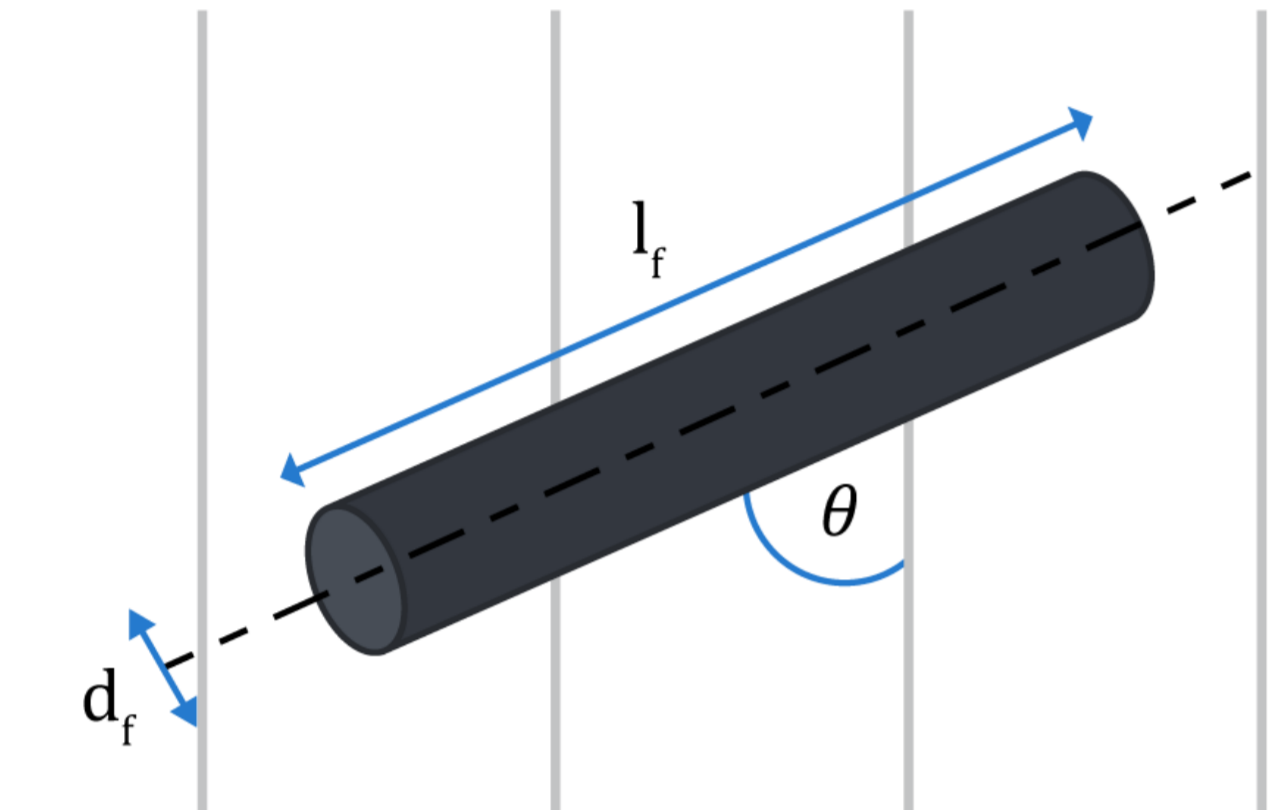


# Numerical Simulation of Fiber Deposition Behavior in an Air-Liquid Interface Exposure System

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### Fiber geometries and their description

Fiber diameter  $d_f$   
Fiber length  $l_f$   
Aspect ratio  $\beta = \frac{l_f}{d_f}$   
Angle of fiber orientation  $\theta$



Determining the shape factor ( $\chi$ ) using the elongated ellipsoid of revolution method!

### Shape factor and drag force

For motion **parallel** to the streamlines:  

$$\chi^{\parallel} = \frac{4}{3}(\beta^2 - 1) / \left\{ \frac{2\beta^2 - 1}{\sqrt{\beta^2 - 1}} \cdot \ln[\beta + \sqrt{\beta^2 - 1}] - \beta \right\}$$

For motion **perpendicular** to the streamlines:  

$$\chi^{\perp} = \frac{8}{3}(\beta^2 - 1) / \left\{ \frac{2\beta^2 - 3}{\sqrt{\beta^2 - 1}} \cdot \ln[\beta + \sqrt{\beta^2 - 1}] + \beta \right\}$$

For **any** motion:  

$$\chi = \chi^{\parallel} \cos^2(\theta) + \chi^{\perp} \sin^2(\theta)$$

↓ Brownian rotation

$$\chi = \frac{1}{3}\chi^{\parallel} + \frac{2}{3}\chi^{\perp} \rightarrow F_D = 3\pi\eta v_{rel}\chi d_f / C_c$$

