

Advances in reconstructing the cosmic-ray energy spectrum with IceTop

The IceCube Collaboration

(a complete list of authors can be found at the end of the proceedings)

E-mail: lilly.pyras@utah.edu, larissa.paul@sdsmt.edu, krawlins@alaska.edu,
ian.reistroffer@mines.sdsmt.edu, amar.thakuri@mines.sdsmt.edu

The IceTop array at the surface of the IceCube Neutrino Observatory measures extensive air showers produced by cosmic-ray particles with energies from PeV up to EeV, covering the transition region from galactic to extragalactic sources. This contribution presents significant improvements that will enhance the measurement of the cosmic-ray energy spectrum. (I) To analyze more than a decade of data with increasing snow overburdens on the detector, an improved method to handle the time-dependent attenuation of the detector signals was developed. (II) New analysis cuts have been developed to increase the measured event rate while improving the reconstruction quality. (III) A new reconstruction method that separately fits the electromagnetic and muonic components, while incorporating data from the deep in-ice detector, enables the reconstruction of air showers with cores outside the IceTop array, up to zenith angles of 50°. These improvements will significantly increase the event statistics and extend the IceTop spectrum towards higher energies.

Corresponding authors: Lilly Pyras^{1*}, Larissa Paul², Katherine Rawlins³, Ian Reistroffer², Amar Thakuri²

¹ *Department of Physics and Astronomy, University of Utah*

² *Physics Department, South Dakota School of Mines and Technology*

³ *Department of Physics and Astronomy, University of Alaska Anchorage*

* Presenter

39th International Cosmic Ray Conference (ICRC2025)
15–24 July 2025
Geneva, Switzerland



ICRC 2025
The Astroparticle Physics Conference
Geneva July 15-24, 2025

1. Introduction and Detector

When high-energy cosmic rays enter Earth's atmosphere, they produce cascades of secondary particles known as extensive air showers (EASs). IceTop, the surface array of the IceCube Neutrino Observatory, detects these air showers in the PeV to EeV energy range, covering what is thought to be the transition region from galactic to extragalactic in origin [1]. This work addresses some of the statistical and systematic limitations of previous spectrum analyses [2, 3], especially at the highest energies, by introducing a data-driven snow model, improved event selection, and a new reconstruction for events with a shower core outside of IceTop. These methods lay the groundwork for a large variety of future analyses in IceTop.

The IceTop array [4] is comprised of 81 “stations”, each containing two tanks (A and B) equipped with two Digital Optical Modules (DOMs). EASs are detected through the Cherenkov light produced by charged particles passing through the ice inside the tanks. If both tanks in a station register a signal, the hits are recorded as Hard Local Coincidence (HLC); a hit is Soft Local Coincidence (SLC) if only one tank recorded a signal. Signals are calibrated to units of vertical equivalent muons (VEM). Reconstruction of EAS events employs a maximum-likelihood method. The expected charge S at a distance r from the shower axis is modeled with a lateral distribution function (LDF), in particular: a ‘Double Logarithmic Parabola’ (DLP) [5]:

$$S(r) = S_{\text{ref}} \cdot \left(\frac{r}{r_{\text{ref}}} \right)^{-\beta - \kappa \cdot \log_{10} \left(\frac{r}{r_{\text{ref}}} \right)}, \quad r_{\text{ref}} = 125 \text{ m}. \quad (1)$$

The expected arrival times of the signals—the geometric shape of the shower front—is modeled by a paraboloid with a Gaussian nose [4]. From these models, the core position and direction of the shower can be reconstructed, as well as the “shower size”: the signal S_{ref} measured at the reference distance r_{ref} from the shower axis.

Previous analyses used only HLC hits for reconstruction, and chose a reference distance of 125 meters, with S_{125} used as a proxy for the primary energy. The reference distance was motivated by earlier studies with a smaller detector [6], dividing IceTop into Subarrays A and B using one tank per station. Recently, this technique has been extended to the full-size detector and higher energies, to study alternative reference distances for air showers with cores located both inside the IceTop array (contained events) and outside of it (uncontained events). By fitting S_{ref} and β separately for Subarray-A and B across different r_{ref} values, we identify the distance that minimizes fluctuations between subarrays. The initial results indicate that the best r_{ref} at all energies is higher for uncontained events compared to contained events. Additionally, for both event types, the optimal r_{ref} increases with energy. This suggests that the most stable S_{ref} lies near the distance where the bulk of the signal information is concentrated relative to the shower core. These findings may offer a more precise approach for LDF reconstruction and subsequently resolution, particularly at higher energies.

2. Snow

The IceTop tanks were deployed in stages over several years ending in 2011, with each tank initially installed flush with the snow surface. Since then, wind-blown snow has steadily accumulated across the array, creating an uneven and time-dependent overburden that varies from tank to tank,

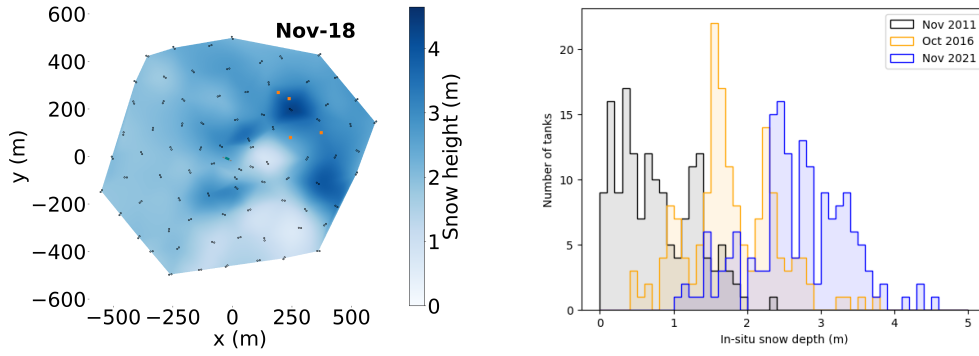


Figure 1: In-situ snow depths of the tanks in IceTop: a) over the array at one particular time, and b) sampled over three disparate times.

as illustrated in Fig. 1. This non-uniform snow cover alters the detector response and makes the reconstruction of air showers inconsistent across different years of data. Attenuation is expected to depend on the energies of the shower particles, which may itself depend on the shower size and the distance from the shower’s core. Thus, to achieve a uniform reconstruction across multiple years, a snow attenuation model must be applicable in a wide range of shower conditions. The previous model, “RADE-3” [7], is used as a basis for its successor, “RADE-4”.

