

# The Large-scale Anisotropy and Flux (de)magnification of Ultrahigh-energy Cosmic Rays in the Galactic Magnetic Field

Teresa Bister<sup>1,[2](https://orcid.org/0000-0003-4005-0857)</sup>  $\bullet$ , Glennys R. Farrar<sup>[3](https://orcid.org/0000-0003-2417-5975)</sup> $\bullet$ [,](https://orcid.org/0000-0003-2417-5975) and Michael Unger<sup>4,[5](https://orcid.org/0000-0002-7651-0272)</sup>  $\bullet$ 

<sup>1</sup> Institute for Mathematics, Astrophysics and Particle Physics, Radboud University Nijmegen, Nijmegen, The Netherlands; [teresa.bister@ru.nl](mailto:teresa.bister@ru.nl) <sup>2</sup> Nationaal Instituut voor Subatomaire Fysica (NIKHEF), Science Park, Amsterd

Received 2024 August 19; revised 2024 October 4; accepted 2024 October 9; published 2024 October 30

#### Abstract

We calculate the arrival direction distribution of ultrahigh-energy cosmic rays (UHECRs) with a new suite of models of the Galactic magnetic field (GMF), assuming sources follow the large-scale structure of the Universe. Compared to previous GMF models, the amplitude of the dipole component of the UHECR arrival flux is significantly reduced. We find that the reduction is due to the accidentally coinciding position of the peak of the extragalactic UHECR flux and the boundary of strong flux demagnification due to the GMF toward the central region of the Galaxy. This serendipitous sensitivity of UHECR anisotropies to the GMF model will be a powerful probe of the source distribution as well as Galactic and extragalactic magnetic fields. Demagnification by the GMF also impacts the visibility of some popular source candidates.

Unified Astronomy Thesaurus concepts: [Cosmic ray astronomy](http://astrothesaurus.org/uat/324) (324); [Cosmic rays](http://astrothesaurus.org/uat/329) (329); [Cosmic ray sources](http://astrothesaurus.org/uat/328) ([328](http://astrothesaurus.org/uat/328)); [Extragalactic magnetic](http://astrothesaurus.org/uat/507) fields (507); [Milky Way magnetic](http://astrothesaurus.org/uat/1057) fields (1057); [Ultra-high-energy cosmic radiation](http://astrothesaurus.org/uat/1733) ([1733](http://astrothesaurus.org/uat/1733)); [Cosmic anisotropy](http://astrothesaurus.org/uat/316) (316); [Large-scale structure of the universe](http://astrothesaurus.org/uat/902) (902)

#### 1. Introduction

Ultrahigh-energy cosmic rays (UHECRs) are the highest energetic particles measured at Earth, with energies from  $10^{18}$ to beyond  $10^{20}$  eV. Their origin remains unclear, mainly because UHECRs are charged nuclei that are deflected by cosmic magnetic fields during their propagation from the sources to Earth. Hence, the directions of sources can only be reconstructed from the UHECR arrival directions when magnetic field deflections are appropriately accounted for. A large part of the effect comes from the Galactic magnetic field (GMF) of the Milky Way, which has a field strength of order  $\mu$ G extending over tens of kiloparsecs. The mass composition of UHECRs becomes heavier with increasing energy  $E(A, Aab)$ et al. [2014](#page-11-0)), with a relatively narrow range of rigidities  $\mathcal{R} \equiv E/Ze \approx 5 \text{ EV}$  (T. Bister & G. R. Farrar [2024](#page-11-0)), for energies  $E \gtrsim 8$  EeV relevant for this work. The Larmor radius of UHECRs is ~5.5 kpc ( $\mathcal{R}/5$  EV)/(B/ $\mu$ G)—hence the GMF has a sizable impact on the propagation of UHECRs.

In recent years, the Jansson–Farrar GMF model from 2012  $(JF12; R. Jansson & G. R. Farrar 2012a, 2012b)$  $(JF12; R. Jansson & G. R. Farrar 2012a, 2012b)$  $(JF12; R. Jansson & G. R. Farrar 2012a, 2012b)$  $(JF12; R. Jansson & G. R. Farrar 2012a, 2012b)$  $(JF12; R. Jansson & G. R. Farrar 2012a, 2012b)$  has been used to test hypotheses about the sources of UHECRs from irregularities in the UHECR arrival directions (e.g., N. Globus et al. [2019](#page-11-0), [2023;](#page-11-0) B. Eichmann & T. Winchen [2020;](#page-11-0) C. Ding et al. [2021](#page-11-0); D. Allard et al. [2022](#page-11-0); B. Eichmann [2022;](#page-11-0) T. Bister  $\&$  G. R. Farrar [2024](#page-11-0)), but the robustness of the conclusions of these studies was difficult to assess due to the absence of realistic alternative GMF models that also fit the full data. Several GMF models fit only Faraday rotation measures (RMs) but not polarized synchrotron emission, and some models only fit for the disk field; see T. Jaffe ([2019](#page-11-0)) and references therein;

Original content from this work may be used under the terms  $\left(\mathrm{cc}\right)$ of the [Creative Commons Attribution 4.0 licence.](http://creativecommons.org/licenses/by/4.0/) Any further distribution of this work must maintain attribution to the author(s) and the title of the work, journal citation and DOI.

see also A. Korochkin et al. ([2024](#page-11-0)) for a recent study of the GMF halo component using high-latitude RMs and polarized synchrotron emission. For comparisons of UHECR anisotropy predictions by some of those models and JF12 see, e.g., M. Erdmann et al. ([2016](#page-11-0)), A. di Matteo & P. Tinyakov ([2018](#page-11-0)), and D. Allard et al. ([2022](#page-11-0)).

Many of the references given above aim at modeling the dipole—the only currently significant anisotropy in the arrival directions of UHECRs at  $E > 8$  EeV (The Pierre Auger Collaboration et al. [2017;](#page-11-0) A. Aab et al. [2018](#page-11-0)). It has a magnitude of  $\sim$ 7.3% and a current significance of 6.9 $\sigma$ (G. Golup [2023](#page-11-0)) in the field of view of the Pierre Auger Observatory (The Pierre Auger Collaboration [2015](#page-11-0)). All higher multipole moments, however, are compatible with isotropy, according to the joint analysis of the Pierre Auger and Telescope Array collaborations (A. Aab et al. [2018;](#page-11-0) L. Caccianiga et al. [2023](#page-11-0)). Using the JF12 model for the GMF, it was verified by T. Bister & G. R. Farrar  $(2024)$  $(2024)$  $(2024)$  that the dipole amplitude including its energy dependence can be explained rather well if UHECR sources follow the extragalactic matter distribution and hence the large-scale structure (LSS) of the Universe, while the measured dipole direction is only roughly right. Additionally, constraints on the source number density and the extragalactic magnetic field (EGMF) smearing were derived by requiring that all higher multipoles are compatible with isotropy.

Recently, new modeling of the GMF has become available in M. Unger & G. R. Farrar  $(2024)$  $(2024)$  $(2024)$ , hereafter [UF23](#page-11-0). In addition to being based on the latest astronomical data, [UF23](#page-11-0) provides a suite of models using a variety of improved functional forms for the field and for the thermal and cosmic-ray electron densities that are needed to predict the observables (RMs and polarized synchrotron emission), intended to encapsulate the uncertainty in the coherent GMF. In this work, we discuss the predictions of the large-scale distribution of arriving UHECRs

<span id="page-1-0"></span>according to the new [UF23](#page-11-0) GMF models. We show in particular the important influence of the magnification and demagnification effect of the GMF.

