

**Contributions of the direct numerical
simulation method to the validation
of statistical turbulence models for
natural convection**

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Introduction

- **Passive decay heat removal in metal and water cooled reactors**
 - experiments (scaled reactor models, water as model fluid)
 - engineering computer codes (e.g. FLUTAN)
- **Validation of statistical turbulence models for natural convection in liquid metals**
 - basic experiments in simple geometries
 - direct numerical simulation

Method of direct numerical simulation

- Conservation equations of mass, momentum and energy

$$\nabla \hat{\mathbf{u}} = 0$$

$$\partial \hat{\mathbf{u}} / \partial t + (\hat{\mathbf{u}} \nabla) \hat{\mathbf{u}} = -\nabla p + \frac{1}{\sqrt{Gr}} \nabla^2 \hat{\mathbf{u}} + \left(T_{ref} - T \right) \frac{\hat{\mathbf{g}}}{|\hat{\mathbf{g}}|}$$

$$\partial T / \partial t + (\hat{\mathbf{u}} \nabla) T = \frac{1}{Pr \sqrt{Gr}} \nabla^2 T$$

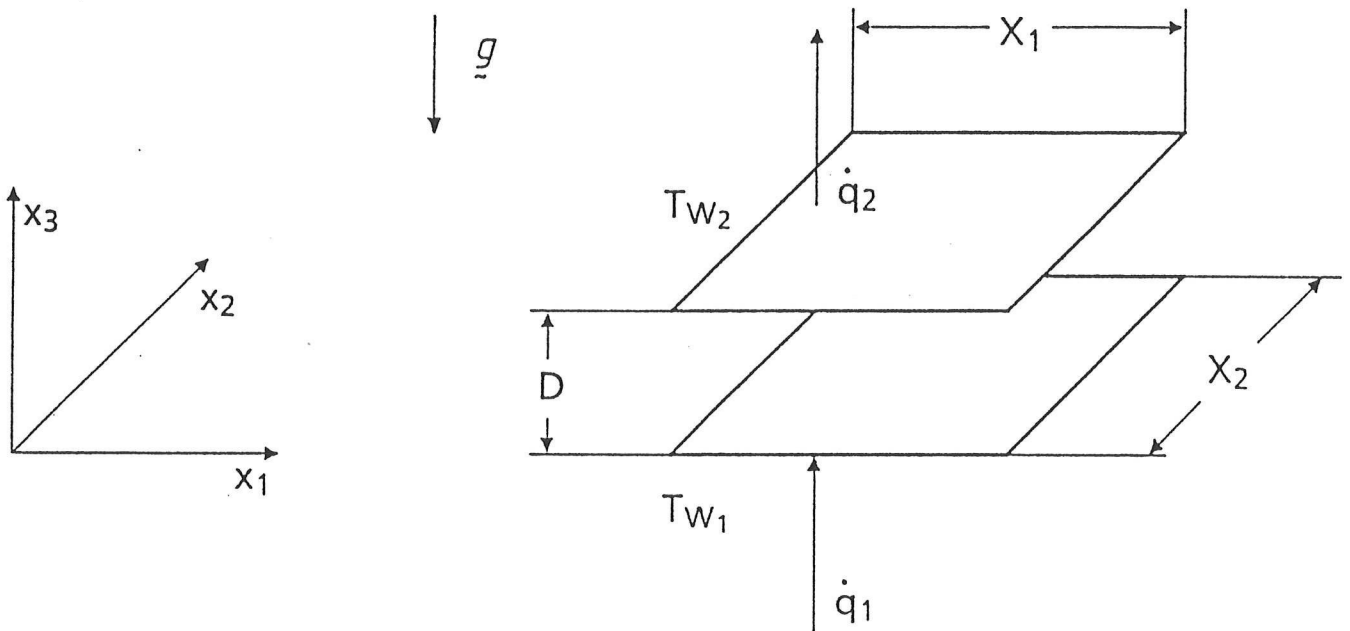
- 3d, time dependent
 - resolve all spatial scales of turbulence
- + no model assumptions, no parameters
- limited to small turbulence levels and simple geometries

Computer code TURBIT

- finite volume method
 - central finite differences
 - staggered grid
- time integration
 - momentum equation: explicit
 - energy equation: explicit or semi-implicit
 - Poisson equation for pressure
- geometry
 - plane channel
 - annulus

