

# On wind speed reductions within and wake lengths behind wind parks – an analytical model

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**Wind energy generation is based on momentum (energy) extraction from the air**

**momentum extraction decelerates the wind**

**→ wind park efficiency depends on the equilibrium wind speed in the interior of the park**

**- equilibrium between extraction and re-supply of momentum**

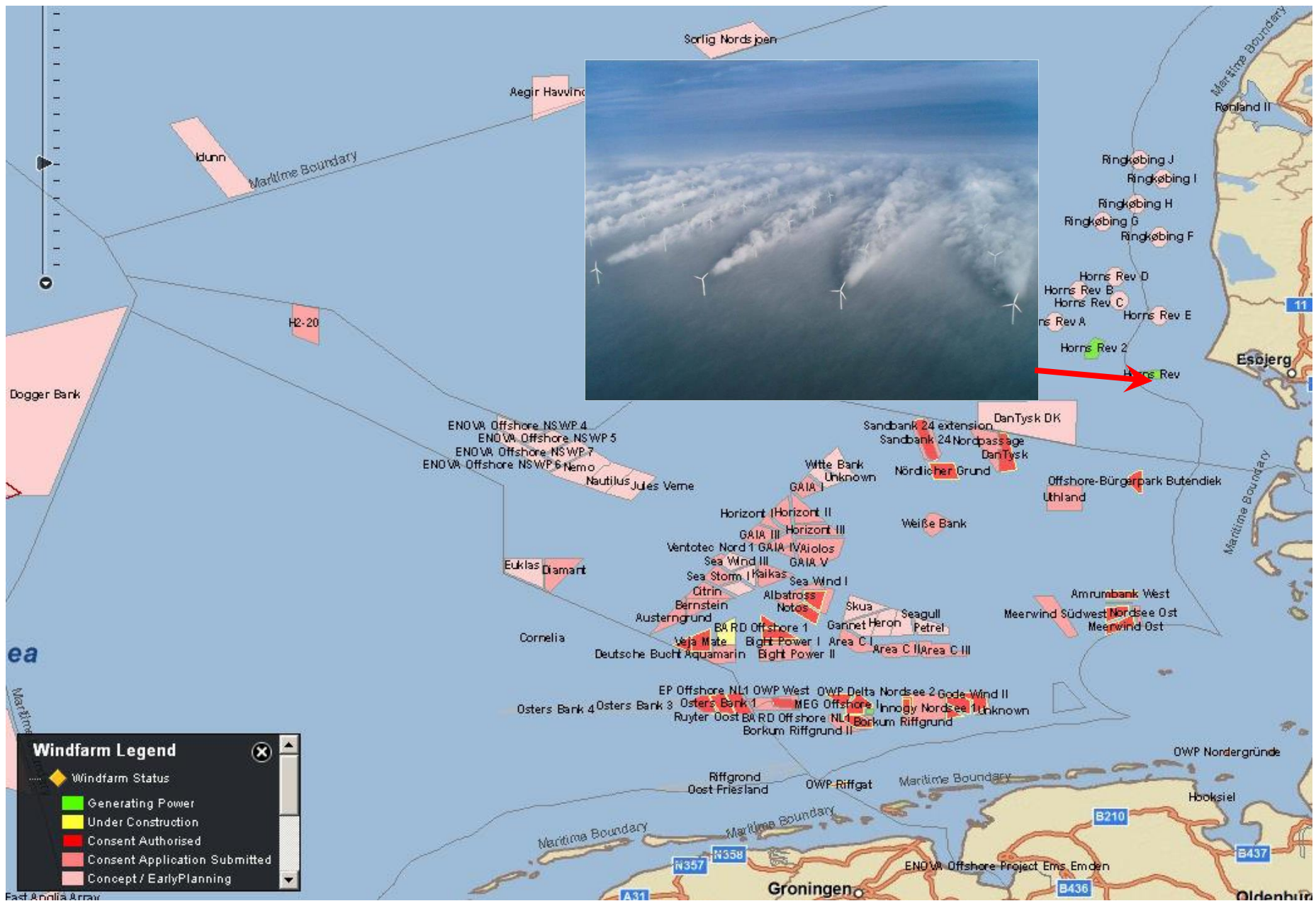
**→ wind park wakes influence other wind parks downstream**

**- wake length is inversely proportional to the momentum re-supply**

**→ for wind park design it is important to know:**

**a) the magnitude of wind speed reduction in the park interior**

**b) the length of wakes**



source: <http://www.4coffshore.com/offshorewind/>

## basic idea of the analytical model

a) reduction of wind speed in the park interior (calculation of the equilibrium condition for the momentum fluxes)