### Particle forces and aerodynamic diameter

Gravity:  

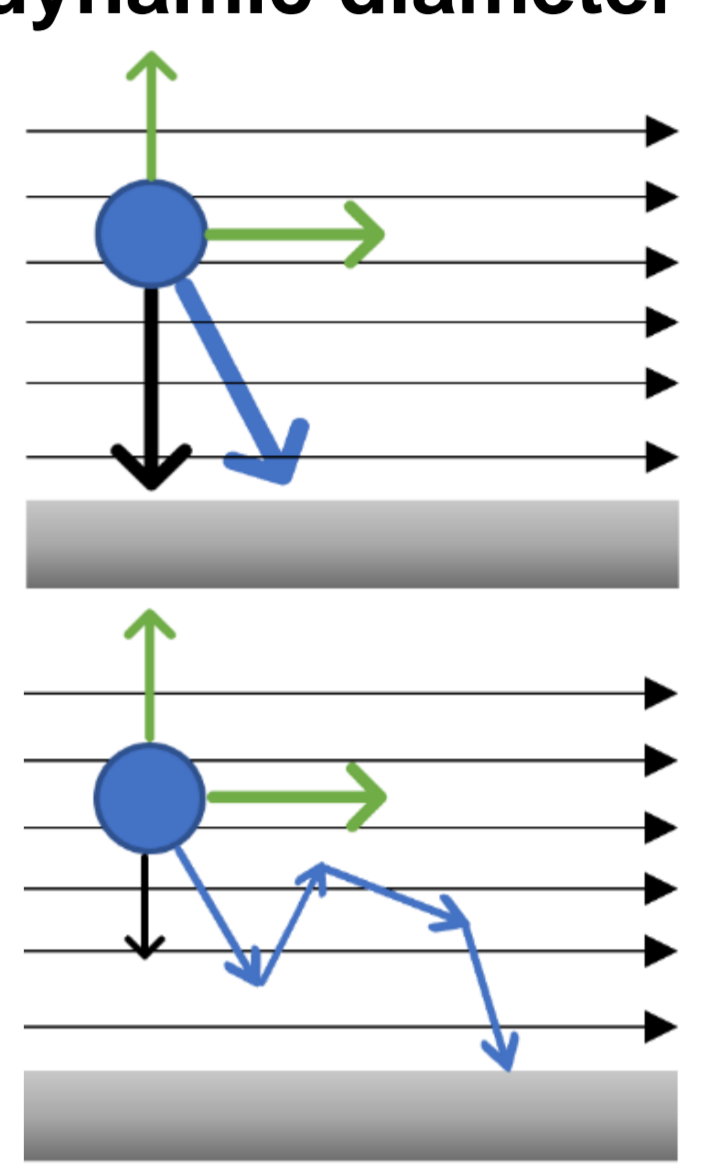
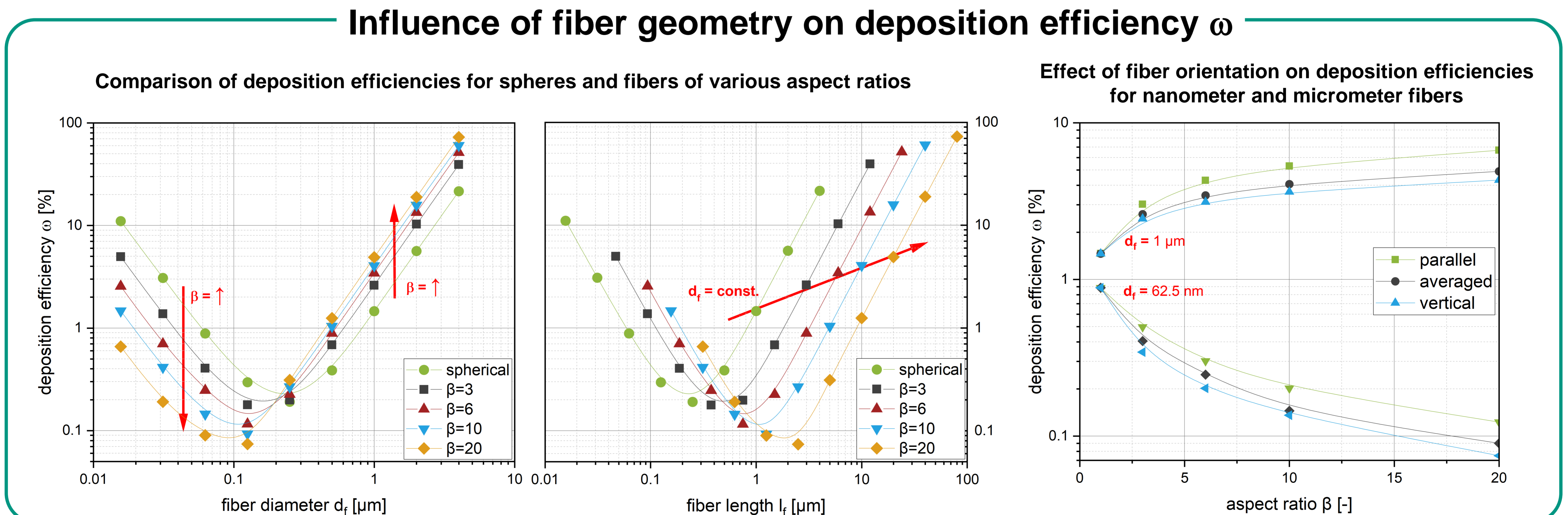
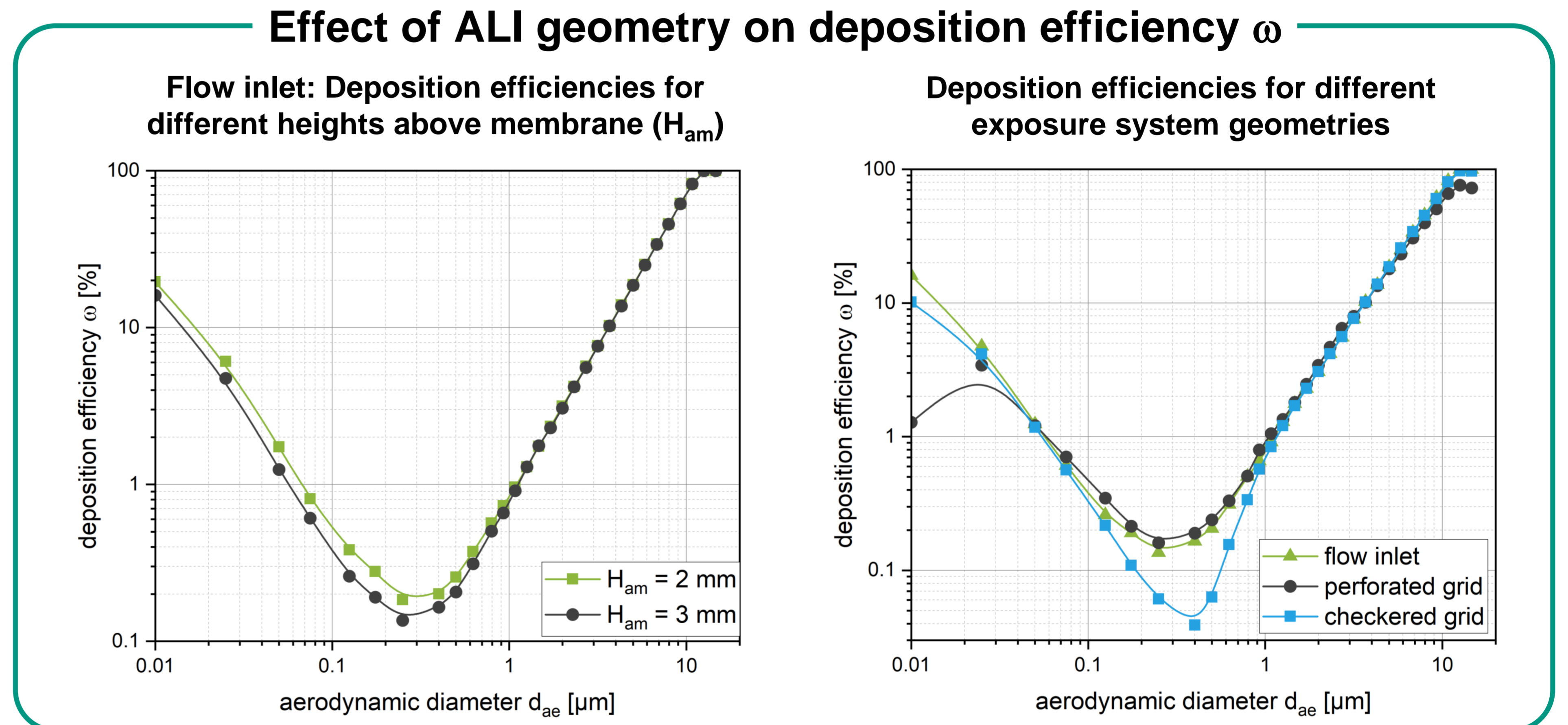
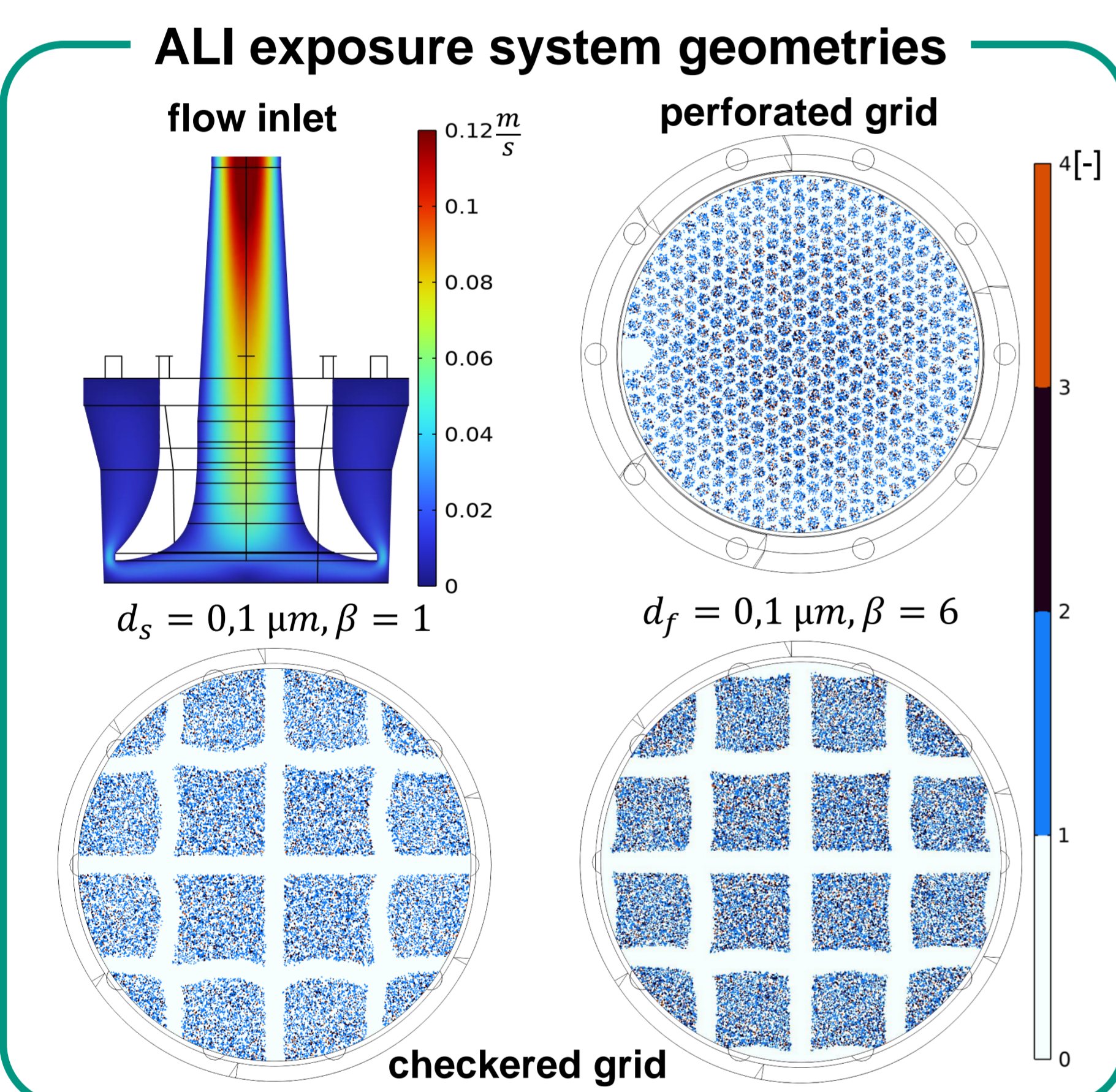
$$F_G = \frac{\pi}{6} d_v^3 (\rho_p - \rho_g) g$$

Diffusion:  

$$F_B = \xi \sqrt{\frac{12\pi k_B \eta T d_v}{\Delta t}}$$

Electric force:  $F_E = eZE$

Aerodynamic diameter:  $d_{ae} = d_f \sqrt{\frac{\rho_p \beta}{\rho_0 \chi}}$


### References

1 Fuchs, N.A. (1964). The Mechanics of Aerosols. Pergamon Pr.: Oxford.

### More information

Please visit Poster 749:  
Numerical Simulation of Fibre Dose in an Air-Liquid-Interface Exposure System,  
Sonja Mülhopt et al.

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