Rayleigh-Bénard convection

- geometry



- dimensionless numbers

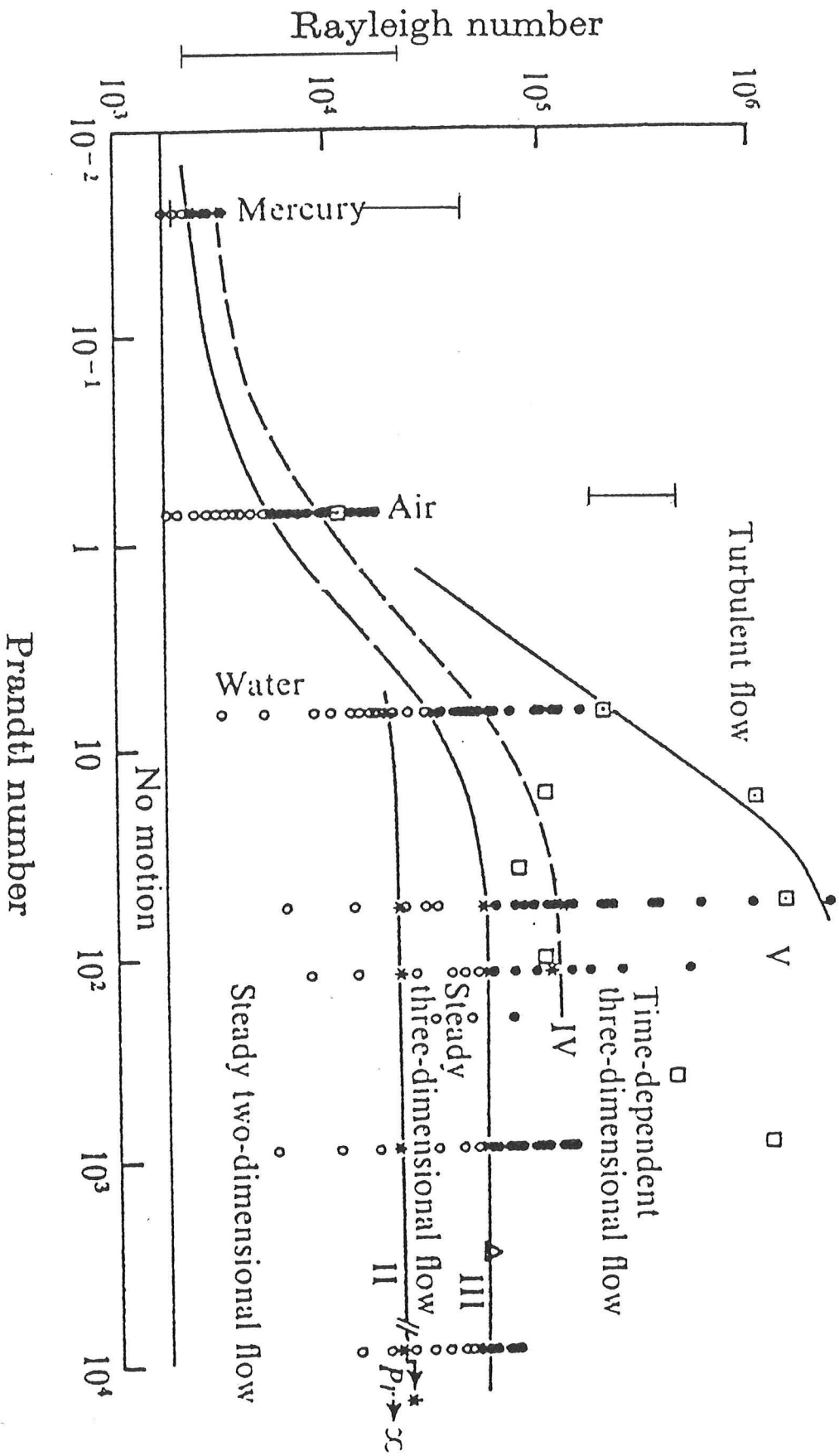
- Rayleigh number $Ra \sim \Delta T_w$
- Prandtl number $Pr = \nu/\kappa$

sodium: $Pr = 0.006$

mercury: $Pr = 0.024$

air: $Pr = 0.71$

Rayleigh-Bénard convection



Statistical Turbulence Models

- closure of $-\overline{u_i' u_j'}$, $-\overline{u_i' T'}$
 - solution of modelled transport equations for turbulent quantities
e.g.: k , ε , $\overline{T'^2}$, ε_T , $-\overline{u_i' u_j'}$, $-\overline{u_i' T'}$
- use DNS-data to
 - analyse exact transport equations for k , ε , ...
 - analyse model assumption for different terms