The relevance of the anisotropic (de)magnification due to the GMF is amplified by the fact that due to energy losses in propagation, the "UHECR illumination" of the Galaxy is quite inhomogeneous. If the source density is high enough that the source distribution reflects the distribution of matter (and UHECRs are not magnetically trapped within nearby Galaxy clusters; A. Condorelli et al. [2023](#page-11-0)), the flux of UHECRs above 8 EeV arriving at the Galaxy will be considerably enhanced in the direction of the Virgo cluster and Great Attractor (see Figure 2 of T. Bister & G. R. Farrar [2024](#page-11-0)). As we show, the alignment of the quite concentrated illumination map with the boundary of GMF demagnification has a strong impact on the predicted dipole magnitude and direction, enabling greater sensitivity in probing the various contributing factors.

#### 2. Dependence of the Anisotropy on the GMF

We follow the analysis of T. Bister & G. R. Farrar  $(2024)$  $(2024)$  $(2024)$ , which refined and extended the work of C. Ding et al.  $(2021)$  $(2021)$  $(2021)$ , where the source distribution follows the extragalactic matter distribution based on CosmicFlows 2 (Y. Hoffman et al. [2018](#page-11-0)) within 350 Mpc, and a uniform source distribution is assumed for larger distances.<sup>6</sup> The UHECR emission spectrum was fitted to the measured cosmic-ray energy spectrum (A. Aab et al. [2020](#page-11-0)) and composition (A. Yushkov [2019](#page-11-0)) at Earth, and the sources were assumed to be identical. For calculating the GMF deflections, we use the eight new [UF23](#page-11-0) models of the coherent field and adopt the Planck retune (The Planck Collaboration et al. [2016](#page-11-0)) of the JF12 random field (R. Jansson & G. R. Farrar [2012a](#page-11-0); "Planck" in the following, but "Pl" in figures) as the baseline choice. The Planck-tuned random field scales down the amplitude of the JF12 random field, as well as refits some other parameters like the amplitude of the Perseus spiral arm, to take into account the improved component separation in WMAP7 and Planck with respect to WMAP5 upon which JF12 was based. We take  $l_c = 60$  pc as a benchmark coherence length and evaluate the influence of "Galactic variance" from the particular realization of the random field by using a second realization of that field. Additionally, we consider a model with  $l_c = 30$  pc. As a further set of comparisons, we also show predictions for the two JF12 models used by T. Bister & G. R. Farrar  $(2024)$  $(2024)$  $(2024)$ : the JF12 model with the original JF12 random field (R. Jansson  $\&$ G. R. Farrar [2012a,](#page-11-0) [2012b](#page-11-0); JF12-full) and the solely coherent version  $(JF12 - req)$ . To be able to judge the effect of the Planck-tuned random field against the original JF12 random field, we also show JF12 with the two realizations of the Planck random field with  $l_c = 60$  pc (JF12-Pl).

#### 2.1. Dipole Direction

In Figure [1,](#page-2-0) the predicted directions of the dipole are shown for the eight different [UF23](#page-11-0) models, as well as for the three tested JF12 models for different energy intervals. The dipole direction varies between energy bins for each GMF model despite the relatively constant rigidity. This is due to the

decreasing propagation length with the energy, which leads to a variation of the distribution of contributing sources between energy bins; see also T. Bister & G. R. Farrar ([2024](#page-11-0)). The [UF23](#page-11-0) models differ by up to ∼50° from each other, considering differences over all energy bins. In general, all models predict the dipole direction relatively close to the indicated  $1\sigma$  and  $2\sigma$  contours of the measured dipole direction, consistent with the origin of the dipole being the anisotropic extragalactic source distribution following the LSS. The dipole directions of the [UF23](#page-11-0) models are in general more south and further away from the Galactic center than found with the JF12 models, especially for lower energies. Additionally, it is visible that the differences between the two random field realizations with  $l_c = 60$  pc and the two tested coherence lengths  $(l_c = 30 \text{ pc}$  and  $l_c = 60 \text{ pc}$ ; see above) are around  $O(15^{\circ})$  at lower energies and  $O(5^{\circ})$  for  $E > 32$  EeV and are thus subdominant to the differences between models. Because the dipole direction hardly differs between the three JF12 models with entirely different random fields (Planck random field, JF12 random field, and no random field), the dipole directions of the [UF23](#page-11-0) models will probably be reasonably stable in regard to updates of the random field model.

The dipole direction depicted in Figure [1](#page-2-0) is calculated from the model for the idealized continuum case of infinite source number density<sup> $n_s = \infty$ . For a more realistic treatment where</sup> sources are discrete and randomly distributed following the LSS, variations of the dipole direction are expected due to cosmic variance. These variations increase strongly with decreasing  $n_s$ . As in T. Bister & G. R. Farrar ([2024](#page-11-0)), we investigate the influence of a finite source density by randomly drawing 10,000 explicit catalogs of sources from the continuous source distribution for each value of  $n<sub>s</sub>$ . The regions encompassing 68% of all dipole directions for the 10,000 simulations are shown in blue in Figure [1](#page-2-0) for the [UF23-](#page-11-0)base model and  $n_s = 10^{-3}$  Mpc<sup>-3</sup> (for reference, the density of Milky Way–like galaxies is  $n_s \sim 10^{-2} \text{ Mpc}^{-3}$ ; C. J. Conselice et al. [2016](#page-11-0)). The uncertainty due to cosmic variance in source locations is significantly greater than that from the variations between the different coherent models or realizations of the random field. This means that the systematic uncertainty in reconstructing the origin of the UHECR dipole is not dominated by the uncertainty on the GMF, within variations of the [UF23](#page-11-0) models. Even though subdominant, there are subtle differences between the individual [UF23](#page-11-0) models regarding how well they reproduce the measured dipole direction. This is discussed further in Appendix [A](#page-4-0).

#### 2.2. Dipole and Quadrupole Amplitudes

In addition to the dipole direction, the dipole amplitude and its energy evolution are important observables that should be reproduced. We choose the quadrupole moment as a representative of all higher multipoles as it is the first to be outside isotropic expectations (see Figure 10 of T. Bister & G. R. Farrar [2024](#page-11-0)), and its measured value including uncertainties is reported in L. Caccianiga et al. ([2023](#page-11-0)). Figure [2](#page-2-0) depicts the dipole and quadrupole moments for the

<sup>&</sup>lt;sup>6</sup> We checked that varying the source evolution outside of the CosmicFlows volume from  $(1 + z)^{0}$  to  $(1 + z)^{\pm 3}$  leads to relative differences of the predicted dipole amplitude  $\leq \pm 20\%$ , i.e., smaller than those from varying the coherent model of the GMF within the [UF23](#page-11-0) suite; see Figure [2](#page-2-0).

In this publication,  $n<sub>s</sub>$  is the density of *contributing* sources. It may be smaller than the actual density of sources if the source emission is strongly beamed (G. R. Farrar [2024](#page-11-0)). For transient sources, it is  $n_s \simeq \Gamma \tau$ , where  $\Gamma$  is the volumetric rate of the transients and  $\tau$  is the mean arrival time spread, which depends on the EGMF; see T. Bister & G. R. Farrar  $(2024)$  $(2024)$  $(2024)$  and references therein.

