [23]. Such behavior is the analogue of critical opalescence in electromagnetically interacting matter [3]. Importantly the critical properties given by Eqs. 2 and 3 are approximately preserved for a small cell size (large  $M$ ) under transformation to the cumulative variables [29,31].

The ideal CP signal, Eqs. 2 and 3, derived for the infinite system in equilibrium, are generally deteriorated by numerous experimental effects present in high-energy nuclear collisions. This includes the system’s finite size and evolution time, other dynamical correlations between particles, and limited acceptance and finite resolution of measurements. Moreover, to experimentally search for CP in high-energy collisions, the dimension and size of the momentum interval must be chosen. Note that unbiased results can be obtained only by analyzing variables and dimensions in which the singular behavior appears [32–34]. Any other procedure is likely to distort the critical-fluctuation signal.

Search for the CP via the study of proton fluctuations was suggested in several publications [25,35–43]. In the case of a pure system exhibiting critical fluctuations, for proton,  $d = \varphi_2 = 5/6$  is expected [3].

### 2.2 Cumulative transformation

Scaled factorial moments are sensitive to the shape of the single-particle momentum distribution. This dependence biases the signal of critical fluctuations. To remove this dependence, one has two possibilities. The first possibility is to exploit the mixed events, where each event is constructed using particles from different experimental events, thereby removing all possible correlations. The objective is to measure the following quantity:

$$\Delta F_2(M) = F_2^{\text{data}}(M) - F_2^{\text{mixed}}(M). \tag{4}$$

It was already verified [8] that this procedure, to a large extent, removes the dependence of  $\Delta F_r(M)$  on the shape of single-particle distribution, at least for  $r = 2$ .

The second possibility is to use cumulative transformation [29], which for a one-dimensional single-particle distribution  $f(x')$  reads:

$$Q_x = \int_a^x f(x')dx' / \int_a^b f(x')dx', \tag{5}$$

where  $a$  and  $b$  are lower and upper limits of the variable  $x'$ . For a two-dimensional distribution  $f(x', y')$  and a given  $x' = x$  the transformation reads

$$Q_y(x) = \int_a^y f(x, y')dy' / \int_a^b f(x, y')dy'. \tag{6}$$

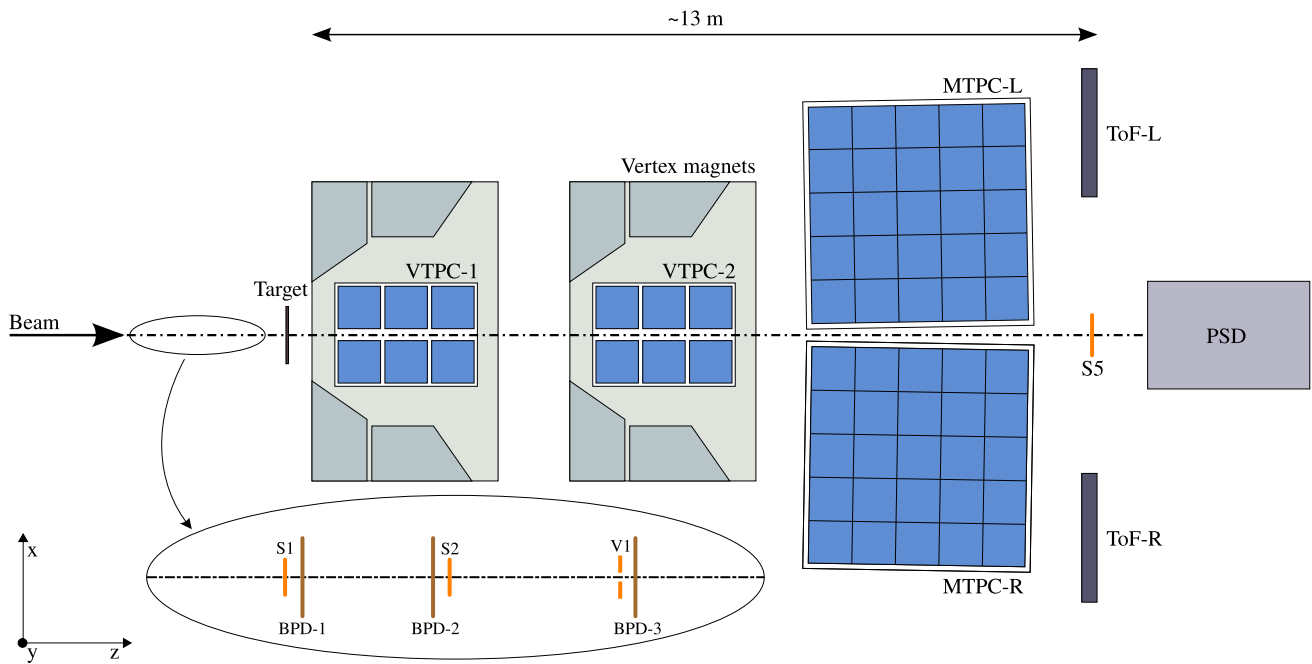
After the cumulative transformation, any single-particle distribution becomes flat, ranging from 0 to 1, see example distributions in Ref. [9], and therefore, it removes the dependence on the shape of the single-particle distribution for uncorrelated particles [29]. It also distorts all non-scale-invariant correlations. On the other hand, the transformation is proven to preserve the critical behaviour [31] given by Eq. 2, at least for the second-order scaled factorial moments.

Both methods are approximate. Subtracting moments for mixed data set may introduce negative  $\Delta F_2(M)$  values [8] and using cumulative quantities mixes the scales of the momentum differences and therefore may distort eventual power-law behavior due to the finite size of the momentum interval,  $\Delta$ .

### 3 The NA61/SHINE detector

The NA61/SHINE detector (see Fig. 2) is a large-acceptance hadron spectrometer situated in the North Area H2 beam-line of the CERN SPS [1]. The main components of the detection system used in the analysis are four large-volume time projection chambers (TPC). Two Vertex TPCs (VTPC-1/2) are located downstream of the target inside superconducting magnets with a maximum combined bending power of 9 Tm. The magnetic field was scaled in proportion to the beam momentum in order to obtain similar  $y - p_T$  acceptance at all beam momenta. The main TPCs (MTPC-L/R) and two walls of pixel time-of-flight (ToF-L/R) detectors are placed symmetrically on either side of the beamline downstream of the magnets. The TPCs were filled with Ar:CO<sub>2</sub> gas mixture in proportions 90:10 for the VTPCs and 95:5 for the MTPCs. The Projectile Spectator Detector (PSD), a zero-degree hadronic calorimeter, is positioned 20.5 m (16.7 m) downstream of the MTPCs at beam momenta of 75 A (13 A, 19 A, 30 A, and 40 A), centered in the transverse plane on the deflected position of the beam.

The PSD consists of 44 modules that cover a transverse area of almost 2.5 m<sup>2</sup>. The central part of the PSD consists of 16 small modules with transverse dimensions of 10 × 10 cm<sup>2</sup> and its outer part consists of 28 large 20 × 20 cm<sup>2</sup> modules. Moreover, a brass cylinder of 10 cm (30 A–75 A GeV/c) or 5 cm (19 A GeV/c) length and 5 cm diameter (degrader) was placed in front of the center of the PSD to reduce electronic saturation effects and shower leakage from the downstream



**Fig. 2** The schematic layout of the NA61/SHINE experiment at the CERN SPS [1] showing the components used for the Ar+Sc energy scan (horizontal cut, not to scale). The detector configuration upstream of the target is shown in the inset. The alignment of the chosen coordinate system is shown on the plot; its origin ( $x=y=z=0$ ) lies in the

middle of VTPC-2, on the beam axis. The nominal beam direction is along the  $z$ -axis. Target is placed at  $z = -580.00$  cm. The magnetic field bends charged particle trajectories in the  $x$ - $z$  (horizontal) plane. The drift direction in the TPCs is along the (vertical)  $y$ -axis

side caused by the Ar beam and its heavy fragments. No degrader was used at 13A GeV/c.

Primary beams of fully ionized  $^{40}\text{Ar}$  nuclei were extracted from the SPS accelerator at beam momenta of 13A, 19A, 30A, 40A, and 75A GeV/c. Two scintillation counters, S1 and S2, provide beam signal, and a veto counter V1, with a 1 cm diameter hole, defines the beam before the target. The S1 counter also provides the timing reference (start time for all counters). Beam particles are selected by the trigger system requiring the coincidence  $T1 = S1 \wedge S2 \wedge \overline{V1}$ . The three beam position detectors (BPDs) placed upstream of the target [1] precisely measure individual beam particle trajectories. Collimators in the beam line were adjusted to obtain beam rates of  $\approx 10^4/s$  during the 10.4 s spill and a super-cycle time of 32.4 s.

The target was a stack of  $2.5 \times 2.5$  cm<sup>2</sup> area and 1 mm thick  $^{45}\text{Sc}$  plates of 6 mm total thickness placed  $\approx 80$  cm upstream of VTPC-1. Impurities due to other isotopes and elements were measured to be 0.3% [44]. No correction was applied for this negligible contamination.

Interactions in the target are selected with the trigger system by requiring an incoming  $^{40}\text{Ar}$  ion and a signal below that of beam ions from S5, a small 2 cm diameter scintillation counter placed on the beam trajectory behind the MTPCs. This minimum bias trigger is based on the breakup of the beam ion due to interactions in and downstream of the tar-

get. In addition, central collisions were selected by requiring an energy signal below a set threshold from the 16 central modules of the PSD, which measure mainly the energy carried by projectile spectators. The cut was set to retain only the events with the  $\approx 30\%$  smallest energies in the PSD. The event trigger condition thus was  $T2 = T1 \wedge S5 \wedge \overline{\text{PSD}}$ .

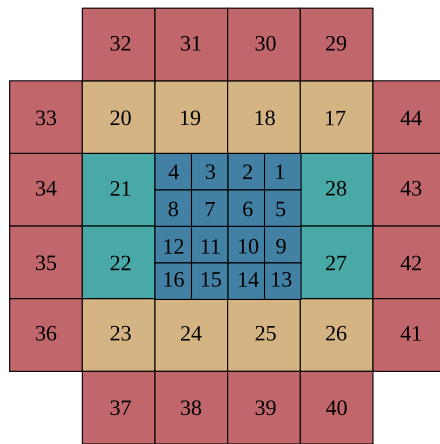
## 4 Analysis

The goal of the analysis was to search for the critical point of the strongly interacting matter by measuring the second-order scaled factorial moments for a selection of protons produced in central  $^{40}\text{Ar} + ^{45}\text{Sc}$  collisions at 13A–75A GeV/c, using statistically independent points and cumulative variables.

### 4.1 Event selection

The NA61/SHINE detector recorded events using 13A–75A GeV/c  $^{40}\text{Ar}$  beam impinging on a stationary  $^{45}\text{Sc}$  target. However, not all of those events contain well-reconstructed central Ar+Sc interactions. Therefore the following criteria were used to select data for further analysis:

- (i) T2 trigger set to select central and semi-central collisions,



■ T2 trigger,  
■ + ■ + ■ 30A, 40A and 75A,  
■ + ■ + ■ + ■ 13A and 19A GeV/c.

