

Implementing a System Generation Aware Unified Conceptual Model

Bachelor's Thesis of

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Zusammenfassung

Kunden erwarten heutzutage hochkonfigurierbare Produkte, die mit Hilfe von Produktlinien entwickelt werden können. Produktlinien beschreiben verschiedene Produktvarianten und Versionen dieser Varianten und drücken damit die Variabilität im Raum durch Varianten und die Variabilität in der Zeit durch Versionen aus. Eine Produktlinie kann in einen Problemraum, der die fur die Nutzer sichtbaren ¨ Eigenschaften oder Verhaltensweisen eines Produktes, die sogenannten Features, und deren Abhängigkeiten beschreibt, und einen Lösungsraum, der die Realisierungsartefakte darstellt, unterteilt werden. Der Stand der Technik lässt folgende ungelöste Herausforderungen erkennen: das Fehlen einer Validierung und Prufung der Re- ¨ alisierbarkeit von Varianten im Zeitverlauf sowie das Fehlen eines einzigen Instruments, das eine Lösung für diese Herausforderung bietet und zudem mit etablierten Werkzeugen kompatibel ist. In dieser Arbeit gehen wir die beschriebenen Herausforderungen an, indem wir ein bestehendes Metamodell, das Unified Conceptual Model [\(UCM\)](#page-14-0), erweitern. Dafür bieten wir eine Implementierung des [UCM](#page-14-0) an, die wir durch die Integration bestehender Konzepte zum Ausdruck von Variabilität im Raum erweitern, um unsere Implementierung an bekannte Werkzeuge, wie FeatureIDE, anzupassen. Wir integrieren auch die Konzepte der Deltamodellierung, um den Unterschied zwischen zwei Versionen im [UCM](#page-14-0) zu beschreiben, und wir verwenden das Modell der System Generation Engineering [\(SGE\)](#page-14-1)-Variationsarten, um Anderungen für die weitere Analyse mit Nominaltypen zu kategorisieren. Wir zeigen die Anwendbarkeit unserer Implementierung, indem wir eine Realisierungsanalyse an einer Erweiterung der bekannten Body Comfort System [\(BCS\)](#page-14-2) Case Study durchfuhren. Wir verwenden das erweiterte [BCS,](#page-14-2) um zu zeigen, dass wir die ¨ [SGE-](#page-14-1)Variationsarten auf ein domänenübergreifendes Produktline anwenden können, und zeigen, dass unsere [UCM-](#page-14-0)Implementierung den semantischen Unterschied zwischen zwei Versionen korrekt beschreibt, indem wir eine Realisierungsanalyse unter Verwendung der [UCM-](#page-14-0)Instanz durchfuhren, die die Version durch Deltas beschreibt. ¨

Abstract

Nowadays, customers expect highly configurable products, which can be developed using the approach of product lines. Product lines describe different product variants and versions of these variants, thus expressing variability in space through variants and variability in time through versions. A product line can be divided into problem space, where the user-visible characteristics or behaviours of a product, called features, and their dependencies are described, and the solution space, which represents the realisation artefacts. The state of the art reveals the following unsolved challenges: the lack of validation and realisability testing of variants over time, and the lack of a single instrument that provides a solution to this challenge and is also compatible with established tools. In this thesis, we approach the described challenges by extending an existing metatmodel, the [UCM.](#page-14-0) Therefore, we propose an implementation of the [UCM,](#page-14-0) which we extend by integrating existing concepts for expressing variability in space in order to adapt our implementation to known tools, such as FeatureIDE. We also integrate the concepts of delta modelling to describe the difference between two versions in the [UCM,](#page-14-0) and we use the model of [SGE](#page-14-1) variation types to categorise changes for further analysis with nominal types. We show the applicability of our implementation by reproducing a realisation analysis on an extension of the well-known [BCS](#page-14-2) Case Study. We use the extended [BCS](#page-14-2) to show that we can apply the [SGE](#page-14-1) variation types to a cross-domain product line, and show that our [UCM](#page-14-0) implementation correctly describes the semantic difference between two versions by performing a realisation analysis using the [UCM](#page-14-0) instance that describes the version by deltas.

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Acronyms

1. Introduction

Product lines [\(PLs](#page-14-5)) are a way of organising the development of software and hardware products that share a common set of configuration options and components [\[NC13\]](#page-63-2). This approach can be used to reduce development costs, time-to-market and improve product quality by utilising common components and considering variability early in the development process. Variability refers to the potential for multiple product variants and versions of variants, which is a common challenge in the development of mass-customized hardware and software products, such as automotive, robotics, embedded systems, and production systems [\[ABKS13\]](#page-62-2).

[PLs](#page-14-5) can be divided into problem space and solution space. The problem space describes the user visible characteristics or behaviours of the product, called features, and their dependencies in the feature model. The solution space represents the realisation artefacts of the features and their dependencies between those artefacts. The artefacts are related to the features in the problem space, linking the conceptual definition in the problem space to the concrete implementation in the solution space [\[ABKS13\]](#page-62-2).

In the problem space, the features of a [PL](#page-14-5) and their dependencies are described in a feature model [\(FM\)](#page-14-4). An example for a [FM](#page-14-4) of a Car [PL](#page-14-5) is shown in Figure [1.1.](#page-17-0) The first version of the Infotainment subsystem of the Car (left side of Figure [1.1\)](#page-17-0), requires the selection of the Radio feature, the Navigation feature, or both features at the same time. If the Navigation feature is selected the Voice Navigation feature can be chosen optionally. This results in five possible configurations of the Infotainment subsystem. The existence of different variants of one system at a certain point in time is called variability in space. The challenge of variability in space is to manage the almost infinite number of configurations that result from the combinatorial explosion as the number of features in the product line increases $[KTS+20]$ $[KTS+20]$.

The transformation of a valid configuration in the problem space into a concrete product in the solution space is a process known as realization. Therefor it is necessary to consider the problem space and the solution space together, which intensifies the challenges of managing variability in space. Figure [1.1](#page-17-0) shows that the Radio feature, the Navigation feature and the Voice Navigation feature are developed on

Figure 1.1: [FM](#page-14-4) of a car [PL](#page-14-5)

the same electronic computing unit [\(ECU\)](#page-14-12), which may cause realisability issues of some configurations. For instance, assume that the [ECU](#page-14-12) provides 2 gigabyte [\(GB\)](#page-14-13) of random access memory [\(RAM\)](#page-14-14), the Radio feature requires 1 [GB,](#page-14-13) and the Navigation feature requires 2 [GB.](#page-14-13) Then a product variant with a radio is realisable. A variant with the Navigation feature can be realised as well, but as the Radio feature and Navigation feature together require 3 [GB](#page-14-13) of [RAM,](#page-14-14) a variant with both features is not realisable. This realisability problem can only be found if problem space and solution space are analysed together.

The Unified Conceptual Model [\(UCM\)](#page-14-0) provides a unified representation of the problem and solution space. Figure [1.2](#page-17-1) shows the [UCM](#page-14-0) with the visualisation of the problem space on the left and the visualisation of the solution space on the right side. Connections between the left and the right side, represent relationships and dependencies between features and hardware and software components. This unified view enables the modelling of dependencies between problem space and solution space and the development of further analysis methods [\[WKR22\]](#page-63-0).

Figure 1.2: Unified Conceptual Model according to [\[WKR22\]](#page-63-0)

Besides variability in space, product line engineering must also consider the continuous evolution of systems, called variability in time. Variability in time can lead to structural changes in the [FM,](#page-14-4) affecting not only individual features but also the overall organisation and relationships between them. This dynamic evolution reflects the continuous adaptation of products to changing needs and market trends. For example, if to the mandatory Manual PW feature a new option, as the Automatic PW feature is added, the structure of the Power Window subsystem may need to be adjusted to consider the new dependency. This structural change can be seen in Figure [1.1](#page-17-0) from Version 1 to Version 2.

The dimension of variability in time also brings with it the challenge of maintaining compatibility between different product versions and ensuring that they work together. The difference in time could, for example, be due to a software update that was installed to vehicles via an over-the-air update for the Infotainment subsystem to provide better and more advanced path finding at Navigation (Version 1 to Version 2 in Figure [1.1\)](#page-17-0). The update requires more hardware resources, which the older versions of the Car [PL](#page-14-5) (Version 1) cannot provide with the [ECU-](#page-14-12)1. Therefore the update can only be applied to later versions of the vehicle equipped with [ECU-](#page-14-12)2.

The challenges of variability are compounded by the interplay of variability in space and time, which increases the complexity of product development and maintenance. For example, a manufacturing system must support a variety of product configurations while adapting to changes in production processes and software versions.

Within the domain of mechanical engineering, the System Generation Engineering [\(SGE\)](#page-14-1) Model [\(SGEM\)](#page-14-15) is a descriptive model that provides a systematic approach to analyse the evolution of system generations over time. The development of new system generations in the [SGEM](#page-14-15) is based on reference (sub-) system and consists of variations of (sub-) systems for reuse (Carryover Variation [\(CV\)](#page-14-9)) or development through Embodiment Variation [\(EV\)](#page-14-16) and Principle Variation [\(PV\)](#page-14-17) which can change the functional principle of (sub-) systems [\[ABR17\]](#page-62-4). The model can be used to express and track variability in time by analyzing changes in system generations over time.

Goal of this Thesis

Analyzing the state of the art reveals the following still unsolved challenges:

- an almost infinite number of configurations
- unifying the problem space and solution space
- validation and realisability testing of variants over time
- lack of a single instrument that offers solutions for all the challenges described

In this bachelor thesis we address these four challenges by implementing tool support for an integrated management of variability in time and space. Therefore, we define the following four Subgoals [\(SGs](#page-14-18)), which represent the tasks to be done in this bachelor thesis.

Subgoal 1

Implementation of the [UCM](#page-14-0) in the Eclipse Modeling Framework [\(EMF\)](#page-14-19).

An instantiable model of the [UCM](#page-14-0) in [EMF](#page-14-19) opens up the possibility of combined analysis across problem and solution space, in particular for realisability testing as proposed by Ochs [\[Och23\]](#page-63-1). Our contribution also includes implementing adapters to import data from FeatureIDE and exchange formats such as CSV and exports them back to FeautreIDE data. The evaluation of this contribution is addressed in [SG](#page-14-18) 2.

Subgoal 2

Application study of the implementation [\(SG](#page-14-18) 1) based on the Body Comfort System [\(BCS\)](#page-14-2) with regard to realisability.

We will evaluate our implementation of the [UCM](#page-14-0) with a replication study. The study aims to replicate existing results of realisation analysis presented by Ochs [\[Och23\]](#page-63-1), which will serve as Ground Truth [\(GT\)](#page-14-8). For the evaluation, we instantiate our implemented [UCM](#page-14-0) with an extension to the well known [BCS](#page-14-2)^{[1](#page-19-4)}-Case Study [\(CS\)](#page-14-7) and apply the realisation analysis method from Ochs [\[Och23\]](#page-63-1). By comparing our results with those of Ochs [\[Och23\]](#page-63-1), we can draw conclusions about the expressiveness of our implementation.

Subgoal 3

Development of a concept for the integration of the [SGEM](#page-14-15) into the [UCM](#page-14-0) with regard to variability in time.

In [SG3](#page-14-18) we integrate concepts of managing variability in time from the [SGEM](#page-14-15) into the [UCM.](#page-14-0) Therefore we identify similarities between both modelling concepts by comparing their variability management mechanisms. The resulting unified model will describe [PL-](#page-14-5)artefacts over time using concepts from the [SGEM](#page-14-15) as additional attributes.

Subgoal 4

Further development of the [BCS](#page-14-2) by adding evolution.