Transport equation for turbulent heat flux $\overline{u_3 T'}$

$$0 = - \frac{\partial}{\partial x_3} \left(\overline{u_3^2 T'} + \overline{p' T'} - \frac{1}{Pr \sqrt{Gr}} \overline{u_3 \frac{\partial T'}{\partial x_3}} - \frac{1}{\sqrt{Gr}} \overline{T' \frac{\partial u_3}{\partial x_3}} \right)$$

D_q

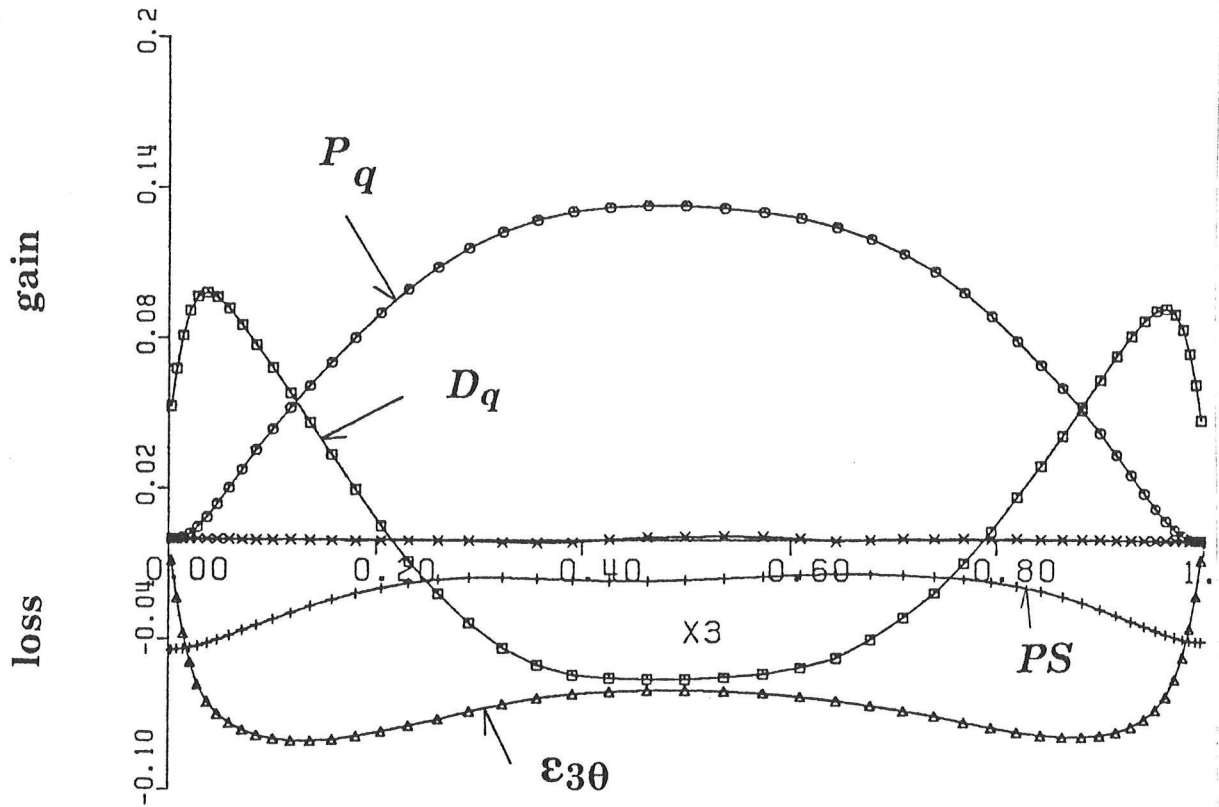
$$- \overline{u_3^2} \frac{\partial \overline{T}}{\partial x_3} + \overline{T'^2} + \overline{p' \frac{\partial T'}{\partial x_3}}$$

P_q PS

$$- \frac{1}{\sqrt{Gr}} \left(1 + \frac{1}{Pr} \right) \overline{\frac{\partial u_3}{\partial x_i} \cdot \frac{\partial T'}{\partial x_i}}$$

