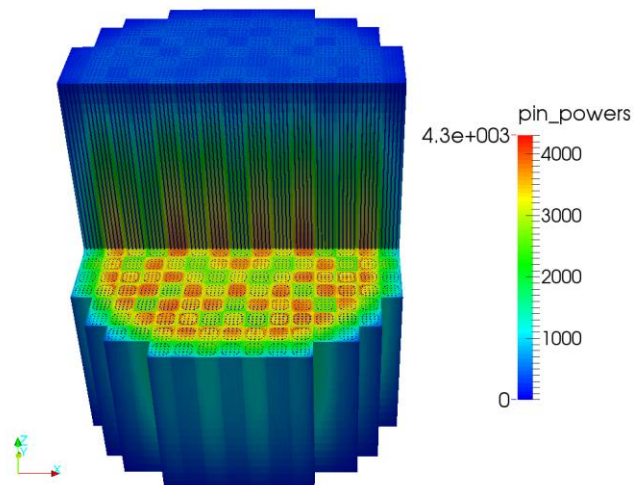


# Demonstration of Full PWR Core Coupled Monte Carlo Neutron Transport and Thermal-Hydraulic Simulations Using Serpent 2/ SUBCHANFLOW

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# Outline

1. Internal coupling between Serpent 2 and SUBCHANFLOW
2. Stochastic mixing fall back for TMS method
3. Channel and sub-channel TH solution verification
4. Full PWR Core Coupled Monte Carlo Neutron Transport and Thermal-Hydraulic Simulation

# Thermal-hydraulic feedback modeling in Serpent

- ‚Half-internal‘ universal multi-physics interface
- Four types of interface:
  - piecewise constant distributions on regular meshes (type 1),
  - weighted averages of point-wise values (type 2),
  - a user-defined functional dependence (type 3)
  - unstructured three-dimensional meshes (type 4)
- Enabling the interface implies using the target motion sampling (TMS) method
- TMS is not compatible with thermal bound scattering and unresolved resonance treatment