In [SG4](#page-14-18) we extend the [BCS](#page-14-2)[-CS](#page-14-7) from [SG](#page-14-18) 2 by introducing several new system versions, that are intended to represent the evolution of the system over time. To this evolution we add [SGE](#page-14-1) variation types to show that this [SGE](#page-14-1) concept can be applied to other domains. We then implement the unified model from [SG](#page-14-18) 3 and instantiate it with two versions of the extended [BCS](#page-14-2) to show how accurate our model implementation can express variability in time.

Structure of the Thesis

The following thesis is structured as follows: Chapter [2](#page-22-0) introduces the basic concepts that have been touched in this introduction. Chapter [3](#page-28-0) covers the design choices

¹<https://github.com/TUBS-ISF/BCS-Case-Study-Full/>

we made to extend the [UCM](#page-14-0) with the goal of [FM](#page-14-4) integration in Section [3.1,](#page-28-1) the integration of [SGE](#page-14-1) concepts through time deltas in Section [3.2](#page-31-0) and the unification of the integration together with the linking of the problem and solution space with mappings to allow the realisation analysis. Chapter [4](#page-36-0) describes the implementation of our previously designed solution approaches, as well as the implementation of the tools required for the evaluation and the evolution of the [BCS,](#page-14-2) where we added new versions and solution space artefacts. In Chapter [5](#page-48-0) we evaluate and discuss our contributions. Chapter [6](#page-58-0) gives an overview of related work. Chapter [7](#page-60-0) summarises the thesis and gives an outlook on future work.

2. Basics

This chapter covers the basic terms and concepts of this thesis. Section [2.1](#page-22-1) introduces basic concepts such as variability in time and space, problem space and solution space. Section [2.2](#page-23-0) introduces the [FM](#page-14-4) as a way of dealing with variability in space and Section [2.3](#page-24-0) discusses the [SGE](#page-14-1) approach as an approach of managing variability in time from a mechanical engineering perspective. Section [2.4](#page-25-0) introduces deltas as another way of dealing with variability in time. Section [2.5](#page-26-0) introduces the [UCM](#page-14-0) as a model in which variability in space and time as well as problem and solution space can be combined.

2.1 Product Line Engineering

[PLs](#page-14-5), according to [\[NC13\]](#page-63-2), provide an approach to mass customisation of (software) systems by constructing the system from reusable parts across a family of related products. This could be, as in our running example, a car [PL](#page-14-5) where each customer can individually customise the car they want to order.

Apel et al. [\[ABKS13\]](#page-62-2) distinguish product line engineering between requirements, known as the problem space, and artefacts that addresses those requirements, known as the solution space. Within this framework the problem space represents the different needs and constraints of user visible characteristics or behaviours of the product, called features, such as whether the car has a radio or not. The solution space comprises the artefacts and design decisions that make up the implementation of the [PL,](#page-14-5) including code, components, architectures and configurations.

Variability refers to the ability of [PLs](#page-14-5) to derive different products from a common set of artefacts [\[ABKS13\]](#page-62-2). The variability of a [PL](#page-14-5) spans two dimensions, one in space, including product configurations and one in time, including the evolution of [PLs](#page-14-5) over time. Variability in space includes product configurations that arise due to constraints between features. These constraints can be satisfied by selecting and deselecting features, resulting in various products, such as a car configuration with and without a radio. Variability in time occurs in a [PL](#page-14-5) through updates, enhancements and adaption from one version to another, leading to products from different

versions. Considering the dimensions of variability in time and space together enables a better understanding of how different product configurations are affected by temporal changes and contributes to better decisions in the development process.

2.2 Feature Model

The problem space describes the user visible characteristics or behaviours of the product, called features, and their dependencies. These features and dependencies can be described in a [FM.](#page-14-4) According to Apel et al. [\[ABKS13\]](#page-62-2), each feature can be referred to by its name. Each feature in a [FM](#page-14-4) can be selected or not, leading to various configurations within a [FM.](#page-14-4) This selection is limited by relations between features, groups of features or constraints that are also part of a [FM.](#page-14-4)

A [FM](#page-14-4) can be represented by propositional formulas, resulting from the dependencies between features, in conjunctive normal form [\(CNF\)](#page-14-20) or by a graphical representation like the feature diagram [\(FD\)](#page-14-6). In the [FD](#page-14-6) features and dependencies are represented as a tree, where each node represents a feature and is labelled with the corresponding feature name. Those dependencies are distinguished in hierarchical tree constrains and cross-tree constrains. The hierarchical tree constrains are categorised in mandatory, optional, or-groups and alternative groups and give the tree its structure.

Tree Structure	Logic Term	
mandatory feature f_i of parent p	$f \Leftrightarrow p$	
optional feature f_i of parent p	$f \Rightarrow p$	
or-group of features f_1, f_2, \ldots, f_k of parent p	$\left(\bigvee^k f_i\right) \Leftrightarrow p$	
	alternative-group of features $\left(\begin{pmatrix} k \\ \nabla f_i \end{pmatrix} \Leftrightarrow p \right) \wedge \begin{pmatrix} k \\ \bigwedge_{i,j,i-j}^k \neg (f_i \wedge f_j) \end{pmatrix}$ $f_1, f_2, \dots f_k$ of parent p	

Table 2.1: Propositional Logic Representation of a [FM](#page-14-4) [\[ABKS13\]](#page-62-2).

The mandatory attribute of a feature is represented by a filled circle in the [FD.](#page-14-6) In our running example, Figure [2.1,](#page-24-1) the feature Finger Protection is mandatory. This means the feature must be selected if the parent feature is selected, what corresponds to an equivalence in logic terms as seen in Table [2.1.](#page-23-1) If the feature is optional the feature can be selected if the parent feature is selected, which corresponds to an implication. An optional feature, in the [FD,](#page-14-6) is represented by an unfilled circle on the feature, as feature Power Window, in Figure [2.1.](#page-24-1)

In an or-group at least one of the features must be selected if the parent feature is selected, as logic term, shown in Table [2.1,](#page-23-1) the or-group is represented by a disjunction over the features in the group which needs to be equivalent to the parent. In the [FD](#page-14-6) an or-group is represented by a filled semicircle on the parent feature, as below feature Infotainment in Figure [2.1.](#page-24-1) If Infotainment is selected either Radio or Navigation or both need to be selected. An alternative-group is represented by an unfilled semicircle on the parent feature, as in the running-example below Power Window. Here exactly one of the features must be selected if the parent feature is

Figure 2.1: [FD](#page-14-6) of the second version of the running example

selected. As a logic term an alternative group is an exclusive or over the group which needs to be equivalent to the parent.

Besides the hierarchical tree constrains, there are also constrains which do not fit into the structure of the tree. Those cross-tree constrains can either be represented by a labelled arrow as in the running example where the feature Voice Navigation requires the features Radio, or by logic term written below the [FD.](#page-14-6)

2.3 System Generation Engineering

In the domain of mechanical engineering, [SGE](#page-14-1) is used to describe the development of products in product generations. Albers [\[ABR17\]](#page-62-4) defines [SGE](#page-14-1) as the development of new product generations based on reference systems. The idea is that every concept added to a product has a reference system, either from another product that has already implemented the same concept, or as an evolution of an existing concept.

The [SGE](#page-14-1) is used to describe generations through [CVs](#page-14-9), [EVs](#page-14-16) and [PVs](#page-14-17). A generation G_{n+1} , with a previous generation G_n , can be understood as set of all variations $G_{n+1} = CV_{n+1} \cup EV_{n+1} \cup PV_{n+1}$ where CV_{n+1} is the set of [CVs](#page-14-9), EV_{n+1} is the set of [EVs](#page-14-16) and PV_{n+1} the set of [PVs](#page-14-17).

As an example, we consider the development of a new generation of our car example to go through the three types of variation. The power window in the first generation $(G₁)$ has a hand crank to move the window up and down manually. In the second generation (G_2) the window can be moved automatically by pressing a button. The system uses hydraulics to raise and lower the window in both the first and second generation, but is controlled once manually and once electrically.

Carryover Variations [\(CVs](#page-14-9)) reuse the reference system, changing only the interface for integration. In our example, this would be the window itself, which remains the same from the first to the second generation.

Embodiment Variations [\(EVs](#page-14-16)) change the shape of the subsystem but keep the principle of the solution. In the example this would be the hydraulics used to raise and lower the window. The principle of the hydraulics does not change but the shape changes because it needs to be controlled electrically.

Principle Variations [\(PVs](#page-14-17)) vary the solution principle by using new ones. A [PV](#page-14-17) always goes with a [EV.](#page-14-16) In the power window example, the hand crank that drives the hydraulics is replaced by a motor that can be controlled by a button, which is a new way of interacting with the power windows hydraulics.

These variation types allow us to calculate the complement of the degree of change over generations, where $\delta_{CV,n+1} = 100\%$ is an adaptive design and $\delta_{CV,n+1} = 0\%$ is a complete redesign of the system. $\delta_{CV,n+1}$ is calculated as follows

$$
\delta_{CV,n+1} = \frac{|CV_{n+1}|}{|G_{n+1}|} = \frac{|CV_{n+1}|}{|CV_{n+1} \cup EV_{n+1} \cup PV_{n+1}|}
$$

Applied to our example we would get a degree of change of 33.33% as only one of our three variation types were a [CV,](#page-14-9) resulting in $\delta_{CV,2} = \frac{1}{3} = 33.33\%$.

2.4 Deltas

Deltas represent the specific changes or variations to accommodate different features, configurations or requirements based on a core model. With regards to [PLs](#page-14-5) this means deltas are the element containing the change for a modeling element from one configuration to another or from one version to another.

Figure 2.2: [FD](#page-14-6) of the running example

In our running example in Figure [2.2](#page-25-1) deltas would describe what changes from Version 1 to Version 2. The feature Manual PW will no longer be mandatory, but in an alternative-group. The feature Automatic PW is added to the same alternativegroup and serves as parent of the new mandatory feature Finger Protection. The modification and the additions can be described by deltas.

Independent of [FMs](#page-14-4) a general model M , according to Schaefer [\[Sch10\]](#page-63-3), is a tuple $M = (E, R)$ of modeling elements E and a relation between those elements R $E \times E$.

A Δ -Model over a model M is a tuple $\Delta = (\delta, Op)$, where δ is a constraint over E and $Op = \{op_1, op_2, \ldots, op_n\}$ is a set of delta operations over the model M which can either add, modify or remove an element e or add or remove a relation between two elements $r(e_1, e_2)$.

The Table [2.2](#page-26-2) shows the delta operations Op of our running example. op_1 is a modification operation, that changes the mandatory tree constraint to an alternativegroup. Then the two new features Automatic PW and Finger Protection are added as op_2 and op_3 and a new mandatory tree constraint is added as op_4 . To the mandatory tree constraint a relation is added from Automatic PW as $op₆$ and a relation from the tree constraint to Finger Protection as op_7 . This sub-tree

i	op_i	e_1	e ₂
1	mod e_1	mandatory tree constraint above Manual PW to	
		alternative-group	
2	add e_1	Automatic PW	
3	add e_1	Finger Protection	
$\overline{4}$	add e_1	mandatory tree constraint	
5	add $r(e_1, e_2)$	alternative-group from op_1	Automatic PW
6	add $r(e_1, e_2)$	Automatic PW	mandatory tree constraint from op_3
7	add $r(e_1, e_2)$	mandatory tree constraint from op_3	Finger Protection

Table 2.2: Delta Operations of the running example

starting at Automatic PW is connected to the rest of the [FD](#page-14-6) by a relation from the alternative-group from op_1 to Automatic PW as op_5 .

