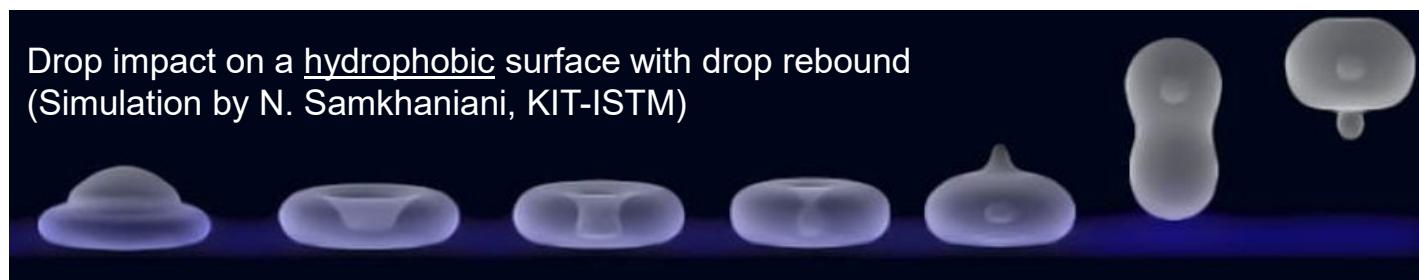
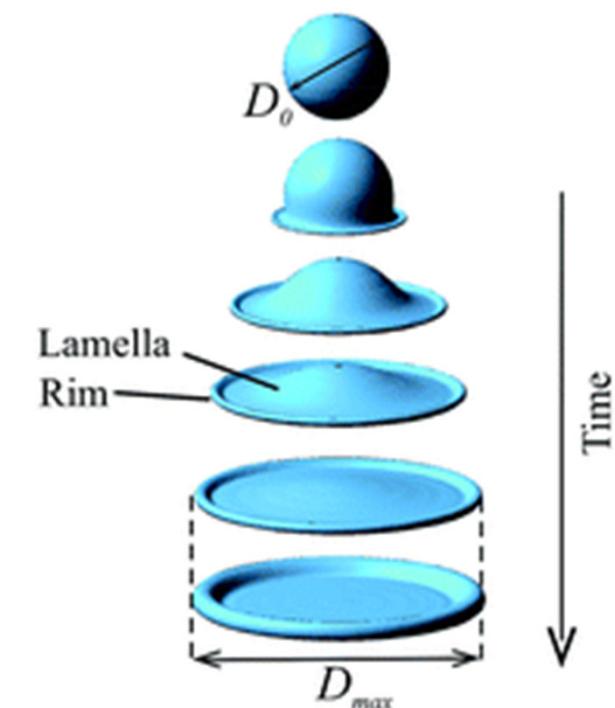


Entwicklung einer universellen analytischen Beziehung für die maximale Ausbreitung eines Tropfens beim Aufprall auf eine Wand

Development of a universal analytical relationship for the maximum spread of a drop when hitting a wall



Wörner et al., *Applied Mathematical Modeling* **95** (2021) 53-73

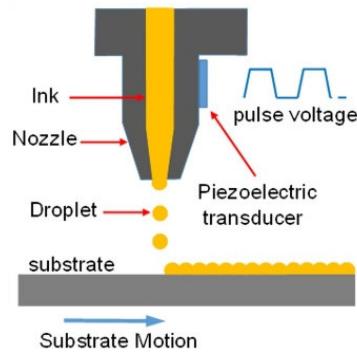


Agriculture spraying of pesticides



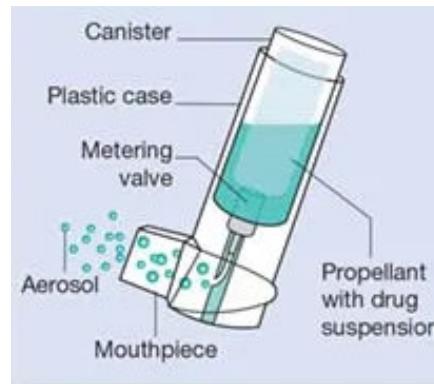
www.spektrum.de

Manufacturing inkjet printed solar cells



www.helmholtz-berlin.de

Medicine aerosol drug delivery



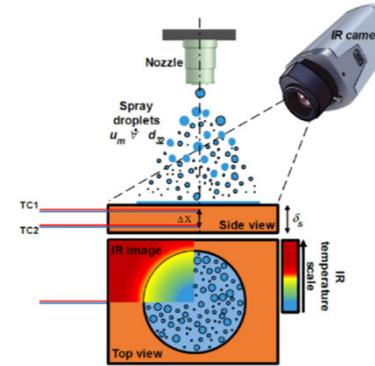
nursekey.com

Forensic bloodstain pattern



en.wikipedia.org

Heat transfer spray cooling



Benther et al. IJHMT (2021)

