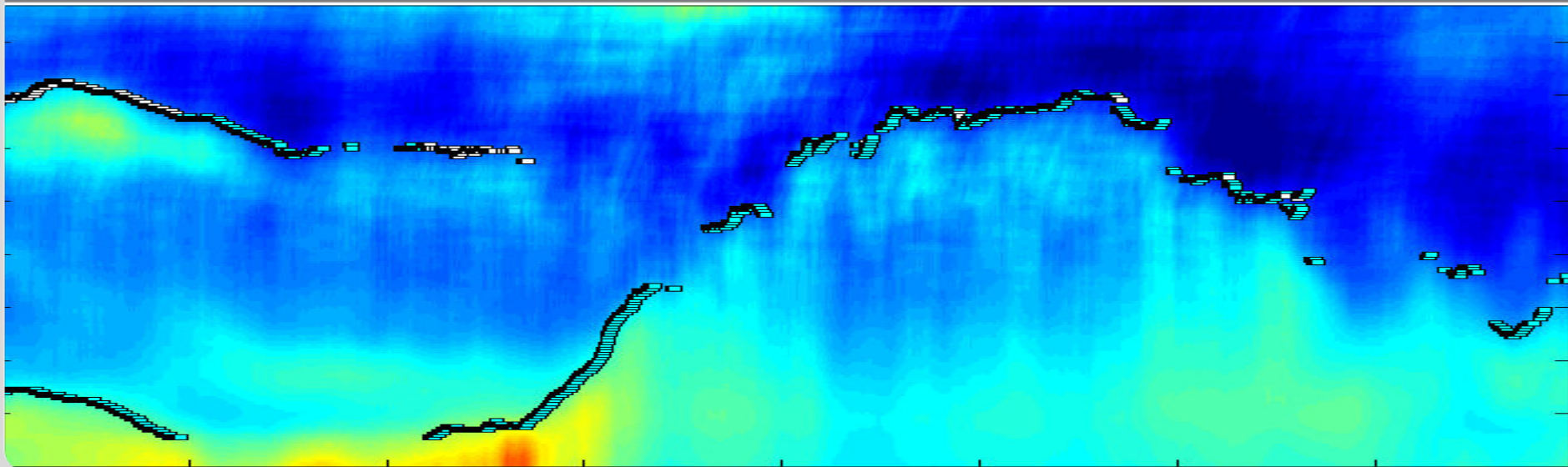


# Different methods to derive the mixing-layer height by remote sensing (including RASS)

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# Introduction

- definition of mixing layer
- relevance for wind energy
  - remote sensing

# Mixing-layer height

## Inversion height

literally: inversion in the temperature profile, increase of temperature with height, strong decrease of moisture, radiation inversions, sinking inversions, surface inversions, lifted inversions

## Mixing-layer height

(mixing height, mixed-layer height)

upper boundary for vertical exchange (mixing), upper boundary of the well-mixed layer, entrainment, defined by the turbulence profile or by the vertical distribution of a tracer (aerosol, pot. temperature)

## Boundary layer height

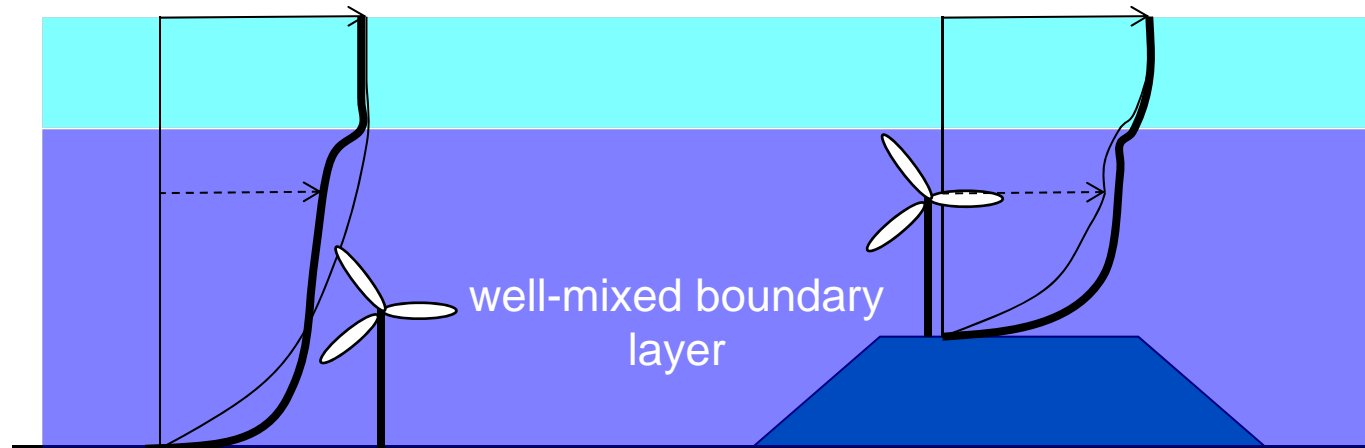
SBL: at night, height of the near-surface layer influenced by surface friction  
CBL: at day, height of convective plumes

boundary layer height  $\approx$  mixing-layer height

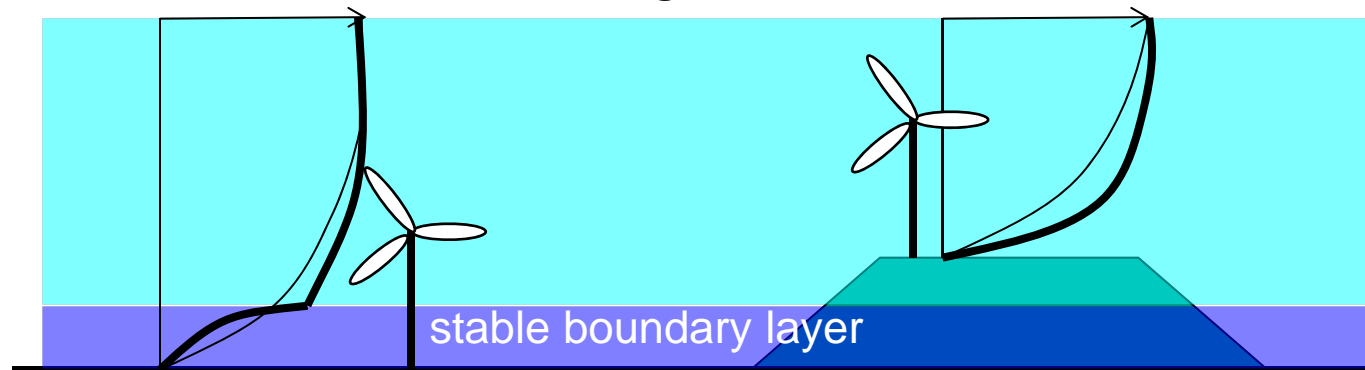
boundary layer height  $\geq$  inversion height

## Mixing-layer height influences diurnal variation of vertical wind profiles

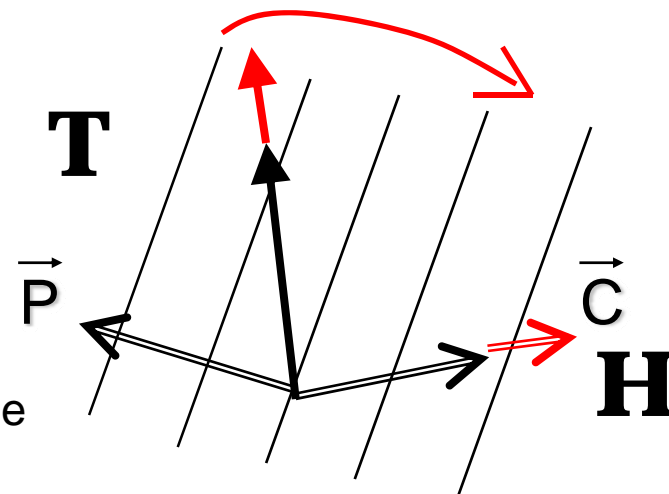
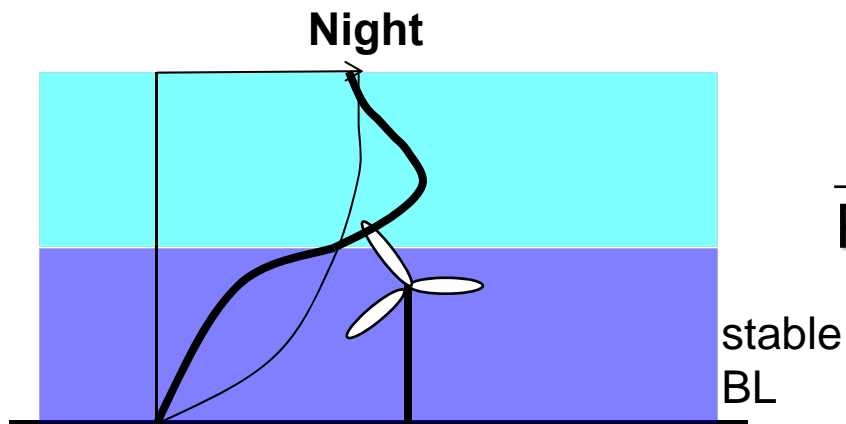
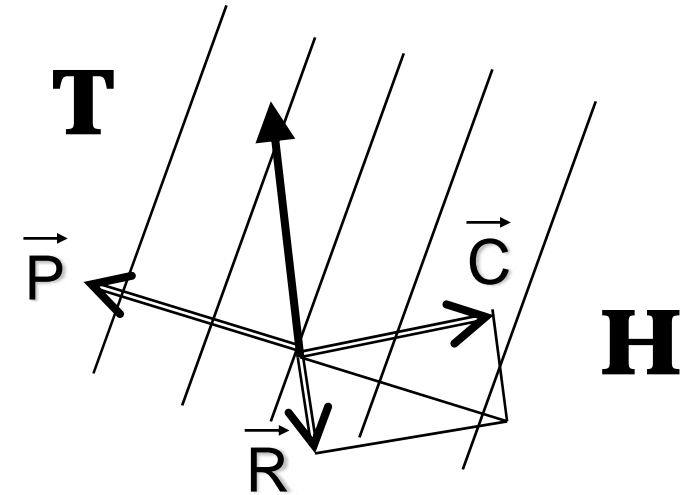
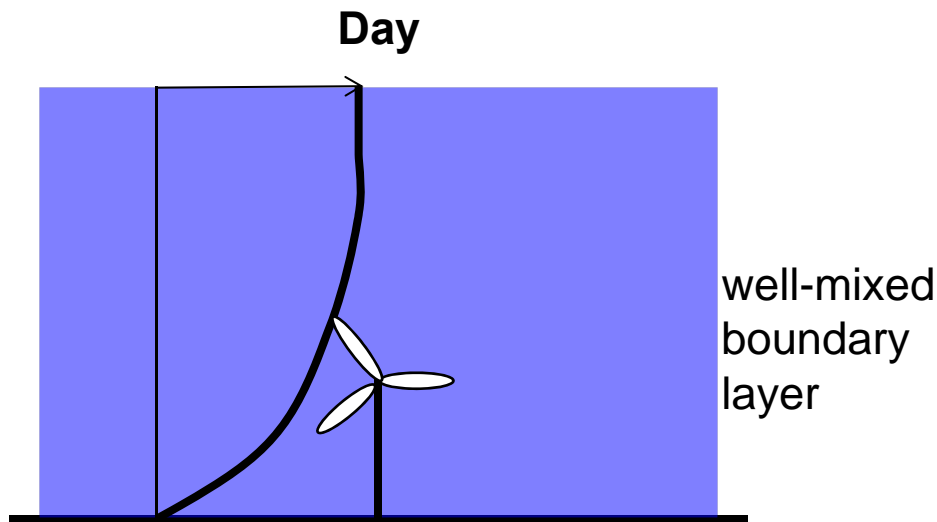
Day



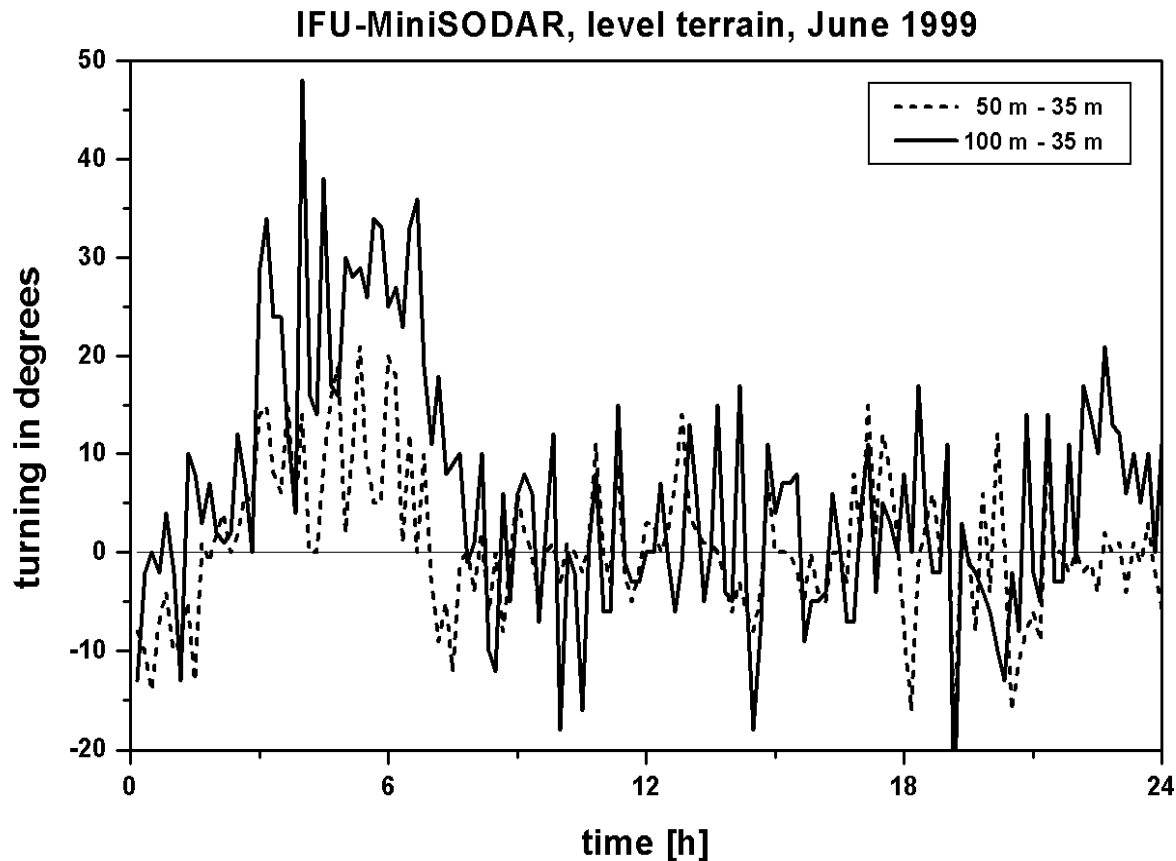
Night



## Nocturnal low-level jet and the turning of wind direction with height



# Mean diurnal variation of the turning of wind direction with height



Emeis, S., 2001: Vertical variation of frequency distributions of wind speed in and above the surface layer observed by sodar. Meteorol. Z., **10**, 141-149.