In this data-driven method, IceTop tank charges from 11 years of data (2011 through 2021) are collected and binned as a function of multiple parameters: the shower size (S_{125}), the perpendicular distance of the tank from the shower core (r), and the slant depth through the snow to the tank ($d = z_{\text{snow}}/\cos(\theta)$). Each tank’s charge (S) is normalized by the S_{125} of the shower it appears in, to make a “log-normalized charge”: $S_{\text{ln}} = \ln(S/S_{125})$. Not-hit tanks ($S = 0$) are also recorded, in a specially-designated bin in log-normalized charge. Within each bin of S_{125} and r , the log-normalized charges are mapped as a function of snow slant depth. Fig. 2 (left) shows a straightforward example of such a map; $\ln(S/S_{125})$ decreases at a rate that corresponds to a characteristic attenuation length λ . At large radii (Fig. 2, center), the situation gets more complicated in two ways: a) the electromagnetic (EM) charges drop below the tank’s threshold and are recorded as non-hits ($S = 0$) instead of as hits, and b) a second structure appears in the charge distribution, from muons. The “muon peak” is largely unaffected by snow attenuation. In this work, a series of 2-D histograms—each such as Fig. 2’s left panels—are fit to a model in which there is both an EM component (with fraction F_{EM}) and a muon component (with fraction $1 - F_{\text{EM}}$). Both are modeled as Gaussians in log-normalized charge $G(S_{\text{ln}}, \mu, \sigma)$. The mean and sigma of the non-attenuating muon component (μ_{μ} and σ_{μ}) are constant with snow depth. But μ_{EM} is modeled to fall off with a characteristic attenuation length λ , and σ_{EM} is modeled to vary linearly with some slope. The detector threshold is modeled as a sigmoid function Y with a central position S_{thresh} and a width of δ . So the function fit is:

$$f(S_{\text{ln}}, d) = (1 - F_{\text{EM}})G(S_{\text{ln}}, \mu_{\mu}, \sigma_{\mu}) + F_{\text{EM}}Y(S_{\text{ln}}, S_{\text{thresh}}, \delta)G(S_{\text{ln}}, \mu_{\text{EM}}, \sigma_{\text{EM}}) \quad (2)$$

where: $\mu_{\text{EM}} = \mu_{\text{EM}_{\text{no snow}}} - d/\lambda$, and $\sigma_{\text{EM}} = \sigma_{\text{EM}_{\text{no snow}}} + \sigma_{\text{EM}_{\text{slope}}} d$.

The number of non-hits at $S = 0$, which is recorded in its own designated bins of the histogram, is modeled as the number of hits expected to fall below the threshold:

$$f_{\text{zeros}} = \frac{1}{2} \left[1 + \text{erf} \left(\frac{S_{\text{thresh}} - \mu_{\text{EM}}}{\sigma_{\text{EM}} \sqrt{2}} \right) \right]. \quad (3)$$

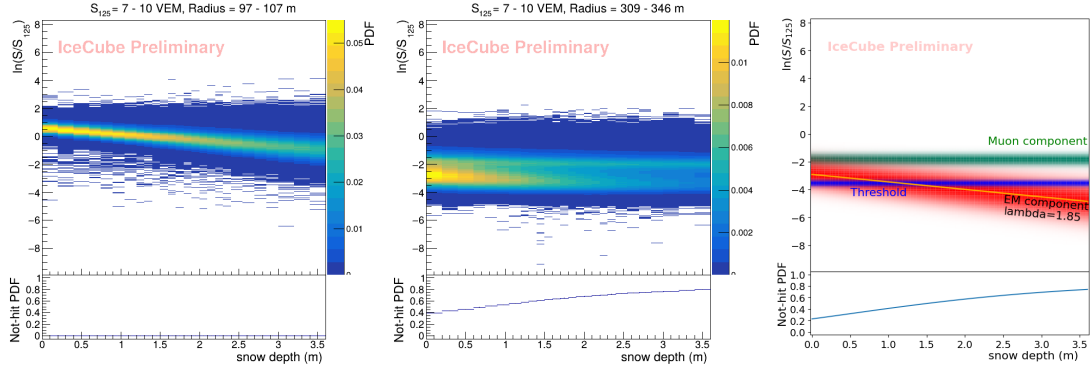


Figure 2: Two-dimensional histograms of log-normalized charge vs. snow depth, for two different distances from the core. Left: at ~ 100 meters, the attenuation of the snow can be easily measured. Center: at ~ 290 meters, the electromagnetic component drops below the detector threshold, and the non-attenuating “muon peak” is also visible. Right: A visualization of the 2-D model fitted to the charges in the center figure, with an EM component (red) and a muon component (green). The effect of a detector threshold (blue) populates the not-hit ($S = 0$) component of the distribution (the lower panels).

The hits and non-hits for the entire 2-D histogram are fitted together. Including the non-hits in the fitting helps greatly to constrain the relationship between the EM Gaussian and the detector threshold. Fig. 2 (right) shows a visualization of the various components of this fit (muon, EM, and threshold), including the non-hits in a separate panel.

Saturation comes into effect at very large charges. For these cases, a modified $\mu_{EM_{sat}}$ is computed (Eq. (4)) as the mean of the saturated distribution, where S_{sat} is the value of S_{ln} above which saturation occurs and F_{under} is the fraction of the distribution that falls below S_{sat} .

$$\mu_{EM_{sat}} = [-\sigma_{EM}^2 G(S_{sat}, \mu_{EM}, \sigma_{EM}) + \mu_{EM} F_{under}] + [(1 - F_{under}) S_{sat}]. \quad (4)$$

If the charges are so large that they are saturated at all snow depths, λ becomes difficult if not impossible to measure. Therefore, in this regime (the upper left of Fig. 3), λ is constrained with an upper limit of 4 meters.