CRC/Transregio 150 Turbulent, chemically reactive multi-phase flows near walls

Internal combustion engine Fuel spray

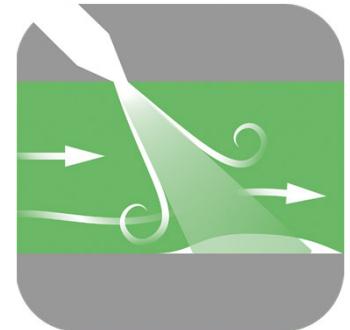


Varnishing spray painting



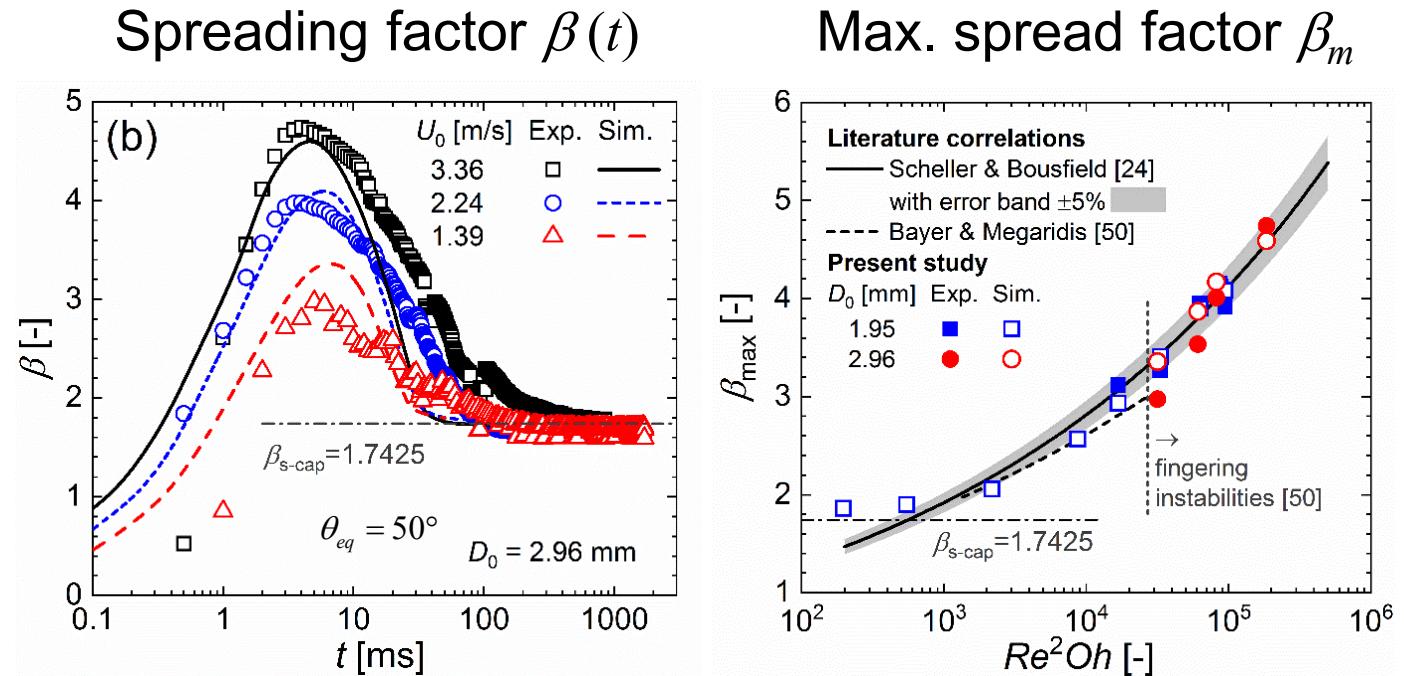
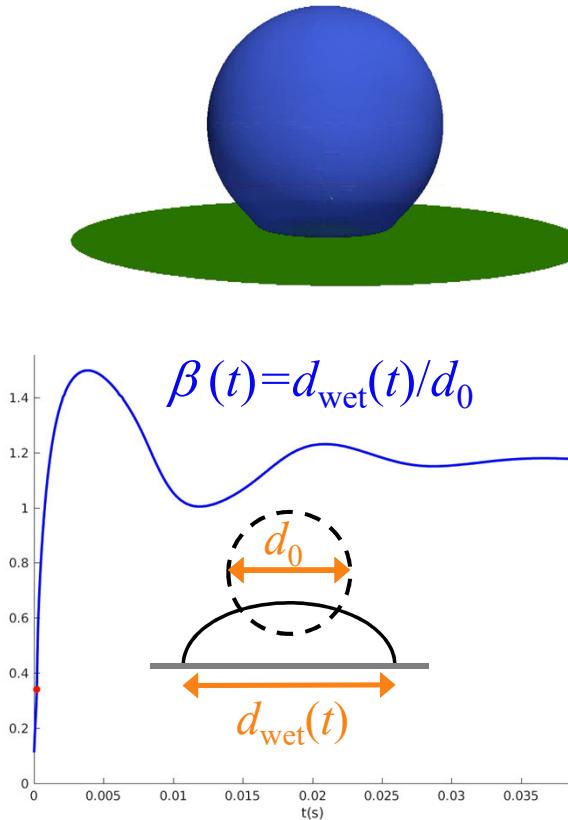
www.durr.com

Exhaust pipe AdBlue spray



Motivation

- Predicting the interaction of a single drop with a dry horizontal surface



 M. Börnhorst, X. Cai, M. Wörner, O. Deutschmann, Maximum spreading of urea water solution during drop impingement, *Chem. Eng. Technol.* **42** (2019) 2419-2427

Objective

- Maximum spread diameter depends on physical properties, on drop size/velocity and on wettability of the solid surface

■ Weber number $We = \rho d_0 u_0^2 / \sigma$

■ Reynolds number $Re = \rho d_0 u_0 / \mu$ (or $Oh = \sqrt{We}/Re$)

■ Contact angle θ (static, equilibrium, advancing, receding, dynamic)

- Classification of theoretical models for maximum spreading

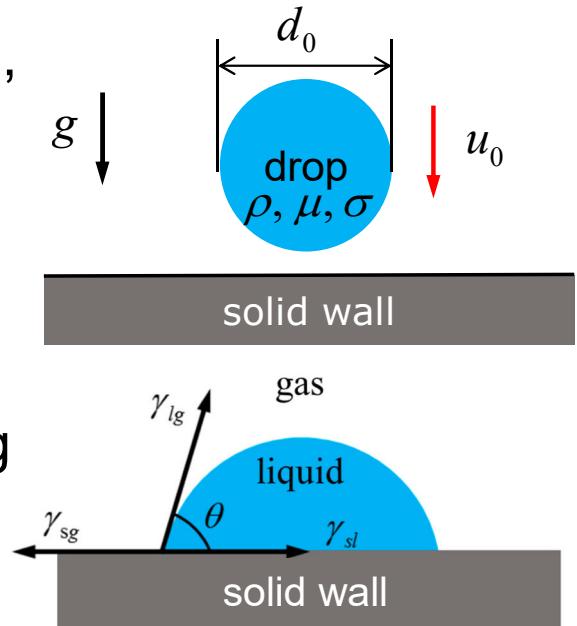
■ Models based on scaling relations valid in certain regimes

■ Mechanistic models based on momentum or **energy balance**

- A universal mechanistic model based on the energy balance is missing

■ Difficulty with low/high viscosity liquids and hydrophilic/hydrophobic surfaces

■ Here, significant progress in development of a universal energy balance model is reported



Outline

- Introduction
 - Motivation and objective
- **Literature survey on models for maximum spreading**
 - Energy balance (EB) approach
 - Scaling in different regimes
- New concepts for closure terms in the energy balance
 - Gas-liquid surface area
 - Dissipation upon maximum spread
- Closure of dissipation function and test of the novel model
 - Parameter determination by asymptotic analysis and experiments
 - Test against experimental data sets from literature
- Conclusions and outlook

Balance of mechanical energy

- General energy balance between initial state ($t = 0$) and state at time $t > 0$
 - Consideration of liquid kinetic energy (E_k) and surface energy (E_s)
 - Gravitational energy (E_g) can be neglected because E_g/E_s is typically small
 - Energy lost by (viscous) dissipation $W \geq 0$
 - Normalization of EB by σS_0 , where S_0 denotes the initial gas-liquid surface area

$$\frac{E_{k,0} - E_k(t)}{\sigma S_0} + \frac{E_{s,0} - E_s(t)}{\sigma S_0} = \frac{W(t)}{\sigma S_0}$$

$$\frac{E_{k,0}}{\sigma S_0} = \frac{(\frac{1}{2} \rho u_0^2)(\frac{\pi}{6} d_0^3)}{\sigma \pi d_0^2} = \frac{\frac{\pi}{12} \rho u_0^2 d_0^3}{\sigma \pi d_0^2} = \frac{We}{12}$$

