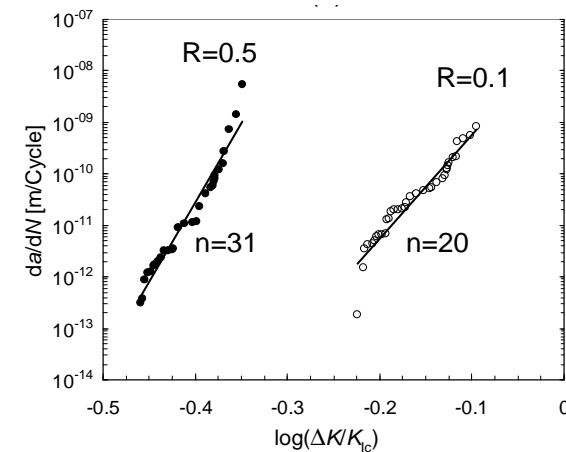
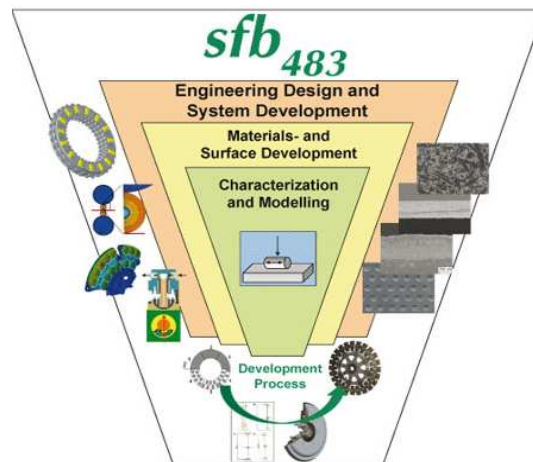


Statistical analysis of fatigue crack propagation for natural flaws in silicon nitride

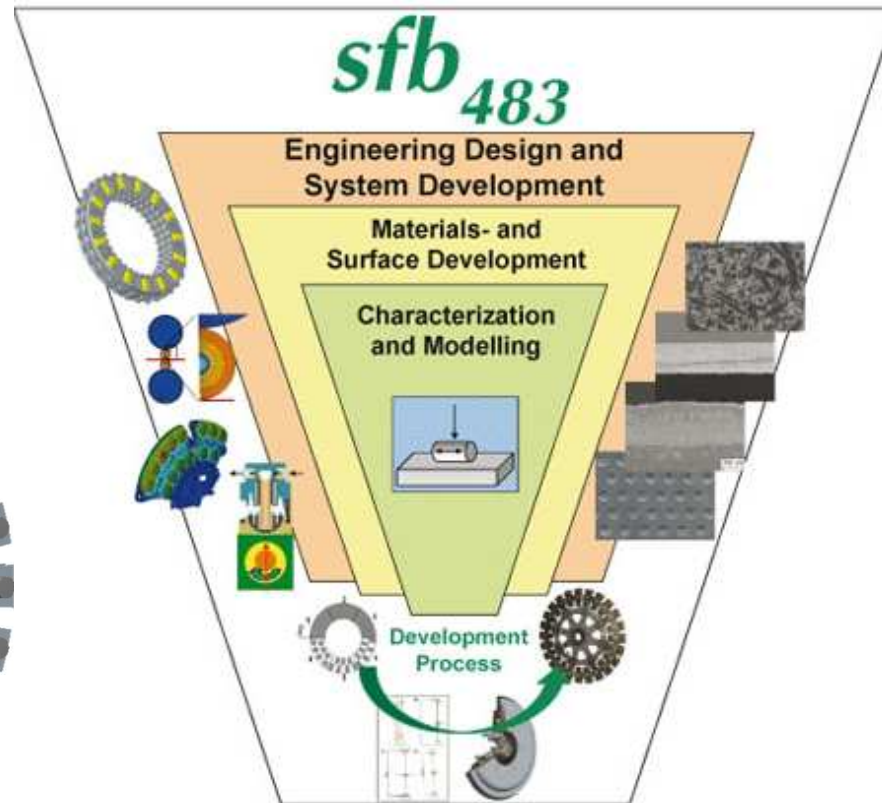
M. Härtelt*, H. Riesch-Oppermann*, J.J. Kruzic**, O. Kraft*

* Karlsruhe Institute of Technology (KIT), Institute of Applied Materials (IAM)

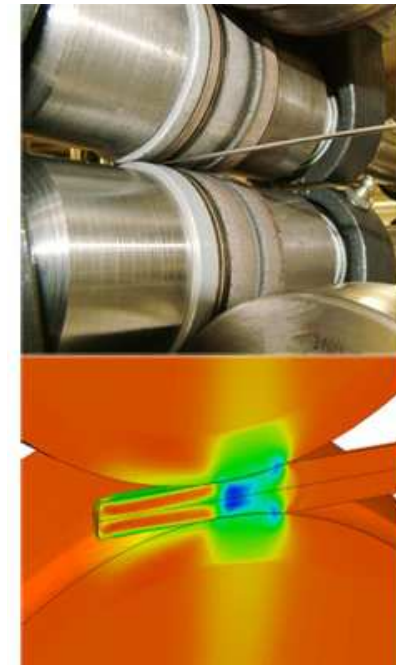
**Oregon State University, School of Mechanical, Industrial, and Manufacturing Engineering



Motivation



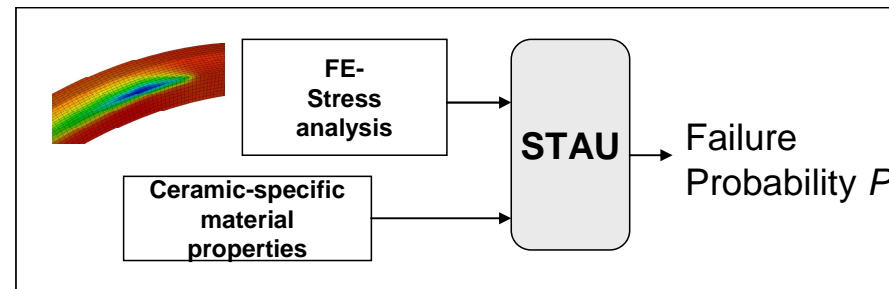
Wire rolling



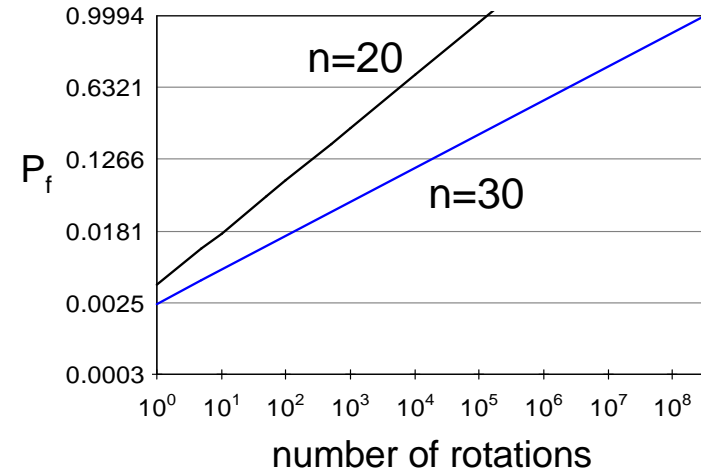
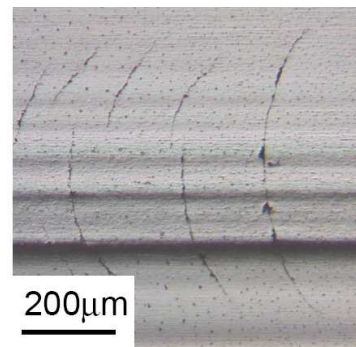
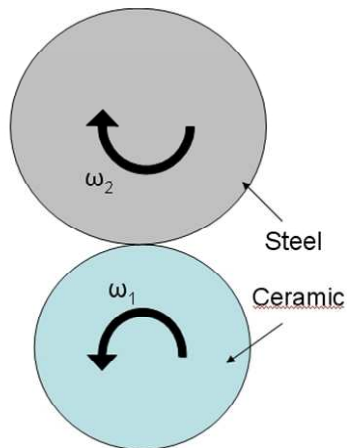
www.sfb483.kit.edu