The application of the operations creates a new model with, depending on the operation, a new element or dependency added, removed or in case of the modification operator first removed and then the modified one added. In our example the model would be Version 1 and after the deltas are applied the new model would be Version 2.

2.5 Unified Conceptual Model

The [UCM](#page-14-0) was created to unify the problem and solution space in one model and also contain concepts for variability in space and time.

Figure 2.3: [UCM](#page-14-0) according to Ananieva et al. [\[AGK](#page-62-1)⁺22]

Figure [2.3](#page-26-1) shows the [UCM](#page-14-0) as class diagram according to Ananieva et al. [\[AGK](#page-62-1)⁺22]. The model allows, similarly to the [FM,](#page-14-4) to include features that are distinguished by their names. The dependencies between features are represented by the class Constraint. Each feature dependency is represented, similarly to the [CNF,](#page-14-20) by a logical term contained in the Constraint. Instances of the class System Revision can be understood as versions of the unified system. They refer to other System Revision instances and to Feature Revision instances. The concepts of variability in space are part of the problem space. The solution space in the model contains products, fragments and classes such as Configuration and Mapping to connect the two spaces. The Product is derived from Configuration and Fragment where a configuration is a selection of Options and a Fragment is a concrete part of the product. Such a fragment can be lines of code or other model elements and gets mapped to an Option by Mapping. This ensures that each selectable Option has a corresponding counterpart in the solution space.

Wittler et al. [\[WKR22\]](#page-63-0) and Ochs [\[Och23\]](#page-63-1) have further developed the [UCM,](#page-14-0) which is shown in Figure [2.4.](#page-27-0) The class Product is derived from a class Configuration, which refers to the problem space and Components of the solution space. The class Component can either be a Software Component and demand Resources or a Hardware Component and grant them. The class Resource consists of a value and a type. The class Resourcetype consists of a name, a unit of measurement, a boundary type, an the boolean attributes isAdditive and isExclusive. The boundary type can either be LOWER, UPPER or EXACT. LOWER states that a requested resource needs to be fulfilled with a provision that is greater than or equal to the requested one. EXACT requires that the provided resource value is equal to the requested one and UPPER requires the provided resource to be less or equal to the requested one. For example the response time type must be boundary type LOWER, because if a software component requires a response time of 12ms, a hardware component with a lower value such as 10ms will satisfy the demand, while a higher value such as 13ms will not. The attribute isAdditive determines whether or not it is allowed to add resources to satisfy a software components demands. For example, if a software component requires 100W of power and two hardware components each provide 70W, then the component's requirements can only be met if the addition of the resource is allowed. The attribute isExclusive determines whether its the resource that can satisfy the demands of multiple Software Components or not.

Our contribution mainly relies on the [UCM](#page-14-0) by Ochs [\[Och23\]](#page-63-1) but also takes parts of concepts considered by Ananieva et al. [\[AGK](#page-62-1)⁺22].

Figure 2.4: [UCM](#page-14-0) according to Ochs [\[Och23\]](#page-63-1)

3. Design

In this chapter the solution approaches are introduced. We extend the [UCM](#page-14-0) to achieve the importation of FeatureIDE data that we addressed in [SG1](#page-14-18) in Section [3.1.](#page-28-1) We further extend the [UCM](#page-14-0) to integrate the [SGE](#page-14-1) and add evolution what we formulated in [SG3](#page-14-18). This solution approach takes place in Section [3.2.](#page-31-0) In Section [3.3](#page-33-0) the design is unified and a specialised mapping is added to connect the problem and solution spaces.

3.1 Feature Model Integration

With respect to [SG1](#page-14-18), we modify the problem space of the [UCM](#page-14-0) so that it represents a feature metamodel. Figure [3.1](#page-29-0) shows an excerpt of the [UCM](#page-14-0) with relevant parts concerning the representation of a feature meta-model. The following section describes the design decisions we made to achieve this goal.

A feature, according to the [FM](#page-14-4) introduced in Section [2.2,](#page-23-0) has a name and can optionally have realisation artefacts in the solution space. Therefore, in the feature metamodel we represent a feature with a name and a boolean property isAbstract.

Apel et al. [\[ABKS13\]](#page-62-2) proposed the [FD](#page-14-6) as representation of the [FM](#page-14-4) which differentiates between feature dependencies represented by tree hierarchy and by cross-tree constraints. Another representation of [FMs](#page-14-4) would be through [CNFs](#page-14-20). The representation through [CNFs](#page-14-20) would simplify the design effort, since we only need to design cross-tree constrains. But we not only want to represent [FMs](#page-14-4), but also want to enable the management of variability in space through our model. Therefore we adopt the differentiation of feature dependencies and introduce two specialisations of constraints to the feature meta-model: Hierarchical tree constraints and cross-tree constraints as detailed in the following.

Hierarchical tree constrains are described through hierarchy types as or-groups, alternative-groups, mandatory and optional, which where introduced in Section [2.2.](#page-23-0) Such a hierarchical tree constraint is always associated to exactly one parent feature and, depending on the hierarchy type, to at least one child feature. In our design, we distinguish between associated features and hierarchy types, as all hierarchical

Figure 3.1: Extended [UCM](#page-14-0) showing only the [FM](#page-14-4) extensions

tree constraints share the characteristic of having associated features. This leads us to the class Tree Constraint which represents the hierarchical tree constraint and needs exactly one Feature as a parent and refers to at least one Feature. The type is represented by a type attribute, which is a reference to an enumerated class Constraint Type that represents the different hierarchy types, mandatory, optional, or, alternative, as names. This structure can be seen in Figure [3.1](#page-29-0) represented by the associations between the classes Feature, Tree Constraint and Constraint Type.

A cross-tree constraint is a propositional logic term with features as literals. Therefore, we introduce an adapted model of a propositional logical formula as follows: A literal can be encapsulated by logical connectives such as not, and, or, implies and equals $(\neg, \wedge, \vee, \Rightarrow, \Leftrightarrow)$. The type of logical connectives determines the number of outgoing nodes. A not node has only one child, implies and equals have two outgoing nodes and or and and have at least two outgoing nodes. A propositional logic term constructed in this way can then be encapsulated again by logical connectives, building up to a tree with a logical connective as root node. The tree constructed in this way is known as a concrete syntax tree [\[AA07\]](#page-62-5) and can be used to represent propositional logic terms. It has the advantage that the order of evaluation of the term is ensured by traversing the concrete syntax trees and no brackets are required. We adapt the idea of concrete syntax trees in our design through the abstract class Logic Node, which represents the nodes of the tree. A node can be either a logical connective or a literal. We design this specialisation through specialised Logic Nodes. Each specialisation of the class Logic Node consists of a different number of children, which are references back to the class Logic Node. The class Not consists of one child, the class Implies and the class Equals consist of exactly two children, the class And and the class Or of at least two children and class Literal has no children but needs a reference to the class Feature instead. The class Cross Tree

Constraint represents the cross-tree constraints and consists of a reference to the class Logic Nodeas the propositional logic term. This design ensures the consistency of an expression even if, for example, the name of the feature changes.

Figure [3.2](#page-30-0) shows the object diagram resulting from the parsed [FD](#page-14-6) of Version 1 of our running example. The features of the [FD](#page-14-6) are represented as instances of the class Feature. For example, the feature Voice Navigation is represented by feats3 and is illustrated by the green arrow. You can see the structuring properties of the tree constraints in treeCons0 and treeCons1 where, as in the [FD,](#page-14-6) the feature Car has two children with different hierarchy types. treeCons2 represents an alternative-group and like the hierarchical tree constraint, has the parent feature Infotainment and two children. The red arrows show how the hierarchical tree constraints are mapped to instances of the class Tree Constraint. Finally, the requires cross tree constraint is represented by cons0, an instance of the class Cross Tree Constraint. A requires cross tree constraint can be understood as an implication and is therefore represented as such in the unified system by expression0 as an instance of Implies. The structure of the concrete syntax tree can be seen in expression0 by having exactly two children which are instances of Literal and each refer to their corresponding features.

Figure 3.2: Representation of the [FM](#page-14-4) of the first version of the running example as object diagram of the extended [UCM](#page-14-0)

The object diagram clearly shows that no information is lost in the transformation from the [FD](#page-14-6) to the unified system. The distinction between tree and cross-tree constrains plays an important role here, as without it the reconstruction of the structure would be almost impossible. This will allow us in the next chapter not only to parse the [FD](#page-14-6) into a unified system, but also to parse a unified system back into a [FD.](#page-14-6)

3.2 Integration of [SGE](#page-14-1) Concepts through Time Deltas

This sections aims to achieve [SG](#page-14-18) 3, where we formulated the goal of developing a concept to model the [SGE](#page-14-1) by integrating the concepts of managing variability in time from the [SGE](#page-14-1) into the [UCM.](#page-14-0)

In Section [2.3](#page-24-0) we introduced the term generation G_{n+1} that can be understood as set of all carryover, embodiment and principle variations $G_{n+1} = CV_{n+1} \cup EV_{n+1} \cup PV_{n+1}$ based on a predecessor generation G_n . For simplicity, we divide these variations into two categories: those that keep the (sub-)system as it is, which are [CVs](#page-14-9), and those that introduce changes, that are [PVs](#page-14-17) and [EVs](#page-14-16). Consequently, a new generation can be conceptualised as the old (sub-)system with the applicable changing variations applied. This concept corresponds to the concept of deltas introduced in Section [2.4.](#page-25-0)

We modify the concept of Δ -models introduced in Section [2.4](#page-25-0) to describe changes of the unified system over time. We understand an instance of the [UCM](#page-14-0) as a model $M = (E, R)$ with the model elements E (e.g. instances of classes Feature and Tree Constraint) and the relations R between elements (e.g. the references of an instance of the class Feature to instances of the class Tree Constraint). In the according Δ -model $\Delta = (\delta, Op|_{R|_{Deltaable}})$ we restrict the delta operations Op to only be defined for $R|_{\text{Deltable}}$. $R|_{\text{Deltaable}}$ is a subset of R and is defined in Equation [3.1.](#page-31-1) This allows us to store the ∆-Model as an ordered list of operations and elements of $R|_{deltaable}$, where the first element is a reference to an existing element in our model and the second element is either a new element or an existing element we wish to remove.

$$
R|_{Deltaable} = (\text{Feature} \times \text{Tree Constant})
$$
\n
$$
\cup (\text{Tree Constant} \times \text{Feature})
$$
\n
$$
\cup (\text{Software Component} \times \text{Resource})
$$
\n
$$
\cup (\text{United System} \times (\text{Feature UCross Tree Constant}
$$
\n
$$
\cup \text{Mapping} \cup \text{Component} \cup \text{Resourceype}))
$$
\n(3.1)

Figure [3.3](#page-32-0) shows the changes we performed on the [UCM](#page-14-0) to add this modified ∆ model. The ∆-model is represented by the class Version with an ordered list of references to Delta as the attribute deltas. As with delta modelling the deltas can be applied. In the class Version we have added the method applyDeltas for this purpose.