- Energy balance at time of maximum spreading ($t = t_m$) assuming $E_k(t_m) = 0$

$$\frac{We}{12} + 1 - \underbrace{\frac{S(t_m)}{S_0}}_{=s_m} + \frac{\cos \theta}{4} \beta_m^2 = \underbrace{\frac{W(t_m)}{\sigma S_0}}_{=w_m}$$

To obtain a relation for β_m
 models for s_m and w_m are required
 → see slides 11 and 12

Scaling in capillary regime – $\beta_m \sim We^{1/2}$

- Initial kinetic energy is completely converted in surface energy at max. spread

$$\frac{E_{k,0}}{\sigma S_0} = \frac{We}{12} \sim \frac{E_{s,m}}{\sigma S_0}$$

- Estimation of surface energy Young's equation

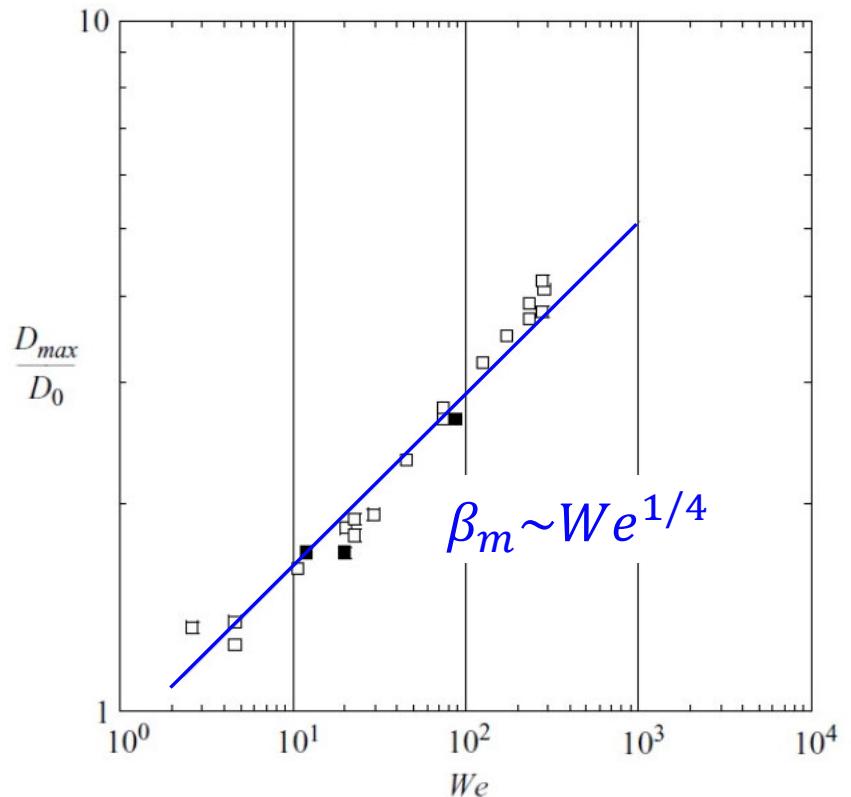
- Change of Gibbs free interfacial energy (per unit area) $\Delta G = \underbrace{\gamma_{gl}}_{=\sigma} + \underbrace{\gamma_{sl} - \gamma_{sg}}_{-\sigma \cos \theta} = \sigma(1 - \cos \theta)$
- At maximum spread

$$\frac{E_{s,m}}{\sigma S_0} \sim \frac{\Delta G \cdot A_{\text{wet}}}{\sigma S_0} = \frac{\sigma(1 - \cos \theta) \frac{\pi}{4} d_m^2}{\pi \sigma d_0^2} = \frac{1 - \cos \theta}{4} \beta_m^2 \rightarrow \beta_m \sim \sqrt{\frac{3We}{1 - \cos \theta}} \sim We^{1/2}$$

- R.E. Ford, C.G.L. Furridge, Impact and spreading of spray drops on foliar surfaces, Society of Chemical Industry, London, 1967, 417-432
- E.W. Collings, A.J. Markworth, J.K. McCoy, J.H. Saunders, *J. Mater. Sci.* **25** (1990) 3677-3682
- T. Bennett, D. Poulikakos, *J. Mater. Sci.* **28** (1993) 963-970

Scaling in capillary regime – $\beta_m \sim We^{1/4}$

- Experiments of Clanet et al. (2004)
 - Impact of water droplets on smooth superhydrophobic surface ($\theta_{eq} = 170^\circ$)
 - Observed experimental scaling $\beta_m \sim We^{1/4}$
 - Explanation by “effective gravity” force due to drop deceleration after impact
- Exp. by Attane et al. (2007), Laan et al. (2014)
 - Scaling $\beta_m \sim We^{1/4}$ is consistent for water but does not hold for other liquids (e.g. blood)
 - The exact conditions under which this scaling occurs are still unclear



- ❑ C. Clanet, C. Beguin, D. Richard, D. Quere, Maximal deformation of an impacting drop, *J. Fluid Mech.* **517** (2004) 199-208
- ❑ P. Attane, F. Girard, V. Morin, An energy balance approach of the dynamics of drop impact on a solid surface, *Phys. Fluids* **19** (2007) 012101
- ❑ N. Laan, K.G. de Bruin, D. Bartolo, C. Josserand, D. Bonn, *Physical Review Applied* **2** (2014) 044018

Scaling in viscous regime

- Initial kinetic energy is mainly dissipated at maximum spread

$$\frac{E_{k,0}}{\sigma S_0} = \frac{We}{12} \sim \frac{W_m}{\sigma S_0}$$

$$W_m = \int_0^{t_m} \int_{V_{\text{drop}}} \mu (\nabla \mathbf{u} + (\nabla \mathbf{u})^T) : \nabla \mathbf{u} dV dt$$

- Chandra & Avedisian (1991)

$$W_m \sim \mu \frac{u_0^2}{h_m^2} \cdot d_0^3 \cdot \frac{d_0}{u_0} \sim \frac{\mu u_0 d_0^4}{h_m^2}$$

$$h_m d_m^2 \sim d_0^3 \quad \rightarrow \quad \beta_m \sim Re^{1/4}$$

volume conservation

(h_m = drop height at maximum spread)