<span id="page-2-0"></span>

Figure 1. Predicted and measured dipole directions in Galactic coordinates: colored markers indicate the dipole directions for different coherent GMF models and two realizations of the random field with  $l_c = 60$  pc (duplicate heavy symbols) and one with  $l_c = 30$  pc (light symbols). The blue region shows the  $1\sigma$  uncertainty due to cosmic variance in the source positions, for the base model with  $l_c = 60$  pc and  $n_s = 10^{-3}$  Mpc<sup>-3</sup>. The black contours represent the 1 $\sigma$  and 2 $\sigma$  uncertainty domains of the measured dinole (G. Golun 2023) of the measured dipole (G. Golup [2023](#page-11-0)).



Figure 2. The markers show the dipole and quadrupole moments,  $d$  and  $Q$ , in the limit of continuous source density ( $n<sub>s</sub> = \infty$ ) for the various GMF models and energy  $>8$  EeV, as in Figure 1. The dashed curves show, for the base GMF model and different values of  $n_s$ , the  $1\sigma$  domain from cosmic variance. The gray regions mark the data  $1\sigma$  uncertainty for the dipole (G. Golup [2023](#page-11-0)) and the quadrupole (L. Caccianiga et al. [2023](#page-11-0)). Note that the measured quadrupole amplitude is not significant as it is compatible with isotropy within  $2\sigma$ .

different [UF23](#page-11-0) GMF models for various source densities. As the source density decreases, cosmic variance from one realization to the next increases, greatly expanding the variation in predictions relative to the case of high source density and increasing the mean values of the dipole and quadrupole amplitudes.

It is noteworthy how similar the dipole and also quadrupole amplitudes are for all [UF23](#page-11-0) models. The variations between different [UF23](#page-11-0) coherent field models are nearly as small as the variation between the tested random field realizations. The predictions of the [UF23](#page-11-0) and JF12 models are also similar for the quadrupole amplitude, when the same random field model is used. While we did not explore the sensitivity to the random field model for the [UF23](#page-11-0) suite, we did check for the three JF12 models covering a range of random magnetic field strengths and coherence lengths that the dipole and quadrupole moments decrease almost linearly with increasing amplitude of the turbulent field part—as expected since the random field smooths out the structure.

However, the dipole amplitude is distinctly smaller in the continuum limit for all [UF23](#page-11-0) models than for even the JF12full model, which has the strongest random field. As elucidated below, the reason for the reduced dipole amplitude with the [UF23](#page-11-0) models relative to the JF12 models can be traced to the interplay between the peaks in the extragalactic flux distribution and the region of strong demagnification from the GMF. On account of this intricate relation, conclusions on the compatible range of source number densities are presently subject to large uncertainties and may change in the future when updated models for the random part of the GMF and better constraints on its coherence length become available. Other uncertainties come from the EGMF, which is largely unknown, and the details of the large-scale structure. In the Appendix [B](#page-5-0), we discuss the possibility of a nonnegligible EGMF.

In Figure 2 we show how the  $1\sigma$  regions of dipole and quadrupole amplitudes evolve with the effective source number density,  $n_s$ , for the [UF23](#page-11-0)-base model. Details and a visualization of the dipole and quadrupole moments for all models and energy bins, including uncertainties, are given in Appendix [C.](#page-6-0) Cosmic variance leads to larger variations of the dipole and quadrupole amplitudes than the variations between the different [UF23](#page-11-0) models already for  $n_s = 10^{-2}$  Mpc<sup>-3</sup>. Therefore, conclusions on the source number density can be drawn with little sensitivity to the specific [UF23](#page-11-0) model. For large source densities, the dipole amplitude in the  $>8$  EeV energy bin is smaller than the measured one for all [UF23](#page-11-0) models.<sup>8</sup> Hence, contrary to the findings of T. Bister  $\&$ G. R. Farrar ([2024](#page-11-0)) using the JF12 model, which showed compatibility for  $n_s \ge 10^{-3.5}$  Mpc<sup>-3</sup>, the present analysis using the [UF23](#page-11-0) models is incompatible with the continuous case and fits best for smaller number density. For the dipole and quadrupole amplitudes of the [UF23](#page-11-0) models to be compatible with the measured ones for  $E \ge 8$  EeV within  $1\sigma$ , in at least a fraction of realizations, the source density has to be  $n_s \sim 10^{-4}$  Mpc<sup>-3</sup> (see also [A](#page-4-0)ppendices A and [C](#page-6-0)). We stress that, as will be discussed in the next section, this conclusion is potentially sensitive to the random field.

<sup>&</sup>lt;sup>8</sup> The mean source distance decreases with the energy on account of composition evolution and energy losses during propagation (see Figure 1 in T. Bister & G. R. Farrar [2024](#page-11-0)). Thus, the too low model dipole amplitude at lower energy cannot be increased by a local source in a suitable direction without increasing even more the already large amplitude for >32 EeV—at least if that source follows the same emission as all others (A. Abdul Halim et al. [2024](#page-11-0)).

<span id="page-3-0"></span>

Figure 3. (a) and (b) Magnification maps for rigidity  $R = 5 \text{ EV}$  (see the text for an explanation). Gray pixels are source directions contributing no events at Earth. Contours indicating the extragalactic directions with large flux (panel (c)) are shown in red. (c) The  $E > 8$  EeV illumination map calculated from the LSS model (T. Bister & G. R. Farrar [2024](#page-11-0)), showing the flux at the edge of the Galaxy.



**Figure 4.** Combined magnification maps for different rigidities of all [UF23](#page-11-0) models with Planck random field, including both  $l_c = 30$  pc and  $l_c = 60$  pc, the latter with two variations. The color bar displays the magnification range in directions where all models agree; for the white area there is no consensus among the models. The directions of source candidates are indicated by stars, and the marker size is proportional to 1/distance.

#### 3. (De)magnification by the GMF

To understand why the dipole amplitude predicted by the [UF23](#page-11-0) models in the continuum limit is so much lower than with the JF12 model, we show in Figure 3 the logarithm of the magnification for the base model and for the JF12-Pl model for  $R \equiv E/eZ = 5 \text{ EV}$  (the mean charge of UHECRs increases with the energy in such a way that the rigidity stays almost constant (A. Abdul Halim et al. [2023,](#page-11-0) [2024;](#page-11-0) D. Ehlert et al. [2023](#page-11-0)) at  $R \approx (5 \pm 3)$  EV over the whole energy range discussed here; see Figure 4 in T. Bister & G. R. Farrar [2024](#page-11-0)). The magnification is defined to be the flux from a standard source in the respective direction, relative to the flux in the absence of the GMF. Cosmic rays from some directions notably from sources behind the central region of the Galaxy are demagnified: they are deflected strongly and simply never reach the solar system. Since energy losses of UHECRs in their passage through the Galaxy are negligible, Liouville's theorem implies that the flux integrated over  $4\pi$  radians is preserved, and hence the existence of demagnified directions implies directions with magnification  $>1$ ; see G. R. Farrar & M. S. Sutherland ([2019](#page-11-0)) for more discussion of the mechanism and also D. Harari et al. ([2000](#page-11-0), [2002](#page-11-0)). Corresponding maps to Figure 3 for all [UF23](#page-11-0) models including also variations of the random field are displayed in Appendix [D](#page-8-0).

Comparing the magnification maps to the extragalactic flux distribution according to the LSS source model (illumination) shown in Figure  $3(c)$ , one sees that the peak flux is in a demagnified region for the [UF23](#page-11-0) models. By contrast, the JF12 model is neutral or even magnifies the flux from those

directions. The difference in magnification thus explains the significantly smaller dipole amplitude for the [UF23](#page-11-0) models compared to the JF12 model. Also, the invisible parts of the extragalactic illumination in the Galactic North explain why the direction of the dipole seen on Earth is displaced more toward the Galactic South for the [UF23](#page-11-0) models.