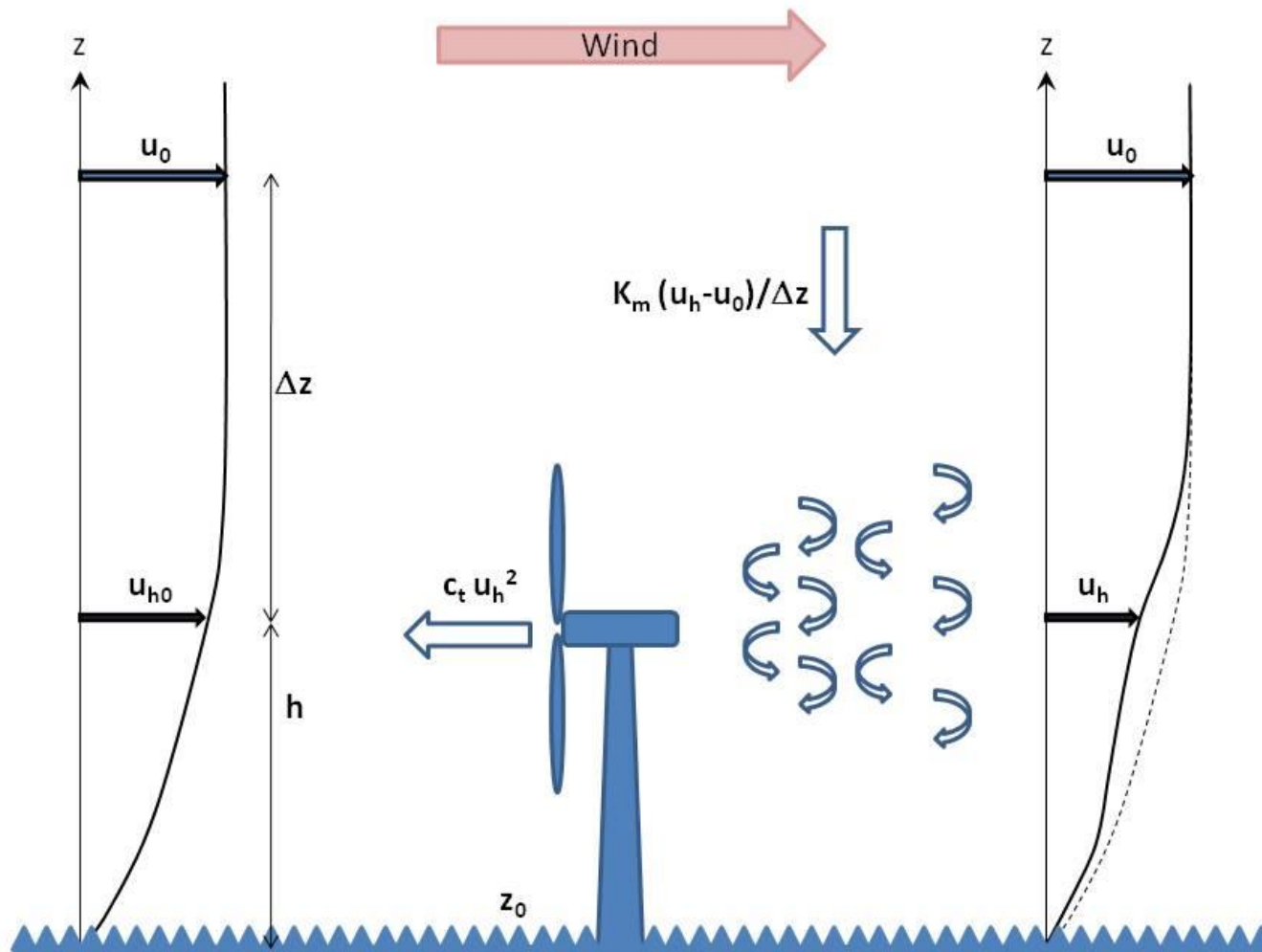
$$C_{teff} u_h^2 = \frac{\kappa u_* z (u_0 - u_h)}{\Delta z \phi_m}$$

extraction = re-supply from above

turbine  
and surface  
drag

flux-gradient-relationship

Emeis, S., 2010: A simple analytical wind park model considering atmospheric stability. *Wind Energy*, 13, 459-469.



# solution of the analytical model

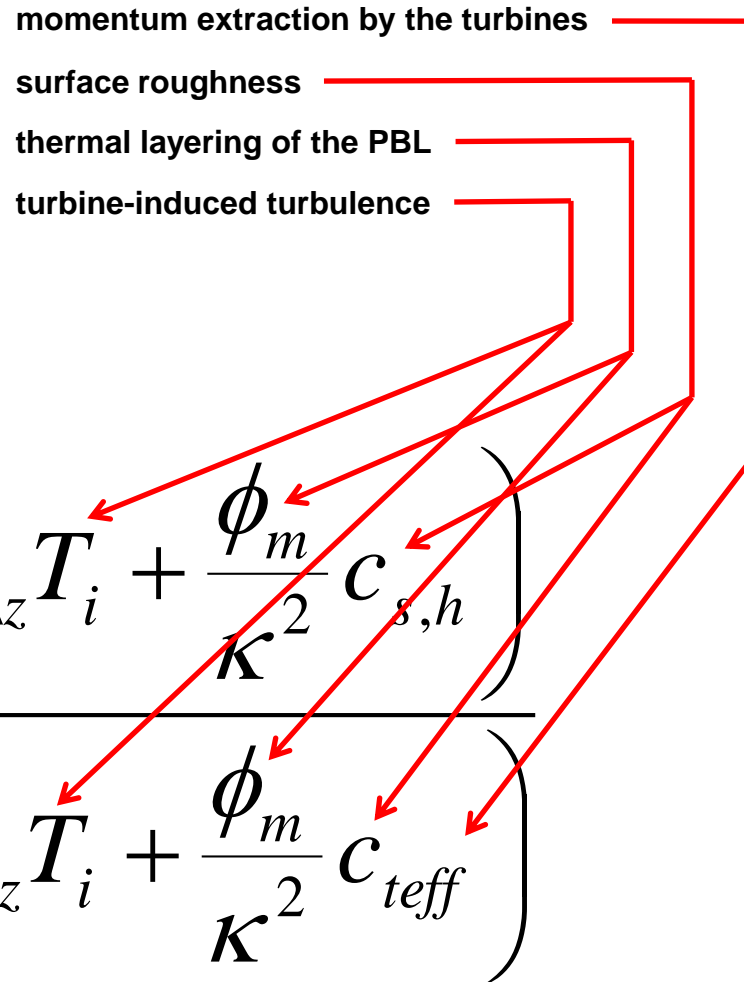
a) reduction of wind speed in the park interior (calculation of the equilibrium condition for the momentum fluxes) :

