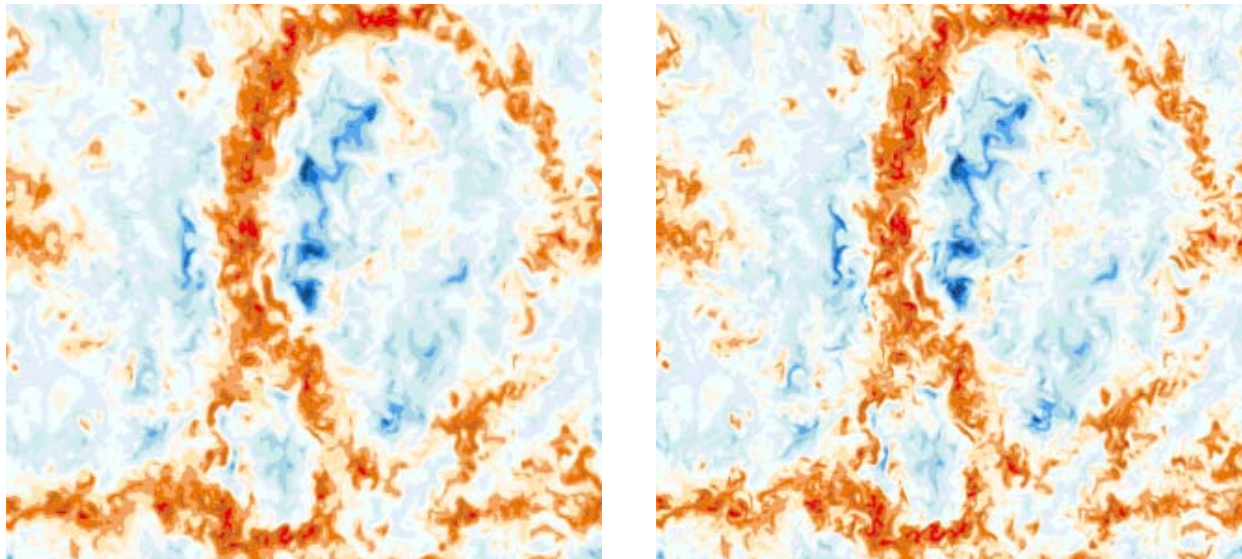


Vertical Grid Nesting For Improved Surface Layer Resolution In Large-Eddy Simulation

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INSTITUTE OF METEOROLOGY AND CLIMATE RESEARCH, ATMOSPHERIC ENVIRONMENTAL RESEARCH, IMK-IFU
Transport Processes in the Atmospheric Boundary Layer.

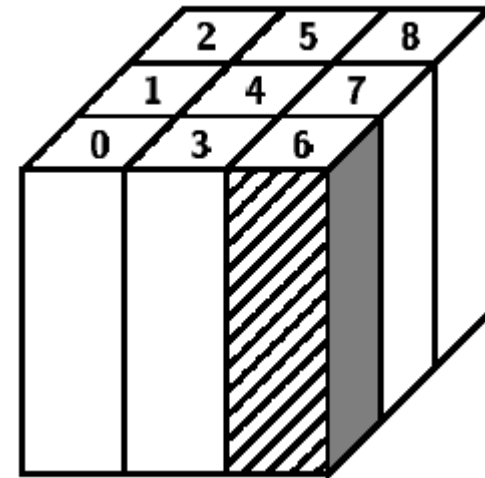


LES: Hardware limitation

- Reynolds numbers of order 10^7 are commonly encountered in the ABL
- Number of grid points required to resolve the energy containing eddies is known to be in the range of $Re^{1.76}$
- Total number of grid points of order 10^{12} are required
- LES of atmospheric flows with high resolution in the surface layer are not feasible yet
- Number of grid points can be reduced using grid nesting approach

Parallelized Large-Eddy Simulation Model (PALM)

- Non-hydrostatic incompressible Boussinesq equations
- SGS turbulence is modeled according to Deardoff (1980)
- Monin-Obukhov similarity is assumed between the surface and the first computational grid point
- Third order three stage Runge-Kutta scheme for time discretization
- 2-D domain decomposition
- Arakawa-C Grid

