

Mixing-layer height and low-level jets

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Introduction

- **definition of mixing layer**
- **definition of low-level jet**
- **relevance for wind energy**
- **remote sensing**

Mixing-layer height

Inversion height

literally: inversion in the temperature profile, increase of temperature with height, strong decrease of moisture, radiation inversions, sinking inversions, surface inversions, lifted inversions

Mixing-layer height

(mixing height, mixed-layer height)

upper boundary for vertical exchange (mixing), upper boundary of the well-mixed layer, entrainment, defined by the turbulence profile or by the vertical distribution of a tracer (aerosol, pot. temperature)

Boundary layer height

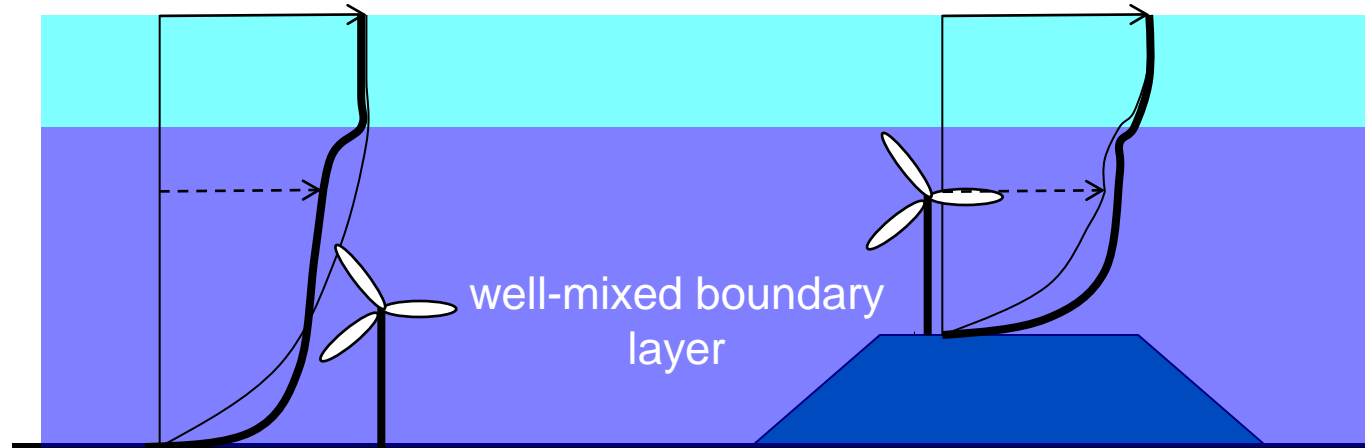
SBL: at night, height of the near-surface layer influenced by surface friction
CBL: at day, height of convective plumes

boundary layer height \approx mixing-layer height

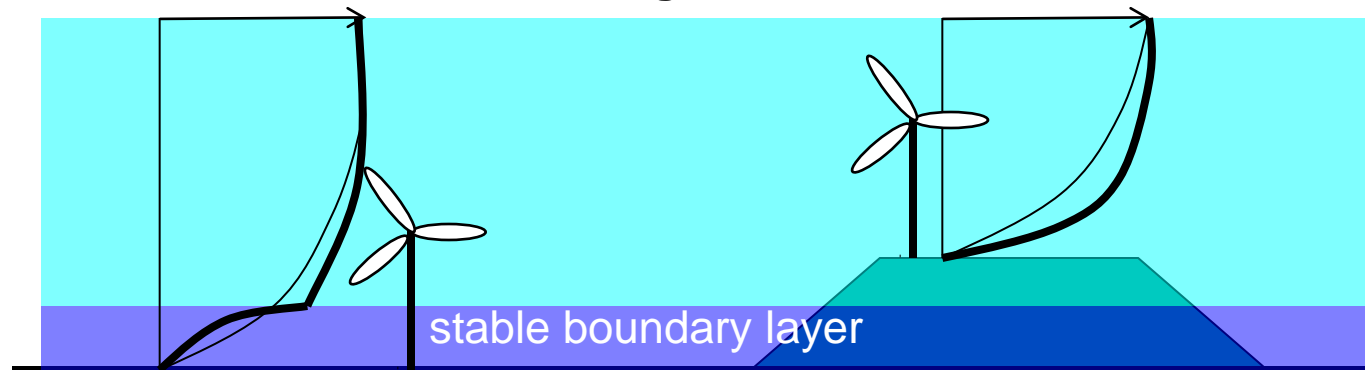
boundary layer height \geq inversion height

Mixing-layer height influences diurnal variation of vertical wind profiles

Day



Night

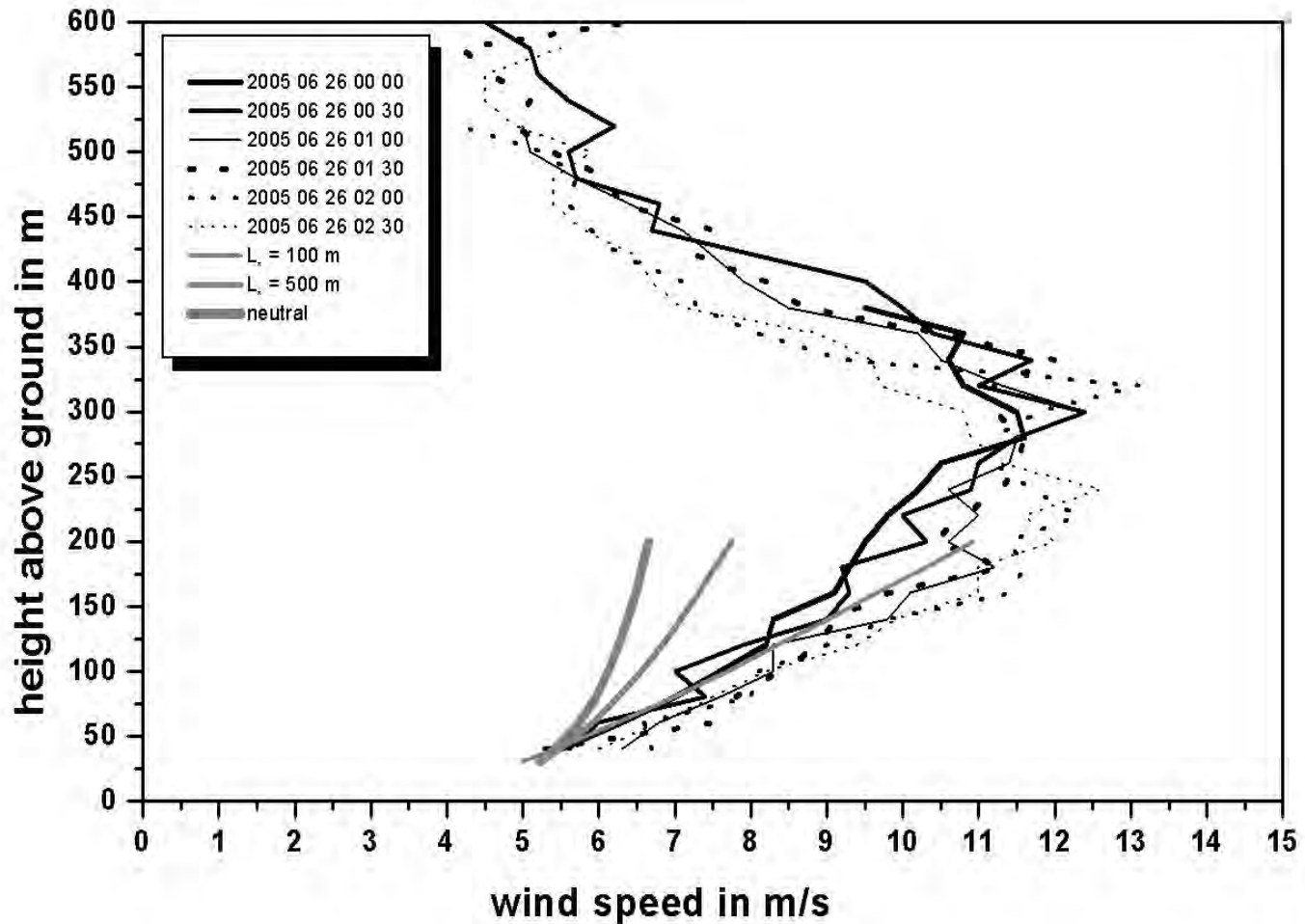


Low-level jet

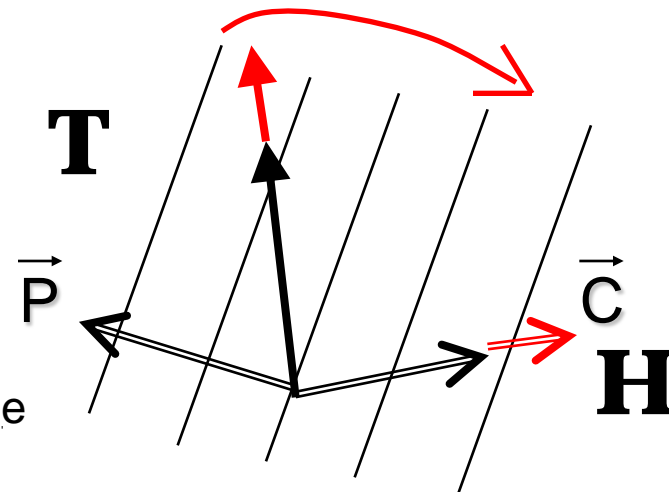
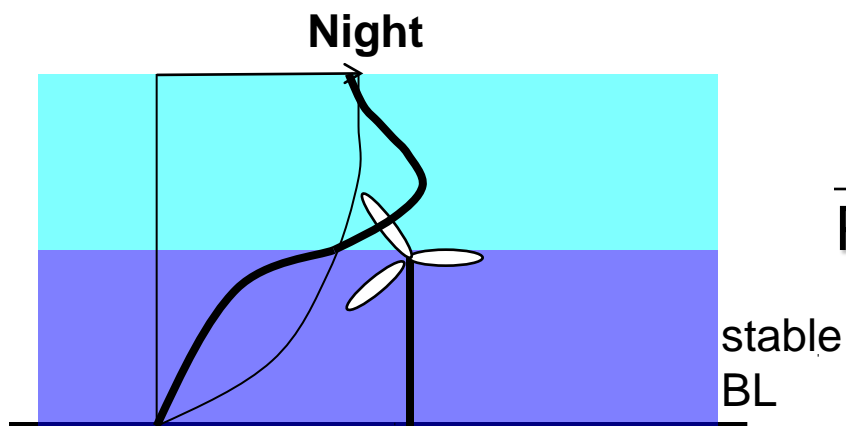
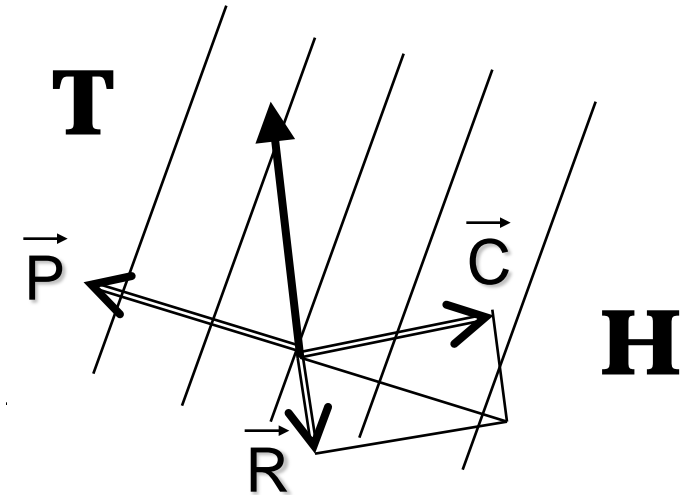
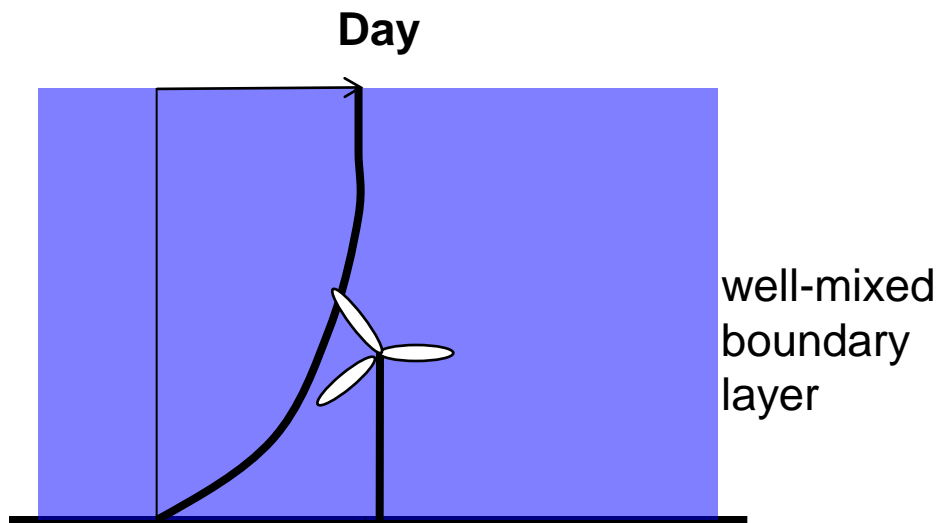
vertical profiles
of wind speed

26 June 2005

AdP Ch d G



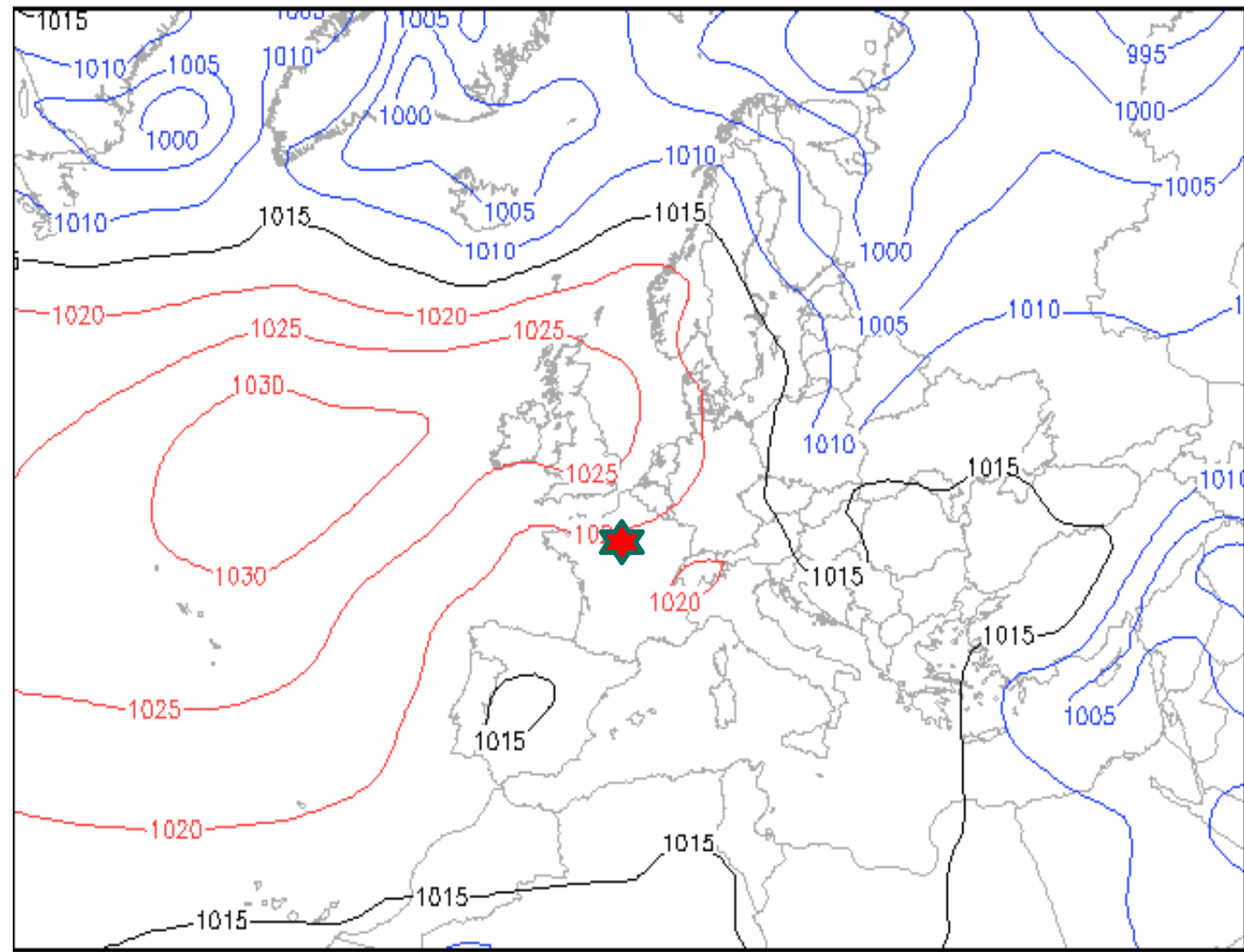
Nocturnal low-level jet and the turning of wind direction with height



**surface pressure
00 GMT**

26 June 2005

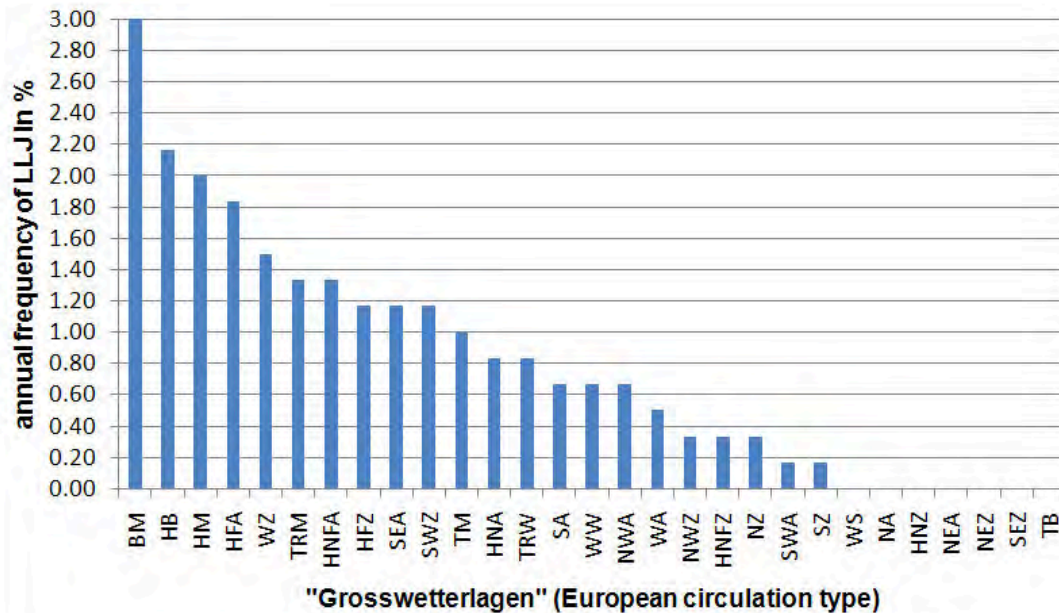
**asterisk denotes
location where
LLJ was observed**



Bodendruck GFS (hPa)

So 26.06.05 00 GMT (Sa 00 + 24)

WetterOnline



frequency of LLJ over Hanover for 20 months in the years 2001 to 2003

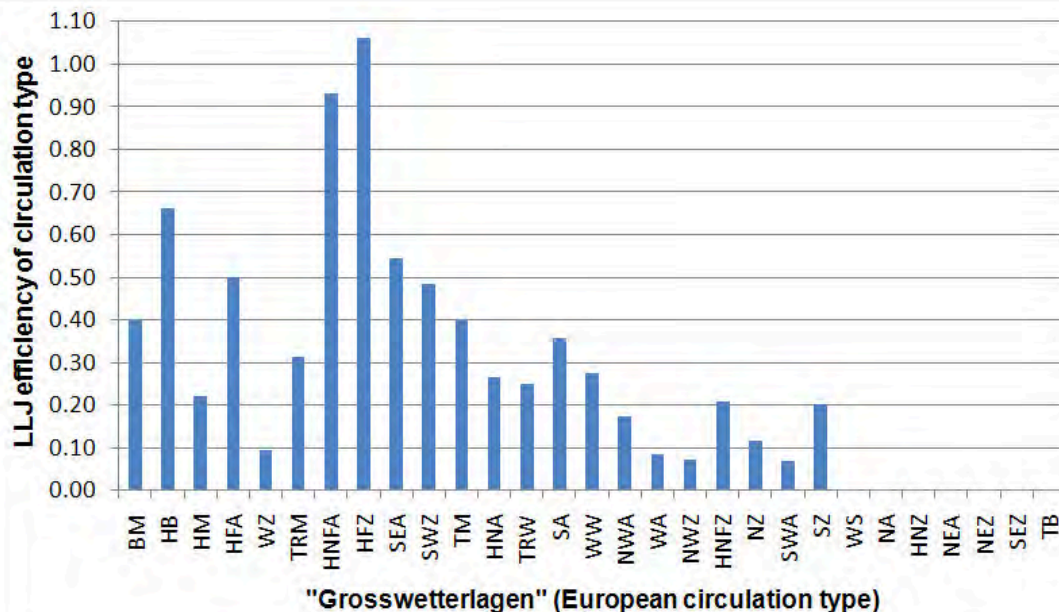
total is 23.17% of all nights

circulation types:

BM ridge over Central Europe
HB high over British Isles
HM high over Central Europe
 ...