← Used for  
Serpent/SCF

# Internal Serpent/SUBCHANFLOW coupling

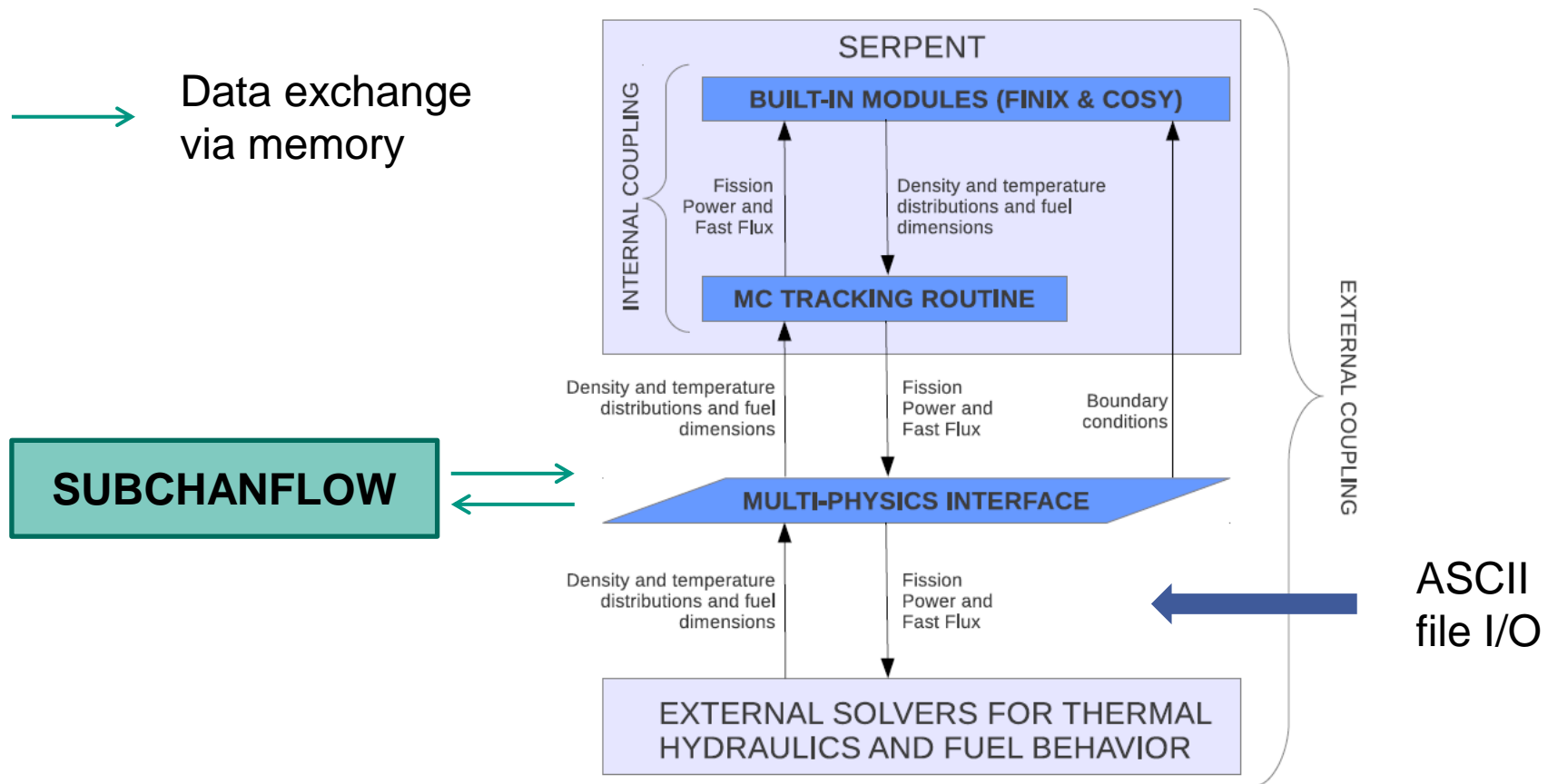