Altogether, each fit has 10 free parameters: μ_μ , σ_μ , $\mu_{EM_{no\ snow}}$, λ , $\sigma_{EM_{no\ snow}}$, $\sigma_{EM_{slope}}$, S_{thresh} , δ , S_{sat} , and F_{EM} . Collecting all of the results from many such fits, we can characterize the behavior of λ , as well as the fraction of the signal which is from the non-attenuating muon peak, both as a function of S_{125} and r , as is shown in Fig. 3. Modeling of the muon fraction from these fit results, and testing the overall model on data from multiple years, are both ongoing efforts. It is expected

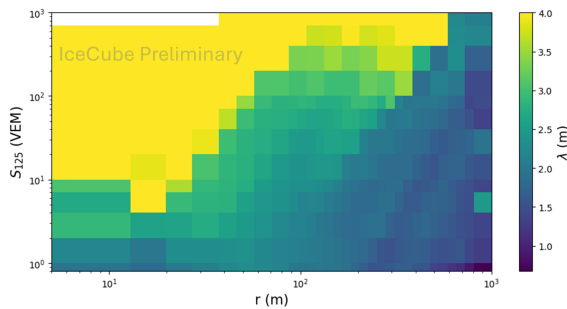


Figure 3: λ as computed for a set of r and S_{125} ranges. At the highest energies (i.e., for the largest S_{125} and smallest r ranges), statistics are too low to reliably compute a 2-D fit, hence the white space in the upper-left.

that the resulting reconstruction behavior from early years of IceTop data (when snow coverage was shallow) will match those from later years, across a larger energy range.

3. Contained Events

The quality cuts used for the last published high-energy spectrum analysis in Ref. [2] were mostly based on topological properties, and they aimed to save events that landed inside the borders of the array. In previous work and in this work, “containment” of an event is parametrized as the distance from the center of the array to the shower core, expressed as a fraction of the distance to the edge of the array in that direction. In this work, new selection criteria have been developed, to enhance energy resolution and increase the event rate, particularly at high energies.

The first of these new cuts is based on the goodness-of-fit from the timing reconstruction: χ^2_{time} . The cut value itself depends on the event’s total charge, because higher-charge events typically involve more triggered tanks, potentially resulting in higher values. The second new cut is based on the ratio of the sum of charges in the outer ring of tanks, to that in the inner array. This cut is motivated by events with shower cores near the edge of the array, which are only reliably reconstructed if they also deposit substantial charges in the inner tanks. Like the timing goodness-of-fit cut, the charge-ratio cut also depends on the total charge; misreconstructed events are often characterized by a low total charge, motivating stricter cuts for such events and looser cuts for those with higher total charges.

These new cuts allow future analyses to relax some of the selection criteria that were necessary in past analyses. For instance, Ref. [2] considered only events from zenith angles of $\cos(\theta) > 0.8$ and containment < 0.96 ; in this work, events out to $\cos(\theta) > 0.7$ and containment < 1.0 are explored. A comparison of energy bias and resolution between the previous work and the work presented here is shown in Fig. 4. The updated cuts yield significant improvements in resolution at the highest energies, while maintaining similar performance at lower energies. Slightly increased bias and resolution at the lowest energies are attributed to the extended zenith range. Fig. 5 demonstrates a noticeable increase in the event statistics, mainly due to the extension of the zenith range. In the bottom panel of Fig. 5, one can see that with the zenith range expansion, an increased rate is expected over the whole energy range. But even when restricting this work to the same zenith range and containment limits as in the previous analysis, an increased rate is still expected for the highest energies. Overall, the newly developed cuts provide better energy resolution and

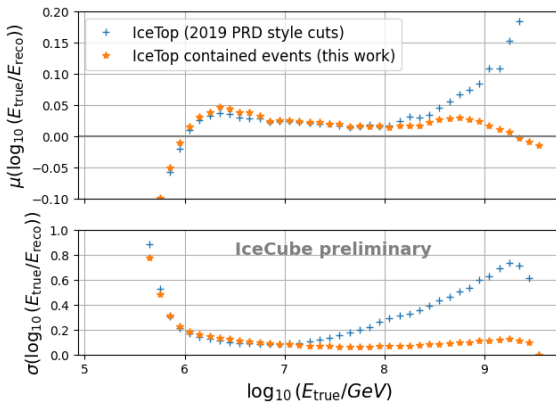


Figure 4: Comparison of the energy bias (top) and resolution (bottom) between the previous analysis in Ref. [2] and this work. Both show great improvements for the new cuts at the highest energies and similar performance for the lower energies. The slightly increased bias and resolution at the lowest energies are due to the increased zenith range.

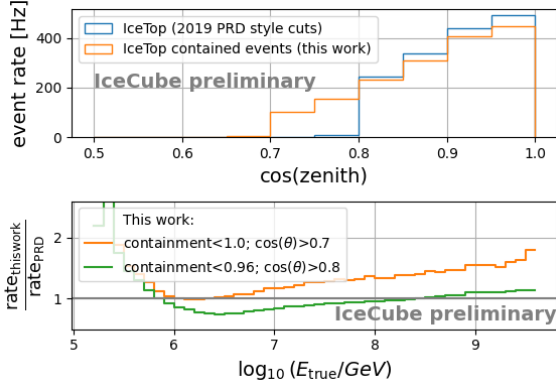


Figure 5: An increase of event statistics is achieved by the new selection.

Top: Shows the increase in event rate due to the increased zenith range. Both histograms are weighted to an H4a flux.

Bottom: The ratio of the rates versus the true energy shows an increased rate over nearly the whole energy range. When restricting the zenith range and the contained area to the smaller values of the previous analysis for both analyses it is visible that for the highest energies a rate increase over all zenith ranges is achieved.

higher event statistics. The absolute cut values will be re-optimized when the updated snow model becomes available, which may further improve the results. This work presents results from a CORSIKA simulation dataset which uses the SIBYLL 2.1 interaction model and the snow overburden corresponding to the year 2012. Comparisons with different interaction models (SIBYLL 2.3, SIBYLL 2.3D, EPOS-LHC and QGSJET-II.04) and snow overburdens for other years (2015 and 2018) yield similar results.

4. Uncontained Events

Previous analyses have required the shower core to land inside the IceTop array, and have been restricted to zenith angles up to 30° , which limits the statistics available at the highest energies. Air showers that land outside the IceTop array are of special interest. These events typically have no saturated tanks even at high energies, and when combined with the in-ice detector, can explore a larger range of zenith angles. This can help increase statistics and introduce greater variation in the distance to the shower maximum.