HFZ high over Scandinavia
HNFA high over North Atlantic
 ...

“efficiency” of a circulation type to produce a LLJ over Hanover for 20 months in the years 2001 to 2003



Relevance for wind energy

The vertical wind profile (equilibrium conditions)

logarithmic law

(with stability correction) $u(z) = (u_*/\kappa) (\ln(z/z_0) - \psi(z/L_*))$

power law

$$u(z) = u(z_A) (z/z_A)^n$$

New proposal
(Gryning et al. 2007)

$$u(z) = \frac{u_{*0}}{\kappa} \left(\ln \left(\frac{z}{z_0} \right) + \frac{z}{L_{MBL,N}} - \frac{z}{z_i} \left(\frac{z}{2L_{MBL,N}} \right) \right)$$

needs information on the PBL or mixing-layer height

Gryning, S.-E., E. Batchvarova, B. Brümmer, H. Jørgensen, S. Larsen, 2007: On the extension of the wind profile over homogeneous terrain beyond the surface boundary layer. *Bound.-Lay. Meteorol.*, **124**, 251–268.

Peña, A., S.-E. Gryning, C.B. Hasager, 2010: Comparing mixing-length models of the diabatic wind profile over homogeneous terrain. *Theor. Appl. Climatol.*, **100**, 325-353.

LLJ can only be described by time-dependent equations!

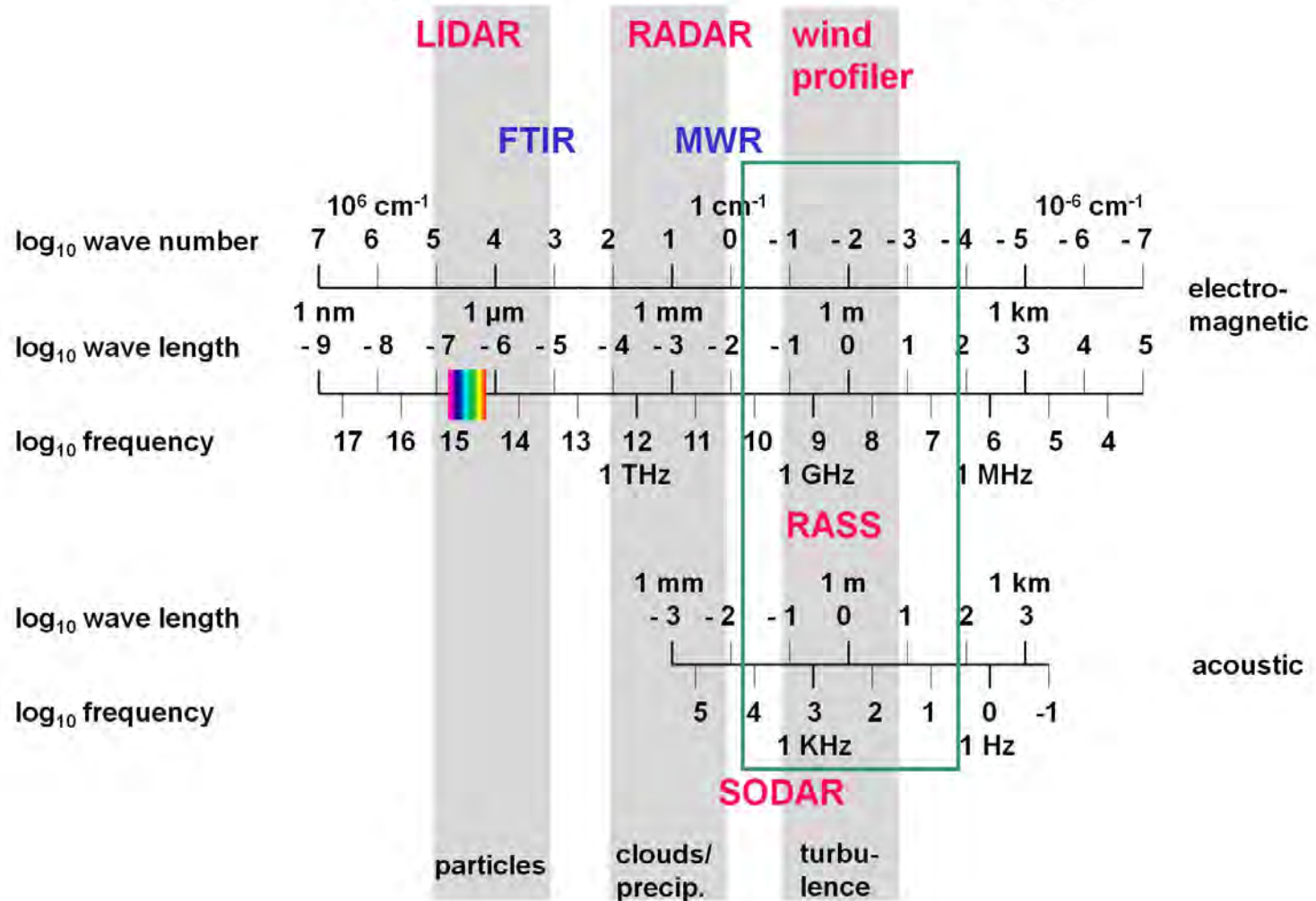
Basic remote sensing techniques

name	principle	spatial resolution	direction	type
RADAR	backscatter, electro-magnetic pulses, fixed wave length	profiling	scanning, slanted	active, monostatic
SODAR	backscatter, acoustic pulses, fixed wave length	profiling	fixed, slanted, vertical	active, usually monostatic
LIDAR ceilometer	backscatter, optical pulses, fixed wave length(s)	profiling	scanning, fixed, horizontal, slanted, vertical	active, monostatic
RASS	backscatter, acoustic, electro-magnetic, fixed wave length	profiling	fixed, vertical	active, monostatic
	absorption, infrared, spectrum	path-averaging	fixed, horizontal, slanted	active, bistatic or passive
FTIR	emission, infrared, spectrum	path-averaging	fixed, horizontal, slanted	passive
DOAS	absorption, optical, fixed wave lengths	path-averaging	fixed, horizontal	active, bistatic
radiometry	electro-magnetic, fixed wave length(s)	averaging, profiling	fixed, scanning, slanted, vertical	passive
tomography	travel time, acoustic, fixed wave length	horizontal distribution	fixed, horizontal	active, multiple emitters and receivers

subject of this lecture

subject of this lecture

Frequencies for atmospheric remote sensing



Emeis, S., 2010: Measurement Methods in Atmospheric Sciences - In situ and remote. Borntraeger, Stuttgart, 272 pp., 103 figs, 28 tables, ISBN 978-3-443-01066-9.

at IMK-IFU

SODAR (Large system),
acoustic backscatter, Doppler
shift analysis → wind, turbulence

SODAR-RASS (Doppler-RASS), acoustic,
electro-magnetic backscatter, determines speed
of sound → wind and temperature profiles



Ceilometer,
backscatter, optical
pulses, wave
length ~ 0.9 μm
→ aerosol profiles

Wind-LIDAR, optical backscatter, Doppler shift
analysis, wave length ~ 1.5 μm → wind and
aerosol profiles



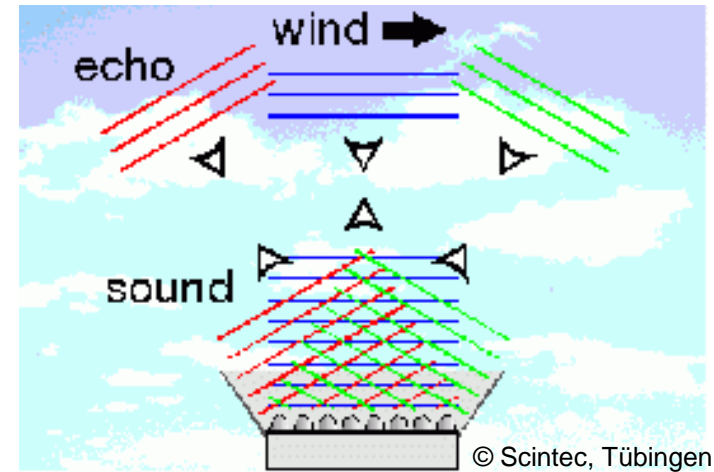
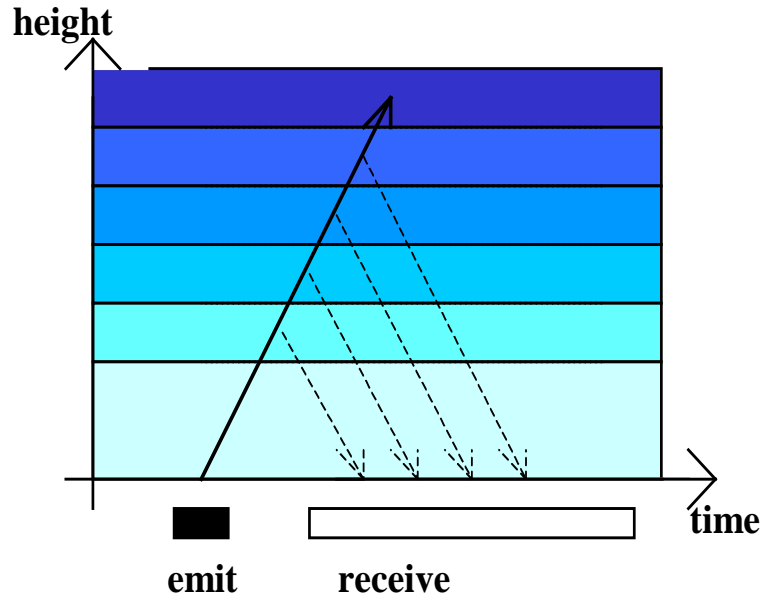
image:
Halo Photonics

SODAR

**algorithms for the determination of
mixing-layer height**

and low-level jet observations

monostatic SODAR: measuring principles



deduction:

sound travel time	=	height
backscatter intensity	=	turbulence
Doppler-shift	=	wind speed

Emission of sound waves
into three directions:

in order to measure all three
components of the wind
(horizontal and vertical)

The SODAR equation:

$$P_R = r^2 (c_s \tau A \varepsilon / 2) P_0 \beta_s e^{-2\sigma r} + P_{bg}$$

P_R received power,

P_0 emitted power,

ε antenna efficiency,

A effective antenna area,

σ sound absorption in air due to classical and molecular absorption due to the collision of water molecules with the oxygen and nitrogen molecules of the air,

r distance between the scattering volume and the instrument,

τ pulse duration (typically between 20 and 100 ms),

β_s backscattering cross-section (typically in the order of $10^{-11} \text{ m}^{-1} \text{ sr}^{-1}$),

c_s sound speed,

P_{bg} background noise.

Emitted power: $\sim 10^3 \text{ W}$, received (backscattered) power: 10^{-15} W

The SODAR equation:

$$P_R = r^2 (c_s \tau A \epsilon / 2) P_0 \beta_s e^{-2\sigma r} + P_{bg}$$

The ratio of the two terms on the right-hand side of the SODAR equation is called signal-to-noise ratio (usually abbreviated as SNR).

The backscattering cross-section β_s is a function of the temperature structure function C_T^2 (Tatarskii 1961).

For a monostatic SODAR we find (Reitebuch 1999) when using the wave number $k = 2\pi/\lambda$:

$$\beta_s(180^\circ) = 0,00408 k^{1/3} C_T^2 / T^2$$

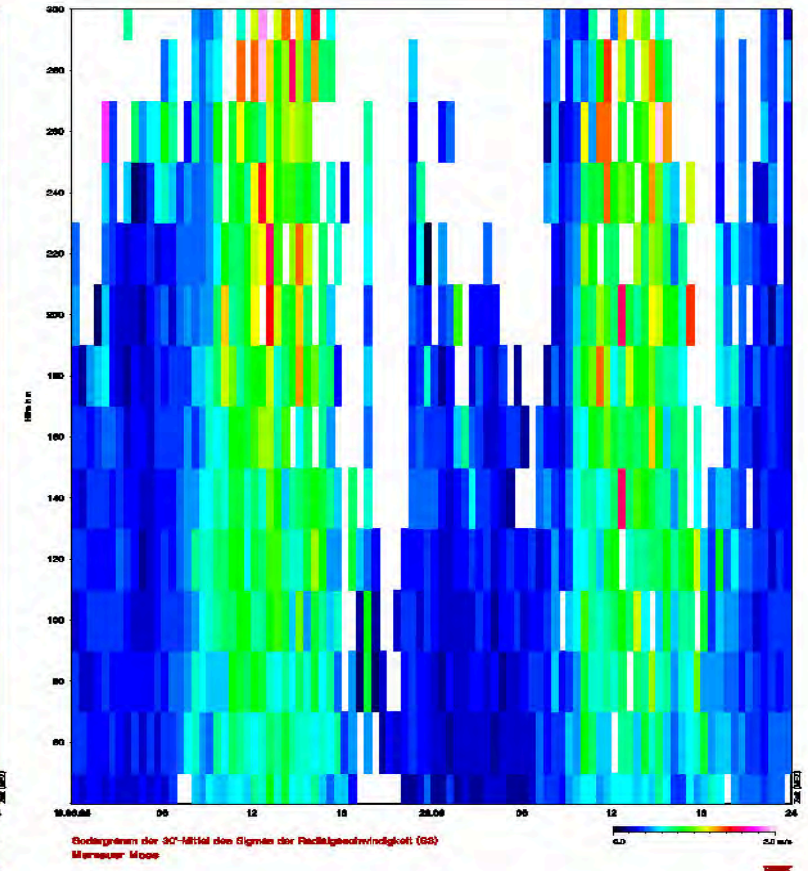
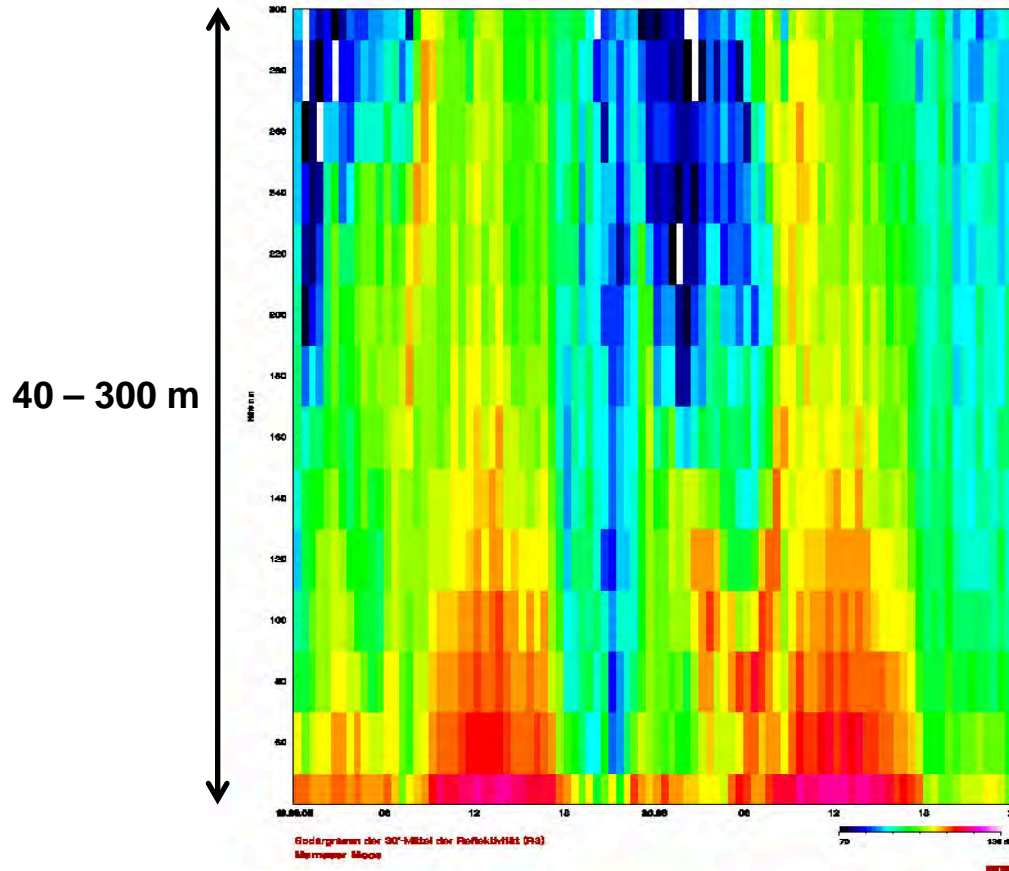
Reitebuch, O., 1999: SODAR-Signalverarbeitung von Einzelpulsen zur Bestimmung hochaufgelöster Windprofile. Schriftenreihe des Fraunhofer-Instituts für Atmosphärische Umweltforschung, Shaker Verlag GmbH Aachen, Bd. 62, 178 S.

Tatarskii, V.I., 1971: The effect of the turbulent atmosphere on wave propagation. Kefer Press, Jerusalem, 472 S.