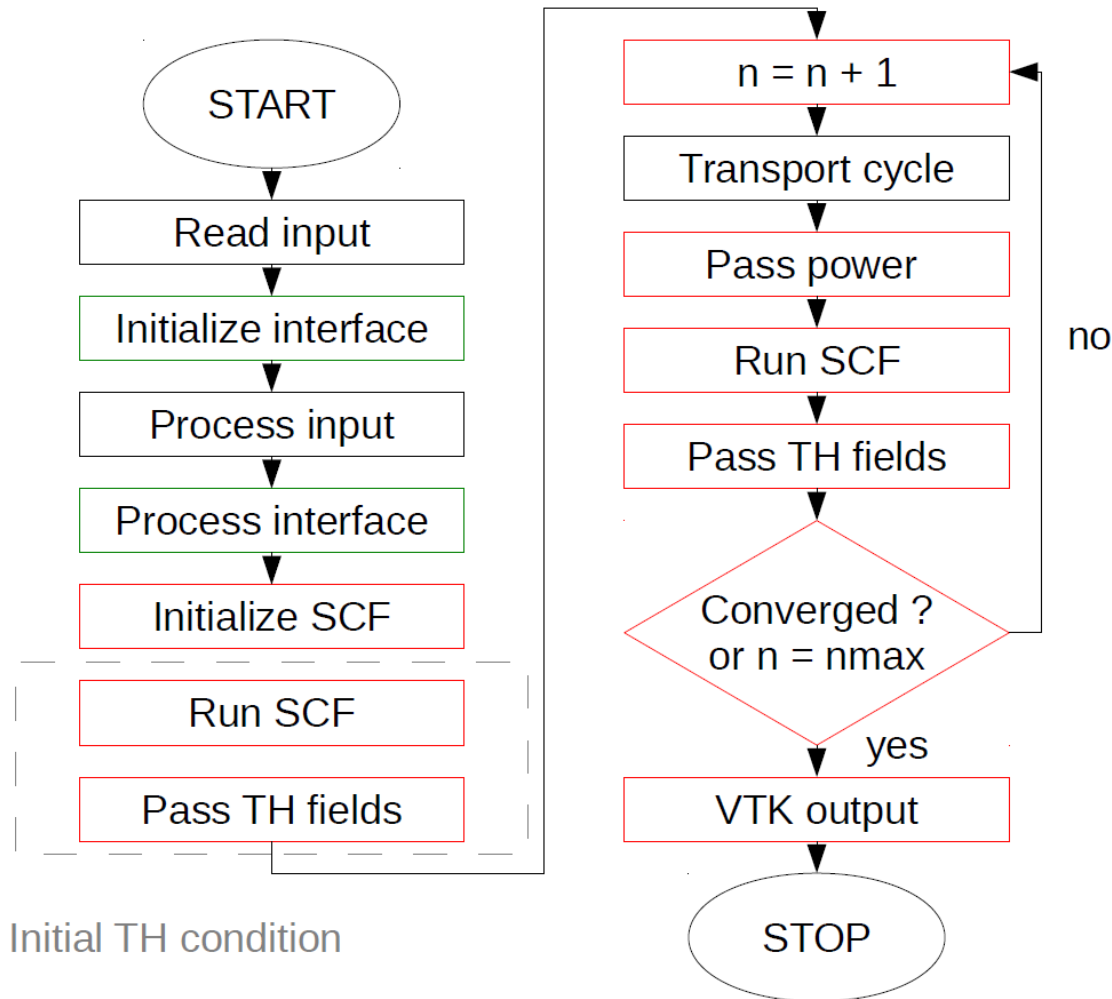
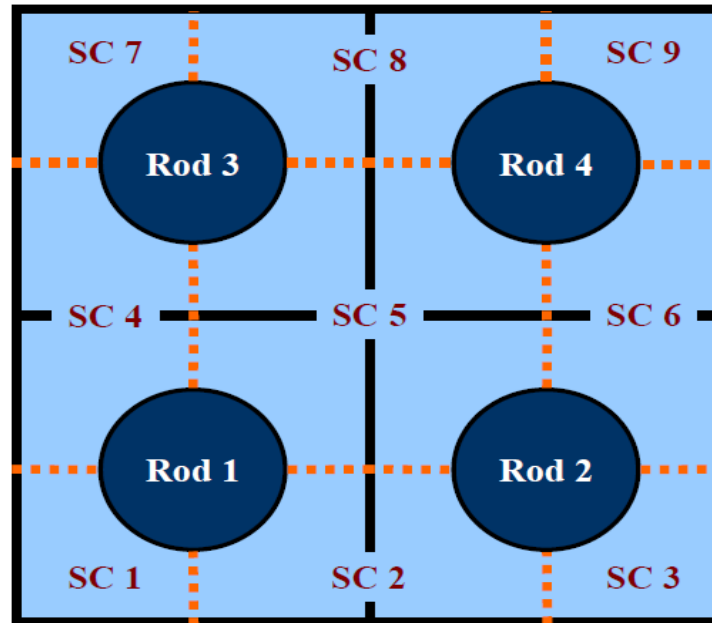