The systematic difference between the magnification maps of the [UF23](#page-11-0) models and JF12 in the region of the peak of the LSS illumination map that lead to the deviation in dipole amplitude can be traced to differences in the respective toroidal halo models. This will be discussed in a separate publication.

To extract the most robust predictions for (de)magnification in the [UF23](#page-11-0) model suite, we display in Figure 4 the combined magnification maps for all of the [UF23](#page-11-0) coherent and random field models studied, where the colored regions are regions of unanimity among the models and in the white regions there is no consensus (for comparison, we also show the respective maps for the JF12 model in Appendix [D](#page-8-0)). It is visible that the variations between models are not very large and that they all agree regarding the large central demagnified area. To demonstrate the implications of this, we also depict the directions of popular source candidates often used in the literature (e.g., J. H. Matthews et al. [2018](#page-11-0); P. Abreu et al. [2022](#page-11-0); B. Eichmann [2022](#page-11-0); A. Abdul Halim et al. [2024](#page-11-0)). Several of those candidates like M83, M87, Mkn421, Mkn501, Cen A, NGC 4945, and NGC 253 lie in the demagnification area for some or most rigidities  $R \leq 5$  EV or in some cases for all rigidities shown.

One further important consequence of the sensitivity of the dipole amplitude to the interplay between the illumination and

<span id="page-4-0"></span>GMF magnification maps is that the predicted dipole amplitude and direction differ substantially when the illumination is replaced by an idealized dipole with the same amplitude and direction—for example the "2MRS dipole," which is often used in the literature, e.g., The Pierre Auger Collaboration et al. ([2017](#page-11-0)), A. Aab et al. ([2018](#page-11-0)), J. D. Bray & A. M. M. Scaife ([2018](#page-11-0)), and A. Bakalová et al. ([2023](#page-11-0)). The amplitude of the predicted dipole is typically a factor of 2 larger with the idealized dipole than with the LSS model for the [UF23](#page-11-0) models, and its direction differs by  $O(20^{\circ} - 60^{\circ})$ ; see Figures in Appendix  $E$ . Thus, it is crucial to take into account the concentrated inhomogeneities in the UHECR arrival flux instead of using a smooth dipole approximation for the illumination map that is based on averaging the galaxy distribution over distances much larger than that of contributing sources.

#### 4. Conclusions

We have investigated the sensitivity of the predicted largescale anisotropy of UHECRs to the coherent part of the GMF and also made a preliminary study of the dependence on the random part of the field. We find that the measured dipole that has been detected in the UHECR arrival flux (The Pierre Auger Collaboration et al. [2017](#page-11-0); A. Aab et al. [2018](#page-11-0)) can be described reasonably well by a model where the sources follow the largescale structure of the universe and UHECRs are deflected by any of the suite of [UF23](#page-11-0) GMF models (as is also the case for the JF12 model; T. Bister & G. R. Farrar [2024](#page-11-0)). For the [UF23](#page-11-0) models, the best agreement with both dipole direction and dipole and quadrupole amplitudes is reached for source number densities of  $O(n_s) = 10^{-3}$  Mpc<sup>-3</sup> in the case of negligible EGMF.

The variations among the predicted dipole and quadrupole amplitudes, and among the dipole directions, when using different [UF23](#page-11-0) models including different setups of the random field are small and subdominant to cosmic variance from random source positioning. Hence, the uncertainty on UHECR arrival directions from the GMF modeling, within the [UF23](#page-11-0) family, will likely not obstruct conclusions about the sources of UHECRs based on their large-scale anisotropies. At the same time, we find enough differences among models, such that in the future with refined treatment of the random field, composition sensitivity, and LSS source modeling, it should be possible to disfavor or prefer some of the models.

An important discovery of our work, which goes beyond specific models of the GMF, is the unanticipated sensitivity of the dipole *amplitude* to the coherent field model. This results from the delicate interplay between demagnification of flux from sources behind the central portion of the galaxy and the direction of strongest extragalactic illumination from the Virgo cluster and Great Attractor. This sensitivity of the dipole amplitude will be a powerful tool to probe not only the GMF but also the UHECR source distribution and potentially even hadronic interaction models, which impact the charge assignment. The pattern of extragalactic illumination changes with UHECR energy, which should help in discriminating different contributing factors in the future.

The area of the sky where the flux is severely demagnified in the [UF23](#page-11-0) model suite includes popular source candidates like M87, M83, and NGC 253, which are thus not expected to contribute many UHECRs at Earth, except for rigidities  $\mathcal{R} > 5$  EV; see Figure [4](#page-3-0). Another consequence of the

demagnification is that using an idealized extragalactic dipole with the same direction and strength, but neglecting the intermediate-scale anisotropy due to energy losses, gives misleading results.

The delicate relationship between the direction and amplitude of the peak extragalactic flux and the blind directions resulting from GMF demagnification implies that conclusions about the GMF model and source number density are sensitive to details of the source distribution as well as the random part of the GMF and the possible influence of the EGMF. Thus conclusions about the UHECR source density and the relevance of cosmic variance in the source distribution must be left to the future when these aspects of the problem are better understood.

#### Acknowledgments

We thank Foteini Oikonomou for the useful feedback on our analysis. The work of T.B. is supported by a Radboud Excellence fellowship from Radboud University in Nijmegen, Netherlands, and that of G.R.F. is supported by National Science Foundation grant No. PHY-2013199. T.B. and M.U. thank the Center for Cosmology and Particle Physics of New York University for its kind hospitality, and T.B. acknowledges the support from the Alfred P. Sloan Foundation facilitating this research and the production of this Letter.

## Appendix A Agreement of the [UF23](#page-11-0) Models with Measured Dipole Directions and Multipole Amplitudes

Even when we cannot make strong judgments regarding the quality of the dipole direction prediction for the different models due to the large influence of cosmic variance and present uncertainties on the random field and the LSS distribution, it is still possible to determine which models lead to a better agreement with the data than others. Figure [5](#page-5-0) (left) shows the number of realizations of source locations (out of 10,000 total, for each  $n<sub>s</sub>$ ) for which the predicted dipole direction is within the  $2\sigma$  uncertainty of the measured dipole direction, simultaneously in all mutually exclusive energy bins  $E = (8-16)EeV$ ,  $E = (16-32)EeV$ , and  $E > 32 EeV$ . At large source number density, when cosmic variance between realizations is subdominant to the differences between models, there are substantial variations between the different [UF23](#page-11-0) models and between the different random field realizations. This can be compared to Figure [1,](#page-2-0) which shows the dipole directions in the continuous limit.

With decreasing source density, the number of compatible realizations decreases as expected since the variance of dipole directions increases. For source densities  $n_s \lesssim 10^{-3}$  Mpc<sup>-3</sup> (which gives better agreement with the measured dipole and quadrupole amplitudes than densities  $n_s \gtrsim 10^{-2}$  Mpc<sup>-3</sup> for the [UF23](#page-11-0) models, as shown in Figure [2](#page-2-0)), the differences between the models decrease, and it is clearly visible that the bulk of [UF23](#page-11-0) models gives a better fit to the dipole direction than the predecessor JF12 model. Comparing the eight [UF23](#page-11-0) models, no best model can be unambiguously identified due to the relatively large fluctuations between different random field setups (large Galactic variance) and the variation of the number of compatible simulations with the source number density, but it can be seen that the spur model consistently presents a worse fit to the dipole direction than the other models.