# example for extreme turning of wind direction with height

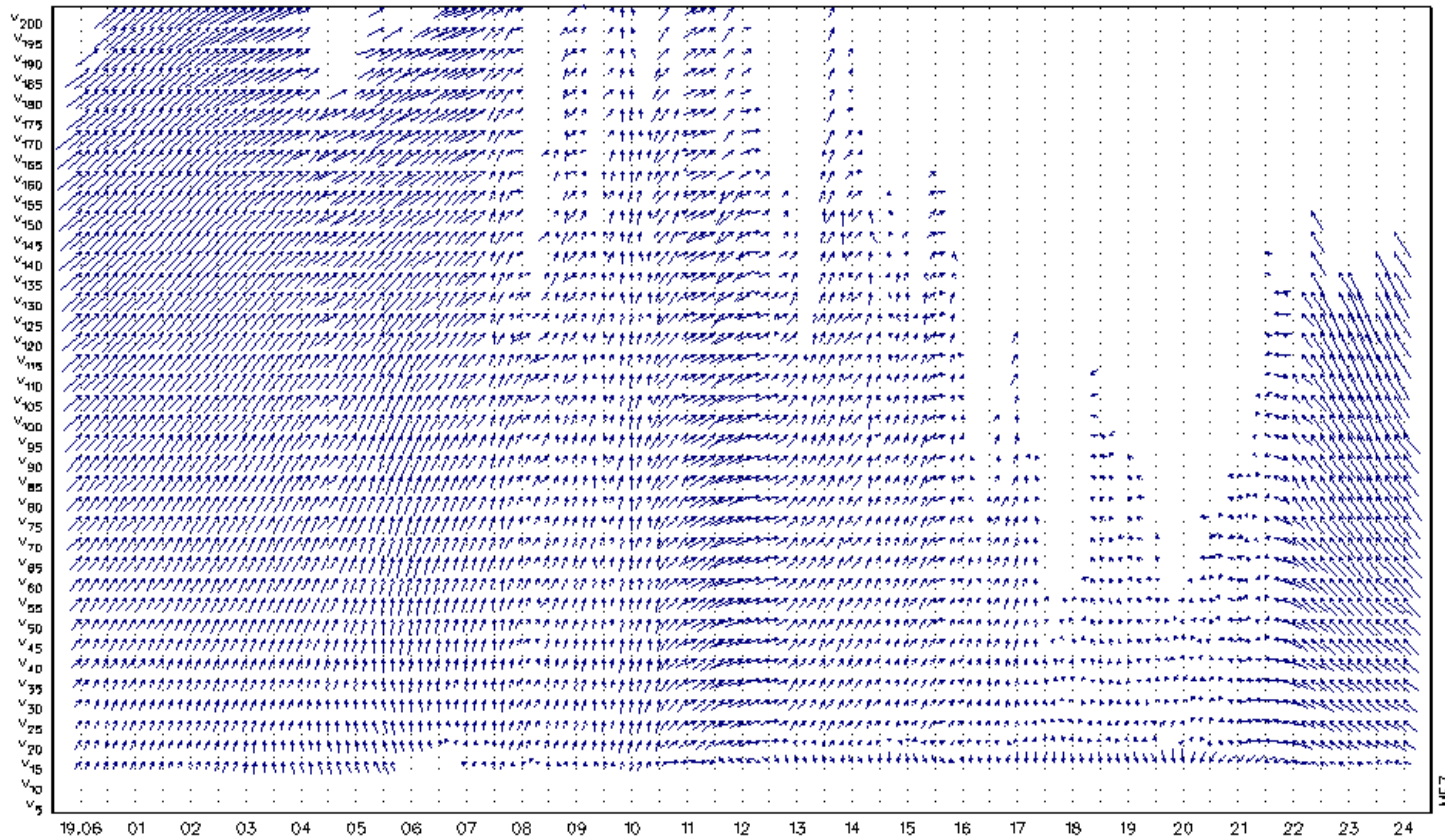


Abb.: 10'-Mittel des Windvektors ( $v_x$ ) für ausgewählte Höhen (x)  
 IFU-MiniSODAR Sachsen-Anhalt Juni 1999

← = 3 m/s Westwind

IFU GAP

Emeis, S., 2001: Vertical variation of frequency distributions of wind speed in and above the surface layer observed by sodar. Meteorol. Z., **10**, 141-149.

# The vertical wind profile

logarithmic law

(with stability correction)  $u(z) = (u_*/\kappa) (\ln(z/z_0) - \psi(z/L_*))$

power law

$$u(z) = u(z_A) (z/z_A)^n$$

---

New proposal  
(Gryning et al. 2007)

$$u(z) = \frac{u_{*0}}{\kappa} \left( \ln \left( \frac{z}{z_0} \right) + \frac{z}{L_{MBL,N}} - \frac{z}{z_i} \left( \frac{z}{2L_{MBL,N}} \right) \right)$$

**needs information on the PBL or mixing-layer height**

Gryning, S.-E., E. Batchvarova, B. Brümmner, H. Jørgensen, S. Larsen, 2007: On the extension of the wind profile over homogeneous terrain beyond the surface boundary layer. Bound.-Lay. Meteorol., **124**, 251–268.

Peña, A., S.-E. Gryning, C.B. Hasager, 2010: Comparing mixing-length models of the diabatic wind profile over homogeneous terrain. Theor. Appl. Climatol., **100**, 325-353.



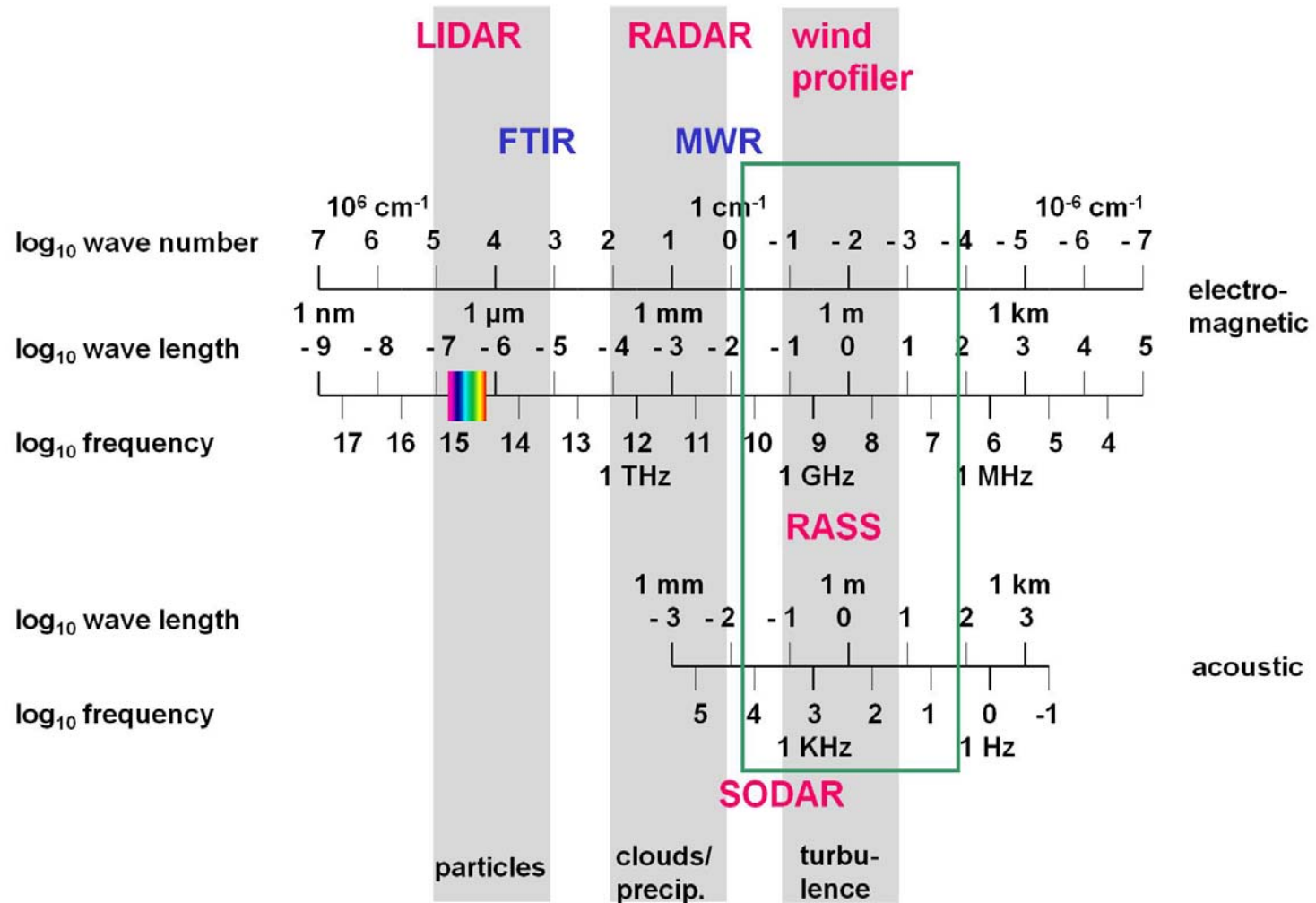
# Basic remote sensing techniques

name	principle	spatial resolution	direction	type
RADAR	backscatter, electro-magnetic pulses, fixed wave length	profiling	scanning, slanted	active, monostatic
SODAR	backscatter, acoustic pulses, fixed wave length	profiling	fixed, slanted, vertical	active, usually monostatic
LIDAR	backscatter, optical pulses, fixed wave length(s)	profiling	scanning, fixed, horizontal, slanted, vertical	active, monostatic
RASS	backscatter, acoustic, electro-magnetic, fixed wave length	profiling	fixed, vertical	active, monostatic
FTIR	absorption, infrared, spectrum	path-averaging	fixed, horizontal, slanted	active, bistatic or passive
FTIR	emission, infrared, spectrum	path-averaging	fixed, horizontal, slanted	passive
DOAS	absorption, optical, fixed wave lengths	path-averaging	fixed, horizontal	active, bistatic
radiometry	electro-magnetic, fixed wave length(s)	averaging, profiling	fixed, scanning, slanted, vertical	passive
tomography	travel time, acoustic, fixed wave length	horizontal distribution	fixed, horizontal	active, multiple emitters and receivers

subject of this lecture

subject of this lecture

## Frequencies for atmospheric remote sensing

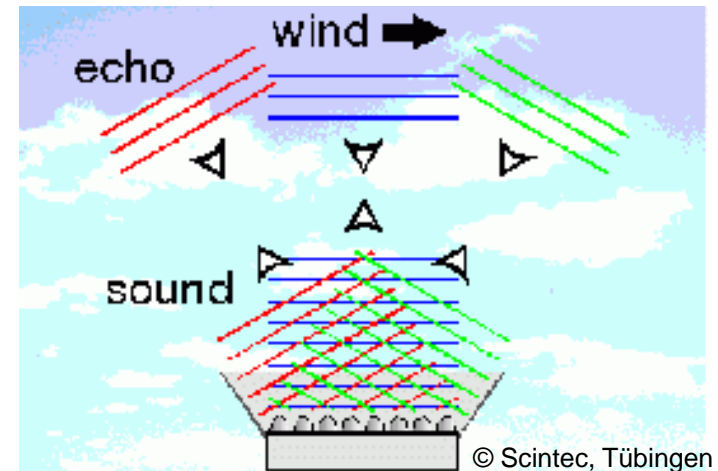
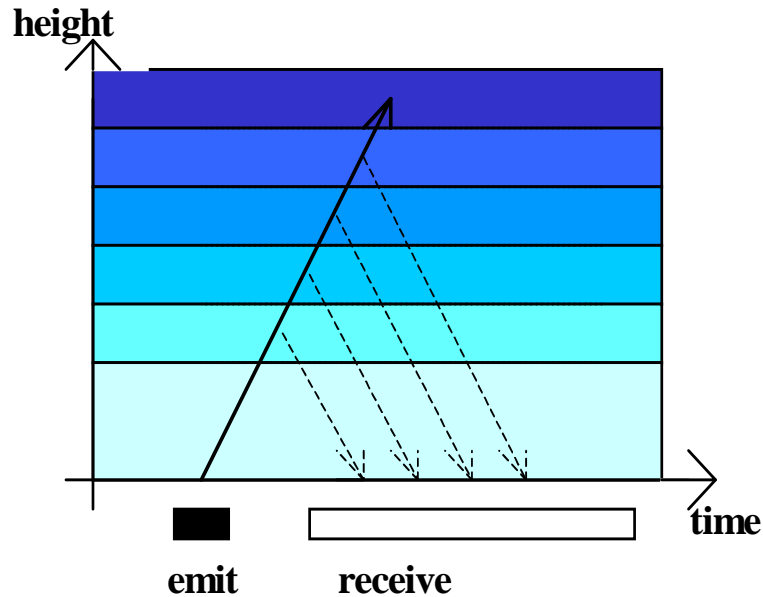


Emeis, S., 2010: Measurement Methods in Atmospheric Sciences - In situ and remote. Borntraeger, Stuttgart, 272 pp., 103 figs, 28 tables, ISBN 978-3-443-01066-9.

# SODAR

## algorithms for the determination of mixing-layer height

# monostatic SODAR: measuring principles



deduction:

sound travel time	=	height
backscatter intensity	=	turbulence
Doppler-shift	=	wind speed

Emission of sound waves  
into three directions:

in order to measure all three  
components of the wind  
(horizontal and vertical)

## The SODAR equation:

$$P_R = r^2 (c_s \tau A \varepsilon / 2) P_0 \beta_s e^{-2\sigma r} + P_{bg}$$

$P_R$  received power,

$P_0$  emitted power,

$\varepsilon$  antenna efficiency,

$A$  effective antenna area,

$\sigma$  sound absorption in air due to classical and molecular absorption due to the collision of water molecules with the oxygen and nitrogen molecules of the air,

$r$  distance between the scattering volume and the instrument,

$\tau$  pulse duration (typically between 20 and 100 ms),

$\beta_s$  backscattering cross-section (typically in the order of  $10^{-11} \text{ m}^{-1} \text{ sr}^{-1}$ ),

$c_s$  sound speed,

$P_{bg}$  background noise.