SODAR sample plot (daytime convective BL)

acoustic backscatter intensity

sigma w

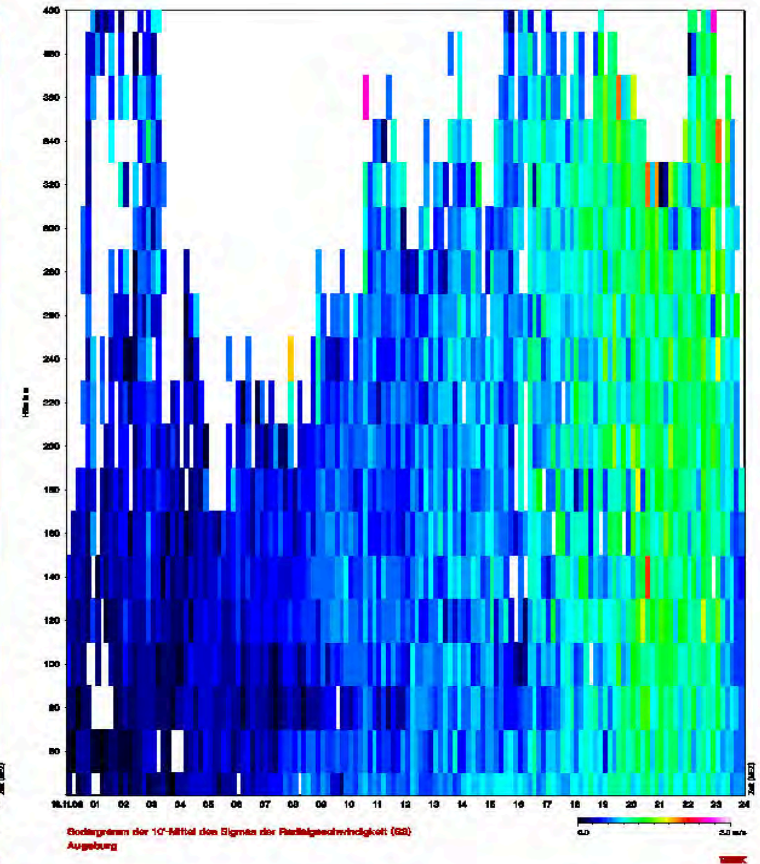
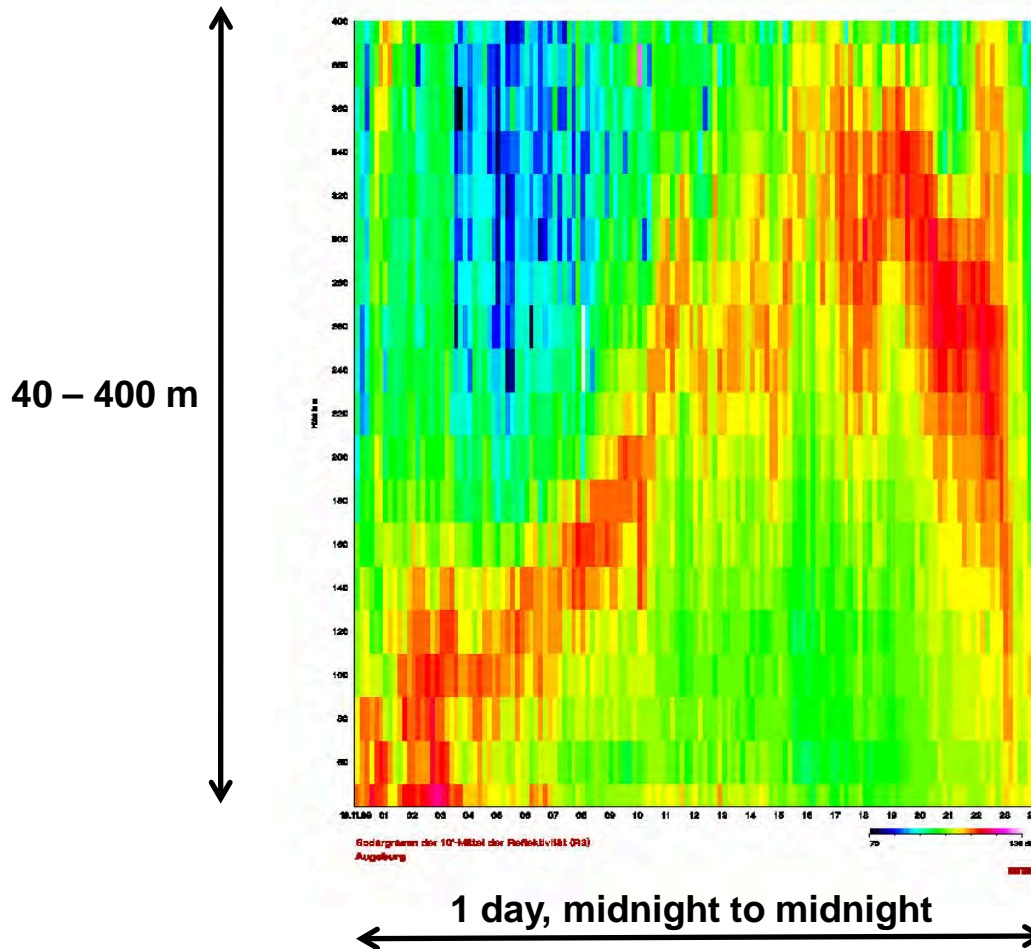


2 days, midnight to midnight

SODAR sample plot (lifted inversion)

acoustic backscatter intensity

sigma w

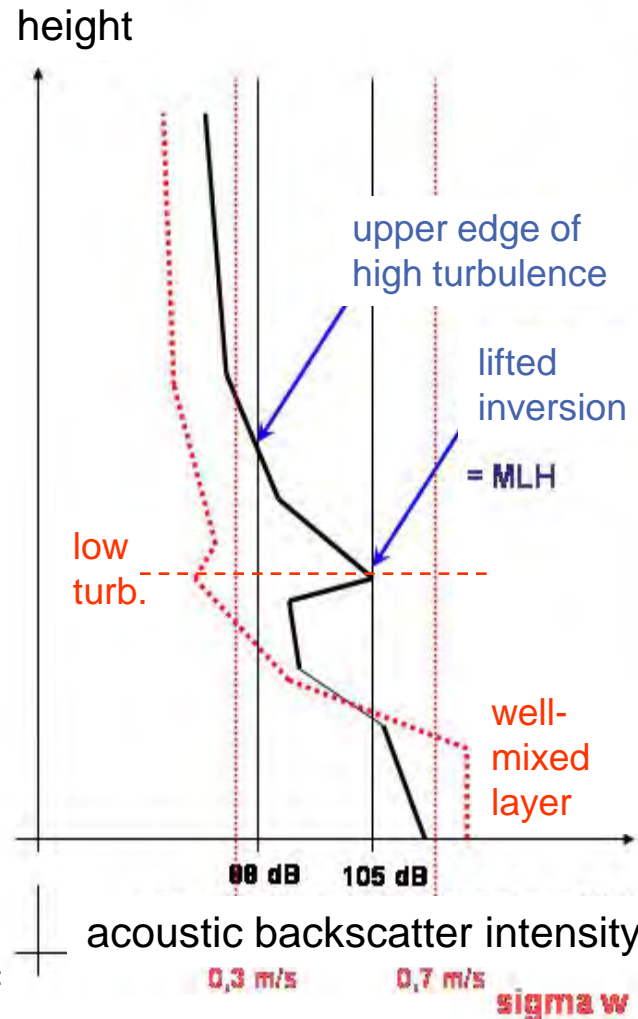


Algorithms to detect MLH from SODAR data

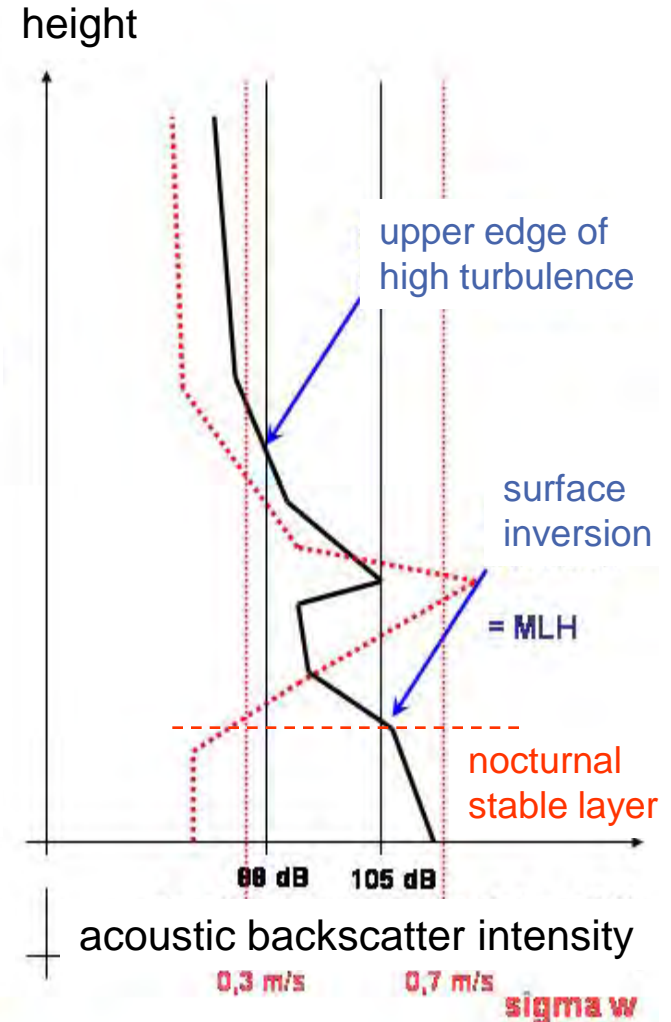
criterion 1:
 upper edge
 of high
 turbulence

criterion 2:
 surface and
 lifted
 inversions

MLH = Min (C1, C2)



example 1: daytime



example 2: night-time

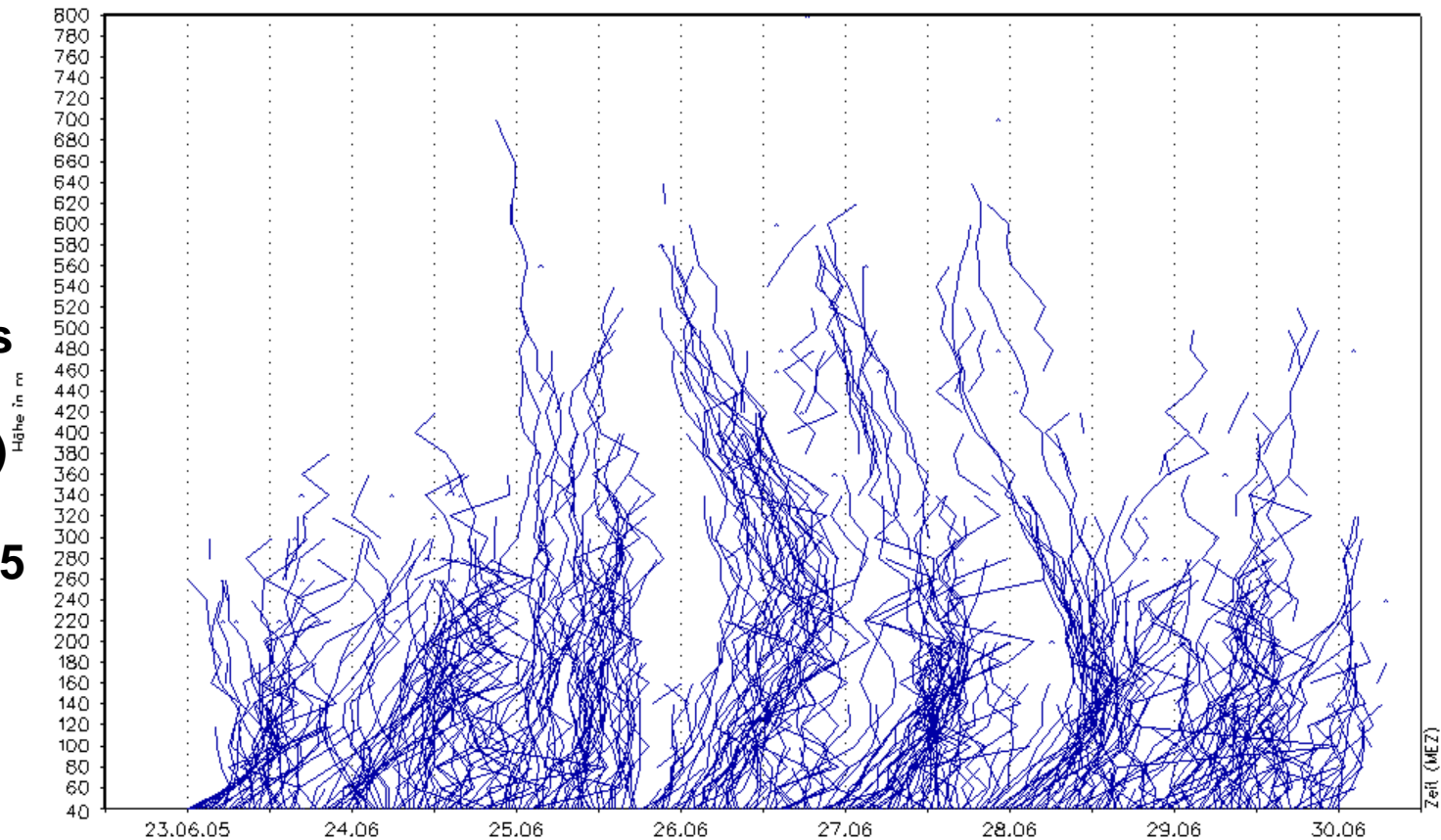
Emeis, S., K. Schäfer, C. Münkel, 2008:
 Surface-based remote sensing of the
 mixing-layer height – a review.
 Meteorol. Z., 17, 621-630.

examples for low-level jet observations with SODAR

vertical profiles
of wind speed
(30 min means)