momentum extraction by the turbines

surface roughness

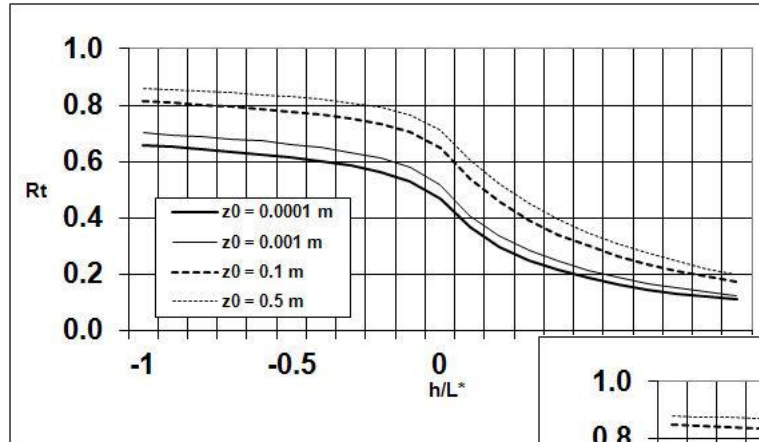
thermal layering of the PBL

turbine-induced turbulence

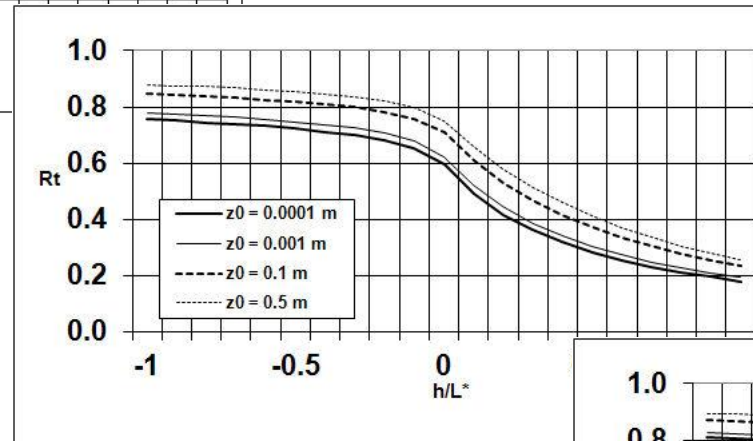
$$R_t = \frac{\left( f_{h,\Delta z} T_i + \frac{\phi_m}{\kappa^2} c_{s,h} \right)}{\left( f_{h,\Delta z} T_i + \frac{\phi_m}{\kappa^2} c_{teff} \right)}$$