Figure: Multi-physics coupling scheme in Serpent 2

# Serpent/SCF coupled iteration algorithm



# Spatial mapping between Serpent and SCF



$$T_{dopp} = (1 - \alpha) T_{f,c} + \alpha T_{f,s}$$

Channel and sub-channel level TH models possible

# Relaxation scheme and convergence criteria

- Relaxation scheme developed by J. Dufek et al.

$$\phi^n = \frac{1}{n} \sum_{i=1}^n \tilde{\phi}^i$$

$$\phi^n = \left(1 - \frac{1}{n}\right) \phi^{n-1} + \frac{1}{n} \tilde{\phi}^n$$

- Convergence checking based on l2 norm

$$\frac{\Delta X}{X} = \frac{\|X^n - X^{n-1}\|_{l^2}}{\|X^n\|_{l^2}} \leq \epsilon_X$$

## Assuring a converged solution

- Coupled convergence is limited by maximum statistical uncertainty of Monte Carlo power tally
  - **Global variance reduction**, i.e. The Uniform Fission Site method (UFS)
- Testing convergence of fission source: Shannon entropy evaluated on a superimposed mesh
- Statistical uncertainty of all coupled fields only available by replica runs

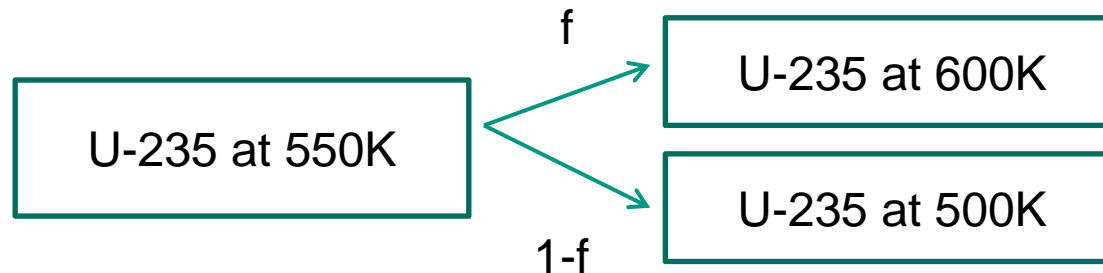


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# How to overcome shortcomings of TMS method?

- TMS method is limited to cases without
  - Thermal bound scattering
  - Need for treatment of unresolved resonance range
- Most coupled Monte Carlo thermal-hydraulic tools utilize stochastic mixing to realize changing cross sections with temperature



Let Serpent automatically fall back to stochastic mixing where TMS is not applicable