The class Delta represents the delta operations and has the attributes type, position, value and valueRef. The attribute type is a reference to Delta Type, which indicates whether the Delta adds, removes or modifies an element. The attribute position of the class Delta, has the same function as the first element of the relation tuple e_1 of $R|_{\text{Deltaable}}$ i.e. to point to the element that has or will have a reference to e_2 which is represented by value and valueRef. To ensure that (position, value) is in $R|_{deltaable}$ each class marked with an orange Δ in Figure [3.3](#page-32-0) implements the interface Delta Operations and can be set as position. The type of value depends on the generic type of Delta Operations which must be the

Figure 3.3: Extended [UCM](#page-14-0) showing only the delta relevant part

same type as the generic type of Delta. The binding can be seen in the legend at the bottom right of Figure [3.3.](#page-32-0)

We integrate concepts of the [SGE](#page-14-1) into delta-modelling by labelling each delta with a [SGE](#page-14-1) variation type. We can consider the class Delta as variation and the class Version as generation, since it is made up of instances of the class Delta. To distinguish between the variation types of the class Delta, we add an attribute variation as a reference to a class Variation Type, which can be either PRINCIPLE, EMBODY-MENT or CARRYOVER, matching the variation types [PV,](#page-14-17) [EV](#page-14-16) and [CV](#page-14-9) we introduced in Section [2.3.](#page-24-0)

We illustrate the functionality of deltas using the object diagram shown in Figure [3.4.](#page-33-1) The left-hand side of the object diagram shows Version 1 of the running example as described in Section [3.1](#page-28-1) and the right-hand side shows the version with its delta. delta0 modifies the instance of the class Tree Constraint referenced by valueRef, i.e. it deletes it and then adds a new instance of the same class referenced by value to the feature referred to by position. As the Figure shows, a delta can take an entire sub-tree and add it to the unified system, rather than just adding one element at a time as suggested by the delta operations in Table [2.2.](#page-26-2)

Figure 3.4: Representation of the [FM](#page-14-4) of the first version of the running example with a delta to version two as object diagram of the extended [UCM](#page-14-0)

3.3 Unifying Variability in Space and Time in Problem and Solution Space

We want to extend the concepts of managing variability in space (Section [3.1\)](#page-28-1) and time (Section [3.2\)](#page-31-0) beyond the boundaries of the problem space. Therefore, we specialise the class Mapping, which is used to connect the problem and solution spaces, by the class Resource Mapping. This class maps a feature to a resource demand, which consists of the value of the demanded resource, the resource type and the id of the software component in which the feature is implemented. We need to use the mapping and not the class Software Component because we still want to be able to manage variability. Therefore, the final resource demand of a software component depends on the version and configuration.

The resulting metamodel, which incorporates all our changes and allows for the management of variability in space and time in the problem and solution space, is shown in Figure [3.5.](#page-34-0) Appendix [A.5](#page-71-0) shows the full diagram.

Figure 3.5: Extended [UCM](#page-14-0)
4. Implementation

This chapter presents the code artefacts we created to implement and evaluate the [UCM](#page-14-0) in Section [4.1](#page-36-0) and the addition of resources to the various versions of the [BCS](#page-14-1) and some new versions in Section [4.2.](#page-39-0)

4.1 Unified Conceptual Model Implementation

This section presents the code artefacts and tools used to implement and evaluate our extended version of the [UCM.](#page-14-0)

4.1.1 Eclipse Modeling Framework

In [SG1](#page-14-2) we already specified that we are using the Eclipse Modeling Framework^{[1](#page-36-1)}. The [EMF](#page-14-3) is used to create and edit models and then generate Java code based on the model. This model-centered view allows to concentrate on the design (Chapter [3\)](#page-28-0), although Java has some limitations that made it necessary to adapt the design.

In Chapter [3](#page-28-0) we designed the Delta with two generic types to ensure that deltas are only applied to relations that are elements of $R|_{\text{Deltaable}}$. The first generic S is the type of e_1 , if we consider (e_1, e_2) as the relation tuple that is an element of $R|_{\text{Deltaable}}$ and the second generic T is the type of e_2 . Delta Operations is an interface with a generic type T and the generic type S extends Delta Operations with the generic type T of Delta bound to the generic type T of Delta **Operations.** This ensures that classes that should be e_1 , implement the interface Delta Operations with the generic T of Delta Operations bound to the type of e_2 . Java does not allow the same interface to be instantiated with another generic class, as class Unified System needs to do, because, as we saw in Section [2.4,](#page-25-0) it implements Delta Operations<Feature>, Delta Operations<Cross Tree Constraint>, Delta Operations<Mapping>, Delta Operations<Component> and Delta Operations<Resource Type>. We can get around this limitation of Java by implementing the interface with the super type Object as Delta Operations<Object> and then distinguish in the methods add and remove the interface implements,

¹<https://eclipse.dev/modeling/emf/>

which instance the argument passed is of. The method modify does not need to be touched since it calls the methods add and remove which then differentiate the instance.

For the serialisation of the unified system, we want the unified system to be build in such a way that when we serialise an instance of it, everything that is relevant to the instance is held by it. In Java we cannot specify whether a variable holds an object or just the reference to it. But [EMF](#page-14-3) has this specification via the containment property. This property requires each object to be contained within another object to be able to save the objects properly. For the class Delta this means that we need to have two different attributes to refer to the value we want to either add or remove. When we want to remove a value we refer to it as valueRef as it is a reference to another object and is already contained in the Unified System. But if we want to add a value, the class Delta contains the value as the attribute value. Since an object cannot be contained in more than one object, the attribute value is removed when the delta is applied, because then the value is contained in the object referred to as position.

To be able to save and load an instance of the unified system and connect to other tools, we want to serialise the unified system. The [EMF](#page-14-3) allows us to save and load the contents of the model to and from a Extensible Markup Language [\(XML\)](#page-14-4) Metadata Interchange $(XMI)^2$ $(XMI)^2$ $(XMI)^2$ file. Listings [4.1](#page-38-0) shows the [XMI](#page-14-5) file containing the parsed [UCM](#page-14-0) representation of Version 1 of our running example (Figure [3.1\)](#page-29-0). The containment property of the [EMF](#page-14-3) plays an important role here, as we want to serialise all references only through the unified system instance. Listing [4.1](#page-38-0) shows this containment in the unified system by the fact that every element in the [XMI](#page-14-5) file is at least one level below the unified system instance. An element consists of either a start-tag \langle name \rangle and an end-tag \langle name \rangle or, if there are no elements contained in between those tags, an empty-tag \langle name \rangle . Each element in the [XMI](#page-14-5) file is named similarly to the name of the reference. For example the Tree Constraint is referenced as treeconstraint from the class Feature and so the element name is also treeconstraint. The attributes of the class, such as the type attribute of Tree Constraint are represented in the tags as [XMI](#page-14-5) attributes. The attributes consist of a name-value pair of the form $name = value$. The name and value are similar to the name and value in the instance of the class in the unified system.

4.1.2 Adapters

FeatureID $E³$ $E³$ $E³$ is the state of the art tool for creating and displaying [FDs](#page-14-6). It is an a Eclipse plugin and we can use the libraries it provides for our adaptation.

Therefore we deserialise a FeatureIDE [FD](#page-14-6) file with the libraries provided by the plugin. The adapter then translates the [FD](#page-14-6) similar to what we have done with our running example in Figure [3.2.](#page-30-0) We extend this adapter further by allowing it to take into account the attributes in the FeatureIDE [FD](#page-14-6) Ochs [\[Och23\]](#page-63-0) uses to store the resource type mappings. To integrate the resource type mappings, we also need to add resource types to the model to give the mapping a resource to

²<https://www.omg.org/spec/XMI/>

³<https://github.com/FeatureIDE/FeatureIDE>

```
1 \ldots]
2 <ucm:UnifiedSystem [...] name="Car ">3 <feats name="Car'' isAbstract="true">
4 | <treeconstraint type="MANDATORY">
5 | <feature name="Infotainment" isAbstract="true">
6 \longrightarrow \langle treeconstraint type="OR">
7 \times feature name="Radio" isAbstract="false"/>
8 | <feature name="Navigation" isAbstract="false">
9 | <treeconstraint type="OPTIONAL">
10 | <feature name="Voice_Navigation" isAbstract="false"/>
11 | </treeconstraint>
12 | \langle/feature>
13 </treeconstraint>
14 \langle /feature>
15 | </treeconstraint>
16 | <treeconstraint type="OPTIONAL">
17 | <feature name="Power_Window" isAbstract="true">
18 | <treeconstraint type="MANDATORY">
19 | <feature name="Manual_PW" isAbstract="false"/>
20 | </treeconstraint>
21 / </feature>
22 </treeconstraint>
23 \le / feats>
24 | <cons id="0">
25 <expression xsi:type=" u cm: Im pli e s ">
26 | \sim <nodes xsi:type="ucm:Literal" featureoption="//@feats.0/
            @ treeconstraint. 0/ @ feature. 0/ @ treeconstraint. 0/ @ feature. 1/@tree constraint.0/@feature.0'27 \vert <nodes xsi:type="ucm:Literal" featureoption="//@feats.0/
            @ treeconstraint. 0/ @ feature. 0/ @ treeconstraint. 0/ @ feature. 0"/>
28 </expression>
29 \le/cons>
30 </ucm:UnifiedSystem>
```
Listing 4.1: Parsed [UCM](#page-14-0) representation of Version 1 of the running-example

reference. So we use the opencs v^4 v^4 library to deserialise the resource types stored in a comma-separated values [\(CSV\)](#page-14-7) file. The same deserialiser can be used to read the [CSV](#page-14-7) file in which Ochs [\[Och23\]](#page-63-0) has stored the resource provisions of the hardware components.

In the [CSV](#page-14-7) resource type file, each line represents a resource type. Each line consists of four values, the first one being the ID of the resource, the second the binary value isAdditive, the third the binary value isExclusive and the last value is boundary where the three possible values are represented by the numbers LOWER : 0, UPPER : 1 and EXACT : 2.

In the resource provisioning file, each row represents a hardware component and each column represents the resource type whose ID matches the corresponding column number when numbered consecutively from zero in ascending order. The value in each cell then represents the quantity or value of the corresponding resource type provided by the hardware component.

⁴<https://opencsv.sourceforge.net/>

The resource demands of a feature are represented by its attributes in the Fea-tureIDE [FD.](#page-14-6) The name of the attribute consists of a tuple (i, j) , where i is the ID of the software component and j is the ID of the resource type. The value of the attribute is the demanded number or value of the resource.

We also wrote an adapter the other way around in order to get a FeatureIDE [FD](#page-14-6) out from a unified system instance. So we read the [UCM](#page-14-0) [XMI](#page-14-5) file and deserialise it with the tools provided by the [EMF](#page-14-3) to a unified system instance. After adapting, the FeatureIDE [FD](#page-14-6) instance is serialised using the libraries provided by FeatureIDE.

4.1.3 Combined Problem Solver

The combined problem solver tool was implemented by Ochs [\[Och23\]](#page-63-0) to calculate all realisable and valid configurations of a FeatureIDE [FD](#page-14-6) with corresponding resource types, and resources provisions and a [CNF](#page-14-8) representation of the [FM.](#page-14-9) We modified his tool to instead take our [XMI](#page-14-5) representation of the unified system to calculate all valid and realisable configurations. We later use this tool to calculate the valid and realisable configurations using the unified system representation for evaluation purposes and to replicate the results of Ochs [\[Och23\]](#page-63-0) achieved using the unmodified combined problem solver tool. Therefore we need to make the following adjustments:

Extract the resource types from Resourcetypes

The resource types are extracted from the serialised unified system instead of the resource type [CSV](#page-14-7) file Ochs [\[Och23\]](#page-63-0) used.

Extract the feature demands from Mappings and the resource provisions from Hardware Components

To extract the corresponding data from the mappings and cross-tree constraints we need to resolve the references in the [XMI](#page-14-5) file, as in line 26 of Listings [4.1.](#page-38-0) The references are built as concatenations of elements of the tree. In the example in line 26 // θ feats. θ stands for the first feats element of the root, the ucm, element. The / stands for going into the selected element and the treeconstraint.0 stands for the first treeconstraint element below the current element.