23-30 June 2005

AdP Ch d G



30'-Mittel der Windgeschwindigkeit (V)
vertical wind profiles

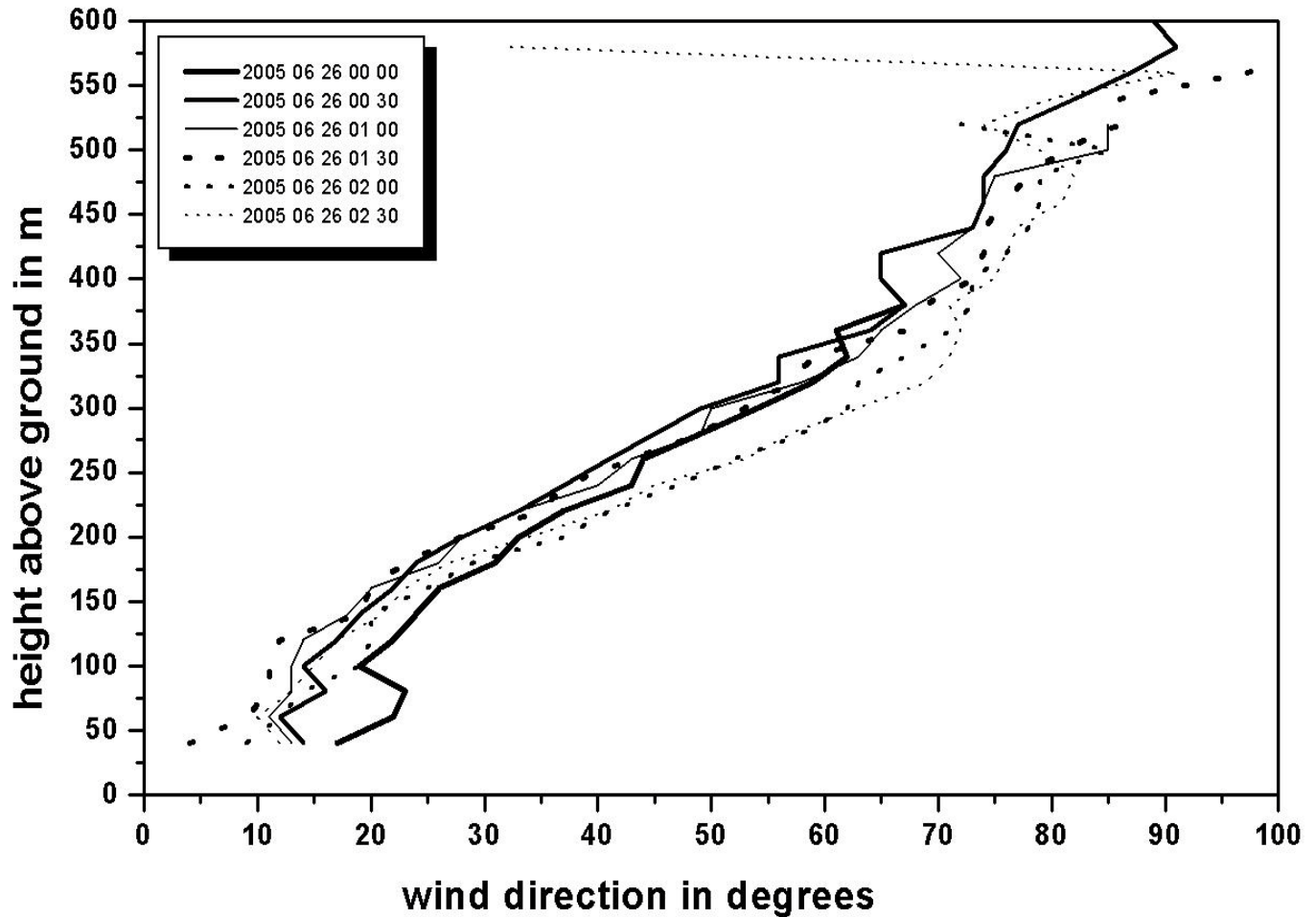
ΔV = 4 m/s

METEK

vertical profiles
of wind direction

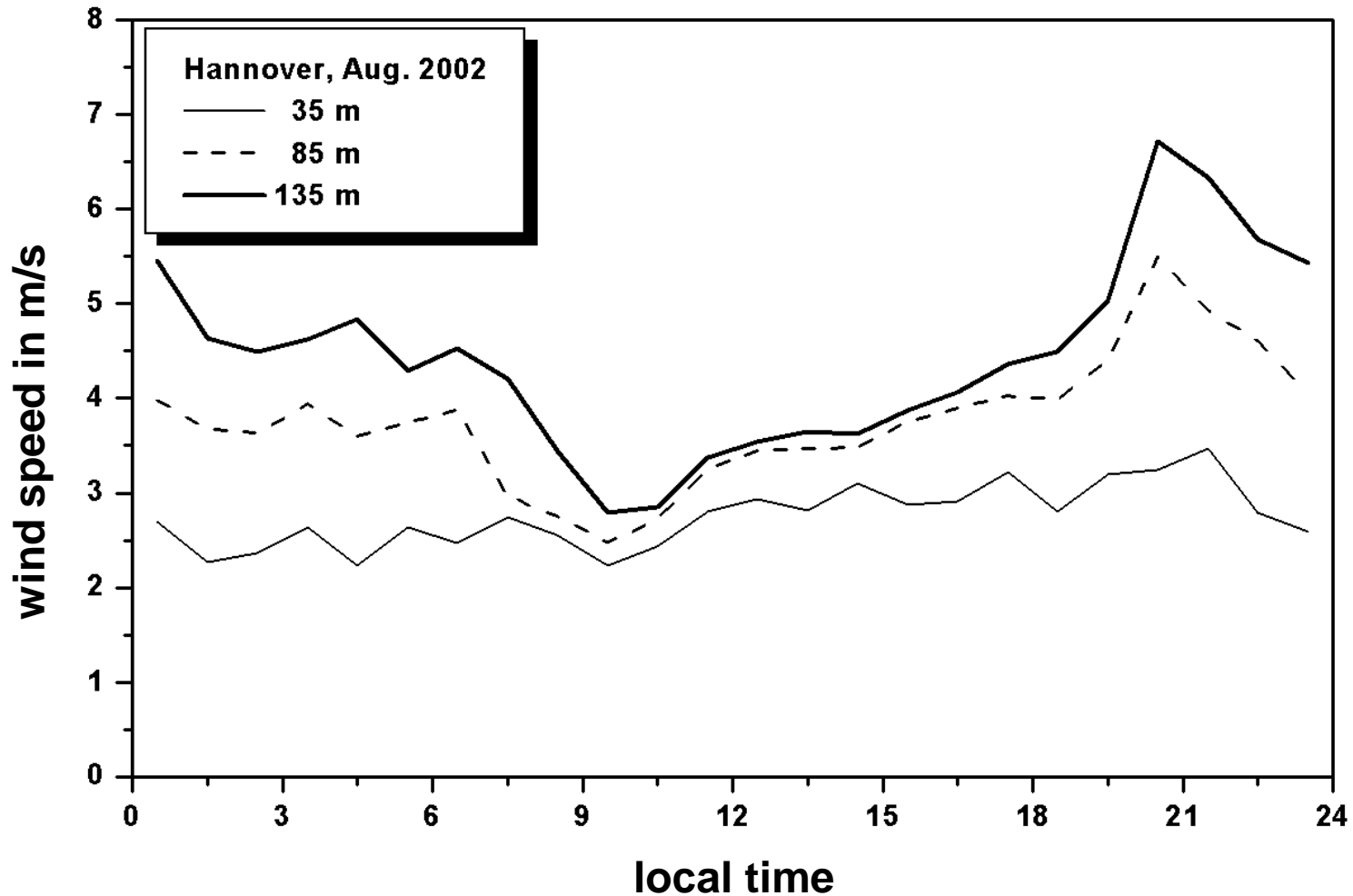
26 June 2005

AdP Ch d G

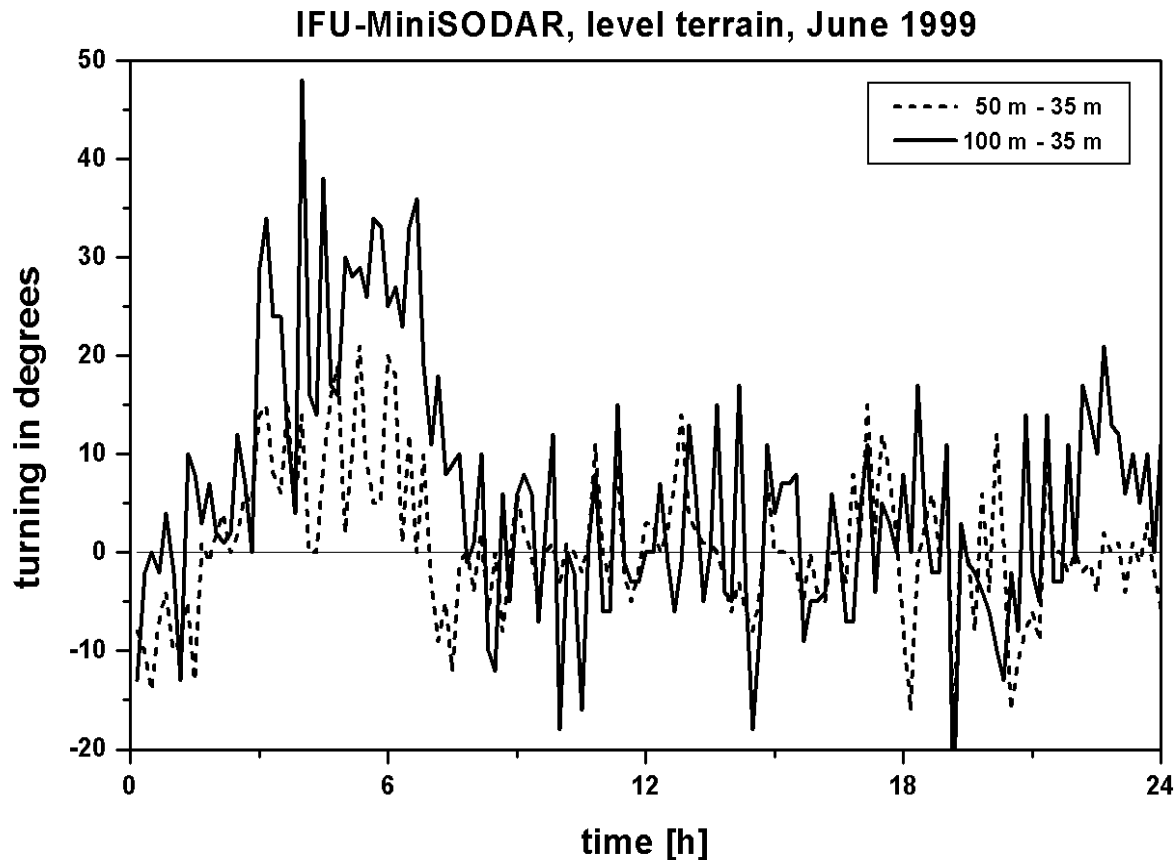


Monthly mean diurnal course of wind speed

August 2002, 17 nights with LLJ



Mean diurnal variation of the turning of wind direction with height

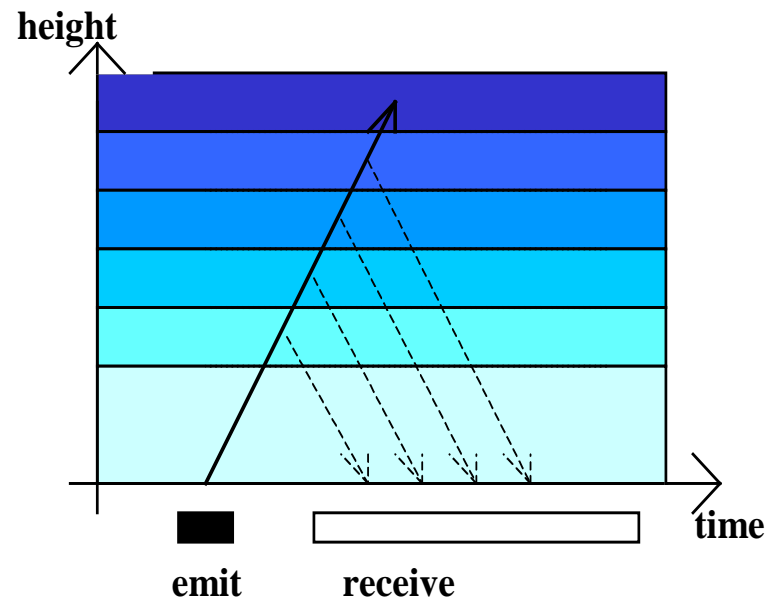


Emeis, S., 2001: Vertical variation of frequency distributions of wind speed in and above the surface layer observed by sodar. Meteorol. Z., **10**, 141-149.

Ceilometer

**algorithms for the determination of
mixing-layer height**

Ceilometer/LIDAR measuring principle



detection:

travel time of signal	= height
backscatter intensity	= particle size and number distribution
Doppler-shift	= cannot be analyzed from ceilometer data
	(available only from a Wind-LIDAR: velocity component in line of sight)

The LIDAR equation:

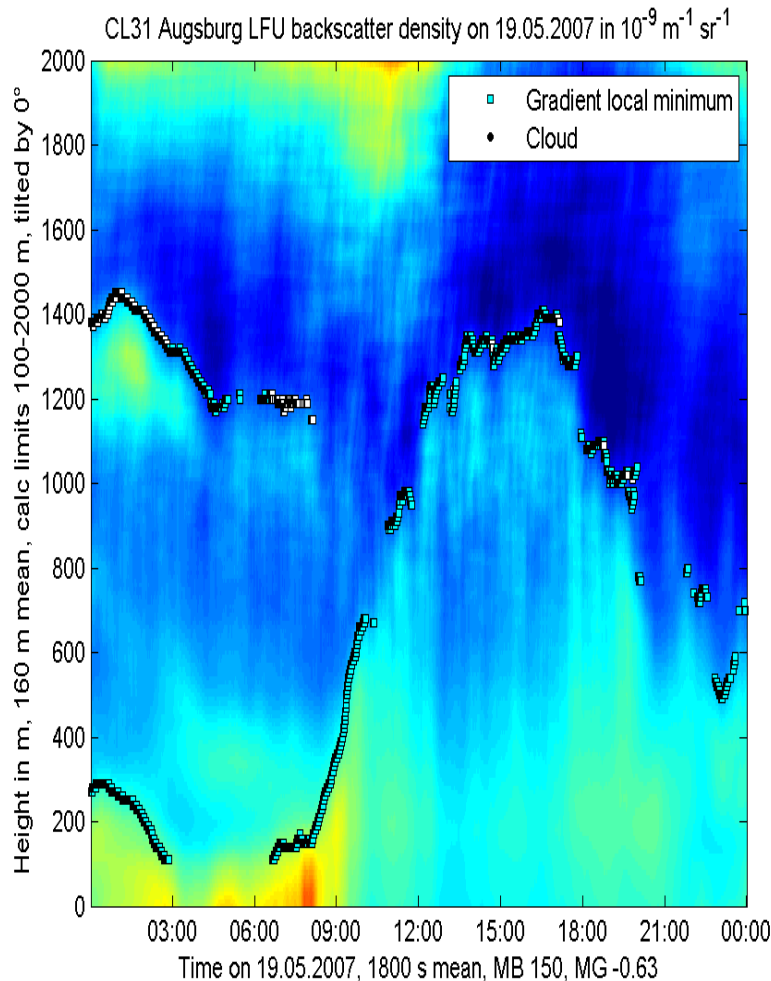
$$P_R(\lambda, r) = r^2 (c\tau A\varepsilon/2) P_0 [\beta_m(\lambda, r) + \beta_p(\lambda, r)] e^{-2\sigma r} + P_{bg}$$

- r** distance between the LIDAR and the backscattering object,
- c** speed of light,
- τ** pulse duration,
- A** antenna area,
- ε** correction term for the detector efficiency and losses due to the lenses,
- P_0** emitted energy,
- β_m** backscatter coefficient for molecules
- β_p** backscatter coefficient for particles,
- σ** absorption of light in the atmosphere,
- P_{bg}** background noise.

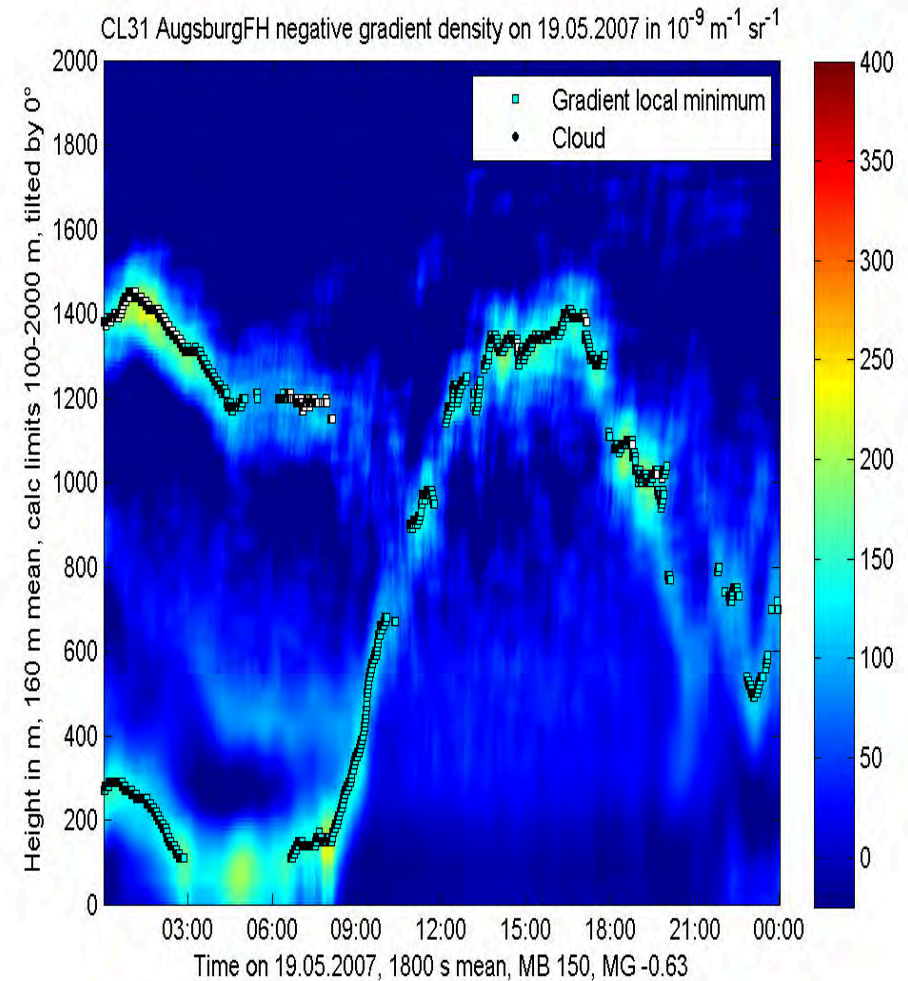
For a ceilometer β_m is negligible and only β_p is important

ceilometer sample plot (daytime convective BL)

optical backscatter intensity



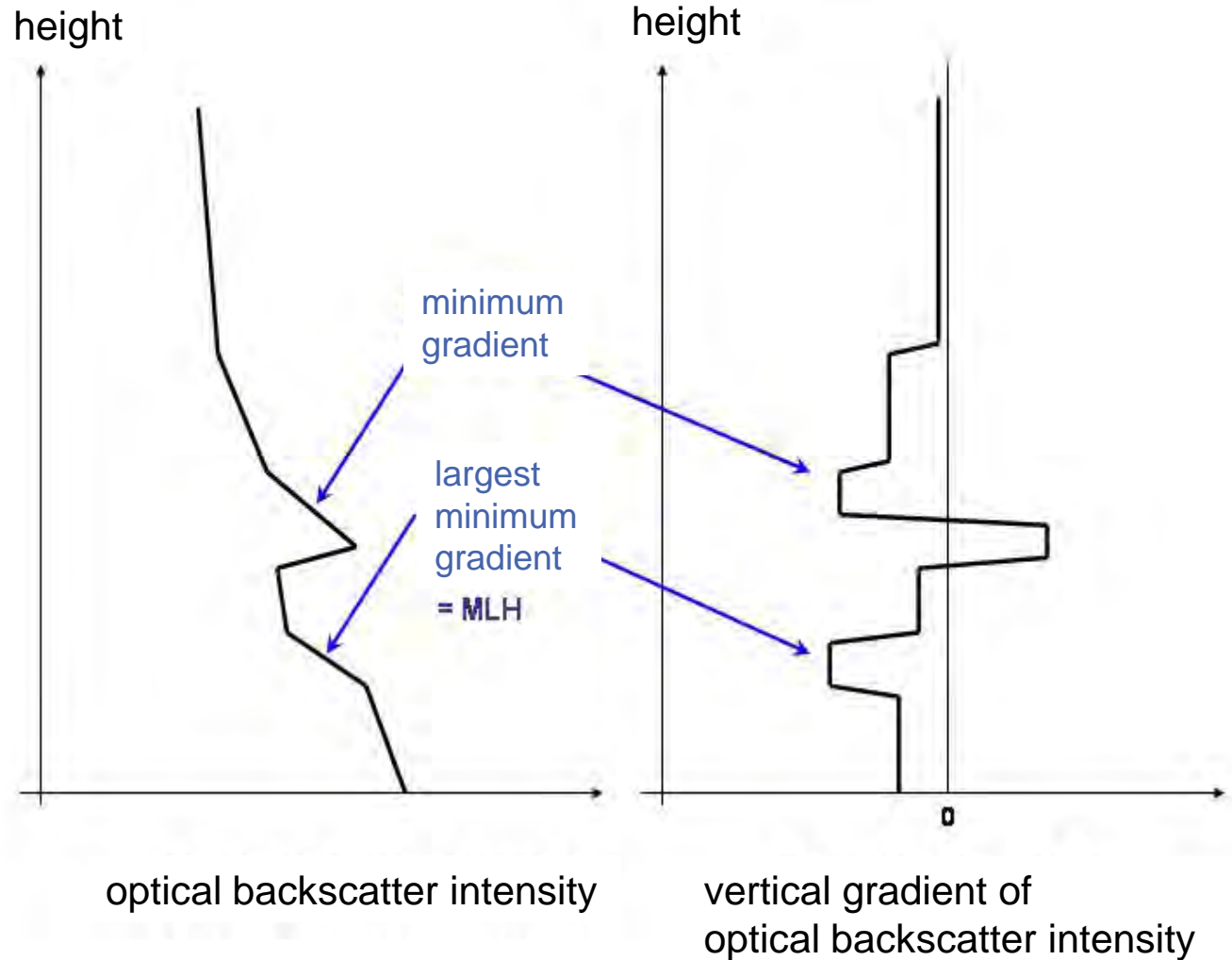
negative vertical gradient of optical backscatter intensity



Algorithm to detect MLH from Ceilometer-Daten

criterion

minimal vertical
gradient of backscatter
intensity (the most
negative gradient)

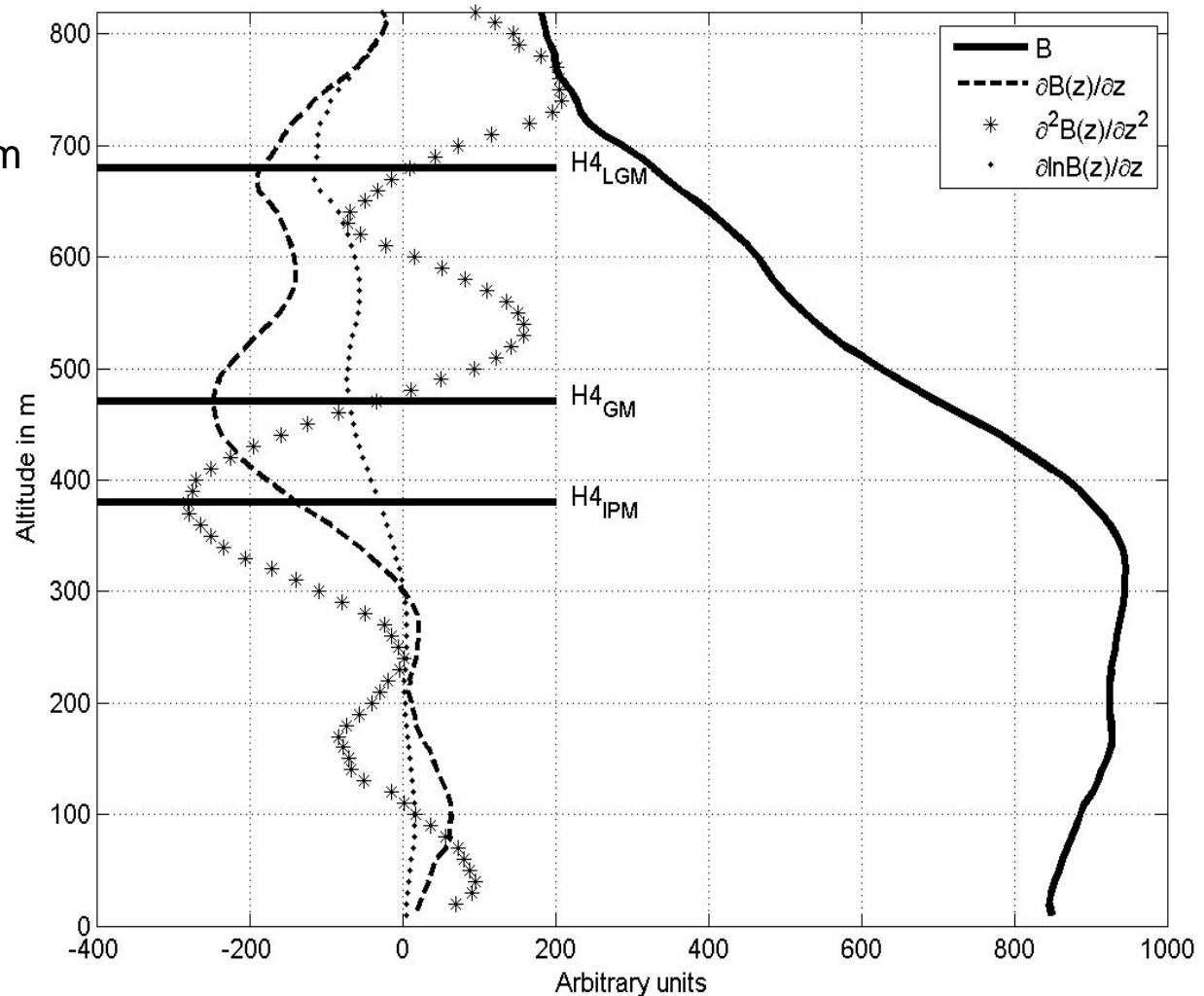


Different gradient methods (see Sicard et al. 2006, BLM 119, 135-157)

logarithmic gradient minimum

gradient minimum

inflection point method
(minimum of 2nd derivative)



comparison of two different ceilometers

LD40

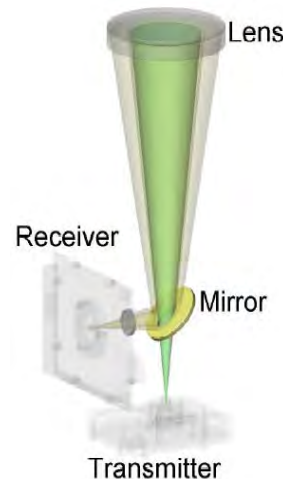
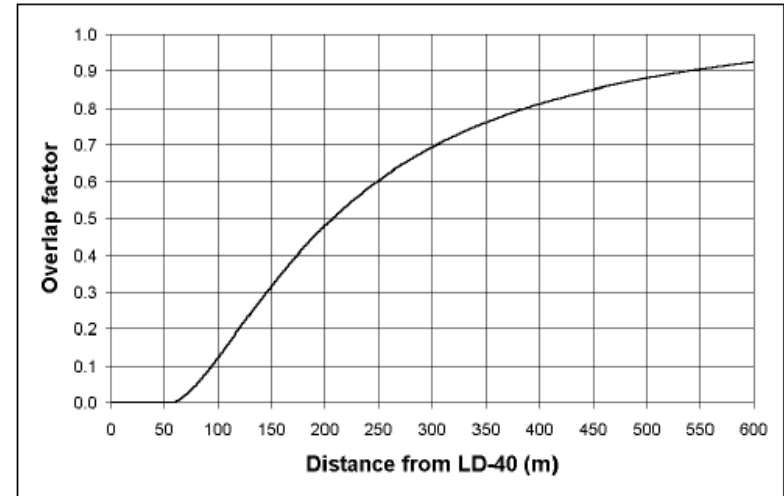
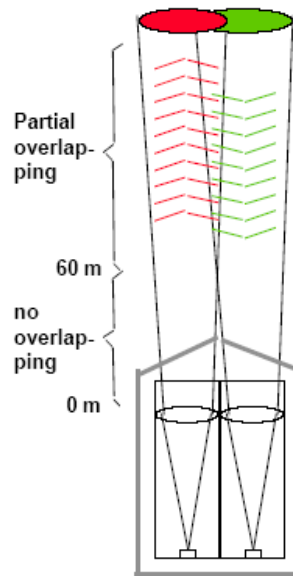
two optical axes

