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Effects of Ground Rubber Loading on Rubber Compounds Studied by the Hyphenated Rheo-NMR and the Palierne Model

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ABSTRACT

This article investigates the effect of ground rubber (GR) loading of rubber compounds using the unique hyphenated Rheo-NMR setup. This setup is used to quantify the effects on the rheological behavior as an emulsion-like blend as well as of the further vulcanization of the GR particle due to sulfur diffusion. The GR as a sustainable component of rubber compounds affects engineering properties. This can be explained by the diffusion of free sulfur from the rubber matrix into the GR particles, resulting in a change in cross-link density (CLD) in the matrix and the GR particles. Another effect that occurs is the emulsion-like blend of GR particles within the rubber matrix describable by adequate constitutive emulsion models. Rubber compounds of styrene-butadiene rubber (SBR) and natural rubber (NR) were used both for the rubber matrix and the self-produced GR. The predictions by the Palierne model describe the rheology with a deviation of up to 15%. NMR results of the GR particle show an increase of 100% in CLD for NR, while SBR shows a decrease of around 13%. Such results have not covered in the literature so far and are of great importance to optimize recycling of rubber materials.

1 | Introduction

More than three million tons of passenger car and truck tires are accumulated every year in the European Union after their use [1]. Worldwide, the amount is assumed to be 10 times higher [2]. To advance toward a circular economy, recycling is essential. A potential method is the incorporation of ground rubber (GR) (particle size ranges from 0.2 to 2 mm) into rubber compounds prior to vulcanization [3–7].

The incorporation of GR particles deteriorates the properties of the final product, for example, tensile strength, compared to formulations without GR particles [5, 8]. This can be explained by both emulsion-like blend of the GR particles in the rubber matrix and a change in CLD in the rubber matrix and GR particles due to sulfur diffusion, as shown in Figure 1.

1.1 | Sulfur Diffusion From Matrix Into GR Particle

The effect of sulfur diffusion from the matrix into the GR particle originates from free, non-covalently bound sulfur (S_8) in the matrix. This diffusion happens during mixing, storage, and vulcanization of the rubber compound. It occurs because S_8 sulfur in the rubber matrix is free and mobile, while sulfur in the already vulcanized GR particles is predominantly covalently bound to the polymer chains. Therefore, there is a difference in the chemical potential of free sulfur. The S_8 diffusion lowers the overall sulfur concentration in the rubber matrix with a certain gradient and raises it in the GR particles. It is evident that higher amounts of sulfur lead to a higher cross-link density (CLD) during vulcanization [5, 9–11]. Therefore, diffusion of free S_8 sulfur leads to an increase in the CLD in the GR particles and to a lower CLD in the

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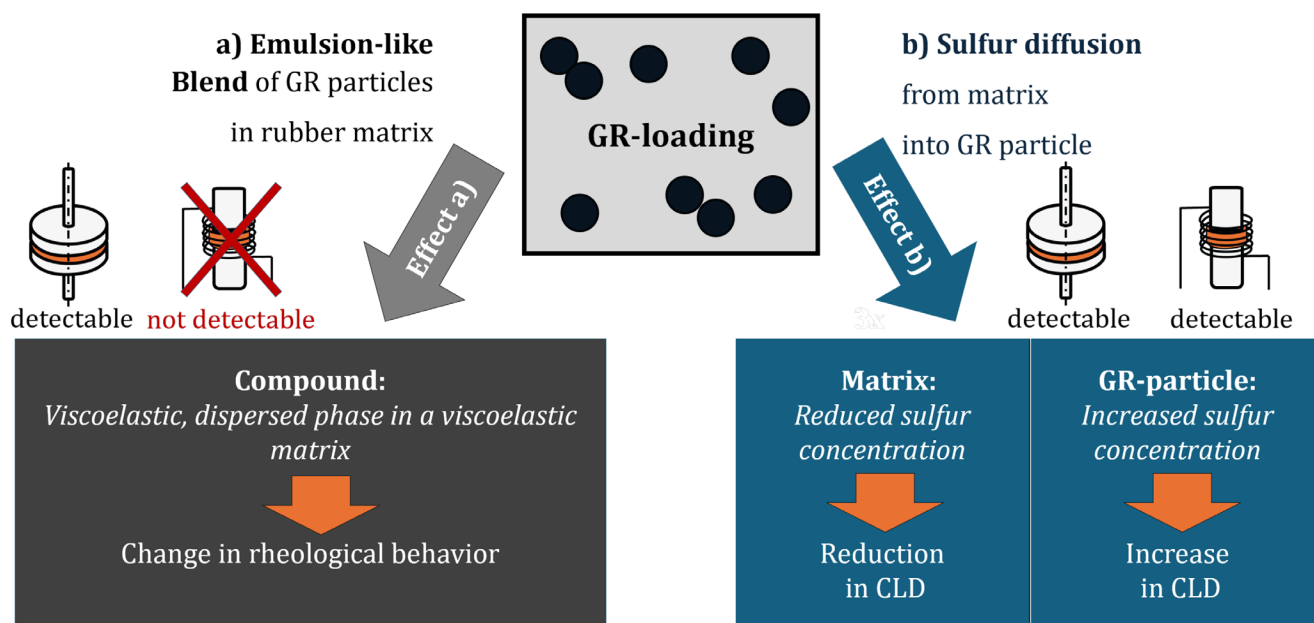


FIGURE 1 | Effects of GR loading on the vulcanization behavior measured by Rheology and TD-NMR. The effect of the emulsion-like blend of GR particles in the rubber matrix can only be measured by rheology, while the change in CLD due to sulfur diffusion can be measured by both rheology and TD-NMR. [Color figure can be viewed at [wileyonlinelibrary.com](https://onlinelibrary.wiley.com)] [9]

rubber matrix material than intended [10]. Additionally, diffusion of accelerators from the GR particles into the rubber matrix alters the free sulfur-to-accelerator ratio in both phases [9].

1.2 | Emulsion-Like Blends of GR Particles in the Rubber Matrix

Another concern encountered when incorporating GR particles in rubber compounds is a theoretical change in the storage modulus G' according to emulsion theories for soft matter. This effect has not been covered in the literature so far. For quantitative description, the well-known Palierne model is used, which can be applied to polymer blends above T_g [12, 13].

The Palierne model describes the rheological behavior of blends of viscoelastic dispersed phase in a viscoelastic matrix under the assumption of a spherical shape of the dispersed phase and includes the effects of hydrodynamic interaction, the size of the dispersed phase, the size distribution, and the interfacial tension. For low interfacial tension ($< 1 \text{ mN m}^{-1}$) and greater radius of the dispersed phase ($> 0.1 \text{ mm}$) the Palierne model can be expressed as [14, 15]:

$$G^* = G_{ma}^* \cdot \left(1 + 3\phi \frac{V_r - 1}{2V_r + 3}\right) \cdot \left(1 + 2\phi \frac{V_r - 1}{2V_r + 3}\right)^{-1}, \quad (1)$$

where G_{ma}^* is the complex modulus of the pure rubber matrix. V_r is the ratio of the complex modulus of the dispersed GR particles (G_{GR}^*) to the complex modulus of the rubber matrix (G_{ma}^*) and ϕ is the volume fraction of GR particles.