Budget of $\overline{u_3'T'}$

- Sodium, $Ra = 24\ 000$

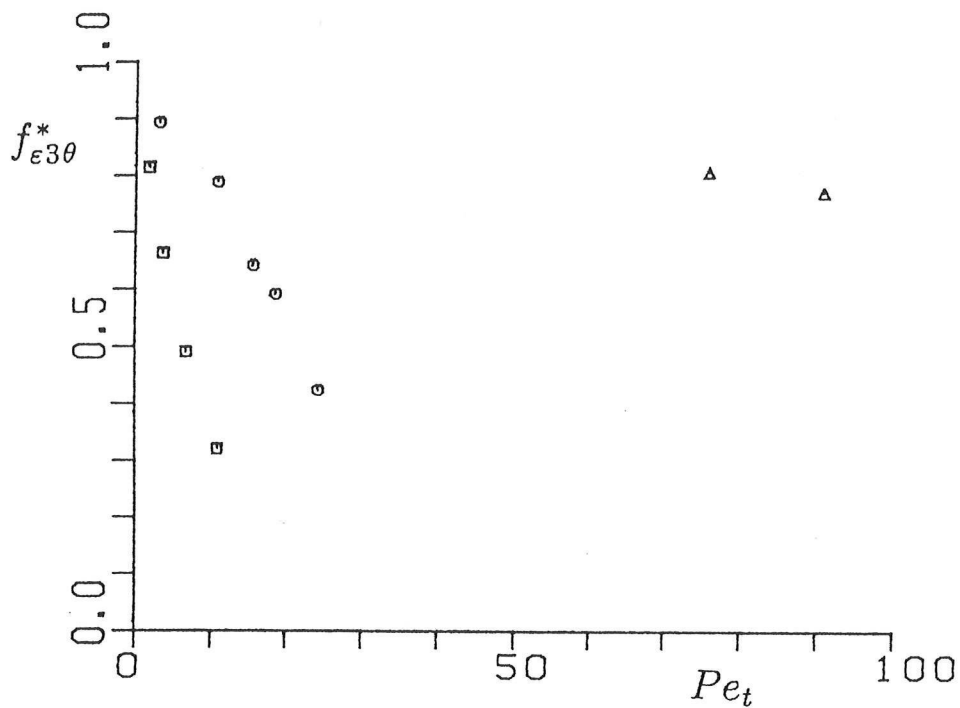


Modelling of $\varepsilon_{i\theta}$

- Shikazono & Kasagi (1993):

$$\varepsilon_{i\theta} = f_{\varepsilon_{i\theta}}^* \frac{1 + Pr}{2\sqrt{Pr} \sqrt{R}} \frac{\varepsilon}{k} \overline{u_i' T'}$$

- Analysis of $f_{\varepsilon_{3\theta}}^*$ by DNS-data



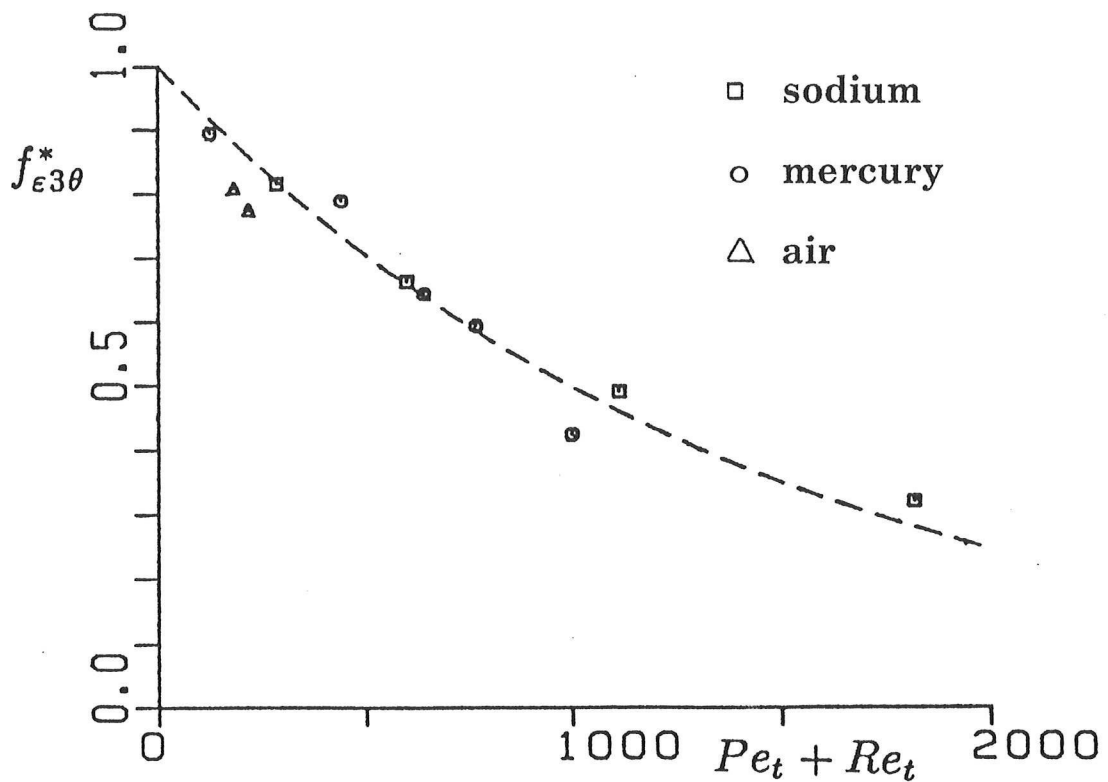
- sodium
- mercury
- △ air

Modelling of $\varepsilon_{i\theta}$

- Shikazono & Kasagi (1993):