Calculate the a [CNF](#page-14-8) of the [FM](#page-14-9) from Cross Tree Constraints and Tree Constraints.

The [CNF](#page-14-8) is constructed by conjuncting the logical term representation of tree constraints and cross-tree constraints. The cross-tree constraints can be transformed into [CNF](#page-14-8) by traversing each concrete syntax tree that presents each cross-tree constraint. The logic terms of a tree-constraint are looked up by the type of the treeconstraint in Table [2.1.](#page-23-0) And then build according to the logic term with the features in the tree-constraint and the parent feature.

4.2 Evolution of the Body Comfort System

This section describes how the existing evolution of the [BCS](#page-14-1) is extended by adding more versions, resource provisions and demands, and how evolution can be classified through [SGE](#page-14-10) operations.

Version 1.0

The base version of the [BCS](#page-14-1) Version 1.0 consists of a 27 features which split up in tree subsystems Security, DoorSystem and HMI, as you can see in the [FM](#page-14-9) in Figure [4.1.](#page-40-0) The feature DoorSystem has electric adjustable Exterior Mirrors [\(EMs](#page-15-0)) that optional can be heatable and Power Windows [\(PW\)](#page-15-1) can be either automatic or manually controlled and need to have a Finger Protection [\(FP\)](#page-15-2). The feature Security is optional and consists of functionality for Alarm System [\(AS\)](#page-15-3), Remote Control Key [\(RCK\)](#page-15-4) or Central Locking System [\(CLS\)](#page-15-5). The feature HMI consists of multiple StatusLEDs which can be chosen individually via an or-group representing status and signal lights. There are six cross-tree constraints in the [FM](#page-14-9) of the [BCS](#page-14-1) [CS.](#page-14-11)

 $LED_AS \Rightarrow AS$ LED_Heatable ⇒ Heatable Control Automatic \Rightarrow \neg Manual PW LED $CLS \Rightarrow CLS$ $RCK \Rightarrow CLS$ Control AS \Rightarrow AS

Figure 4.1: [FM](#page-14-9) of [BCS](#page-14-1)

Table 4.1: Resource Types of Version 1.0

Hardware Component (hw_i)	Provisions $(r p_k^j)$
infotainment-hardware (hw_0)	$rp_0^0 = 8$ $rp_1^0 = 25$ $rp_6^0 = 4$ $rp_7^0 = 16$
$\texttt{security-hardware}(hw_1)$	$rp_1^2 = 16$ $rp_3^1 = 700$ $rp_{4}^{1} = 1$ $rp_{5}^{1}=4$

Table 4.2: Resource Provisions of Version 1.0

Feature	Software Component sw_i	Resource Demands rd_k^i
LED_AS	sw_0	$rd_0^0 = 2$
LED_FP	sw_0	$rd_0^0 = 1$
LED_CL	sw_0	$rd_0^0 = 1$
LED_PW	sw_0	$rd_0^0 = 1$
LED_EM	sw_0	$rd_0^0 = 1$
LED_Heatable	sw_0	$rd_0^0 = 1$
Electric	sw_1	$rd_1^7=10$ $rd_1^1 = 5$
Heatable	sw_1	$rd_1^1=20$
FP	sw_2	$rd_6^2 = 1$
Manual_PW	sw_2	$rd_6^2 = 2$
Automatic_PW	\mathcal{SW}_2	$rd_7^2=5$ $rd_6^2 = 3$
RCK	sw_3	$rd_2^3 = 2$ $rd_3^3 = 10$
Control_Automatic_PW	sw_1	$\frac{rd_7^1 = 5}{rd_2^3 = 2}$
	sw_3	
Adjust_EM	sw_2	$rd_7^2=10$ $rd_2^3 = 2$
	sw_3	
Control_AS	sw_3	$rd_2^3 = 2$ $rd_2^3 = 2$
Safety_Function	sw_3	$rd_2^3 = 2$
AS	sw_3	$rd_3^3 = 100$ $rd_5^3 = 4$
Interior_Monitoring	sw_3	$rd_3^3 = 700$ $rd_5^3 = 1$
CLS	sw_3	$rd_3^3 = 10$
Automatic_Locking	sw_3	$rd_4^3 = 1$

Table 4.3: Resource Demands of Version 1.0

In the solution space Ochs [\[Och23\]](#page-63-0) added four software components. The hmicontroller (sw_0) controls the Human Machine Interface [\(HMI\)](#page-15-6) and all StatusLEDs. The power-window-controller (sw_1) controls the PW and exterior-mirror-controller (sw_2) the EM. At last the security-controller (sw_3) controls the Security subtree.

In Table [4.1](#page-41-0) the resource types are specified. As introduced in Section [2.5,](#page-26-0) a resource type has an identifier k and the three resource type properties is Additive, isExclusive and boundary.

The resource demands can be found in Table [4.3.](#page-42-0) The resources are provided by the hardware components in Table [4.2](#page-41-1) where each hardware component provides an amount or number of resources.

The resource provisions are designed to not fulfil all resource demands thus not all valid configurations are also realisable. In this version the resource demands of the feature Interior_Monitoring, $rd_5^3 = 1$, can not be fulfilled. The resource type $r₅$ describing the number of Security Video Cameras has an EXACT boundary. In the resource provisions only hw_1 provides $rp_5^1 = 4$ which does not match the request exactly. This means that out of 11616 valid configurations only 6528 different configurations are realisable.

Version 1.1

Version 1.1 makes changes of the architecture because of new passenger safety regulations. The new safety regulations require a dedicated hardware, to separate security and safety. For this purpose hardware safety-hardware is added and takes over all resource provisions related to passenger safety.

Appendix [A.1.2](#page-64-0) shows the details in tables.

Version 2.0

In Version 2.0 Figure [4.2](#page-44-0) shows, that the subsystem rooted in feature Wiper is added as a mandatory feature. The feature Wiper needs either a High_Quality_Sensor or a Low_Quality_Sensor to detect rain and a High_Quality_Wiper or a Low_- Quality_Wiper to remove rain from the windshield. The low quality wiper can only be on or off and the low quality wiper only detects rain or not, while the high quality features can be more granular. Optionally a Clean feature can be chosen to clean the windshield.

The extension of the BodyComfortSystem through Wiper is a [PV.](#page-14-12) All the features that are [PVs](#page-14-12) have a green border in Figure [4.2.](#page-44-0) The StatusLED Feature itself is only an [EV.](#page-14-13) All the feature that are [EVs](#page-14-13) have an orange border in Figure [4.2.](#page-44-0) Everything else is not changed and thus are [CVs](#page-14-14).

From this example we can generalise rules to classify the variation types in [FDs](#page-14-6). A feature that is adding a new concept or solution principle to the system can be considered as [PV.](#page-14-12) Parent features of such a [PV](#page-14-12) are at least an [EV](#page-14-13) since their shape needs to change if a new feature is added. Only if the variation is not present or minimised to only a change of parameters the variation is a [CV.](#page-14-14)

Figure 4.2: [FM](#page-14-9) of [BCS](#page-14-1) Version 2.0

Table 4.4: Resource Types added in Version 2.0

Feature	Software Component sw_i	Resource Demands rd_k^i
LED_Wiper	sw_0	$rd_0^0 = 1$
LED_Frost_Protection	sw_0	$rd_0^0 = 1$
LED Clean	sw_0	$rd_0^0 = 1$
Clean	sw_4	$rd_s^4 = 1$ $rd_{10}^4=1$
Frost_Protection	sw_4	$rd_9^4=1$
Low_Quality_Wiper	sw_4	$rd_1^4=10$ $rd_7^4=5$
High_Quality_Wiper	sw_4	$rd_1^4=10$ $rd_7^4 = 10$
Low_Quality_Sensor	sw_4	$rd_7^4=5$
High_Quality_Sensor	sw_4	$rd_7^4=10$

Table 4.5: Resource Demands added in Version 2.0

Hardware Component (hw_i)	Provisions $(r p_{\nu}^j)$
infotainment-hardware (hw_0)	$rp_0^0 = 8$ $rp_1^0 = 35$ $rp_7^0 = 16$
$\texttt{security-hardware}(hw_1)$	$rp_2^1 = 16$ $rp_{3}^{1}=700$ $rp_{4}^{1}=1$ $rp_{5}^{1}=4$
safety-hardware (hw_2)	$rp_3^2 = 10$ $rp_6^2 = 4$ $rp_{8}^{2} = 1$ $rp_{0}^{2} = 1$ $rp_{10}^2 = 1$

Table 4.6: Resource Provisions of Version 2.0

As software component the wiper-controller (sw_4) is added to control the wiper subsystem. The Wiper feature can be seen as a feature for passenger safety because the driver can see better with a clean windshield. This is the reason why the required resource demands of Table [4.5,](#page-45-0) except for the LEDs, are provided by the safety-hardware as you can see in Table [4.6.](#page-45-1)

The model has nine StatusLEDs but safety-hardware only provides eight. Therefore not every configuration is buildable.

Version 3.0

Version 3.0 adds electric seat adjustment with memory function on the driver's key. Therefore, a new feature Seat is added as optional child of the feature BodyComfort-System and the resource types number of motors and long-term memory are added. These are demanded by a new software component seat-controller (sw_5) and get fulfilled by the infotainment-hardware.

Appendix [A.1.4](#page-65-0) shows the details in tables and diagrams.

Version 3.1

It was discovered that there was no hardware component that satisfies the demand of exactly one security camera for Interior_Monitoring, why in this Version security-hardware-2 was added which fulfills the demand of the feature Interior_Monitoring. In addition, demands for the response time to the finger protection functionality are added.

Appendix [A.1.5](#page-66-0) shows the details in tables.

Version 4.0

In Version 4.0 a new feature Windows_Heatable is added as an optional child of BodyComfortSystem with its own StatusLED. A new software component windowsheat-controller (sw_6) is added, which demands the use of a temperature sensor that is already included by the wiper update.

Appendix [A.1.6](#page-67-0) shows the details in tables and diagrams.

Version 5.0

In Version 5.0 a new feature Automatic_Headlights is added as an optional child of BodyComfortSystemand the resource types number of parking lights, number of daytime running lights, number of low beams, number of high beams, number of ambient light sensors and number of front proximity sensors are added. These resource types are demanded by a new software component, the headlight-controller $(sw₇)$, and provided by a new hardware component, headlight-hardware.

Appendix [A.1.7](#page-68-0) shows the details in tables and diagrams.

Version 5.1

In response to customer feedback requesting more granular control over lighting options, Automatic_Headlights gets divided into three distinct choices: Beam, Parking_Lights, and Daytime_Running_Lights. Instead of a binary decision of whether to have automatic headlights or not, customers can now select from a range of automatic lighting options, tailoring their vehicle's lighting setup to better suit their needs and preferences.

Now the corresponding resource types can be removed and only number of ambient light sensors and number of front proximity sensors are kept from the previous version but with another ID. Also the headlight-controller (sw_7) now requests a certain Power Specification to light up or dim the different headlight features. The headlight-hardware now needs to provide a lot of Power instead of the Lights.

Appendix [A.1.8](#page-69-0) shows the details in tables and diagrams.

5. Evaluation

In this chapter we evaluate the implementation of the [UCM](#page-14-0) described in Chapter [3](#page-28-0) [\(SG](#page-14-2) 1 & 2) and the [SGE](#page-14-10) described in Chapter [3](#page-28-0) through the extended [BCS](#page-14-1)[-CS](#page-14-11) implemented in Chapter [4](#page-36-2) [\(SG](#page-14-2) 4). For the evaluation of our [SGs](#page-14-2) we derive the following Research Questions [\(RQs](#page-14-15)):

[RQ](#page-14-15) 1: Can the [UCM](#page-14-0) be used to reproduce realisation analysis?