Motivation

- Predicting component reliability based on natural flaws



- Example: Rolling contact fatigue test



- Predictions are strongly affected by the crack growth exponent

Motivation

Scope of this talk

- Obtain more information on crack propagation behaviour of natural flaws in ceramics
- Reduce uncertainties in the parameters

Overview

- Calculation of crack growth curves
- Example: Si_3N_4
- Pooling procedure
- Fracture mechanics model

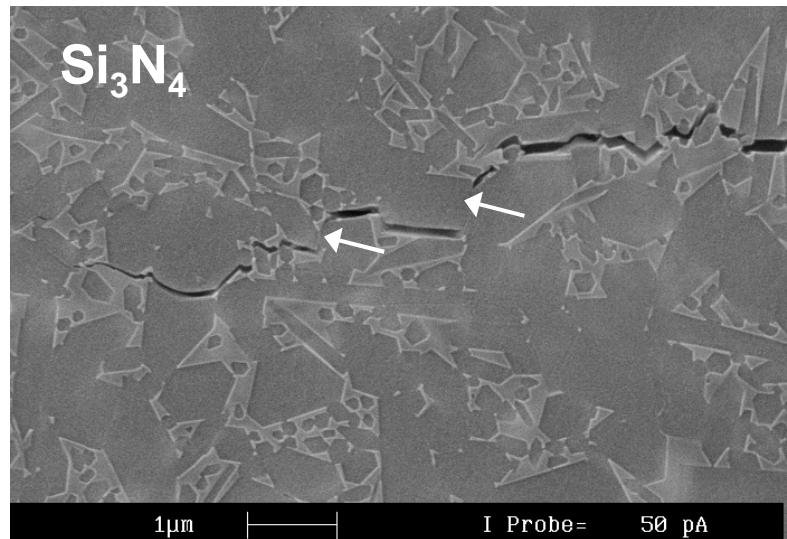
Slow crack propagation in ceramics

Subcritical crack propagation

- Quasi-static effect

$$\frac{da}{dt} = A_S \cdot \left(\frac{K_I}{K_{Ic}} \right)^{n_S}$$

A_S, n_S : material properties



Cyclic crack propagation

- Degradation of strengthening effects (grain bridging)

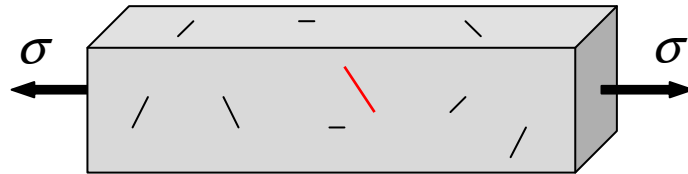
$$\frac{da}{dN} = A \cdot \left(\frac{\Delta K_I}{K_{Ic}} \right)^n$$

A, n : material properties, may depend on the load ratio R

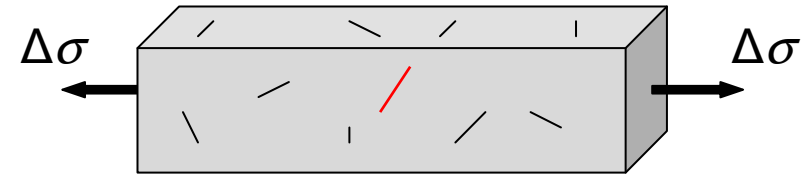
Image: S. Fünfschilling (KIT)

Crack propagation curves

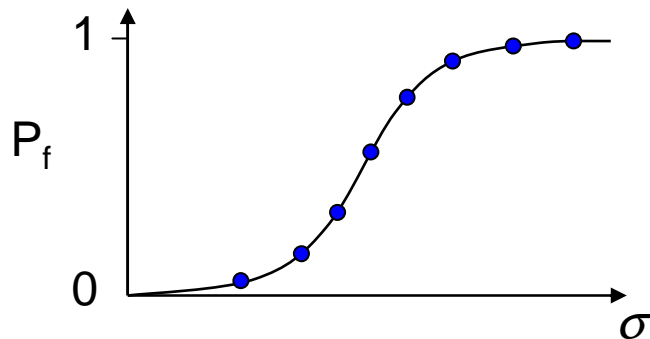
Strength tests



Lifetime test
(cyclic load amplitude $\Delta\sigma$)

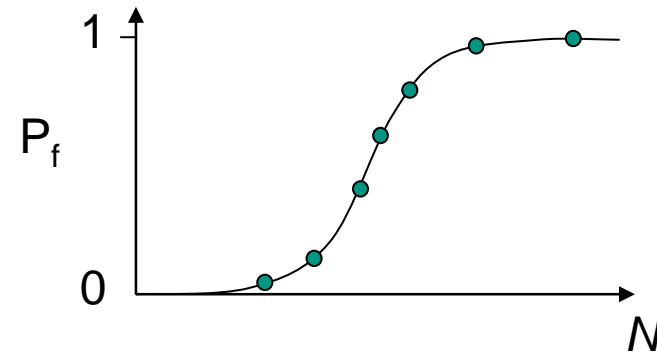


fracture stress distribution



flaw size distribution
↔

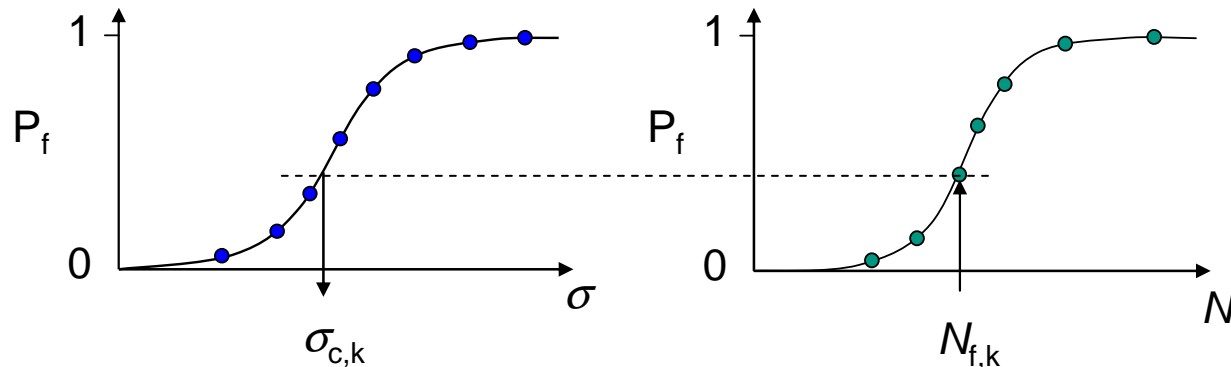
lifetime distribution



- Fracture governed by critical flaw
- Strength and lifetime distribution related by flaw size distribution
→ Statistical procedure