# a) reduction of wind speed in the park interior

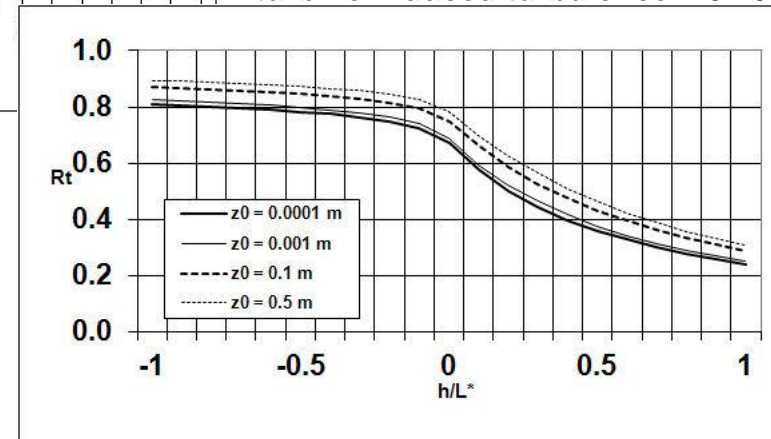
turbine-induced turbulence = 0.00



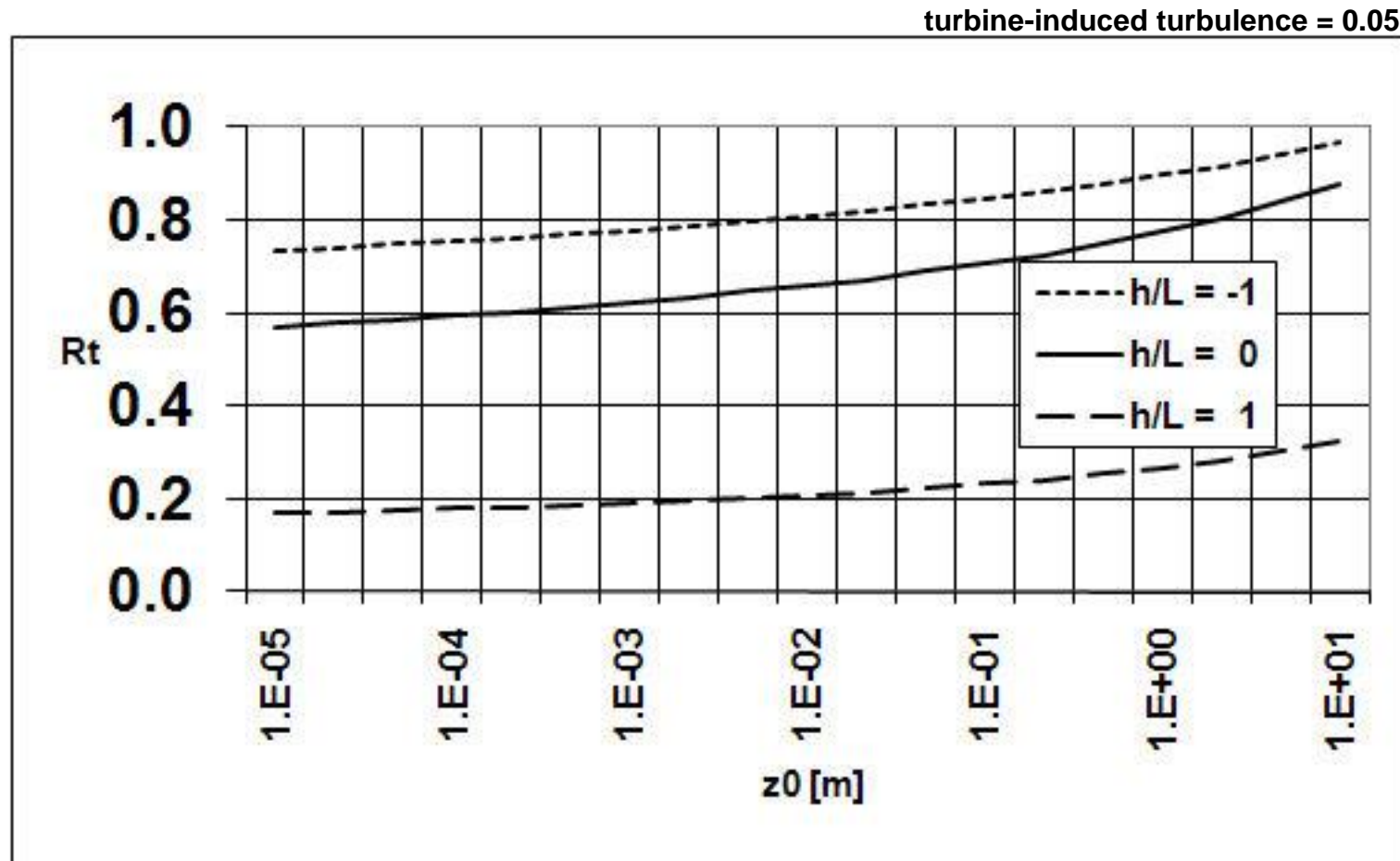
turbine-induced turbulence = 0.05



turbine-induced turbulence = 0.10

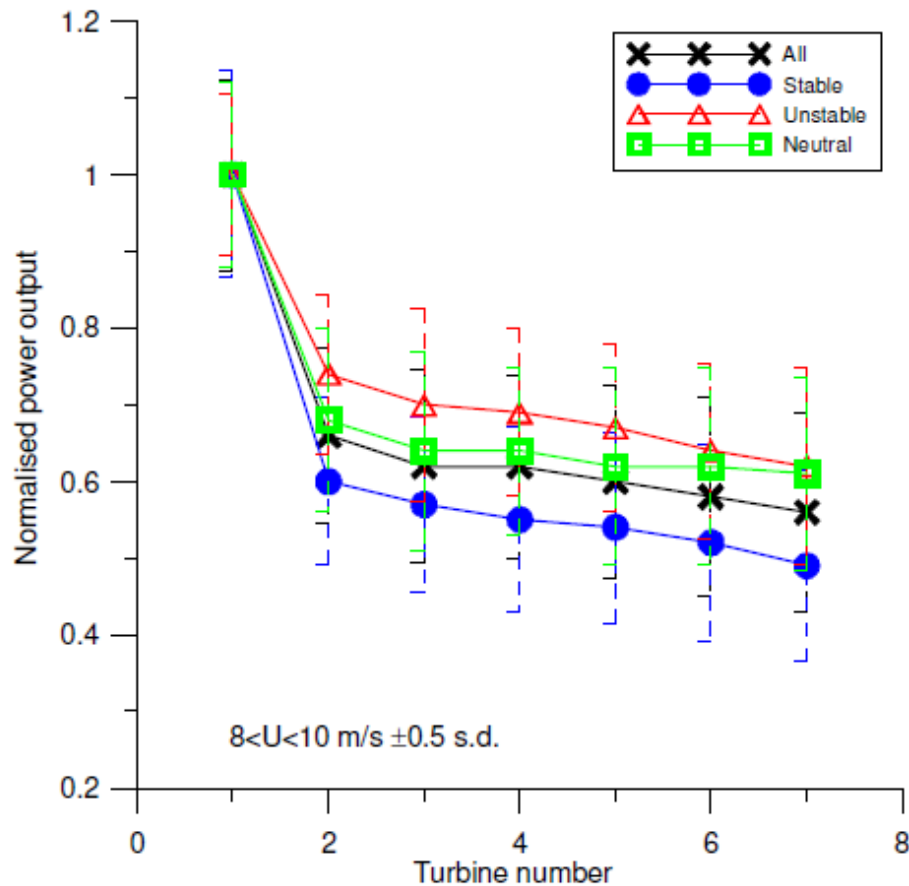


# a) reduction of wind speed in the park interior





## a) reduction of wind speed in the park interior measurements at Nysted wind park (Baltic sea)



Barthelmie R, Frandsen ST, Rethore PE, Jensen L., 2007:  
Analysis of atmospheric impacts on the development  
of wind turbine wakes at the Nysted wind farm.  
Proceedings of the European Offshore Wind Conference,  
Berlin 4.-6.12.2007.

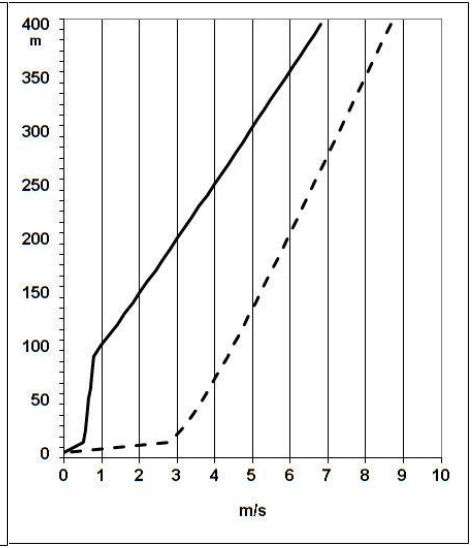
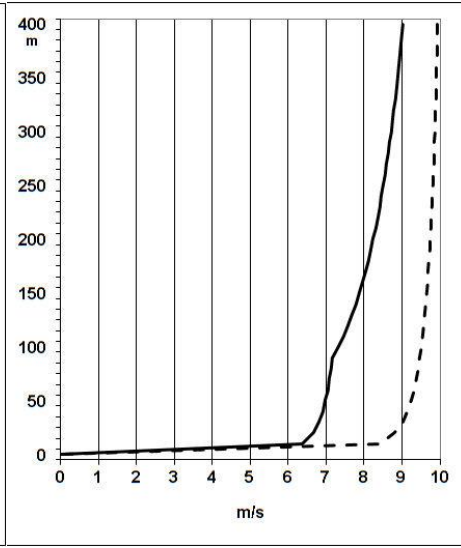
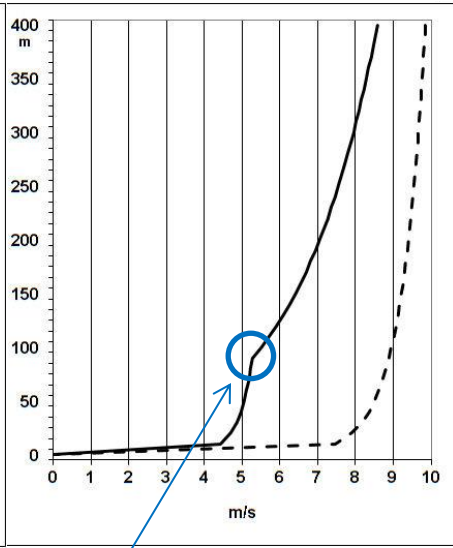
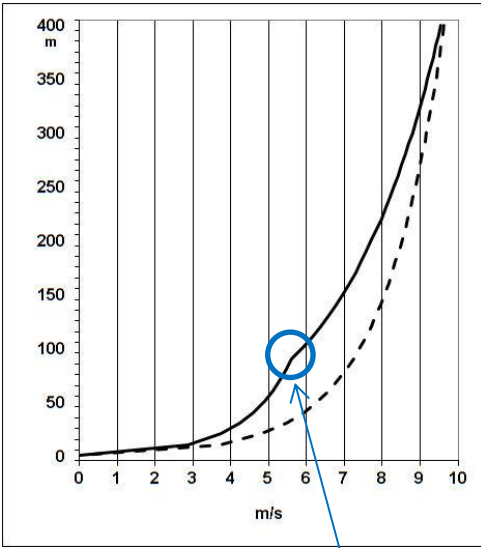
a) reduction of wind speed in the park interior  
vertical wind profiles in the park  
and upstream (undisturbed)