**Fig. 3** Event centrality selection using the PSD energy. Modules used in the centrality class determination were chosen based on the anti-correlation between the measured energy and the track multiplicity in a given event. All modules were used for 13A and 19A GeV/c. For 30A, 40A, and 75A GeV/c 28 central modules were chosen. For the T2 trigger, 16 central modules were used

- (ii) beam particle detected in at least three planes out of four of BPD-1 and BPD-2 and in both planes of BPD-3,
- (iii) no off-time beam particle detected within a time window of  $\pm 4 \mu\text{s}$  around the trigger particle,
- (iv) no interaction-event trigger detected within a time window of  $\pm 25 \mu\text{s}$  around the trigger particle,
- (v) a high-precision interaction vertex with z position (fitted using the beam trajectory and TPC tracks) no further than 2 cm away from the center of the Sc target.

### 4.2 Centrality selection

The final results presented in this paper refer to the 0–10% of  $^{40}\text{Ar} + ^{45}\text{Sc}$  collisions with the lowest energy value measured by a subset of PSD modules (see Fig. 3). The selection of the

modules was to optimize the sensitivity to projectile spectators. For more details see Ref. [45]. Online event selection by the hardware trigger (T2) used a threshold on the sum of electronic signals from the 16 central modules of the PSD set to accept  $\approx 30\%$ ,  $35\%$ ,  $30\%$ ,  $35\%$ , and  $20\%$  of the inelastic  $^{40}\text{Ar} + ^{45}\text{Sc}$  collisions at 13A–75A GeV/c. To select 0–10% central collision events, an upper limit of energy values measured by a subset of modules are 143, 264, 446, 666, and 1290.6 GeV corresponding to  $^{40}\text{Ar} + ^{45}\text{Sc}$  collisions at 13A–75A GeV/c.

The event statistics after applying the selection criteria are summarized in Table 1.

### 4.3 Single-track selection

To select tracks of primary charged hadrons and to reduce the contamination by particles from secondary interactions, weak decays, and off-time interactions, the following track selection criteria were applied:

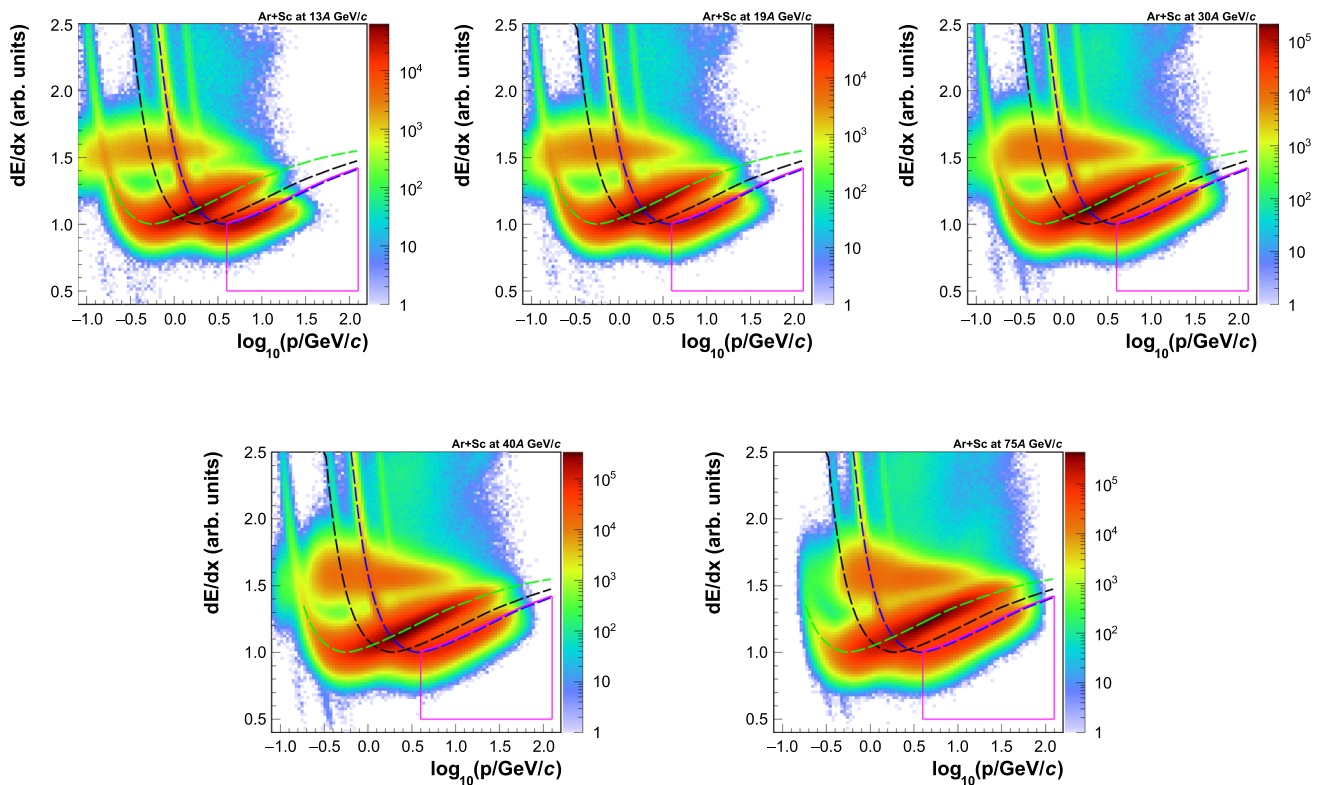
- (i) track momentum fit including the interaction vertex is required to have converged,
- (ii) total number of reconstructed points on the track is required to be greater than 30,
- (iii) the sum of the number of reconstructed points in VTTPC-1 and VTTPC-2 is required to be greater than 15,
- (iv) the ratio of the number of reconstructed points to the number of potential (maximum possible) points is required to be greater than 0.5 and less than 1.1,
- (v) number of points used to calculate energy loss ( $dE/dx$ ) is required to be greater than 30,
- (vi) the distance between the track extrapolated to the interaction plane and the vertex (track impact parameter) is required to be smaller than 4 cm in the horizontal (bending) plane and 2 cm in the vertical (drift) plane.

As the analysis concerns mid-rapidity protons, only particles with center-of-mass rapidity (assuming proton mass) between 0 and 0.75 were considered. Only particles with transverse momentum components,  $p_x$  and  $p_y$ , values lower than 1.5 GeV/c were accepted for the analysis.

**Table 1** The statistics of selected events for  $^{40}\text{Ar} + ^{45}\text{Sc}$  collisions at beam momentum ( $p_{beam}$ ) of 13A–75A GeV/c

$p_{beam}$ (GeV/c)	Number of events after cuts ( $10^6$ )				
	T2 trigger	Beam quality	Beam off-time	Vertex z position	0–10% of most central
13A	2.14	1.60	1.56	1.48	0.50
19A	2.51	2.00	1.93	1.83	0.52
30A	3.71	2.93	2.85	2.74	0.91
40A	5.71	4.87	4.74	4.53	1.29
75A	2.89	2.44	2.37	2.32	1.16





**Fig. 4** Energy loss versus the logarithm of the total momentum of positively charged particles measured with the NA61/SHINE Time Projection Chambers in the selected  $^{40}\text{Ar} + ^{45}\text{Sc}$  events at 13A–75A GeV/c.

#### 4.3.1 Proton selection

To identify proton candidates, positively charged particles were selected. Their ionization energy loss ( $dE/dx$ ) in TPCs is taken to be greater than 0.5 and less than the proton Bethe-Bloch value increased by the 15% difference between the values for kaons and protons while the momentum is in the relativistic-rise region (from 4 to 125 GeV/c). The energy loss versus the logarithm of the total momentum of the selected positive particles for  $^{40}\text{Ar} + ^{45}\text{Sc}$  collisions at 13A–75A GeV/c is shown in Fig. 4. The selected region is marked with a magenta line.

This procedure was found to select, on average, about 60% of protons. The remaining average kaon contamination is of the order of a few percent, depending on collision energy, see Ref. [46].

Similar to the kinematic acceptance, the random removal of 40% of protons belongs to the definition of the experimental results outlined in Sect. 5. The corresponding random proton losses do not bias the final results of the independent production of protons in the transverse momentum space. The results for correlated protons will be biased by the selection (see Sect. 6.2). Since this aspect is unavoidable and cannot be removed or corrected for in a model-independent

The picture's dashed blue, black, and green lines are nominal Bethe-Bloch lines for protons, kaons, and pions, respectively. The graphical cut selecting proton candidates is marked with a magenta line

manner, it should be included in comparisons with models (see Sect. 6).

#### 4.4 Acceptance maps

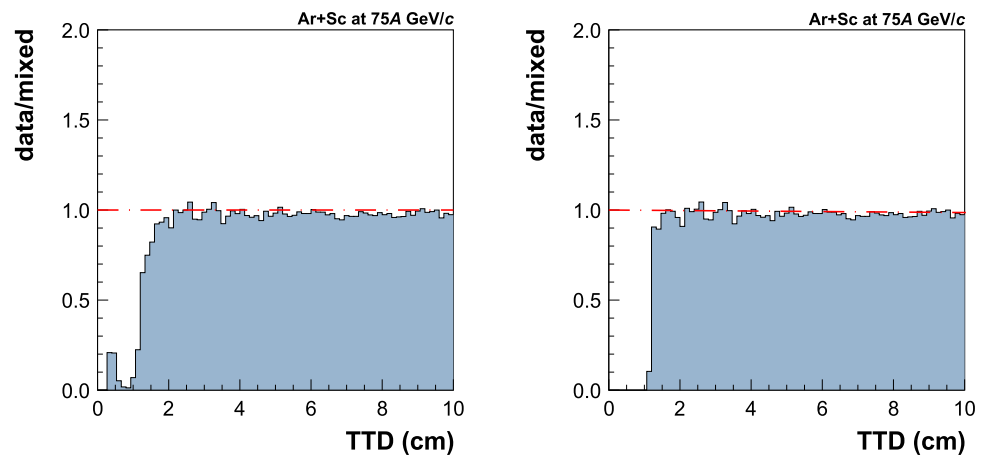
##### 4.4.1 Single-particle acceptance map

A three-dimensional ( $p_x$ ,  $p_y$  and center-of-mass rapidity) acceptance maps [47] for central  $^{40}\text{Ar} + ^{45}\text{Sc}$  collisions at 13A–75A GeV/c were created to describe the momentum region selected for this analysis. These maps were calculated by comparing the number of Monte Carlo-generated mid-rapidity protons before and after detector simulation and reconstruction. Only particles from the regions with at least 70% reconstructed particles are analyzed. The single-particle acceptance maps have to be used for calculating model predictions and they are given in Ref. [47].

##### 4.4.2 Two-particle acceptance map

The Time Projection Chambers (the main tracking devices of NA61/SHINE) cannot distinguish tracks that are too close to each other in space. At a small distance, their clusters overlap, and signals are merged. Consequently, the TPC cluster finder

**Fig. 5** The two-track distance distribution of the ratio of the number of track pairs in data and mixed events. The example for central  $^{40}\text{Ar} + ^{45}\text{Sc}$  collisions at 75A GeV/c is given. The left plot shows the distribution before the mTTD cut and the right one after. See text for details



**Table 2** Numerical values of the mTTD cut parameters (see Eq. 9) used to analyze central  $^{40}\text{Ar} + ^{45}\text{Sc}$  collisions at 13A–75A GeV/c. Particle pairs with momenta inside the ellipses are rejected

$p_{beam}$ (GeV/c)	TTD cut (cm)	$r_\rho$ (GeV/c) $^{-1}$	$r_{s_y}$	$r_{s_x}$	$r_{\rho s_x}$ (GeV/c) $^{-1}$	$r_{s_x \rho}$ (GeV/c) $^{-1}$	$\theta$
13A	3.5	0.470	0.004	0.047	0.470	0.004	5
19A	2.8	0.121	0.003	0.010	0.121	0.003	8
30A	2.8	0.123	0.002	0.013	0.123	0.002	13
40A	2.2	0.043	0.002	0.010	0.043	0.002	15
75A	2.2	0.080	0.002	0.011	0.020	0.002	31

frequently rejects overlapping clusters, and the tracks can be lost. Moreover, the TPC track reconstruction may fail to merge two track fragments. This can generate split tracks out of a single track.