# Role of majorant cross section with varying material density and temperature (1/2)

1. Sample neutron path length from

$$l = -\frac{\log(\xi)}{\Sigma_{maj}}$$

$\xi$  is a uniformly distributed random variable

Method only discussed  
for OK basis CE cross  
sections

2. Accept or reject collision point candidate based on

$$g(\vec{r}) = \rho(\vec{r}) / \rho_{max}$$

3. Sample collision nuclide based on nuclide-wise majorants

$$p_n = \frac{\Sigma_{maj,n}(E)}{\Sigma_{maj}(E)}$$

4. Sample velocity and direction of target from Maxwellian distribution, switch into target-at-rest frame

# Role of majorant cross section with varying material density and temperature (2/2)

5. Accept or reject collision point candidate based on

$$\xi < \frac{\Sigma_{tot,n}^{0K}(\vec{r}, E')}{\Sigma_{maj,n}(E)}$$

6. Sample reaction type based on nuclide microscopic cross sections

Bound atoms do not  
have a Maxwellian  
velocity distribution

## Stochastic mixing fall back for TMS

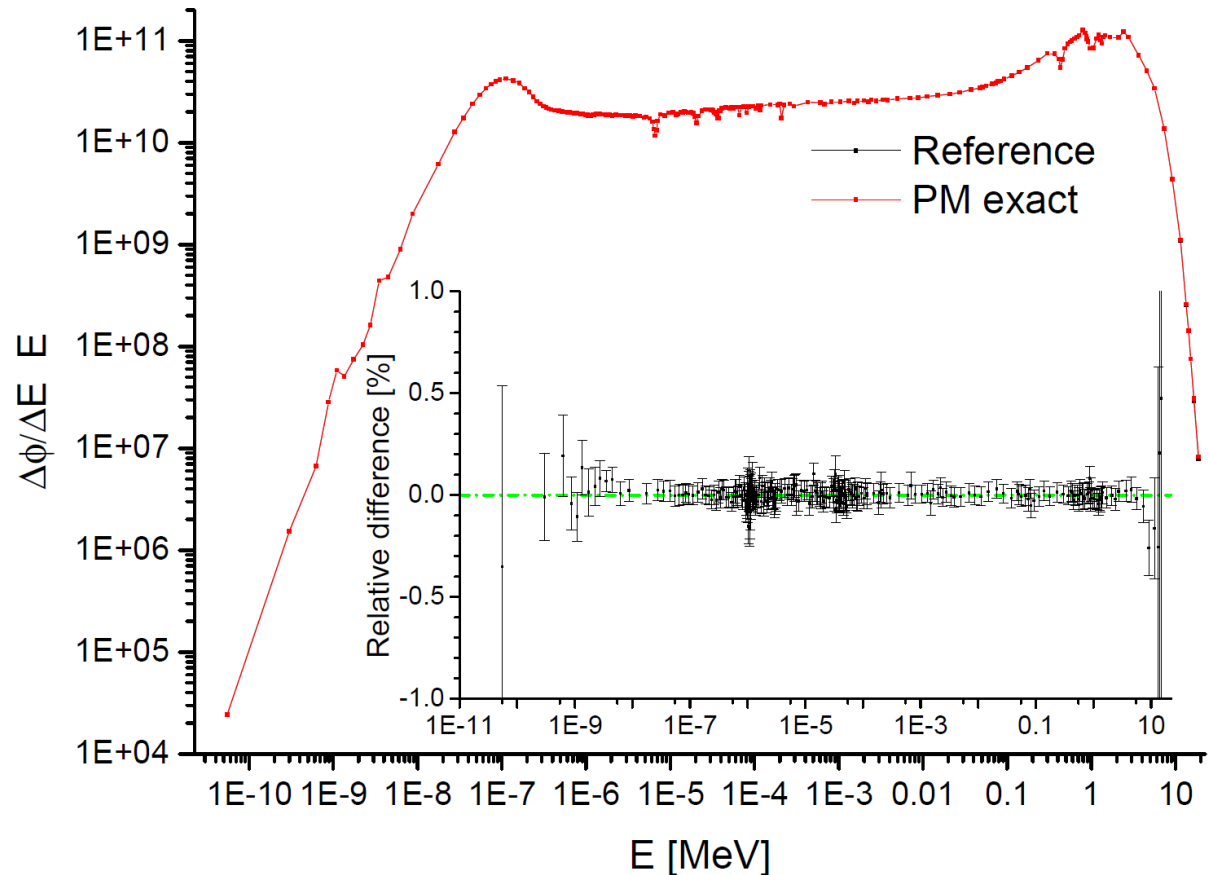
4. *If collision nuclide has no thermal scattering data associated with it*  
Sample velocity and direction of target from Maxwellian distribution, switch into target-at-rest frame