**neutral**

**unstable**

**stable**



**$z_0 = 1 \text{ m (land)}$**

**$z_0 = 0,0001 \text{ m (offshore)}$**

constant density of turbines in the park, 5% additional turbulence intensity due to the turbines

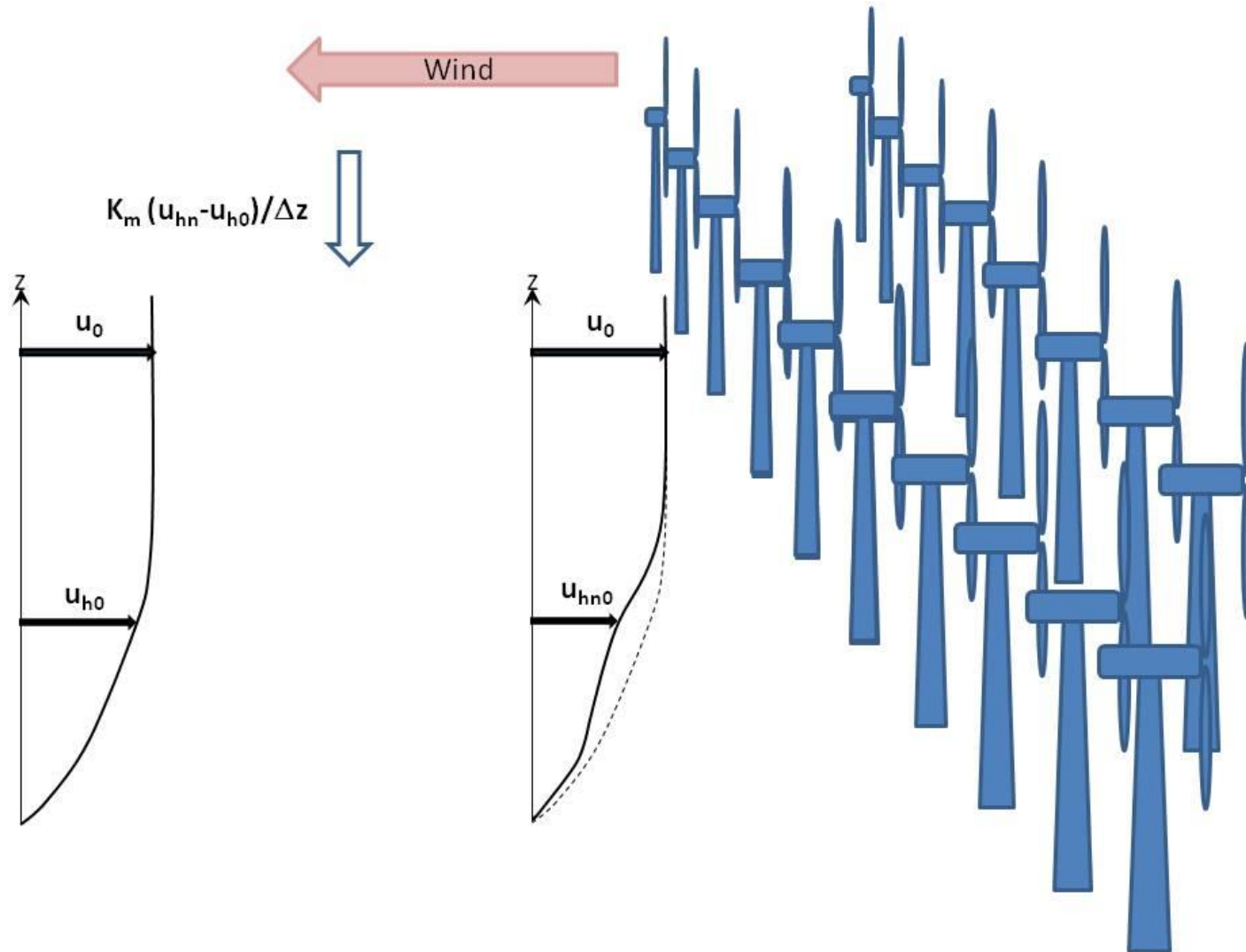
**nearly identical wind speed at hub height**

**b) speed-up of wind speed downstream of the wind park:**

$$\frac{\Delta u_{hn}}{\Delta t} = \frac{\kappa u_* z}{\Delta z^2} (u_{h0} - u_{hn})$$