**Emitted power:  $\sim 10^3 \text{ W}$ , received (backscattered) power:  $10^{-15} \text{ W}$**

The SODAR equation:

$$P_R = r^2 (c_s \tau A \epsilon / 2) P_0 \beta_s e^{-2\sigma r} + P_{bg}$$

The ratio of the two terms on the right-hand side of the SODAR equation is called signal-to-noise ratio (usually abbreviated as SNR).

The backscattering cross-section  $\beta_s$  is a function of the temperature structure function  $C_T^2$  (Tatarskii 1961).

For a monostatic SODAR we find (Reitebuch 1999) when using the wave number  $k = 2\pi/\lambda$ :

$$\beta_s(180^\circ) = 0,00408 k^{1/3} C_T^2 / T^2$$

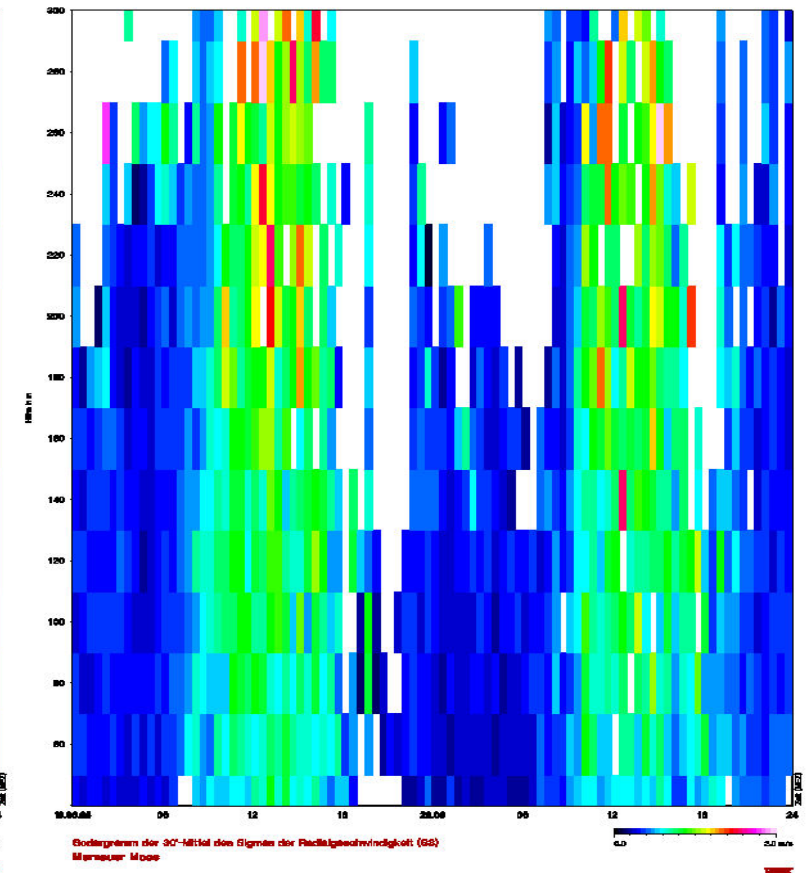
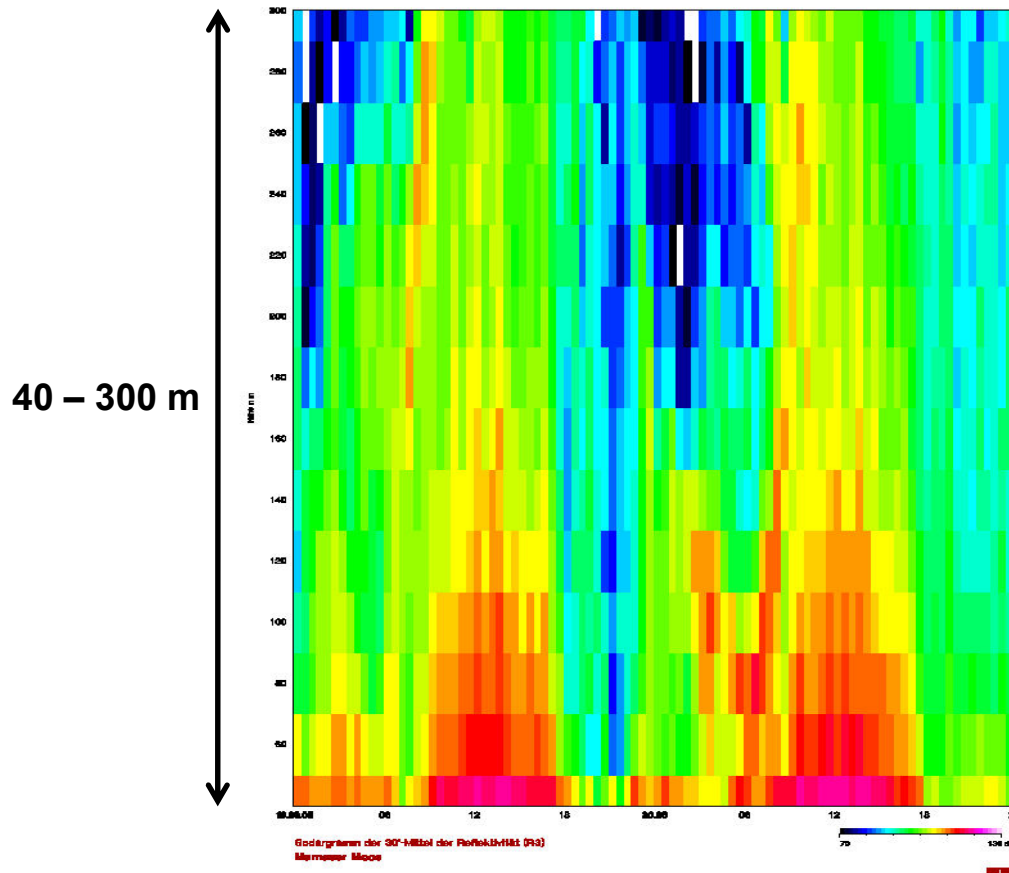
Reitebuch, O., 1999: SODAR-Signalverarbeitung von Einzelpulsen zur Bestimmung hochaufgelöster Windprofile. Schriftenreihe des Fraunhofer-Instituts für Atmosphärische Umweltforschung, Shaker Verlag GmbH Aachen, Bd. 62, 178 S.

Tatarskii, V.I., 1971: The effect of the turbulent atmosphere on wave propagation. Kefer Press, Jerusalem, 472 S.

# SODAR sample plot (daytime convective BL)

## acoustic backscatter intensity

## sigma w

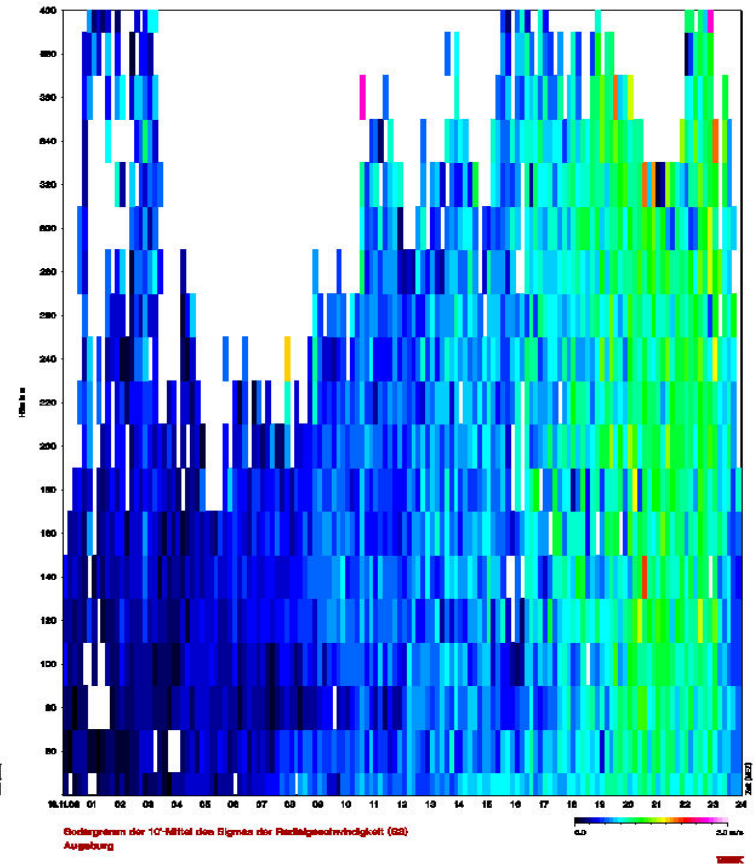
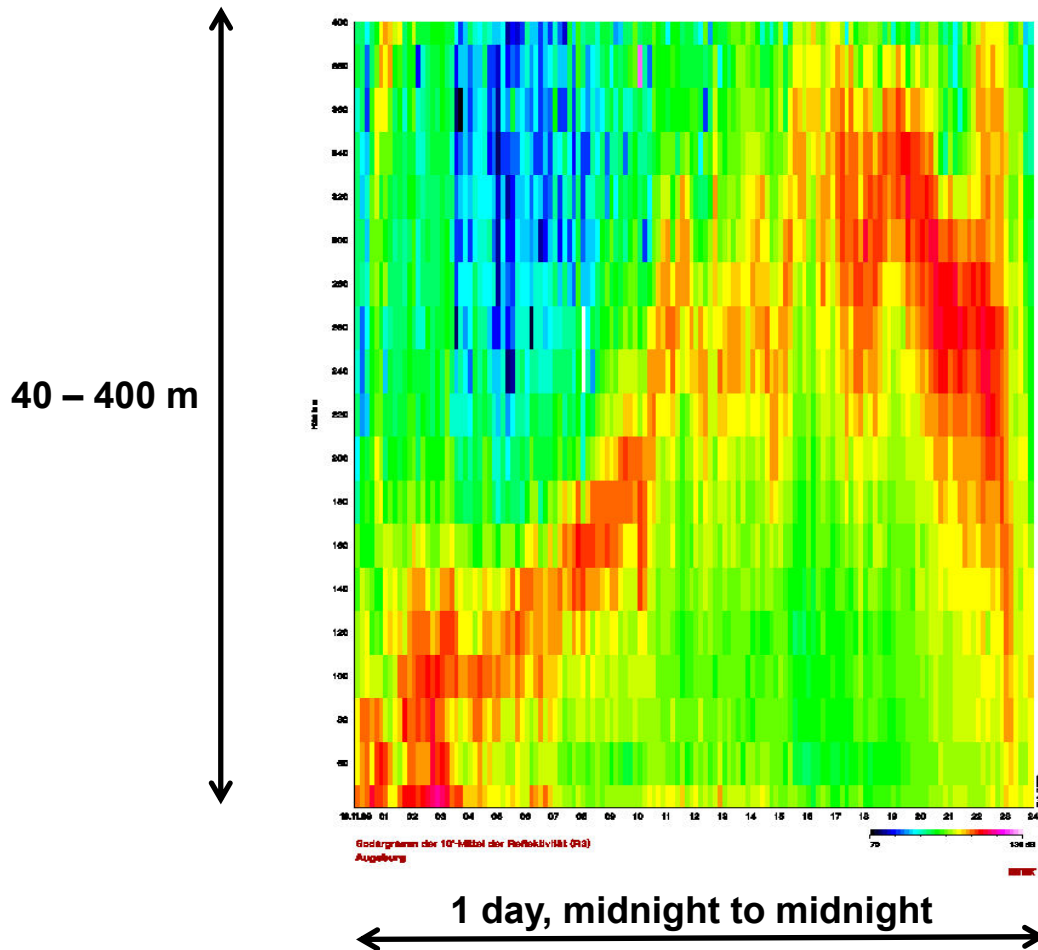


2 days, midnight to midnight

# SODAR sample plot (lifted inversion)

## acoustic backscatter intensity

## sigma w



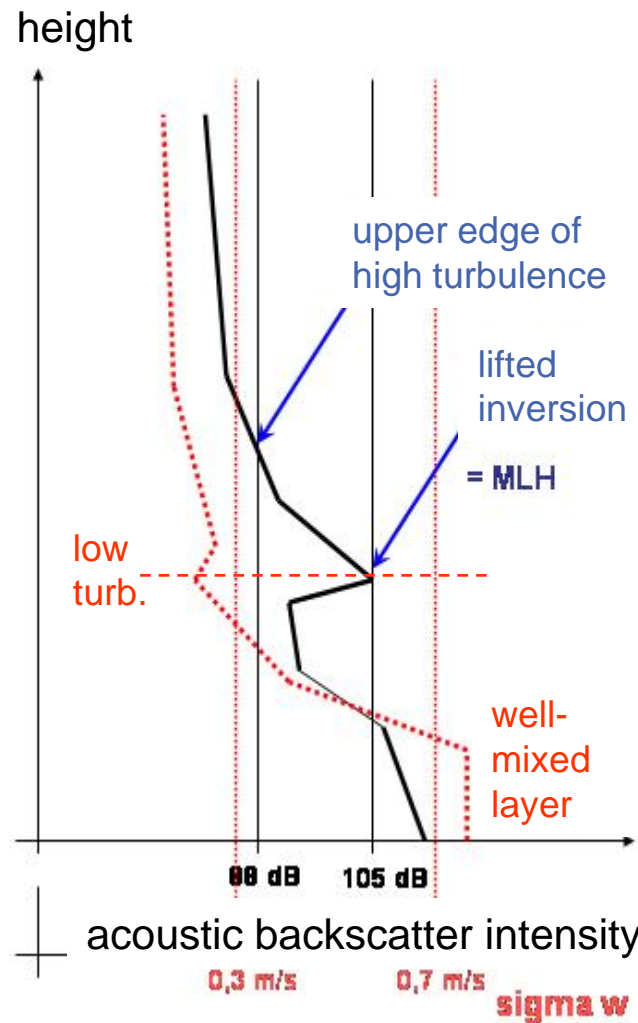


# Algorithms to detect MLH from SODAR data

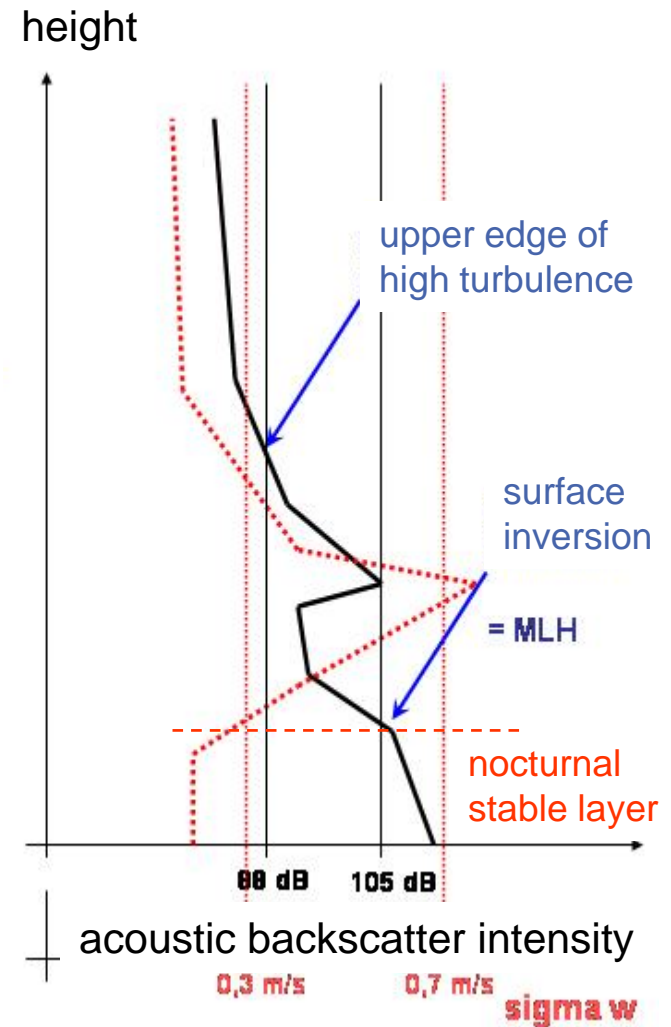
criterion 1:  
 upper edge  
 of high  
 turbulence