- Clanet et al. (2004)

$$W_m \sim \mu \frac{u_0^2}{h_m^2} \cdot d_m d_0^2 \cdot \frac{d_0}{u_0} \sim \frac{\mu u_0 d_m d_0^3}{h_m^2} \quad \rightarrow \quad \beta_m \sim Re^{1/5} \quad (\text{Scaling observed in experiment of Madejski})$$

- S. Chandra, C.T. Avedisian, *Proc. Royal Society London. Series A: Mathematical and Physical Sciences* **432** (1991) 13-41
- C. Clanet, C. Beguin, D. Richard, D. Quere, Maximal deformation of an impacting drop, *J. Fluid Mech.* **517** (2004) 199-208
- J. Madejski, Solidification of droplets on a cold surface, *Int. J. Heat Mass Transf.* **19** (1976) 1009-1013

Transition between both regimes

■ Capillary regime $P < 1$

- All initial energy is transferred in surface energy at maximum spreading

$$\beta_m \sim We^{1/2}$$

■ Viscous regime $P > 1$

- Clanet et al. (2004), Fedorchenko et al. (2005), Roisman (2009)

$$\beta_m \sim Re^{1/5}$$

■ Impact parameter P serves to distinguish both regimes

- $b = 4/5$ (Clanet), $b = 1/2$ (Fedorchenko), $b = 2/5$ (Eggers)

■ Rescaling methods (e.g. Laan et al., 2014)

- Regime discrimination parameter $A = 1.24$ is of order 1

$$P = \frac{We}{Re^b}$$

$$\beta_m Re^{-1/5} = \frac{P^{1/2}}{A + P^{1/2}}$$

- 📖 C. Clanet, C. Beguin, D. Richard, D. Quere, Maximal deformation of an impacting drop, *J. Fluid Mech.* **517** (2004) 199-208
- 📖 A.I. Fedorchenko, A.-B. Wang, Y.-H. Wang, *Phys. Fluids* **17** (2005) 093104
- 📖 I.V. Roisman, Inertia dominated drop collisions, Part II., *Phys. Fluids* **21** (2009)
- 📖 J. Eggers, M.A. Fontelos, C. Josserand, S. Zaleski, *Phys. Fluids* **22** (2010) 062101
- 📖 N. Laan, K.G. de Bruin, D. Bartolo, C. Josserand, D. Bonn, *Physical Review Applied* **2** (2014) 044018

EB – Modeling of gas-liquid surface area s_m

- Geometrical approximations for drop shape

- Disk with negligible height

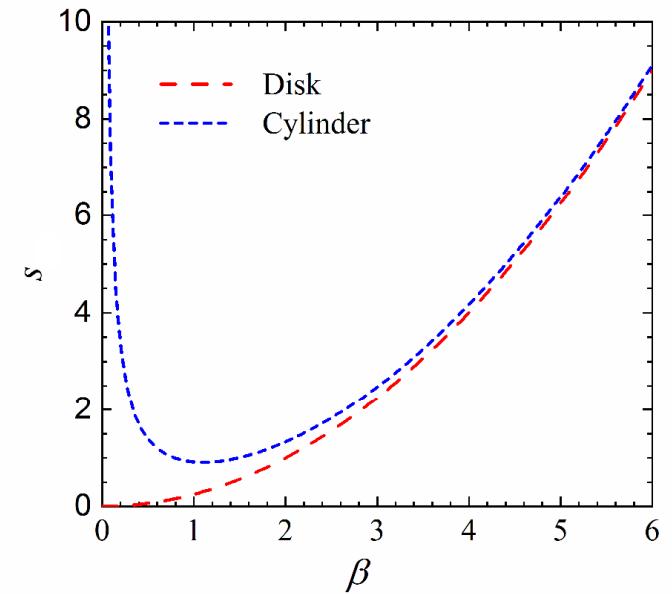
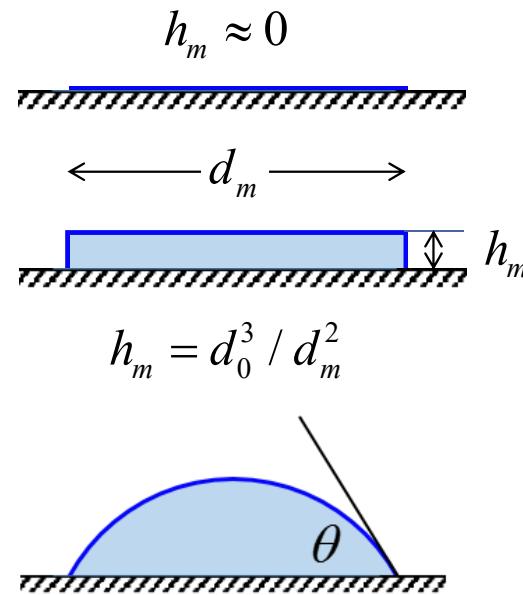
$$s_{\text{disk}}(\beta) = \frac{\beta^2}{4}$$

- Cylinder with finite height

$$s_{\text{cyl}}(\beta) = \frac{\beta^2}{4} + \frac{2}{3\beta}$$

- Spherical cap (sc)

$$s_{\text{sc}}(\theta) = \sqrt[3]{\frac{2}{(2 + \cos \theta)^2 (1 - \cos \theta)}}$$



- 📖 R.E. Ford, C.G.L. Furmidge, Impact and spreading of spray drops on foliar surfaces, Society of Chemical Industry, London, 1967, 417-432
- 📖 T. Mao, D.C.S. Kuhn, H. Tran, Spread and rebound of liquid droplets upon impact on flat surfaces, *AIChE J.* **43** (1997) 2169-2179
- 📖 H. Park, W.W. Carr, J. Zhu, J.F. Morris, Single drop impaction on a solid surface, *AIChE J.* **49** (2003) 2461-2471

EB – Modeling of dissipation w_m

■ Mechanistic dissipation models

$$W_m = \int_0^{t_m} \int_{V_{\text{diss}}} \mu (\nabla \mathbf{u} + (\nabla \mathbf{u})^T) : \nabla \mathbf{u} dV dt$$

$$\approx \mu \cdot u_c^2 \cdot L_c^{-2} \cdot t_m \cdot V_{\text{diss}}$$

- Various proposals for u_c, L_c, t_m all yield $w_m = W_m / (\sigma S_0) \sim \beta_m^n$ with exponent $n = 2 - 6.5$
- Combinations of models for s_m and w_m give energy balance models of very different form
- *Is dissipation model appropriate? Different dissipation contributions: viscous b.l., c.l. friction, ...*