$$\varepsilon_{i\theta} = f_{\varepsilon i\theta}^* \frac{1 + Pr}{2\sqrt{Pr} \sqrt{R}} \frac{\varepsilon}{k} \overline{u_i'^2 T}$$

- Analysis of $f_{\varepsilon 3\theta}^*$ by DNS-data



--- $f_{\varepsilon i\theta}^* = \exp(-C_{\varepsilon i\theta} (Re_t + Pe_t))$

$$C_{\varepsilon 3\theta} \approx 0.0007$$

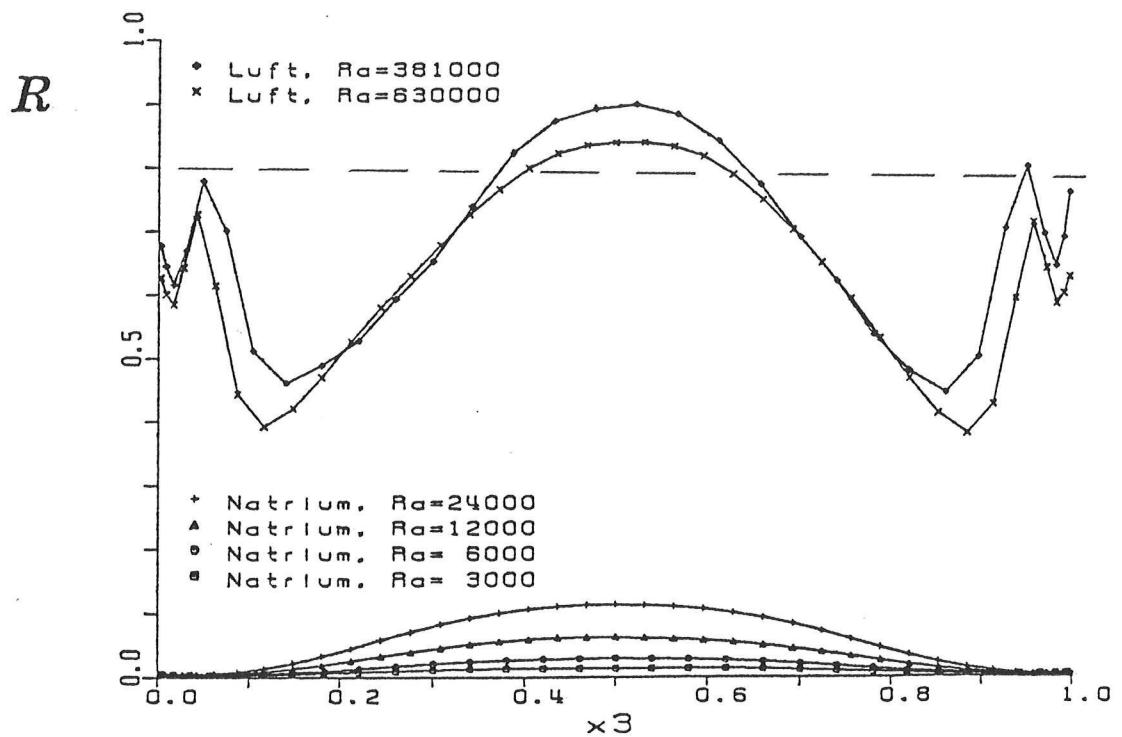
Closure of sink term ε_T

- Launder (1975)

$$\varepsilon_T = \frac{1}{R} \frac{\overline{T'^2}/2}{k} \varepsilon$$

$$R \approx 0.8$$

- evaluation of R



Conclusions

- **Direct numerical simulation**

- no assumptions about turbulence
- numerical experiment
- simple geometries
- small turbulence levels

here: Rayleigh-Bénard convection,
three fluids

- **Validation of statistical turbulence models**

- evaluation of all correlations
- analysis of budgets of turbulent quantities
- analysis of model assumptions
- calibration of coefficients and improvement of models