wave length: 855 nm
height resolution: 7.5 m
max. range: 13000 m

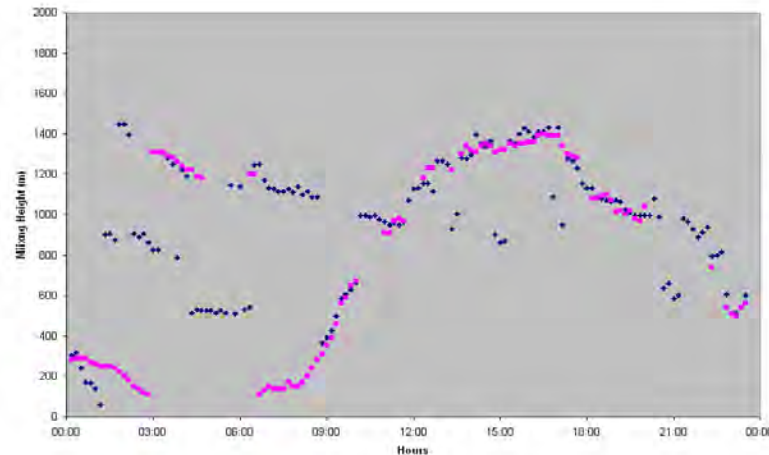
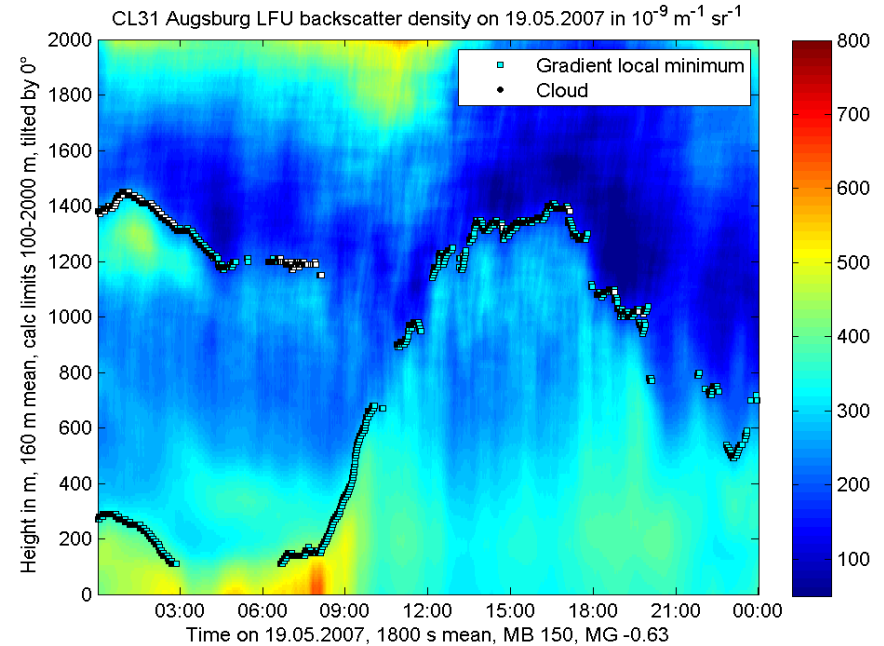
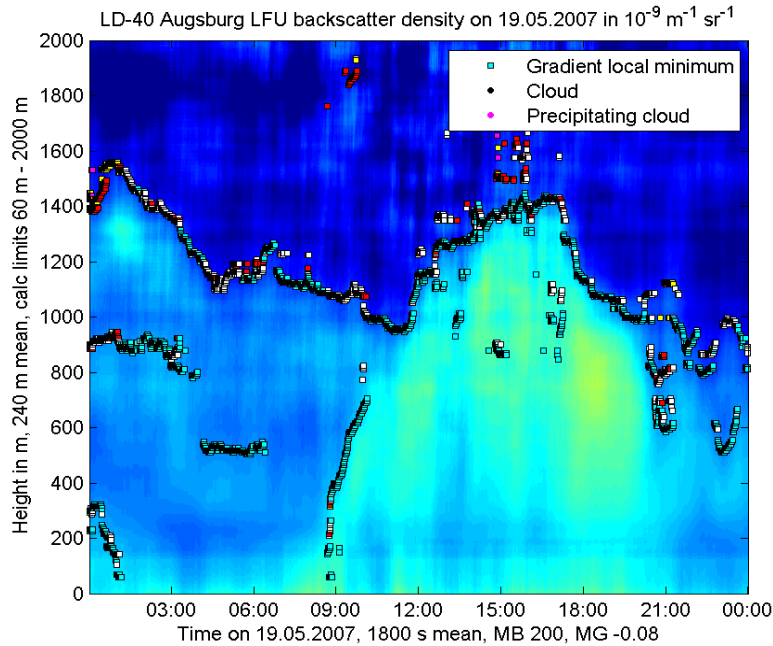
CL31 / CL51

one optical axis

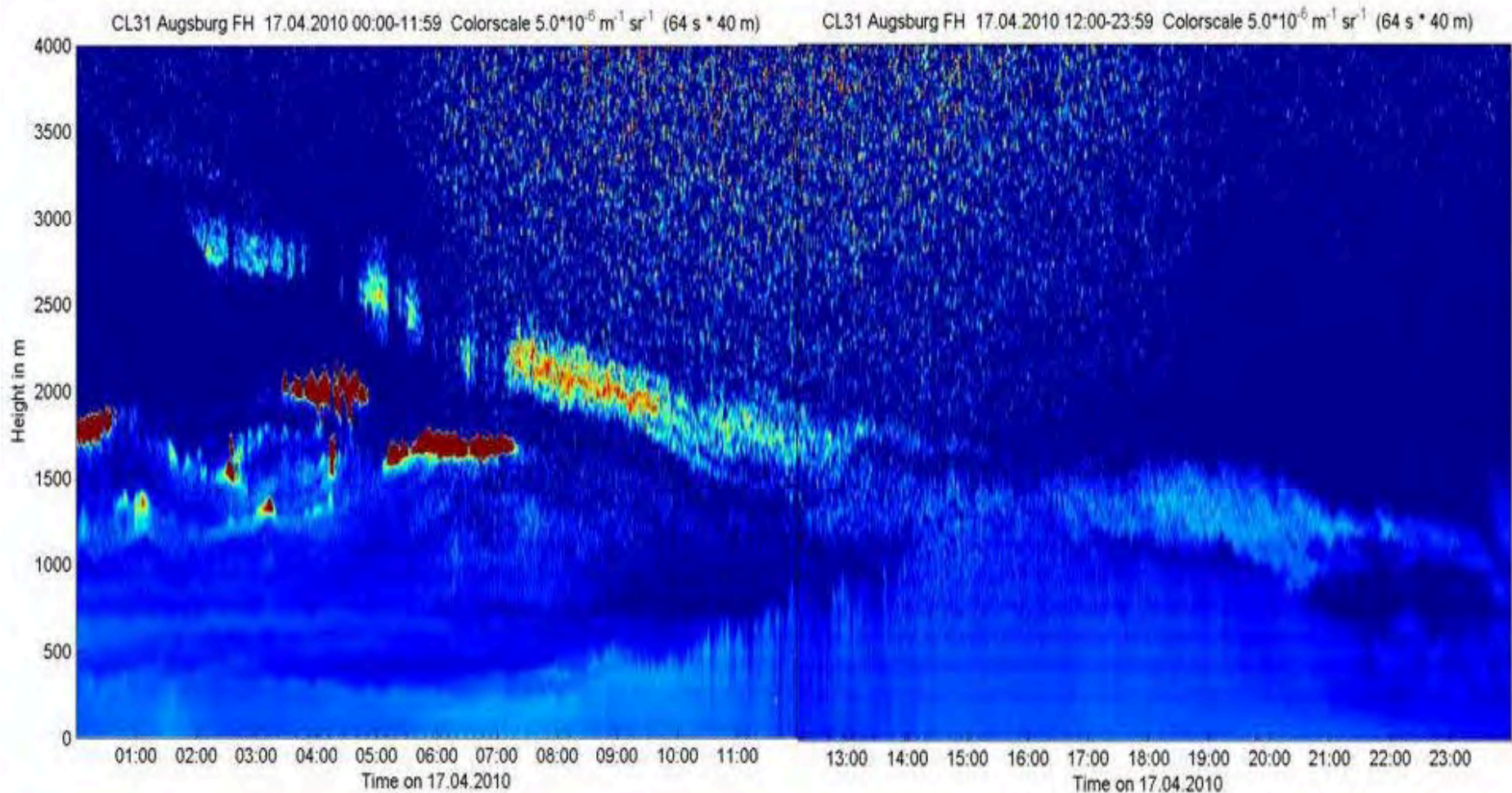
wave length: 905 nm
height resolution: 5 m
max. range: 7500 m



comparison of LD40 and CL31



Eyjafjallajökull ash cloud over Southern Germany



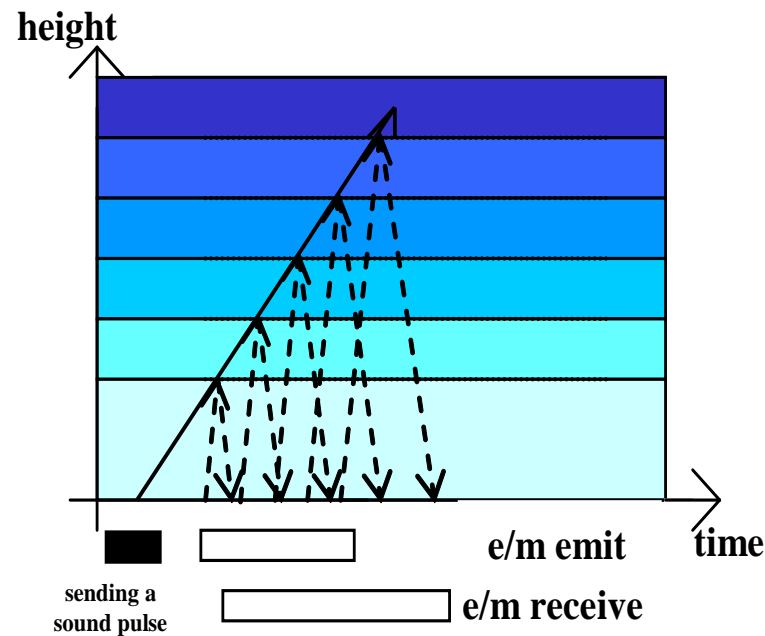
read more: Emeis, S., R. Forkel, W. Junkermann, K. Schäfer, H. Flentje, S. Gilge, W. Fricke, M. Wiegner, V. Freudenthaler, S. Groß, L. Ries, F. Meinhardt, W. Birmili, C. Münkel, F. Obleitner, P. Suppan, 2011: Measurement and simulation of the 16/17 April 2010 Eyjafjallajökull volcanic ash layer dispersion in the northern Alpine region. Atmos. Chem. Phys., 11, 2689–2701

RASS

principles of operation

examples

RASS measuring principle



detection:

travel time of em./ac. signal	= height	
ac. backscatter intensity	= turbulence	(identical to SODAR)
ac. Doppler-shift	= line-of-sight wind speed	(identical to SODAR)
em. Doppler shift	= sound speed → temperature	

RASS (radio-acoustic remote sensing)

measures vertical temperature profiles

Bragg-RASS: windprofiler plus acoustic component

Doppler-RASS: SODAR plus electro-magnetic component

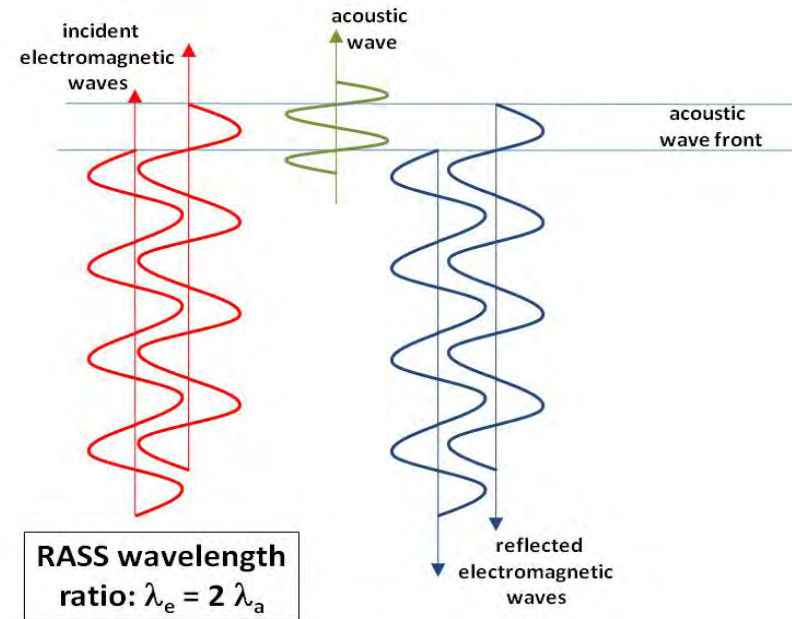
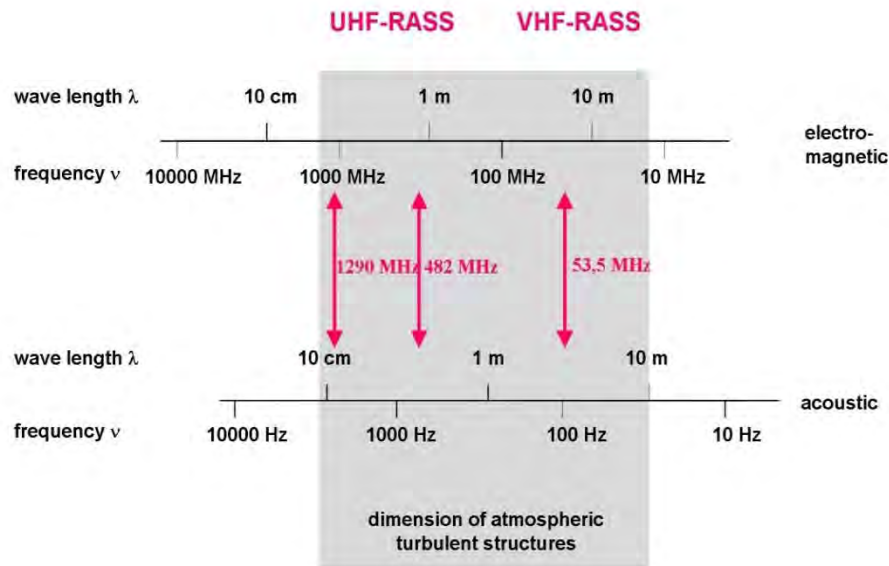
UHF RASS (boundary layer)

VHF RASS (troposphere)

RASS: frequencies

**Bragg condition:
acoustic wavelength = 1/2 electro-magnetic wavelength**

electro-magnetic - acoustic frequency pairs for RASS devices



Emeis, S., 2010: Measurement Methods in Atmospheric Sciences - In situ and remote. Borntraeger, Stuttgart, 272 pp., 103 figs, 28 tables, ISBN 978-3-443-01066-9.



SODAR-RASS (Doppler-RASS)

(METEK)

acoustic frequ.: 1077 Hz

radio frequ.: 474 MHz

resolution: 20 m

lowest

range gate: ca. 40 m

vertical range: 540 m



Bragg-RASS

acoustic frequ.: about 3000 Hz

radio frequ.: 1290 MHz

resolution: 50 m

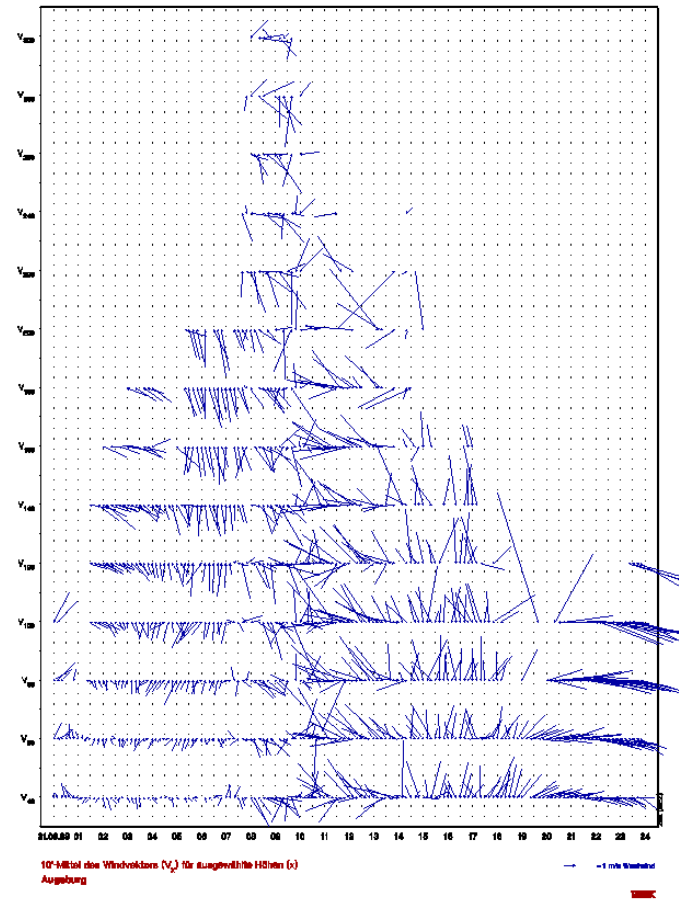
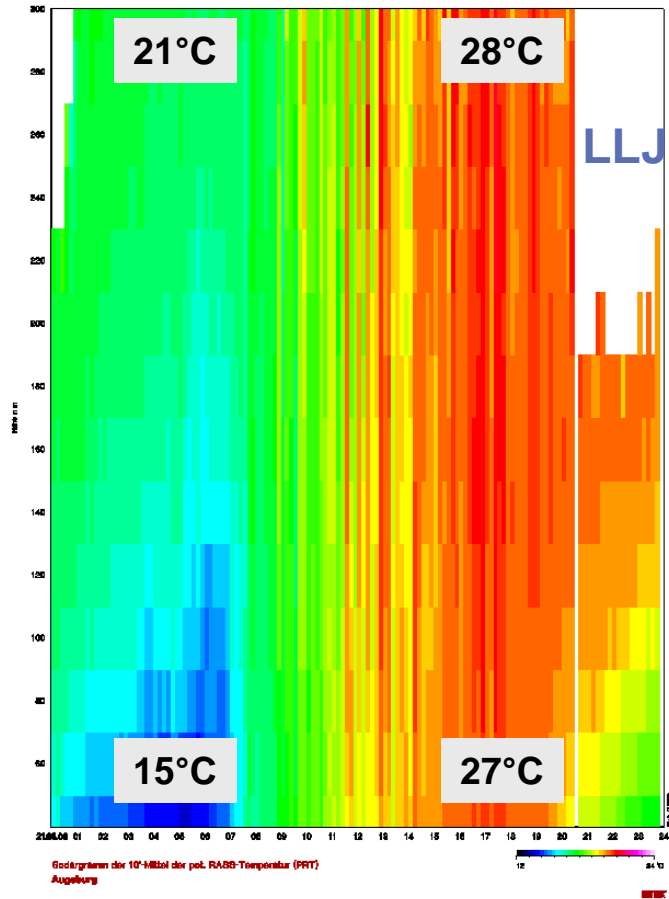
lowest

range gate: ca. 200 m

vertical range: 1000 m

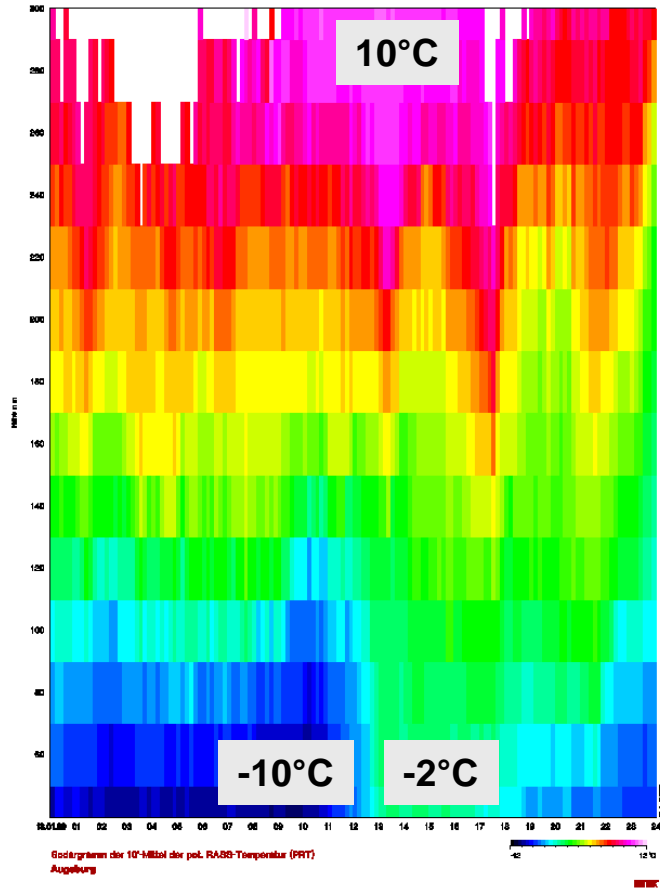
example RASS data: summer day potential temperature (left), horizontal wind (right)