Literature	Energy models
Chandra and Avedisian (1991) ²¹	$1.5 \frac{\text{We}}{\text{Re}} \beta_{\max}^4 + (1 - \cos \theta) \beta_{\max}^2 - \left(\frac{1}{3} \text{We} + 4 \right) \approx 0$
Pasandideh-Fard <i>et al.</i> (1996) ²²	$\beta_{\max} = \sqrt{\frac{\text{We} + 12}{3(1 - \cos \theta) + 4 \frac{\text{We}}{\sqrt{\text{Re}}}}}$
Mao <i>et al.</i> (1997) ³⁵	$\left[\frac{1}{4} (1 - \cos \theta) + 0.2 \frac{\text{We}^{0.83}}{\text{Re}^{0.33}} \right] \beta_{\max}^3 - \left(\frac{\text{We}}{12} + 1 \right) \beta_{\max} + \frac{2}{3}$
Ukiwe and Kwok (2005) ²³	$(\text{We} + 12) \beta_{\max} = 8 + \beta_{\max}^3 \left[3(1 - \cos \theta) + 4 \frac{\text{We}}{\sqrt{\text{Re}}} \right]$
Gao and Li (2014) ³⁴	$1 + \frac{\text{We}}{12} = \frac{1}{6} \left(\frac{D}{r_c} + \frac{D}{R_c} \right) + 4\theta_a \frac{r_c R_c}{D^2} + \left(\frac{R_c}{D} - \frac{r_c}{D} \sin \theta_a \right)$ $+ \left(\frac{R_c}{D} + \frac{r_c}{D} \sin \theta_a \right)^2 \left(\frac{4}{3} \frac{\text{We}}{\sqrt{\text{Re}}} - \cos \theta_a \right)$
Wildeman <i>et al.</i> (2016) ⁹	$\frac{12}{\text{We}} + \frac{1}{2} = \beta_{\max}^2 \frac{3(1 - \cos \theta)}{\text{We}} + \frac{\alpha}{\sqrt{\text{Re}}} \beta_{\max}^2 \sqrt{\beta_{\max} - 1}$ no-slip, $\text{We} > 30$

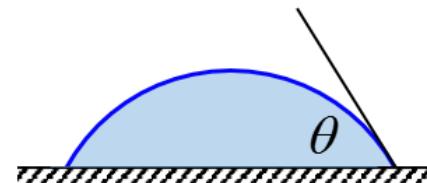
Table from Aksoy *et al.*, *Phys. Fluids* **34** (2022) 042106

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New model for gas-liquid surface area

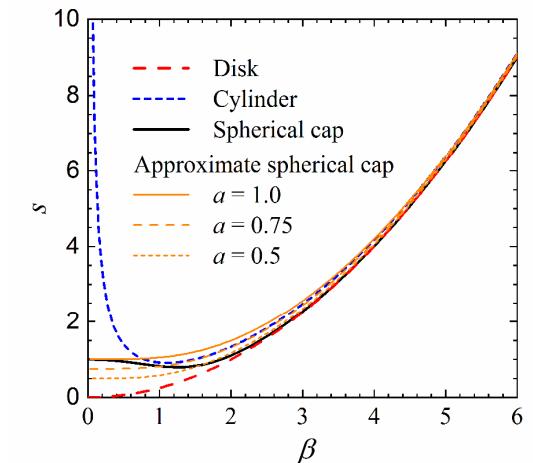
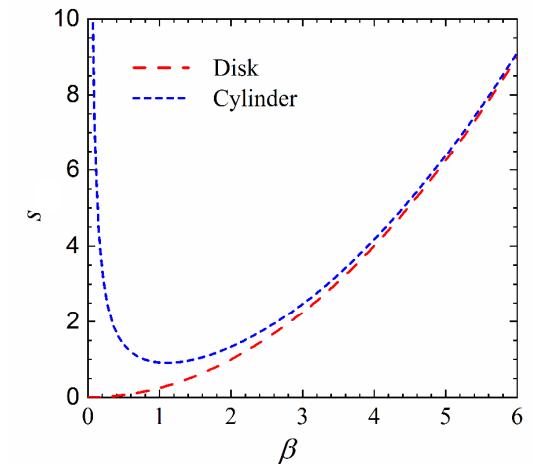
- The disk and cylinder shape models are not suitable for low β (hydrophobic surfaces) and cannot describe the initial state where $s_0 = 1$
- Spherical cap $s_{sc} = s_{sc}(\theta)$
 - New relation $s_{sc} = s_{sc}(\beta)$



$$s_{sc}(\beta) = \frac{\sqrt[3]{\beta^6 + 8\sqrt{\beta^6 + 16} + 32}}{4} - \frac{\beta^2}{4} + \frac{\beta^4}{4\sqrt[3]{\beta^6 + 8\sqrt{\beta^6 + 16} + 32}}$$

- Approximate spherical cap (new model)

$$\beta^6 + 8\sqrt{\beta^6 + 16} + 32 \approx (\beta^2 + 4a)^3 \rightarrow s_{asc}(\beta, a) = a + \frac{1}{4} \frac{\beta^4}{\beta^2 + 4a}$$



New concept for modeling of dissipation

- Existing models do not respect the upper physical bound for dissipation
- Energy balance between initial state and terminal deposition state ($t = t_{eq}$)

$$\frac{We}{12} + 1 - \underbrace{\frac{S(t_{eq})}{S_0}}_{=s_{eq}} + \frac{\cos \theta}{4} \beta_{eq}^2 = \underbrace{\frac{W(t_{eq})}{\sigma S_0}}_{=w_{eq}} \xrightarrow{eq=sc} w_{eq} = \frac{We}{12} + \underbrace{1 - \sqrt[3]{(2 + \cos \theta)(1 - \cos \theta)^2 / 4}}_{0 \leq w_{eq,s} \leq 1}$$

$$s_{eq} = s_{sc}(\theta) = \sqrt[3]{\frac{2}{(2 + \cos \theta)^2(1 - \cos \theta)}}$$

$$\beta_{eq} = \beta_{sc}(\theta) = \sqrt[3]{\frac{4 \sin^3 \theta}{(2 + \cos \theta)(1 - \cos \theta)^2}}$$

- New model for dissipation upon maximum spread
 - Dissipation function f_w needs to be determined

$$w_m = f_w w_{eq}, \quad 0 \leq f_w \leq 1$$

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Energy balance with the two new concepts

- Introducing the proposed models for s_m and w_m in the energy balance yields

$$\frac{1}{4} \frac{\beta_m^4}{\beta_m^2 + 4a} - \frac{\cos \theta}{4} \beta_m^2 - \underbrace{\left[\frac{We}{12} + 1 - a - f_w \left(\frac{We}{12} + 1 - \sqrt[3]{(2 + \cos \theta)(1 - \cos \theta)^2 / 4} \right) \right]}_{=Q} = 0$$