Crack propagation curves

- Indirect method for calculating crack growth curves (Fett et al.¹)

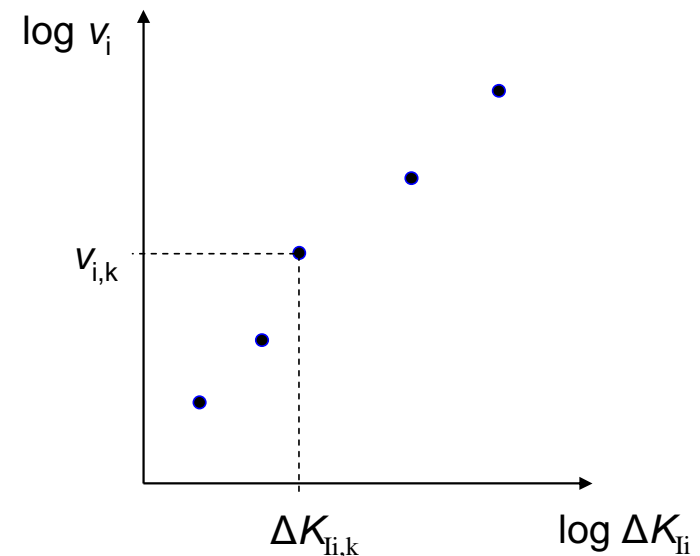


- Each lifetime $N_{f,k}$ is assigned to a strength $\sigma_{c,k}$
- initial crack propagation rate $v_{i,k}$:

$$v_i = \frac{2\Delta K_i^2}{N_f \Delta \sigma^2 Y^2} \cdot \frac{d \log(\Delta K_i)}{d \log(\Delta \sigma^2 N_f Y^2)}$$

$$\Delta K_{Ii} = \Delta \sigma Y_I \sqrt{a_i}$$

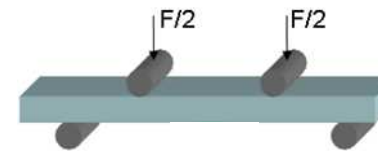
ΔK_{Ii} – initial stress intensity range



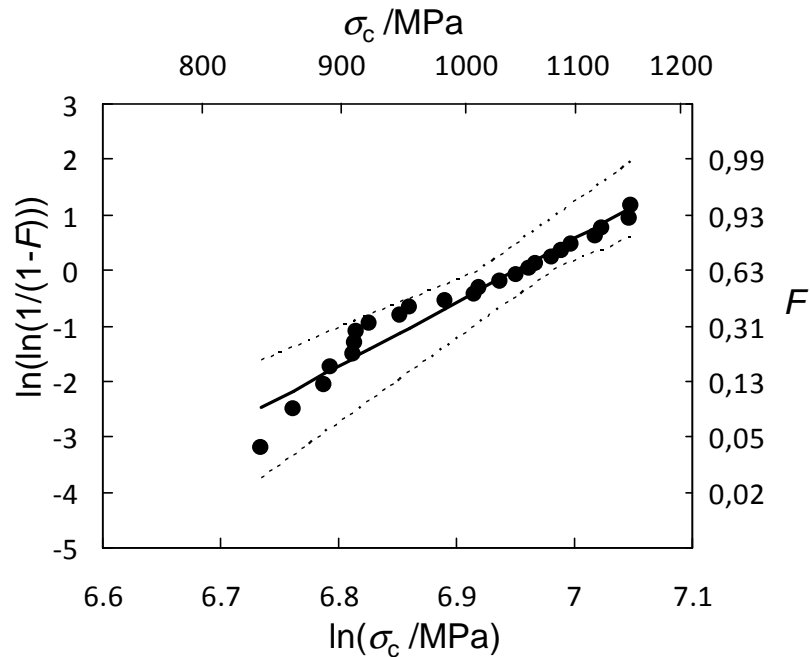
¹ T. Fett et al., *J. Mater. Sci.*, 26 (12) 3320–3328 (1991).

Si₃N₄ – SL200

- Commercial powder: 3% Y₂O₃ and 3% Al₂O₃
- 4-point-bending setup (static and cyclic test)