300 m

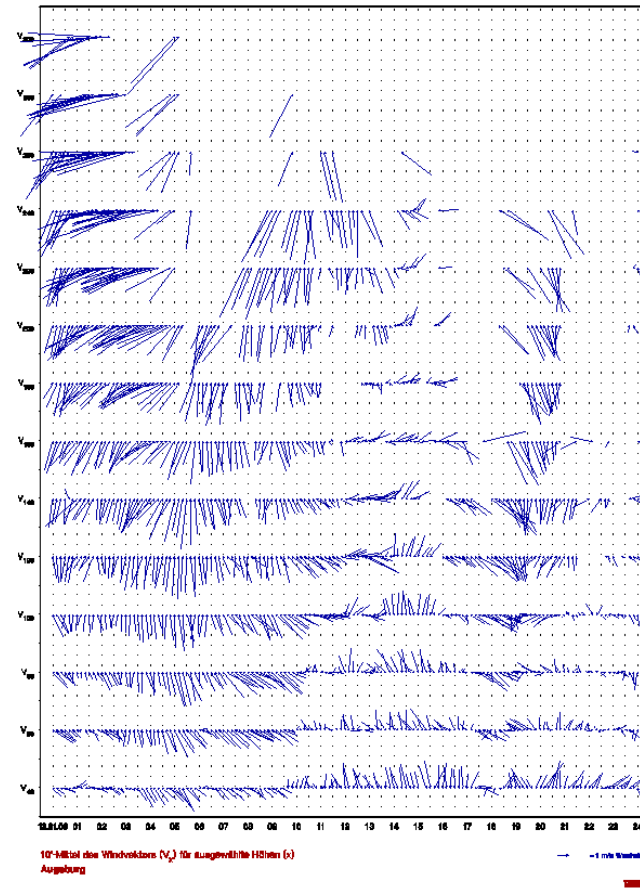


example RASS data: winter day potential temperature (left), horizontal wind (right)

300 m

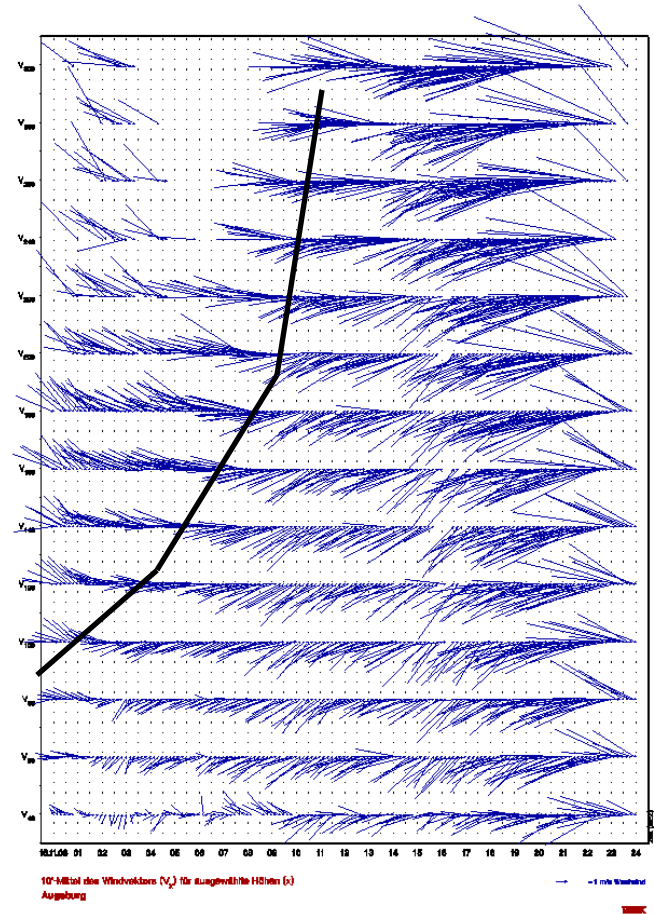
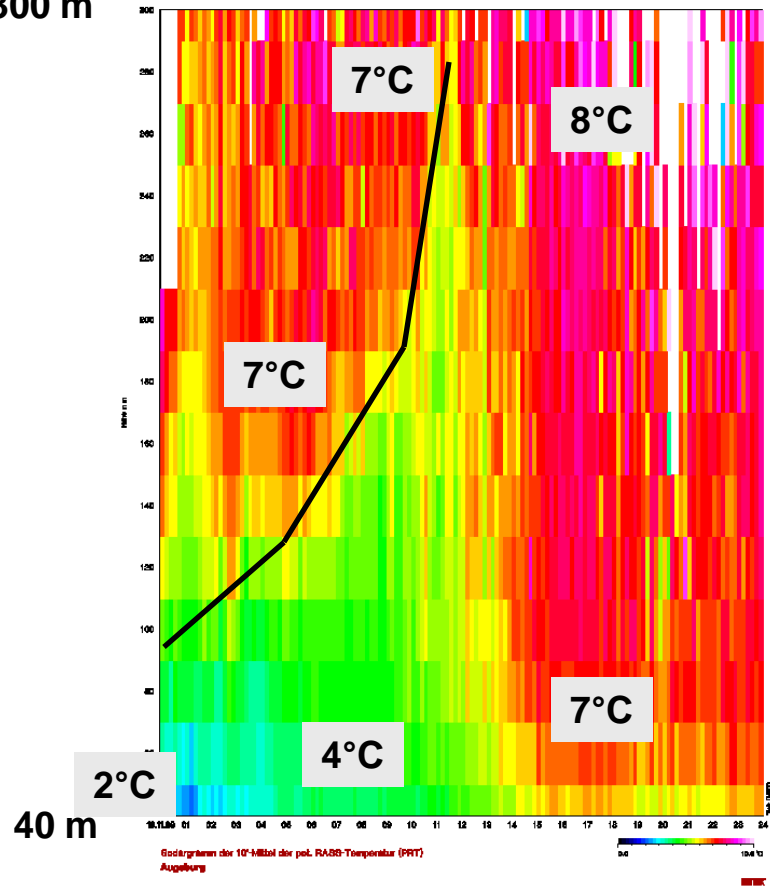


40 m



example RASS data: inversion potential temperature (left), horizontal wind (right)

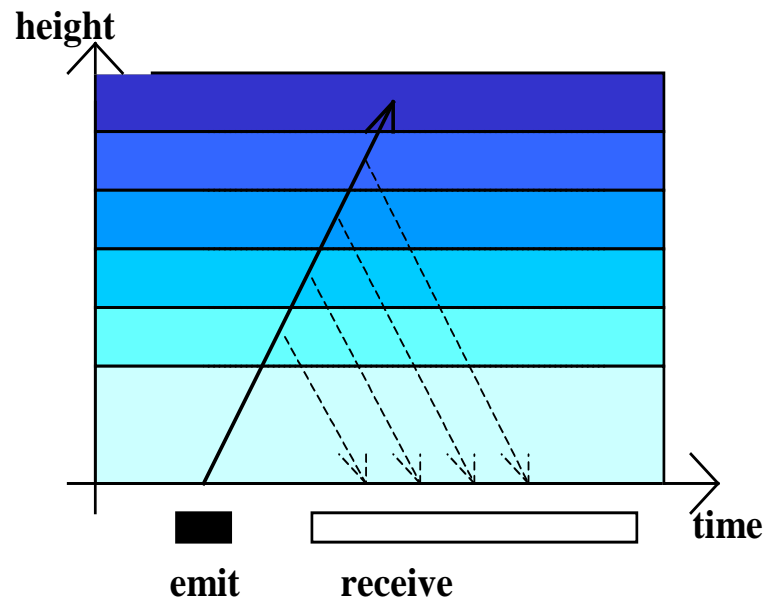
300 m



Doppler windlidar

**wind, turbulence, aerosol detection,
mixing-layer height, low-level jet**

Doppler windlidar measuring principle



detection:

travel time of signal	= height
backscatter intensity	= particle size and number distribution
depolarisation	= particle shape
Doppler-shift	= wind speed in the line of sight

mobile Doppler windlidar from Halo Photonics



sample data from
windlidar

April 16, 2010

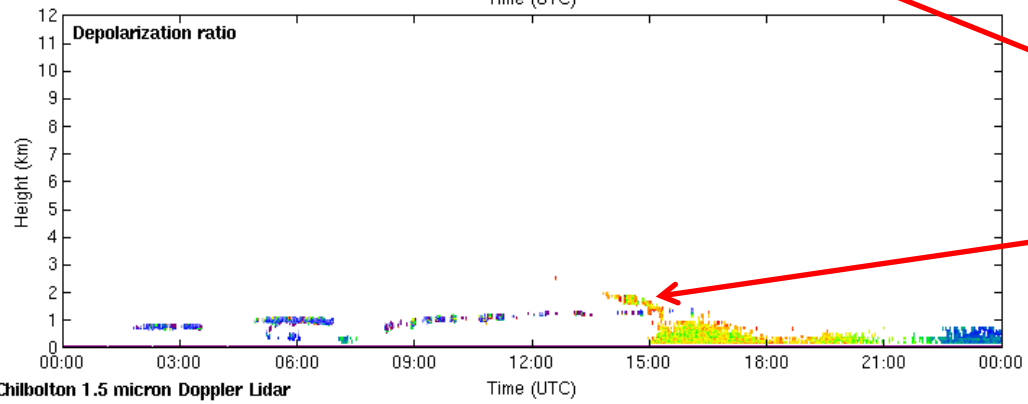
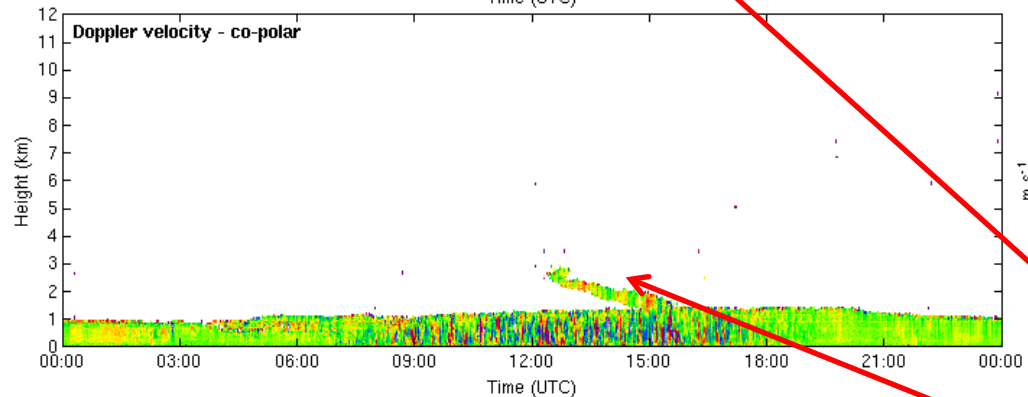
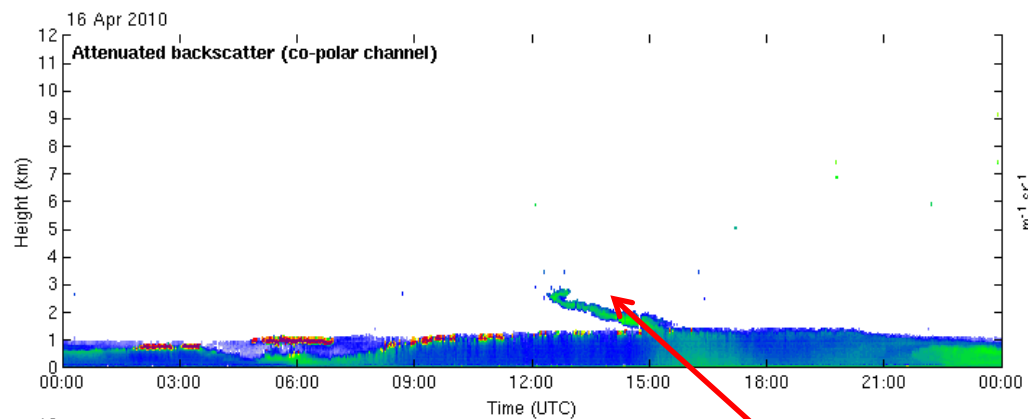
by
Univ. of Reading

taken at

Chilbolton, UK

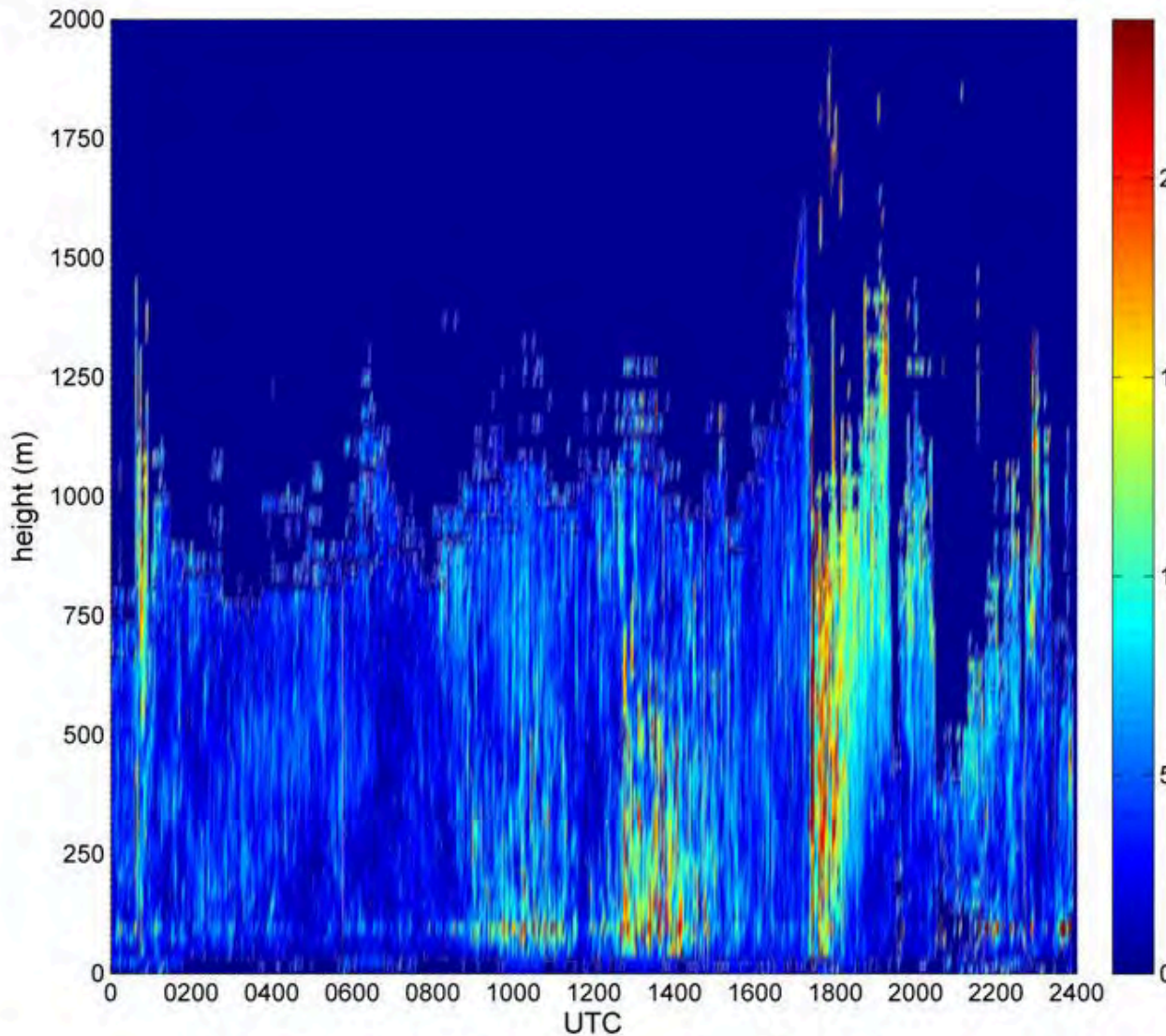
http://www.met.reading.ac.uk/radar/realtime/archive/doppler-lidar/20100416_chilbolton_halo-doppler-lidar.png

