



Forschungszentrum Karlsruhe
in der Helmholtz-Gemeinschaft

Institut für Reaktorsicherheit

Problems of a 3D VOF research code for confined geometries to compute bubble rise in an extended domain

Martin Wörner

Forschungszentrum Karlsruhe, Institut für Reaktorsicherheit

*11th International Topical Meeting on Nuclear Reactor Thermal-Hydraulics
Open Forum: Interface tracking test cases
Avignon, France, October 2–6, 2005*



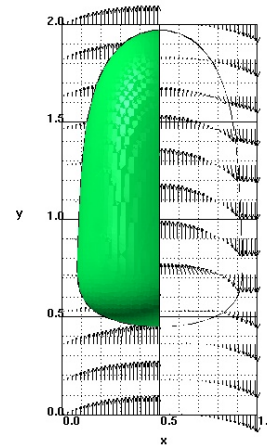
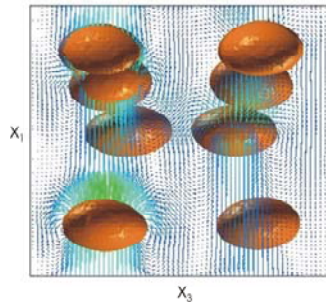
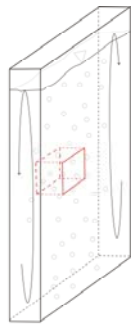
Overview

- Short description of in-house code
- Short description of test case 1
 - Spherical cap bubble in stagnant liquid
- Estimation of required grid size
 - Size of computational domain
 - Number of mesh cells
- Conclusions



In-house code TURBIT-VOF

- Designed to compute 3D bubble flow in confined rectangular geometries
 - Taylor-bubble in square mini-channels
 - Flat bubble column

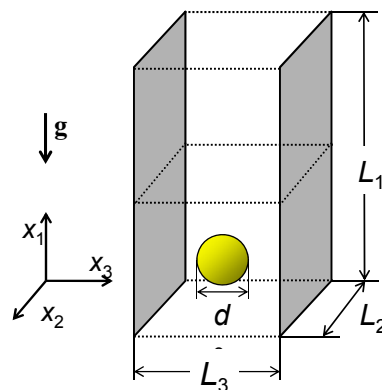


3



Features of TURBIT-VOF

- 3D PLIC-VOF method: interface is locally approximated by a plane
- Cartesian co-ordinate system
 - Rectangular 3D domain with two side walls (or four side walls)
 - *2D axi-symmetric coordinates are not implemented*
- Periodic b.c. in vertical and spanwise directions x_1 and x_2
- Grid spacing
 - Uniform in periodic directions
 - Optionally non-equidistant in wall-normal direction

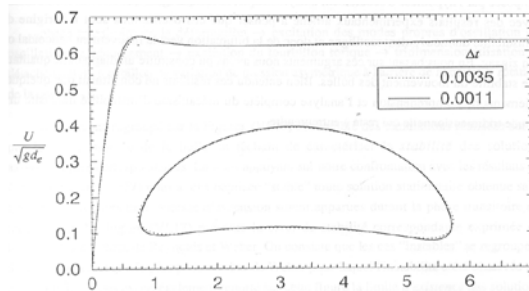


4



Test case 1: Rise of a spherical cap bubble in a stagnant liquid

- Compute the displacement of an initially spherical inclusion with the following non-dimensional properties $Mo = 0.056$, $Bo = 40$, $\rho_L/\rho_V = 100$ and $\mu_L/\mu_V = 100$.



- As an example, we suggest the following physical properties: $\rho_L = 1000 \text{ kg.m}^{-3}$, $\rho_V = 10 \text{ kg.m}^{-3}$, $\mu_L = 0.273556 \text{ Pa.s}^{-1}$, $\mu_V = 0.00273556 \text{ Pa.s}^{-1}$, $\sigma = 0.1 \text{ N.m}$, $g = 10 \text{ kg.s}^{-2}$, $d_e = 0.02 \text{ m}$.

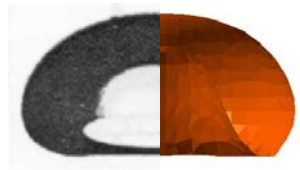
5



Ellipsoidal cap bubble $Mo=266$, $E\ddot{o}=243$

Experiment Bhaga & Weber

$(\Gamma_\rho \approx 0,0008; \Gamma_\mu \approx 10^{-5})$



TURBIT-VOF

$(\Gamma_\rho = 0,5; \Gamma_\mu = 1)$



6



Estimate of size of computational domain for test case 1

- Test case requirements for horizontal directions (minimum):
 $L_2 = L_3 = 10d_e$
- Estimation of vertical distance of bubble rise

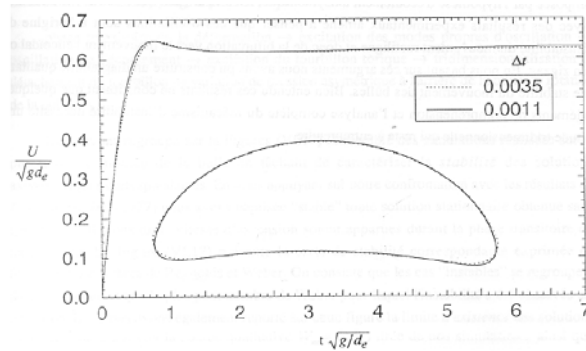
$$U \approx 0.6\sqrt{gd_e}$$

$$t \approx 7\sqrt{\frac{d_e}{g}}$$

$$\Rightarrow H = U \cdot t = 4.2d_e$$

$$L_1 > 2H = 8.4d_e$$

$$\Rightarrow L_1 = 10d_e$$



7



Estimate of number of mesh cells

- The adequate representation of surface tension force requires accurate computation of the interface curvature
- For this the bubble diameter must be resolved by a minimum number of mesh cells
 - Number of mesh cells per bubble diameter $n_B \geq 16$
- Estimation of total number of mesh cells:

$$N = (10d_e)^3 \cdot \left(\frac{n_B}{d_e}\right)^3 = 1000n_B^3$$

$$n_B = 16 \Rightarrow N \approx 4,000,000$$

$$n_B = 20 \Rightarrow N \approx 8,000,000$$

- Largest grid used up to now: $N \approx 2,000,000$ cells

8



Conclusions

- For a purely 3D Cartesian PLIC-VOF code based on a structured grid test case 1 requires a large number of mesh cells
 - Most cells are spent in regions far away of the bubble where there is almost no liquid flow at all
- Test case 1 is well suited for codes with
 - 2D axi-symmetric coordinates
 - 3D codes which use an unstructured grid