The mixed data set is constructed by randomly swapping particles from different events so that each particle in each mixed event comes from different recorded events.

For each pair of particles in both recorded and mixed events, a two-track distance (TTD) is calculated. It is the average distance of their tracks in  $x$ - $y$  plane at eight different  $z$  planes ( $-506, -255, -201, -171, -125, 125, 352,$  and  $742$  cm). The TPC’s limitation in recognizing close tracks is illustrated in Fig. 5 (left) for  $^{40}\text{Ar} + ^{45}\text{Sc}$  collisions at 75A GeV/c. The data to mixed ratio is significantly below one for TTD less than  $\approx 2$  cm. The TTD cut values for each data set are listed in Table 2.

Calculating TTD requires knowledge of the NA61/SHINE detector geometry and magnetic field. Hence, it is restricted to the Collaboration members. Here, a momentum-based two-track distance (mTTD) cut is introduced.

The mTTD cut removes the remaining split tracks from the data after the potential point ratio cut (see Sect. 4.3), and it provides the precise definition of the biased region in which we do not have good efficiency for measuring two-tracks. Due to its momentum-based definition of the biased region, the mTTD cut can be used for model comparison of the experimental results without having access to the internal NA61/SHINE resources.

The magnetic field bends the trajectory of charged particles in the  $x$ - $z$  plane. Thus, it is most convenient to express the momentum of each particle in the following momentum coordinates:

$$\begin{aligned} s_x &= p_x/p_{xz} = \cos(\Psi), \\ s_y &= p_y/p_{xz} = \sin(\lambda), \\ \rho &= 1/p_{xz}, \end{aligned} \tag{7}$$

where  $p_{xz} = \sqrt{p_x^2 + p_z^2}$ .

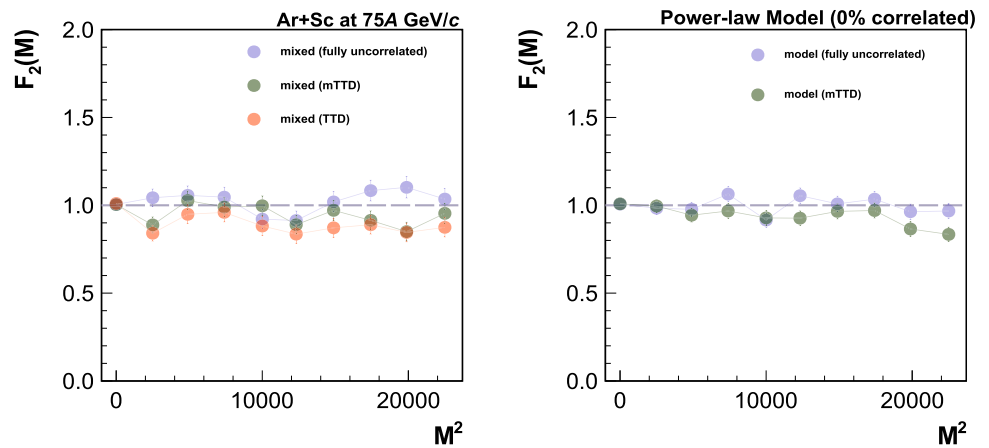
For each pair of particles, a difference in these coordinates is calculated as:

$$\begin{aligned} \Delta s_x &= s_{x,2} - s_{x,1}, \\ \Delta s_y &= s_{y,2} - s_{y,1}, \\ \Delta \rho &= \rho_2 - \rho_1. \end{aligned} \tag{8}$$

The distributions of particle pairs’ momentum difference for pairs with TTD less than  $\approx 2$  cm (as an example for Ar+Sc collisions at 75A GeV/c) are parameterized with ellipses in the new momentum coordinates. Such parameterized elliptical cuts are defined as:

$$\begin{aligned} \left(\frac{\Delta \rho}{r_\rho}\right)^2 + \left(\frac{\Delta s_y}{r_{s_y}}\right)^2 &\leq 1, \\ \left(\frac{\Delta s_x}{r_{s_x}}\right)^2 + \left(\frac{\Delta s_y}{r_{s_y}}\right)^2 &\leq 1, \end{aligned}$$

**Fig. 6** Example of the TTD or mTTD cut impact on mixed events for central  $^{40}\text{Ar} + ^{45}\text{Sc}$  collisions at 75 A GeV/c (left) and on the Power-law Model [19] with uncorrelated particles only (right). The blue circles correspond to the dependence of  $F_2(M)$  on  $M^2$  where neither TTD nor mTTD cut is applied to the mixed events or the Power-law Model. Green and red points correspond to either TTD or mTTD cut applied



**Table 3** Fraction of the total number of selected events used to calculate second-order scaled factorial moments for the chosen number of cumulative momentum cells

Number of cells $M^2$	$1^2$	$50^2$	$70^2$	$86^2$	$100^2$	$111^2$	$122^2$	$132^2$	$141^2$	$150^2$
Fraction of all events (%)	0.5	3.0	5.0	7.0	9.0	11.0	13.0	15.5	17.0	19.0

**Table 4** The  $\sigma_x$  and  $\sigma_y$  parameters, see text for details, used for smearing of proton transverse momentum in simulated  $^{40}\text{Ar} + ^{45}\text{Sc}$  collisions at 13A–75 A GeV/c

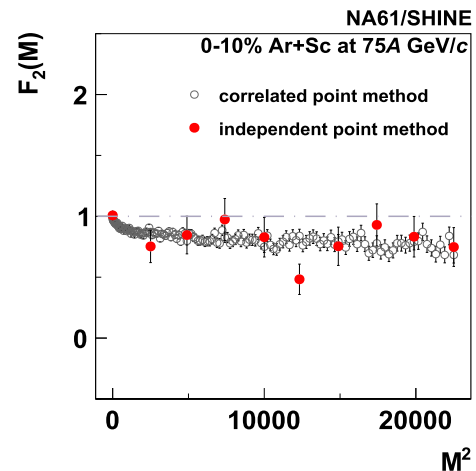
$p_{beam}$ (GeV/c)	$\sigma_x$ (MeV/c)	$\sigma_y$ (MeV/c)
13A	4.8	3.5
19A	4.6	3.4
30A	4.0	3.2
40A	3.5	3.1
75A	3.1	3.1

$$\left( \frac{\Delta\rho \cos\theta - \Delta s_x \sin\theta}{r_{\rho s_x}} \right)^2 + \left( \frac{\Delta\rho \sin\theta + \Delta s_x \cos\theta}{r_{s_x \rho}} \right)^2 \leq 1, \quad (9)$$

where  $r_{\rho s_x}$  and  $r_{s_x \rho}$  is the semi-major and semi-minor axis of an ellipse formed by  $\Delta\rho$  and  $\Delta s_x$ , and  $\theta$  is the angle from the positive horizontal axis to the ellipse's major axis.

Proton pairs with momenta difference inside the ellipses (Eq. 9) are rejected. The mTTD cut provides the precise definition of the biased region (see Fig. 5 right). The mTTD cut can replace the TTD cut. The parameters of the mTTD cut (see Eq. 9) are given in Table 2, and the mTTD cut is used as a two-particle acceptance map for the data analysis (see Sect. 5) and comparison with the models (see Sect. 6).

The effect of the mTTD cut for  $^{40}\text{Ar} + ^{45}\text{Sc}$  collisions at 75 A GeV/c mixed events, and the Power-law Model (see Sect. 6.2) is shown in Fig. 6. The dependence of  $F_2(M)$  on  $M^2$  in cumulative transverse momentum space for  $M^2 > 1$  is systematically below  $F_2(M = 1)$  when TTD or mTTD cut is applied to fully uncorrelated mixed events (left) and the Power-law Model with uncorrelated particles only (right).

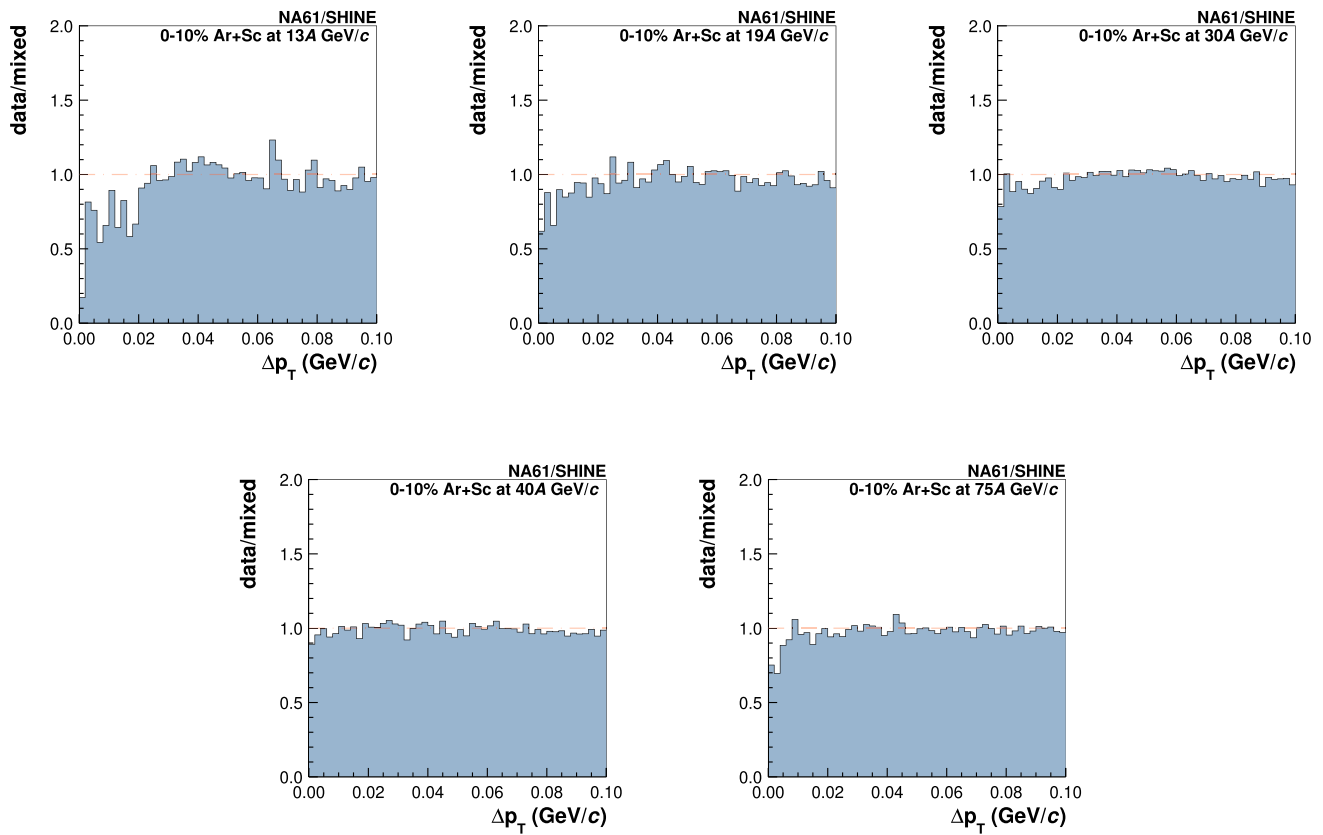


**Fig. 7** Example comparison of the independent and correlated point methods for 0–10% central  $^{40}\text{Ar} + ^{45}\text{Sc}$  collisions at 75 A GeV/c. Results on the dependence of the scaled factorial moment of the proton multiplicity distribution on the number of subdivisions in cumulative transverse momentum space  $M^2$  for  $1^2 \leq M^2 \leq 150^2$ . Open and closed circles represent the results obtained using correlated and independent point methods

#### 4.5 Statistically-independent data points

The intermittency analysis gives the dependence of scaled factorial moments on the number of subdivisions of transverse momentum or cumulative transverse momentum intervals. In the past intermittency analyses, the same data set was used to obtain results for each number of subdivisions. The results for different  $M^2$  were statistically correlated. Therefore, the full covariance matrix is required for proper statistical treatment of the results. A visual inspection of the plot with correlated points may lead to misleading conclusion as





**Fig. 8** Two-particle correlation functions in  $\Delta p_T$  for selected proton candidates within analysis acceptance for central  $^{40}\text{Ar} + ^{45}\text{Sc}$  collisions at 13A–75A GeV/c are shown. The data distribution includes the mTTD cut, whereas the mixed one does not

the correlation between points is not displayed. An example comparison of the independent and correlated point methods for 0–10% central  $^{40}\text{Ar} + ^{45}\text{Sc}$  collisions at 75A GeV/c is shown in Fig. 7.

