

# 3D REGULARIZED SPEED-MAP RECONSTRUCTION IN ULTRASOUND TRANSMISSION TOMOGRAPHY



<sup>1</sup>Brno University of Technology, Czech Republic

Radovan Jiřík<sup>1</sup>, Igor Peterlík<sup>1</sup>, Jiří Jan<sup>1</sup>, Nicole Ruiter<sup>2</sup>, Michael Zapf<sup>2</sup>

<sup>2</sup>Forschungszentrum Karlsruhe, Germany

## Aim

- for breast cancer diagnostics
- sound-speed closely related to the pathological tissue state
- stand-alone imaging application or for correction of reflectivity imaging algorithm

## Challenge

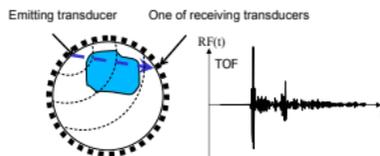
- Classical approach
  - 2D ring of transducers
  - large (high) transducers – high SNR
  - dense distribution of transducers
  - only 2D information
  - filtered backprojection (similarly to CT)
- Presented approach
  - 3D distribution of transducers
  - small transducers – low SNR
  - sparse distribution of transducers
  - complete 3D information at once
  - regularized algebraic reconstruction

## Data acquisition

- tank filled with water
- transducers on surface
- each time one transducer in the emitter mode, all other transducers record the received RF signals
- all combinations of sending and receiving elements
- unfocused wave
- 6 motor positions



## Algebraic sound-speed reconstruction



$$\text{Contributions of voxels on the path: } TOF = \sum_i T_i \quad T_i = d_i \cdot \frac{1}{c_i} \quad TOF = \sum_i d_i \cdot s_i$$

TOF time-of-flight – time span between emitting and receiving of the first pulse  
 $T_i$  time-of-flight through  $i$ -th voxel  
 $d_i$  path length through  $i$ -th voxel  
 $c_i$  sound-speed in  $i$ -th voxel  
 $s_i$  time-of-flight per unit distance in  $i$ -th voxel (unknowns)

$$\begin{aligned} \text{Path 1: } & TOF_1 = \sum_{j=1}^N d_{1,j} s_j \\ \text{Path 2: } & TOF_2 = \sum_{j=1}^N d_{2,j} s_j \\ & \dots \\ \text{Path K: } & TOF_K = \sum_{j=1}^N d_{K,j} s_j \end{aligned} \quad \begin{bmatrix} d_{1,j} \\ d_{2,j} \\ \dots \\ d_{K,j} \end{bmatrix} \cdot \begin{bmatrix} s_j \end{bmatrix} = \begin{bmatrix} TOF_1 \\ \dots \\ TOF_K \end{bmatrix}$$

... overdetermined system of linear equations:  $Rf = p$

## Regularization

- Why:
- errors in transmission pulse detection, hence also in TOF (wave front aberration, noise)
  - some equations can be left out as outliers (wave front aberration, noise) => smaller degree of equation-set overdetermination
  - sparse transducer distribution (technical limitations)

Solution formulation:

- incorporation of the spatial context in the reconstruction
- edge preserving regularization:

$$f = \arg \min_f \left( J_1(f) + \lambda^2 J_2(f) \right)$$

$$J_1(f) = \frac{1}{2} \|p - Rf\|^2$$

$$J_2(f) = \sum_k \phi(|D_x f|_k / \delta) + \sum_k \phi(|D_y f|_k / \delta) + \sum_k \phi(|D_z f|_k / \delta)$$

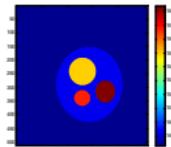
$J_1(f)$  least-squares term  
 $J_2(f)$  regularization term  
 $D_x f, D_y f, D_z f$  differences between neighboring voxels  
 $\delta, \lambda$  regularization parameters  
 $\phi$  potential (penalization) function:

Possible potential functions:

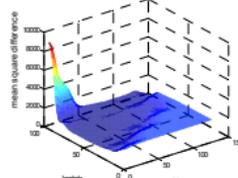


## Results on synthetic data

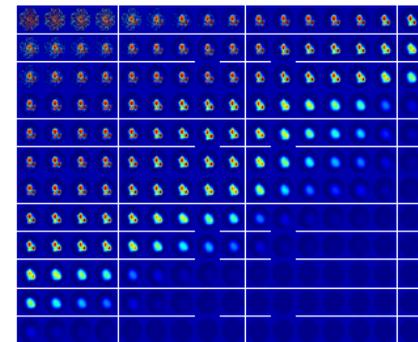
Synthetic phantom:



Estimation of regularization parameters:

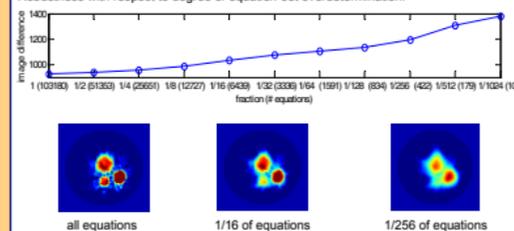


Corresponding reconstructed images:

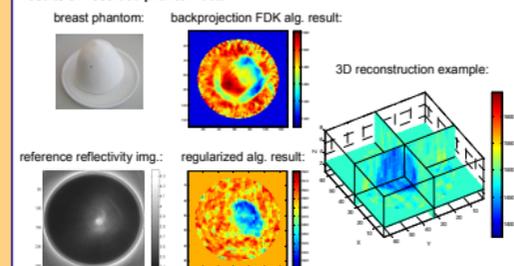


## Results on synthetic data

Robustness with respect to degree of equation-set overdetermination:



## Results on recorded phantom data



## Conclusions

- algebraic reconstruction for sparse distribution of transducers possible with regularization
- regularization parameters – compromise between edge preserving and spatial consistency
- optimal regularization parameters found for simulated data (with SNR same as in reality – 11dB)
- optimal regularization parameters – valley, not separate point
- image reconstruction still reasonable with a low fraction of the complete equation set => wide space for selection of only "good" equations (RF signals)
- phantom measurements gave clear breast delineation
- regularized reconstruction provided better breast delineation than FDk filtered backprojection
- need for better evaluation
  - need for measurements on sound-speed phantom with known ground-truth sound-speed values
  - need for more realistic simulation used for synthetic data generation
- part of volume processed so far due to memory limitations – need for distributed equation solver

## Acknowledgement

We are grateful for support from

- Czech Ministry of Education, Youth and Sports (Research Center DAR, proj. no. 1M6798555601)
- Joint programs of the German Academic Exchange Service and Czech Academy of Science,
- MetaCentrum for offering the computational resources