<span id="page-5-0"></span>

Figure 5. Number of random realizations of source locations, out of 10,000 total for each  $n<sub>s</sub>$ , for which the predicted dipole direction (left) or the dipole direction, dipole amplitude, and quadrupole amplitude all simultaneously (right) lie within the measured  $2\sigma$  uncertainty in all of the the mutually exclusive energy bins ( $E = (8$  $-16$ )EeV,  $E = (16-32)$ EeV, and  $E > 32$  EeV). Different GMF models are shown with different markers; their thickness indicates the random field coherence length, as in Figure [1](#page-2-0). Duplicate markers denote two realizations of the turbulent field for the same coherent field. The markers for each value of  $n_s/Mpc^{-3} = 10^{-6}$ ,  $10^{-5}$ ,...,10<sup>-2</sup> are offset on the x-axis for better visibility. The gray region (left) marks the range of  $n_s$  satisfying the dipole and quadrupole amplitudes discussed in the main text. For comparison, the arrows indicate estimates for the source number densities of different steady source candidate classes: Milky Way–like galaxies (C. J. Conselice et al. [2016](#page-11-0)), low-luminosity AGNs (L. C. Ho [2008](#page-11-0)), star-forming galaxies (C. Gruppioni et al. [2013](#page-11-0)), starburst galaxies (C. Gruppioni et al. [2013;](#page-11-0) K. Murase & M. Fukugita [2019](#page-11-0)), and high-luminosity AGNs (P. N. Best & T. M. Heckman [2012;](#page-11-0) C. Gruppioni et al. [2013](#page-11-0)).

We show in Figure 5 (right) the number of simulations out of 10,000 total where the dipole direction and the dipole amplitude *and* the quadrupole amplitude are all within  $2\sigma$  of the measured value. From Figure  $5$  (left) it is clear that because of cosmic variance, the number of simulations agreeing with the measured dipole direction decreases strongly with the source density. This is as expected and thus does not necessarily exclude small source densities. However, from Figure [2](#page-2-0) we know that densities  $n_s \lesssim 10^{-5}$  Mpc<sup>-3</sup> are disfavored (for negligible EGMF) as they lead to too large quadrupole amplitudes. Large source densities  $n_s \gtrsim$  $10^{-2}$  Mpc<sup>-3</sup> on the other hand generally lead to too small dipole amplitudes for the [UF23](#page-11-0) models. In general, agreement with all three observables is most often reached for  $n_s = 10^{-3}$  Mpc<sup>-3</sup> and especially for the twistX, expX, neCl and base models. These models can even reach a neCl, and base models. These models can even reach a compatible dipole amplitude for large source densities  $n_s = 10^{-2}$  Mpc<sup>-3</sup>. The random field realization plays a very large role in that case, and a compatibility with all three observables is only reached for few specific models. The nebCor, synCG, and cre10 models, even though being a fair fit for the dipole direction, as visible in Figure  $5$  (left), are less often compatible with the multipole amplitudes than the other models and are thus not favored according to Figure 5 (right). The spur model is also disfavored according to Figure 5 (right), but that is due to the dipole direction not fitting as well as explained above.

## Appendix B Influence of the EGMF

Another important impact on the anisotropy of the UHECR flux comes from the EGMF, which can dampen the multipole moments significantly. T. Bister  $\&$  G. R. Farrar ([2024](#page-11-0)) modeled this effect by a smoothing of the arrival flux of the following form (A. Achterberg et al. [1999](#page-11-0)):

$$
\delta\theta = 2^\circ \cdot 9 \frac{B}{nG} \frac{10 \text{ EV}}{E/Z} \frac{\sqrt{\overline{D} L_c}}{\text{Mpc}} = 2^\circ \cdot 9 \beta_{\text{EGMF}} \frac{10 \text{ EV}}{E/Z} \sqrt{\frac{\overline{D}}{\text{Mpc}}},\tag{B1}
$$

with the EGMF field strength  $B$ , the EGMF coherence length  $L_c$ , and the mean source distance  $\overline{D}$ . In the second equality, the combination  $\beta_{\text{EGMF}} \equiv B / nG \sqrt{L_c / Mpc}$  is introduced to isolate the quantity that can be constrained.

Using the JF12 model for the GMF, T. Bister & G. R. Farrar ([2024](#page-11-0)) investigated which combination of the EGMF parameter  $\beta_{\text{EGMF}}$  and the source density  $n_s$  can produce a large enough dipole moment while keeping all higher multipole moments small enough to agree with the data. Here, we update these findings using now the [UF23](#page-11-0) models for the GMF. For comparability we use the same definition of two criteria (note that these criteria are slightly different than the ones used above in the main text):

- 1. The dipole moment in the Auger field of view at  $E > 8$  EeV should be  $d_{8 \text{ EeV}} > 5\%$ . This value is around  $2.5\sigma$  below the value measured by Auger (G. Golup [2023](#page-11-0)), so it constitutes approximately a 99% C.L. lower limit on the dipole amplitude.
- 2. All the higher multipole moments  $C_{l>1}$  must be within the 99% isotropic expectation for all energy ranges  $(E = (8-16) \text{ EeV}, E > 8 \text{ EeV}, E = (16-32) \text{ EeV}, \text{ and}$  $E > 32$  EeV).

In Figure [6,](#page-6-0) the number of simulations that fulfill both criteria simultaneously is visualized, both for the JF12  $full$  and a selection of the [UF23](#page-11-0) models. Here we choose to show the base, nebCor, neCL, and twistX models. where the latter three exhibit the smallest and largest dipole

<span id="page-6-0"></span>

Figure 6. Combined constraints on the the source number density  $n_s$  and EGMF parameter  $\beta_{\text{EGMF}} \equiv B / nG \sqrt{L_c / Mpc}$ . Taken from T. Bister & G. R. Farrar ([2024;](#page-11-0) Figure [11](#page-11-0)), the gray filled contours with the intensity bar at the top show the number of simulations out of 1000 total, using the JF12 full model for the GMF, that have both a sufficiently large dipole and higher multipole moments small enough to be compatible with the 99% isotropic expectations as found for the data. The navy, light-blue, red, and green contours indicate the regions encompassing 1 (dotted), 20 (dashed), and 100 (solid) simulations that fulfill both criteria for the base, neCL, nebCor, and  $twistX$  models. Characteristic estimates of the number densities of some twistX models. Characteristic estimates of the number densities of some steady source candidates are shown with vertical lines: Milky Way–like galaxies (C. J. Conselice et al. [2016](#page-11-0)), low-luminosity AGNs (L. C. Ho [2008](#page-11-0)), star-forming galaxies (C. Gruppioni et al. [2013](#page-11-0)), starburst galaxies (C. Gruppioni et al. [2013;](#page-11-0) K. Murase & M. Fukugita [2019](#page-11-0)), high-luminosity AGNs (P. N. Best & T. M. Heckman [2012](#page-11-0); C. Gruppioni et al. [2013](#page-11-0)), and blazars (Ajello et al. [2013](#page-11-0)). Indicative loci of transient source candidates are shown with rotated lines (long gamma-ray bursts; D. Wanderman & T. Piran [2010](#page-11-0)), tidal disruption events (TDEs; S. van Velzen & G. R. Farrar [2014;](#page-11-0) I. Andreoni et al. [2022](#page-11-0)), and black hole–neutron star mergers (Abbott et al. [2023](#page-11-0)); see T. Bister & G. R. Farrar ([2024](#page-11-0)) for more details.