In the independent point method, statistically independent data subsets were used to obtain results for different subdivision numbers. Consequently, the results for different subdivision numbers are statistically independent. Only the diagonal elements of the covariance matrix are non-zero, making the complete relevant information needed to interpret the results easy to present graphically and use in statistical tests.

The procedure decreases the number of events used to calculate each data point, increasing the statistical uncertainties of individual points and thereby necessitating a reduction in the number of data points. The number of events used in each subset was selected to obtain similar statistical uncertainties for different subsets. Table 3 presents the fractions of all selected events used to calculate each of the 10 points.

#### 4.6 Uncertainties and biases

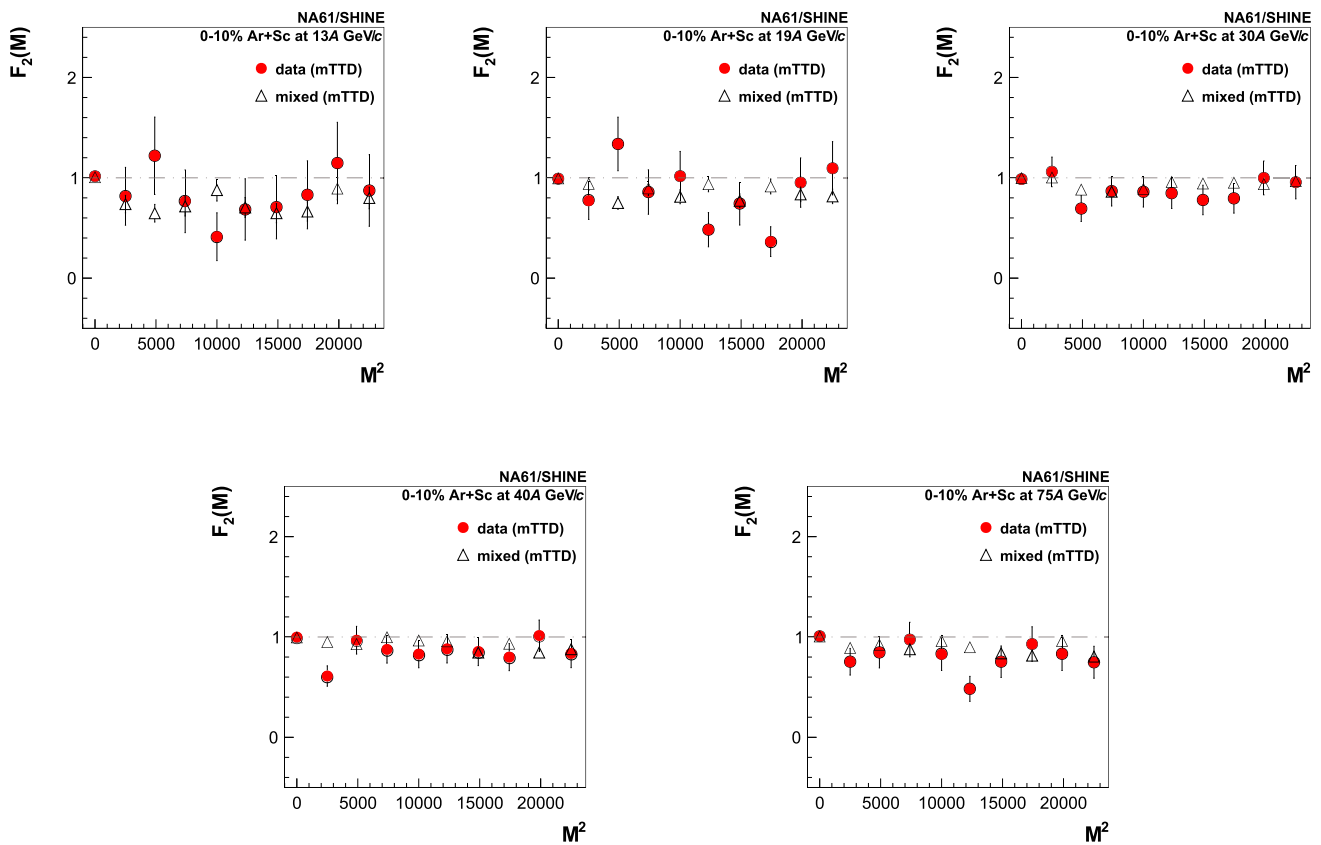
The standard expression for the scaled factorial moments, Eq. 1 can be rewritten as

$$F_2(M) = 2M^2 \frac{\langle N_2(M) \rangle}{\langle N \rangle^2}, \tag{10}$$

where  $N_2(M)$  denotes a total number of particle pairs in  $M^2$  bins in an event. Then the statistical uncertainties can be calculated using the standard error propagation:

$$\frac{\sigma_{F_2}}{|F_2|} = \sqrt{\frac{(\sigma_{N_2})^2}{\langle N_2 \rangle^2} + 4 \frac{(\sigma_N)^2}{\langle N \rangle^2} - 4 \frac{(\sigma_{N_2 N})^2}{\langle N \rangle \langle N_2 \rangle}}. \tag{11}$$

The final results presented in Sect. 5 are not corrected for possible biases. Their magnitude was estimated by comparing results for pure EPOS1.99 [48] and EPOS1.99 subjected to



**Fig. 9** Results on the dependence of the scaled factorial moment of proton multiplicity distribution on the number of subdivisions in cumulative transverse momentum space  $M^2$  for  $1^2 \leq M^2 \leq 150^2$ . Results are shown for 0–10% central  $^{40}\text{Ar} + ^{45}\text{Sc}$  collisions at 13A–75A GeV/c.

Closed red circles indicate the experimental data. Corresponding results for mixed events (open triangles) are also shown. Both the data and mixed events include the mTTD cut. Only statistical uncertainties are indicated

the detector simulation, reconstruction, and data-like analysis. Figure 15 shows the comparison for  $^{40}\text{Ar} + ^{45}\text{Sc}$  collisions at 13A–75A GeV/c. Their differences are significantly smaller than the statistical uncertainties of the experimental data and increase with  $M^2$  up to about 0.1 at large  $M^2$  values. Note that protons generated by EPOS1.99 do not show a significant correlation in the transverse momentum space, see Sect. 6. In this case, the momentum resolution does not affect the results significantly.

In the case of the critical correlations, the impact of the momentum resolution may be significant, see Ref. [49] and Sect. 6 for detail. Thus a comparison with models including short-range correlations in the transverse momentum space requires smearing of momenta according to the experimental resolution, which can be approximately parameterized as:

$$\begin{aligned} p_x^{\text{smearred}} &= p_x^{\text{original}} + \delta p_x \quad \text{and} \\ p_y^{\text{smearred}} &= p_y^{\text{original}} + \delta p_y, \end{aligned} \quad (12)$$

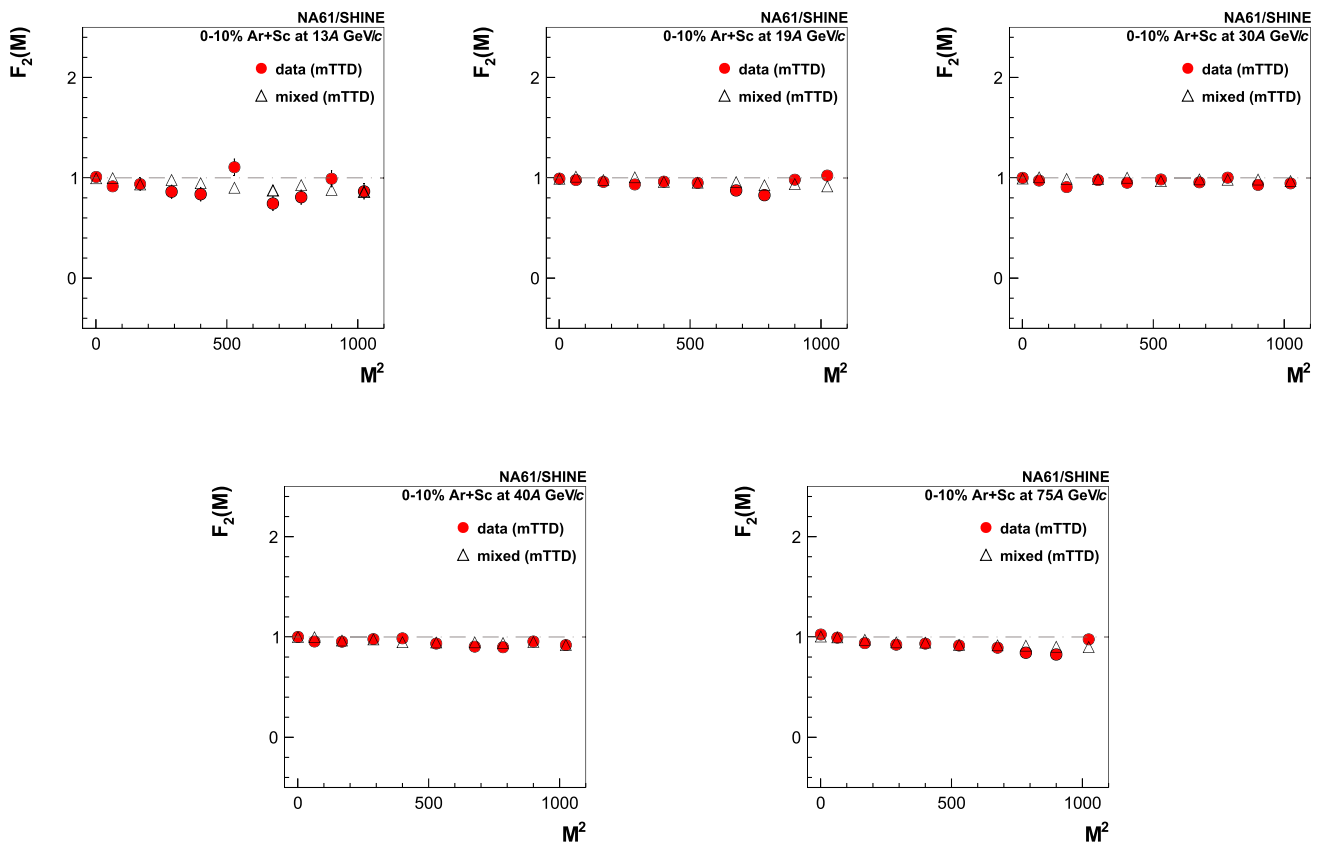
where  $\delta p_x$  and  $\delta p_y$  are randomly drawn from a Gaussian distribution with  $\sigma_x$  and  $\sigma_y$  values for central  $^{40}\text{Ar} + ^{45}\text{Sc}$  collisions at 13A–75A GeV/c from the Table 4.