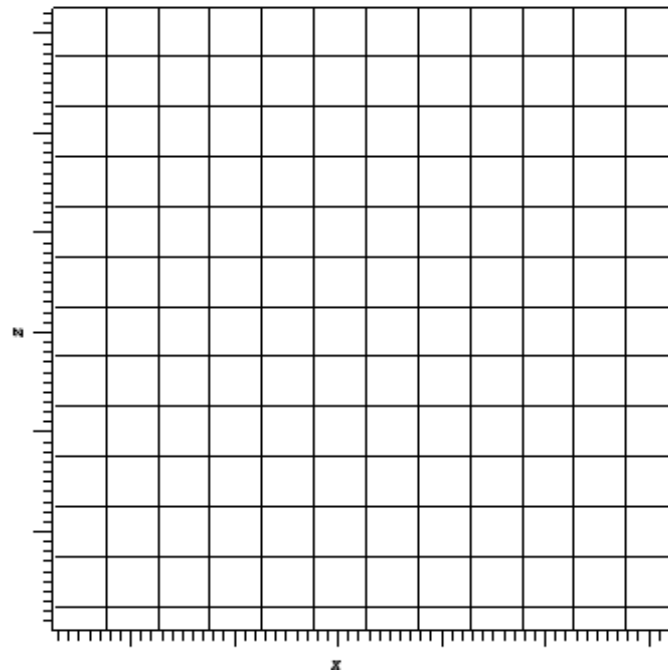


S. Raasch and M. Schröter, Meteorologische Zeitschrift, 2001

Nested Grid Approach

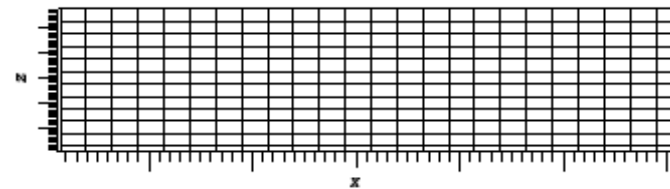
- Horizontal grid nesting is common in numerical weather prediction models
- Vertical grid nesting studies: Sullivan et al. 1996 and PALM Group - University of Hannover, 2003

Coarse Grid



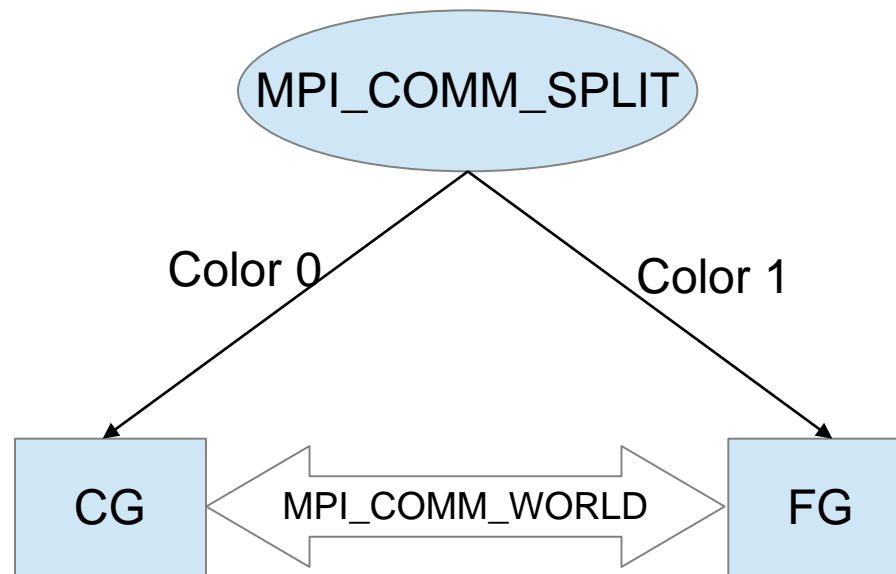
- Equal horizontal extent
- Cyclic lateral Boundary Conditions (BC)
- Integer nesting ratio