Both the diffusion of sulfur and the emulsion-like blend of GR particles in the rubber matrix lead to a significant change in G' . Therefore, it is challenging to study both effects individually.

The simultaneous measurement of molecular and macroscopic properties during vulcanization by the unique Rheo-NMR combination helps to differentiate between these two effects.

1.3 | Measurement of the Vulcanization Reaction and CLD

Macroscopically, the rubber vulcanization reaction is typically studied through its time dependent rheological response, such as tracking the development of the storage modulus G' during the formation of a chemically crosslinked network. For this purpose, closed-cavity rheometers (CCR) are commonly utilized in rubber research and industry. The cavity of this instrument is sealed to allow the application of pressure during vulcanization. A grooved cone–cone geometry is used to prevent wall slippage at high strain amplitudes [16]. According to the theory of rubber elasticity, the plateau modulus G_N is proportional to the effective CLD ν (in mol mm^{-3}) of the network at a given temperature T [17], which can be written as:

$$G_N = \nu RT, \quad (2)$$

where R is the universal gas constant. Typically, $G'(t_{vulc})$ [18, 19], the absolute value of the torque $|S^*|(t_{vulc})$ [5, 9, 20], or the in-phase torque $S'(t_{vulc})$ [3, 11] (reflecting the elastic contribution) are used to monitor the time dependent vulcanization.

On a molecular length scale ($< 10 \text{ nm}$) [21] the influence of the crosslinking upon the network chain dynamics can be studied by time-domain nuclear magnetic resonance (TD-NMR) utilizing a low-field NMR relaxometer (Larmor frequency range of 10 to 60 MHz). By using pulse sequences such as Hahn echo or Carr–Purcell–Meiboom–Gill (CPMG) it is possible to measure and quantify proton transverse relaxation times, which are sensitive to the local molecular mobility of

the polymer segments. An increase in the degree of crosslinking typically results in shorter ^1H transverse relaxation times (T_2) [19, 22–25]. Continuously measuring the average T_2 and T_2 distributions of the polymer protons by TD-NMR with a time resolution of approximately 30 s is a method monitoring the network constitution. At measurement temperatures well above the glass transition T_g (typically $T > T_g + 100\text{ K}$), the NMR transverse relaxation (T_2^*) of rubber is dominated by the fluctuating motion between crosslinks and is therefore a function of the CLD. Additionally, at these temperatures T_2 is rather independent of the temperature [24–28].

For crosslinked polymers, extensive studies have been conducted to establish a molecular-macroscopic correlation by measuring both the macroscopic modulus through rheological methods and the microscopic dynamics via TD-NMR measurements [18, 19, 22, 24, 29–31]. These studies indicate that at the above mentioned temperatures, the inverse transverse relaxation time (T_2^{*-1}) increases linearly with the molecular weight of the network chains (typical slope of $1\text{ kg mmol}^{-1}\text{ s}^{-1}$ [22]).

The group of Wilhelm developed a setup that couples a high-end plate–plate rheometer with a low-field NMR relaxometer (abbreviated “Rheo-NMR”) and thus provides the opportunity to obtain an in situ molecular-macroscopic correlation of various polymer materials [19, 21, 32–34]. This unique setup correlates both parameters, G' and T_2^{*-1} . That addresses the frequently encountered issues related to correlation measurements obtained from different devices, as varying methods may differ in sample preparation, experimental design, and measurement conditions, such as heating rate, exact temperature, or thermal conductivity. Consequently, direct correlation of such data is rare. Nie et al. applied Rheo-NMR to compare conventional and efficient vulcanization systems and obtained a direct molecular-macroscopic correlation between G' and T_2^{*-1} [19].

1.4 | Scope of This Article

This article presents an analysis of vulcanization in pure and GR loaded rubber compounds by Rheo-NMR. During the vulcanization of six different rubber compounds, both the rheological characterization and the TD-NMR experiments were carried out simultaneously. Each data set was analyzed to evaluate the vulcanization reaction measured with the different methods to assess the impact of the GR loading. Additionally, the direct G' - T_2^{*-1} -correlation was analyzed for the pure compounds during vulcanization. The Palierne model was used to compare the results with theoretical predictions with the measured data of G' . In addition, the resulting change in the transverse relaxation

time of the GR particles T_2^{*-1} is determined and analyzed to assess the further vulcanization of the GR particles.

2 | Materials and Methods

The studied materials are identical to those used by Frosch et al. [35]. The sample processing is the same as the processing in the cited article.

2.1 | Rubber Compound Formulations and Mixing Conditions

In the presented study two different basic rubber formulations based on natural rubber (NR) and styrene-butadiene rubber (SBR) were investigated. The different formulations with their respective amount of GR, including the trade names of each component, are shown in ref. [35].

The GR is produced the same way as the pure compounds, but is vulcanized, cryogenic ground, and then mixed into the respective matrix compound.

Throughout this article the pure rubber compounds without GR are named NR_{ma} and SBR_{ma} rubber compounds and serve as reference samples. The SBR_{ma} compounds and the GR loaded rubber compounds with SBR in the rubber matrix will be called SBR compounds and vice versa. In diagrams a SBR rubber compound is shown with a violet rectangle and NR compounds are shown with a turquoise rectangle. Additionally, GR loading is indicated with circles inside this rectangle with their associated color.

Table 1 shows a comparison of some selected molecular properties of the two polymers used.

The detailed procedure for mixing the different samples is described by Frosch et al. [35]. In this article, six samples with the respective volume fraction of GR particles were analyzed as shown in Table 2. The volumetric fraction of the GR particle in the rubber compounds is in all combinations very similar and corresponds to an typical used level, while higher concentrations ($< 50\%$) are with certain adjustments reachable [38].

2.2 | Vulcanization Kinetics Using a Closed-Cavity Rheometer

A SIS V50 from TA Instruments, Eschborn, Germany (former Scarabaeus) was used to analyze the vulcanization kinetics

TABLE 1 | Comparison of the molecular properties of the used polymers for the different compounds and GR particles.

Polymer	Density [kg l^{-1}]	Trans-1,4-content [%]	Cis-1,4-content [%]	Vinyl-1,2-content [%]	T_g [$^{\circ}\text{C}$]	Mooney viscosity ^c [MU]
NR	0.93 ^b	$< 1^b$	99 ^b	$< 1^b$	-73^b	50.7
SBR	0.94 ^a	76 ^a	9 ^a	15 ^a	-50^b	49 ^a

^aTaken from ref. [36].

^bTaken from ref. [37].

^cML (100 $^{\circ}\text{C}$, 1 + 4 min).

TABLE 2 | Studied samples in this article with their respective calculated compound density ρ and the volume fraction ϕ of the GR particles in the rubber compound.

Sample notation	Symbol in diagrams	Matrix polymer	GR polymer	ρ [kg l ⁻¹]	ϕ (GR particles) [%]
NR _{ma}		NR	—	1.131	—
NR _{ma} + NR _{GR}		NR	NR	1.131	15.8
NR _{ma} + SBR _{GR}		NR	SBR	1.132	15.6
SBR _{ma}		SBR	—	1.140	—
SBR _{ma} + SBR _{GR}		SBR	SBR	1.140	15.8
SBR _{ma} + NR _{GR}		SBR	NR	1.139	15.9

Note: Sample notation follows the following principle: >matrix polymer<_{ma} +>Ground rubber polymer<_{GR}.

of all samples as a reference. A time sweep was conducted at $T = 160^\circ\text{C}$, with an angular frequency of $\omega/2\pi = 1.67\text{Hz}$, and an oscillation strain amplitude of $\gamma_0 = 0.5\%$.