**volcanic ash
from
Eyjafjallajokull**



Chilbolton 1.5 micron Doppler Lidar

realtime data: <http://www.chilbolton.rl.ac.uk/weather/lidar.htm>



**sample data from
windlidar**

**wind speeds in m/s
(colour bar)**

June 22, 2011

by IMK-IFU

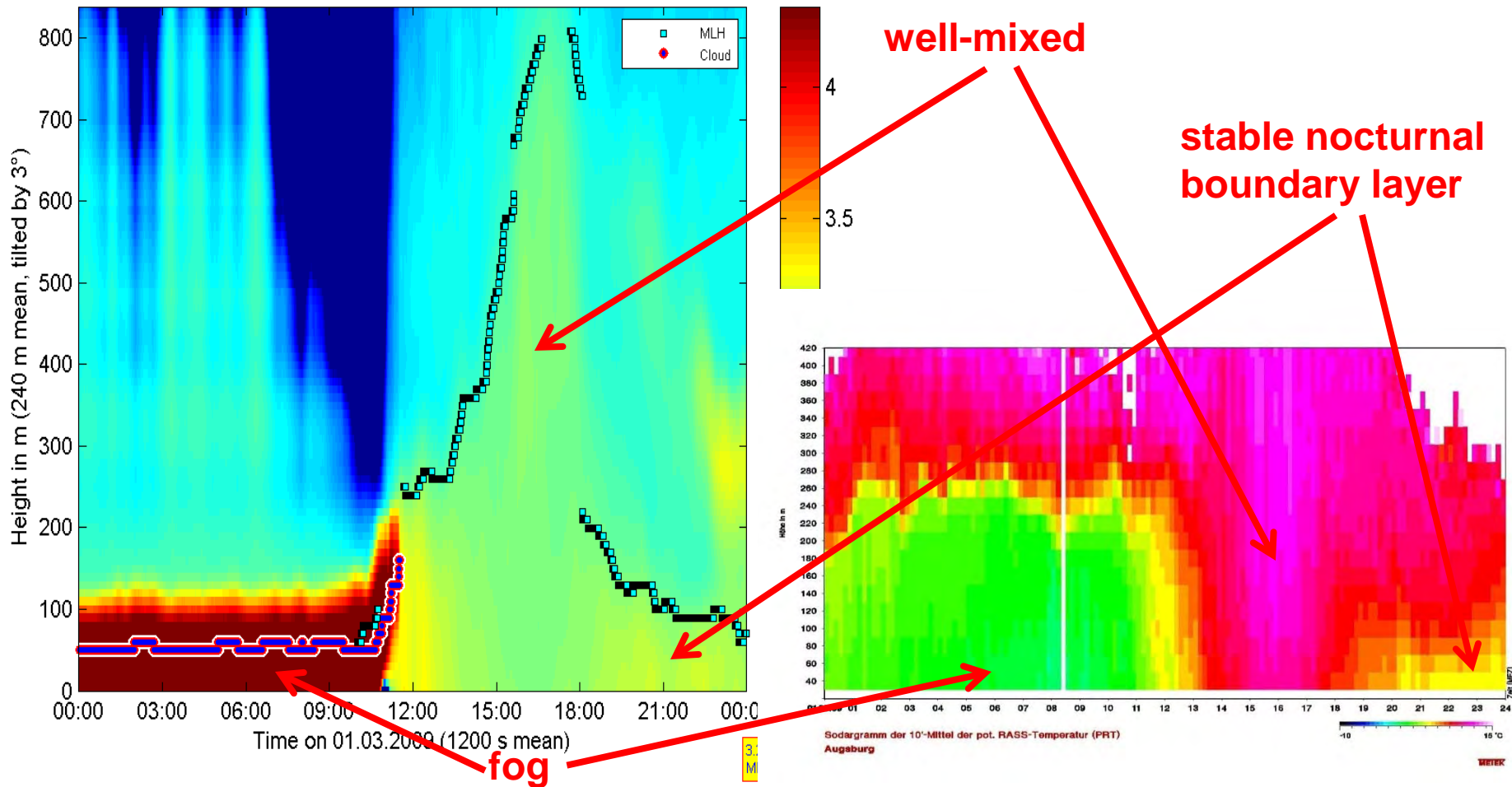
taken at

**Garmisch-Partenk.,
Germany**

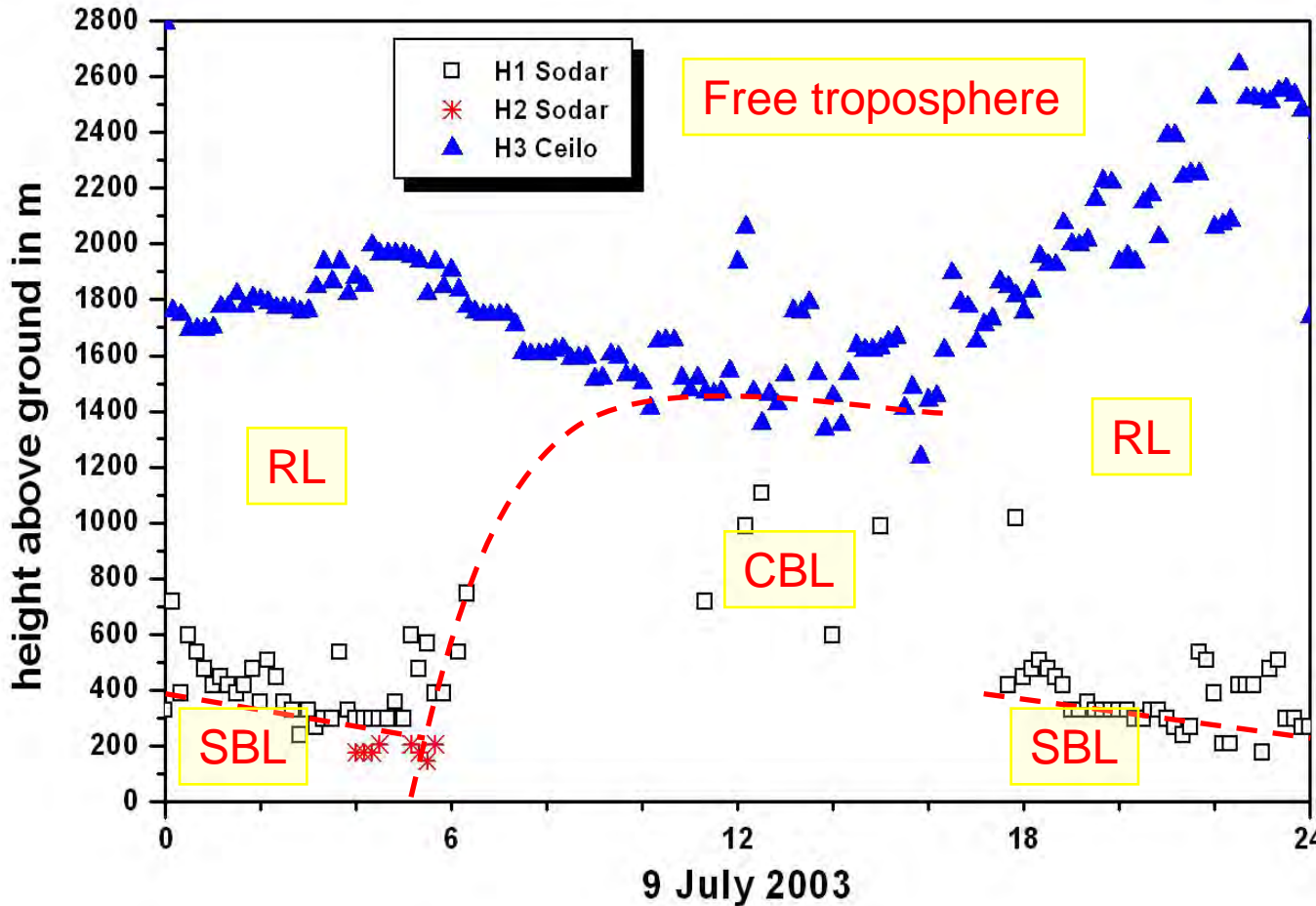
Comparisons between different instruments

comparison of RASS data (potential temperature, right) with aerosol backscatter from a ceilometer (left)

CL31 Augsburg AVA log₁₀ of backscatter with MLH on 01.03.2009 in 10⁻⁹ m⁻¹ sr⁻¹



Detection of the diurnal variation of PBL structure from SODAR and Ceilometer data taken in Budapest



SBL:

stable boundary layer (usually at night and in winter)

CBL:

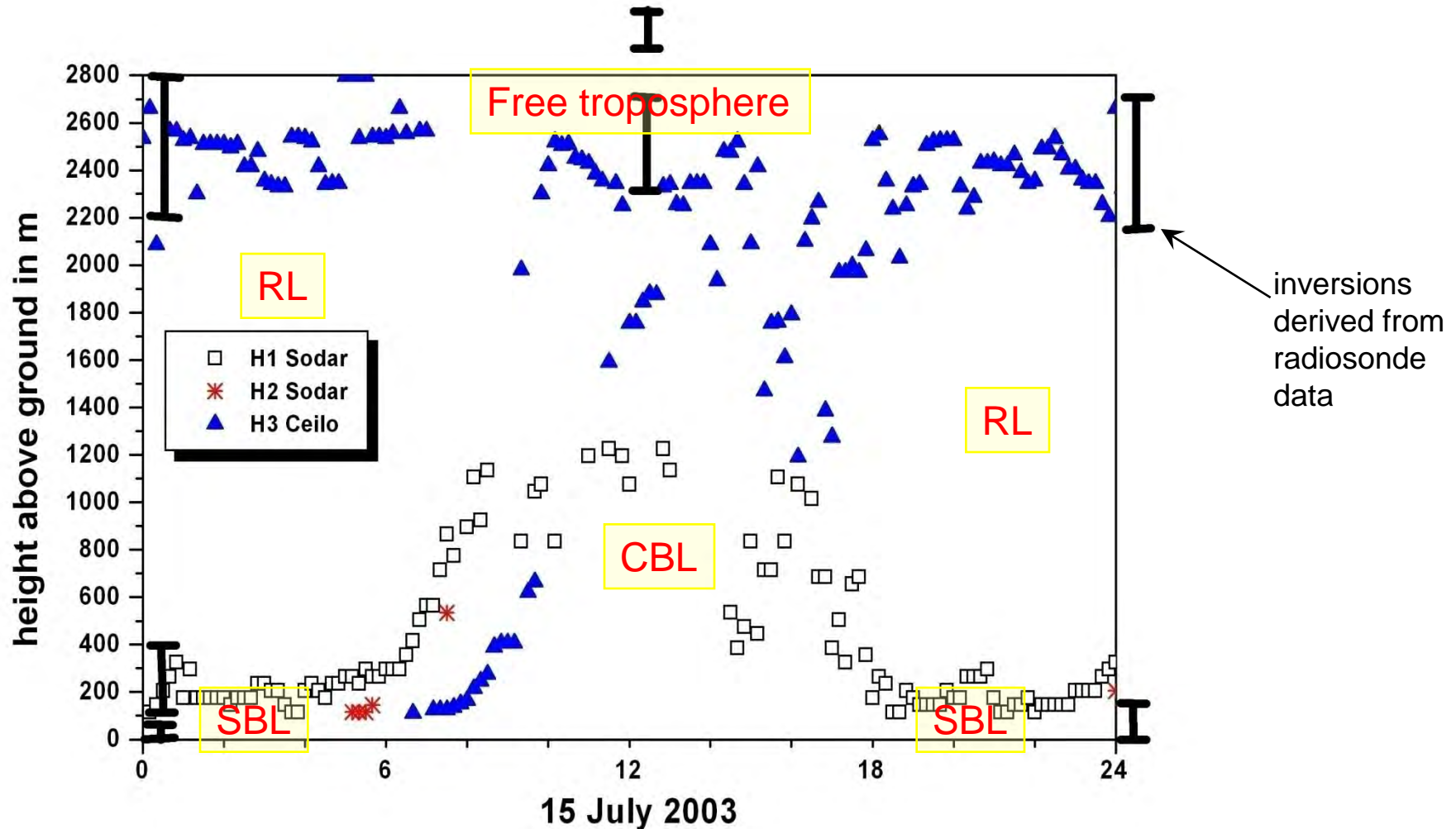
convective boundary layer (usually at daytime due to strong insolation)

RL:

residual layer (usually at night-time)

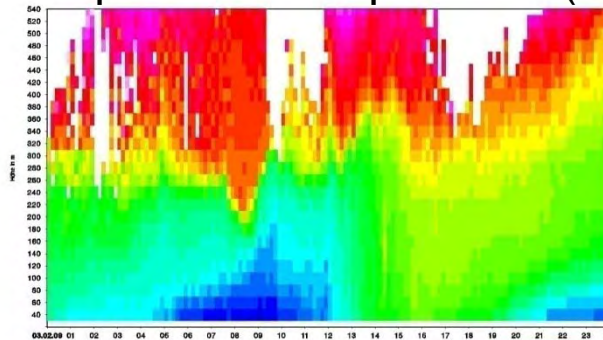
Emeis, S., K. Schäfer, 2006: Remote sensing methods to investigate boundary-layer structures relevant to air pollution in cities. *Bound.-Lay Meteorol.*, 121, 377-385,

Differences in MLH detection from SODAR and Ceilometer data taken in Budapest



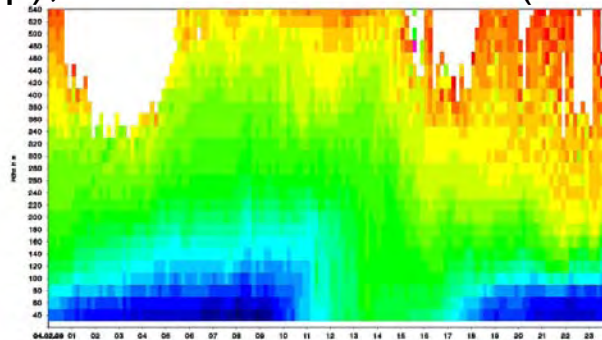
Emeis, S., K. Schäfer, 2006: Remote sensing methods to investigate boundary-layer structures relevant to air pollution in cities. *Bound.-Lay Meteorol.*, 121, 377-385,

potential temperature (top), backscatter SODAR (middle), Ceilometer (bottom)



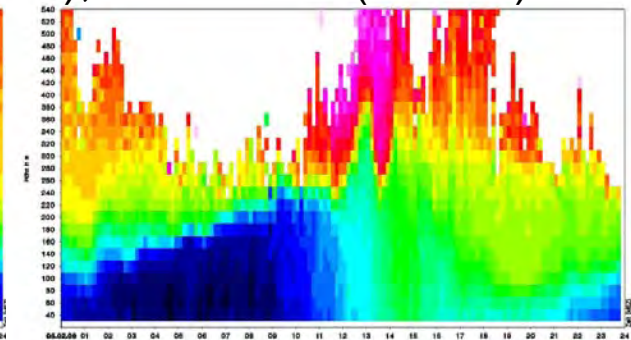
Sodagramm der 10'-Mittel der pot. RASS-Temperatur (PRT)
Augsburg

Feb. 3



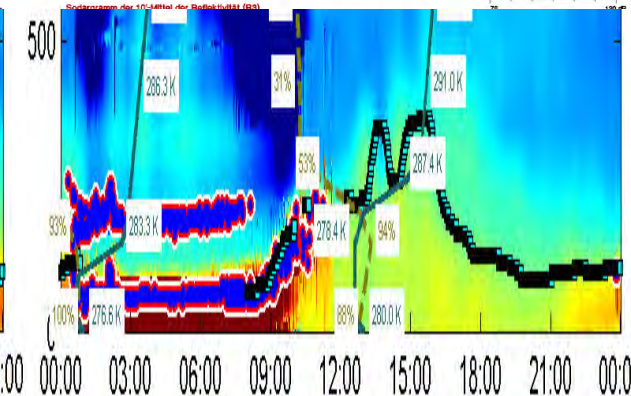
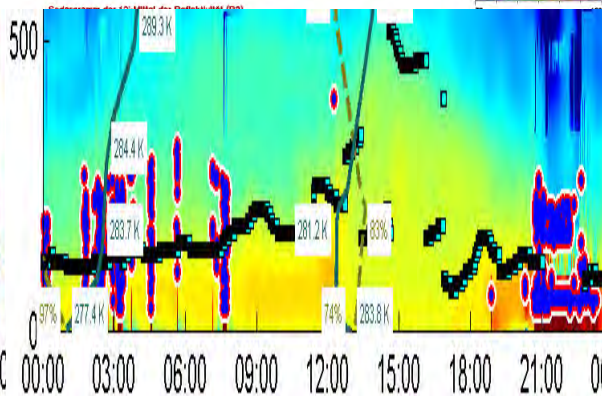
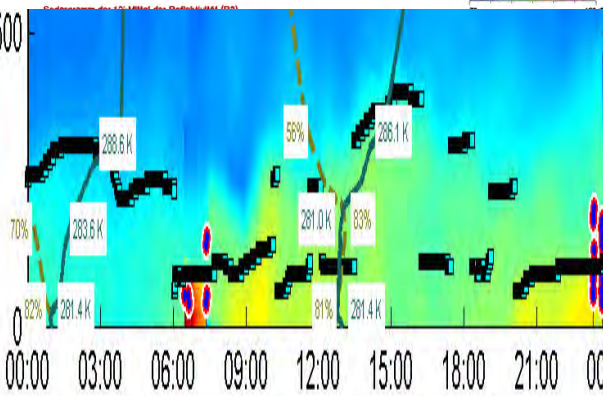
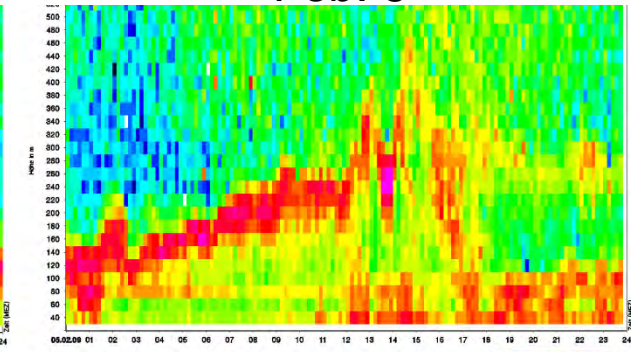
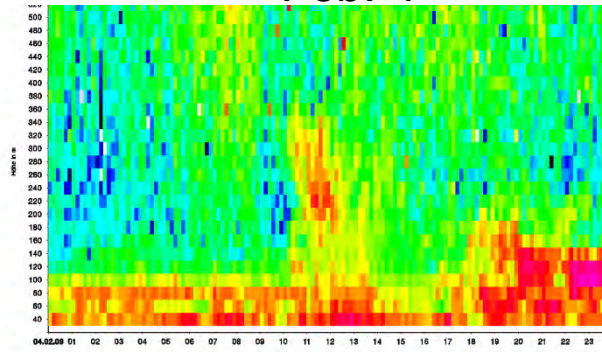
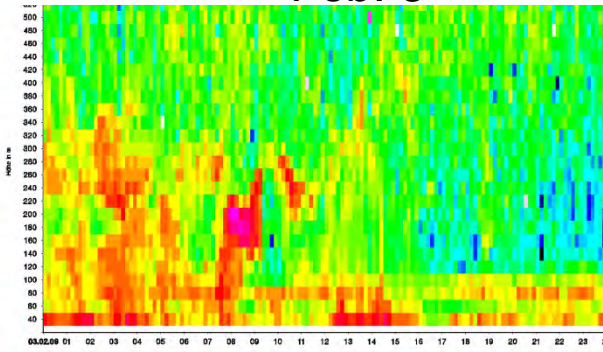
Sodagramm der 10'-Mittel der pot. RASS-Temperatur (PRT)
Augsburg

Feb. 4

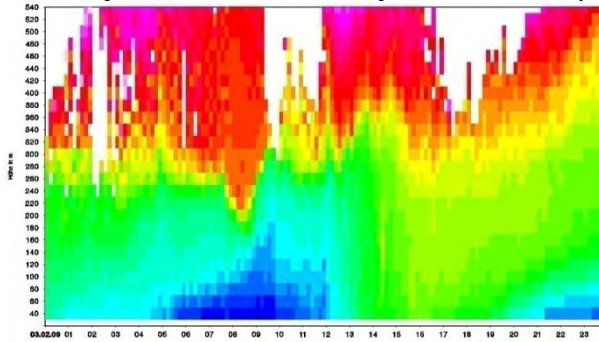


Sodagramm der 10'-Mittel der pot. RASS-Temperatur (PRT)
Augsburg

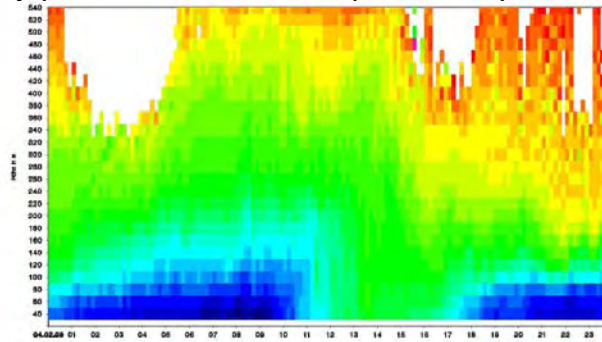
Feb. 5



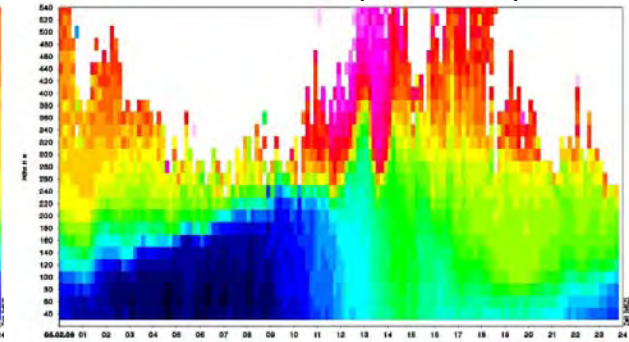
potential temperature (top), MLH RASS (middle), MHL SODAR/Ceilo (bottom)



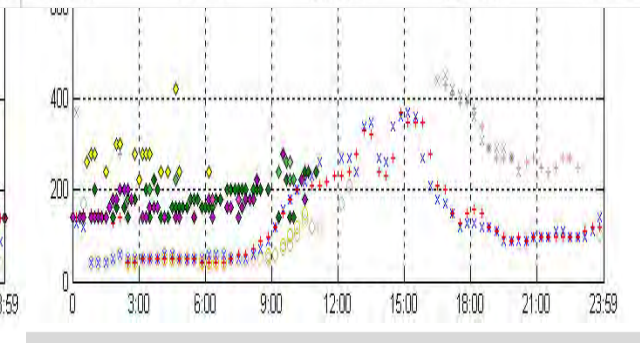
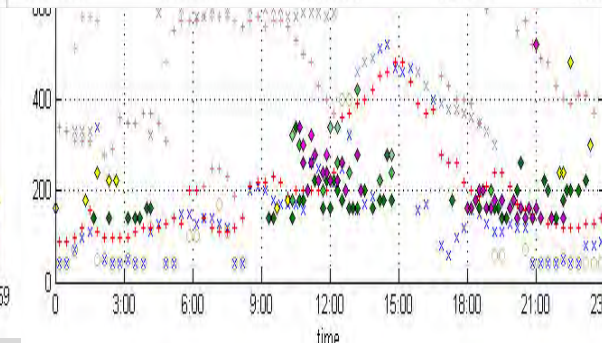
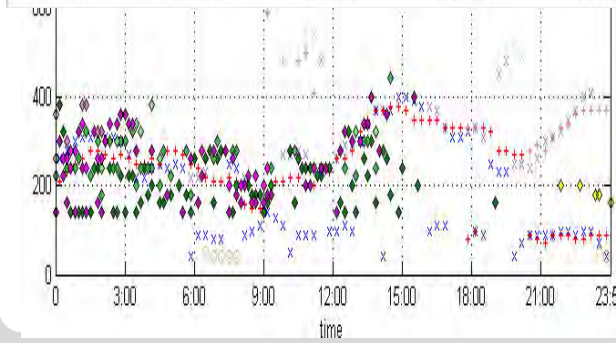
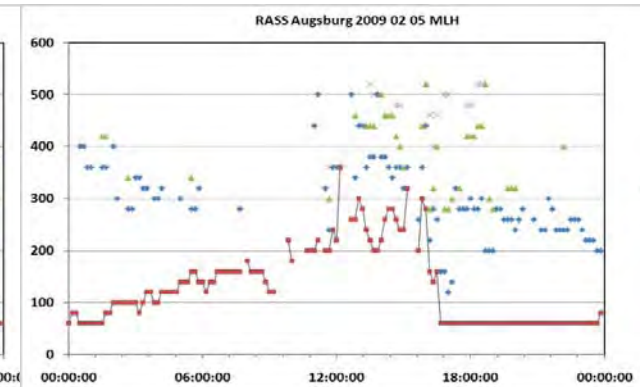
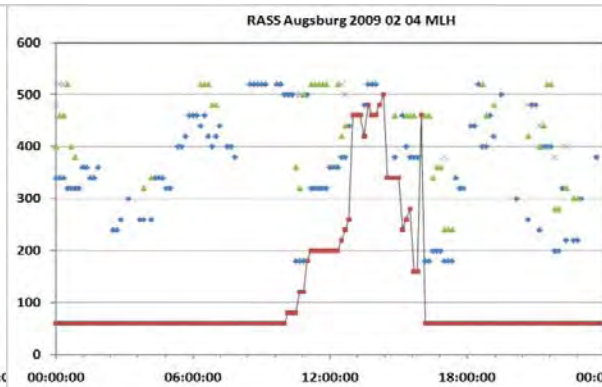
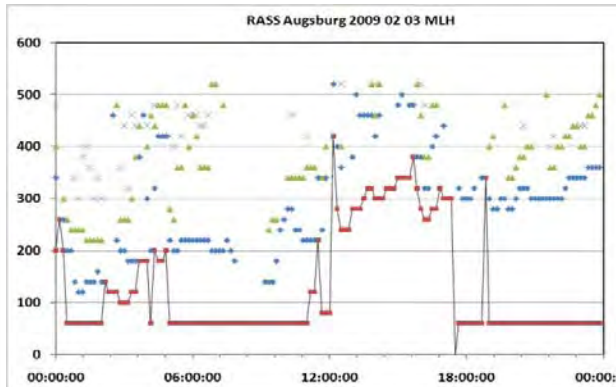
Feb. 3



Feb. 4



Feb. 5



Summary

Clicker question:

Which instrument is best?