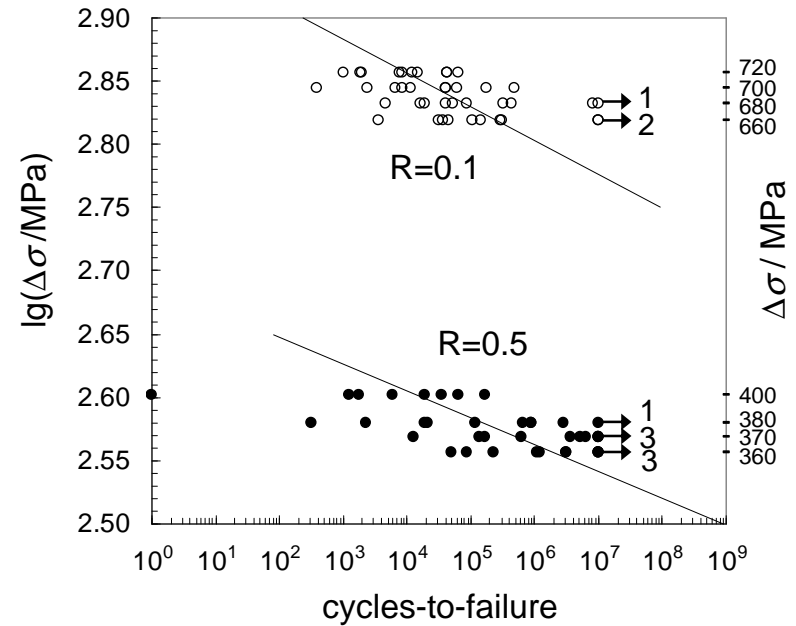


Strength distribution



$m=12; \sigma_0=1044 \text{ MPa}$

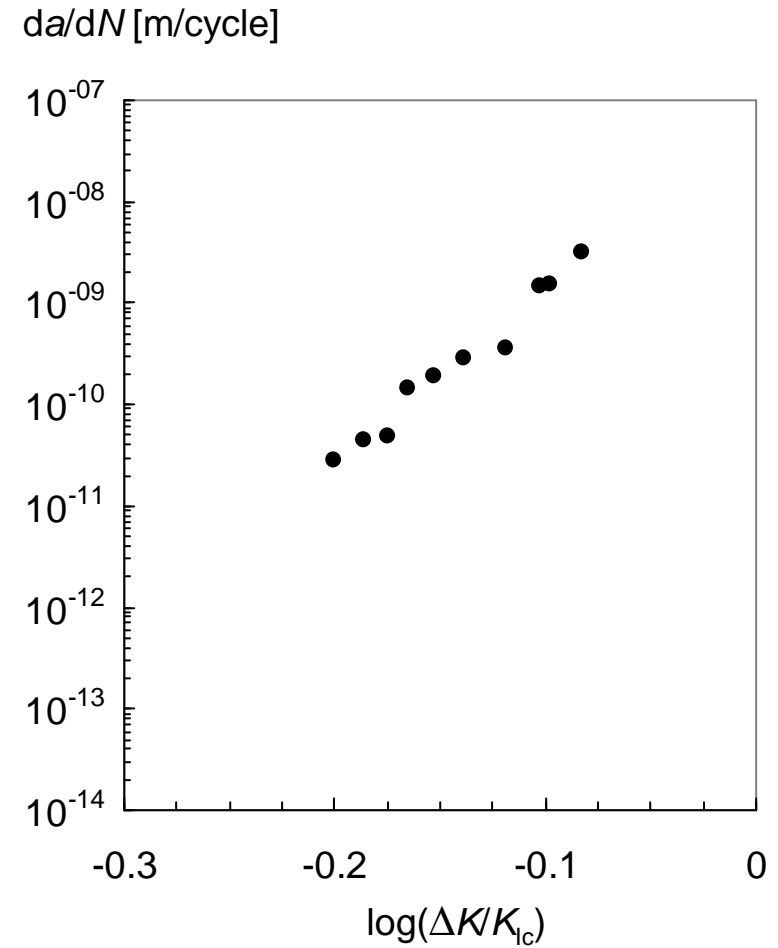
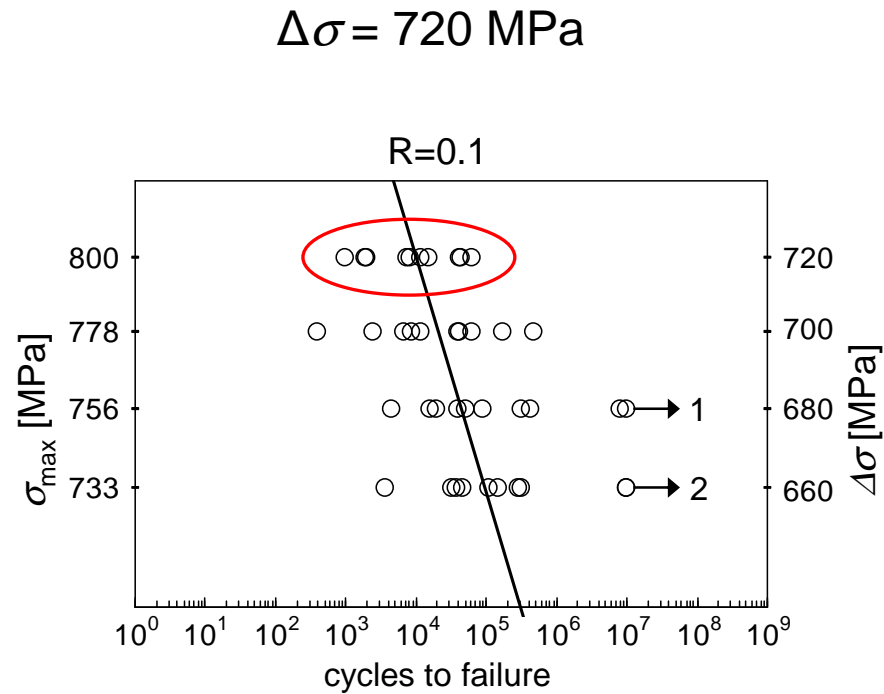
S-N-curve in ambient air



Experiments: T. Schwind et al., *Int. J. Mat. Res.*, 99, 1090–1097, 2008

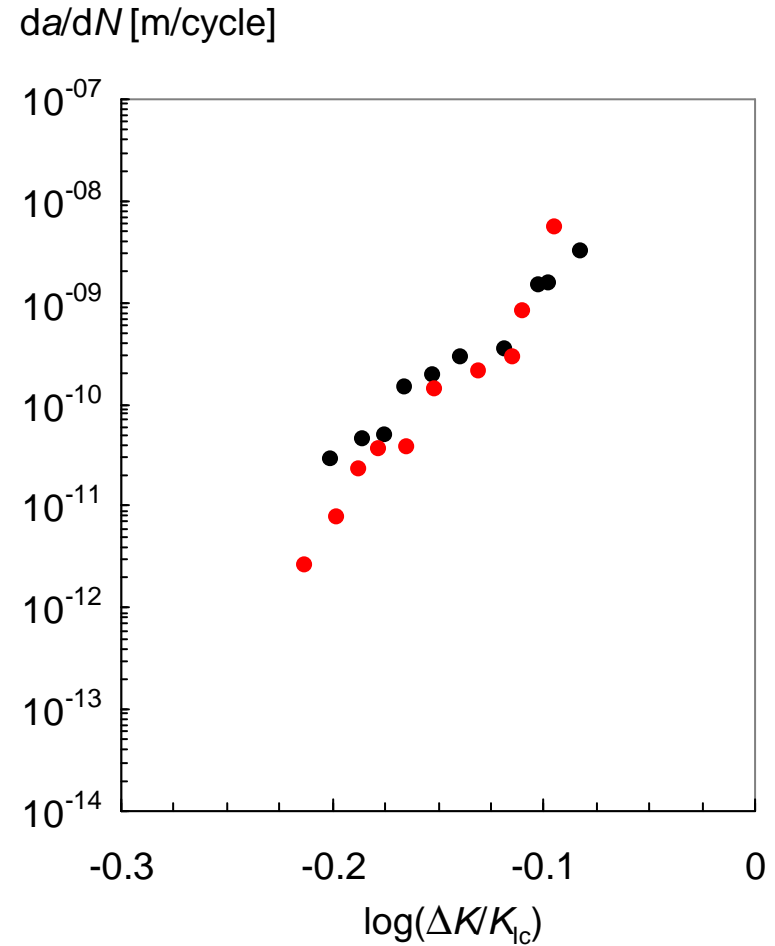
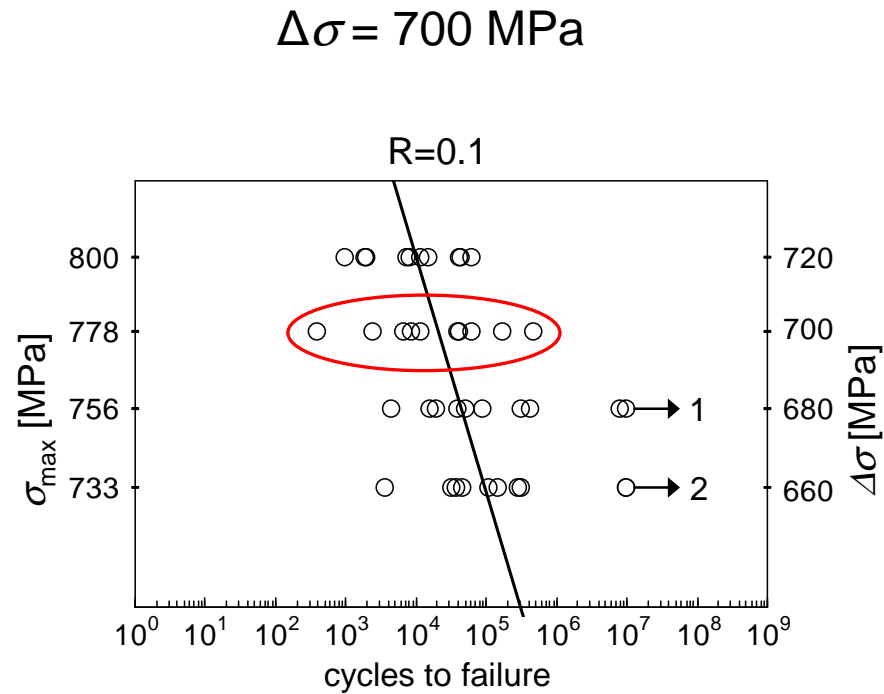
Crack growth curve R=0.1