- Solution of this fourth order equation in β_m

$$\beta_m = \sqrt{\frac{2(Q + a \cos \theta) + 2\sqrt{(Q + a \cos \theta)^2 + 4aQ(1 - \cos \theta)}}{1 - \cos \theta}}$$

$$Q > 0 \rightarrow \beta_m > 0$$

- Assumed relationship for the dissipation function

- The exponents b of the Reynolds number and c of the impact parameter are determined by asymptotic analysis

$$f_w = \frac{P^c}{A + P^c}$$

$$P = WeRe^{-b}$$

Asymptotic analysis ($a = 1$) – Case 1

- Assumption $(Q + \cos \theta)^2 \gg 4Q(1 - \cos \theta)$ i.e. $Q \gg 4 - 6\cos \theta$

$$\beta_m = \sqrt{\frac{2(Q + \cos \theta) + 2\sqrt{(Q + \cos \theta)^2 + 4Q(1 - \cos \theta)}}{1 - \cos \theta}} \approx \sqrt{\frac{4Q}{1 - \cos \theta}} \approx \sqrt{\frac{4}{1 - \cos \theta} \frac{A}{A + P^c} \frac{We}{12}}$$

$$P^c = We^c Re^{-bc}$$

- Assumption $We \gg 12$

$$Q = \frac{We}{12} - f_w \left(\frac{We}{12} + 1 - \sqrt[3]{(2 + \cos \theta)(1 - \cos \theta)^2 / 4} \right) \rightarrow Q \approx (1 - f_w) \frac{We}{12} = \frac{A}{A + P^c} \frac{We}{12}$$

Capillary regime $P^c < A$

$$\beta_m \approx \sqrt{\frac{We}{3(1 - \cos \theta)}} \sim We^{1/2} \checkmark$$

Viscous regime $P^c > A$

$$\beta_m \approx \sqrt{\frac{AP^{-c}We}{3(1 - \cos \theta)}} \sim We^{(1-c)/2} Re^{bc/2} ! = Re^{1/5} \rightarrow c = 1, b = 2/5$$

Eggers (2010)

$$P = We Re^{-2/5}$$

Asymptotic analysis ($a = 1$) – Case 2

- Assumption $(Q + \cos \theta)^2 \ll 4Q(1 - \cos \theta)$ i.e. $Q \ll 4 - 6\cos \theta \leq 10$

$$\beta_m = \sqrt{\frac{2(Q + \cos \theta) + 2\sqrt{(Q + \cos \theta)^2 + 4Q(1 - \cos \theta)}}{1 - \cos \theta}} \approx \sqrt[4]{\frac{16Q}{1 - \cos \theta}} \approx \sqrt[4]{\frac{16}{1 - \cos \theta} \frac{A}{A + P^c} \frac{We}{12}}$$

$$P^c = We^c Re^{-bc}$$

- Assumption $We \gg 12$

$$Q = \frac{We}{12} - f_w \left(\frac{We}{12} + 1 - \sqrt[3]{(2 + \cos \theta)(1 - \cos \theta)^2 / 4} \right) \rightarrow Q \approx (1 - f_w) \frac{We}{12} = \frac{A}{A + P^c} \frac{We}{12}$$

Capillary regime $P^c < A$

$$\beta_m \approx \sqrt[4]{\frac{4}{3} \frac{We}{1 - \cos \theta}} \sim We^{1/4} \quad \checkmark$$

Viscous regime $P^c > A$

$$\beta_m \approx \sqrt[4]{\frac{4}{3} \frac{AP^{-c}We}{1 - \cos \theta}} \sim We^{(1-c)/4} Re^{bc/4} \stackrel{!}{=} Re^{1/5} \rightarrow c = 1, b = 4/5$$

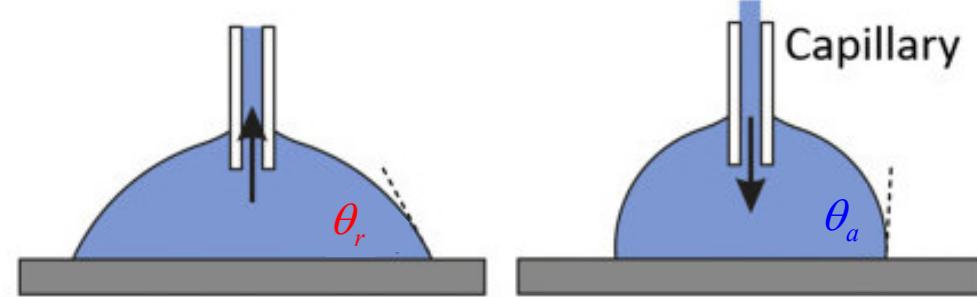
Clanet (2004)

$$P = We Re^{-4/5}$$

Determination of parameter A in $f_w = P/(A + P)$

- Evaluation of relative dissipation from literature data on maximum spread

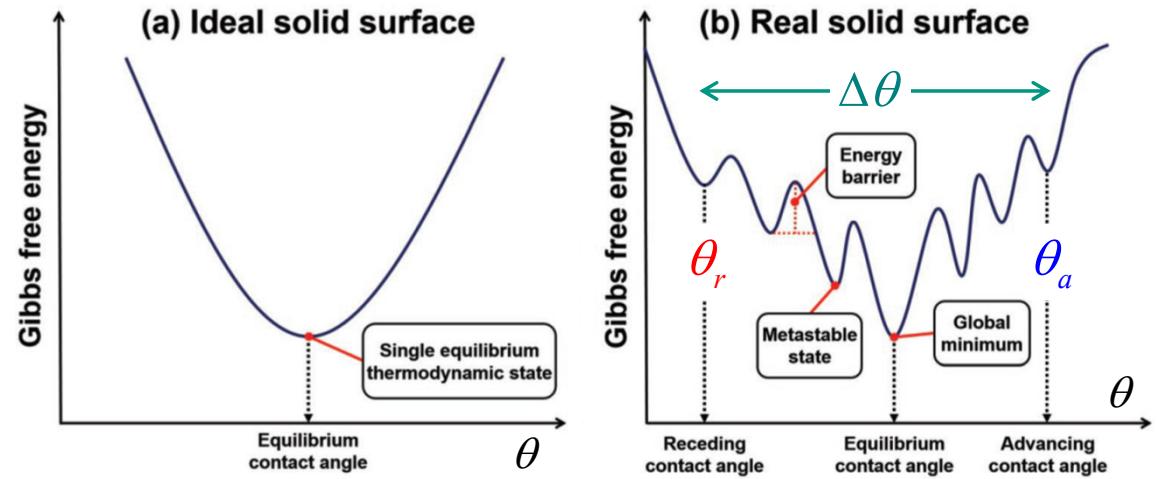
$$f_w = \frac{w_m}{w_{eq}} \approx \frac{\frac{We}{12} + 1 - s_{asc}(\beta_m, a) + \frac{\cos \theta_a}{4} \beta_m^2}{\frac{We}{12} + 1 - \sqrt[3]{\frac{(2 + \cos \theta_r)(1 - \cos \theta_r)^2}{4}}}$$



- Which contact angle to use?