However, reconstructing uncontained events requires new methods. In particular, IceTop-InIce *coincidence* events are analyzed. The in-ice detector records signals from highly energetic muon bundles near the shower axis, providing an anchor for both the shower's core position and direction. While the electromagnetic component dominates near the shower core and produces HLC hits in IceTop, the signal further from the core is dominated by muons, which typically produce SLC hits. As muons are the primary contributors at large lateral distances, using SLC information becomes crucial for reconstructing air showers with cores far outside the array. To account for this, a *two-component lateral distribution function* (LDF) [8, 9] is employed that fits the charge distribution for the EM and muonic components separately using HLC and SLC hits. The EM charge distribution is described by the DLP function (Eq. (1)) with $\kappa = 0.30264$ as determined in Ref. [4]. To account for a more stable fit of the EM LDF, a larger reference distance of $r_{\text{EM, ref}} = 400$ m is chosen, as discussed in Section 1. The muon contribution is based on the Greisen LDF [10]:

$$S_\mu = S_{\mu,550} \left(\frac{r}{r_\mu} \right)^{-\beta_\mu} \left(\frac{r + 320 \text{ m}}{r_\mu + 320 \text{ m}} \right)^{-\gamma}, \quad r_\mu = 550 \text{ m}. \quad (5)$$

Where $S_{\mu,550}$ is the signal strength at a distance of 550 m of the shower core and β_μ and γ describe the slope of the muon LDF. Details can be found in Ref. [8]. The reconstruction is performed

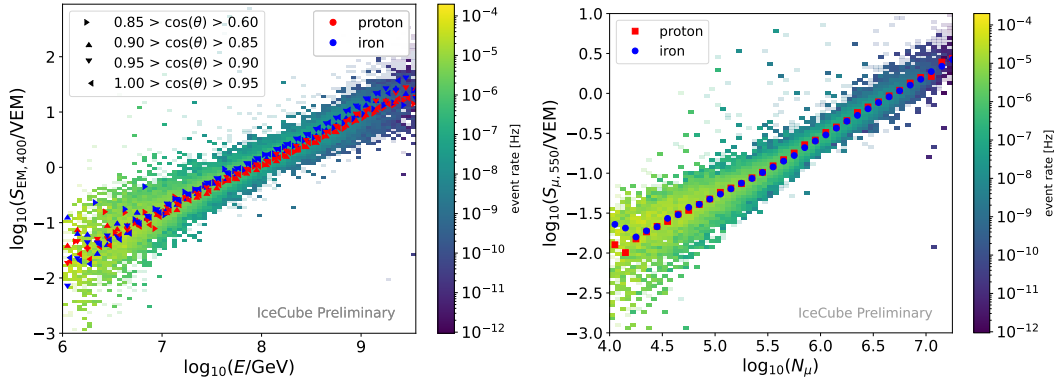


Figure 6: Energy proxy, $S_{EM,400}$ (left), and muon number proxy, $S_{\mu,550}$ (right) as a function true energy and true muon number, respectively. The 2d-histogram shows all simulated events (SIBYLL 2.1) weighted to a H4a cosmic-ray spectrum. The shaded events are excluded in the analysis. The markers show the mean value for the indicated zenith angles (left) and the complete zenith band (right). The marker color indicates the primary particle.

within the RockBottom framework [11] and uses a three-step maximum-likelihood method where the charges and timing of the measured signals are compared to the expected charge and timing distributions.

Step 1: An overall fit to a single IceTop LDF (S_{EM} and β_{EM} from Eq. (1)) as well as the track position and direction (x, y, θ, ϕ, t) is performed, using a combined likelihood from both IceTop HLC hits and in-ice hit information. S_{EM} is seeded with a weighted charge summed over all stations as suggested in Ref. [12].

Step 2: With the track position and direction from Step 1 held fixed, a "two-LDF" IceTop reconstruction is performed using both HLC's and SLC's from IceTop alone. The normalization and slope of the EM and muonic LDF (S_{EM}, β_{EM}), ($S_{\mu}, \beta_{\mu}, \gamma$) are fitted.

Step 3: The final step combines the features of Step 1 and Step 2. Information from both IceTop (HLC's and SLC's) and the in-ice detector are used for a combined reconstruction of a two-LDF model in IceTop and the position and direction of the track. All ten parameters—(S_{EM}, β_{EM}), ($S_{\mu}, \beta_{\mu}, \gamma$), and (x, y, θ, ϕ, t) — are fitted simultaneously.

The parameters S_{em} and S_{μ} are related to the primary cosmic ray energy and the number of muons, respectively. Their relationships are shown in Fig. 6. The simulated events are generated using CORSIKA [13] with the SIBYLL 2.1 hadronic interaction model [14], assuming the H4a cosmic ray flux model [15]. To ensure reliable in-ice information, only events located outside the 0.9 containment area of IceTop but within the 0.9 containment of IceCube are considered. Furthermore, events must show a coincidence between IceTop and IceCube and exceed a total charge of 100 PE in both detector components independently. To enhance the reconstruction quality, events with a total charge below 150 PE in HLC hits are excluded. Additional selection criteria are applied based on the bounds of the parameters β_{EM} and β_{μ} , as well as a fit quality requirement. Events not passing these cuts are shown with reduced opacity in Fig. 6. The resulting resolution and bias obtained with a cubic fit to the mean values are presented in Fig. 7. In the energy range from 10^7 GeV to 10^9 GeV, the energy resolution is below 0.2 in $\log_{10} E$. At higher energies, limited statistics reduce reliability.

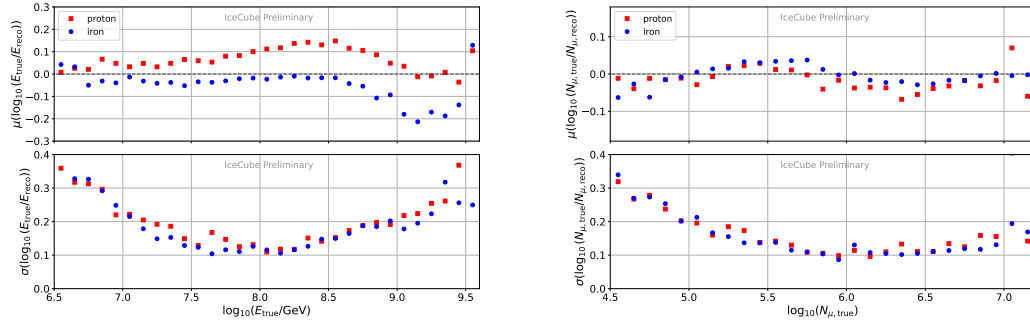


Figure 7: Left: Energy bias (upper) and resolution (lower) obtained with a cubic fit to the mean values of the four zenith angular ranges shown in Fig. 6. Right: Muon number bias (upper) and resolution (lower) obtained with one cubic fit.