Uncertainties on the final results presented in Sect. 5 correspond to statistical uncertainties.

## 5 Results

This section presents results on second-order scaled factorial moments (Eq. 1) of  $\approx 60\%$  randomly selected protons (losses due to proton misidentification) with momentum smeared due to reconstruction resolution (Eq. 12) produced within the acceptance maps defined in Sect. 4.4 by strong and electromagnetic processes in 0–10% central  $^{40}\text{Ar} + ^{45}\text{Sc}$  interactions at 13A–75A GeV/c. The results are shown as a function of the number of subdivisions in transverse momentum space – the so-called intermittency analysis. The analysis was performed for cumulative and original transverse momentum components. Independent data subsets were used to calculate the results for each subdivision.

Uncertainties correspond to statistical ones. Biases estimated using the EPOS1.99 [50] model (see Sect. 6) are signifi-



**Fig. 10** Results on the dependence of the scaled factorial moment of proton multiplicity distribution on the number of subdivisions in cumulative transverse momentum space  $M^2$  for  $1^2 \leq M^2 \leq 32^2$ . Results are shown for 0–10% central  $^{40}\text{Ar} + ^{45}\text{Sc}$  collisions at 13A–75A GeV/c.

Closed red circles indicate the experimental data. Corresponding results for mixed events (open triangles) are also shown. Both the data and mixed events include the mTTD cut. Only statistical uncertainties are indicated

icantly smaller than the statistical uncertainties of the experimental data.

### 5.1 Two-particle correlation function

The two-particle correlation function,  $\Delta p_T$ , of selected proton candidates within the analysis acceptance for central  $^{40}\text{Ar} + ^{45}\text{Sc}$  collisions at 13A–75A GeV/c is shown in Fig. 8. The correlation function is the ratio of normalized  $\Delta p_T$  distributions for data and mixed events. The data distribution includes the mTTD cut, whereas the mixed one does not. The decrease of the correlation function at  $\Delta p_T \approx 0$  is due to anti-correlation introduced by the mTTD cut.

### 5.2 Subdivisions in cumulative transverse momentum space

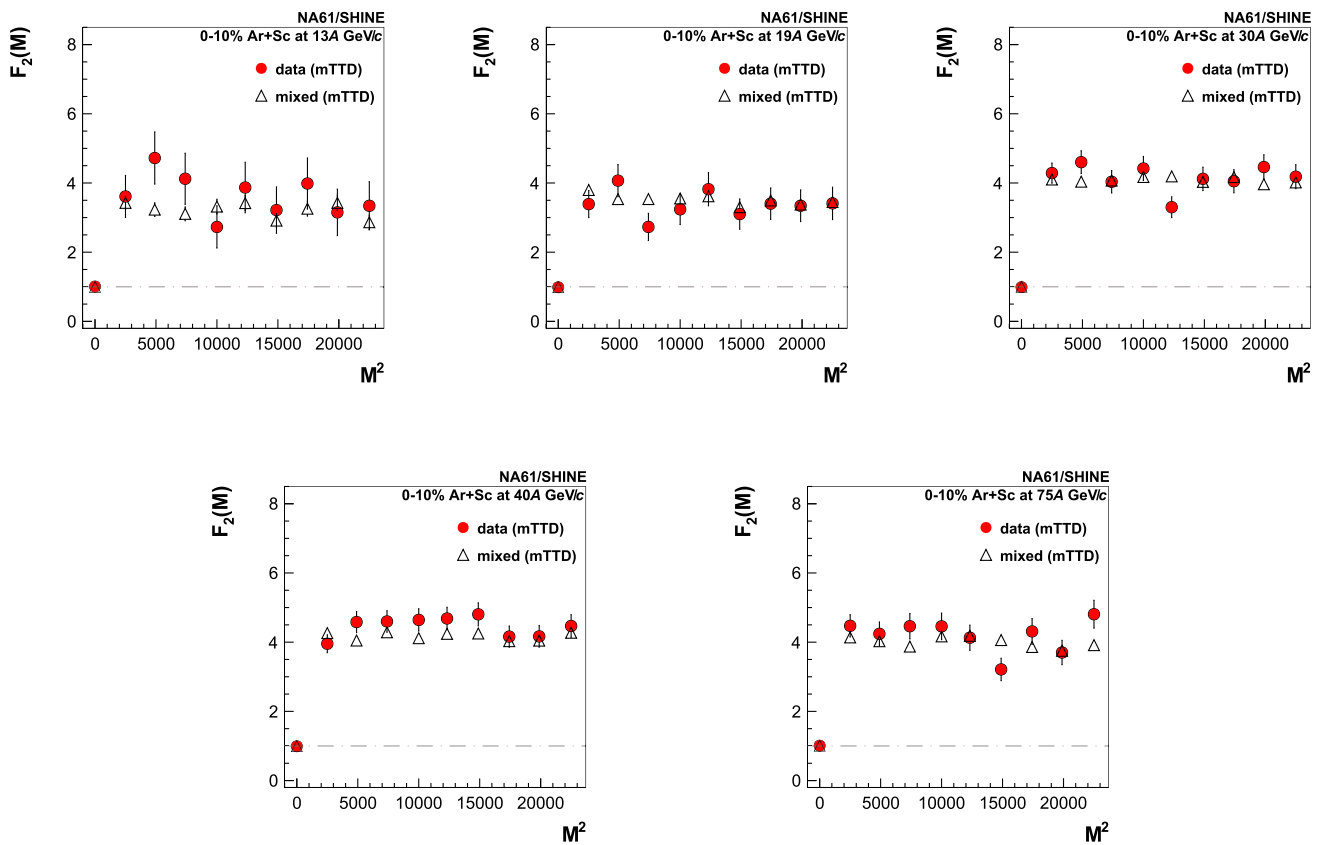
Figures 9 and 10 present the dependence of the factorial moment on the number of subdivisions in cumulative-transverse momentum space for the maximum subdivision

number of  $M = 150$  and  $M = 32$ , respectively. The latter, coarse subdivision, was introduced to limit the effect of experimental momentum resolution; see Ref. [49] and below for details. The experimental results are shown for 0–10% central  $^{40}\text{Ar} + ^{45}\text{Sc}$  collisions at 13A–75A GeV/c. As a reference, the corresponding results for mixed events are also shown.

By construction, the multiplicity distribution of protons in mixed events for  $M = 1$  equals the corresponding distribution for the data. In mixed events, the only correlation of particles in the transverse momentum space is due to the mTTD cut. Both the data and mixed events include the mTTD cut. The mTTD cut is necessary to properly account for the detector resolution – losses of close-in-space tracks.

The results for subdivisions in cumulative transverse momentum space,  $F_2(M)$  for  $M > 1$  are systematically below  $F_2(M = 1)$ . It is likely due to the anti-correlation generated by the mTTD cut to the data (see Sect. 4.4.2 for details).

$$\Delta p_T = \sqrt{(p_{x1} - p_{x2})^2 + (p_{y1} - p_{y2})^2}$$



**Fig. 11** Results on the dependence of the scaled factorial moment of proton multiplicity distribution on the number of subdivisions in transverse momentum space  $M^2$  for  $1^2 \leq M^2 \leq 150^2$ . Results are shown for 0–10% central  $^{40}\text{Ar} + ^{45}\text{Sc}$  collisions at 13A–75A GeV/c. Closed red

circles indicate the experimental data. Corresponding results for mixed events (open triangles) are also shown. Both the data and mixed events include the mTTD cut. Only statistical uncertainties are indicated

The experimental results show no increase of  $F_2(M)$  with  $M^2$ . There is no indication of the critical fluctuations for selected proton candidates.

mixed events with the mTTD cut on  $M^2$  ( $\Delta F_2(M) \approx 0$ ). There is no indication of the critical fluctuations for selected protons.

### 5.3 Subdivisions in transverse momentum space

Figures 11 and 13 present the results which correspond to the results shown in Figs. 9, and 10 but subdivisions are done in the transverse momentum space. By construction,  $F_2(1)$  values are equal for subdivisions in cumulative transverse-momentum space and transverse-momentum space. But for the latter,  $F_2(M)$  rapidly increases from the value  $F_2(M = 1)$  to approximate plateau at  $M \approx 20$ . This dependence is primarily due to the non-uniform shape of the single-particle transverse momentum distributions, see Sect. 2.2. It can be accounted for by comparing the experimental data results with those obtained for the mixed events using  $\Delta F_2(M)$ . The dependence of  $\Delta F_2(M)$  on the number of subdivisions,  $M^2$  are shown in Figs. 12 and 14 for fine and coarse binning.

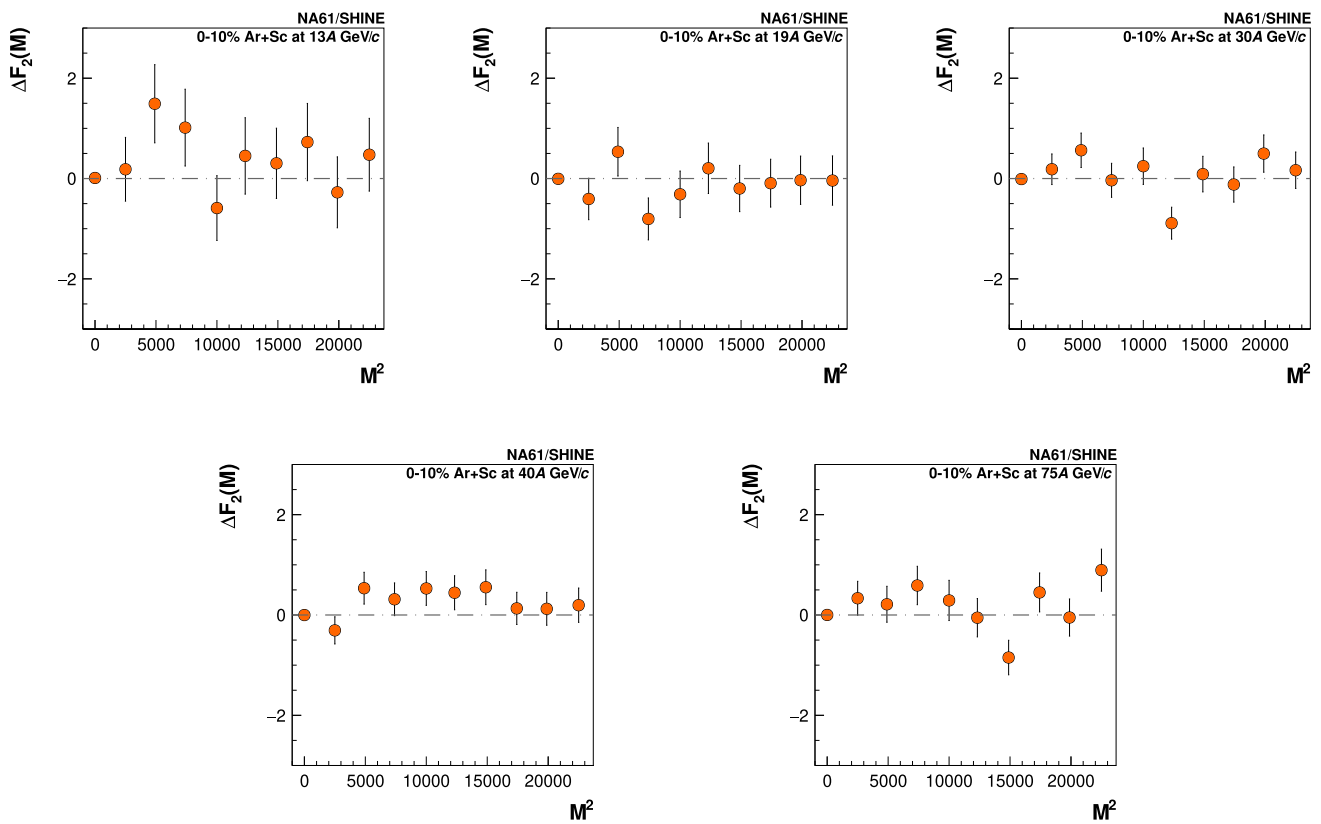
The experimental results presented in Figs. 11, 12, 13 and 14 do not show any significant difference to the results for

## 6 Comparison with models

This section presents a comparison of the experimental results with two models. The first one, EPOS1.99 [50], takes into account numerous sources of particle correlations, in particular, conservation laws and resonance decays, but without critical fluctuations. The second one, the Power-law Model [51], produces pairs of particles correlated by the power law inside the pair and fully uncorrelated particles.