With [RQ](#page-14-15) 1 we evaluate the first [SG](#page-14-2) which aims to unify and simplify existing tools and considerations as the four file solution of Ochs [\[Och23\]](#page-63-0) for realisation analysis using [FDs](#page-14-6) with corresponding resource provisions and demands. We will evaluate this goal, by replicating the results of Ochs [\[Och23\]](#page-63-0) [\(SG2](#page-14-2)). Therefore, we compare the sets of valid and realisable configurations of two [CSs](#page-14-11), once calculated from the four files and once calculated from our one file solution. We expect the sets to match exactly and then we can consider the implementation of the [UCM](#page-14-0) as complete and accurate in the parts the [CSs](#page-14-11) are covering.

[RQ](#page-14-15) 2: Can concepts of delta modelling be used to express variability in time in the extended [UCM?](#page-14-0)

With [RQ](#page-14-15) 2 we evaluate the third [SG](#page-14-2) which aims to include concepts of the [SGE](#page-14-10) to manage variability in time and transfer these concepts to the [UCM](#page-14-0) using time deltas. These deltas can express the [SGE](#page-14-10) variation types. We will evaluate this goal by verifying the capability to manage variability in time of our implementation with the [BCS-](#page-14-1)[CS](#page-14-11) evolution we created in [SG](#page-14-2) 4. We consider the sets of valid and realisable configurations of two successive versions of the [BCS-](#page-14-1)[CS](#page-14-11) as [GT.](#page-14-16) To calculate the [GT](#page-14-16) we use the approach provided by Ochs [\[Och23\]](#page-63-0). We then use our approach to identify the valid and realisable configurations for the [CS](#page-14-11) evolution an compare our results to the [GT.](#page-14-16) We expect the sets to match exactly and then we can consider the implementation of the [UCM](#page-14-0) as able to express variability in time. We also calculate the degree of change, a metric to express how much of the system changes from one system generation to another, for the [BCS](#page-14-1) evolution to show that the concepts of variation types of the [SGE](#page-14-10) can be used for cross-domain [PLs](#page-14-17).

5.1 Experiment Setup

5.1.1 Research Question 1

Ochs [\[Och23\]](#page-63-0) used four files to compute all the valid and realisable configurations, whereas our unified approach requires only one file containing the instance of the [UCM.](#page-14-0) This instance is instantiated with the [FM,](#page-14-9) the resource provisions and the resource types. The unified system model was developed in version 2.36.0.v20231107- 0612 of the [EMF](#page-14-3) using Java version 1.8. The combined problem solver used to compute the [GT](#page-14-16) and the modified version of the combined problem solver, which takes the serialised unified system as input and computes our results, were run in Python 1.10.

Ochs [\[Och23\]](#page-63-0) used two [CSs](#page-14-11), [CS](#page-14-11) 1 and the [BCS](#page-14-1)[-CS,](#page-14-11) to evaluate his results. The first [CS, CS](#page-14-11) 1, is used to maximize the coverage of the developed concepts and the [BCS](#page-14-1)[-CS](#page-14-11) to show that his work also scales to a typically used case study. The [CSs](#page-14-11) are explained in more detail below:

Case Study 1

Even though we only need one file, we will spread the explanation of [CS](#page-14-11) 1 over several representations for better clarity as we did before in Section [4.2](#page-39-0) for the [BCS](#page-14-1)[-CS.](#page-14-11)

[CS](#page-14-11) 1 covers a car [PL](#page-14-17) that aims to cover the twelve possible characteristics of resource types. Table [5.1](#page-50-0) shows these characteristics, which are the combination of the different values of the attributes isAdditive, isExclusive and boundary. The meaning of these attributes was discussed in Section [2.5.](#page-26-0)

The [FD](#page-14-6) of the [CS](#page-14-11) includes 13 features and no cross-tree constraints, as shown in Figure [5.1.](#page-49-0) The customer can choose between a big and a small infotainment system and whether or not he wants a tyre-pressure monitor and electric adjustable seats. If the customer decides to have electric adjustable seats there can be chosen between a 6-way and a 10-way seat adjustment and between front and back or only front motorization. Mandatory for all configurations is the monitoring for critical components. The allocation of resources to the features together with a software component is shown in Table [5.3](#page-51-0) and the resource provisions are shown in Table [5.3.](#page-51-0)

Figure 5.1: [FM](#page-14-9) of [CS1](#page-14-11)

ID	isAdditive	isExclusive	boundary	Unit	Description
θ	False	False	LOWER	MBit/s	Communication Bandwidth
1	False	False	UPPER	ms	Response Time
$\overline{2}$	False	False	EXACT	GHz	Infotainment Core Clock
3	False	True	LOWER	Mbit/s	CCM Communication Bandwidth
4	False	True	UPPER		CCM Screen Resolution
5	False	True	EXACT		Screen Resolution
6	True	False	LOWER	GByte	Memory
7	True	False	UPPER		no. Touchscreens
8	True	False	EXACT		no. Screens
9	True	True	LOWER		no. Seat Adjustment Actuators
10	True	True	UPPER		no. Seats
11	True	True	EXACT		no. Tyre Pressure Sensors

Table 5.1: Resource Types of [CS1](#page-14-11)

Hardware Component (hw_i)	Provisions $(r p_{\nu}^j)$
	$rp_0^0 = 15$
	$rp_1^0 = 50$
infotainment-hardware (hw_0)	$rp_2^0 = 3$
	$rp_6^0 = 8$
	$rp_7^0 = 1$
	$rp_3^1 = 5$
ccm-hardware (hw_1)	$rp_A^1 = 1$
	$rp_6^1 = 4$
	$rp_{8}^{1} = 1$
car-periphery-hardware (hw_2)	$rp_{5}^{2} = 1$
	$rp_{9}^{2} = 6$
	$rp_{10}^2 = 2$
	$rp_{11}^2 = 4$

Table 5.2: Resource Provisions of [CS1](#page-14-11)

Body Comfort System-Case Study Version 1.0

We use Version 1.0 of the [BCS](#page-14-1) evolution history, which we described in detail in Section [4.2.](#page-39-0)

Ochs [\[Och23\]](#page-63-0) used a modified version of the [BCS](#page-14-1)[-CS.](#page-14-11) Instead of the cross-tree constraint Control_Automatic $\Rightarrow \neg$ Manual_PW seen in Figure [4.1](#page-40-0) he used Control_Automatic ⇔ ¬ Manual_PW. This modification results in less valid and realisable configurations, because an equation is more stringent than an implication.

To obtain the corrected [GT](#page-14-16) consisting of the set of valid and realisable configurations we ran the combined problem solver of Ochs [\[Och23\]](#page-63-0) with the corrected data and collected the results as [GT.](#page-14-16)

Feature	Software Component sw_i	Resource Demands rd_k^i
infotainment-small	sw_0	$rd_0^0 = 5$ $rd_1^0 = 100$ $rd_2^0 = 1$ $rd_6^0 = 2$ $rd_7^0 = 1$
infotainment-big	sw_0	$rd_0^0 = 10$ $rd_1^0 = 100$ $rd_2^0 = 3$ $rd_6^0 = 6$ $rd_7^0 = 3$
critical-component-monitoring	sw_1	$rd_4^1=1$ $rd_6^1=2$ $rd_8^1 = 1$
	sw_2	$rd_3^2=2$ $rd_6^2=1$
electric-seats	sw_3	$rd_5^3 = 1$
seat-adjustment-6way	sw_3	$rd_9^3 = 6$
seat-adjustment-10way	sw_3	$rd_9^3 = 10$
seat-motorisation-front	sw_3	$rd_{10}^3 = 2$
seat-motorisation-front-back	sw_3	$rd_{10}^3 = 4$
tyre-pressure-monitoring	sw_4	$rd_{11}^4=4$

Table 5.3: Resource Demands of [CS1](#page-14-11)

5.1.2 Research Question 2

To show that the deltas in the [UCM](#page-14-0) are working as intended we create two serialised instances of the unified system to compare them to our [GT.](#page-14-16) The first instance consists of Version 1.0 of the [BCS-](#page-14-1)[CS](#page-14-11) and contains deltas representing what changes from Version 1.0 to Version 2.0, which adds the wiper system. The second instance consists of the first instance but the deltas are applied. We take the tool of Ochs [\[Och23\]](#page-63-0) to create the [GT](#page-14-16) consisting of the set of valid and realisable configurations for Version 1.0 and Version 2.0. For the evaluation we compare the sets of valid and realisable configurations of Version 1.0 [\(GT\)](#page-14-16) with the unified system instance with unapplied deltas and the sets of valid and realisable configurations of Version 2.0 [\(GT\)](#page-14-16) with the applied deltas instance. If the sets of realisable configurations are the same in each case we assume that our delta model works as intended.

Besides the verification of the integration of deltas we want to show that [SGE](#page-14-10) variation types can be applied to models outside the domain of mechanical engineering. Therefore, we calculate the complement of the degree of change, of the [FDs](#page-14-6) of the [BCS](#page-14-1) evolution we implemented in Chapter [4.](#page-36-2) We introduced the complement of the degree of change in Section [2.3](#page-24-0) as the share of [CVs](#page-14-14), δCV , i. Based on the size of the change, we expect a larger (more than 20%) or smaller (less than 20%) value for the degree of change. This expectation will serve as [GT](#page-14-16) for the comparison. For Version 1.0 we expect the degree of change to be at 100% because the whole system is new. For Version 1.1 we expect the degree of change to be 0% because no features are modified. For Version 2.0 we expect a high degree of change because many features are added, where the change to Version 3.0 is very small. The difference from Version 3.0 to Version 3.1 is expected to be 0% as no features are modified. The degree of change for Version 4.0 is expected to be low, but higher than of Version 3.0 and the degree of change of Version 5.0 is expected to be as low as the degree of change of Version 3.0. The degree of change of Version 5.1 is expected to be higher than the degree of change of Version 5.0 but lower than of Version 2.0.

5.2 Experiment Execution

For the first two experiments we need to calculate the valid and realisable configurations that will serve as [GT](#page-14-16) and our results. The [GT](#page-14-16) is calculated with the combined problem solver and our results are calculated with the modified combined problem solver, taking as input the unified system instances representing the [CSs](#page-14-11). To compare these sets we need to introduce a compare operator. According to Ochs [\[Och23\]](#page-63-0) two configuration sets (CS) are equal, $A \equiv_{CS} B$, if the cardinality of the sets are equal and for each configurations from the first set A there needs to be the same configuration in the second set B . A configuration is equal to another if both configurations have the same features selected.

For the [GT](#page-14-16) of the first experiment we run the combined problem solver of Ochs [\[Och23\]](#page-63-0) with the [FD](#page-14-6) and the [CNF](#page-14-8) representation of the [CS](#page-14-11) provided by the FeatureIDE and the [CSV](#page-14-7) files representing the resource types and resource provisions of the [CSs](#page-14-11). The files are provided by Ochs [\[Och23\]](#page-63-0). The files can also be rebuilt based on the figure and tables that describe each [CS.](#page-14-11) To calculate the valid and realisable configurations with the new method we first parse the files used to calculate the [GT](#page-14-16) into a unified system instance with the adapter tool we wrote and then serialise this instance to a file with the unified system serialise tool. The serialised file is processed by the modified version of the combined problem solver, that calculates our result. The [GT](#page-14-16) and our results are then compared by the evaluation tool we wrote.