criterion 2:  
 surface and  
 lifted  
 inversions

MLH = Min (C1, C2)



example 1: daytime

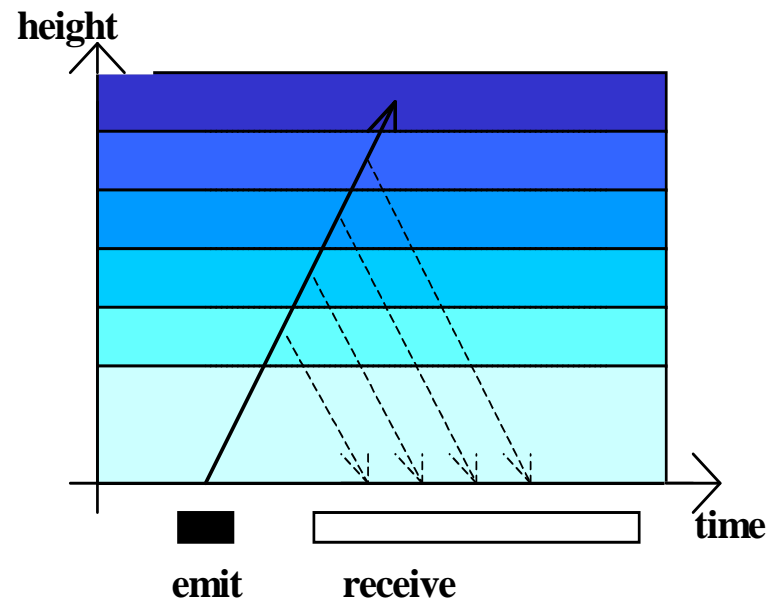


example 2: night-time

# Ceilometer

**algorithms for the determination of  
mixing-layer height**

# Ceilometer/LIDAR measuring principle



detection:

travel time of signal	= height
backscatter intensity	= particle size and number distribution
Doppler-shift	= cannot be analyzed from ceilometer data
	(available only from a Wind-LIDAR: velocity component in line of sight)

The LIDAR equation:

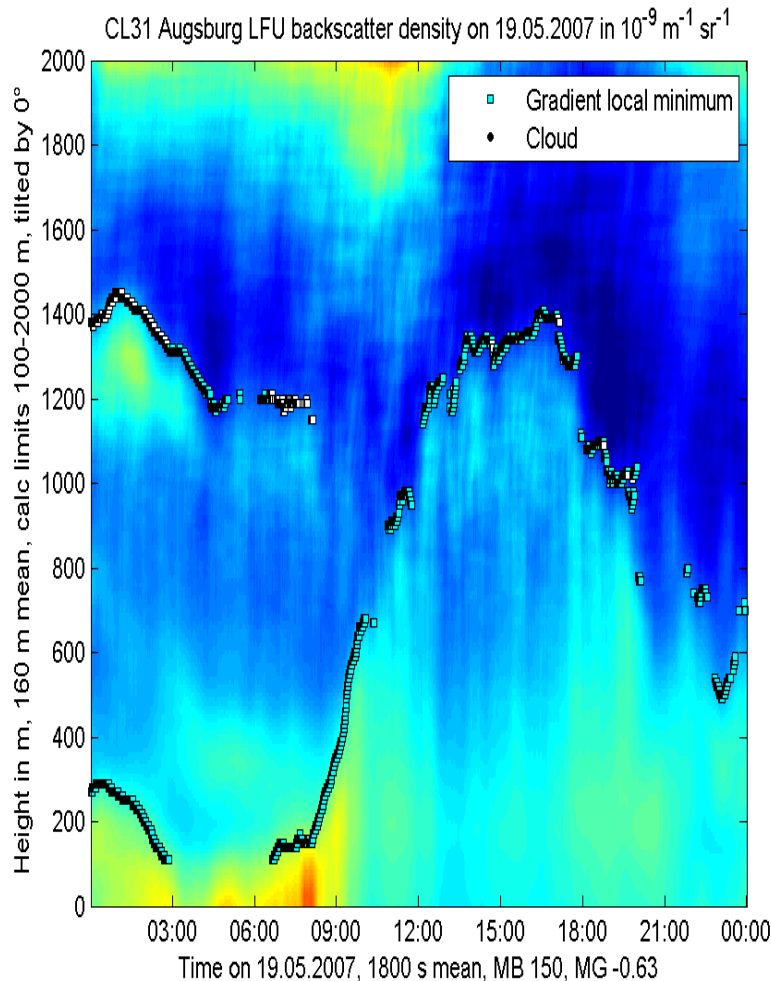
$$P_R(\lambda, r) = r^2 (c\tau A\varepsilon/2) P_0 [\beta_m(\lambda, r) + \beta_p(\lambda, r)] e^{-2\sigma r} + P_{bg}$$

- $r$**  distance between the LIDAR and the backscattering object,
- $c$**  speed of light,
- $\tau$**  pulse duration,
- $A$**  antenna area,
- $\varepsilon$**  correction term for the detector efficiency and losses due to the lenses,
- $P_0$**  emitted energy,
- $\beta_m$**  backscatter coefficient for molecules
- $\beta_p$**  backscatter coefficient for particles,
- $\sigma$**  absorption of light in the atmosphere,
- $P_{bg}$**  background noise.

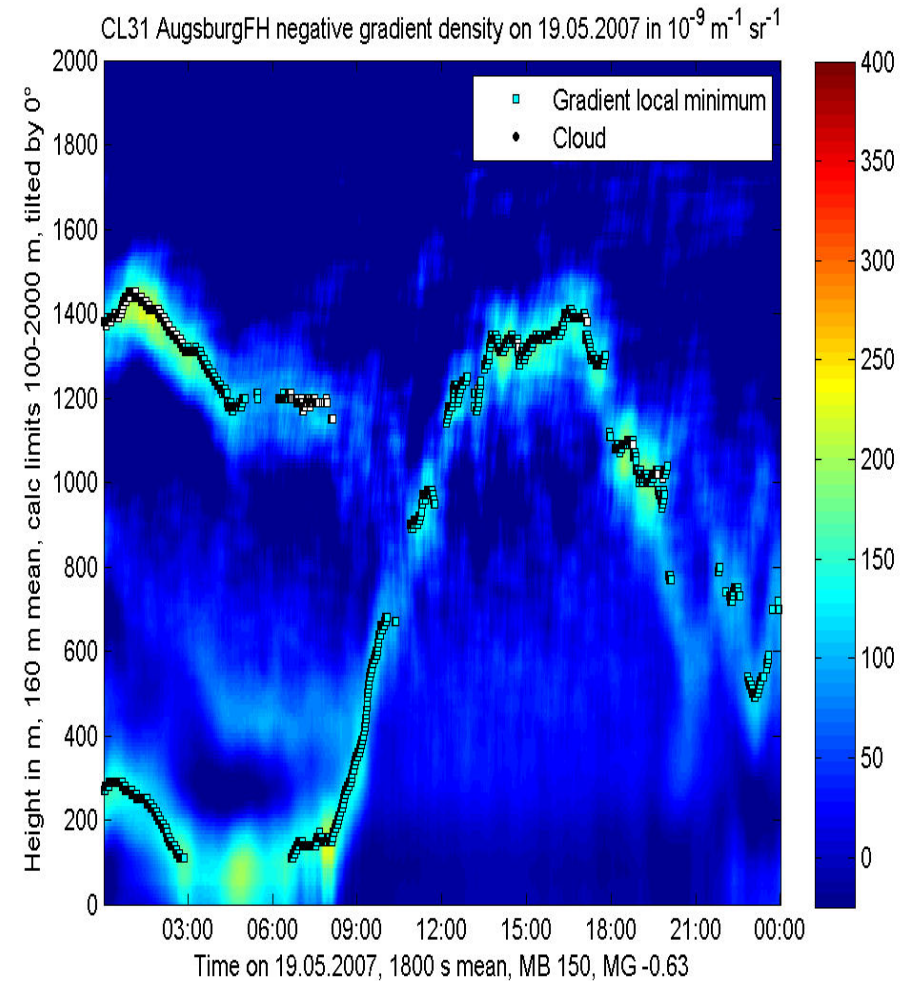
For a ceilometer  $\beta_m$  is negligible and only  $\beta_p$  is important

# ceilometer sample plot (daytime convective BL)

## optical backscatter intensity



## negative vertical gradient of optical backscatter intensity



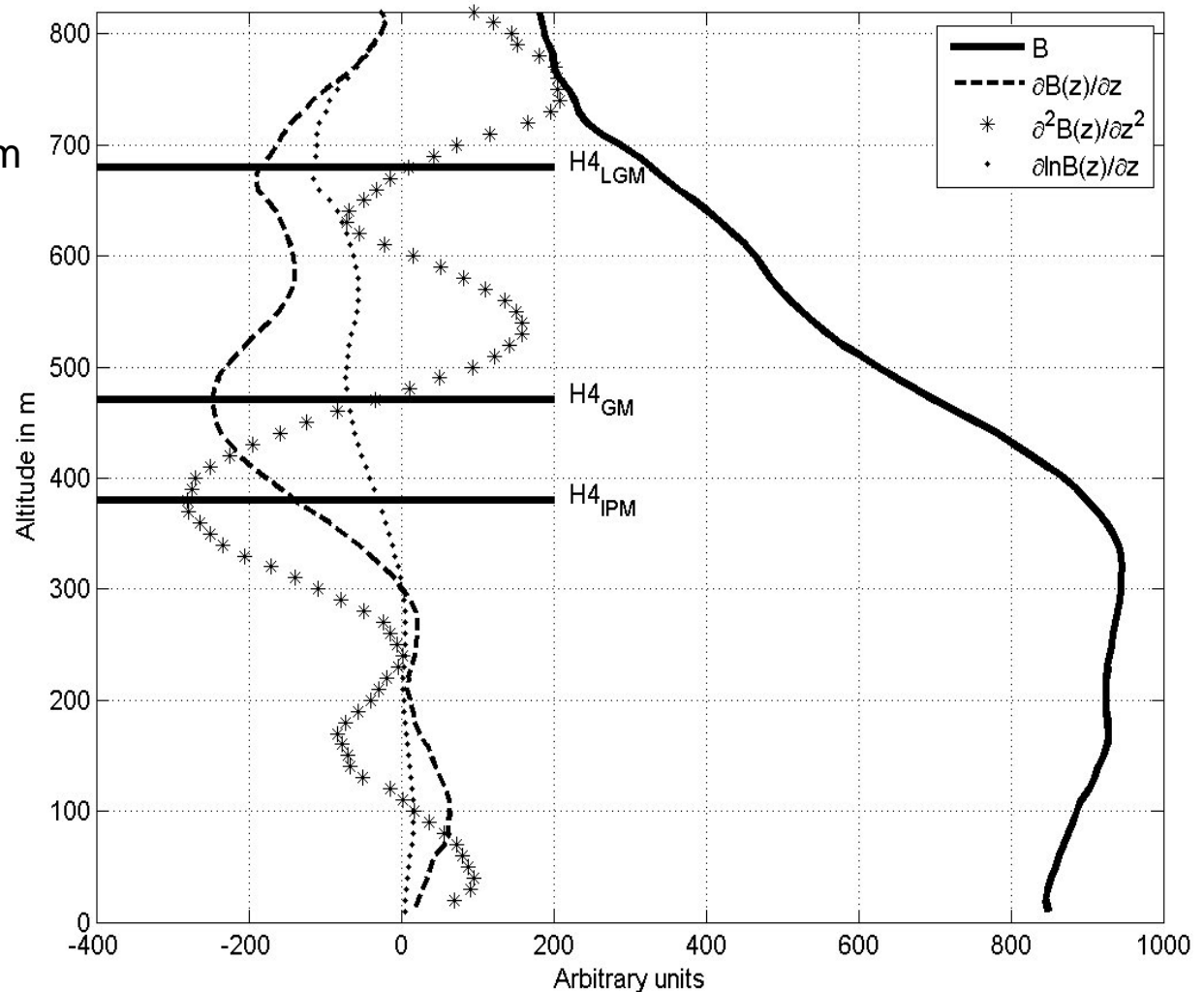


# Different gradient methods (see Sicard et al. 2006, BLM 119, 135-157)

logarithmic gradient minimum

gradient minimum

inflection point method  
(minimum of 2<sup>nd</sup> derivative)