- Separate evaluation for each load level $\Delta\sigma$



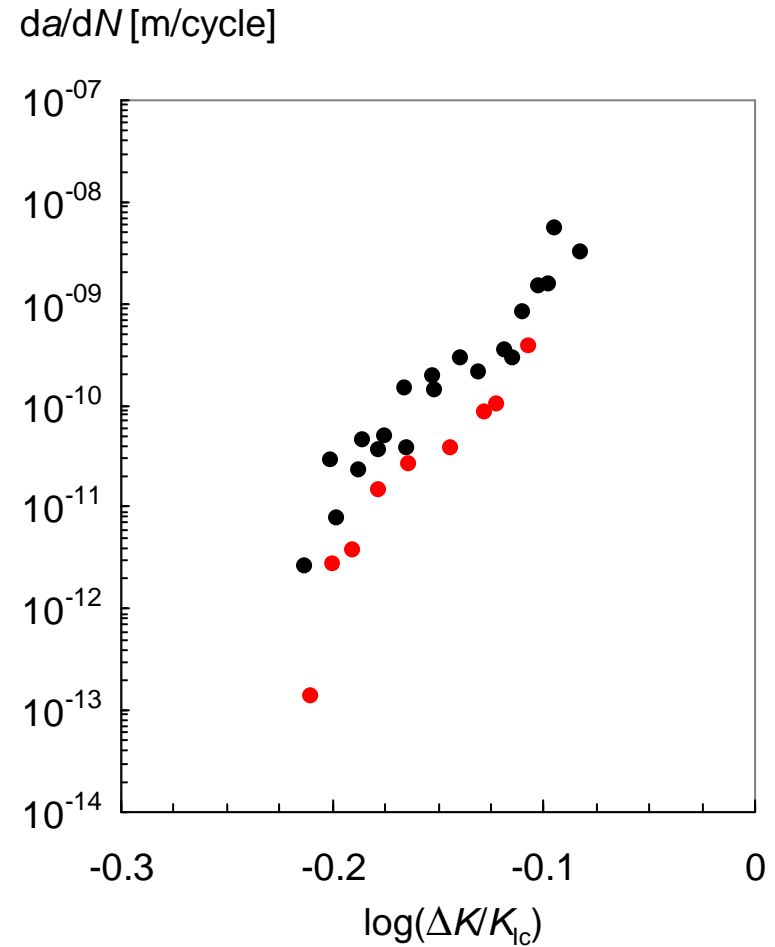
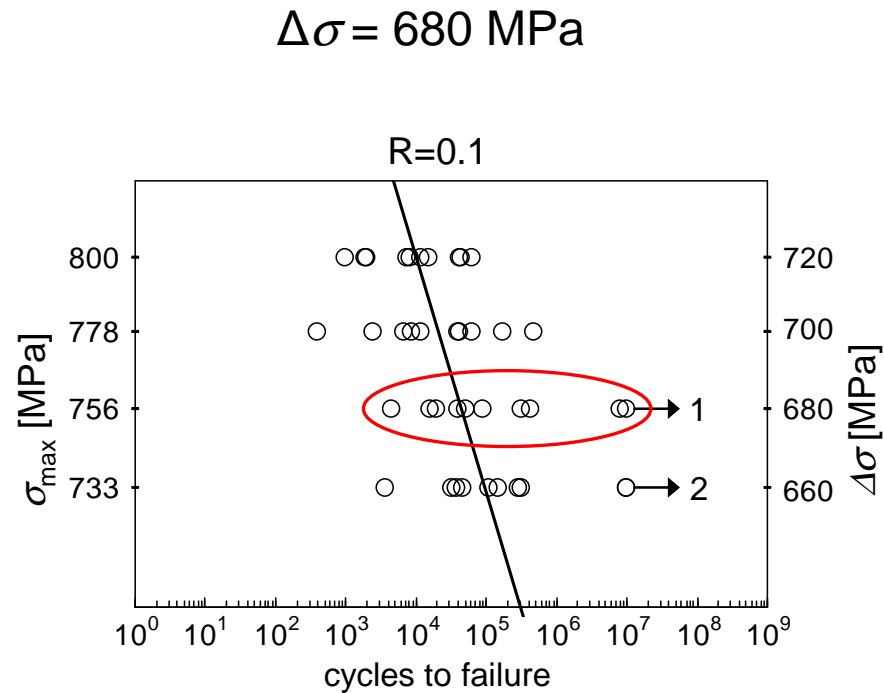
Crack growth curve R=0.1

- Separate evaluation for each load level $\Delta\sigma$



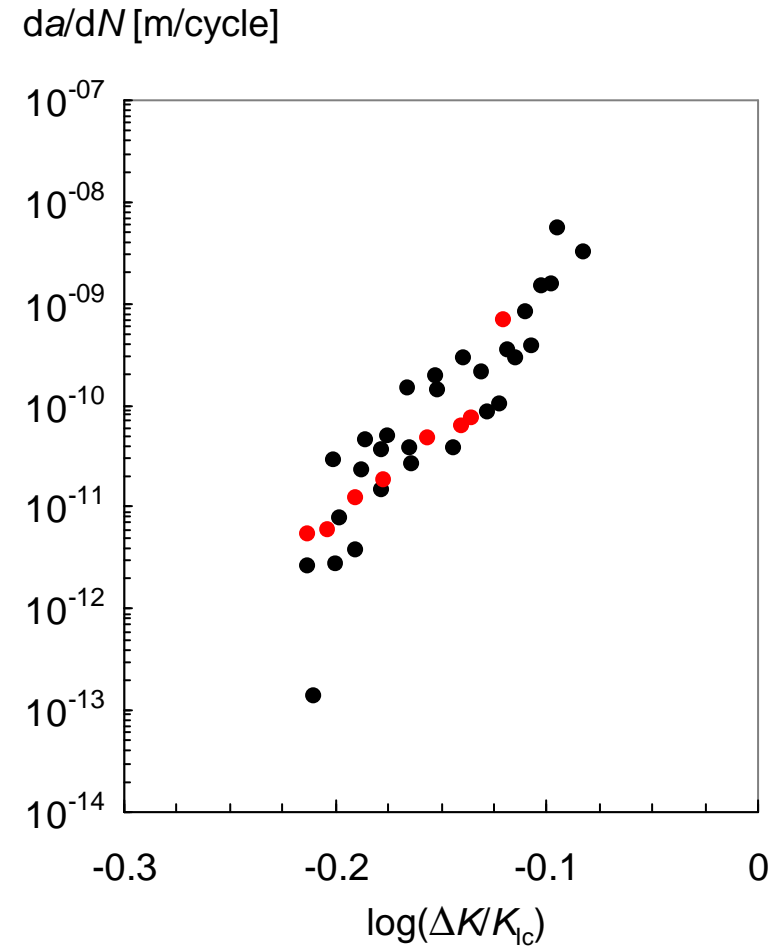
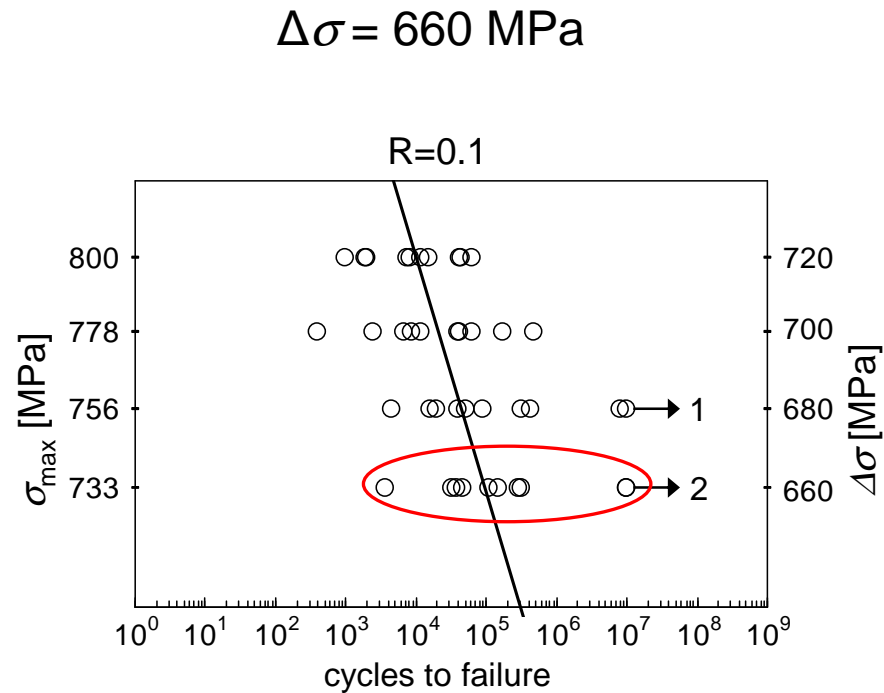
Crack growth curve R=0.1