2.3 | Rheo-NMR

2.3.1 | Rheo-NMR Setup

There are different hyphenated Rheo-NMR setups with their respective applications. A combination of high-field NMR with a simple shear experiment is used to evaluate shear fields [39–44]. With a unique combination of a compact low-field NMR magnet and a high-end oscillatory rheometer we can carry out rheological characterization in shear, both in the linear and nonlinear regime. The detailed device descriptions are named at the end of this section. The latter setup is used in this article. A schematic overview of this setup and the magnet has been published multiple times [19, 21, 32–34]. The magnet is constructed with NdFeB magnet bars in a Halbach array to create a static homogeneous magnetic field ($\Delta B_0/B_0 \approx 1 \cdot 10^{-3}$) with a field strength of $\Delta B_0 \approx 0.59\text{ T}$, which corresponds to a 1H Larmor frequency of $\omega_L/2\pi \approx 25\text{ MHz}$. The pulse lengths for 90° and 180° are $t_{90} = 2.8\text{ }\mu\text{s}$ and $t_{180} = 5.4\text{ }\mu\text{s}$, respectively [32]. The receiver dead time was determined to be 10 μs . During the Rheo-NMR measurement, the magnet was electrically heated and kept constant at 45°C to reduce the drift of the B_0 field. The rheological measurements were conducted using a ceramic plate–plate geometry with 13 mm. The design of the probe, the heating unit, the thermal isolation, and the magnetic-field shielding can be found in ref. [32]. A DHR 3 (TA Instruments, USA) was used for rheological measurements. During vulcanization, the temperature of the sample was controlled by a Bruker Variable Temperature (BVT) unit (Bruker, Rheinstetten, Germany). A nitrogen gas flow of 900 L min^{-1} was used to heat and to prevent sample oxidation.

TD-NMR data were measured using a Minispec mq20 amplifier from Bruker, Rheinstetten, Germany. The rheological data were measured using a DHR-3 from TA Instruments, Eschborn, Germany.

2.4 | Measurement of Rheology and TD-NMR by Rheo-NMR

The rubber compounds were pressed into 1.5 mm sheets at 40°C for 3 min, to avoid crosslinking and then disks with a diameter of 10 mm were punched. The samples were then loaded in a few seconds onto the upper plate and then the geometry was closed at a normal force of 0.3 N (resulting in an initial pressure of 96 Pa). After $t_{\text{vulc}} > 100\text{ s}$ the normal force was increased to 40 N (resulting in a final pressure of 32 kPa) to prevent the formation of bubbles inside the rubber compound due to vulcanization. This time was found to be as late as possible to prevent significant flow of the rubber from getting out of the geometry, but as early as needed to prevent the formation of bubbles. The procedure results in a sample with 13 mm and no bubbles after vulcanization.

All isothermal crosslinking experiments were carried out at $T_{\text{vulc}} = 140^\circ\text{C}$, 150°C , and 160°C . Two vulcanization experiments were performed for each rubber compound to assess the reproducibility. The time dependent rheological properties were quantified by dynamic time sweep at $\omega/2\pi = 1.67\text{ Hz}$ and at a strain amplitude of $\gamma_0 = 1\%$ using a grooved plate–plate geometry to prevent wall slippage.

Simultaneous TD-NMR transverse relaxation measurements were continuously executed with a combined pulse sequence of a magic sandwich echo (MSE) and multiple echoes of “xx4.” The xx4 is a CPMG (based on Carr and Purcell [45] and Meiboom and Gill [46]) pulse sequence with 180° phase shifting after each 180° -pulse, which can prevent spin-locking [47]. Several authors report that the T_2 determined by a CPMG pulse sequence depends on the pulse spacing [48, 49]. To avoid any confusion about the determined value of T_2 , it will be named as an apparent transverse relaxation time, T_2^{*-1} , which still reflects the semi-local molecular dynamics. The recycle delay (RD) was set as 2.5 s, corresponding to five times the longitudinal relaxation time T_1 , to provide quantitative relaxation of the protons. During vulcanization the decaying transverse magnetization intensity $I(t_{\text{vulc}})$ from the MSE-xx4 pulse sequence was recorded as a function of the total sequence time $\Delta\tau_{\text{xx4}}$ with eight scans applied for each NMR relaxation signal. This results in a $t_{\text{NMR}} = 29.5\text{ s}$ for each TD-NMR data point

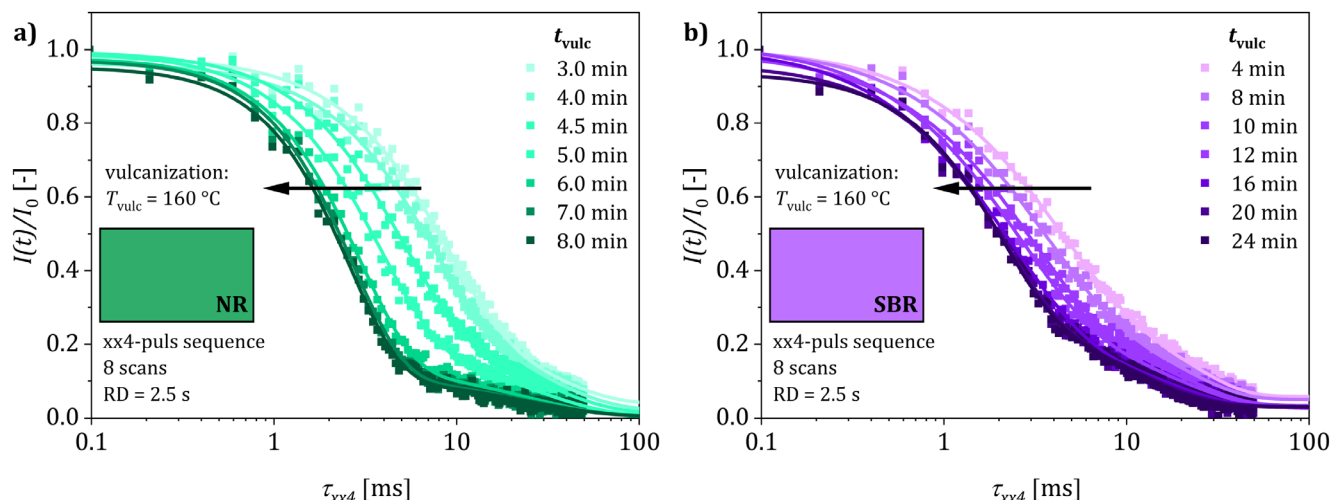


FIGURE 2 | An example of the evolution of normalized magnetization $I(\tau)/I_0$ during vulcanization from TD-NMR measurements with the xx4-CPMG pulse sequence at specially selected t_{vulc} . I_0 is defined as the first measured $I(\tau = 0.01 \mu\text{s})$. In (a) the evolution of the signal of the NR_{ma} compound and in (b) of the SBR_{ma} compound can be seen. The data were fitted using Equation (4). The resulting T_2^{*-1} can be found in Figure 5 at all measured t_{vulc} . The MSE signal was not used for investigation, consequently not shown. [Color figure can be viewed at [wileyonlinelibrary.com](https://onlinelibrary.wiley.com)]

T_2^{*-1} , extracted from fitting the relaxation curve obtained (see below). The xx-4 pulse sequence was applied with a spacing time $2\Delta\tau_{\text{xx4}} = 200 \mu\text{s}$ and 512 echoes.