Fine Grid



MPI Coupling Strategy

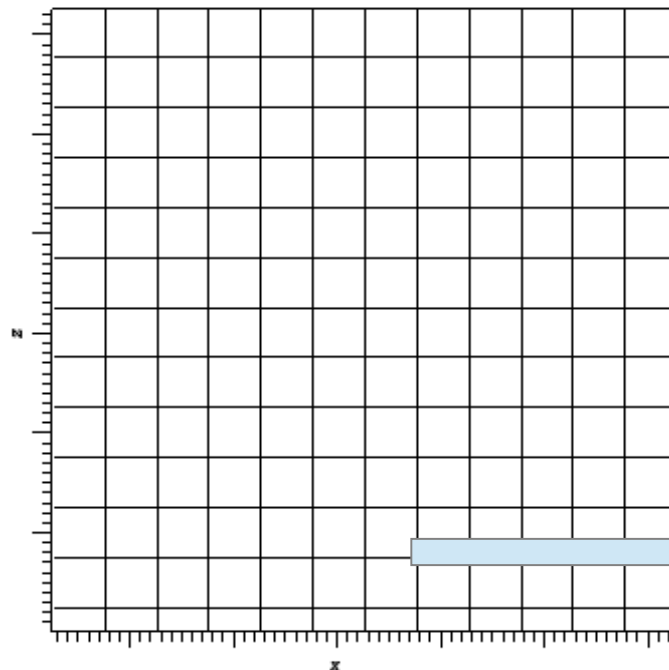
- MPI-1 standards adopted (no processor spawning)
- MPI_COMM_SPLIT to distribute the available processor cores between Fine Grid (FG) and Coarse Grid (CG) groups.



Interpolation

- Initialize the Fine Grid (prognostic variables & surface fluxes)
- To set top Boundary Conditions for the Fine Grid.
 - Dirichlet: Horizontal velocities and potential temperature

■ Scheme: Clark and Farley (1984)

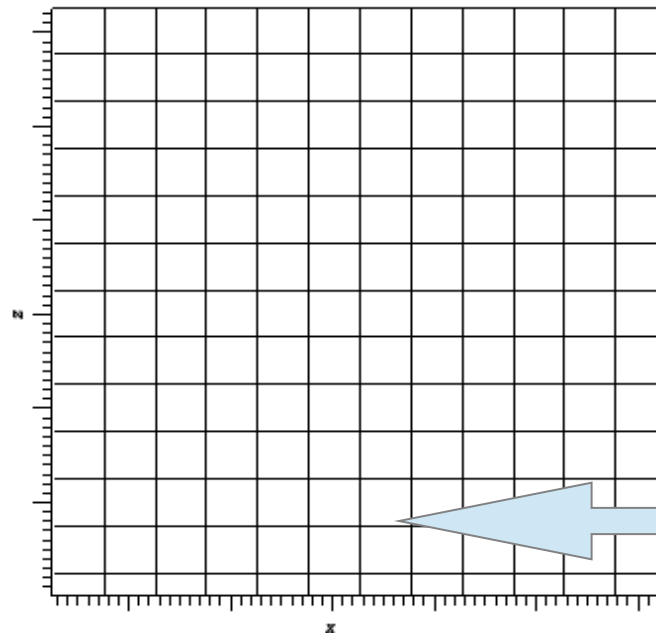


$$\begin{aligned} \phi_k &= E_{i-1}^k \Phi_{i-1} + E_i^k \Phi_i + E_{i+1}^k \Phi_{i+1} \\ E_{i-1}^k &= \frac{\epsilon_k (\epsilon_k - 1)}{2} + \alpha \\ E_i^k &= (1 - \epsilon_k^2) - 2\alpha \\ E_{i+1}^k &= \frac{\epsilon_k (\epsilon_k + 1)}{2} + \alpha \\ \epsilon_k &= \frac{(2k - 1)\Delta x - \Delta X}{2\Delta X} \quad k = 1, \dots, n \\ \alpha &= \frac{\left(\frac{\Delta x}{\Delta X}\right)^2 - 1}{24} \end{aligned}$$