- Separate evaluation for each load level $\Delta\sigma$

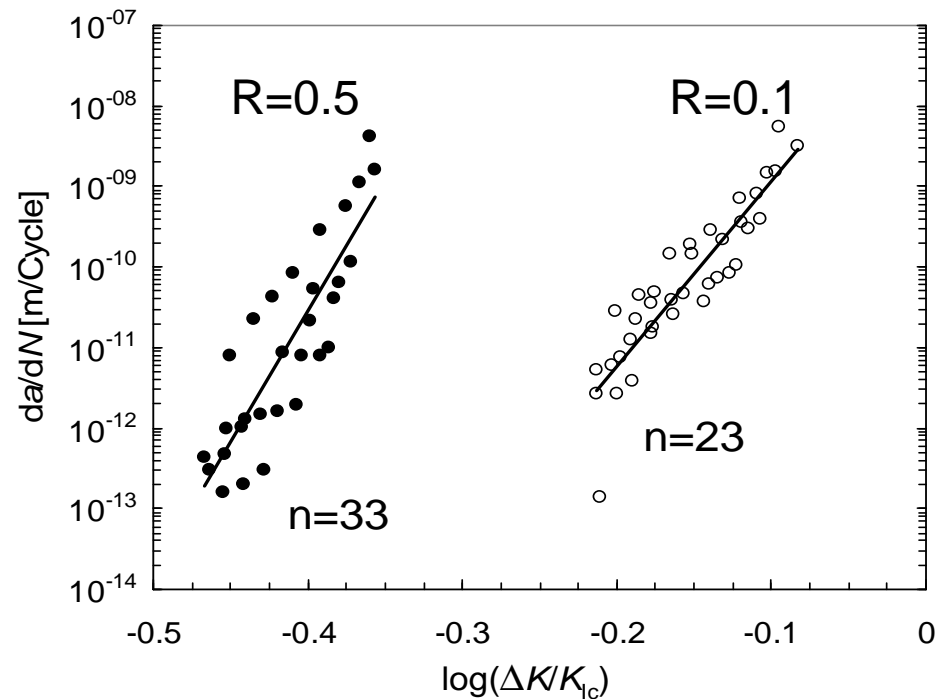


Crack growth curve R=0.1

- Separate evaluation for each load level $\Delta\sigma$



Crack growth curves



■ power-law fit:

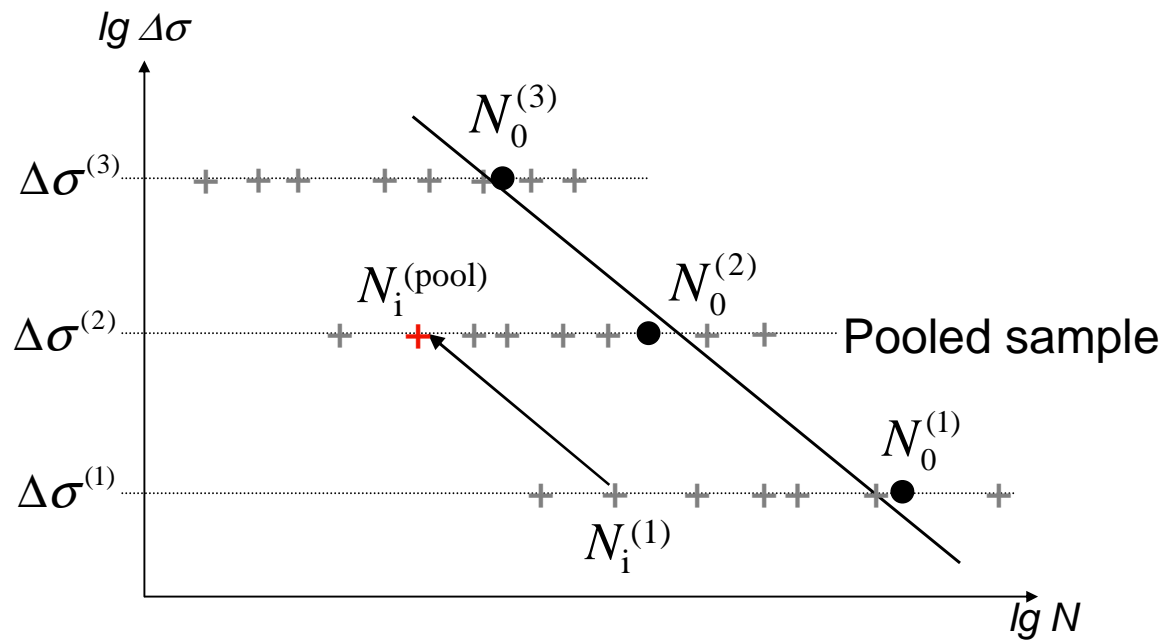
$$\frac{da}{dN} = A \cdot \left(\frac{\Delta K_I}{K_{Ic}} \right)^n$$

- Crack growth exponent n depends on the load ratio R
- Scatter in data caused by sparse database available for each $\Delta\sigma$
 - Uncertainty in the parameters

M. Härtelt et al., J.Am.Ceram.Soc., (2011), in press

Pooling procedure

- Increase number of data available for one load level



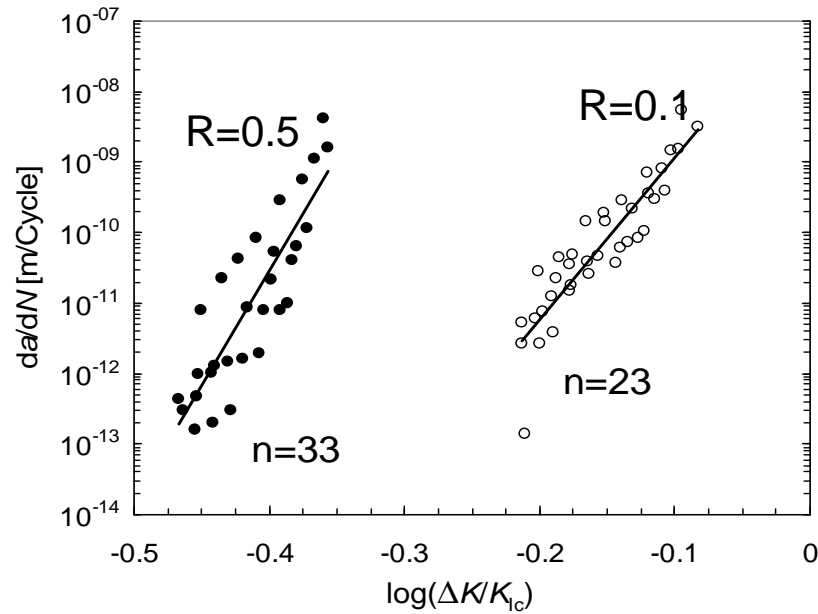
- Conversion using Weibull-distribution:

$$N_i^{(pool)} = N_i^{(1)} \left(\frac{N_0^{(pool)}}{N_0^{(1)}} \right)$$

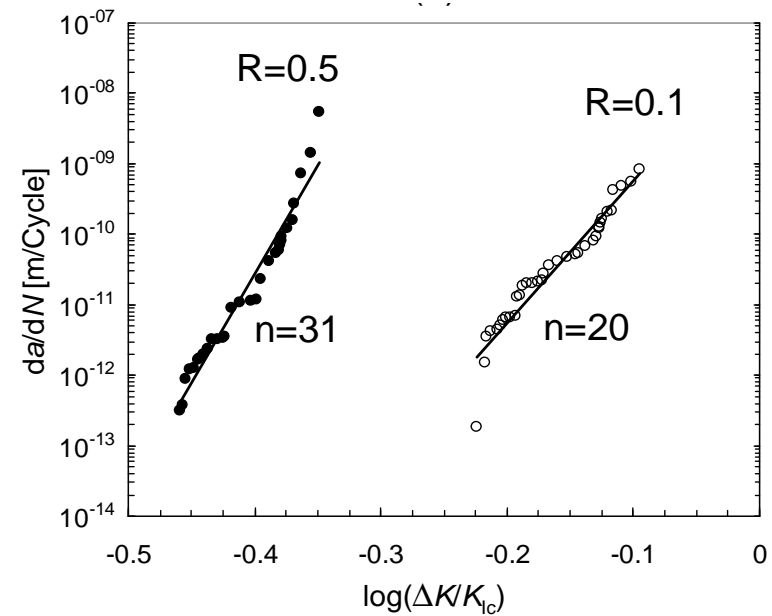
- Relation between $\Delta\sigma$ and N_0 follows from S-N-curve fit

Pooled crack growth curves

unpooled



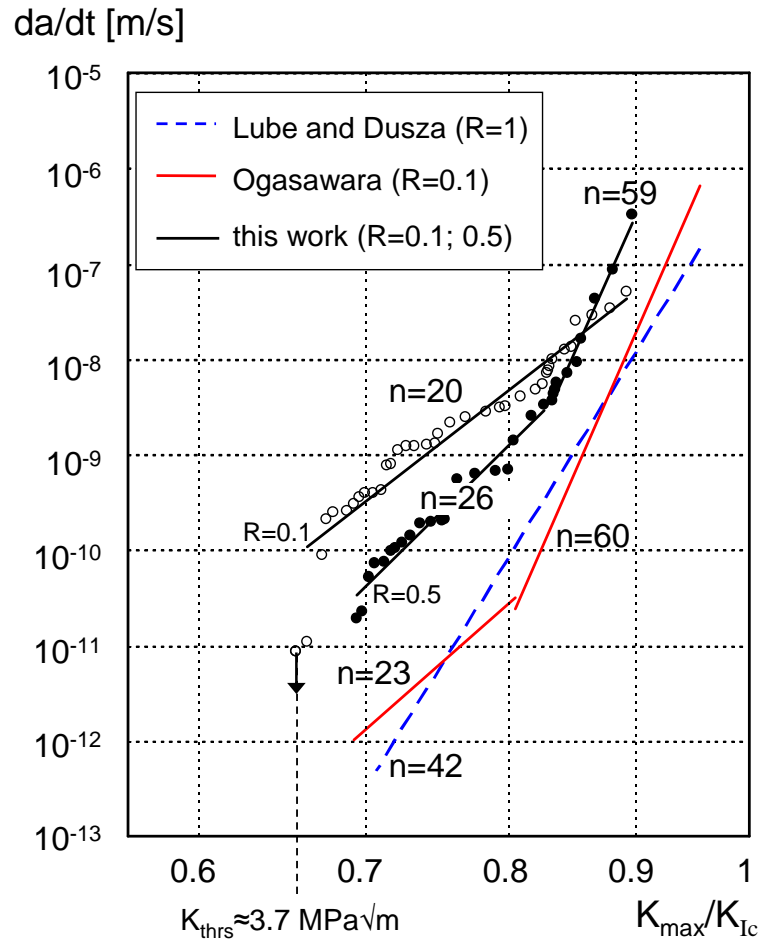
pooled



- Scatter (uncertainty in n) is decreased by pooling
- variation of n with R remains

M. Härtelt et al., J.Am.Ceram.Soc., (2011), in press

Pooled crack growth curves



- Pooling allows for better comparison with other data from natural flaws
- Bi-modal shape for R=0.5

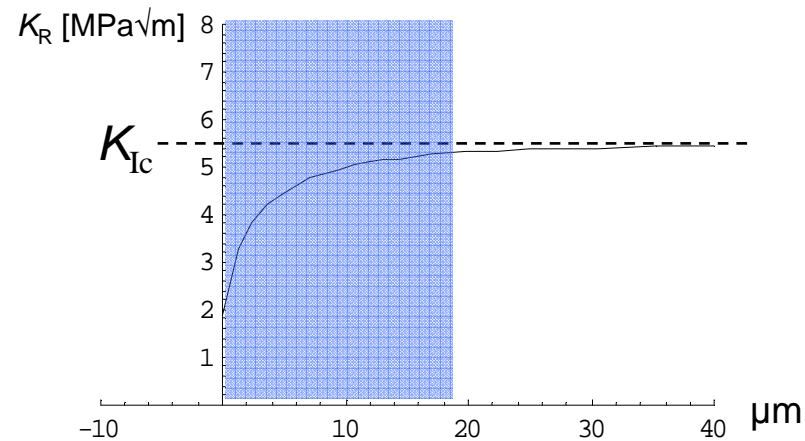
M. Härtelt et al., J.Am.Ceram.Soc., (2011), in press

Ogasawara et al., J.Am.Ceram.Soc. 77[2] 514 (1994)

Lube and Dusza, J.Eur.Ceram.Soc. 27[2-3] 1203 (2007)

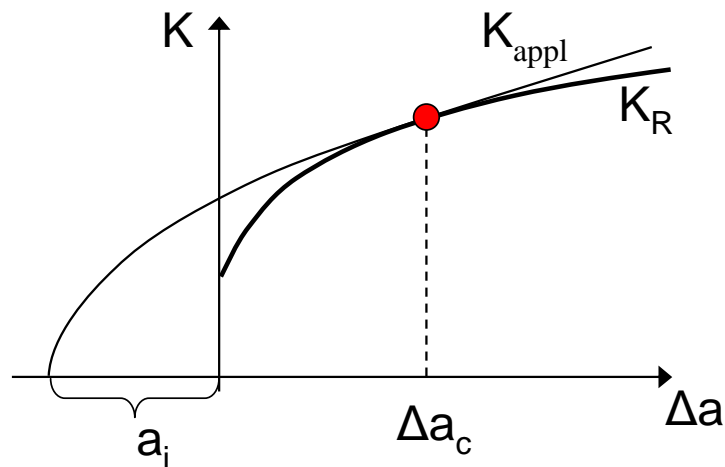
Fracture mechanics model: R-curve

- $\Delta K_{II} = \Delta \sigma Y_I \sqrt{a_i} \rightarrow a_i$ from strength measurement