The reconstruction of the muon number shows a better performance in terms of resolution and bias, and is compatible with the results obtained for contained events, as reported in Ref. [8, 9]. Ongoing efforts aim to further optimize both bias and resolution. Possible improvements include the use of a zenith- and distance-dependent conversion function, adjustments to the reference distance, and tighter selection cuts. These results demonstrate that the reconstruction of uncontained events is feasible. The selection criteria can be tailored to the specific goals of the analysis and offer a valuable complement to the well-established reconstruction of contained events—extending the phase space of reconstructable cosmic rays to larger zenith angles and higher energies.

5. Conclusion

Efforts to enhance IceTop’s measurement of the cosmic-ray spectrum are advancing along multiple fronts, aiming to increase statistics at the highest energies and reduce systematic uncertainties in that regime. The newly developed snow model allows for a uniform analysis of more than a decade of data. Improved selection criteria preserve more contained events with higher purity, while the capability to reconstruct uncontained events expands the accessible zenith range, enabling future analyses of the energy spectrum and composition of high-energy cosmic rays.

References

- [1] **Particle Data Group Collaboration** Collaboration, S. Navas *et al.*, *Phys. Rev. D* **110** (Aug, 2024) 030001.
- [2] **IceCube Collaboration**, M. G. Aartsen *et al.*, *Phys. Rev. D* **100** no. 8, (2019) 082002.
- [3] **IceCube Collaboration**, M. G. Aartsen *et al.*, *Phys. Rev. D* **102** (2020) 122001.
- [4] **IceCube Collaboration**, R. Abbasi *et al.*, *Nucl. Instrum. Meth. A* **700** (2013) 188–220.
- [5] **IceCube Collaboration**, S. Klepser *et al.*, *ICRC 2008*, 4, p. 35–38.
- [6] F. Kislak, *PhD thesis*, Humboldt University of Berlin, 2011.
- [7] **IceCube Collaboration**, K. Rawlins *et al.*, *PoS ICRC2023* (2024) 377.
- [8] **IceCube Collaboration**, M. Weyrauch, *PoS ICRC2025* (2025) 437. these proceedings.
- [9] **IceCube Collaboration**, L. Draper, F. Varsi, and D. Soldin, *PoS ICRC2025* (2025) 424. these proceedings.
- [10] K. Greisen, *Ann. Rev. Nucl. Part. Sci.* **10** (1960) 63–108.
- [11] **IceCube Collaboration**, A. Leszczynska *et al.*, *PoS ICRC2023* (2023) 366.
- [12] G. Ros *et al.*, *Astropart. Phys.* **35** (2011) 140–151.
- [13] D. Heck, J. Knapp, J. N. Capdevielle, G. Schatz, and T. Thouw, *FZKA-6019* (2, 1998).
- [14] E.-J. Ahn, R. Engel, T. K. Gaisser, P. Lipari, and T. Stanev, *Phys. Rev. D* **80** (2009) 094003.
- [15] T. K. Gaisser, *Astropart. Phys.* **35** (2012) 801–806.