**speed-up = re-supply from above**

**Emeis, S., 2010: A simple analytical wind park model considering atmospheric stability. Wind Energy, 13, 459-469.**



## solution of the analytical model

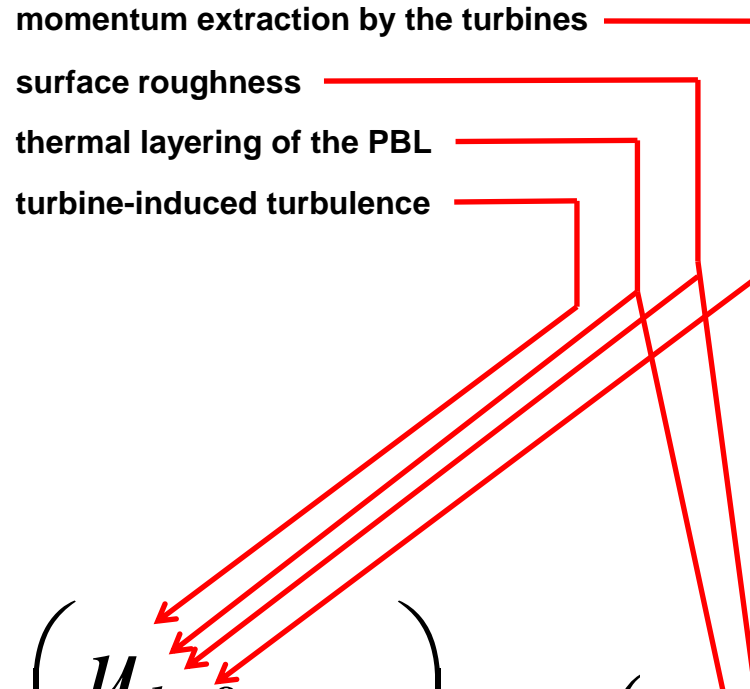
b) speed-up of wind speed downstream of the wind park:

momentum extraction by the turbines

surface roughness

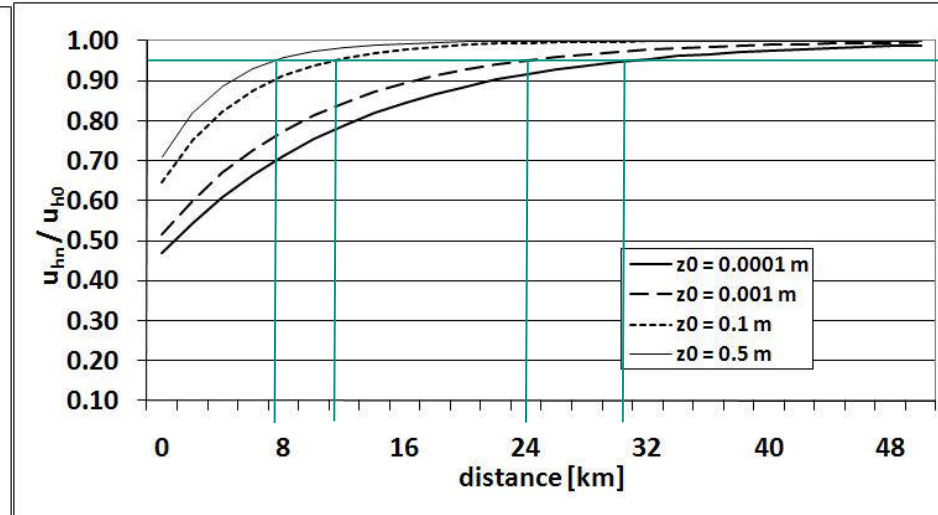
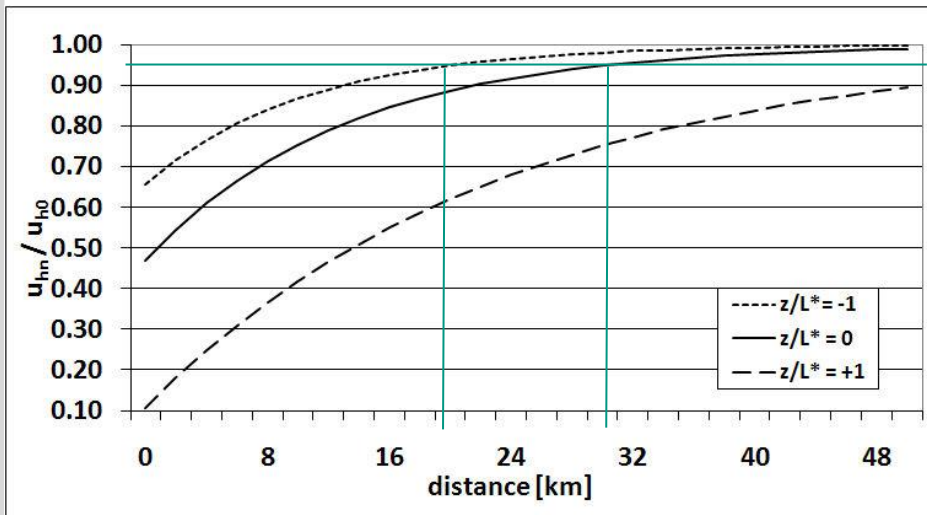
thermal layering of the PBL

turbine-induced turbulence

$$R_n = \frac{u_{hn}(t)}{u_{h0}} = 1 + \left( \frac{u_{hn0}}{u_{h0}} - 1 \right) \exp(-at)$$