# comparison of two different ceilometers

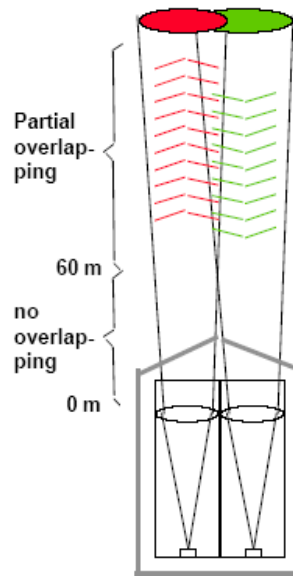
## LD40

two optical axes

wave length: 855 nm

height resolution: 7.5 m

max. range: 13000 m



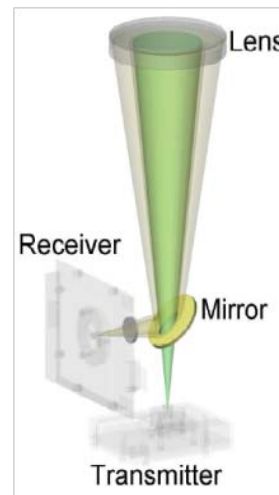
## CL31

one optical axis

wave length: 905 nm

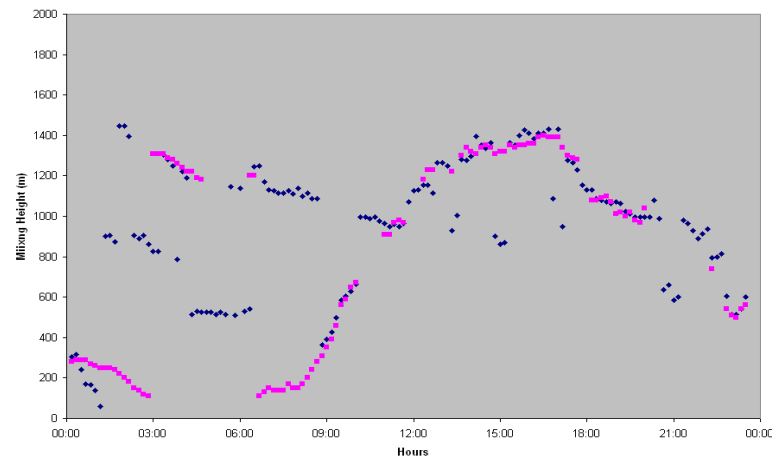
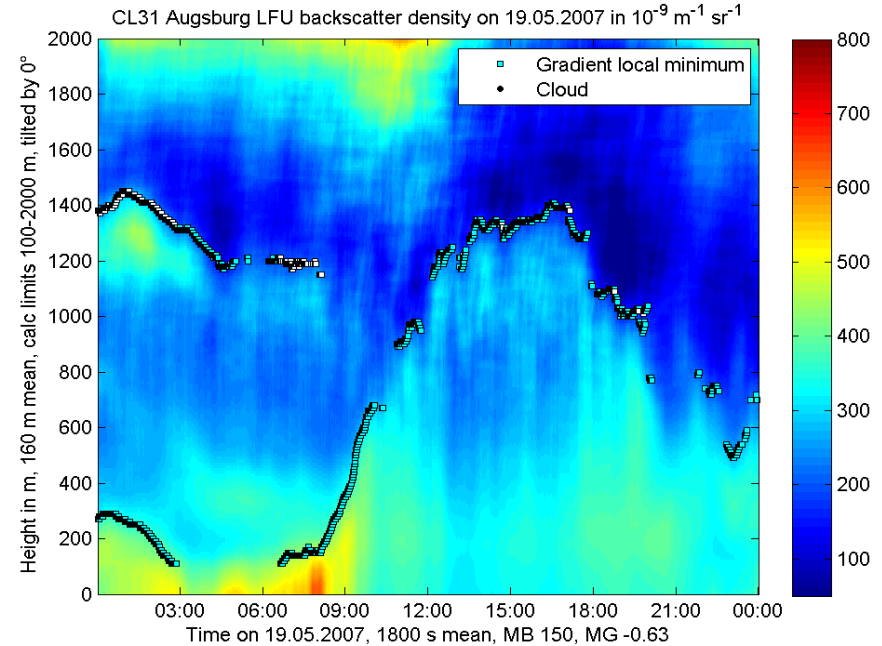
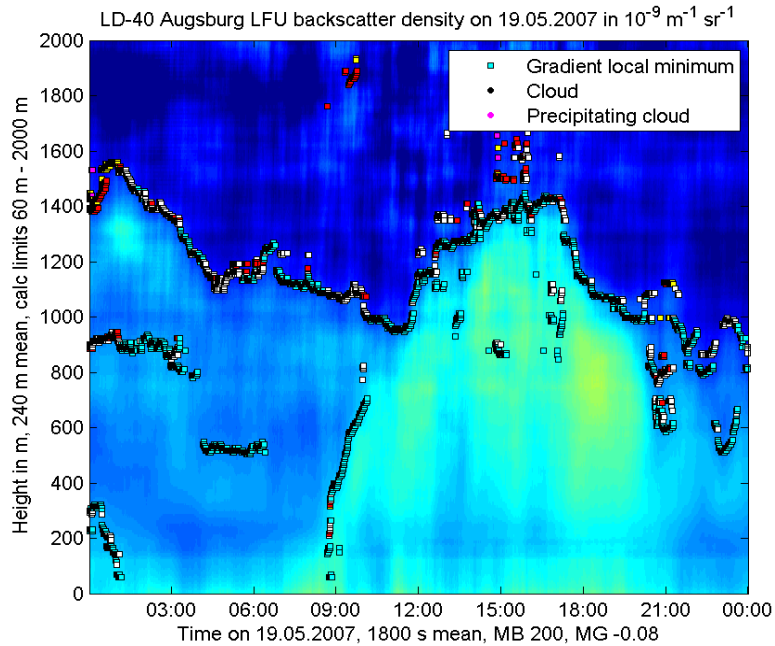
height resolution: 5 m

max. range: 7500 m

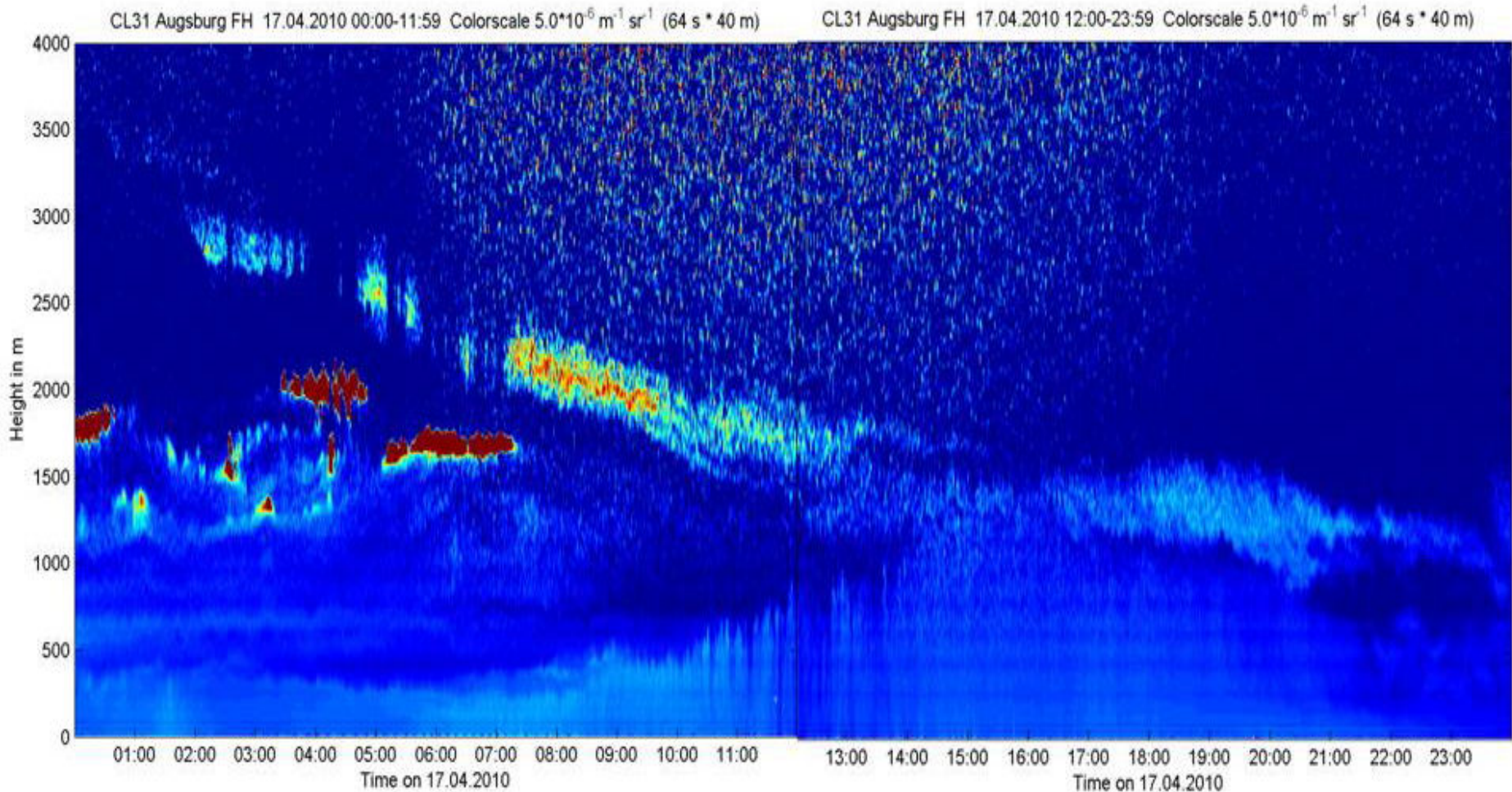




# comparison of LD40 and CL31

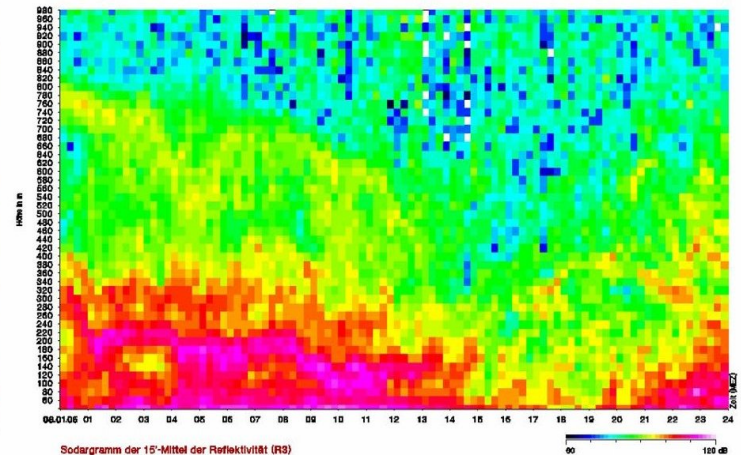
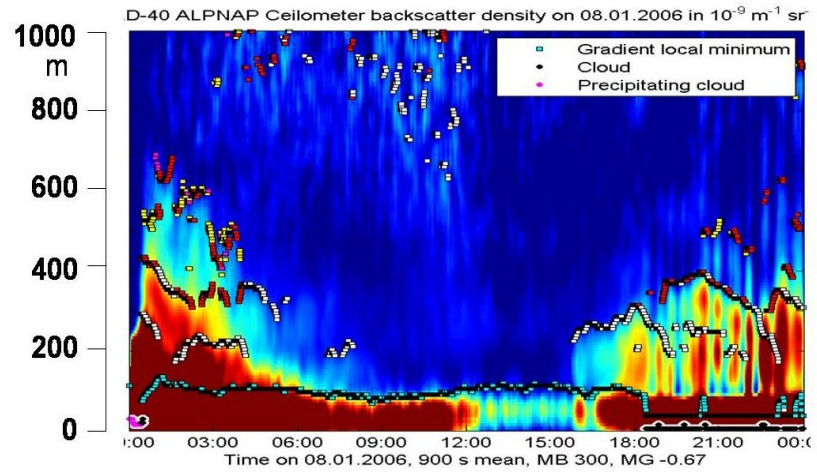


# Eyjafjallajökull ash cloud over Southern Germany



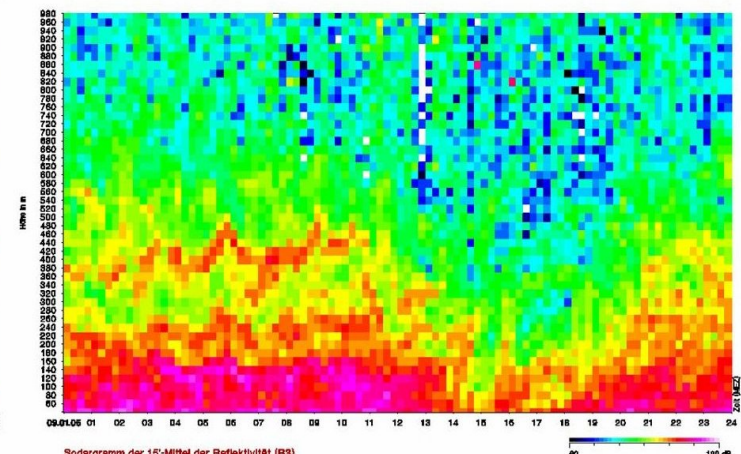
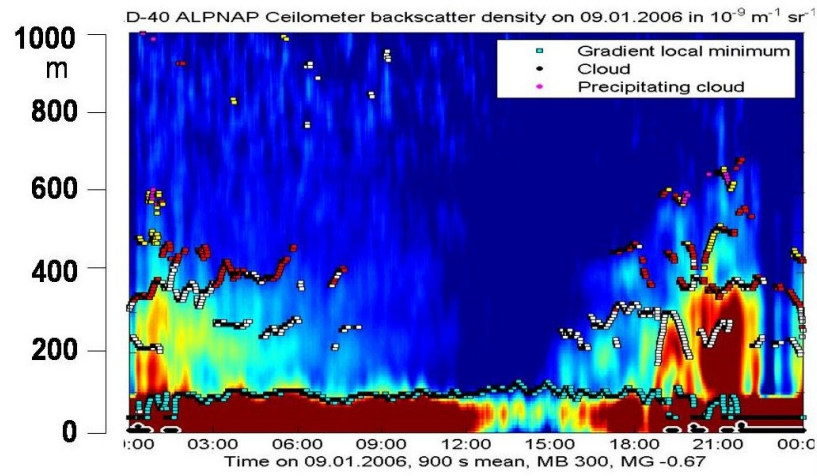
# Application examples for SODAR and Ceilometer