- Steeply rising R-curve¹ affects failure criterion used for natural flaws

- Calculation of ΔK_{II} : R-curve behaviour

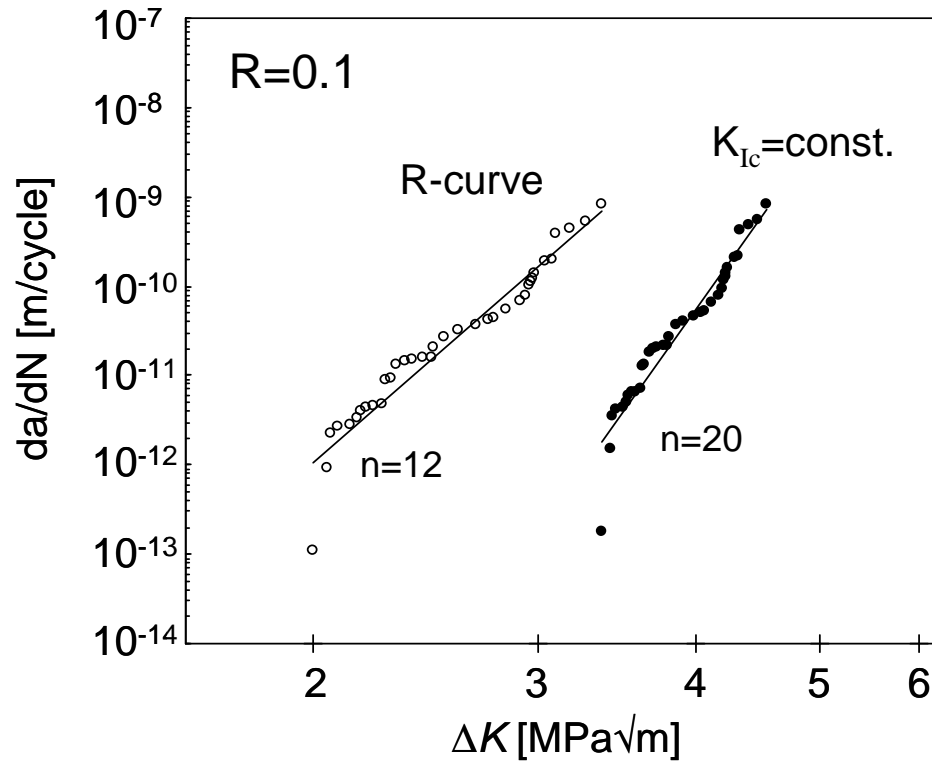


$$\Delta K_{II} = \Delta \sigma Y_I \sqrt{a_i}$$

a_i : initial flaw size from tangent criterion

[1] T. Fett et al., J.Am.Ceram.Soc. 91[11]:3638 (2008)

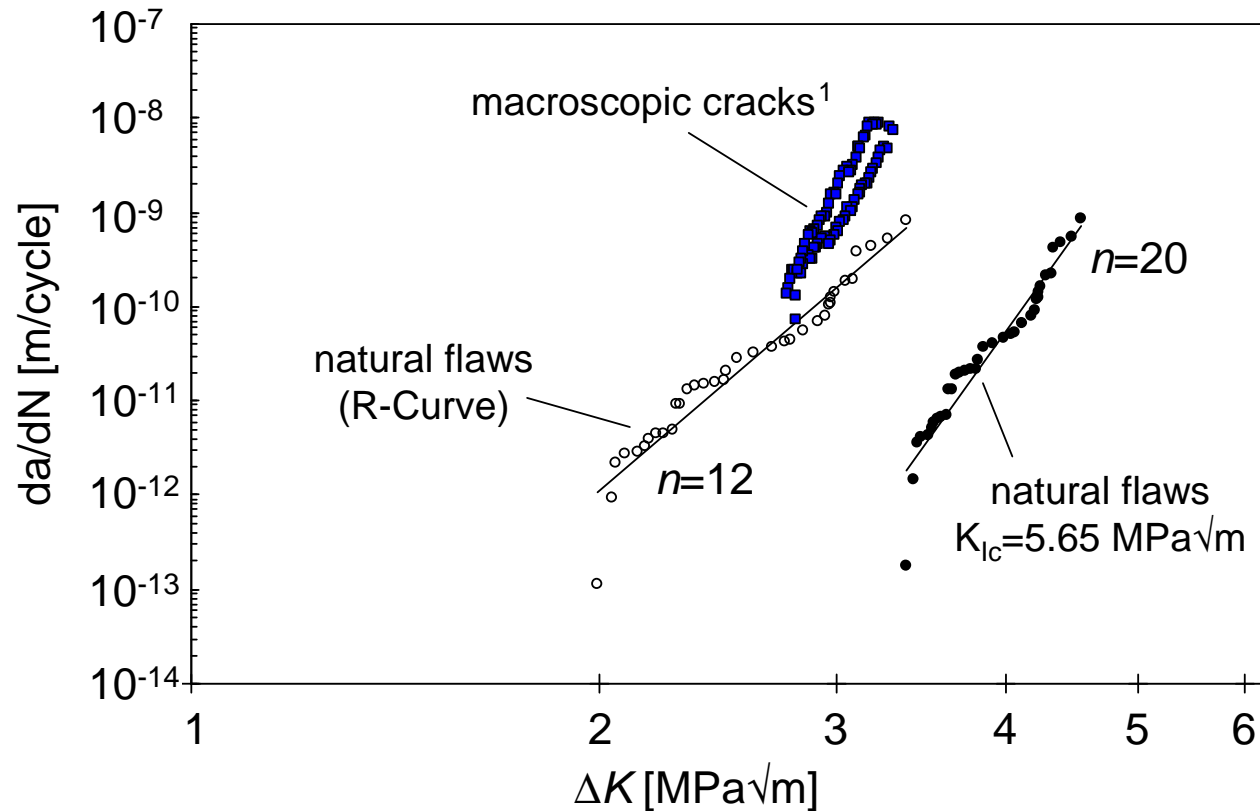
R-curve influence



$$K_{Ic} = 5.65 \text{ MPa}\sqrt{m}$$

- R-curve: ΔK_{Ii} -values decrease \rightarrow shift of crack growth curve
- Crack growth exponent decreases \rightarrow shape of R-curve

R-curve influence



¹ experiments: J. Kruzic

- Better agreement with crack growth curves from macroscopic cracks obtained for the same material

Summary

- Statistical evaluation of crack growth curves for natural flaws
- Indirect method combining strength and lifetime tests

Si₃N₄-SL200:

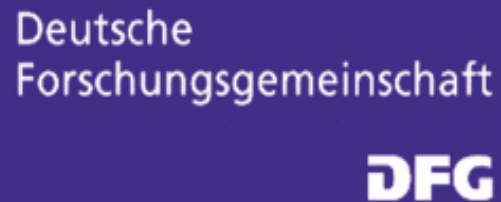
- Sparse lifetime database → Uncertainty in the estimated parameters
- Pooling:
 - reduce scatter in the crack growth curves by combining measurements from different load levels $\Delta\sigma$.
 - gives better insight in the fatigue mechanism
- Consideration of R-curve
 - allows for comparison with data from macroscopic cracks
 - gives more realistic crack growth data

Acknowledgements

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Dr. Thomas Schwind



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