- A sodar**
- B ceilometer**
- C wind lidar**
- D RASS**
- E don't know**

quality criteria:

data availability

vertical range

direct/indirect detection

Doppler analysis

☺ ☺ ☺ ☹️* **RASS** delivers temperature profiles, wind profiles are additionally available.
MLH directly from temperature profiles. LLJ from wind profiles.
Does not work properly under high wind speeds. Restricted range.

☺ ☺ ☺ ☹️* **wind lidar** detects wind profiles, aerosol distribution and water droplets.
 It has to be assumed that the aerosol follows the thermal structure of the atmosphere and the wind.
MLH from aerosol backscatter, wind speed variance, LLJ from wind profiles.
Does not work properly in extreme clear (aerosol-free) air and during precipitation events and fog.

☺ ☺ ☹️*☹️* **Ceilometer** detects aerosol distribution and water droplets. It has to be assumed that the aerosol follows the thermal structure of the atmosphere.
MLH indirectly from aerosol backscatter using a MLH algorithm.
Does not work properly in extreme clear (aerosol-free) air and during precipitation events and fog.

☺ ☹️*☹️*☹️* **SODAR** detects wind profiles, temperature fluctuations and gradients, but no absolute temperature.
MLH indirectly from acoustic backscatter (MLH algorithm). LLJ from wind profiles.
Does not work properly under perfectly neutral stratification, with very high wind speeds, and during stronger precipitation events. Restricted range.

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Emeis, S., 2012: Wind Energy Meteorology - Atmospheric physics for wind power generation. Springer Heidelberg etc., to appear in autumn 2012.

boundary-layer remote sensing with application examples:

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overview on the entire range of meteorological measurement methods:

Emeis, S., 2010: Measurement Methods in Atmospheric Sciences. In situ and remote. Series: Quantifying the Environment Vol. 1. Borntraeger Stuttgart. XIV+257 pp., 103 Figs, 28 Tab. ISBN 978-3-443-01066-9.

Horns Rev wake clouds explained

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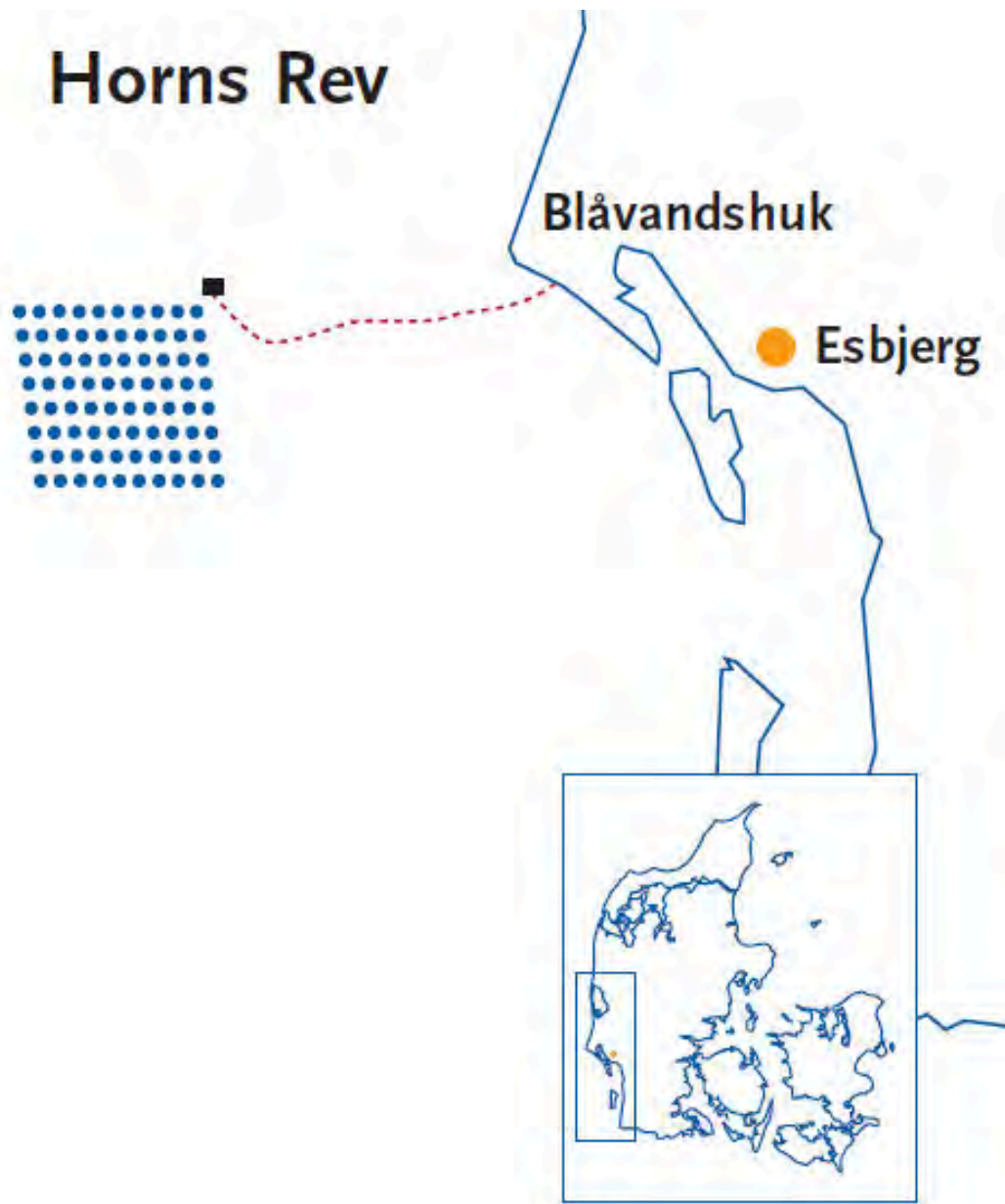
INSTITUTE OF METEOROLOGY AND CLIMATE RESEARCH, Atmospheric Environmental Research



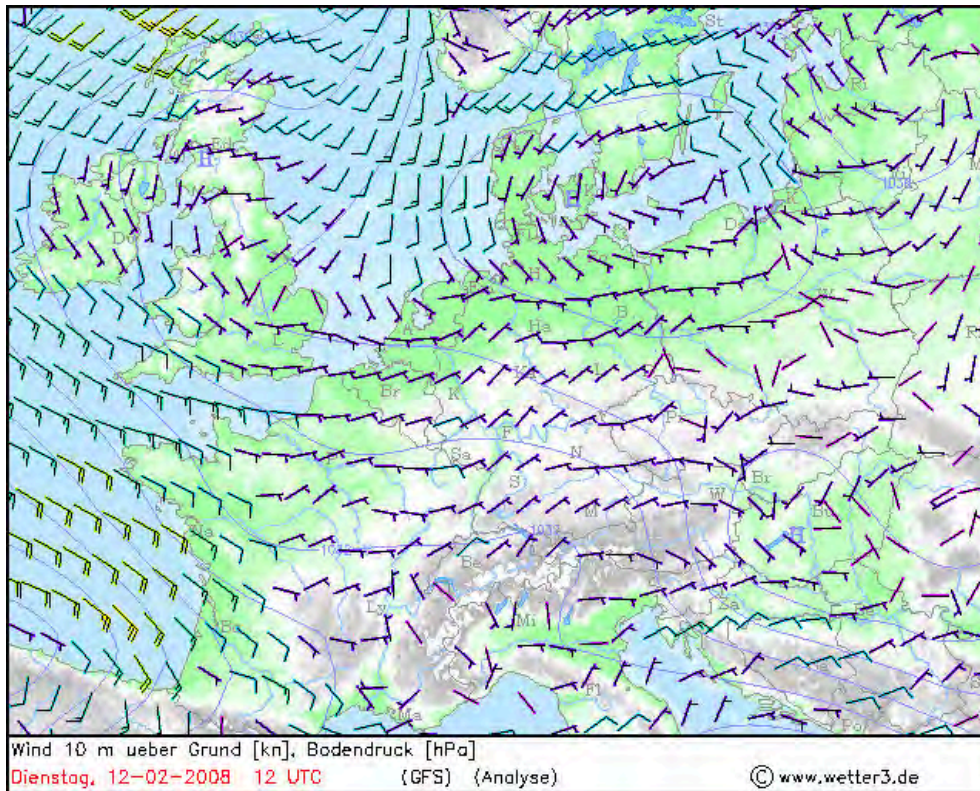


Photo: Vattenfall/C. Steiness

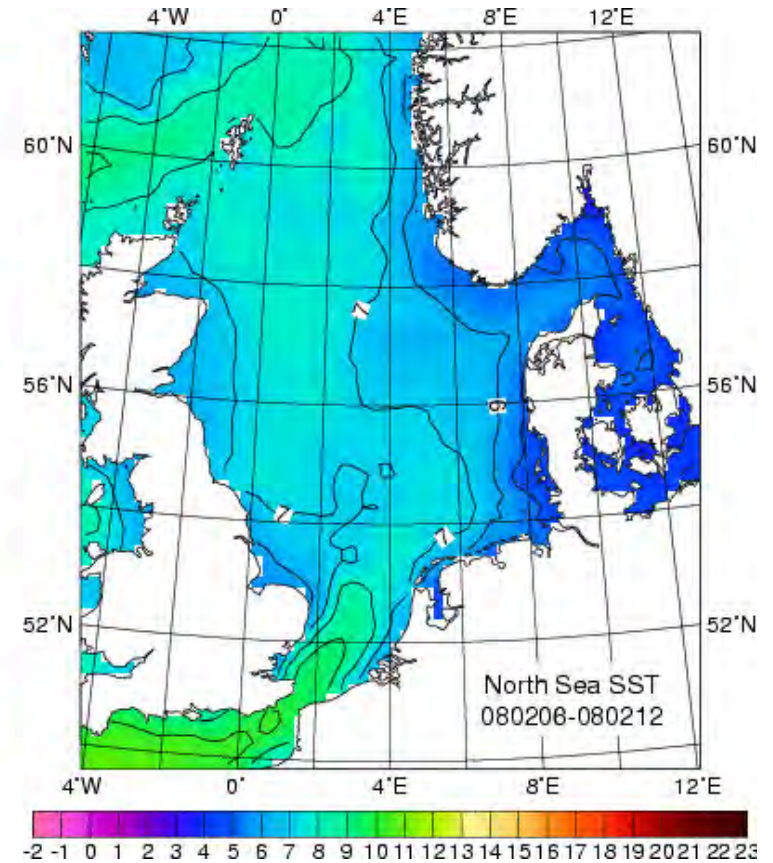
Horns Rev



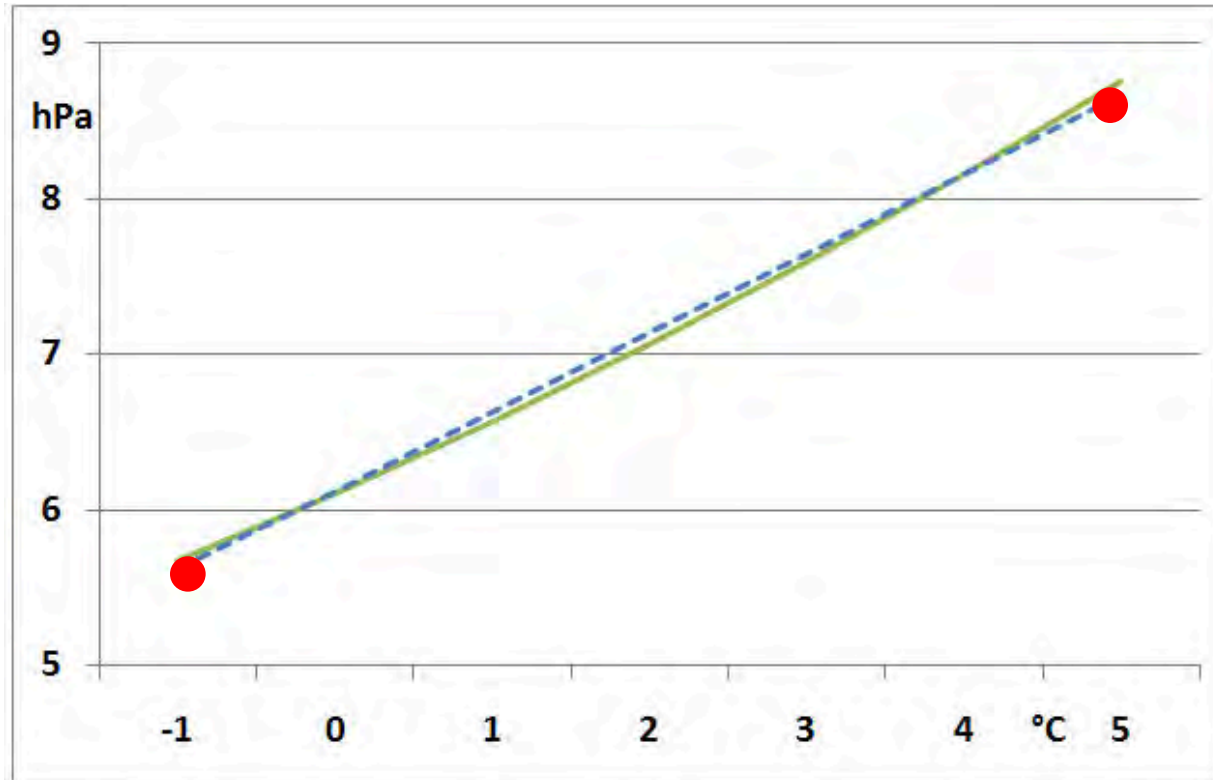
10 m wind



SST (°C)



explanation of wake clouds: mixing fog on February 12, 2008



air directly over the water:

air at hub height:

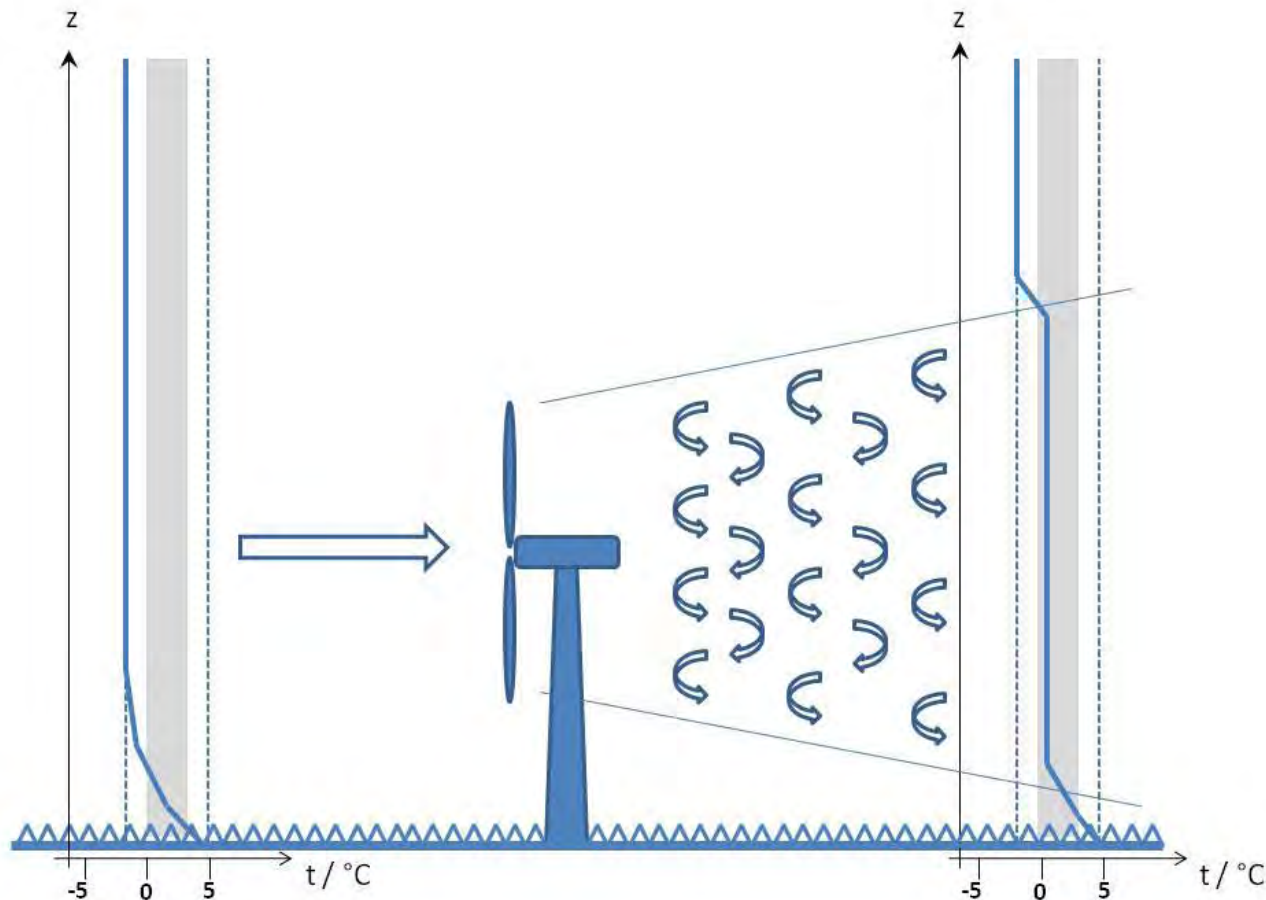
after mixing:

5°C, more than 99% relative humidity

-1°C, more than 99% relative humidity

2°C, above 101% humidity → clouds

explanation of wake clouds: mixing fog on February 12, 2008



air directly over the water:
 air at hub height:
 after mixing:

5°C, more than 99% relative humidity
 -1°C, more than 99% relative humidity
 2°C, above 101% humidity → clouds



Photo: Vattenfall/C. Steiness



Photo: Vattenfall/C. Steiness

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http://www.dewi.de/dewi/fileadmin/pdf/publications/Magazin_37/07.pdf

**Thank you very
much for your
attention**