Anterpolation

■ Weighted averaging of the FG data to the CG in the overlapping region

■ TKE Germano identity $E = \tilde{e} + \frac{1}{2} (\overline{u_i \tilde{u}_i} - \tilde{u}_i \tilde{u}_i)$

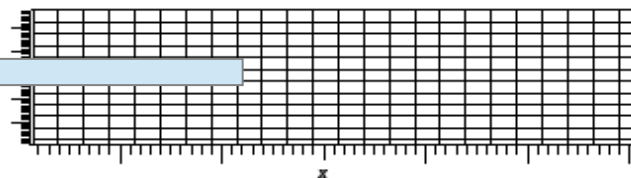


$$\Phi = \tilde{\phi} = \sum_{i=1}^{nx} \sum_{j=1}^{ny} \sum_{k=1}^{nz} \bar{\phi}_{i,j,k} \frac{\Delta x}{\Delta X} \frac{\Delta y}{\Delta Y} \frac{\Delta z}{\Delta Z}$$

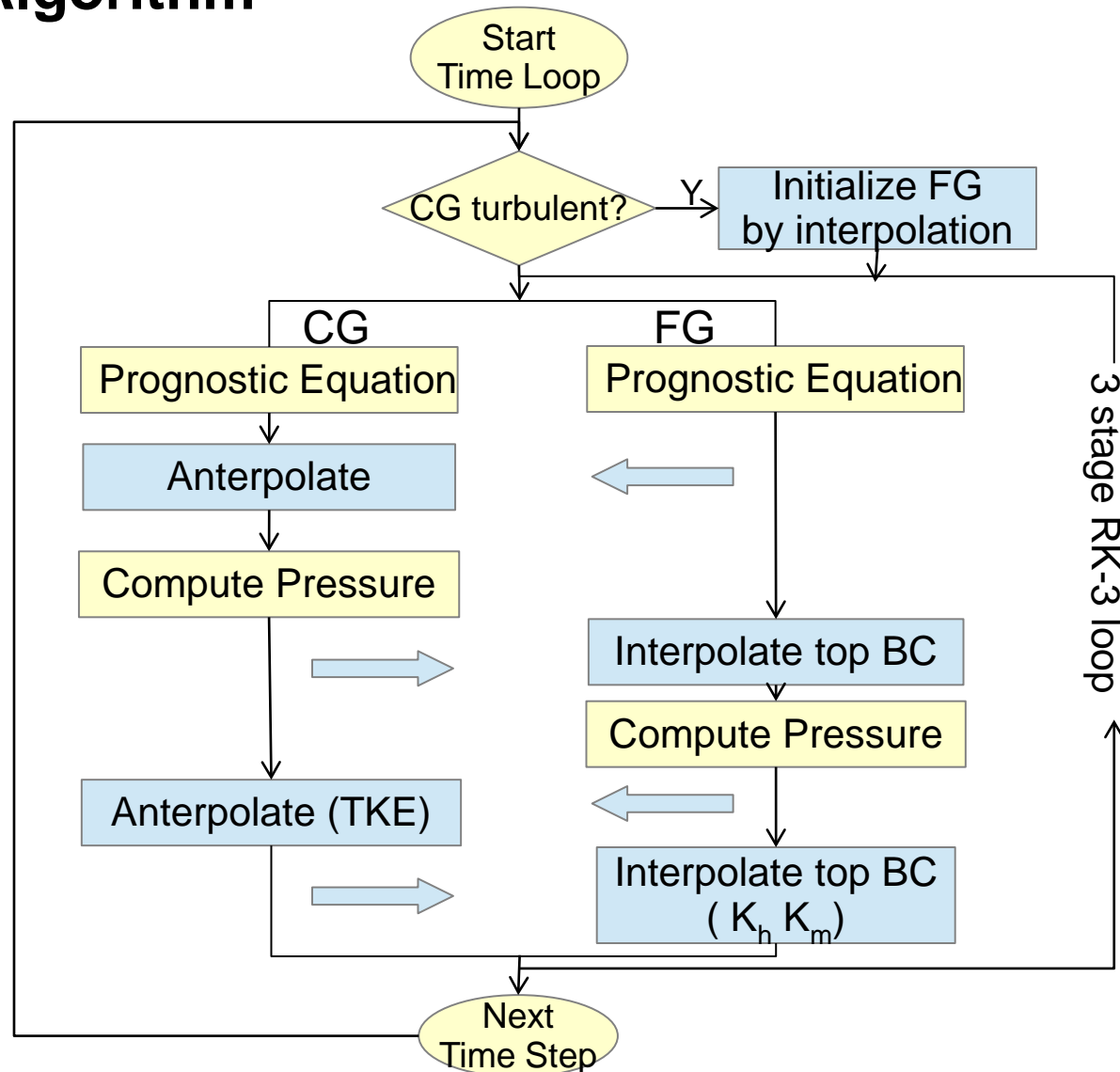
$$U = \tilde{u} = \sum_{j=1}^{ny} \sum_{k=1}^{nz} \bar{u}_{i,j,k} \frac{\Delta y}{\Delta Y} \frac{\Delta z}{\Delta Z}$$