# Detection of multiple layering Ceilometer and SODAR observations from an Alpine valley

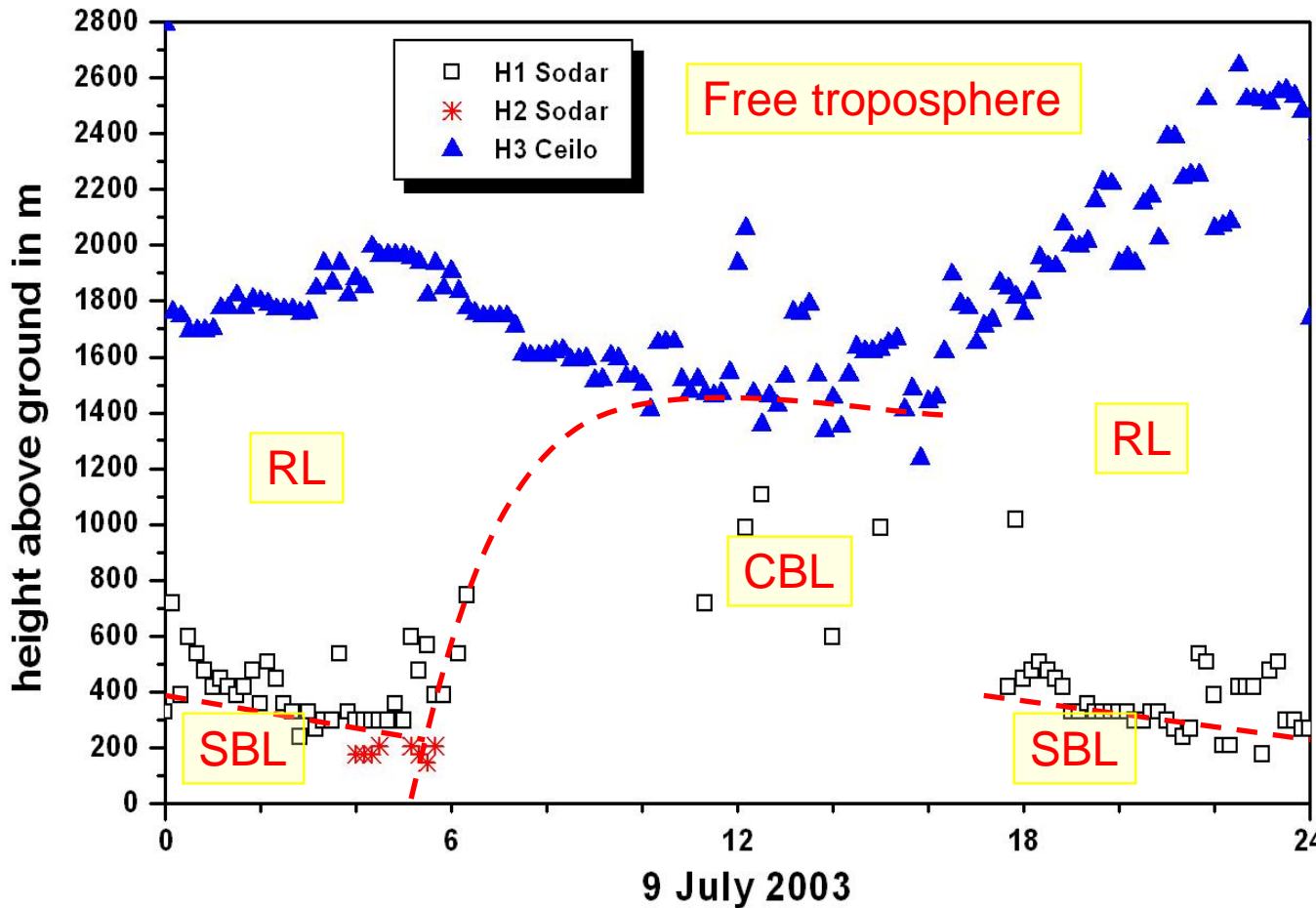


optical backscatter intensity

acoustic backscatter intensity



# Detection of the diurnal variation of PBL structure from SODAR and Ceilometer data taken in Budapest



SBL:

stable boundary layer (usually at night and in winter)

CBL:

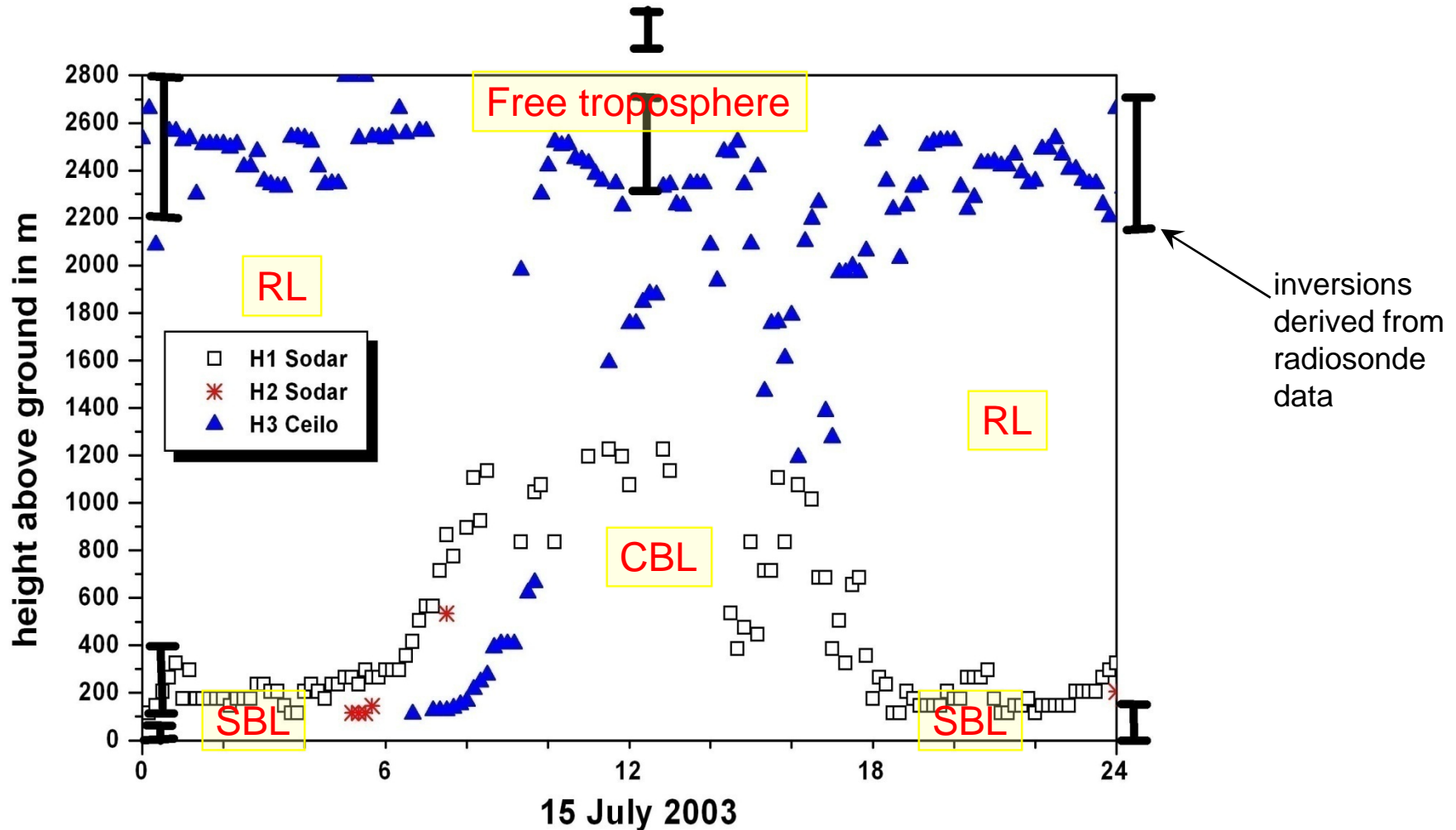
convective boundary layer (usually at daytime due to strong insolation)

RL:

residual layer (usually at night-time)

Emeis, S., K. Schäfer, 2006: Remote sensing methods to investigate boundary-layer structures relevant to air pollution in cities. *Bound.-Lay Meteorol.*, 121, 377-385,

# Differences in MLH detection from SODAR and Ceilometer data taken in Budapest



Emeis, S., K. Schäfer, 2006: Remote sensing methods to investigate boundary-layer structures relevant to air pollution in cities. *Bound.-Lay Meteorol.*, 121, 377-385,

# RASS

**principles of operation**

**examples**

**RASS (radio-acoustic remote sensing)**

**measures vertical temperature profiles**

**Bragg-RASS: windprofiler plus acoustic component**

**Doppler-RASS: SODAR plus electro-magnetic component**

**UHF RASS (boundary layer)**

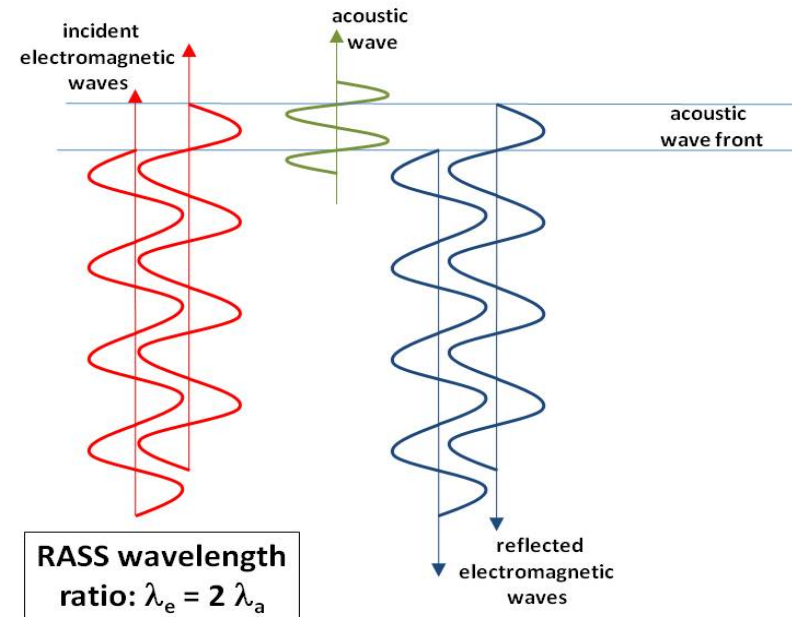
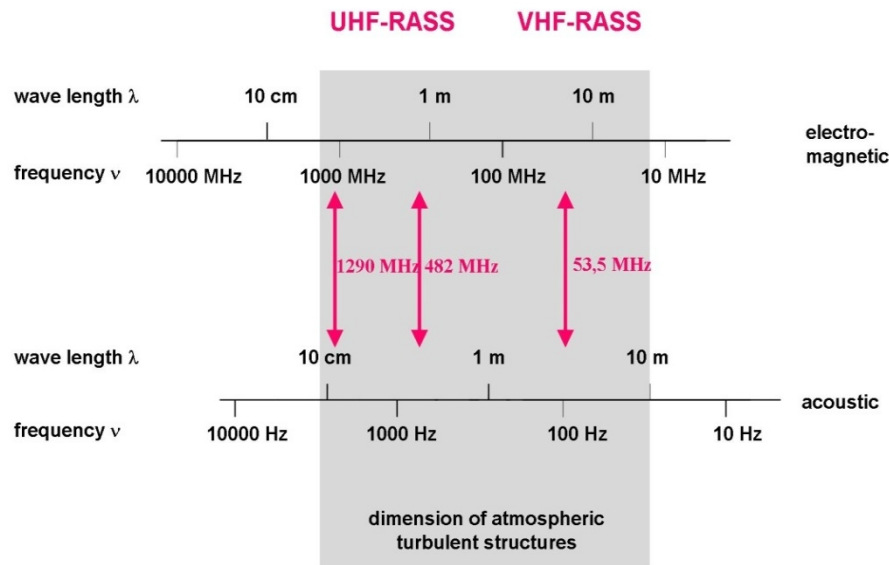
**VHF RASS (troposphere)**



# RASS: frequencies

**Bragg condition:  
acoustic wavelength =  $\frac{1}{2}$  electro-magnetic wavelength**

electro-magnetic - acoustic frequency pairs for RASS devices



Emeis, S., 2010: Measurement Methods in Atmospheric Sciences - In situ and remote. Borntraeger, Stuttgart, 272 pp., 103 figs, 28 tables, ISBN 978-3-443-01066-9.



## SODAR-RASS (Doppler-RASS)

(METEK)