2.4.1 | TD-NMR Data Analysis

The TD-NMR data were analyzed using the transverse relaxation time T_2 . The T_2 is more strongly influenced by the strength of local proton–proton spin–spin interactions ($< 2 \text{ nm}$) in a rubber network at temperatures much higher than T_g . Therefore, T_2 is sensitive to the density and motion constraints of the chemical and physical network junctions in rubber. At temperatures far above T_g ($T > T_g + 100 \text{ K}$), segmental motion of the polymer in crosslinked rubber networks (typical correlation time of fast local segmental motion $\tau_{\text{fast}} < 10^{-8} \text{ s}$) is inherently anisotropic. The reason is either a restriction by the permanent chemical crosslinks or a limitation of the reptation tube confined by temporary and trapped chain entanglements [50–53]. A small fraction q ($q \approx 10^{-4}$) of the dipolar interaction is retained at a slow correlation time τ_{slow} (typically $\tau_{\text{slow}} = 10^{-3} \text{ s}$) of the overall motion of the entire network chain. The relaxation of the magnetization of the free chain ends is estimated to decay purely exponentially. This assumption leads to the following fit equation for the total magnetization decay according to published literature [24, 28, 29, 53]:

$$I(\tau) = I_{\text{ma}} \exp \left\{ -\frac{\tau}{T_2} - qM_2\tau_{\text{slow}}^2 \left[\exp \left(-\frac{\tau}{\tau_{\text{slow}}} \right) + \frac{\tau}{\tau_{\text{slow}}} - 1 \right] \right\} + I_{\text{ce}} \exp \left(-\frac{\tau}{T_2} \right), \quad (3)$$

where $I(\tau)$ is the magnetization intensity, T_2 is the characteristic transverse relaxation time, and I_{ma} and I_{ce} are the fractions of the network chains and free dangling chain ends, respectively. A Weibull-type exponential decay function can be used to simplify the anisotropic movement [19, 54, 55]. Then, the decay of magnetization can be expressed in a simplified way:

$$I(\tau) = I_{\text{ma}} \exp \left[-\left(\frac{\tau}{T_{2,\text{ma}}^*} \right)^\beta \right] + I_{\text{ce}} \exp \left(-\frac{\tau}{T_{2,\text{ce}}^*} \right) + y_0, \quad (4)$$

with a factor $\beta = 0.5 - 2$. The introduced subscripts “ma” and “ce” indicate the fast magnetization decay of the matrix polymer motion and the slow, chain end magnetization decay, reflecting the mobile polymer motion, respectively. The fractions I_{ma} and I_{ce} are the corresponding fractions of protons, which describe the fast and the slow relaxation, respectively.

Figure 2 shows the time evolution of the normalized magnetization during the CPMG pulse sequence during the vulcanization of (a) the NR_{ma} compound and (b) the SBR_{ma} compound. The relaxation behavior of the rubber magnetization was described by Equation (4). The parameter β was determined to be around 1.4 and 1.0 for the investigated NR and SBR compounds, respectively, while $T_{2,\text{ce}}^{*-1}$ was kept unchangeable for all fits to be 25 ms for all samples. These determined β and $T_{2,\text{ce}}^{*-1}$ parameters were fixed for the further fitting procedure to reduce the total number of free fit parameters.

The GR loaded compounds show a combined signal of the GR particles and the rubber matrix. Due to this a second, fast relaxing term is used (subscript “GR”) to describe the magnetization decay of the GR particles. The resulting equation can be found in Equation (5).

$$I(\tau) = I_{\text{ma}} \exp \left[-\left(\frac{\tau}{T_{2,\text{ma}}^*} \right)^{\beta_{\text{ma}}} \right] + I_{\text{GR}} \exp \left[-\left(\frac{\tau}{T_{2,\text{GR}}^*} \right)^{\beta_{\text{GR}}} \right] + I_{\text{ce}} \exp \left(-\frac{\tau}{T_{2,\text{ce}}^*} \right) + y_0, \quad (5)$$

with the factors β_{ma} and $\beta_{\text{ma}} = 0.5 - 2$.

However, observations indicate that distinguishing between the signals of the GR particles and the surrounding rubber matrix

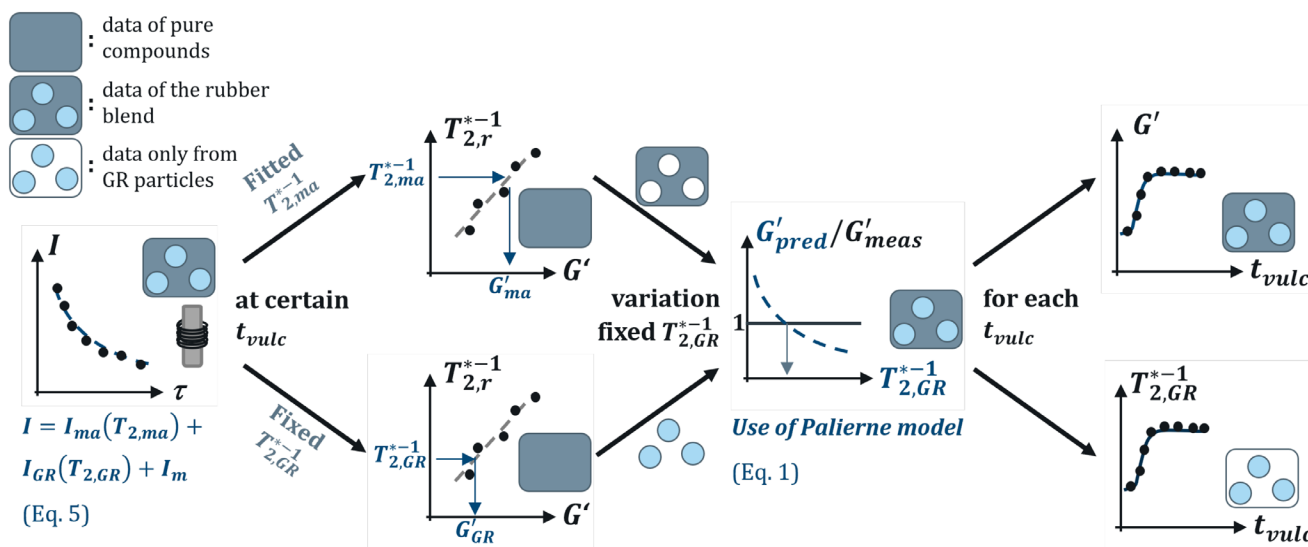


FIGURE 3 | Procedure used to calculate the G' prediction for the GR loaded compounds using the results from the Rheo-NMR of the pure compounds. $T_{2,GR}^{*-1}$ and $T_{2,ma}^{*-1}$ are used to determine the respective G' . The Palierne model is calculated using the different resulting G^* . To calculate G^* , G'' is interpolated using G' of the pure compounds. [Color figure can be viewed at [wileyonlinelibrary.com](https://onlinelibrary.wiley.com/doi/10.1002/app.71322)]