$$V = \tilde{v} = \sum_{i=1}^{nx} \sum_{k=1}^{nz} \bar{v}_{i,j,k} \frac{\Delta y}{\Delta Y} \frac{\Delta z}{\Delta Z}$$

$$W = \tilde{w} = \sum_{i=1}^{nx} \sum_{j=1}^{ny} \bar{w}_{i,j,k} \frac{\Delta x}{\Delta X} \frac{\Delta y}{\Delta Y}$$



Nesting Algorithm



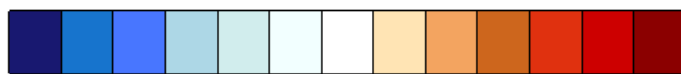
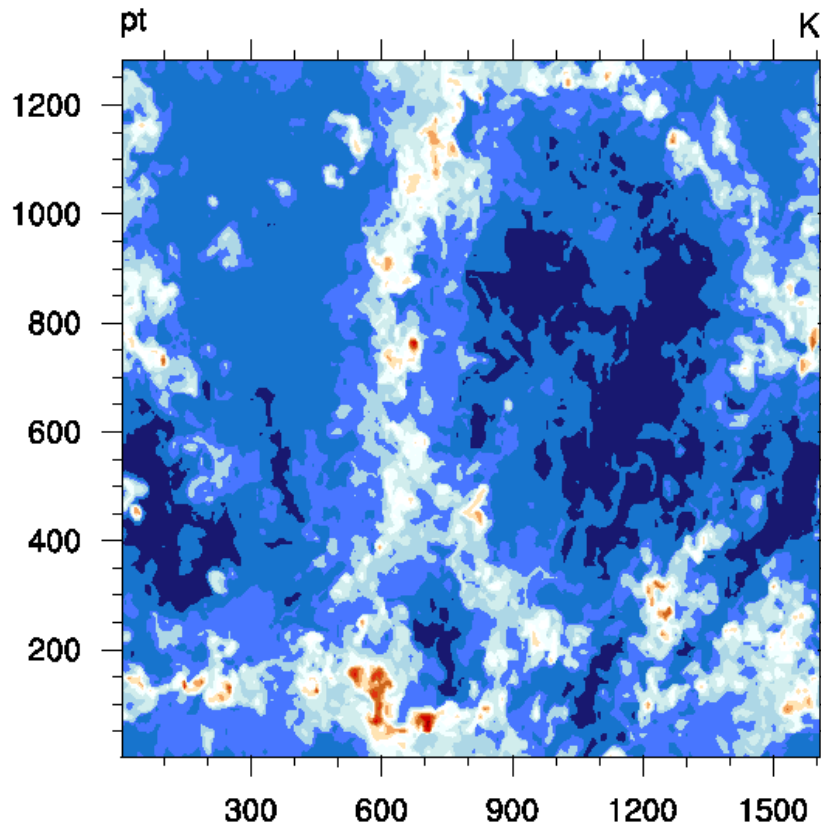
Test Case