- Equilibrium contact angle θ_{eq}
- Advancing contact angle θ_a
- Receding contact angle θ_r
- Hysteresis** $\Delta\theta = \theta_a - \theta_r$

-  C.H. Kung, P.K. Sow, B. Zahiri, W. Mérida,
Advanced Materials Interfaces **6** (2019) 1900839
-  H.-J. Butt et al., *Current Opinion in Colloid & Interface Science* **59** (2022) 101574



Determination of parameter A in $f_w = P/(A + P)$

- Evaluation of relative dissipation from literature data on maximum spread

$$f_w = \frac{w_m}{w_{eq}} \approx \frac{\frac{We}{12} + 1 - s_{asc}(\beta_m, a) + \frac{\cos \theta_a}{4} \beta_m^2}{\frac{We}{12} + 1 - \sqrt[3]{\frac{(2 + \cos \theta_a)(1 - \cos \theta_a)^2}{4}}$$

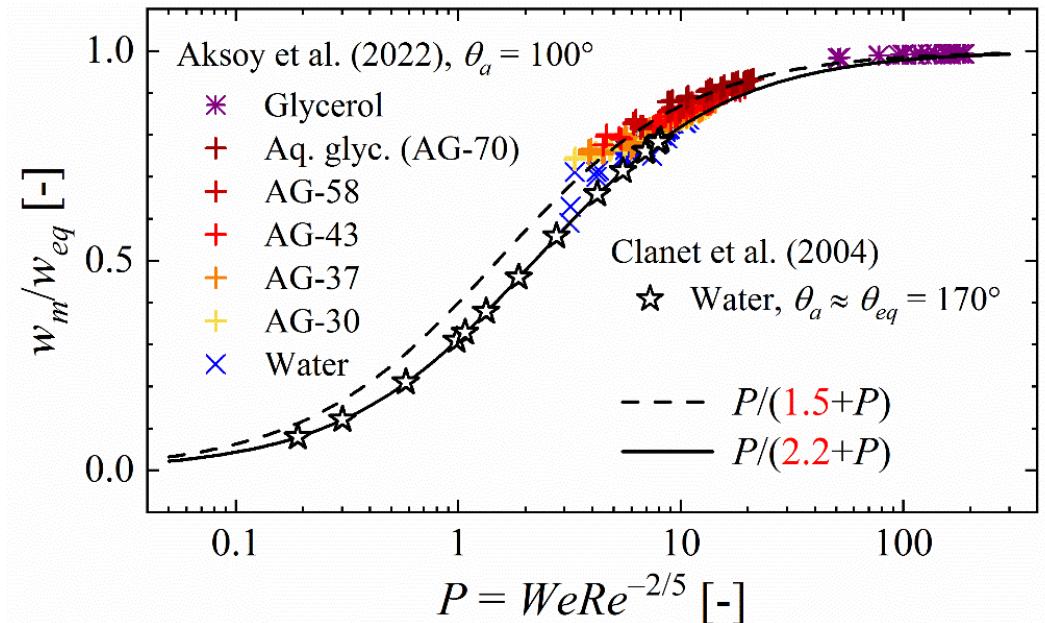
- We use $a = 3/4$ since this gives best agreement with cylinder model

$$\rightarrow s_{asc}(\beta_m) = \frac{3}{4} + \frac{1}{4} \frac{\beta_m^4}{\beta_m^2 + 4 \cdot \frac{3}{4}}$$

- Experimental data of Aksoy et al. (2022)

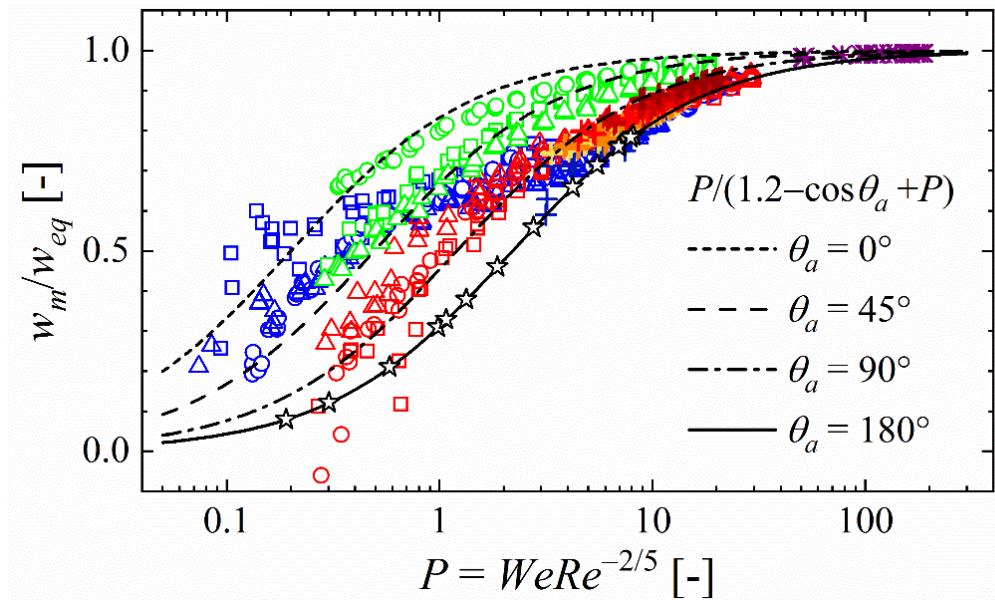
- Seven different liquids, $57 < We < 460$, $4 < Re < 9200$, $\theta_a = 100^\circ$ (294 data points)

█ Y.T. Aksoy, P. Eneren, E. Koos, M.R. Vetrano, Spreading of a droplet impacting on a smooth flat surface, *Phys. Fluids* **34** (2022) 042106
█ C. Clanet, C. Beguin, D. Richard, D. Quere, Maximal deformation of an impacting drop, *J. Fluid Mech.* **517** (2004) 199-208



Determination of parameter A (continued)

- Regime discrimination parameter A depends on the advancing contact angle θ_a
- Experimental data of Lee et al. (2016); reported θ_d and θ_{eq} , assumption $\theta_a = \theta_d$
 - Three different liquids and surfaces, $1 < We < 1200$, $40 < Re < 17\,800$, $44^\circ < \theta_a < 123^\circ$