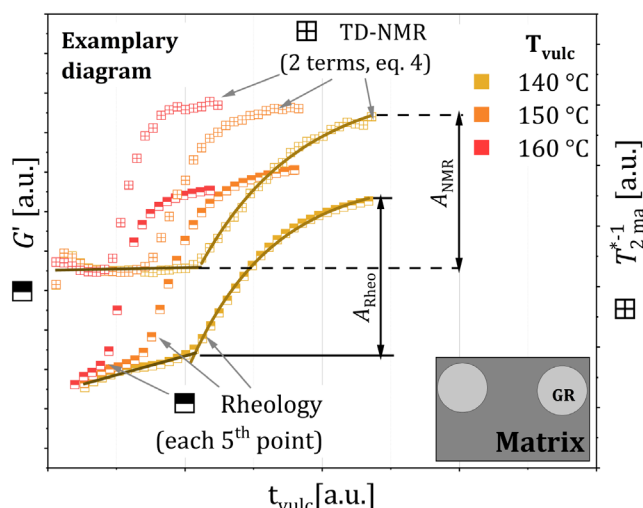


FIGURE 4 | Exemplary diagram for the vulcanization measured using the Rheo-NMR, showing how to read the diagram. The different colors indicate the respective vulcanization temperature. The different filling indicates by measurement method. The schematic picture at bottom right shows, the respective compound. Pure compounds are shown without circles, GR loaded compounds shown with circles. The amplitudes of vulcanization A_{Rheo} and A_{NMR} were determined by using the difference between the last point and the point at the end of incubation time. Incubation time was determined as the crossover of the linear fit at the first part and the monoexponential fit in the second part. [Color figure can be viewed at [wileyonlinelibrary.com](https://onlinelibrary.wiley.com/doi/10.1002/app.71322)]

remains challenging only using TD-NMR. This differentiation can be realized by combining the TD-NMR data to the rheology data using a constitutive model and then comparing this with the measured rheological results. The procedure for achieving this is described below. $T_{2,ce}^{*-1}$ was kept fixed at 0.04 ms^{-1} for all fitting procedures.

2.4.2 | Calculation Procedure for G' Using the Palierne Model

The Palierne model uses the G^* of both the rubber matrix and of the GR particles, G_{ma}^* and G_{GR}^* , respectively, to calculate G^* of the blend. To extract G' from the Rheo-NMR data a four steps procedure needs to be applied. The graphical overview of this procedure is shown in Figure 3.

The first step is to determine $T_{2,ma}^{*-1}$ by fitting Equation (5) to the TD-NMR data, while keeping $T_{2,GR}^{*-1}$ fixed at a certain value. In the second step, these two values are then used to interpolate to G'_{ma} and G'_{GR} , respectively, by using the T_{2}^{*-1} vs. G' -correlation of the pure compounds. In the third step, G'_{ma} and G'_{GR} are used to interpolate for the respective G'' . These values are used to calculate the G' of the blend by applying the Palierne model (Equation 1). In the last step, this procedure is repeated iteratively until the highest agreement of the predication by the Palierne model and measured G' is received ($G'_{pred}/G'_{meas} \approx 1$). A direct fit of both parameters is not applicable, because the fit procedure is not robust enough. Therefore, this procedure helps to validate the fit results of the individual $T_{2,ma}^{*-1}$ and $T_{2,GR}^{*-1}$ by applying their rheological prediction to the measured. Without the simultaneous measurement of Rheology and TD-NMR this would not be possible.

3 | Results and Discussion

3.1 | Vulcanization Kinetics

The vulcanization related properties ($T_{2,ma}^{*-1}(t_{vulc})$ and $G'(t_{vulc})$) can be measured simultaneously by the unique hyphenated Rheo-NMR setup. Figure 4 shows an example of such a measurement at three different T_{vulc} . A detailed explanation can be found in the caption of that figure.