- Domain Size: 1.6 x 1.28 x 1.2 km
- Fine grid vertical extent: 200 m
- Surface Heat flux varied sinusoidally between of 0.08 and 0.12 K m /s
- Simulated Time: 2 hr

	No. of Grid Points	$\Delta x, \Delta y, \Delta z$	CPU cores	Wall time
Coarse Grid	200 x 160 x 300 = 9.6 M	8, 8, 4	80	5.5 hrs
Fine Grid (Nesting ratio: 2)	400 x 320 x 100 = 12.8 M	4, 4, 2	160	5.5 hrs
Reference	400 x 320 x 600 = 76.8 M	4, 4, 2	200	9.3 hrs

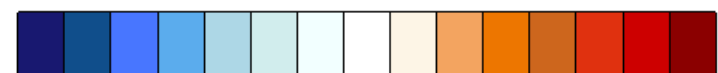
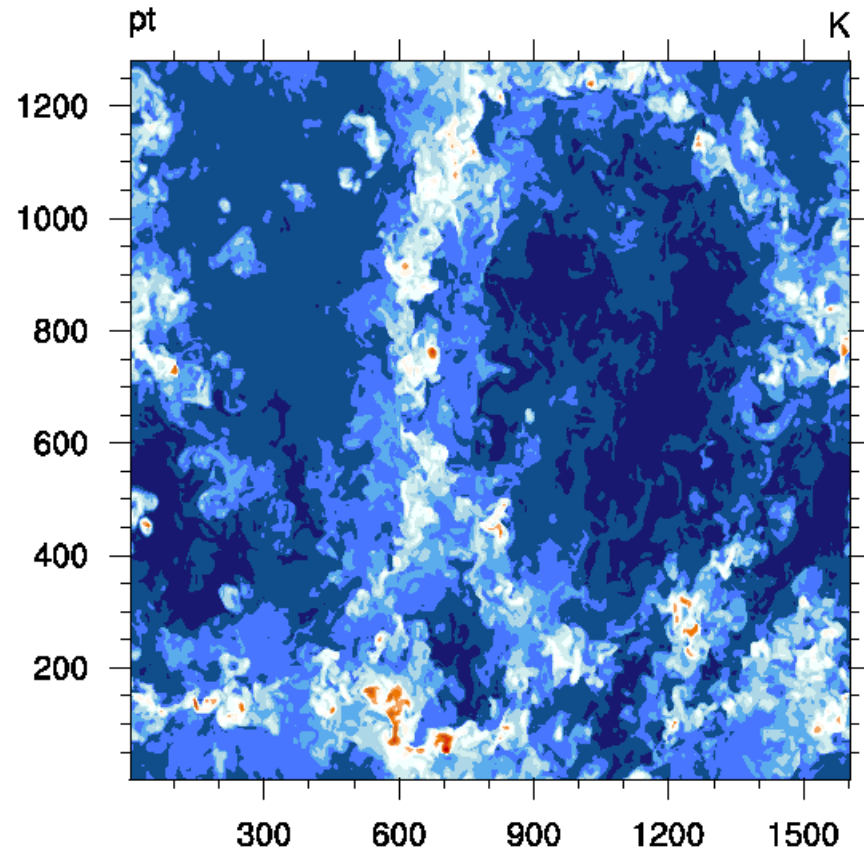
Results: Potential Temperature at 100m