For the second experiment we calculated the set of valid and realisable configurations that build the [GT](#page-14-16) for Version 1.0 and Version 2.0 of the [BCS-](#page-14-1)[CS](#page-14-11) with the combined problem solver. To calculate the [GT](#page-14-16) for Version 1.0 we can use the same files as before, and for Version 2.0 we obtain the necessary files by creating them based on the figure and tables of the [CS](#page-14-11) described in Section [4.2.](#page-39-0) To create the unified system instance with deltas we take the unified system of Version 1.0 of the [BCS](#page-14-1) and add deltas describing the added and modified features, mappings, resource types and resource provisions. We then serialise the unified system instance and apply the deltas we added to serialise the new state of the unified system instance. We calculate the sets of valid and realisable configurations based on the two unified system instances as in the experiment before. We then compare the set of valid and realisable configurations obtained from the unified system instance with the unapplied deltas with Version 1.0 of the [GT](#page-14-16) and the set of valid and realisable configurations obtained from the unified system instance with applied deltas with Version 2.0 of the [GT.](#page-14-16)

In the last experiment we calculated the degree of change or more specifically the complement of the degree of change for the [FDs](#page-14-6) of the [BCS](#page-14-1) to address the second part of the second [RQ.](#page-14-15) Therefore we counted the amount of features labelled as [CV,](#page-14-14) [EV](#page-14-13) and [PV](#page-14-12) and then calculated according to the formula in Section [2.3](#page-24-0) δ_{CV_i} for every [FD.](#page-14-6)

5.3 Results

Table [5.4](#page-53-0) shows the evaluation results for the first experiment. The number of valid configurations of [CS1](#page-14-11) is $|CS_{CS1}| = 20$ and of the [BCS](#page-14-1) is $|CS_{BCS-V1}| = 11616$. The number of valid and realisable configurations are expected to be $|RS_{CS1}^{GT}| = 4$ for [CS1](#page-14-11) and $|RS_{BCS}^{GT}| = 6528$ for the [BCS.](#page-14-1)

Table 5.4: Quantitative results of our results compared to the [GT](#page-14-16) for [CS1](#page-14-11) and [BCS.](#page-14-1)

We computed $|RS_{CS1}^R| = 4$ valid and realisable configurations for [CS1](#page-14-11) and $|RS_{BCS}^R| =$ 6528 for the [BCS.](#page-14-1) The number of valid and realisable configurations for both [CSs](#page-14-11) is equal to the expected number of the [GT.](#page-14-16) We then compared the sets of configura-tions with the set of the [GT](#page-14-16) and found an exact coverage $(RS_{CS1}^R \equiv_{CS} RS_{CS1}^{GT}$ and $RS_{BCS}^{R} \equiv_{CS} RS_{BCS}^{GT}$).

Table [5.5](#page-53-1) shows the evaluation results for the second experiment, including the [GT](#page-14-16) for Version 1.0 and 2.0 of the [BCS](#page-14-1) and the [BCS](#page-14-1) with deltas unapplied and deltas applied. The number of valid configurations for Version 1.0 of the [BCS](#page-14-1) is $|CS_{BCS-V1}| = 11616$ and for Version 2.0 is $|CS_{BCS-V2}| \ge 115055$. The number of valid and realisable configurations are expected to be $|RSS_{BCS-\Delta}^{GT}| = 6528$ for Version 1.0 of the [BCS](#page-14-1) and $|RS_{BCS-\Delta-Applied}^{GT}| = 55296$ for Version 2.0 of the [BCS.](#page-14-1)

Table 5.5: Quantitative results of our results compared to the [GT](#page-14-16) for unapplied and applied deltas to [BCS.](#page-14-1)

We computed $|RS_{BCS-\Delta}^R| = 6528$ valid and realisable configurations for the [BCS](#page-14-1) with unapplied deltas and $|RS_{BCS-\Delta-Applied}^{R}| = 55296$ for the [BCS](#page-14-1) with applied deltas. The number of valid and realisable configurations for both versions is equal to the expected number of the [GT.](#page-14-16) We then compared the sets of configurations with the set of the [GT](#page-14-16) and found an exact coverage $(RS_{BCS-\Delta}^{R} \equiv_{CS} RS_{BCS-\Delta}^{GT}$ and $RS_{BCS-\Delta-Applied}^{R} \equiv_{CS} RS_{BCS-\Delta-Applied}^{GT}$.

\mathcal{L}	Version	$ G_i $	PV_i	EV_i	$\delta_{CV,i}$	degree of change	GТ
θ	Version 1	28	28	0	0%	100%	100%
	Version 1.1	28	0	0	100\%	0%	0%
\mathcal{D}	Version 2	45	17	3	55.56\%	44.44\%	$>20\%$
3	Version 3	46		1	95.65%	4.35%	${<}20\%$
	Version 3.1	46	0	0	100\%	0%	0%
5	Version 4	48	2	3	89.58%	10.42\%	${<}20\%$
6	Version 5	49			95.92%	4.08%	${<}20\%$
	Version 5.1	52	3	2	90.38%	9.62%	${<}20\%$

Table [5.6](#page-54-0) shows the share of [CVs](#page-14-14) in the different versions of the [FM](#page-14-9) of the [BCS](#page-14-1) we calculated as the third experiment. The share of [CVs](#page-14-14), $\delta_{CV,i}$ is the complement of the degree of change.

Table 5.6: Share of [CVs](#page-14-14) of the [BCS](#page-14-1) [FMs](#page-14-9)

The proportion of [CVs](#page-14-14) in the first version is 0%, which corresponds to a degree of change of 100%, as in the [GT.](#page-14-16) The proportion of [CVs](#page-14-14) in Version 1.1 and Version 3.1 is also in line with the [GT](#page-14-16) at 100%. For Version 2 we can see from the table, almost half of the variations were not carried over, which is a high degree of change. Version 3.0 and Version 5.0 have a low degree of change of about 5%. Version 4.0 has a higher degree of change for than Version 3.0, but is also low at about 10% , as in Version 5.1.

5.4 Discussion

In the following we will answer the [RQs](#page-14-15) and discuss our results.

[RQ 1: Can the UCM be used to reproduce realisation analysis?](#page-48-0)

As shown in the section above, the [UCM](#page-14-0) can be used to reproduce realisation analysis. We showed that the implemented [UCM](#page-14-0) can be used for the computation of all valid and realisable features by reproducing the realisation analysis of Ochs [\[Och23\]](#page-63-0). We calculated the same sets of valid and realisable configurations using our unified system instances, leading to the conclusion that the [UCM](#page-14-0) can be used to reproduce realisation, which answers our first [RQ.](#page-14-15) We also showed the correctness of our [UCM](#page-14-0) implementation with respect to the representation of [FDs](#page-14-6) and solution space artefacts.

[RQ 2: Can concepts of delta modelling be used to express variability in time in](#page-48-1) [the extended UCM?](#page-48-1)

We integrated the concepts of delta modelling into the [UCM](#page-14-0) to express variability in time. To show that our implementation is capable of semantically expressing the differences between two versions, we performed a realisation analysis on the two versions and compared the resulting sets of valid and realisable configurations with the [GT.](#page-14-16) The exact coverage of the two sets leads to the conclusion that delta modelling concepts can be used to express variability in time in the [UCM,](#page-14-0) which answers the second [RQ.](#page-14-15) The third experiment showed that [SGE](#page-14-10) variation types can be applied to [FDs](#page-14-6). Therefore, we calculated the degree of change between successive versions of [FDs](#page-14-6), which were in the range we expected for each version as our [GT.](#page-14-16) This shows that the concepts of [SGE](#page-14-10) can be applied to models outside the domain of mechanical engineering. Although we have applied these concepts to another model, they cannot be applied in the same way to the variation we have implemented in the [UCM,](#page-14-0) because deltas in the [UCM](#page-14-0) may contain whole sub-trees or modelling elements that are not comparable to [FDs](#page-14-6). Further work can start here to develop appropriate concepts.

5.5 Threats to Validity

In this section we will discuss threats to validity. Firstly we will discuss internal threats relating to the the design and conduct of the evaluation and secondly external threats relating to generalisability.

5.5.1 Internal Threats to Validity

Our evaluation primarily focused on comparing sets of valid and realisable configurations, focusing mainly on features, constraints, resource types, mappings, hardware components, deltas and versions. This evaluation does not provide full coverage of all implemented classes in the [UCM,](#page-14-0) as certain elements such as Software Component and specific methods of the Delta Operations interface were not included. However, the classes and methods not included in the evaluation have very similar functionality to the classes covered by the evaluation. The included elements are therefore a representative sample of the system functionality, minimising the risk of malfunction in the elements not included. In addition, potential inconsistencies in the models and tools could lead to biases or errors. To counter this, we rely on existing and state of the art models and tools, which we only need to integrate or modify. This reduces risk as we do not have to develop everything from scratch. In addition, our reliance on the [GT](#page-14-16) formed by Ochs [\[Och23\]](#page-63-0) carries a significant risk, as any inaccuracies or discrepancies in this reference could affect our evaluation results. The risks may be migrated for the [GT](#page-14-16) formed by Ochs [\[Och23\]](#page-63-0) for the following reasons. The set of valid and realisable configurations is always smaller than the set of valid configurations. This is by design, because the [CSs](#page-14-11) were created in such a way that not every configuration is realisable even if it is valid. Also, the rule of which configurations are not realisable where made as simple as possible to allow manual verification. The valid configurations, unlike the valid and realisable configurations, were computed by the FeatureIDE which is a widely used tool. We also minimised the risk of errors in our model by using bi-directional parsing from FeatureIDE [FDs](#page-14-6) into a unified system instance. This parsing ensures that no data is lost in the parsing process and that the features and constraints work as intended.

5.5.2 External Threats to Validity

External threats to validity could limit the generalisability of the research findings. Firstly, the focus on the [BCS](#page-14-1)[-CS](#page-14-11) means that the findings may not be generalisable to other contexts. Focusing primarily on one [CS](#page-14-11) is not representative of other [PLs](#page-14-17). However, we used the [BCS](#page-14-1)[-CS](#page-14-11) in particular because, according to Müller et al. $[MLD⁺09]$ $[MLD⁺09]$, it was developed with experts to mimic a real [PL,](#page-14-17) which increases

the generalisability of the results of our experiment. Another threat to external validity are scalability issues, as the analysis is limited to computing the valid and realisable configurations for Version 1.0 and 2.0 of the [BCS-](#page-14-1)[CS,](#page-14-11) with later versions shown as too complex to compute in an acceptable time. This limitation can be explained by combinatorial explosion, where the number of possible combinations grows exponentially. Although we have not been able to compute the valid and realisable configurations for later versions, we have been able to model them as a unified system and, as demonstrated with Version 1.0 and Version 2.0 of the [BCS-](#page-14-1)[CS,](#page-14-11) given enough time it would be possible to compute the results for later versions. However, our work focuses on modelling and replicating existing results and since we have shown that our work can be used to replicate existing [CSs](#page-14-11) and we have not changed any analysis algorithms, as long as realisation analysis is possible with other methods, we can also perform it with our method.