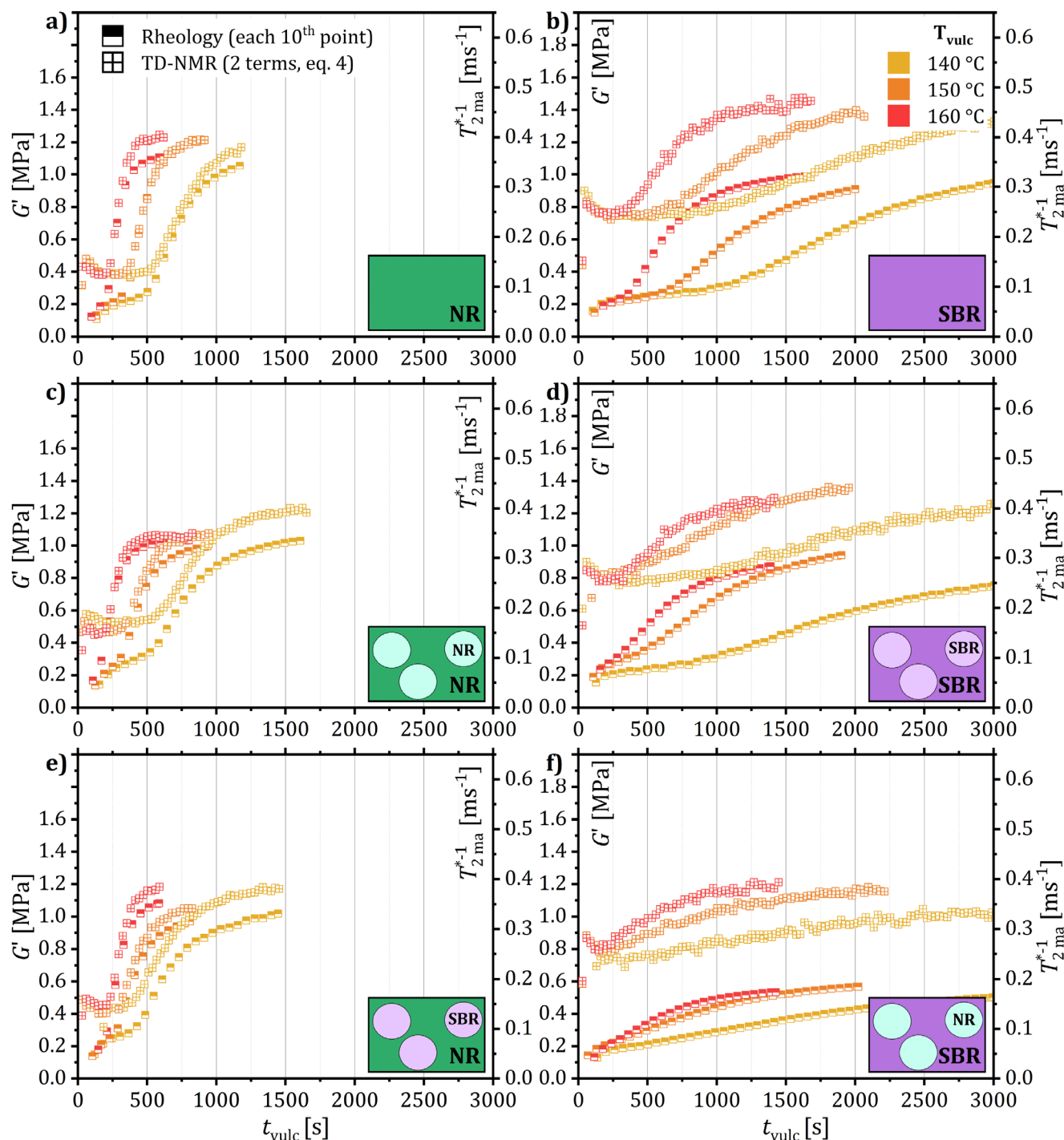


FIGURE 5 | The G' (■) and $T_{2,ma}^{*-1}$ (□) from the simultaneously measured rheology and TD-NMR during vulcanization of the pure and GR loaded (30 phr) rubber compounds at various vulcanization temperatures. The graphs show the vulcanization of the pure rubber compounds in (a) and (b), the rubber compounds with GR particles based on the same polymer as the rubber matrix in (c) and (d), and the rubber compounds with GR particles based on the contrary polymer in (e) and (f). The various Amplitudes A due to vulcanization are used in Table 3 exemplarily shown in (a) and (c) to quantify the impact of GR loading on the final CLD. [Color figure can be viewed at [wileyonlinelibrary.com](https://onlinelibrary.wiley.com)]

The results of these measurements are shown in Figure 5 for both materials of the pure rubber matrix in (a, b) and the GR loaded rubber compounds studied in (c–f).

The vulcanization can be quantified using the resulting amplitudes A_{Rheo} and A_{NMR} as shown in Figure 5 for the rheology and TD-NMR data, respectively. These amplitudes are used

to analyze the impact of GR loading on the CLD, since the amplitude A correlates with CLD. For better comparison, the amplitude of the GR loaded compound (A_{GR}) is normalized to the amplitude of the pure compound (A_{pure}) of the respective matrix polymer. The amplitude is also determined during vulcanization using the CCR. All results are shown in Table 3.

The rheological data determined by Rheo-NMR and by the CCR at all measured T_{vulc} exhibit agreement in the range of the standard deviation for all samples, validating the Rheo-NMR measurements. All GR loaded compounds exhibit a decrease in the amplitude compared to the pure rubber matrix compound (indicated by a value < 1). This decrease measured with rheology (Rheology in Rheo-NMR and CCR) and TD-NMR show the same level for most samples. In contrast, the $SBR_{ma} + NR_{GR}$ shows higher deviation between rheology (51% decrease) and TD-NMR (32% decrease). It should also be pointed out that the effect is similar at all T_{vulc} indicated by the low standard deviation.

The explanation for this difference may lie in the different effects detected by rheology and TD-NMR (Figure 1). Although rheology is influenced by both a decrease in the final CLD as a result of sulfur diffusion and a change due to the emulsion-like blending of the GR particles in the rubber matrix, TD-NMR only measures the decrease in the final CLD. We can assume that A_{GR} of rheology and TD-NMR show the same reduction due to

TABLE 3 | The ratio of the respective determined amplitude during vulcanization of the GR loaded compound (A_{GR}) to the amplitude of the pure compound (A_{pure}) at all T_{vulc} .

Rubber compound	$A_{GR} / A_{pure} [-]$			
	via rheology (by CCR)	via rheology		via TD-NMR (by Rheo-NMR)
		(by Rheo-NMR)	(by Rheo-NMR)	
$NR_{ma} + NR_{GR}$	0.80 ± 0.04	0.73 ± 0.06	0.83 ± 0.07	
$NR_{ma} + SBR_{GR}$	0.87 ± 0.04	0.93 ± 0.04	0.95 ± 0.10	
$SBR_{ma} + SBR_{GR}$	0.83 ± 0.03	0.86 ± 0.08	0.88 ± 0.03	
$SBR_{ma} + NR_{GR}$	0.50 ± 0.03	0.49 ± 0.03	0.68 ± 0.04	

Note: This indicates the drop of the respective property due to the GR loading. Two samples were measured at each T_{vulc} . Therefore, the values shown represent the mean and standard deviation calculated from six measurements.

the reduced CLD resulting from sulfur diffusion, if the type of crosslinks arising remain the same as in the pure compounds [19]. Therefore, there is an additional reduction of up to 29%, which is not only explained by sulfur diffusion. The agreement between the rheology obtained from Rheo-NMR and CCR indicates that the two methods can be reliably compared.

Such a shown reduction in CLD, represented by A_{GR} / A_{pure} , typically leads to lower hardness, tensile strength, and elasticity [3], emphasizing the practical importance of this effect. The Palierne model is used to assess the effect of the emulsion-like blend of GR particles in the rubber matrix on the rheological properties.

3.2 | Molecular-Macroscopic Correlation by Rheo-NMR

The simultaneous measurement of rheology data and TD-NMR data enables a direct correlation of macroscopic-molecular properties. To obtain this correlation, $G'(t_{vulc})$ is interpolated to match the corresponding t_{vulc} measured by TD-NMR. Figure 6 shows the results for the pure rubber compounds studied.

To assess the influence of the GR particles on the rheological properties, the theoretical prediction of G^* is calculated using these molecular-macroscopic correlations and the Palierne model according to Figure 3. The comparison of the prediction and the measured data is depicted in Figure 7.

The prediction made by the Palierne model describes the data of all compounds with a deviation of up to 5%. Only the compounds $NR_{ma} + NR_{GR}$ and $SBR_{ma} + NR_{GR}$ at $T_{vulc} = 140^\circ\text{C}$ show higher deviations of up to 15%. This leads to the conclusion that the Palierne model can be used to describe GR loaded compounds with the given uncertainties.

Nevertheless, the difference in the predictability for NR_{GR} compared to SBR_{GR} at $T_{vulc} = 140^\circ\text{C}$ shows a still unknown effect. Since this effect is independent of the used matrix and only

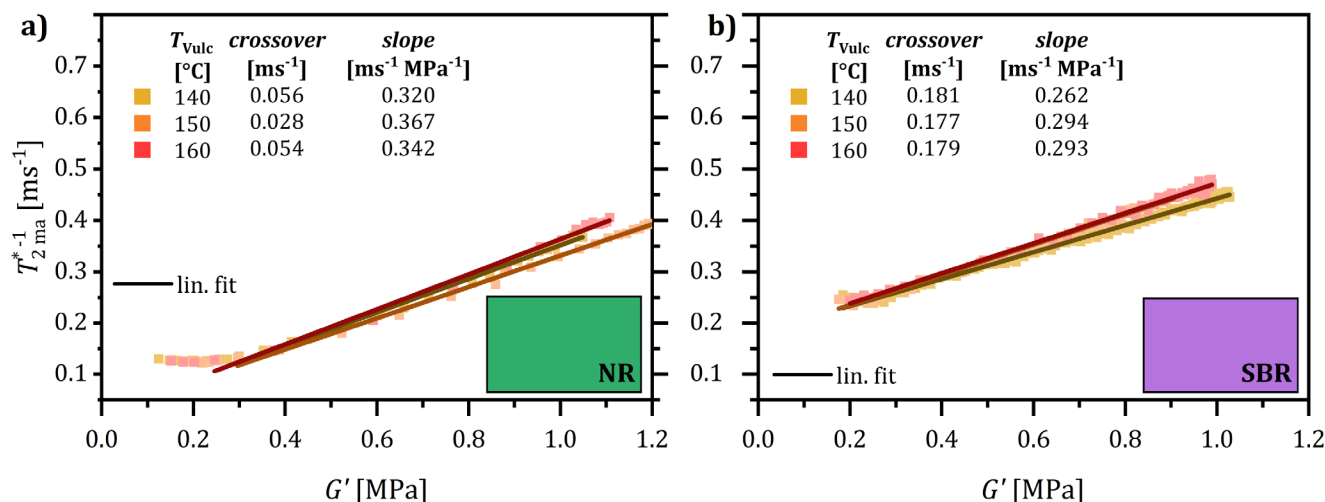


FIGURE 6 | Direct correlation of the molecular influenced $T_{2,ma}^{*-1}$ versus the macroscopic property G' , which indicates the relation of segmental mobility to macroscopic behavior. The correlation is shown for the pure rubber compounds without GR. (a) The NR_{ma} compound and (b) the SBR_{ma} compound. [Color figure can be viewed at [wileyonlinelibrary.com](https://onlinelibrary.wiley.com/doi/10.1002/app.71322)]