CG: 2 hr



300.8 301 301.2 301.4 301.6 301.8

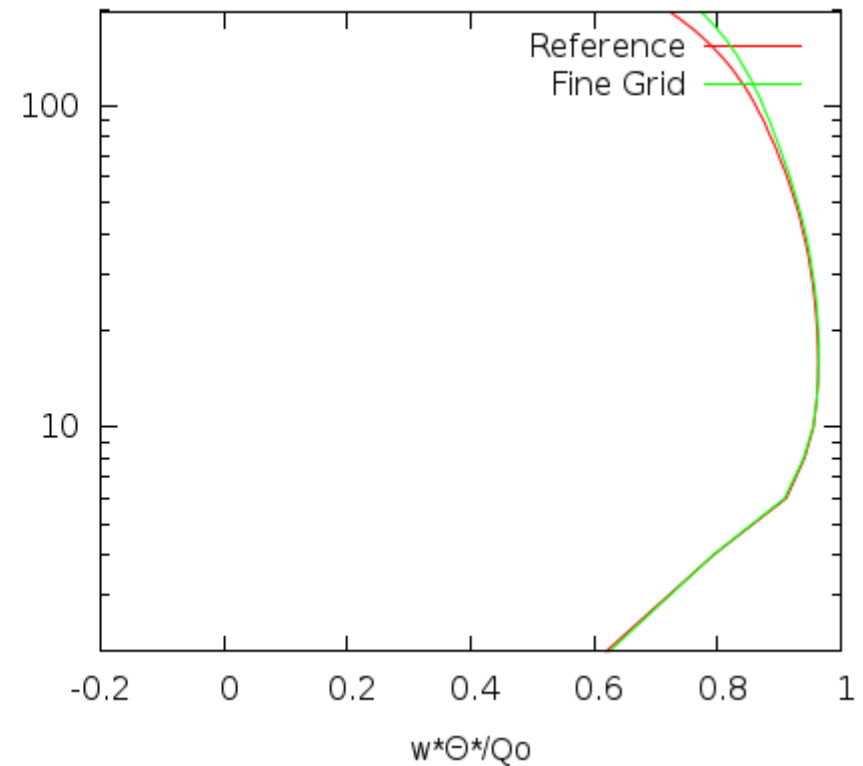
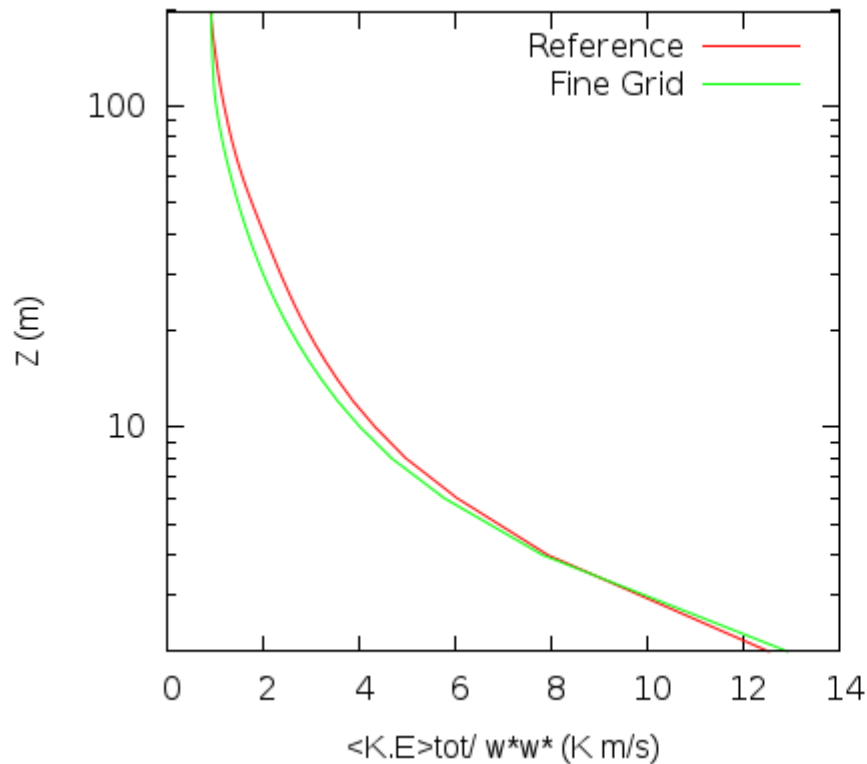
FG: 2 hr



300.8 301 301.2 301.4 301.6 301.8 302

Results: T.K.E and Heat Flux

Averaged profiles after 2 hour simulation



Future Work

- Evaluate speed-up for large-scale simulations
- Identify optimal nesting ratio and processor distribution between CG & FG
- Include topography / surface heterogeneities
- Alternative interpolation and coupling strategy
- “Sponge” Layer

Thank you for listening.