## b) speed-up of wind speed behind the wind park

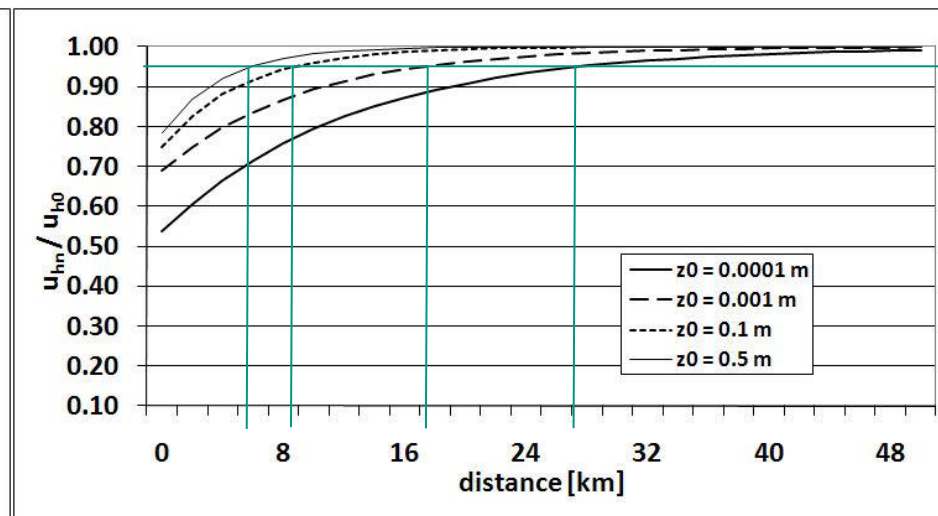
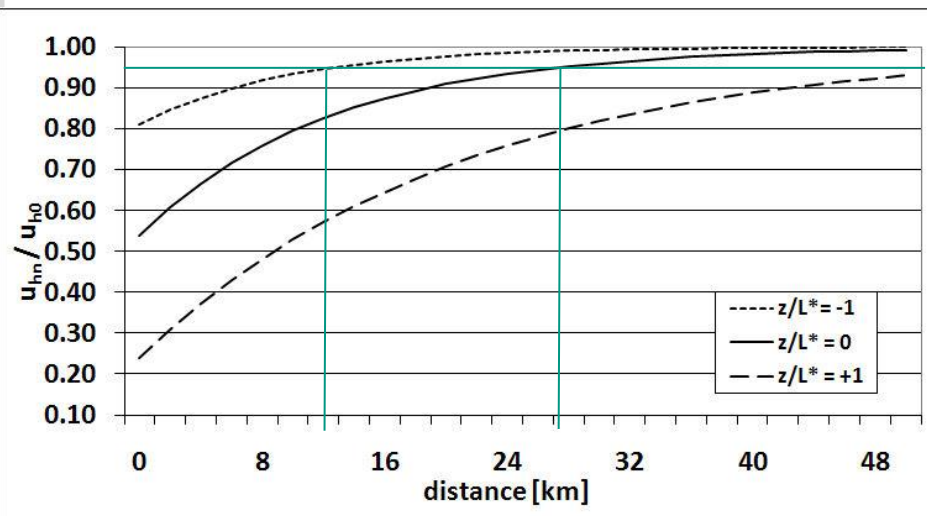
turbine-induced turbulence = 0.00



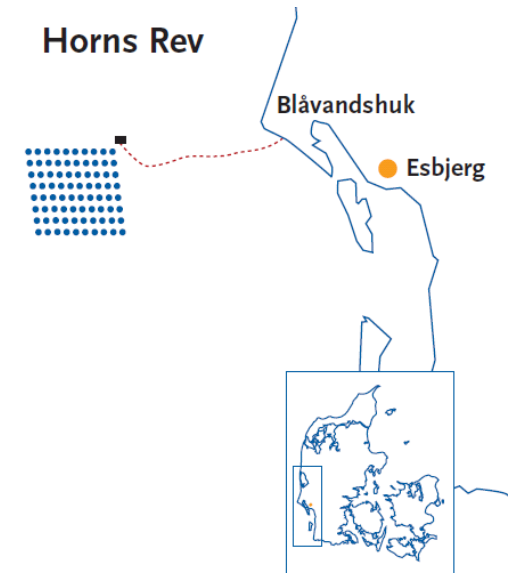
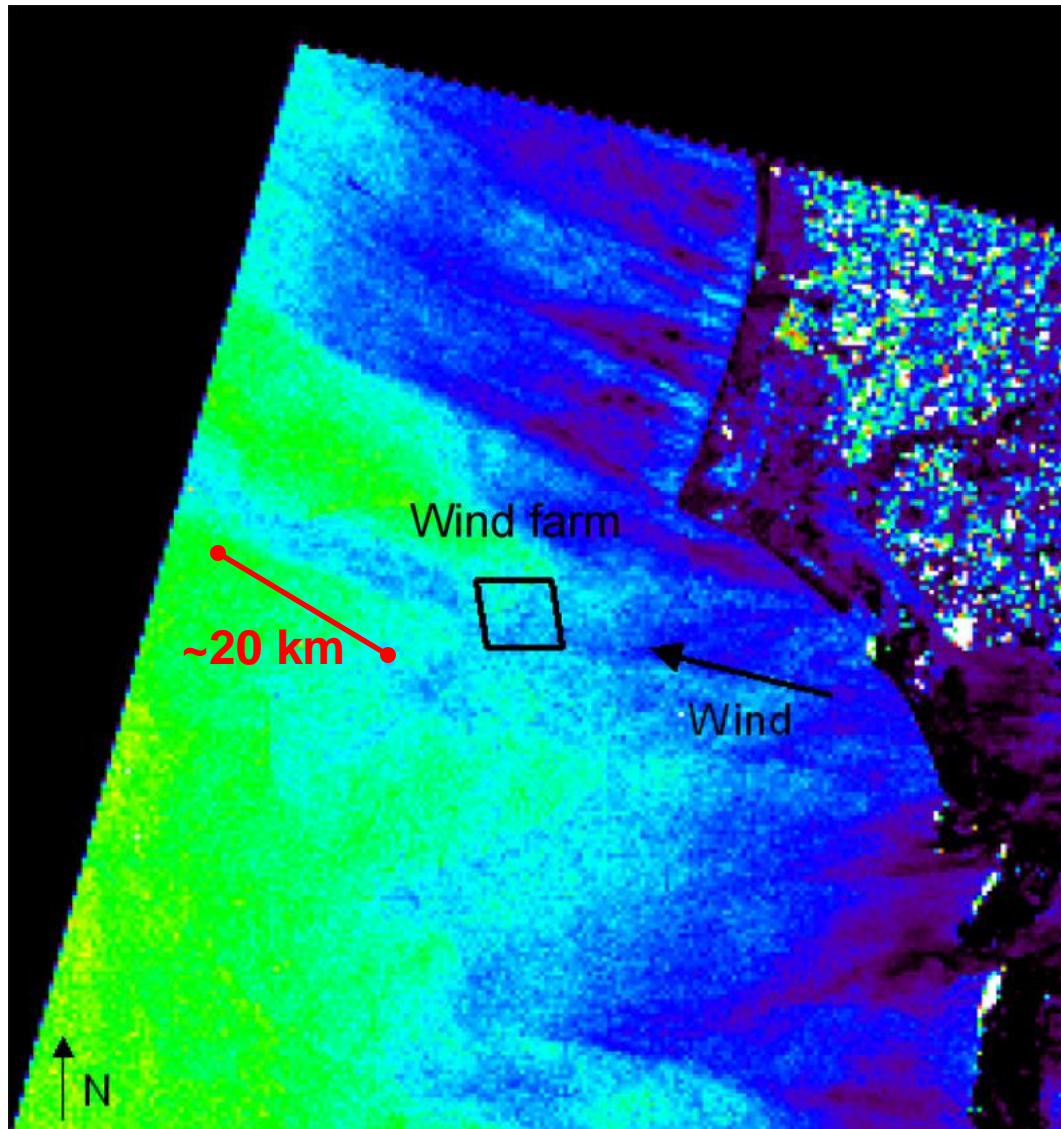
$z_0 = 0.0001$  m