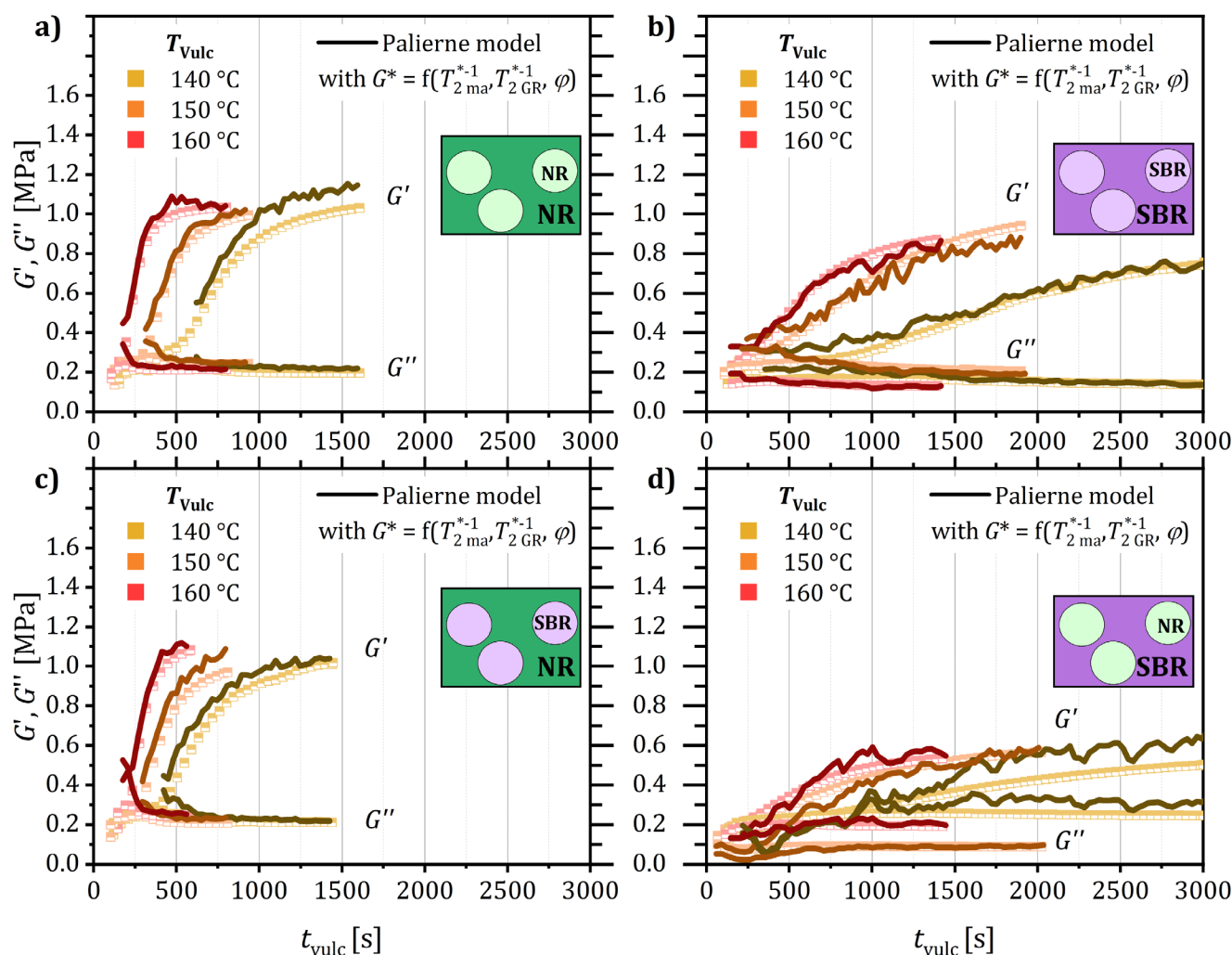


FIGURE 7 | The measured macroscopic property G' and G'' and the respective prediction made using the Palierne model. The results are shown for the rubber compounds with GR particles based on the same polymer as the rubber matrix in (a, b), and the rubber compounds with GR particles based on the contrary polymer in (c, d). [Color figure can be viewed at [wileyonlinelibrary.com](https://onlinelibrary.wiley.com)]

at a certain T_{vulc} a GR related property should be the reason. According to the Palierne model, differences in interfacial interactions should not significantly influence the data at the observed order of magnitude [15]. A difference in the resulting cross-link structure (more polysulfidic crosslinks) at the given conditions for NR_{GR} may explain this deviation by changing the $G'-T_2^{*-1}$ -correlation. This effect is not captured in the used procedure and is well described by Nie et al. [19].

The applied procedure also gives information about the further vulcanization of the GR. This is shown in Figure 8 for the compounds studied.

The results show that the NR_{GR} behaves differently compared to the SBR_{GR} . The NR_{GR} shows an increase in $T_{2,GR}^{*-1}$ during vulcanization indicating a further increase in CLD. The final increase is approximately 87.5% within the NR matrix and approximately 100% within the SBR matrix compared to the final $T_{2,ma}^{*-1}$ of the NR_{ma} compound. The SBR_{GR} does not show a clear change in $T_{2,GR}^{*-1}$ during vulcanization itself, indicating that there is no further vulcanization. Additionally, $T_{2,GR}^{*-1}$ of SBR_{GR} is lower than the final $T_{2,ma}^{*-1}$ of the SBR_{ma} compound by 12.5%.

The hypothesis is that NR_{GR} increases sulfur diffusion from matrix to the GR particles. The explanation might be due to a higher vulcanization rate of NR compared to SBR as can be seen in Figure 5, which increases the chemical potential of free sulfur during the vulcanization and promotes diffusion. Additionally, the NR compound shows a higher coefficient of diffusion according to ref. [56]. This explanation agrees with the results described in the literature [35, 56]. For the SBR_{GR} we assume that the cryogenic grinding process damages the network of SBR_{GR} , what reduces the CLD of this network. This can be explained by higher T_g of the used SBR compared to the used NR (see Table 1). The higher T_g broadens the brittle regime of that material and increases therefore the mechanochemical impact of the cryogenic grinding on the polymer network.