amplitudes and the largest quadrupole amplitude, respectively (Figure [7](#page-7-0)). While for the JF12 model negligible field strengths and very large source densities were preferred, for all shown [UF23](#page-11-0) models smaller source densities and larger EGMFs are favored. This is as expected due to the smaller dipole amplitudes with the [UF23](#page-11-0) models that have to be compensated by smaller source densities, as seen above. The parameter space that is compatible with the data is very broad and extends over multiple orders of magnitude in source density. The region where most simulations fulfill both criteria stated above is at very small source densities of around  $n_s \sim 10^{-8}$  Mpc<sup>-3</sup> in combination with a sizeable EGMF of around  $\beta_{\text{EGMF}} \sim 1 \text{ nG Mpc}^{1/2}$ . Comparing this to the densities of different source classes as indicated in Figure 6, the favored region overlaps with the density of blazars (Ajello et al. [2013](#page-11-0)). More abundant source classes like starburst galaxies, other types of active galactic nuclei (AGNs), or even Milky Way–like galaxies are, however, also all compatible with the [UF23](#page-11-0) models. The same is true for all transient source classes indicated in Figure 6. Note, as shown in Section [2](#page-1-0), the dipole direction is almost completely random for these small source densities.

As in the case without EGMF described above, the region of the parameter space of  $n_s$  and  $\beta_{\text{EGMF}}$  is very sensitive to the LSS model and the random part of the GMF and may hence be subject to change once updated models of that become available. Additionally, a more accurate treatment of the EGMF deflections than the simplified smearing we employ here could lead to changes of the compatible values for the source density and EGMF parameters.

# Appendix C Dipole and Quadrupole Amplitudes

In Figure [7](#page-7-0), we show the dipole and quadrupole amplitudes and their  $1\sigma$  uncertainties for various source number densities, for the different GMF models and no EGMF, as a function of energy.

<span id="page-7-0"></span>

Figure 7. Top row: the markers show the dipole and quadrupole moments, d and Q, in the limit of continuous source number density ( $n_s = \infty$ ) for the various GMF models. The black markers indicate the data 1σ uncertainty regions for the dipole (G. Golup [2023](#page-11-0)) and quadrupole (L. Caccianiga et al. 2023). Second–sixth row: when the density of sources is finite, cosmic variance in the source locations leads to variations of the dipole and quadrupole amplitude, here indicated by the error bar showing the inner 68% of the distribution (for one realization of the model with  $l_c = 60$  pc). For  $10^{-5}$  Mpc<sup>-3</sup>  $\le n_s \le 10^{-3}$  Mpc<sup>-3</sup>, both the [UF23](#page-11-0) dipole and quadrupole moments agree with the data within  $1\sigma$  for all models.

# Appendix D Additional Magnification Maps

<span id="page-8-0"></span>In Figure [8,](#page-9-0) the magnification maps for all [UF23](#page-11-0) models with  $l_c = 60$  pc, as well as for the JF12 models with different random field models, are shown. To determine how much the uncertainty on the random field influences the magnification map, we show in the second row the magnification maps for the base model with the three tested random fields (two realizations with  $l_c = 60$  pc and one with  $l_c = 30$  pc). The particular realization of the random field makes almost no difference to the magnification map, while the coherence length can have a visible impact. Especially the exact form and size of the demagnified region are sensitive to the coherence length.

Figure [9](#page-10-0) displays the combined magnification maps (see Section [3](#page-3-0) for an explanation) for all combinations of JF12 and random field models used in this work. It is visible that the areas of magnification and demagnification are distinctly different as for the [UF23](#page-11-0) models. Many of the depicted source candidates like Mkn501 and NGC 253 again lie in the demagnification area for rigidities  $R \le 5$  EV, but sources in the equatorial North like Mkn421 or M82 are significantly magnified with JF12 in contrast to [UF23](#page-11-0).

<span id="page-9-0"></span>THE ASTROPHYSICAL JOURNAL LETTERS, 975:L21 (12pp), 2024 November 1 Bister, Farrar, & Unger



(a) JF12-reg (compare to (Farrar & Suther-(b) JF12-full  $l_c = 30 \text{ pc}$  (compare to (Farrar(c) JF12 + Planck  $l_c = 60 \text{ pc}$ land 2019))  $&$  Sutherland 2019))



(d) UF23 base + Planck  $l_c = 60 \text{ pc}$ 

(e) UF23 base + Planck  $l_c = 60 \text{ pc}$ , 2nd realization

(f) UF23 base + Planck  $l_c = 30 \,\text{pc}$ 



(g) UF23 cre10 + Planck  $l_c = 60 \text{ pc}$ 

(h) UF23 expX + Planck  $l_c = 60 \text{ pc}$ 



(i) UF23 nebCor + Planck  $l_c = 60 \text{ pc}$ 



(j) UF23 neCL + Planck  $l_c = 60 \text{ pc}$ 







(l) UF23 synCG + Planck  $l_c = 60 \,\mathrm{pc}$ 



Figure 8. (a)–(m) Magnification maps for rigidity  $\mathcal{R} = 5$  EV (as in Figure [3](#page-3-0)) for various GMF models including also variations of the random field. Contours indicating the extragalactic directions with large flux predicted by the LSS model (panel (n)) are shown in red. (n) The  $E > 8$  EeV illumination map calculated from the LSS model (T. Bister & G. R. Farrar [2024](#page-11-0)), showing the flux at the edge of the Galaxy.

<span id="page-10-0"></span>

Figure 9. Combined magnification maps (as in Figure [4](#page-3-0)) for the JF12 model with the different random fields used in this work (JF12-regular, JF12-full with  $l_c$  = 30 pc, and JF12-Planck with  $l_c$  = 60 pc, the latter with two variations), illustrating the sensitivity of the magnification to the random field and—by comparing to Figure [4](#page-3-0)—the general differences between the JF12 and [UF23](#page-11-0) coherent models as a function of rigidity. The color bar displays the magnification range in directions where all combinations of JF12 and random models agree; for the white area there is no consensus among the models. The directions of source candidates are indicated by stars, and the marker size is proportional to  $1/\text{distance}$ .

## Appendix E Idealized Extragalactic Dipole

In Figure 10 we show the dipole amplitude predicted by the LSS model, compared to a model where the flux at the edge of the galaxy (the "illumination map," Figure  $3(c)$  $3(c)$ ) is replaced by an idealized dipole with the same amplitude and direction as for the LSS model. The amplitude of the LSS dipole at the edge of the galaxy is 6.2% for the  $E = (8-16)EeV$  energy bin, 8.1% for  $E > 8$  EeV, 11.9% for  $E = (16-32)$ EeV, and 21.5% for  $E > 32$  EeV (T. Bister & G. R. Farrar [2024](#page-11-0)). It is visible that the dipole amplitude is highly sensitive to the inhomogeneities in the extragalactic flux. For all shown [UF23](#page-11-0) models, the amplitude of the LSS model is significantly smaller (around a factor of 2) than for the model with idealized extragalactic dipole, while this relation is the other way around for the JF12-reg model. This is due to the intricate relation between the illumination and the magnification of the GMF, which differs significantly between the [UF23](#page-11-0) and JF12 models, as explained in the main text.