### 6.1 EPOS

Minimum bias  $^{40}\text{Ar} + ^{45}\text{Sc}$  events have been generated with EPOS1.99 for comparison. Signals from the NA61/SHINE detector were simulated with GEANT3 software, and the



**Fig. 12** Results on the dependence of  $\Delta F_2(M)$  of proton multiplicity distribution on the number of subdivisions in transverse momentum space  $M^2$  for  $1^2 \leq M^2 \leq 150^2$ . Results for 0–10% central  $^{40}\text{Ar} + ^{45}\text{Sc}$

collisions at 13A–75A GeV/c are shown. Both the data and mixed events include the mTTD cut. Only statistical uncertainties are indicated

generated events were reconstructed using the standard NA61/SHINE procedure.

The number of forward spectators is used to select central EPOS1.99 events of  $^{40}\text{Ar} + ^{45}\text{Sc}$  collisions at 13A–75A GeV/c. To calculate model predictions (pure EPOS), 0–10% most central collisions were analyzed. Protons and proton pairs within the single-particle and two-particle acceptance maps were selected. Moreover, 60% of accepted protons were randomly selected for the analysis to account for the limited proton identification in the experiment (see Fig. 4).

Results for the reconstructed EPOS events were obtained as follows. The model events were required to have the reconstructed primary vertex. Selected protons and proton pairs (matching the generated particles used for identification) were subjected to the same cuts as used for the experimental data analysis (see Sect. 4). The results for the pure and the reconstructed EPOS events are compared in Fig. 15 for central  $^{40}\text{Ar} + ^{45}\text{Sc}$  collisions at 13A–75A GeV/c. One concludes that for the EPOS-like physics, the experimental biases are smaller than the statistical uncertainties of the data.

Finally, the experimental results are compared with the pure EPOS predictions for central  $^{40}\text{Ar} + ^{45}\text{Sc}$  collisions at

13A–75A GeV/c and are shown in Fig. 16. No significant differences are found.

### 6.2 Power-law model

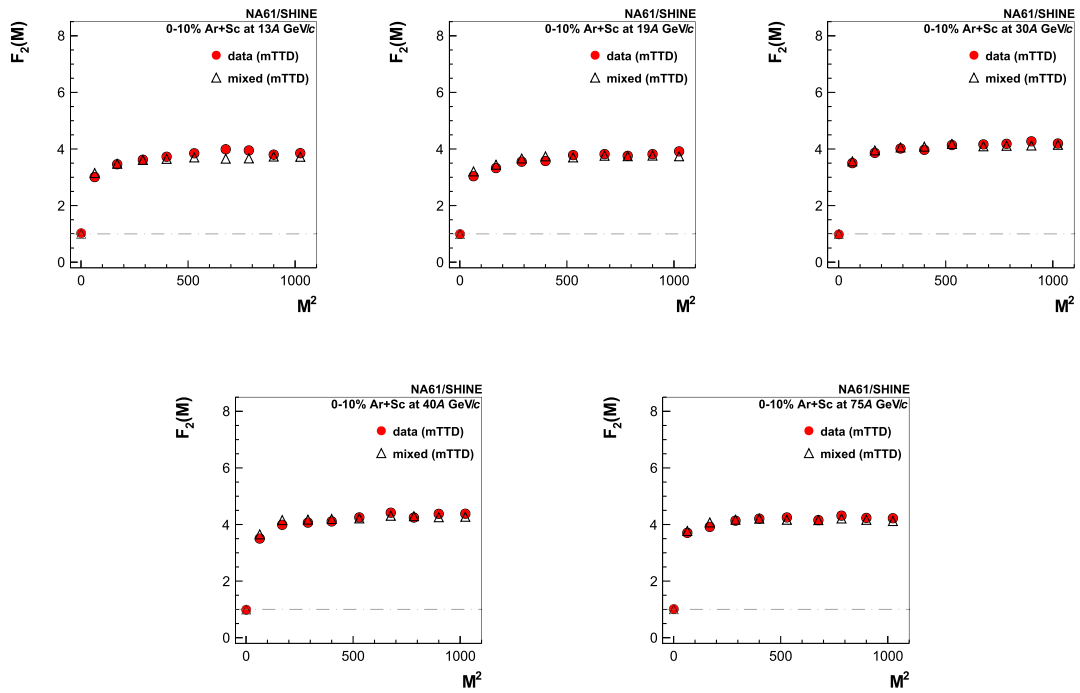
Inspired by expectations of the power-law correlations between particles near the critical point [3], the Power-law model [19] was developed to compare with the experimental result.

It generates momenta of uncorrelated and correlated protons with a given single-particle transverse momentum distribution in events with a given multiplicity distribution. The correlated protons are produced in pairs, and their correlation inside the pair is given the power law as described in Ref. [19]. The model has two controllable parameters:

- (i) fraction of correlated particles,  $r$ ,
- (ii) strength of the correlation (the power-law exponent),  $\phi$ .

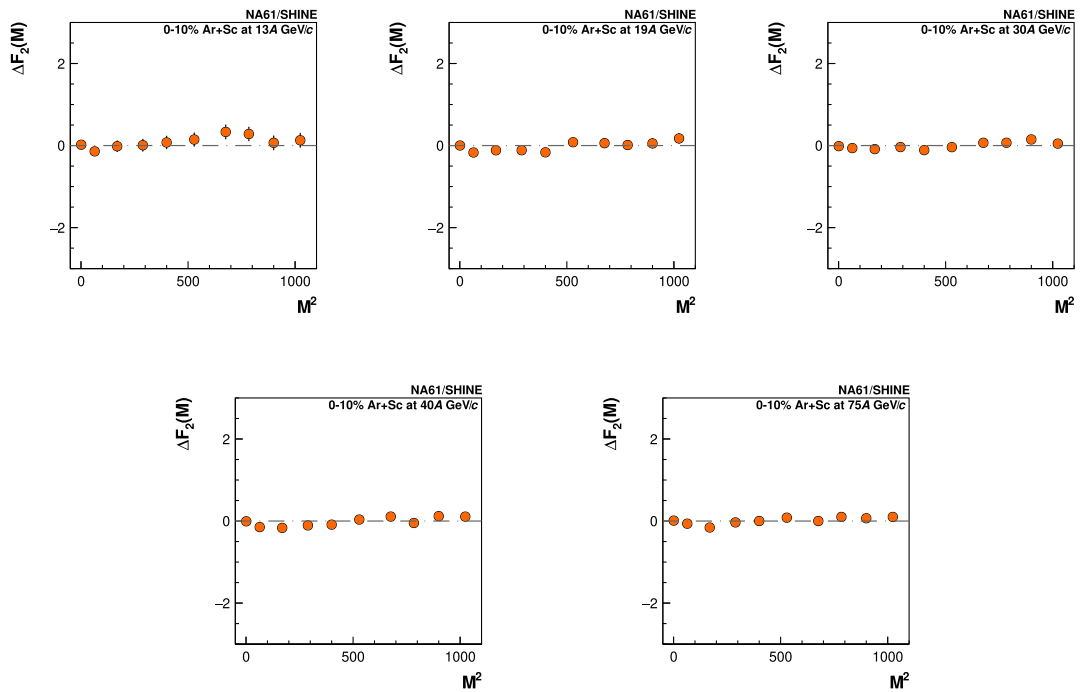
The transverse momentum of particles is drawn from the input transverse momentum distribution. Correlated-particle pairs' transverse momentum difference follows a power-law





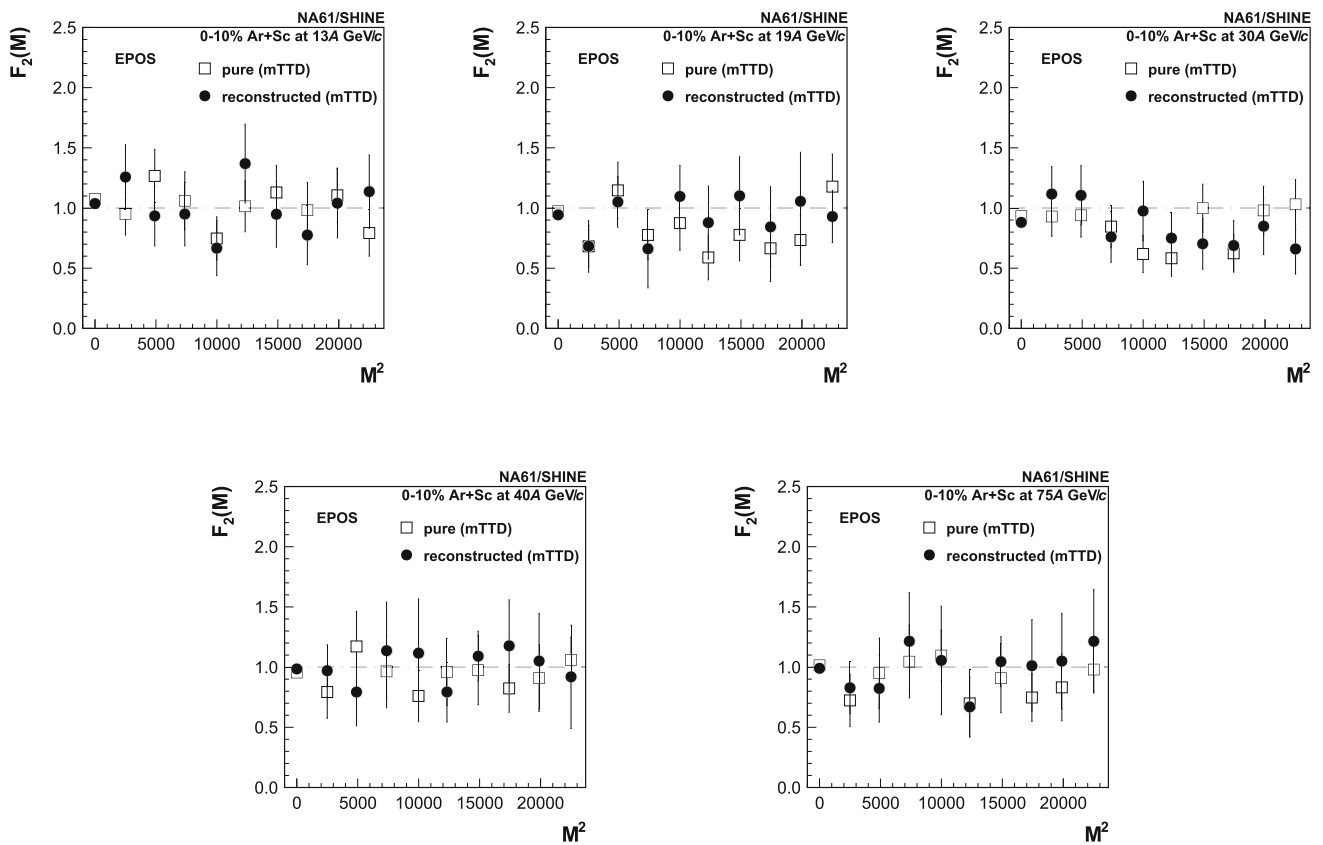
**Fig. 13** Results on the dependence of the scaled factorial moment of proton multiplicity distribution on the number of subdivisions in transverse momentum space  $M^2$  for  $1^2 \leq M^2 \leq 32^2$ . Results are shown for 0–10% central  $^{40}\text{Ar} + ^{45}\text{Sc}$  collisions at 13A–75A GeV/c. Closed red

circles indicate the experimental data. Corresponding results for mixed events (open triangles) are also shown. Both the data and mixed events include the mTTD cut. Only statistical uncertainties are indicated