6. Related Work

This chapter presents concepts and models that are relevant to our work. We analysed concepts that express variability in time or space within the domains of software engineering and mechanical engineering and approaches that introduce metamodels related to the [UCM.](#page-14-0)

Concepts to express Variability in Time and Space

Apel et al. [\[ABKS13\]](#page-62-0) divide [PL](#page-14-17) into problem and solution space and introduce the [FM](#page-14-9) as a model that allows the management of variability in space by the [FD](#page-14-6) as a graphical representation. The [SGE](#page-14-10) is a concept of expressing variability in time in the domain of mechanical engineering by expressing successor generations through different types of variations, starting from a previous generation, according to Albers et al. [\[ABR17\]](#page-62-1). The concept of delta modelling express the change operations to a system instance, this can be applied either to configurations to manage variability in space according to Schaefer [\[Sch10\]](#page-63-2) or to versions to manage variability in time according to Lity et al. [\[LKS16\]](#page-62-2). These concepts and models provide solutions for expressing variability in time or space. However, these preceding approaches cannot cover variability in time and space at the same time as in the case of the [FM](#page-14-9) and [SGE,](#page-14-10) or cannot provide realisation analysis because they do not cover problem and solution space. We integrated the expression of variability in time by adopting the idea of [FD](#page-14-6) and integrated the [SGE](#page-14-10) variation types through time deltas, which we also used to express variability in time. This allows us to cover variability in time and space and to cover problem and solution space through the unified approach of the [UCM.](#page-14-0)

Combined Variability Models

The [UCM](#page-14-0) is a metamodel proposed by Ananieva et al. [\[AGK](#page-62-3)⁺22] to express variability in time and space in [PLs](#page-14-17). The solution space of this model was extended by Wittler et al. [\[WKR22\]](#page-63-3) and Ochs [\[Och23\]](#page-63-0) with a more precise model that allow analyses such as realisation analysis. Our work replicates the realisation analysis by implementing the [UCM](#page-14-0) and performing the analysis directly on an instance of the [UCM,](#page-14-0) which was previously performed outside the boundaries of the model.

Consistency Models

Atkinson et al. [\[ASB10\]](#page-62-4) proposed the approach of a Single Underlying Model [\(SUM\)](#page-14-18) where a single, unified model serves as the foundation for multiple perspectives in view-based development. Burger [\[Bur13\]](#page-62-5) introduces Virtual [SUM](#page-14-18) [\(VSUM\)](#page-14-19) as a unified metamodel which is constructed by defining consistency relations between involved metamodels. The [UCM](#page-14-0) we developed can be seen as a [SUM,](#page-14-18) since the [UCM](#page-14-0) is the foundation for multiple different perspectives we combine, as variants through the integration of the [FD](#page-14-6) or versions through delta modelling. The [UCM](#page-14-0) already includes approaches for the mapping between features and the concrete realisation in the solution space by software and hardware components, but lacks a concrete realisation for maintaining constancy between features and their realisation in software and hardware components.

7. Conclusion and Outlook

This thesis addresses the description and management of variability in space and time of a generic [PL](#page-14-17) in a unified model. The [UCM](#page-14-0) is a model that unifies the problem and solution space and is able to describe variability in space and time. [FDs](#page-14-6) enable the management of variability in space and the [SGE](#page-14-10) is used in the domain of mechanical engineering to manage variability in time. We integrate these concepts into the [UCM](#page-14-0) to enable the management of variability in time and space.

We structured this thesis along the following [SGs](#page-14-2) we introduced in Chapter [1:](#page-16-0)

- [SG1](#page-14-2) [Implementation of the UCM in the EMF](#page-19-0)
- [SG2](#page-14-2) [Application study of the implementation \(SG 1\) based on the BCS with regard](#page-19-1) [to realisability](#page-19-1)
- [SG3](#page-14-2) [Development of a concept for the integration of the SGEM into the UCM with](#page-19-2) [regard to variability in time](#page-19-2)
- [SG4](#page-14-2) [Further development of the BCS by adding evolution](#page-19-3)

We addressed [SG](#page-14-2) 1 in Section [3.1](#page-28-1) and Section [4.1.](#page-36-0) Therefore, we extended the [UCM](#page-14-0) to allow us to manage variability in time. We then implemented the [UCM](#page-14-0) in the [EMF](#page-14-3) and also implemented adapters to import and export from and to FeatureIDE [FD](#page-14-6) serialisations. We also added adapters to import resource types and resource provisions from [CSV](#page-14-7) files as used by Ochs [\[Och23\]](#page-63-0). These adapted files can then be saved as serialised instance of [UCM](#page-14-0) to allow the application of analysis techniques such as realisation analysis.

[SG](#page-14-2) 2 was addressed in Chapter [5](#page-48-2) and Section [4.1.](#page-36-0) We implemented the tool support for the replication study of the solution space analysis proposed by Ochs [\[Och23\]](#page-63-0), where the realisation of valid configurations is addressed. We used the serialisation of the [UCM](#page-14-0) implemented in [SG](#page-14-2) 1 as input for the modified analysis method. In the evaluation, we investigated whether our implementation of the [UCM](#page-14-0) is able to reproduce existing realisation analysis results from Ochs [\[Och23\]](#page-63-0). We applied the realisation analysis method to two [CSs](#page-14-11) and then compared our results with the [GT,](#page-14-16) provided by Ochs [\[Och23\]](#page-63-0). We found exact coverage in the sets of valid and realisable configurations of both [CSs](#page-14-11), thus proving the applicability of our implementation of the [UCM.](#page-14-0)

[SG](#page-14-2) 3 was addressed in Section [3.2,](#page-31-0) where we used delta modelling to describe changes between two versions of a [PL.](#page-14-17) We integrate this concept into the [UCM,](#page-14-0) which enables it to express variability in time. The deltas, designed in the [UCM,](#page-14-0) can be labelled with the [SGE](#page-14-10) variation types, allowing the description of variation types in cross-domain [PLs](#page-14-17).

We addressed [SG](#page-14-2) 4 in Section [4.2](#page-39-0) and Chapter [5,](#page-48-2) where we applied our implementation of variability in time in the [UCM](#page-14-0) to the [BCS-](#page-14-1)[CS.](#page-14-11) Therefore, we extended the [BCS](#page-14-1) in terms of evolution and solution space artefacts, which allowed us to perform realisability analysis on the different versions of the [BCS.](#page-14-1) We used this realisability analysis to evaluate whether the implementation of the [UCM](#page-14-0) was able to semantically express differences between two versions with our concept of variability in time. We found an exact coverage of the sets of valid and realisable configurations, which we expressed by delta modelling and compared with the [GT.](#page-14-16) Thus, we showed that our concept of variability in time in the [UCM](#page-14-0) is capable of correctly specifying all changes between two versions of the subject system.

At the current state of our work, if a mapping points to a feature and the feature is removed, the model is inconsistent because the mappings feature reference points to a removed feature but is not itself removed. To circumvent such inconsistencies structure-preserving deltas could be added, which enable cascading deletions.

With the extended [UCM,](#page-14-0) we provide a metamodel that covers the management of variability in space and time in both the problem and solution space. This opens up opportunities for further development of tools for joint analysing of the problem and solution space, such as combined realisation analysis.

The [SGE](#page-14-10) variation types in our work are applied only to features, while originally in the domain of mechanical engineering the [SGE](#page-14-10) variation types were applied to hardware components. Since we label deltas with variation types and deltas can be applied to arbitrary elements in a metamodel, other elements could be considered for change analysis in future work.

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A. Appendix

A.1 Body Comfort System-Case Study

A.1.1 Version 1.0

See Section [4.2.](#page-39-0)

A.1.2 Version 1.1 - Safety

Table A.1: Resource Provisions of Version 1.1

A.1.3 Version 2.0 - Wiper System

See Section [4.2.](#page-39-0)

A.1.4 Version 3.0 - Electric Seat Adjustment Based on Key IDs

Figure A.1: [FM](#page-14-9) of [BCS](#page-14-1) Version 3.0

Table A.2: Resource Types added in Version 3.0

seat-controller (sw₅)

	Feature Software Component sw_i Resource Demands rd_k^i .	
Seat	sw_5	$rd_{11}^5=1$ $rd_{12}^5=2$ $rd_7^5 = 5$

Table A.3: Resource Demands added in Version 3.0

Hardware Component (hw_i)	Provisions $(r p_k^j)$
infotainment-hardware (hw_0)	$rp_0^0 = 8$ $rp_1^0 = 35$
	$rp_7^0 = 16$
	$rp_{11}^0 = 1$
	$rp_{12}^0 = 1$
	$rp_2^1 = 16$
$\texttt{security-hardware}(hw_1)$	$rp_{3}^{1}=700$
	$rp_{4}^{1}=1$
	$rp_{5}^{1}=4$
	$rp_3^2 = 10$
	$rp_6^2 = 4$
safety-hardware (hw_2)	$rp_{8}^{2} = 1$
	$rp_{9}^{2} = 1$
	$rp_{10}^2 = 1$

Table A.4: Resource Provisions of Version 3.0

A.1.5 Version 3.1 - Safer Passengers 2

Table A.5: Resource Types added in Version 3.1

Table A.6: Resource Demands added in Version 3.1

Hardware Component (hw_i)	Provisions $(r p_k^j)$
infotainment-hardware (hw_0)	$rp_0^0 = 12$ $rp_1^0 = 35$ $rp_7^0 = 16$ $rp_{11}^0 = 1$ $rp_{12}^0 = 1$
$\mathtt{security}$ -hardware (hw_1)	$rp_2^1 = 16$ $rp_{3}^{1}=700$ $rp_{4}^{1}=1$ $rp_{5}^{1}=4$
\texttt{safety} -hardware (hw_2)	$rp_3^2 = 10$ $rp_6^2 = 4$ $rp_s^2 = 1$ $rp_{9}^{2} = 1$ $rp_{10}^2 = 1$ $rp_{13}^2=2$
security-hardware-2 (hw_3)	$rp_5^3 = 1$

Table A.7: Resource Provisions added in Version 3.1

A.1.6 Version 4.0 - Heatable Windows

Figure A.2: [FM](#page-14-9) of [BCS](#page-14-1) Version 4.0

windows-heat-controller (sw_6)

Table A.8: Resource Demands added in Version 4.0

A.1.7 Version 5.0 - Automatic Headlights

Figure A.3: [FM](#page-14-9) of [BCS](#page-14-1) Version 5.0

		ID isAdditive isExclusive boundary Unit Description		
14	True	True	LOWER	no. Parking Lights
15	True	True	LOWER	no. Daytime Running Lights
16	True	True	LOWER	no. Low Beam
17	True	True	LOWER	no. High Beam
18	True	False	LOWER	no. Ambient Light Sensor
19	True	False	LOWER	no. Front Proximity Sensor

Table A.9: Resource Types added in Version 5.0

headlight−controller (sw7)

Feature	Software Component sw_i Resource Demands rd_k^i	
Automatic_Headlights	sw_7	$rd_{14}^7=1$ $rd_{15}^7 = 1$ $rd_{16}^{7} = 1$ $rd_{17}^7=1$ $rd_{18}^7 = 1$ $rd_{19}^{7} = 1$

Table A.10: Resource Demands added in Version 5.0

Hardware Component (hw_i) Provisions (rp_k^j)	
headlight-hardware (hw_4)	$rp_{14}^4=1$ $rp_{15}^4 = 1$ $rp_{16}^4 = 1$ $rp_{17}^4 = 1$ $rp_{18}^4 = 1$ $rp_{19}^4=1$

Table A.11: Resource Provisions added in Version 5.0

A.1.8 Version 5.1 - Automatic Headlights Decisions

Figure A.4: [FM](#page-14-9) of Version 5.1 [BCS](#page-14-1)

ID		is Additive is Exclusive boundary Unit Description		
	True	True	LOWER	no. Parking Lights
-15	True	True	LOWER	no. Daytime Running Lights-
–16	True	True	LOWER	no. Low Beam
$\frac{17}{1}$	True	True	LOWER	no. High Beam
1814	True	False	LOWER	no. Ambient Light Sensor
1915	True	False	LOWER	no. Front Proximity Sensor

Table A.12: Resource Types added and removed in Version 5.1

Table A.13: Resource Demands added and removed in Version 5.1

Table A.14: Resource Provisions modified in Version 5.1

A.2 Modified Unified Conceptual Model Full