acoustic frequ.: 1500 – 2200 Hz

radio frequ.: 474 MHz

resolution: 20 m

lowest

range gate: ca. 40 m

vertical range: 540 m



## Bragg-RASS

acoustic frequ.: about 3000 Hz

radio frequ.: 1290 MHz

resolution: 50 m

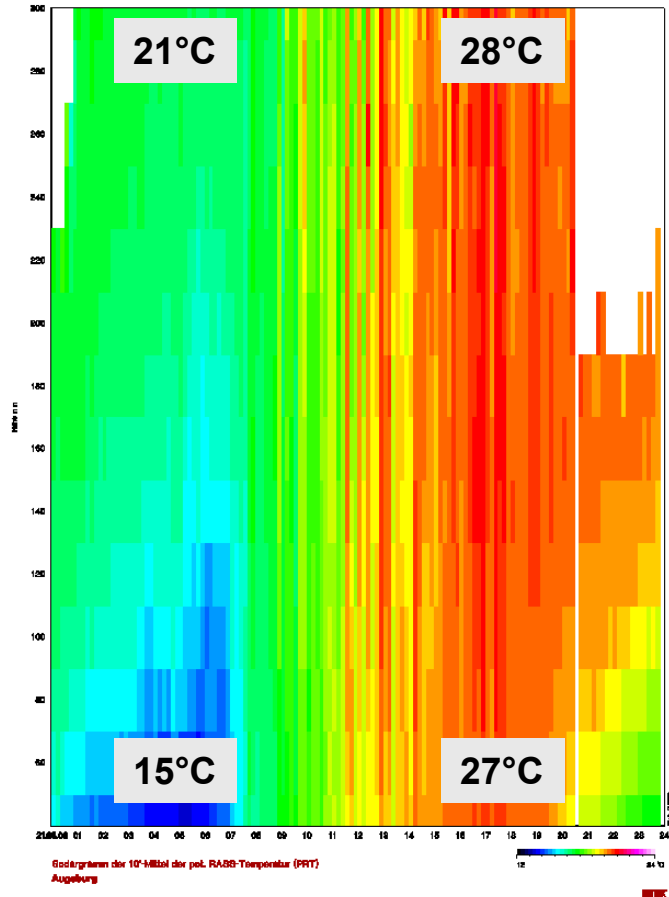
lowest

range gate: ca. 200 m

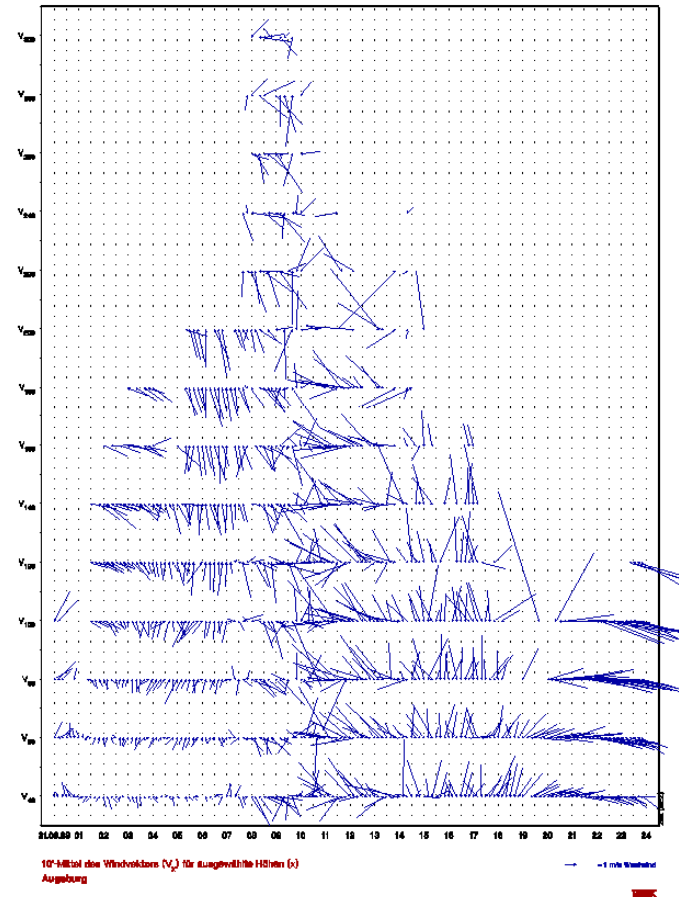
vertical range: 1000 m

# example RASS data: summer day potential temperature (left), horizontal wind (right)

300 m



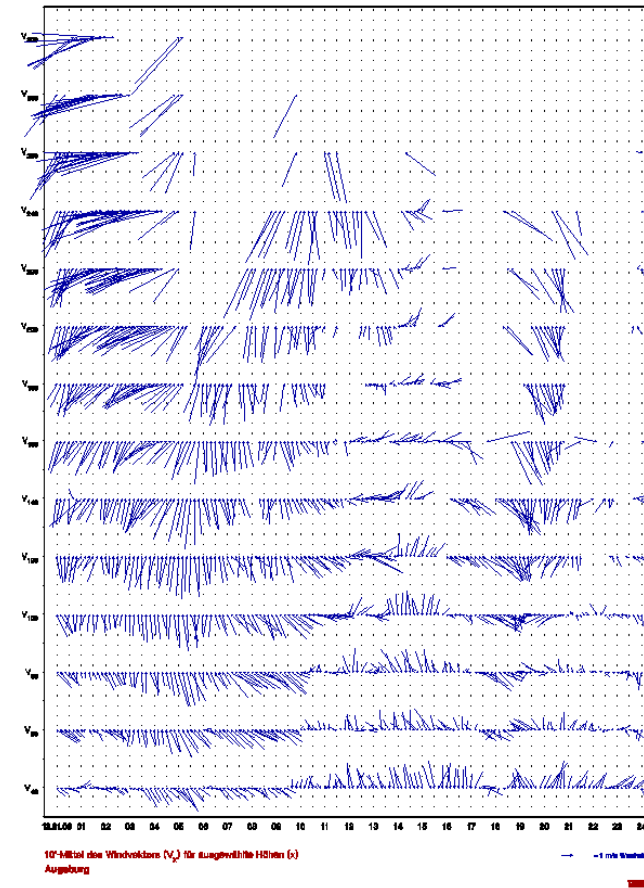
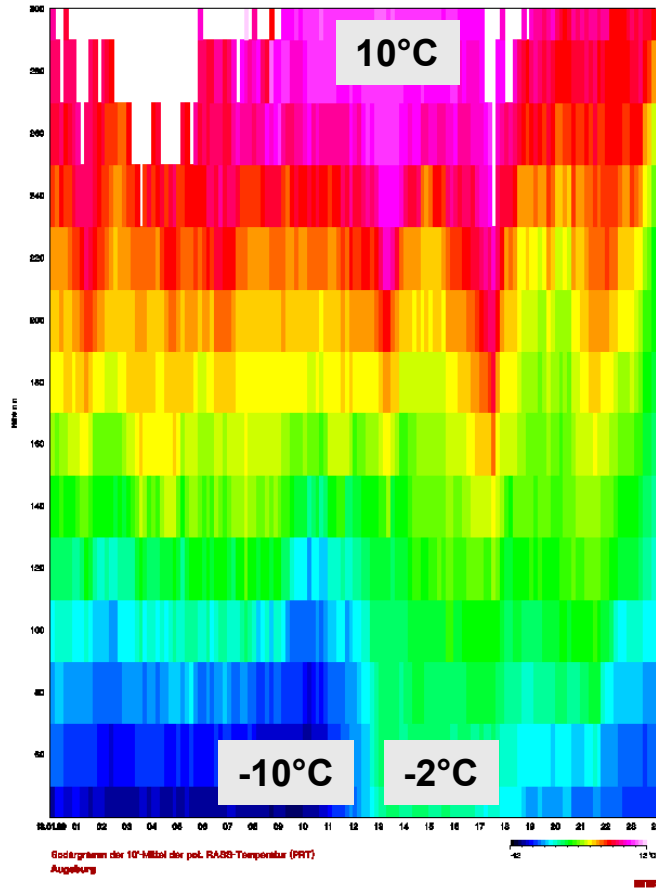
40 m



# example RASS data: winter day

## potential temperature (left), horizontal wind (right)

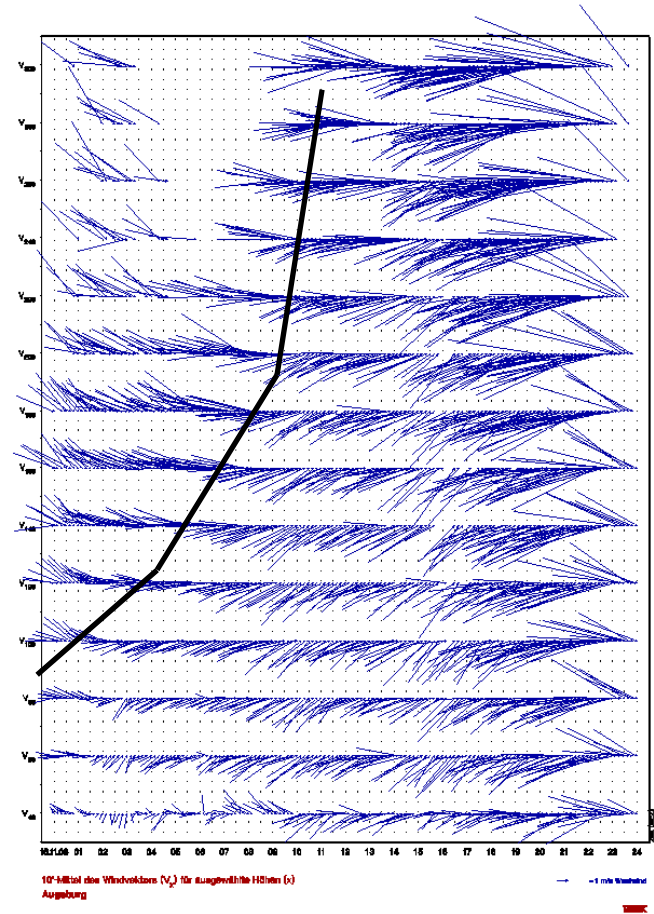
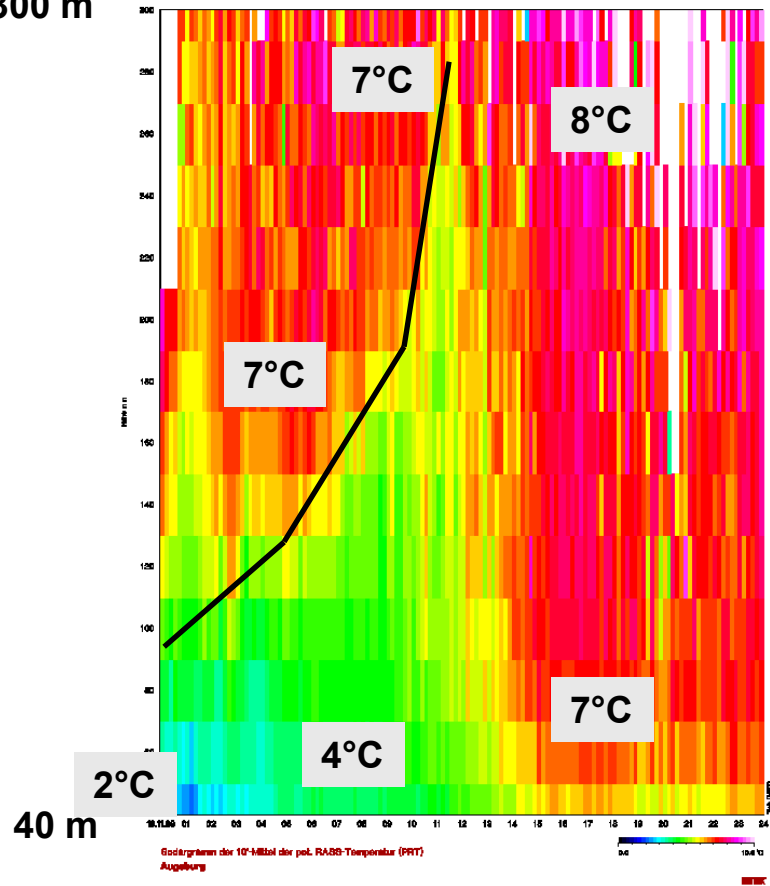
300 m



# example RASS data: inversion

## potential temperature (left), horizontal wind (right)

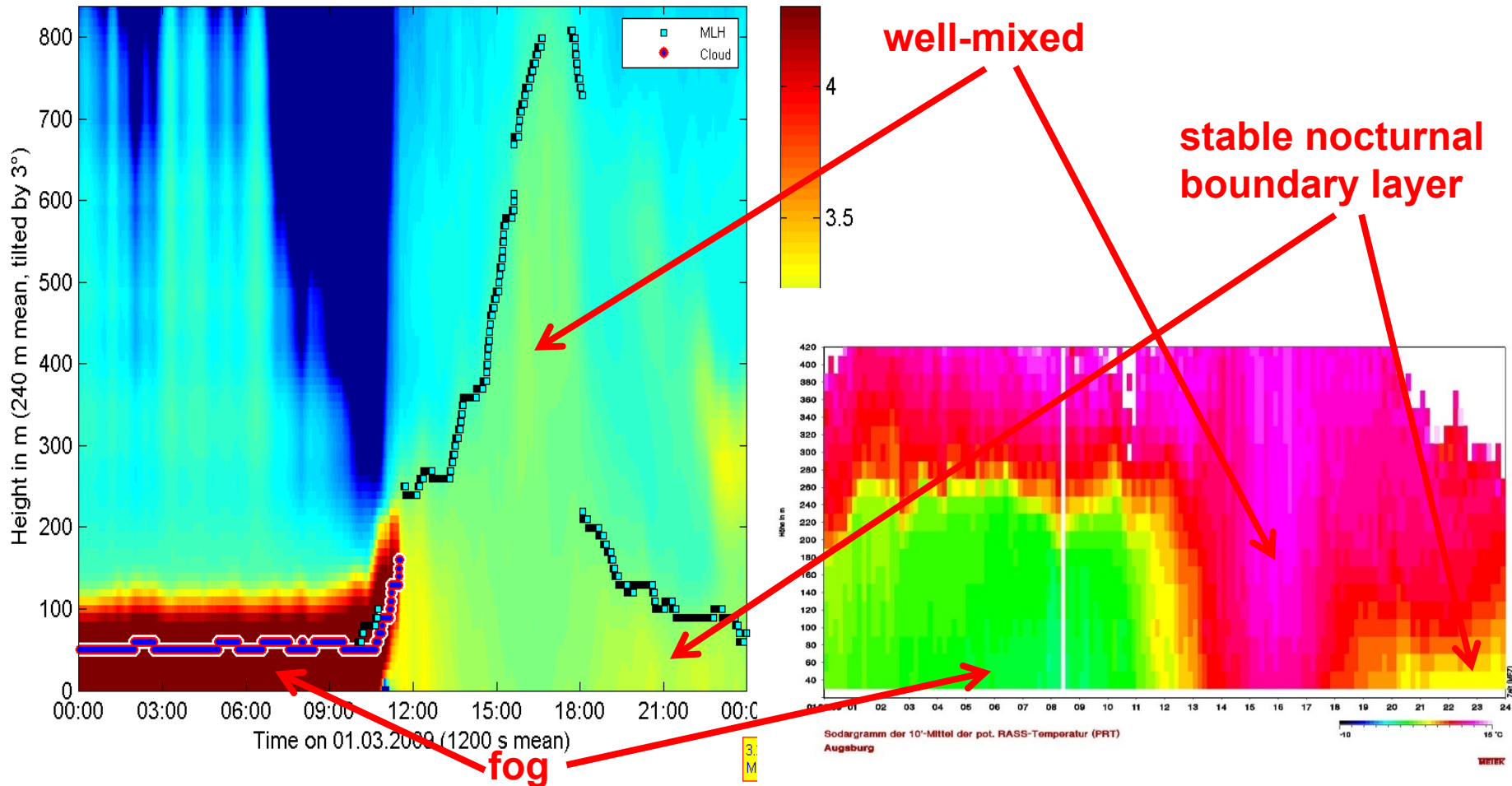
300 m



# temperature profile and pollution

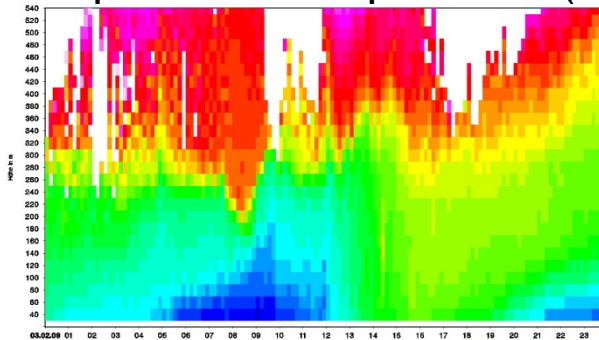
comparison of RASS data (potential temperature, right)  
with aerosol backscatter from a ceilometer (left)

CL31 Augsburg AVA  $\log_{10}$  of backscatter with MLH on 01.03.2009 in  $10^{-9} \text{ m}^{-1} \text{ sr}^{-1}$