- Model for the dissipation function

$$f_w = \frac{WeRe^{-2/5}}{\underbrace{1.2 - \cos \theta_a}_{=A(\theta_a)} + WeRe^{-2/5}}$$

- For fixed impact parameter $P = WeRe^{-2/5}$ hydrophobic surfaces dissipate less energy upon maximum spreading as compared to hydrophilic surfaces
 \rightarrow enables drop rebound

 J.B. Lee et al., Universal rescaling of drop impact on smooth and rough surfaces, *J. Fluid Mech.* **786** (2016) R4

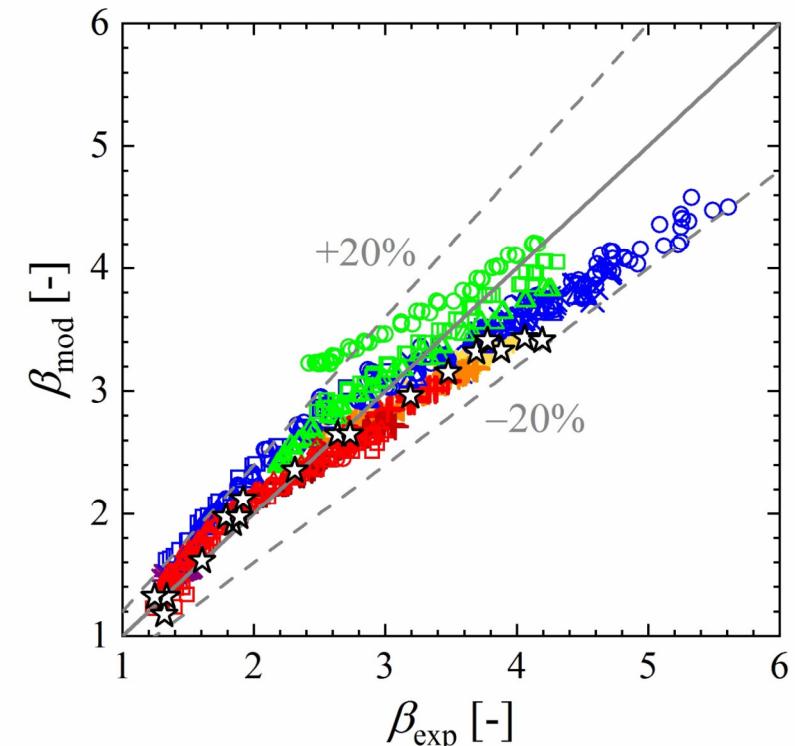
Test of the proposed new model

$$\beta_m = \sqrt{\frac{2(\mathcal{Q} + \frac{3}{4} \cos \theta_a) + 2\sqrt{(\mathcal{Q} + \frac{3}{4} \cos \theta_a)^2 + 4(1 - \cos \theta_a)\mathcal{Q}}}{1 - \cos \theta_a}}$$

$$\mathcal{Q} = 1 - \frac{3}{4} + \frac{We}{12} - \frac{WeRe^{-2/5}}{1.2 - \cos \theta_a + WeRe^{-2/5}}$$

$$\times \left(\frac{We}{12} + 1 - \sqrt[3]{\frac{(2 + \cos \theta_a)(1 - \cos \theta_a)^2}{4}} \right)$$

- Parity plot against experimental data
 - Agreement is within $\pm 20\%$
 - For all experimental data it is $\mathcal{Q} > 0$



- 📖 Y.T. Aksoy, P. Eneren, E. Koos, M.R. Vetrano, Spreading of a droplet impacting on a smooth flat surface, *Phys. Fluids* **34** (2022) 042106
- 📖 J.B. Lee et al., Universal rescaling of drop impact on smooth and rough surfaces, *J. Fluid Mech.* **786** (2016) R4
- 📖 C. Clanet, C. Beguin, D. Richard, D. Quere, Maximal deformation of an impacting drop, *J. Fluid Mech.* **517** (2004) 199-208

Conclusions

- Existing energy balance models for max. spread have two shortcomings
 - Gas-liquid area is not properly modelled for superhydrophobic surfaces (low β_m)
 - Models for dissipation do not account for proper upper physical limit
- Proposal of new concepts for the two closure terms in the energy balance
 - Approximate spherical cap (asc) model for gas-liquid surface area
 - Model for dissipation that respects the upper physical limit
- Proposal of a new 'universal' energy balance model for maximum spread
 - Model comprises power law scaling for viscous regime and both capillary regimes
 - Model is explicit and thus no iteration is required
 - Dissipation function is determined from exp. data with wide ranges of We , Re , θ_a
 - Model is in good agreement with exp. with a maximum deviation of about 20%

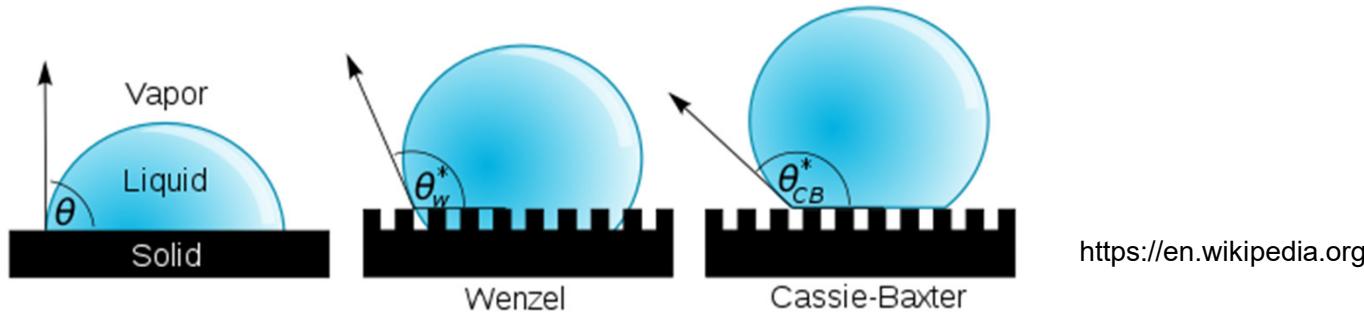
Outlook

■ Directions for model refinement

- The current model assumes zero kinetic energy at maximum spread
- The current model for total dissipation w_{eq} assumes zero c.a. hysteresis
- Test model against further experimental and numerical data from literature
- Goal: regime discrimination parameter $A = A(\theta_a, \Delta\theta)$
 → measurement of the advancing and the receding contact angle is required

■ Extend model to surfaces with regular roughness

- Wenzel and Cassie-Baxter wetting states



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CRC/Transregio 150
Turbulent, chemically reactive
multi-phase flows near walls



Deutsche
Forschungsgemeinschaft

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