

# Limitations of two energy balance closure parameterizations

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## Motivation: the energy balance closure problem

The **eddy-covariance technique** tends to underestimate the fluxes of sensible ( $Q_H$ ) and latent heat ( $Q_E$ ) by 10-30%. Consequently, the turbulent heat fluxes are not in balance with the net radiation ( $-Q_S^*$ ) and the ground heat flux ( $Q_G$ ), which is known as the **energy balance closure problem**. The energy balance ratio ( $R$ ),

$$R = \frac{Q_H + Q_E}{-Q_S^* - Q_G}$$

is usually smaller than 1.

Since the eddy-covariance method is widely used to determine fluxes of energy and trace gases on an ecosystem scale, a robust **parameterization of the missing turbulent energy** is necessary. Here, we tested two approaches that can be found in the literature: **Huang et al. (2008)** and **Panin and Bernhofer (2009)**.

## Data I: aircraft measurements (Canada)

Flight details (Fig. 1):

- BOREAS, 1994: 16 flights
- BERMS, 2002: 4 flights
- height: ~ 30 m a.g.l.
- length: ~ 110 km

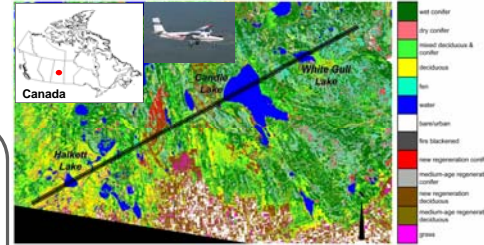
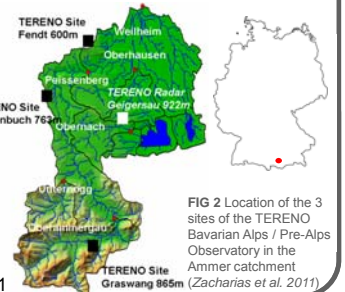
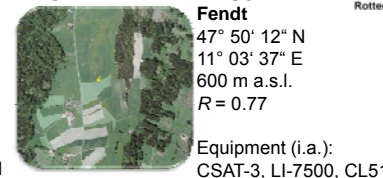
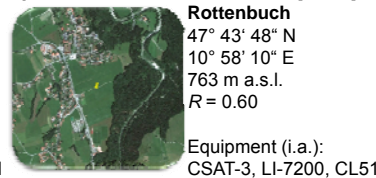
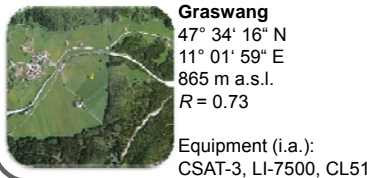


FIG 1 Location of the 20 flights conducted by the Twin Otter Research aircraft during BOREAS and BERMS and land use in the investigation area (Hall et al. 1997)

## Energy balance closure from airborne data:

1. Calculate cross-scalograms (wavelet transform) of  $w$  and  $T/w$  and  $q$
2. Determine flux contribution of scales  $< 2$  km
3.  $R = \frac{(Q_H + Q_E)_{scales < 2km}}{(Q_H + Q_E)_{all scales}}$

## Data II: tower measurements (TERENO, Bavarian Alps / pre-Alps Observatory)



## Parameterization by Huang et al. (2008)

Description:

- large-eddy simulation of the homogeneous convective boundary layer
- considers atmospheric conditions
- energy imbalance ( $I$ ) due to the presence of turbulent organized structures
- parameterization of the energy imbalance for every 30-min period

$$I = \frac{Q_H + Q_E}{-Q_S^* - Q_G} - 1$$

$$I \sim f_1\left(\frac{u_*}{w_*}\right) \times f_2\left(\frac{z}{z_i}\right)$$

$u_*$ : friction velocity,  $w_*$ : Deardorff velocity,  $z$ : measurement height;  $z_i$ : boundary-layer depth

Results:

- only daytime data were analyzed ( $-Q_S^* > 30 \text{ W m}^{-2}$ )
- dependence of energy imbalance on  $u_* / w_*$ : function  $f_1$  could not be confirmed; no correlation with  $u_* / w_*$  was found (Fig. 3)
- dependence of energy imbalance on  $z / z_i$ : also no correlation (data not shown)
- but: **weak dependence of imbalance on  $u_*$**  at 2 of 3 TERENO sites (Fig. 4)