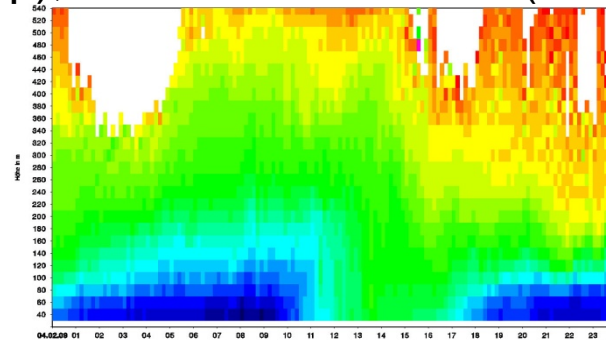


# RASS data Augsburg February 2009

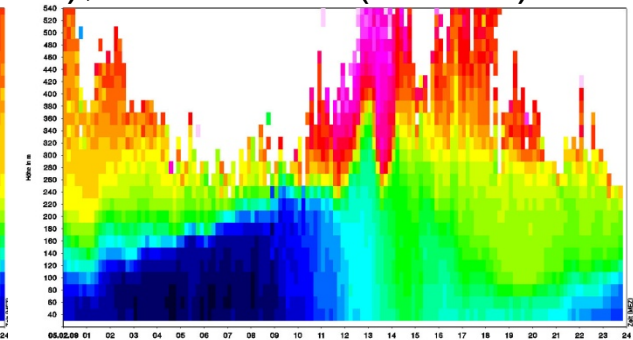
potential temperature (top), backscatter SODAR (middle), Ceilometer (bottom)



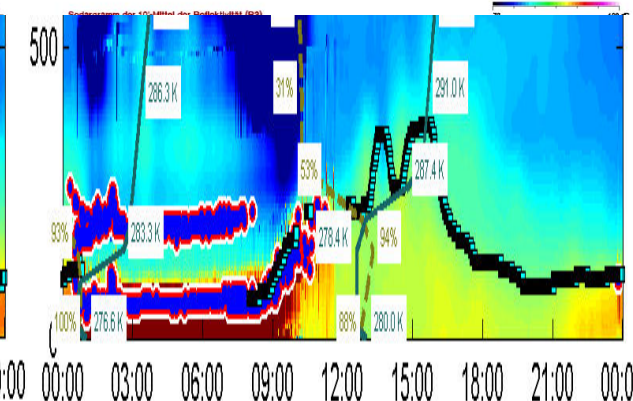
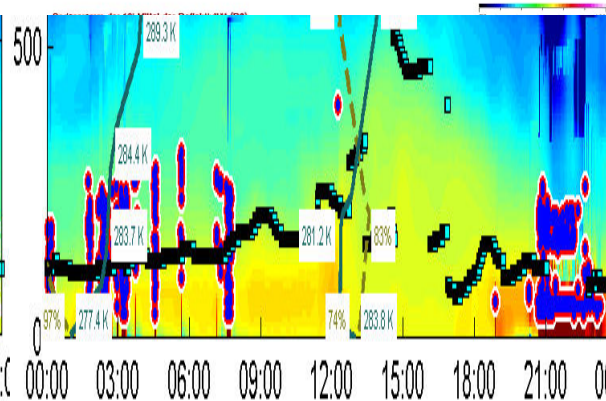
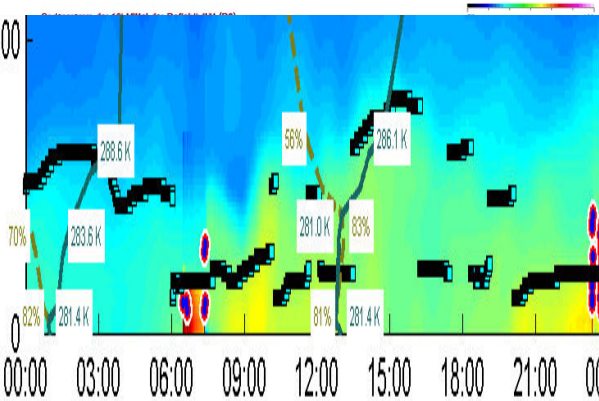
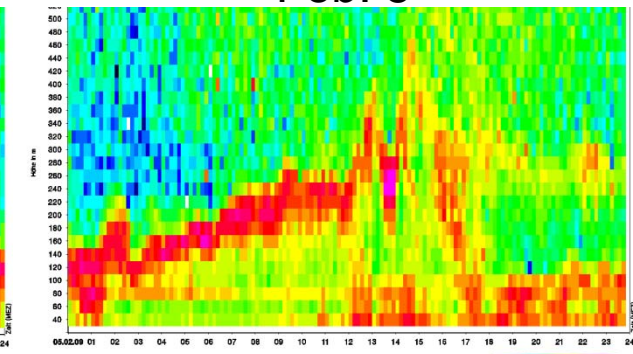
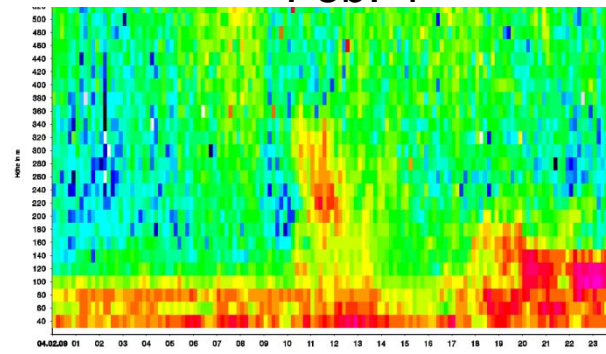
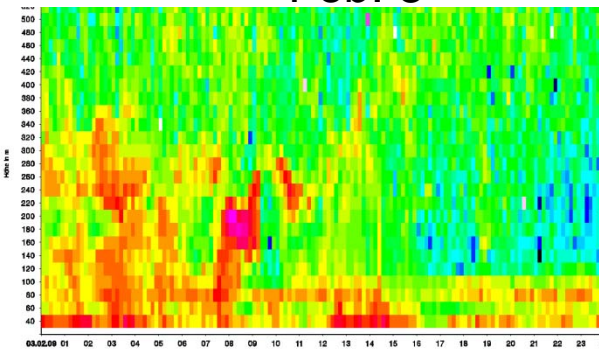
Feb. 3



Feb. 4



Feb. 5

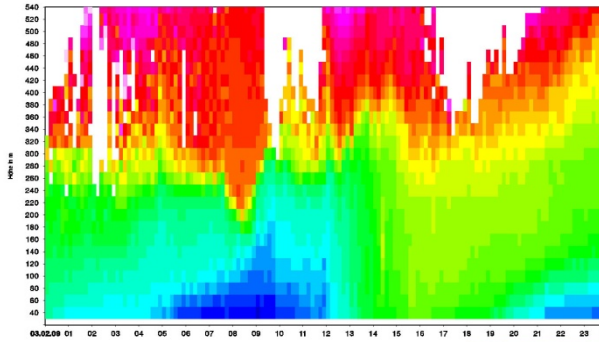




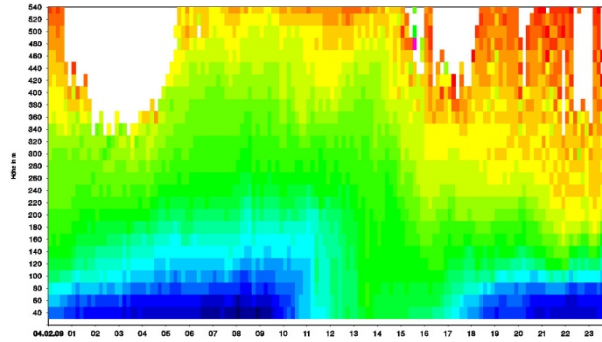
# RASS data Augsburg February 2009



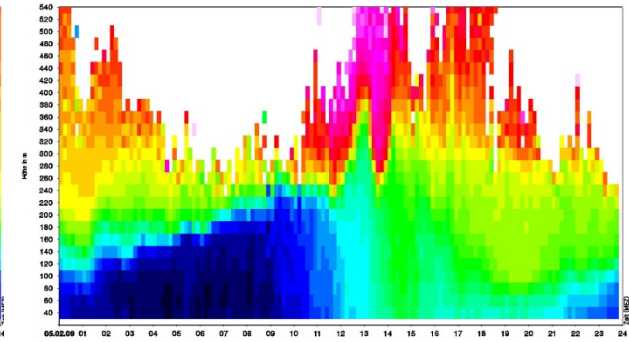
potential temperature (top), MLH RASS (middle), MHL SODAR/Ceilo (bottom)



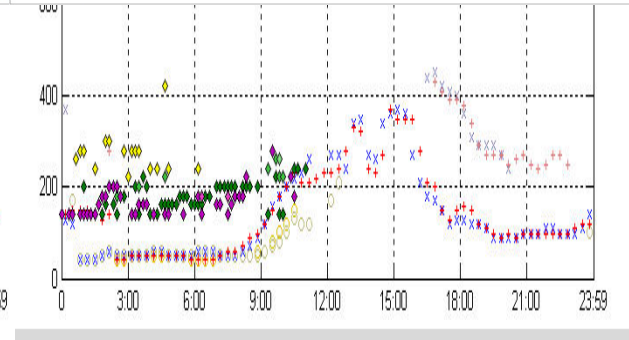
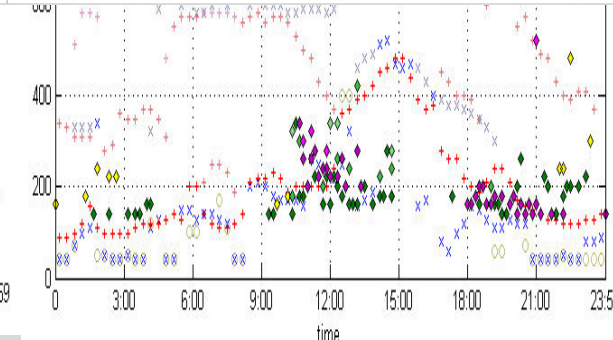
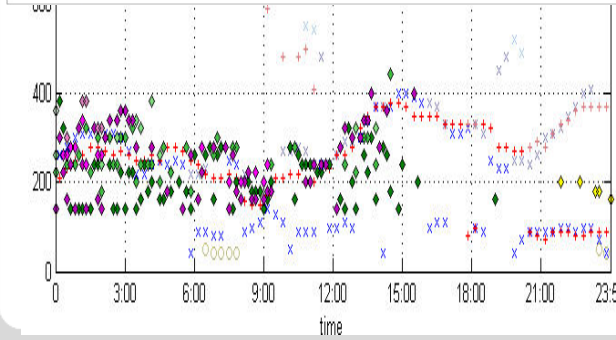
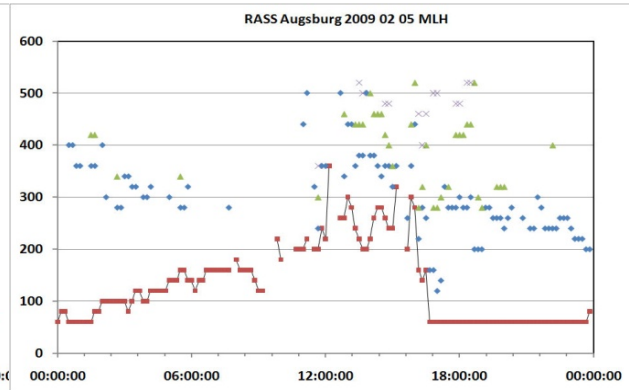
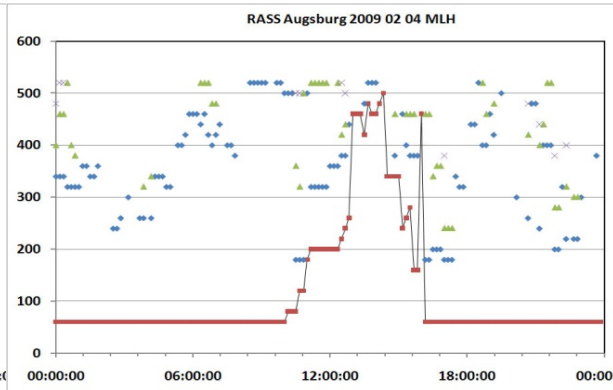
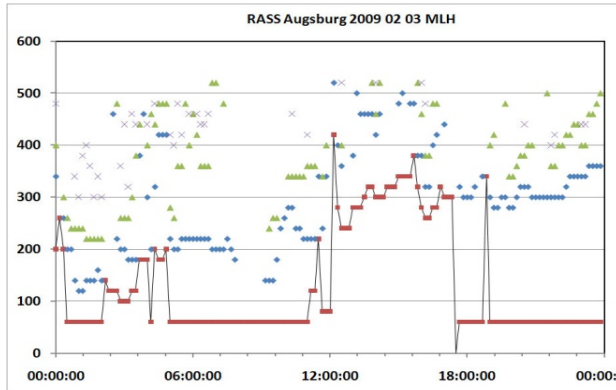
Feb. 3



Feb. 4



Feb. 5



# Summary

# Overview on methods using ground-based remote sensing for the derivation of the mixing-layer height

method	short description
acoustic ARE method	analysis of <b>acoustic received echo</b> intensity profiles
“ HWS method	analysis of <b>horizontal wind speed</b> profiles
“ VWV method	analysis of <b>vertical wind variance</b> profiles
“ <b>EARE method</b>	<b>analysis of acoustic backscatter intensity and vertical wind variance profiles (enhanced acoustic received echo method)</b>
optical threshold method	detection of a given backscatter intensity threshold
“ <b>gradient method</b>	<b>analysis of optical backscatter intensity profiles</b>
“ idealised backscatter method	analysis of optical backscatter intensity profiles
“ wavelet method	analysis of optical backscatter intensity profiles
“ variance method	analysis of optical backscatter intensity profiles
acoustic / electro-magnetic	ARE method applied to sodar and wind profiler data
acoustic / optical	EARE method plus gradient method
electro-magnetic / electro-magnetic	combination of a sodar-RASS and a wind profiler RASS: analysis of the vertical temperature profile plus analysis of the electro-magnetic backscatter intensity profile
acoustic / in situ	ARE method plus in-situ surface flux measurement

<b>RASS</b>	<b>analysis of the temperature profile from the measured speed of sound</b>
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## Conclusions:

😊😊😊💣 **RASS** directly delivers temperature profiles, MLH, inversions, and stable layers can easily be detected, wind profiles are additionally available.

Does not work properly under high wind speeds. Restricted range.

😊😊💣💣 **Ceilometer** detects aerosol distribution and water droplets. It has to be assumed that the aerosol follows the thermal structure of the atmosphere. Inversions and MLH can indirectly be inferred with a MLH algorithm.

Does not work properly in extreme clear (aerosol-free) air and during precipitation events and fog.

😊💣💣💣 **SODAR** detects temperature fluctuations and gradients, but no absolute temperature. Inversions and stable layers can indirectly be inferred with a MLH algorithm.

Does not work properly under perfectly neutral stratification, with very high wind speeds, and during stronger precipitation events. Restricted range.

# Literature

## SODAR:

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**Thank you very  
much for your  
attention**