turbine-induced turbulence = 0.10

neutral



## b) speed-up of wind speed behind the wind park measurements (Envisat, SAR) at Horns Rev ( 4 km x 5 km)



[http://www.hornsrev.dk/nyheder/brochurer/Horns\\_Rev\\_TY.pdf](http://www.hornsrev.dk/nyheder/brochurer/Horns_Rev_TY.pdf)

25. 02. 2003

© ERS SAR/Risø  
[http://galathea3.emu.dk/satelliteeye/projekter/wind/back\\_uk.html](http://galathea3.emu.dk/satelliteeye/projekter/wind/back_uk.html)

## Conclusions:

wind speed reduction: offshore stronger than onshore

- (partial) compensation of higher offshore wind speed
- offshore requires a larger distance between turbines

larger harvest from wind parks during unstable stratification

- offshore: annual cycle of energy production
- onshore: diurnal cycle of energy production

offshore wake length is three to four times larger than onshore

- offshore requires larger distances between wind parks

analytical model is strongly simplified

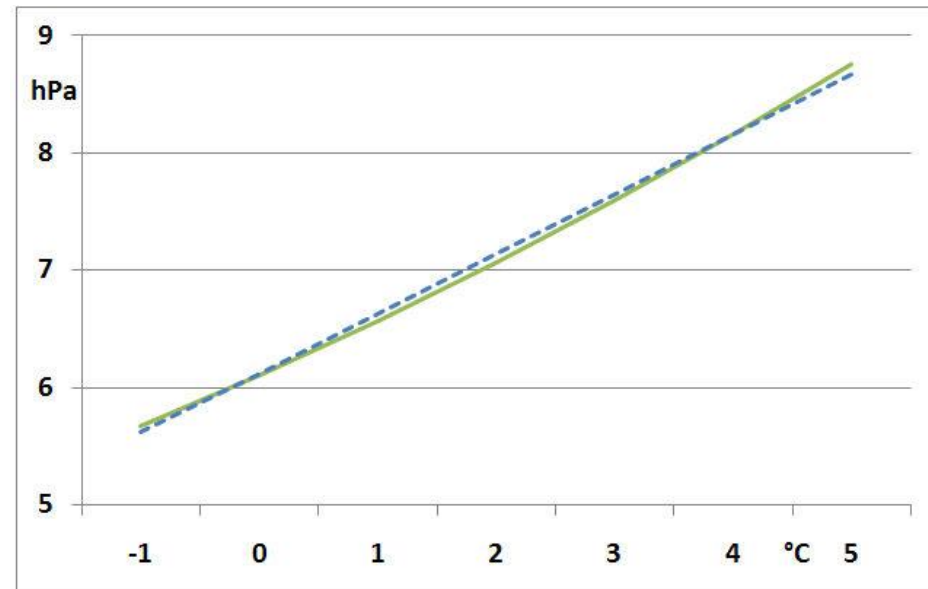
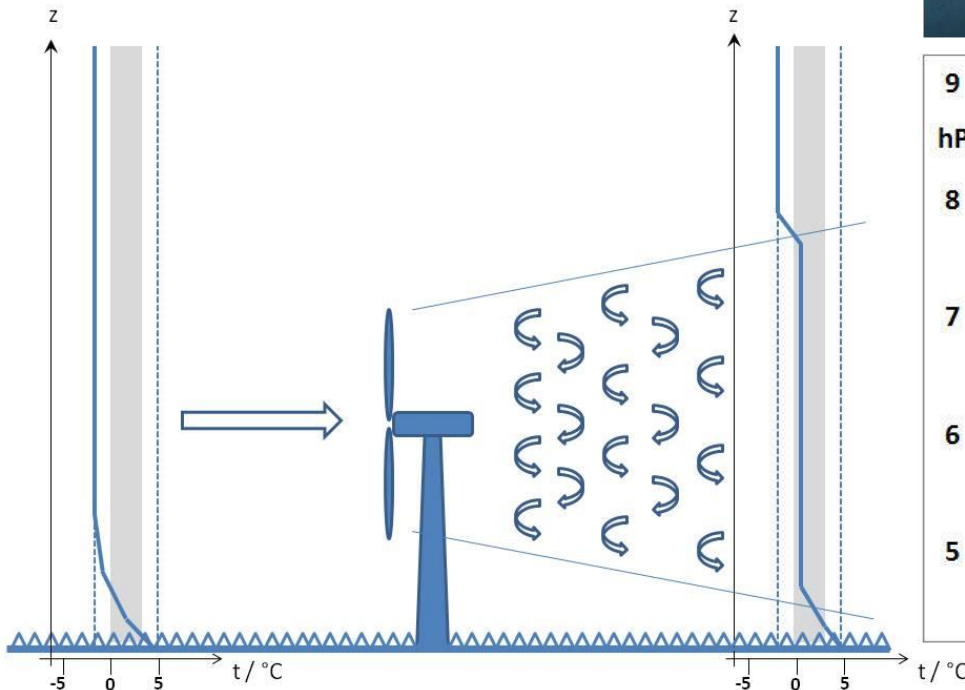
- only for rough estimation, exact simulations with numerical models necessary



# explanation of wake clouds: mixing fog (see poster outside!)



12. 02. 2008



air directly over the water:  
air at hub height:  
after mixing:

5°C, more than 99% relative humidity  
-1°C, more than 99% relative humidity  
2°C, above 101% humidity → clouds

**Thank you for your attention**