4 | Conclusion and Outlook

This article investigated the effect of GR loading of rubber compounds. The unique hyphenated Rheo-NMR setup was used to quantify the effect on the rheological behavior as an emulsion-like blend as well as on the further vulcanization of the GR particle due to sulfur diffusion.

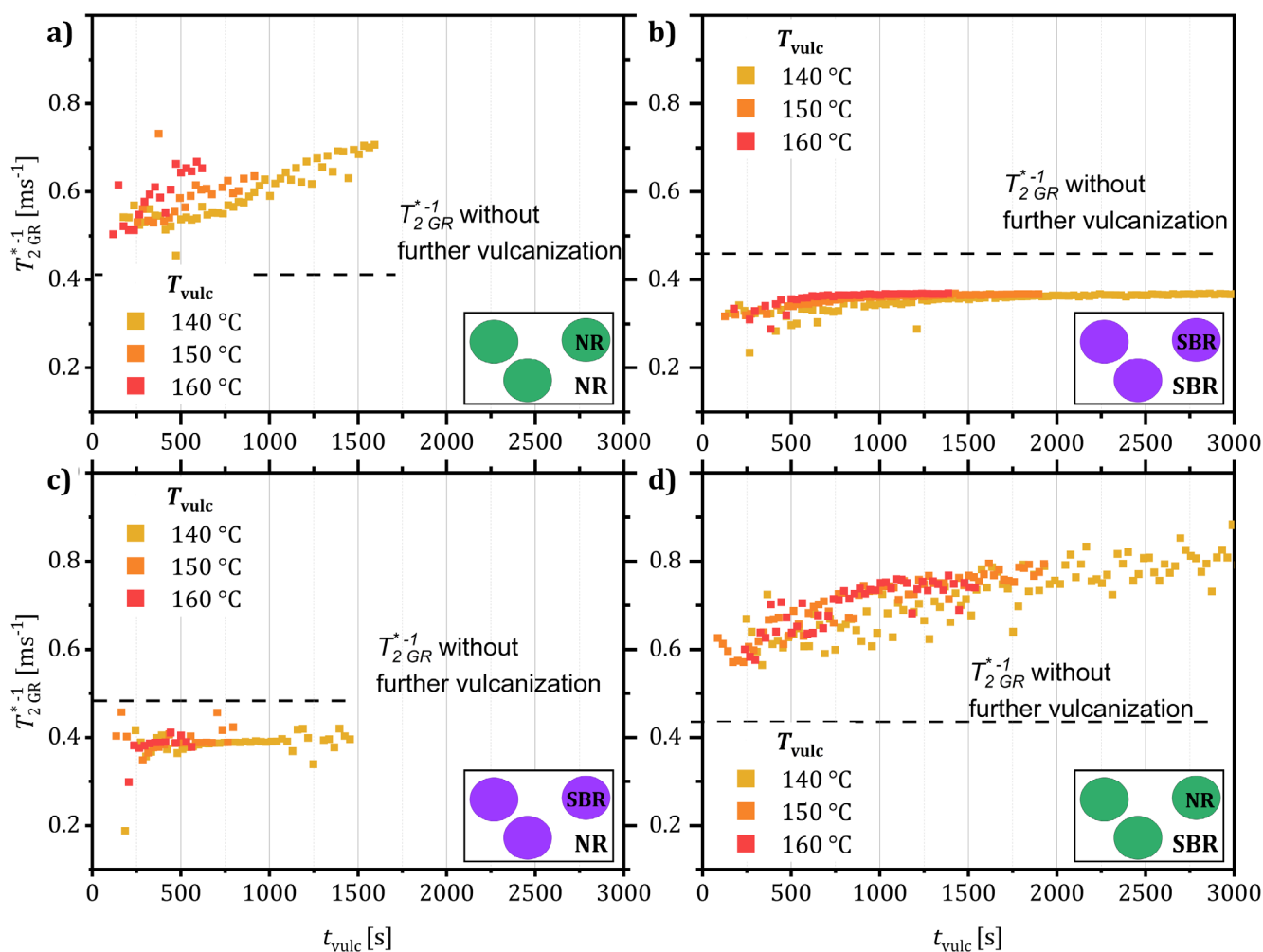


FIGURE 8 | Resulting $T_{2,GR}^{*-1}$ of the GR particles achieved by comparing the prediction made with the Palierne model with the measured data. The results are shown for the rubber compounds with GR particles based on the same polymer as the rubber matrix in (a, b), and the rubber compounds with GR particles based on the contrary polymer in (c, d). NR_{GR} shows increase in $T_{2,GR}^{*-1}$ indicating a further vulcanization reaction, while SBR_{GR} shows no change during vulcanization. [Color figure can be viewed at [wileyonlinelibrary.com](https://onlinelibrary.wiley.com/doi/10.1002/app.71322)]

GR loading was found to lead to a decrease in final parameters, namely $T_{2,ma}^{*-1}$ and G' , consistent with previously published literature [5, 9–11]. This effect is explained in the literature by the diffusion of free S_8 sulfur from the rubber matrix into the GR particle. The effect of the emulsion-like blend on the rheological properties of GR loaded compounds has not been covered in literature so far.

The simultaneous measurement of both rheological and time-domain NMR (TD-NMR) data by the Rheo-NMR setup allows to differentiate between the effects of the emulsion-like blending and the change in CLD due to sulfur diffusion. The linear correlation between the TD-NMR data and the rheological properties of the pure compounds received by plotting $T_{2,ma}^{*-1}$ versus G' and the Palierne model are used. By vary $T_{2,GR}^{*-1}$, G' can be predicted for the GR loaded compounds. The Palierne model describes the vulcanization of the GR loaded compounds with a deviation of up to 15%. The resulting $T_{2,GR}^{*-1}$ shows an increase during the vulcanization depending on the polymer in the GR. The NR_{GR} shows an increase of up to 100% independent of the matrix compound, while the SBR_{GR} shows no further increase. This increase may be correlated with an increase in CLD.

This received information is essential to understand and improve the performance of GR loaded compounds. This emphasizes the importance of the use of the Rheo-NMR setup for rubber recycling.

This article deserves as a framework for further studies of GR loading in rubber compounds. Further research should explore different rubbers and variations of crosslinking systems, including alternative accelerators. Additionally, the impact of the particle size of the GR used and concentration should be investigated more in detail. It is also important to detect the maximum concentration of GR, where the Palierne model is applicable. A deeper understanding of all of these effects can help to optimize GR loaded compounds. In addition, a hyphenated Rheo-IR setup [57] can be utilized to validate the results presented in this study and obtain a clearer understanding of the results obtained.

Author Contributions

Tim Schüle: writing – original draft, investigation, conceptualization, methodology, validation, visualization, writing – review and editing, software, formal analysis, project administration, data curation,

resources. **Stefan A. Frosch**: writing – review and editing, investigation, methodology. **Manfred Wilhelm**: funding acquisition, writing – review and editing, supervision, resources, project administration. **Volker Herrmann**: supervision, resources, writing – review and editing, funding acquisition, validation, project administration. **Johannes Krückel**: funding acquisition, writing – review and editing, supervision, resources, project administration. **Sarah L. Palloks**: writing – review and editing, software, methodology, investigation.

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Conflicts of Interest

The authors declare no conflicts of interest.

Data Availability Statement

The data that support the findings of this study are available from the corresponding author upon reasonable request.

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