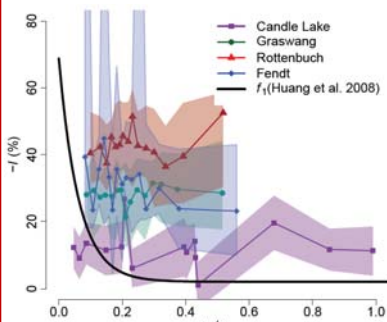


FIG 3 Energy imbalances ( $-I$ ) for 16 aircraft flights above Candle Lake during BOREAS and for the TERENO sites Graswang, Rottenbuch and Fendt vs. the ratio of friction velocity ( $u_*$ ) to Deardorff velocity ( $w_*$ ); shaded areas indicate interquartile ranges and, for Candle Lake, the random error of the airborne measurements (Eder et al. 2014, modified)

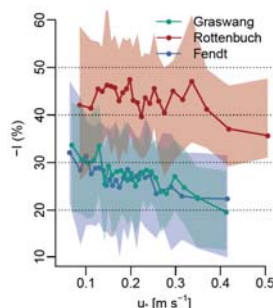


FIG 4 Energy imbalance ( $-I$ ) vs. friction velocity ( $u_*$ ) for Graswang, Rottenbuch and Fendt; shaded areas indicate interquartile ranges

Discussion / Conclusions:

- The parameterization is **not applicable** to our surface-layer data.
- neglects any influence of surface heterogeneities
- $w_*$  is not an appropriate scaling parameter for the surface layer
- the large-eddy simulation model used by Huang et al. (2008) has an insufficient grid resolution close to the surface

## Parameterization by Panin and Bernhofer (2008)

Description:

- empirical parameterization, based on eddy-covariance measurements
- considers properties of the landscape (surface roughness heterogeneities)
- energy imbalance due to secondary circulations generated by heterogeneities
- parameterization of the mean energy balance correction factor ( $k_f$ ) for a site

$$k_f = \frac{-Q_S^* - Q_G}{Q_H + Q_E}$$

$$k_f \sim \frac{z_{\text{eff}}}{L_{\text{eff}}}$$

$z_{\text{eff}}$ : effective surface roughness,  $L_{\text{eff}}$ : horizontal scale of the heterogeneities

Results:

- Determination of heterogeneity index ( $z_{\text{eff}}/L_{\text{eff}}$ ): surface roughness maps (Fig. 5),  $L_{\text{eff}}$ : Fourier transform along selected transects
- **$k_f$  factor of TERENO sites is larger** (i.e. energy balance closure is poorer) than expected (Fig. 6)
- the data from Candle Lake match well with the data of Panin and Bernhofer (2008)

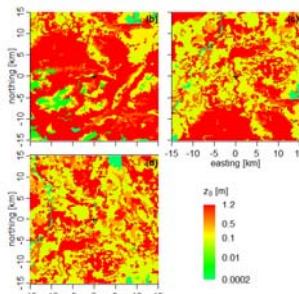


FIG 5 Surface roughness maps of (a) the Candle Lake area and the TERENO sites at (b) Graswang, (c) Rottenbuch and (d) Fendt; in (b)-(d), black crosses mark the approximate location of the EC systems (Eder et al. 2014)

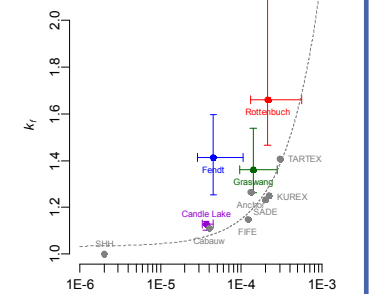


FIG 6 Energy balance correction factor ( $k_f$ ) for the Candle Lake area and the EC systems at Graswang, Rottenbuch and Fendt vs. heterogeneity index ( $z_{\text{eff}}/L_{\text{eff}}$ ); data from Panin and Bernhofer (2008) are displayed in grey (Eder et al. 2014)

Discussion / Conclusions:

- A **rough qualitative estimate** of the energy imbalance is possible.
- neglects any surface heterogeneity other than surface roughness, e.g. surface temperature, surface moisture, topography
- $L_{\text{eff}}$  is the crucial parameter, but there should be an 'optimum scale' of heterogeneities (e.g. 4-9 times  $z_i$ , cf. Patton et al. 2005)

## References

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## Acknowledgements

This work was conducted within the Helmholtz Young Investigator Group "Capturing all relevant scales of biosphere-atmosphere exchange – the entigmatic energy balance closure problem", which is funded by the Helmholtz-Association through the President's Initiative and Networking Fund, and by KIT.