Full Author List: IceCube Collaboration

R. Abbasi¹⁶, M. Ackermann⁶³, J. Adams¹⁷, S. K. Agarwalla^{39, a}, J. A. Aguilar¹⁰, M. Ahlers²¹, J.M. Alameddine²², S. Ali³⁵, N. M. Amin⁴³, K. Andeen⁴¹, C. Argüelles¹³, Y. Ashida⁵², S. Athanasiadou⁶³, S. N. Axani⁴³, R. Babu²³, X. Bai⁴⁹, J. Baines-Holmes³⁹, A. Balagopal V.^{39, 43}, S. W. Barwick²⁹, S. Bash²⁶, V. Basu⁵², R. Bay⁶, J. J. Beatty^{19, 20}, J. Becker Tjus^{9, b}, P. Behrens¹, J. Beise⁶¹, C. Bellenghi²⁶, B. Benkel⁶³, S. BenZvi⁵¹, D. Berley¹⁸, E. Bernardini^{47, c}, D. Z. Besson³⁵, E. Blaufuss¹⁸, L. Bloom⁵⁸, S. Blot⁶³, I. Bodo³⁹, F. Bontempo³⁰, J. Y. Book Motzkin¹³, C. Boscolo Meneguolo^{47, c}, S. Böser⁴⁰, O. Botner⁶¹, J. Böttcher¹, J. Braun³⁹, B. Brinson⁴, Z. Brisson-Tsavoussis³², R. T. Burley², D. Butterfield³⁹, M. A. Campana⁴⁸, K. Carloni¹³, J. Carpio^{33, 34}, S. Chattopadhyay^{39, a}, N. Chau¹⁰, Z. Chen⁵⁵, D. Chirkin³⁹, S. Choi⁵², B. A. Clark¹⁸, A. Coleman⁶¹, P. Coleman¹, G. H. Collin¹⁴, D. A. Coloma Borja⁴⁷, A. Connolly^{19, 20}, J. M. Conrad¹⁴, R. Corley⁵², D. F. Cowen^{59, 60}, C. De Clercq¹¹, J. J. DeLaunay⁵⁹, D. Delgado¹³, T. Delmeulle¹⁰, S. Deng¹, P. Desiati³⁹, K. D. de Vries¹¹, G. de Wasseige³⁶, T. DeYoung²³, J. C. Díaz-Vélez³⁹, S. DiKerby²³, M. Dittmer⁴², A. Domi²⁵, L. Draper⁵², L. Dueser¹, D. Durnford²⁴, K. Dutta⁴⁰, M. A. DuVernois³⁹, T. Ehrhardt⁴⁰, L. Eidenschink²⁶, A. Eimer²⁵, P. Eller²⁶, E. Ellinger⁶², D. Elsässer²², R. Engel^{30, 31}, H. Erpenbeck³⁹, W. Esmail⁴², S. Eulig¹³, J. Evans¹⁸, P. A. Evenson⁴³, K. L. Fan¹⁸, K. Fang³⁹, K. Farrag¹⁵, A. R. Fazely⁵, A. Fedynitch⁵⁷, N. Feigl⁸, C. Finley⁵⁴, L. Fischer⁶³, D. Fox⁵⁹, A. Franckowiak⁹, S. Fukami⁶³, P. Fürst¹, J. Gallagher³⁸, E. Ganster¹, A. Garcia¹³, M. Garcia⁴³, G. Garg^{39, a}, E. Genton^{13, 36}, L. Gerhardt⁷, A. Ghadimi⁵⁸, C. Glaser⁶¹, T. Glüsenkamp⁶¹, J. G. Gonzalez⁴³, S. Goswami^{33, 34}, A. Granados²³, D. Grant¹², S. J. Gray¹⁸, S. Griffin³⁹, S. Griswold⁵¹, K. M. Groth²¹, D. Guevel³⁹, C. Günther¹, P. Gutjahr²², C. Ha⁵³, C. Haack²⁵, A. Hallgren⁶¹, L. Halve¹, F. Halzen³⁹, L. Hamacher¹, M. Ha Minh²⁶, M. Handt¹, K. Hanson³⁹, J. Hardin¹⁴, A. A. Harnisch²³, P. Hatch³², A. Haungs³⁰, J. Häußler¹, K. Helbing⁶², J. Hellrung⁹, B. Henke²³, L. Hennig²⁵, F. Henningsen¹², L. Heuermann¹, R. Hewett¹⁷, N. Heyer⁶¹, S. Hickford⁶², A. Hidvegi⁵⁴, C. Hill¹⁵, G. C. Hill², R. Hmaid¹⁵, K. D. Hoffman¹⁸, D. Hooper³⁹, S. Hori³⁹, K. Hoshina^{39, d}, M. Hostert¹³, W. Hou³⁰, T. Huber³⁰, K. Hultqvist⁵⁴, K. Hymon^{22, 57}, A. Ishihara¹⁵, W. Iwakiri¹⁵, M. Jacquart²¹, S. Jain³⁹, O. Janik²⁵, M. Jansson³⁶, M. Jeong⁵², M. Jin¹³, N. Kamp¹³, D. Kang³⁰, W. Kang⁴⁸, X. Kang⁴⁸, A. Kappes⁴², L. Kardum²², T. Karg⁶³, M. Karl²⁶, A. Karle³⁹, A. Katil²⁴, M. Kauer³⁹, J. L. Kelley³⁹, M. Khanal⁵², A. Khatee Zathul³⁹, A. Kheirandish^{33, 34}, H. Kimku⁵³, J. Kiryluk⁵⁵, C. Klein²⁵, S. R. Klein^{6, 7}, Y. Kobayashi¹⁵, A. Kochocki²³, R. Koirala⁴³, H. Kolanoski⁸, T. Kontrimas²⁶, L. Köpke⁴⁰, C. Kopper²⁵, D. J. Koskinen²¹, P. Koundal⁴³, M. Kowalski^{8, 63}, T. Kozynets²¹, N. Krieger⁹, J. Krishnamoorthi^{39, a}, T. Krishnan¹³, K. Kruiswijk³⁶, E. Krupczak²³, A. Kumar⁶³, E. Kun⁹, N. Kurahashi⁴⁸, N. Lad⁶³, C. Lagunas Gualda²⁶, L. Lallement