**Fig. 14** Results on the dependence of  $\Delta F_2(M)$  of proton multiplicity distribution on the number of subdivisions in transverse momentum space  $M^2$  for  $1^2 \leq M^2 \leq 32^2$ . Results for 0–10% central  $^{40}\text{Ar} + ^{45}\text{Sc}$

collisions at 13A–75A GeV/c are shown. Both the data and mixed events include the mTTD cut. Only statistical uncertainties are indicated



**Fig. 15** Results on the dependence of the scaled factorial moment of proton multiplicity distribution on the number of subdivisions in cumulative transverse momentum space,  $M^2$  for  $1^2 \leq M^2 \leq 150^2$ , for events generated with EPOS1.99. Results are shown for 0–10% central

$^{40}\text{Ar} + ^{45}\text{Sc}$  collisions at 13A–75A GeV/c. Closed black circles represent reconstructed EPOS, and open rectangles indicate pure (smeared) EPOS. Both pure and reconstructed EPOS include the mTTD cut. Only statistical uncertainties are indicated

distribution:

$$\rho(|\Delta\vec{p}_T|) \sim |\Delta\vec{p}_T|^{-\phi}, \tag{13}$$

where the exponent  $0 \leq \phi < 1$ . For  $r = 0$ , the Power-law model results correspond to the mixed event results. The exponent  $\phi$  is related to the intermittency index  $\varphi_2$  as:

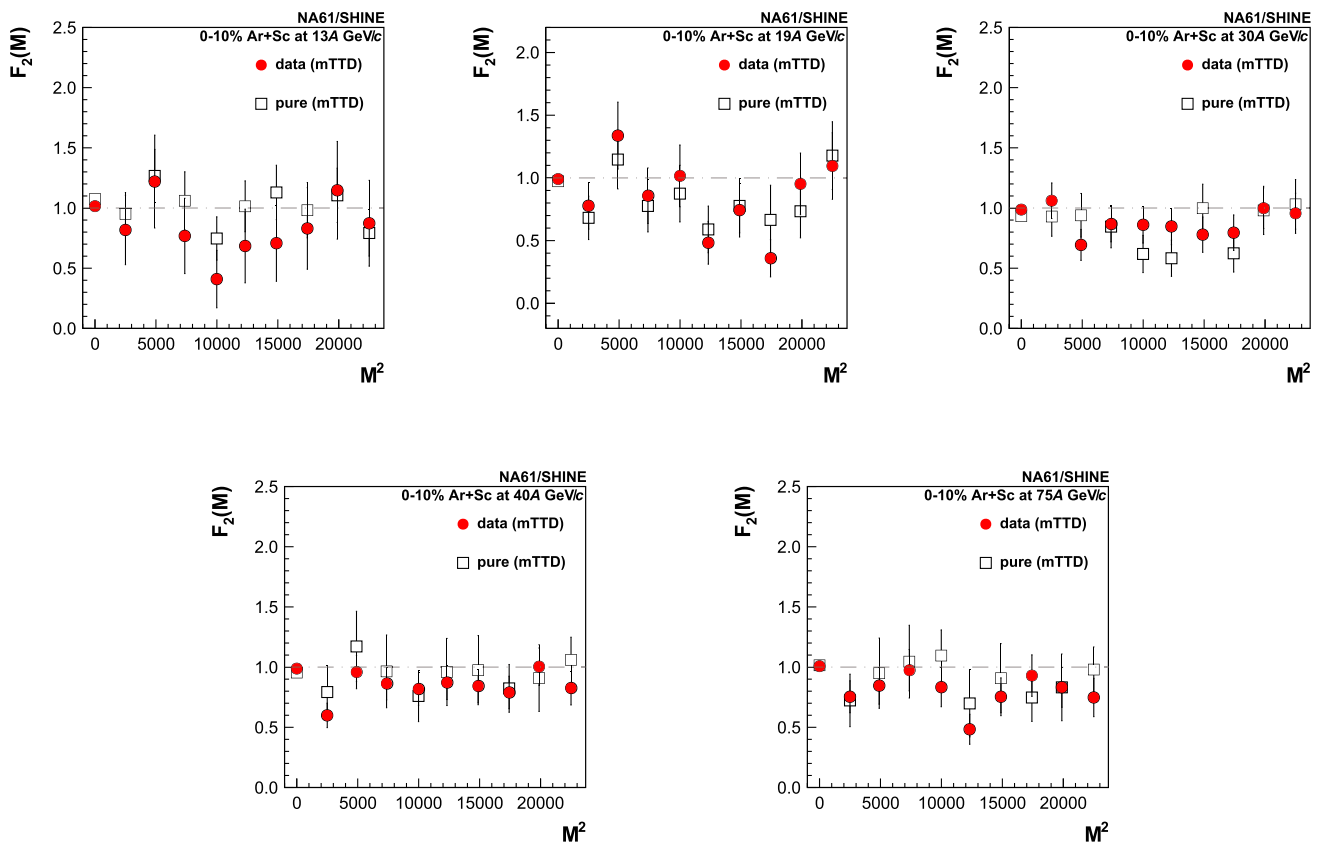
$$\varphi_2 \approx \frac{\phi + 1}{2}. \tag{14}$$

Azimuthal angle distribution is assumed to be uniform. The momentum component along the beamline,  $p_z$ , is calculated assuming a uniform rapidity distribution from 0 to 0.75 and proton mass.

Many high-statistics data sets have been produced using the Power-law Model with multiplicity and inclusive transverse momentum distributions taken from experimental data. Each data set has a different fraction of correlated particles (varying from 0 to 2%) and a different power-law exponent (varying from 0.00 to 0.95). The following effects have been included:

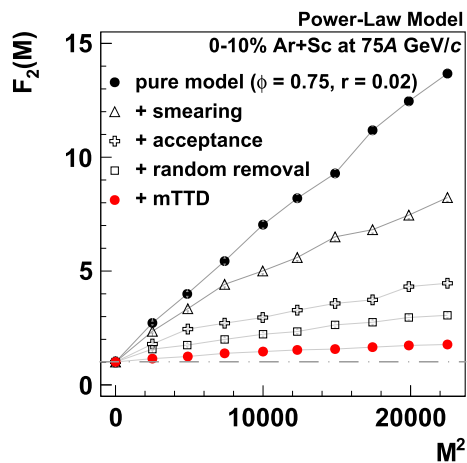
- (i) Gaussian smearing of momentum components to mimic reconstruction resolution of the momentum (see Eq. 12),
- (ii) single-particle acceptance map (see Sect. 4.4),
- (iii) two-particle acceptance map (see Sect. 4.4.2),
- (iv) random exchange of 40% of correlated particles with uncorrelated ones to simulate 60% acceptance of protons (preserves the desired multiplicity distribution but requires generating more correlated pairs at the beginning) (see Sect. 4.3.1).

In Fig. 17, experimental effects are successively included and their impact on the pure model result is shown for the Power-law model parameters,  $r = 0.02$  and  $\phi = 0.75$ . The multiplicity and transverse momentum of particles, and experimental effects (such as smearing, acceptance, random removal, and mTTD) are taken from 0–10% central  $^{40}\text{Ar} + ^{45}\text{Sc}$  collisions at 75A GeV/c and incorporated into the pure model data sets. If experimental effects are included separately then the pure model results decrease by 38%, 72%, 50%, and 11% by smearing, acceptance, random removal, and the mTTD effect, respectively.



**Fig. 16** Results on the dependence of the scaled factorial moment of proton multiplicity distribution on the number of subdivisions in cumulative transverse momentum space  $M^2$  for  $1^2 \leq M^2 \leq 150^2$ . Closed red circles indicate the experimental data. Corresponding results for

the EPOS1.99 model (open squares) were also shown for comparison. Results are shown for 0–10% central  $^{40}\text{Ar} + ^{45}\text{Sc}$  collisions at 13A–75A GeV/c. Results for data and EPOS were obtained using the mTTD cut. Only statistical uncertainties are indicated



**Fig. 17** Dependence of the scaled factorial moment on the number of subdivisions in the cumulative transverse momentum for the Power-law model with the power-law exponent set to 0.75 and fraction of correlated particles to 2%. Each line presents a result with a different effect included successively in the pure model data tuned for 0–10% central  $^{40}\text{Ar} + ^{45}\text{Sc}$  collisions at 75A GeV/c

Next, all generated data sets with all the above effects included have been analyzed the same way as the experimental data. Obtained  $F_2(M)$  results have been compared with the corresponding experimental results and  $\chi^2$  and a  $p$  value were calculated. Statistical uncertainties from the model with similar statistics to the data were used for the calculation. Examples of such comparisons for central  $^{40}\text{Ar} + ^{45}\text{Sc}$  collisions at 75A GeV/c are presented in Fig. 18.

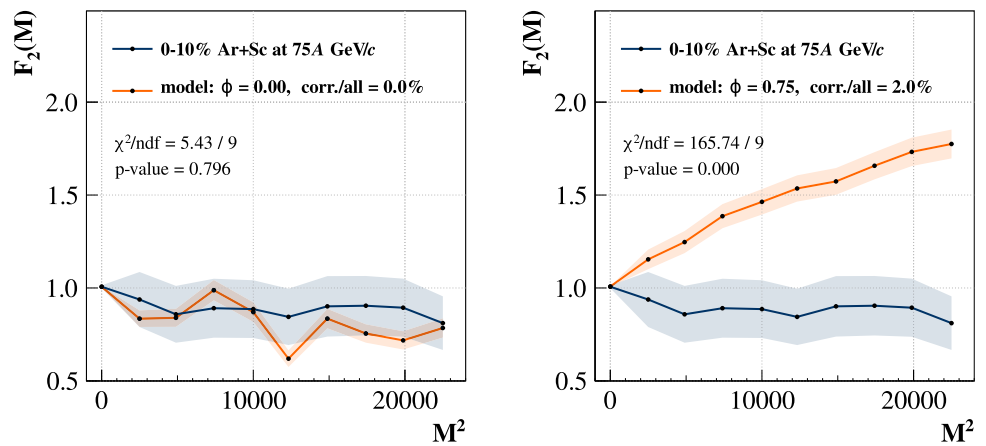
Figure 19 shows obtained exclusion plots as a function of the fraction of correlated protons and the intermittency index (calculated from power-law exponent) for central  $^{40}\text{Ar} + ^{45}\text{Sc}$  collisions at 13A–75A GeV/c and 150A GeV/c.