In Figure [11](#page-11-0), we show the dipole directions calculated when replacing the flux at the edge of the galaxy predicted by the LSS model by the idealized dipole. The direction of the dipole calculated at Earth differs substantially—by  $O(20^{\circ}$  to 60°)– between this simplification and the realistic model where the sources follow the LSS. Also, the direction predicted using the idealized dipole is systematically displaced toward the north, especially for lower energies, and moves significantly less with the energy than for the LSS model. Comparing the prediction for the base model with idealized dipole to the uncertainty contour from cosmic variance for  $n_s = 10^{-3}$  $n_s = 10^{-3}$  $n_s = 10^{-3}$  Mpc<sup>-3</sup> (Figure 1), it is visible that the predicted dipole direction of the idealized



Figure 10. Dipole amplitude dependence on the extragalactic flux: the thin markers indicate the predicted dipole amplitude for the LSS model (T. Bister & G. R. Farrar [2024](#page-11-0)) for selected GMF models. The respective thicker markers of the same form show the dipole amplitude prediction when the LSS illumination map is replaced by a smooth dipole with the same magnitude and direction demonstrating the sensitivity of the observed dipole amplitude to the inhomogeneities in the illumination map. The black markers represent the measured dipole amplitude and its  $1\sigma$  uncertainty (G. Golup [2023](#page-11-0)).

dipole model is even outside that sizable uncertainty for lower energies.

This test demonstrates that simply replacing an extragalactic source catalog by its dipole component (the "2MRS dipole," which is often used in the literature, e.g., The Pierre Auger Collaboration et al. [2017](#page-11-0); A. Aab et al. [2018;](#page-11-0) J. D. Bray & A. M. M. Scaife [2018](#page-11-0); A. Bakalová et al. [2023](#page-11-0)) and ignoring higher multipoles of the distribution can only give a rough idea of the deflection direction and expected dipole amplitude but should not be expected to produce accurate predictions of the expected anisotropy at Earth.

<span id="page-11-0"></span>THE ASTROPHYSICAL JOURNAL LETTERS, 975:L21 (12pp), 2024 November 1 Bister, Farrar, & Unger



Figure 11. Dipole direction dependence on the extragalactic flux, for different energy thresholds in Galactic coordinates: the thin markers indicate the predicted dipole directions for the LSS model (T. Bister & G. R. Farrar 2024) for selected GMF models. The respective thicker markers of the same form show the dipole direction prediction when the LSS illumination map is replaced by a smooth dipole with the same magnitude and direction—demonstrating the sensitivity of the observed dipole direction to the inhomogeneities in the illumination map. The black contours represent the  $1\sigma$  and  $2\sigma$  uncertainty domains of the measured dipole (G. Golup 2023).

#### ORCID iDs

Teresa Bister • [https:](https://orcid.org/0000-0003-4005-0857)//orcid.org/[0000-0003-4005-0857](https://orcid.org/0000-0003-4005-0857) Glennys R. Farrar  $\bullet$  [https:](https://orcid.org/0000-0003-2417-5975)//orcid.org/[0000-0003-2417-5975](https://orcid.org/0000-0003-2417-5975) Michael Unge[r](https://orcid.org/0000-0002-7651-0272) **the [https:](https://orcid.org/0000-0002-7651-0272)**//orcid.org/[0000-0002-7651-0272](https://orcid.org/0000-0002-7651-0272)