Arnaud¹⁰, M. Lamoureux³⁶, M. J. Larson¹⁸, F. Lauber⁶², J. P. Lazar³⁶, K. Leonard DeHoltan⁶⁰, A. Leszczyńska⁴³, J. Liao⁴, C. Lin⁴³, Y. T. Liu⁶⁰, M. Liubarska²⁴, C. Love⁴⁸, L. Lu³⁹, F. Lucarelli²⁷, W. Luszczyk^{19, 20}, Y. Lyu^{6, 7}, J. Madsen³⁹, E. Magnus¹¹, K. B. M. Mahn²³, Y. Makino³⁹, E. Manao²⁶, S. Mancina^{47, e}, A. Mand³⁹, I. C. Mariş¹⁰, S. Marka⁴⁵, Z. Marka⁴⁵, L. Marten¹, I. Martinez-Soler¹³, R. Maruyama⁴⁴, J. Mauro³⁶, F. Mayhew²³, F. McNally³⁷, J. V. Mead²¹, K. Meagher³⁹, S. Mechbal⁶³, A. Medina²⁰, M. Meier¹⁵, Y. Merckx¹¹, L. Merten⁹, J. Mitchell⁵, L. Molchany⁴⁹, T. Montaruli²⁷, R. W. Moore²⁴, Y. Morii¹⁵, A. Mosbrugger²⁵, M. Moulai³⁹, D. Mousadi⁶³, E. Moyaux³⁶, T. Mukherjee³⁰, R. Naab⁶³, M. Nakos³⁹, U. Naumann⁶², J. Necker⁶³, L. Neste⁵⁴, M. Neumann⁴², H. Niederhausen²³, M. U. Nisa²³, K. Noda¹⁵, A. Noell¹, A. Novikov⁴³, A. Obertacke Pollmann¹⁵, V. O'Dell³⁹, A. Olivas¹⁸, R. Orsoe²⁶, J. Osborn³⁹, E. O'Sullivan⁶¹, V. Palusova⁴⁰, H. Pandya⁴³, A. Parenti¹⁰, N. Park³², V. Parrish²³, E. N. Paudel⁵⁸, L. Paul⁴⁹, C. Pérez de los Heros⁶¹, T. Pernice⁶³, J. Peterson³⁹, M. Plum⁴⁹, A. Pontén⁶¹, V. Poojyam⁵⁸, Y. Popovych⁴⁰, M. Prado Rodriguez³⁹, B. Pries²³, R. Procter-Murphy¹⁸, G. T. Przybylski⁷, L. Pyras⁵², C. Raab³⁶, J. Rack-Helleis⁴⁰, N. Rad⁶³, M. Ravn⁶¹, K. Rawlins³, Z. Rechav³⁹, A. Rehman⁴³, I. Reistoffer⁴⁹, E. Resconi²⁶, S. Reusch⁶³, C. D. Rho⁵⁶, W. Rhode²², L. Ricca³⁶, B. Riedel³⁹, A. Rifaie⁶², E. J. Roberts², S. Robertson^{6, 7}, M. Rongen²⁵, A. Rosted¹⁵, C. Rott⁵², T. Ruhe²², L. Ruohan²⁶, D. Ryckbosch²⁸, J. Saffer³¹, D. Salazar-Gallegos²³, P. Sampathkumar³⁰, A. Sandrock⁶², G. Sanger-Johnson²³, M. Santander⁵⁸, S. Sarkar⁴⁶, J. Savelberg¹, M. Scarnera³⁶, P. Schaile²⁶, M. Schaufel¹, H. Schieler³⁰, S. Schindler²⁵, L. Schlickmann⁴⁰, B. Schlüter⁴², F. Schlüter¹⁰, N. Schmeisser⁶², T. Schmidt¹⁸, F. G. Schröder^{30, 43}, L. Schumacher²⁵, S. Schwirn¹, S. Sclafani¹⁸, D. Seckel⁴³, L. Seen³⁹, M. Seikh³⁵, S. Seunarine⁵⁰, P. A. Seville Myhr³⁶, R. Shah⁴⁸, S. Shefali³¹, N. Shimizu¹⁵, B. Skrzypek⁶, R. Snihur³⁹, J. Soedingrekso²², A. Sogaard²¹, D. Soldin⁵², P. Soldin¹, G. Sommani⁹, C. Spannfellner²⁶, G. M. Spiczak⁵⁰, C. Spiering⁶³, J. Stachurska²⁸, M. Stamatikos²⁰, T. Stanev⁴³, T. Stezelberger⁷, T. Stürwald⁶², T. Stuttard²¹, G. W. Sullivan¹⁸, I. Taboada⁴, S. Ter-Antonyan⁵, A. Terliuk²⁶, A. Thakuri⁴⁹, M. Thiesmeyer³⁹, W. G. Thompson¹³, J. Thwaites³⁹, S. Tilav⁴³, K. Tollefson²³, S. Toscano¹⁰, D. Tosi³⁹, A. Trettin⁶³, A. K. Upadhyay^{39, a}, K. Upshaw⁵, A. Vaidyanathan⁴¹, N. Valtonen-Mattila^{9, 61}, J. Valverde⁴¹, J. Vandenbroucke³⁹, T. van Eeden⁶³, N. van Eijndhoven¹¹, L. van Rootselaar²², J. van Santen⁶³, F. J. Vara Carbonell⁴², F. Varsi³¹, M. Venugopal³⁰, M. Vereecken³⁶, S. Vergara Carrasco¹⁷, S. Verpoest⁴³, D. Veske⁴⁵, A. Vijai¹⁸, J. Villarreal¹⁴, C. Walck⁵⁴, A. Wang⁴, E. Warrick⁵⁸, C. Weaver²³, P. Weigel¹⁴, A. Weindl³⁰, J. Weldert⁴⁰, A. Y. Wen¹³, C. Wendt³⁹, J. Werthebach²², M. Weyrauch³⁰, N. Whitehorn²³, C. H. Wiebusch¹, D. R. Williams⁵⁸, L. Witthaus²², M. Wolf²⁶, G. Wrede²⁵, X. W. Xu⁵, J. P. Yañez²⁴, Y. Yao³⁹, E. Yildizci³⁹, S. Yoshida¹⁵, R. Young³⁵, F. Yu¹³, S. Yu⁵², T. Yuan³⁹, A. Zegarelli⁹, S. Zhang²³, Z. Zhang⁵⁵, P. Zhelnin¹³, P. Zilberman³⁹