White areas above the line correspond to a  $p$  value of less than 5% and may be considered excluded (for this particular model). Fluctuations of the exclusion lines in Fig. 19 are due to limited statistics of the experimental data.

Results for the coarse subdivision have low statistical uncertainties (see Fig. 10), thus small deviations from the

Note, that in the previously published paper on  $^{40}\text{Ar} + ^{45}\text{Sc}$  at 150A GeV/c [9], the same notation was used for intermittency index ( $\varphi_2$ ) and power-law exponent ( $\phi$ ).

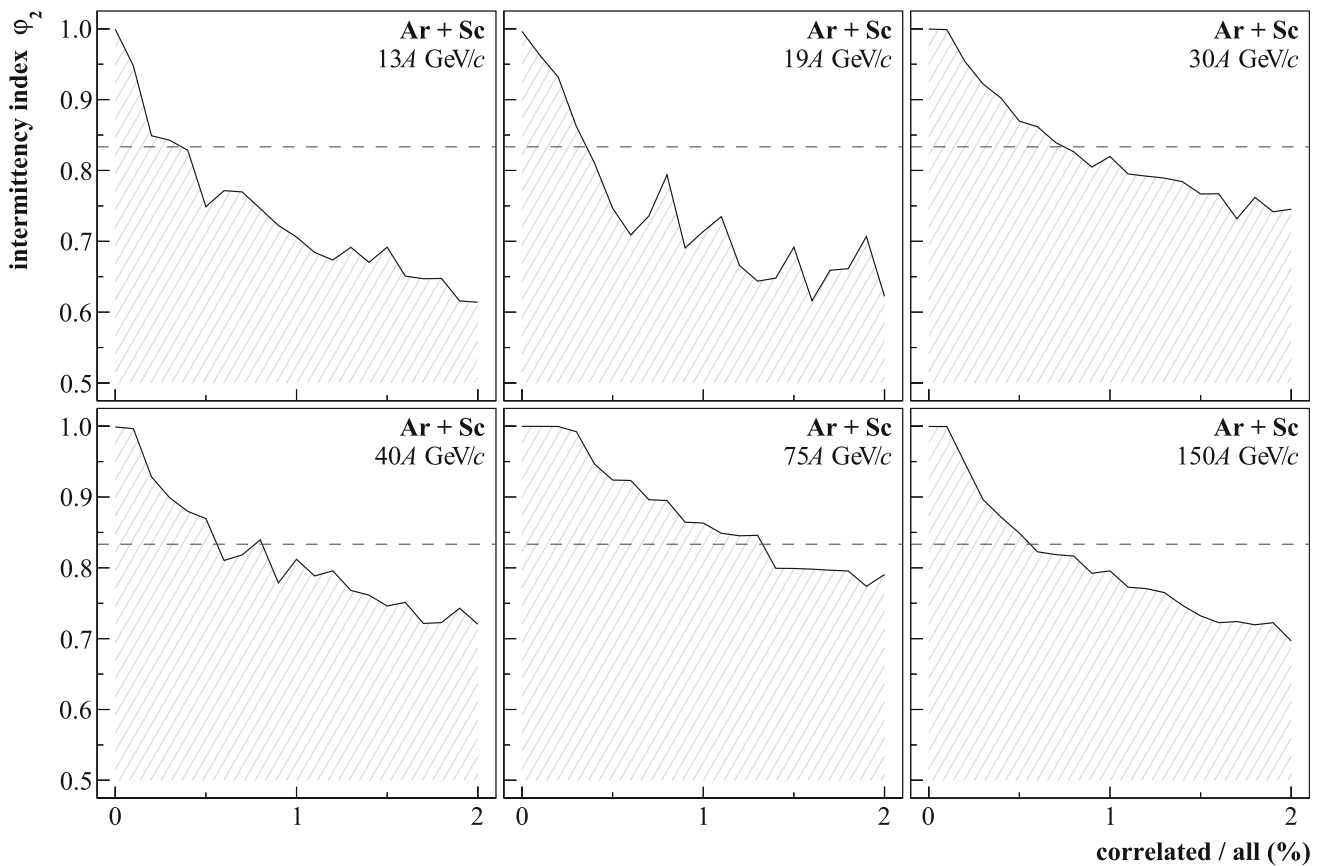
**Fig. 18** Examples of comparison of results for two Power-law Model data sets with the experimental data for central  $^{40}\text{Ar} + ^{45}\text{Sc}$  collisions at 75A GeV/c. The left panel includes model predictions assuming only uncorrelated protons, whereas the right one shows predictions for 2.0% of correlated protons with power-law exponent  $\phi = 0.75$



behavior expected for uncorrelated particle production due to non-critical correlations (conservation laws, resonance decays, quantum statistics, and others), as well as possible experimental biases, may lead to a significant decrease of the  $p$ -values. Thus, exclusion plots for the coarse subdivisions were not calculated.

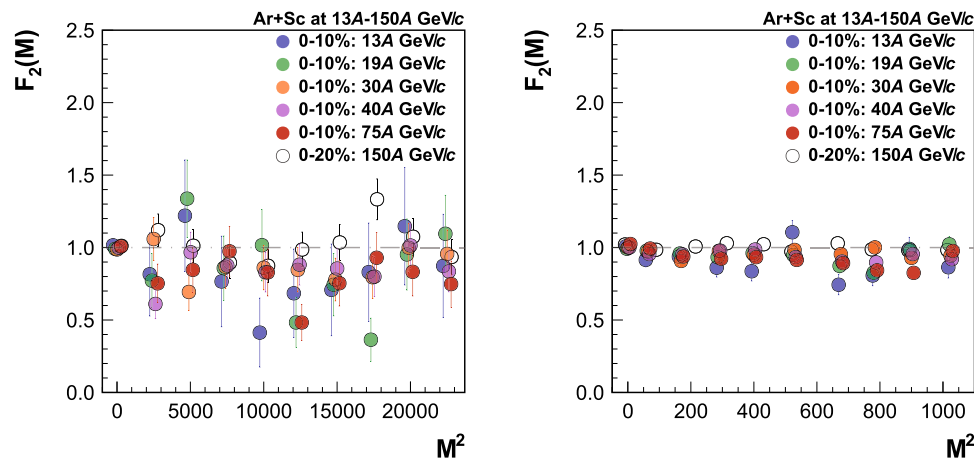
The intermittency index  $\varphi_2$  for an infinite system at QCD critical point is expected to be  $\varphi_2 = 5/6$  [3], assuming that the

latter belongs to the 3D-Ising universality class. If this value is set as the power-law exponent of the Power-law model with fine subdivisions (see Fig. 19), for the NA61/SHINE data on 0–10% central  $^{40}\text{Ar} + ^{45}\text{Sc}$  collisions at 13A–75A GeV/c, an upper limit on the fraction of correlated protons of the order of 1% is suggested by the data. It should be underlined that these numbers are specific to the Power-law Model. Analyses made with other models, which could provide different



**Fig. 19** Exclusion plots for the Power-law model [19] parameters – the fraction of correlated protons and the power-law exponent for central  $^{40}\text{Ar} + ^{45}\text{Sc}$  collisions at 13A–75A GeV/c and 150A GeV/c. The white

areas above the line correspond to  $p$  values less than 5%. The exclusion plots were obtained using data (see Fig. 9) for the fine subdivisions ( $1^2 \leq M^2 \leq 150^2$ )



**Fig. 20** Summary of the proton intermittency results from the NA61/SHINE Ar+Sc energy scan. Results on the dependence of the scaled factorial moment of proton multiplicity distribution on the number of subdivisions in cumulative transverse momentum space  $M^2$  for  $1^2 \leq M^2 \leq 150^2$  (left) and  $1^2 \leq M^2 \leq 32^2$  (right) are shown. The

open circles represent results on 0–20% central  $^{40}\text{Ar} + ^{45}\text{Sc}$  collisions at 150A GeV/c [9]. Closed circles indicate the experimental data results obtained within this work for 0–10% central  $^{40}\text{Ar} + ^{45}\text{Sc}$  collisions at 13A, 19A, 30A, 40A, and 75A GeV/c. Points for different energies are slightly shifted in horizontal axis to increase readability

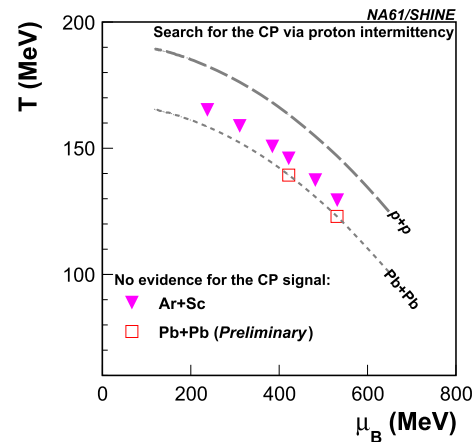
values depending on the assumed scenarios, remain beyond the scope of this paper.

## 7 Summary

This paper reports on the search for the critical point of strongly interacting matter in central  $^{40}\text{Ar} + ^{45}\text{Sc}$  collisions at beam momenta of 13A, 19A, 30A, 40A, and 75A GeV/c. Results on second-order scaled factorial moments of proton multiplicity distribution at mid-rapidity are presented. Protons produced in strong and electromagnetic processes in  $^{40}\text{Ar} + ^{45}\text{Sc}$  interactions and selected by the single- and two-particle acceptance maps, as well as the identification cuts, are used.

The scaled factorial moments are shown as a function of the number of subdivisions of transverse momentum space – the so-called intermittency analysis. The analysis was performed for cumulative and non-cumulative transverse momentum components. Independent data sets were used to calculate results for each subdivision. The influence of several experimental effects was discussed and quantified. The results show no intermittency signal. A summary of the proton intermittency from the Ar+Sc energy scan results is shown in Fig. 20. The experimental data are consistent with the mixed events and the EPOS model predictions.

The key physics result of this article is the absence of an intermittency signal, which implies there are no prominent structures of the QCD critical point observed in 0–10% central  $^{40}\text{Ar} + ^{45}\text{Sc}$  collisions at 13A, 19A, 30A, 40A, and 75A GeV/c via proton intermittency analysis. The ongoing critical point search studies via proton intermittency are sum-



**Fig. 21** Diagram of chemical freeze-out temperature and baryon-chemical potential. The dashed line indicates parameters in  $p+p$  interactions and the dotted line in the central Pb+Pb collisions; points estimated and extrapolated ( $\mu_B$  for  $p+p$ ) based on Ref. [52]. The colored points mark reactions (Ar+Sc and Pb+Pb [53]) in the  $T - \mu_B$  phase diagram for which the search for the critical point was conducted, and no evidence for the critical point was found

marized on the diagram of chemical freeze-out temperature and chemical potential (estimated based on Ref. [52]) and shown in Fig. 21. An upper limit on the fraction of correlated protons of the order of 1% is suggested by the data based on a comparison with the Power-law model [19].

The intermittency analysis of other reactions recorded within the NA61/SHINE program on strong interactions is well advanced, and new results should be expected soon.



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