#### References

- Aab, A., Abreu, P., Aglietta, M., et al. 2014, [PhRvD,](https://doi.org/10.1103/PhysRevD.90.122006) [90, 122006](https://ui.adsabs.harvard.edu/abs/2014PhRvD..90l2006A/abstract)
- Aab, A., Abreu, P., Aglietta, M., et al. 2018, [ApJ](https://doi.org/10.3847/1538-4357/aae689), [868, 4](https://ui.adsabs.harvard.edu/abs/2018ApJ...868....4A/abstract)
- Aab, A., Abreu, P., Aglietta, M., et al. 2020, [PhRvD,](https://doi.org/10.1103/PhysRevD.102.062005) [102, 062005](https://ui.adsabs.harvard.edu/abs/2020PhRvD.102f2005A/abstract)
- Abbott, R., Abbott, T. D., Acernese, F., et al. 2023, [PhRvX,](https://doi.org/10.1103/PhysRevX.13.041039) [13, 041039](https://ui.adsabs.harvard.edu/abs/2023PhRvX..13d1039A/abstract)
- Abdul Halim, A., Abreu, P., Aglietta, M., et al. 2023, [JCAP,](https://doi.org/10.1088/1475-7516/2023/05/024) [2023, 024](https://ui.adsabs.harvard.edu/abs/2023JCAP...05..024A/abstract)
- Abdul Halim, A., Abreu, P., Aglietta, M., et al. 2024, [JCAP,](https://doi.org/10.1088/1475-7516/2024/01/022) [2024, 022](https://ui.adsabs.harvard.edu/abs/2024JCAP...01..022A/abstract)
- Abreu, P., Aglietta, M., Albury, J. M., et al. 2022, [ApJ,](https://doi.org/10.3847/1538-4357/ac7d4e) [935, 170](https://ui.adsabs.harvard.edu/abs/2022ApJ...935..170A/abstract)
- Achterberg, A., Gallant, Y. A., Norman, C. A., & Melrose, D. B. 1999, arXiv: astro-ph/[9907060](http://arxiv.org/abs/astro-ph/9907060)
- Ajello, M., Romani, R. W., Gasparrini, D., et al. 2013, [ApJ,](https://doi.org/10.1088/0004-637X/780/1/73) [780, 73](https://ui.adsabs.harvard.edu/abs/2014ApJ...780...73A/abstract)
- Allard, D., Aublin, J., Baret, B., & Parizot, E. 2022, [A&A](https://doi.org/10.1051/0004-6361/202142491), [664, A120](https://ui.adsabs.harvard.edu/abs/2022A&A...664A.120A/abstract)
- Andreoni, I., Coughlin, M. W., Perley, D. A., et al. 2022, [Natur](https://doi.org/10.1038/s41586-022-05465-8), [612, 430](https://ui.adsabs.harvard.edu/abs/2022Natur.612..430A/abstract)
- Bakalová, A., Vícha, J., & Trávníček, P. 2023, [JCAP,](https://doi.org/10.1088/1475-7516/2023/12/016) [2023, 016](https://ui.adsabs.harvard.edu/abs/2023JCAP...12..016B/abstract)
- Best, P. N., & Heckman, T. M. 2012, [MNRAS,](https://doi.org/10.1111/j.1365-2966.2012.20414.x) [421, 1569](https://ui.adsabs.harvard.edu/abs/2012MNRAS.421.1569B/abstract)
- Bister, T., & Farrar, G. R. 2024, [ApJ](https://doi.org/10.3847/1538-4357/ad2f3f), [966, 71](https://ui.adsabs.harvard.edu/abs/2024ApJ...966...71B/abstract)
- Bray, J. D., & Scaife, A. M. M. 2018, [ApJ](https://doi.org/10.3847/1538-4357/aac777), [861, 3](https://ui.adsabs.harvard.edu/abs/2018ApJ...861....3B/abstract)
- Caccianiga, L., Anchordoqui, L., Bianciotto, M., et al. 2023, ICRC ([Nagoya](https://doi.org/10.22323/1.444.0521)), 444, 521
- Condorelli, A., Biteau, J., & Adam, R. 2023, [ApJ,](https://doi.org/10.3847/1538-4357/acfeef) [957, 80](https://ui.adsabs.harvard.edu/abs/2023ApJ...957...80C/abstract)
- Conselice, C. J., Wilkinson, A., Duncan, K., & Mortlock, A. 2016, [ApJ,](https://doi.org/10.3847/0004-637X/830/2/83) [830, 83](https://ui.adsabs.harvard.edu/abs/2016ApJ...830...83C/abstract)
- di Matteo, A., & Tinyakov, P. 2018, [MNRAS,](https://doi.org/10.1093/mnras/sty277) [476, 715](https://ui.adsabs.harvard.edu/abs/2018MNRAS.476..715D/abstract)
- Ding, C., Globus, N., & Farrar, G. R. 2021, [ApJL](https://doi.org/10.3847/2041-8213/abf11e), [913, L13](https://ui.adsabs.harvard.edu/abs/2021ApJ...913L..13D/abstract)
- Ehlert, D., Oikonomou, F., & Unger, M. 2023, [PhRvD,](https://doi.org/10.1103/PhysRevD.107.103045) [107, 103045](https://ui.adsabs.harvard.edu/abs/2023PhRvD.107j3045E/abstract)
- Eichmann, B., Kachelrieß, M., & Oikonomou, F. 2022, [JCAP,](https://doi.org/10.1088/1475-7516/2022/07/006) [07, 006](https://ui.adsabs.harvard.edu/abs/2022JCAP...07..006E/abstract)
- Eichmann, B., & Winchen, T. 2020, [JCAP](https://doi.org/10.1088/1475-7516/2020/04/047), [2020, 047](https://ui.adsabs.harvard.edu/abs/2020JCAP...04..047E/abstract)
- Erdmann, M., Muller, G., Urban, M., & Wirtz, M. 2016, [APh](https://doi.org/10.1016/j.astropartphys.2016.10.002), [85, 54](https://ui.adsabs.harvard.edu/abs/2016APh....85...54E/abstract)
- Farrar, G. R. 2024, arXiv:[2405.12004](http://arxiv.org/abs/2405.12004)
- Farrar, G. R., & Sutherland, M. S. 2019, [JCAP,](https://doi.org/10.1088/1475-7516/2019/05/004) [2019, 004](https://ui.adsabs.harvard.edu/abs/2019JCAP...05..004F/abstract)
- Globus, N., Fedynitch, A., & Blandford, R. D. 2023, [ApJ,](https://doi.org/10.3847/1538-4357/acaf5f) [945, 12](https://ui.adsabs.harvard.edu/abs/2023ApJ...945...12G/abstract)
- Globus, N., Piran, T., Hoffman, Y., Carlesi, E., & Pomarede, D. 2019, [MNRAS](https://doi.org/10.1093/mnras/stz164), [484, 4167](https://ui.adsabs.harvard.edu/abs/2019MNRAS.484.4167G/abstract)
- Golup, G. & The Pierre Auger Collaboration 2023, ICRC ([Nagoya](https://doi.org/10.22323/1.444.0252)), 444, 252
- Gruppioni, C., Pozzi, F., Rodighiero, G., et al. 2013, [MNRAS](https://doi.org/10.1093/mnras/stt308), [432, 23](https://ui.adsabs.harvard.edu/abs/2013MNRAS.432...23G/abstract)
- Harari, D., Mollerach, S., & Roulet, E. 2000, [JHEP,](https://doi.org/10.1088/1126-6708/2000/02/035) [2000, 035](https://ui.adsabs.harvard.edu/abs/2000JHEP...02..035H/abstract)
- Harari, D., Mollerach, S., Roulet, E., & Sánchez, F. 2002, [JHEP,](https://doi.org/10.1088/1126-6708/2002/03/045) [2002, 045](https://ui.adsabs.harvard.edu/abs/2002JHEP...03..045H/abstract) Ho, L. C. 2008, [ARA&A,](https://doi.org/10.1146/annurev.astro.45.051806.110546) [46, 475](https://ui.adsabs.harvard.edu/abs/2008ARA&A..46..475H/abstract)
- Hoffman, Y., Carlesi, E., Pomarede, D., et al. 2018, [NatAs,](https://doi.org/10.1038/s41550-018-0502-4) [2, 680](https://ui.adsabs.harvard.edu/abs/2018NatAs...2..680H/abstract)
- Jaffe, T. 2019, [Galax,](https://doi.org/10.3390/galaxies7020052) [7, 52](https://ui.adsabs.harvard.edu/abs/2019Galax...7...52J/abstract)
- Jansson, R., & Farrar, G. R. 2012a, [ApJL,](https://doi.org/10.1088/2041-8205/761/1/L11) [761, L11](https://ui.adsabs.harvard.edu/abs/2012ApJ...761L..11J/abstract)
- Jansson, R., & Farrar, G. R. 2012b, [ApJ](https://doi.org/10.1088/0004-637X/757/1/14), [757, 14](https://ui.adsabs.harvard.edu/abs/2012ApJ...757...14J/abstract)
- Korochkin, A., Semikoz, D., & Tinyakov, P. 2024, arXiv:[2407.02148](http://arxiv.org/abs/2407.02148)
- Matthews, J. H., Bell, A. R., Blundell, K. M., & Araudo, A. T. 2018, [MNRAS:](https://doi.org/10.1093/mnrasl/sly099) [Letters,](https://doi.org/10.1093/mnrasl/sly099) [479, L76](https://ui.adsabs.harvard.edu/abs/2018MNRAS.479L..76M/abstract)
- Murase, K., & Fukugita, M. 2019, [PhRvD,](https://doi.org/10.1103/PhysRevD.99.063012) [99, 063012](https://ui.adsabs.harvard.edu/abs/2019PhRvD..99f3012M/abstract)
- The Pierre Auger Collaboration 2015, [NIMA](https://doi.org/10.1016/j.nima.2015.06.058), [798, 172](https://ui.adsabs.harvard.edu/abs/2015NIMPA.798..172P/abstract)
- The Pierre Auger Collaboration, Aab, A., Abreu, P., et al. 2017, [Sci,](https://doi.org/10.1126/science.aan4338) [357, 1266](https://ui.adsabs.harvard.edu/abs/2017Sci...357.1266P/abstract)
- The Planck Collaboration, Adam, R., Ade, P. A. R., et al. 2016, [A&A](https://doi.org/10.1051/0004-6361/201528033)[,](https://ui.adsabs.harvard.edu/abs/2016A&A...596A.103P/abstract) [596, A103](https://ui.adsabs.harvard.edu/abs/2016A&A...596A.103P/abstract)
- Unger, M., & Farrar, G. R. 2024, [ApJ](https://doi.org/10.3847/1538-4357/ad4a54), [970, 95](https://ui.adsabs.harvard.edu/abs/2024ApJ...970...95U/abstract)
- van Velzen, S., & Farrar, G. R. 2014, [ApJ](https://doi.org/10.1088/0004-637X/792/1/53), [792, 53](https://ui.adsabs.harvard.edu/abs/2014ApJ...792...53V/abstract)
- Wanderman, D., & Piran, T. 2010, [MNRAS,](https://doi.org/10.1111/j.1365-2966.2010.16787.x) [406, 1944](https://ui.adsabs.harvard.edu/abs/2010MNRAS.406.1944W/abstract)
- Yushkov, A. & The Pierre Auger Collaboration 2019, ICRC ([Madison, WI](https://doi.org/10.22323/1.358.0482))[,](https://ui.adsabs.harvard.edu/abs/2019ICRC...36..482Y/abstract) [358, 482](https://ui.adsabs.harvard.edu/abs/2019ICRC...36..482Y/abstract)