¹ III. Physikalisches Institut, RWTH Aachen University, D-52056 Aachen, Germany

² Department of Physics, University of Adelaide, Adelaide, 5005, Australia

³ Dept. of Physics and Astronomy, University of Alaska Anchorage, 3211 Providence Dr., Anchorage, AK 99508, USA

⁴ School of Physics and Center for Relativistic Astrophysics, Georgia Institute of Technology, Atlanta, GA 30332, USA

⁵ Dept. of Physics, Southern University, Baton Rouge, LA 70813, USA

⁶ Dept. of Physics, University of California, Berkeley, CA 94720, USA

⁷ Lawrence Berkeley National Laboratory, Berkeley, CA 94720, USA

⁸ Institut für Physik, Humboldt-Universität zu Berlin, D-12489 Berlin, Germany

⁹ Fakultät für Physik & Astronomie, Ruhr-Universität Bochum, D-44780 Bochum, Germany

¹⁰ Université Libre de Bruxelles, Science Faculty CP230, B-1050 Brussels, Belgium

- ¹¹ Vrije Universiteit Brussel (VUB), Dienst ELEM, B-1050 Brussels, Belgium
- ¹² Dept. of Physics, Simon Fraser University, Burnaby, BC V5A 1S6, Canada
- ¹³ Department of Physics and Laboratory for Particle Physics and Cosmology, Harvard University, Cambridge, MA 02138, USA
- ¹⁴ Dept. of Physics, Massachusetts Institute of Technology, Cambridge, MA 02139, USA
- ¹⁵ Dept. of Physics and The International Center for Hadron Astrophysics, Chiba University, Chiba 263-8522, Japan
- ¹⁶ Department of Physics, Loyola University Chicago, Chicago, IL 60660, USA
- ¹⁷ Dept. of Physics and Astronomy, University of Canterbury, Private Bag 4800, Christchurch, New Zealand
- ¹⁸ Dept. of Physics, University of Maryland, College Park, MD 20742, USA
- ¹⁹ Dept. of Astronomy, Ohio State University, Columbus, OH 43210, USA
- ²⁰ Dept. of Physics and Center for Cosmology and Astro-Particle Physics, Ohio State University, Columbus, OH 43210, USA
- ²¹ Niels Bohr Institute, University of Copenhagen, DK-2100 Copenhagen, Denmark
- ²² Dept. of Physics, TU Dortmund University, D-44221 Dortmund, Germany
- ²³ Dept. of Physics and Astronomy, Michigan State University, East Lansing, MI 48824, USA
- ²⁴ Dept. of Physics, University of Alberta, Edmonton, Alberta, T6G 2E1, Canada
- ²⁵ Erlangen Centre for Astroparticle Physics, Friedrich-Alexander-Universität Erlangen-Nürnberg, D-91058 Erlangen, Germany
- ²⁶ Physik-department, Technische Universität München, D-85748 Garching, Germany
- ²⁷ Département de physique nucléaire et corpusculaire, Université de Genève, CH-1211 Genève, Switzerland
- ²⁸ Dept. of Physics and Astronomy, University of Gent, B-9000 Gent, Belgium
- ²⁹ Dept. of Physics and Astronomy, University of California, Irvine, CA 92697, USA
- ³⁰ Karlsruhe Institute of Technology, Institute for Astroparticle Physics, D-76021 Karlsruhe, Germany
- ³¹ Karlsruhe Institute of Technology, Institute of Experimental Particle Physics, D-76021 Karlsruhe, Germany
- ³² Dept. of Physics, Engineering Physics, and Astronomy, Queen's University, Kingston, ON K7L 3N6, Canada
- ³³ Department of Physics & Astronomy, University of Nevada, Las Vegas, NV 89154, USA
- ³⁴ Nevada Center for Astrophysics, University of Nevada, Las Vegas, NV 89154, USA
- ³⁵ Dept. of Physics and Astronomy, University of Kansas, Lawrence, KS 66045, USA
- ³⁶ Centre for Cosmology, Particle Physics and Phenomenology - CP3, Université catholique de Louvain, Louvain-la-Neuve, Belgium
- ³⁷ Department of Physics, Mercer University, Macon, GA 31207-0001, USA
- ³⁸ Dept. of Astronomy, University of Wisconsin—Madison, Madison, WI 53706, USA
- ³⁹ Dept. of Physics and Wisconsin IceCube Particle Astrophysics Center, University of Wisconsin—Madison, Madison, WI 53706, USA
- ⁴⁰ Institute of Physics, University of Mainz, Staudinger Weg 7, D-55099 Mainz, Germany
- ⁴¹ Department of Physics, Marquette University, Milwaukee, WI 53201, USA
- ⁴² Institut für Kernphysik, Universität Münster, D-48149 Münster, Germany
- ⁴³ Bartol Research Institute and Dept. of Physics and Astronomy, University of Delaware, Newark, DE 19716, USA
- ⁴⁴ Dept. of Physics, Yale University, New Haven, CT 06520, USA
- ⁴⁵ Columbia Astrophysics and Nevis Laboratories, Columbia University, New York, NY 10027, USA
- ⁴⁶ Dept. of Physics, University of Oxford, Parks Road, Oxford OX1 3PU, United Kingdom
- ⁴⁷ Dipartimento di Fisica e Astronomia Galileo Galilei, Università Degli Studi di Padova, I-35122 Padova PD, Italy
- ⁴⁸ Dept. of Physics, Drexel University, 3141 Chestnut Street, Philadelphia, PA 19104, USA
- ⁴⁹ Physics Department, South Dakota School of Mines and Technology, Rapid City, SD 57701, USA
- ⁵⁰ Dept. of Physics, University of Wisconsin, River Falls, WI 54022, USA
- ⁵¹ Dept. of Physics and Astronomy, University of Rochester, Rochester, NY 14627, USA
- ⁵² Department of Physics and Astronomy, University of Utah, Salt Lake City, UT 84112, USA
- ⁵³ Dept. of Physics, Chung-Ang University, Seoul 06974, Republic of Korea
- ⁵⁴ Oskar Klein Centre and Dept. of Physics, Stockholm University, SE-10691 Stockholm, Sweden
- ⁵⁵ Dept. of Physics and Astronomy, Stony Brook University, Stony Brook, NY 11794-3800, USA
- ⁵⁶ Dept. of Physics, Sungkyunkwan University, Suwon 16419, Republic of Korea
- ⁵⁷ Institute of Physics, Academia Sinica, Taipei, 11529, Taiwan
- ⁵⁸ Dept. of Physics and Astronomy, University of Alabama, Tuscaloosa, AL 35487, USA
- ⁵⁹ Dept. of Astronomy and Astrophysics, Pennsylvania State University, University Park, PA 16802, USA
- ⁶⁰ Dept. of Physics, Pennsylvania State University, University Park, PA 16802, USA
- ⁶¹ Dept. of Physics and Astronomy, Uppsala University, Box 516, SE-75120 Uppsala, Sweden
- ⁶² Dept. of Physics, University of Wuppertal, D-42119 Wuppertal, Germany
- ⁶³ Deutsches Elektronen-Synchrotron DESY, Platanenallee 6, D-15738 Zeuthen, Germany
- ^a also at Institute of Physics, Sachivalaya Marg, Sainik School Post, Bhubaneswar 751005, India
- ^b also at Department of Space, Earth and Environment, Chalmers University of Technology, 412 96 Gothenburg, Sweden
- ^c also at INFN Padova, I-35131 Padova, Italy
- ^d also at Earthquake Research Institute, University of Tokyo, Bunkyo, Tokyo 113-0032, Japan
- ^e now at INFN Padova, I-35131 Padova, Italy

Acknowledgments

The authors gratefully acknowledge the support from the following agencies and institutions: USA – U.S. National Science Foundation-Office of Polar Programs, U.S. National Science Foundation-Physics Division, U.S. National Science Foundation-EPSCoR, U.S. National Science Foundation-Office of Advanced Cyberinfrastructure, Wisconsin Alumni Research Foundation, Center for High Throughput Computing (CHTC) at the University of Wisconsin–Madison, Open Science Grid (OSG), Partnership to Advance Throughput Computing (PATH), Advanced Cyberinfrastructure Coordination Ecosystem: Services & Support (ACCESS), Frontera and Ranch computing project at the Texas Advanced Computing Center, U.S. Department of Energy-National Energy Research Scientific Computing Center, Particle astrophysics research computing center at the University of Maryland, Institute for Cyber-Enabled Research at Michigan State University, Astroparticle physics computational facility at Marquette University, NVIDIA Corporation, and Google Cloud Platform; Belgium – Funds for Scientific Research (FRS-FNRS and FWO), FWO Odysseus and Big Science programmes, and Belgian Federal Science Policy Office (Belspo); Germany – Bundesministerium für Forschung, Technologie und Raumfahrt (BMFT), Deutsche Forschungsgemeinschaft (DFG), Helmholtz Alliance for Astroparticle Physics (HAP), Initiative and Networking Fund of the Helmholtz Association, Deutsches Elektronen Synchrotron (DESY), and High Performance Computing cluster of the RWTH Aachen; Sweden – Swedish Research Council, Swedish Polar Research Secretariat, Swedish National Infrastructure for Computing (SNIC), and Knut and Alice Wallenberg Foundation; European Union – EGI Advanced Computing for research; Australia – Australian Research Council; Canada – Natural Sciences and Engineering Research Council of Canada, Calcul Québec, Compute Ontario, Canada Foundation for Innovation, WestGrid, and Digital Research Alliance of Canada; Denmark – Villum Fonden, Carlsberg Foundation, and European Commission; New Zealand – Marsden Fund; Japan – Japan Society for Promotion of Science (JSPS) and Institute for Global Prominent Research (IGPR) of Chiba University; Korea – National Research Foundation of Korea (NRF); Switzerland – Swiss National Science Foundation (SNSF).