*else*

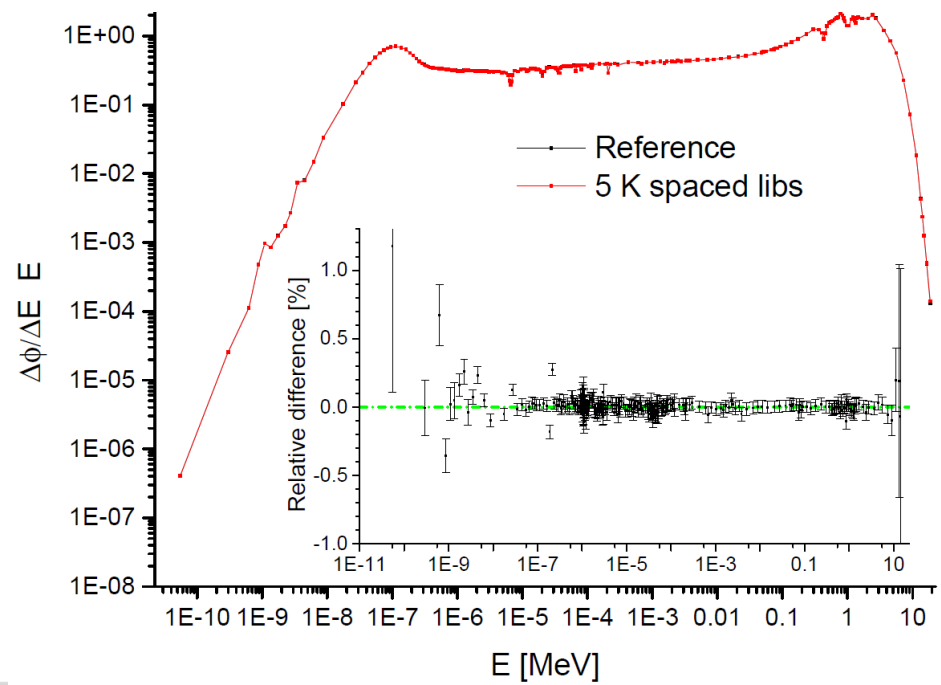
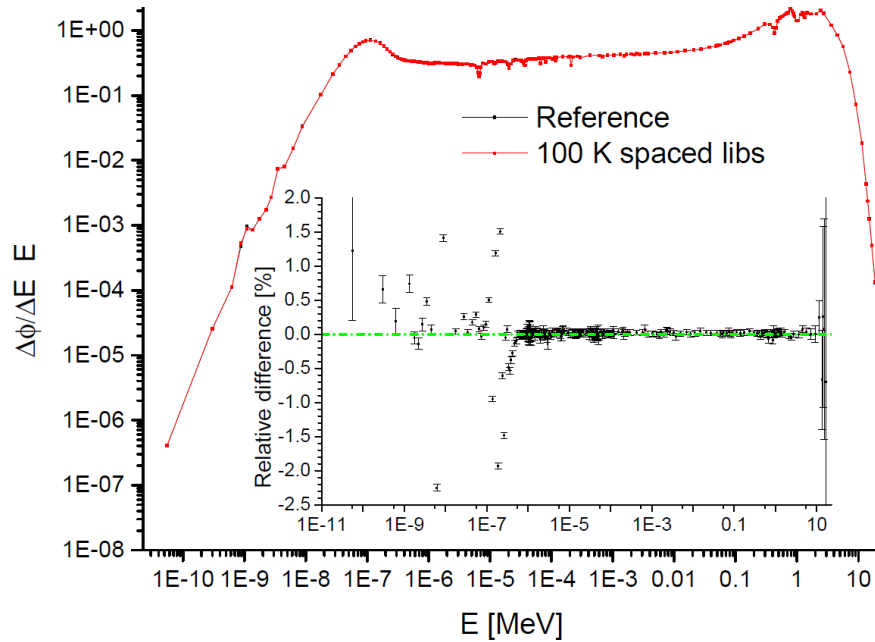
identify two scattering nuclides with temperatures enclosing the local temperature, compute the mixing fraction and use it to sample which scattering nuclide to use, do NOT transform into target-at-rest frame

# Code verification for stochastic mixing fall back

- Infinite lattice of 3.65755m high fresh UOX 4.2wt% fuel pins
- Two axial water zones: 500K and 600K
- Fuel temperature 900K and structures at 600K



# Necessary temperature spacing of $S(\alpha, \beta)$



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# Channel TH solution verification case (1/3)

- Code-to-code benchmark with TRIPOLI/SUBCHANFLOW
- 3x3 minicore from NURISP boron dilution benchmark
- JEFF 3.1.1 CE nuclear data
- Coupled convergence <1% for TH fields

Vacuum

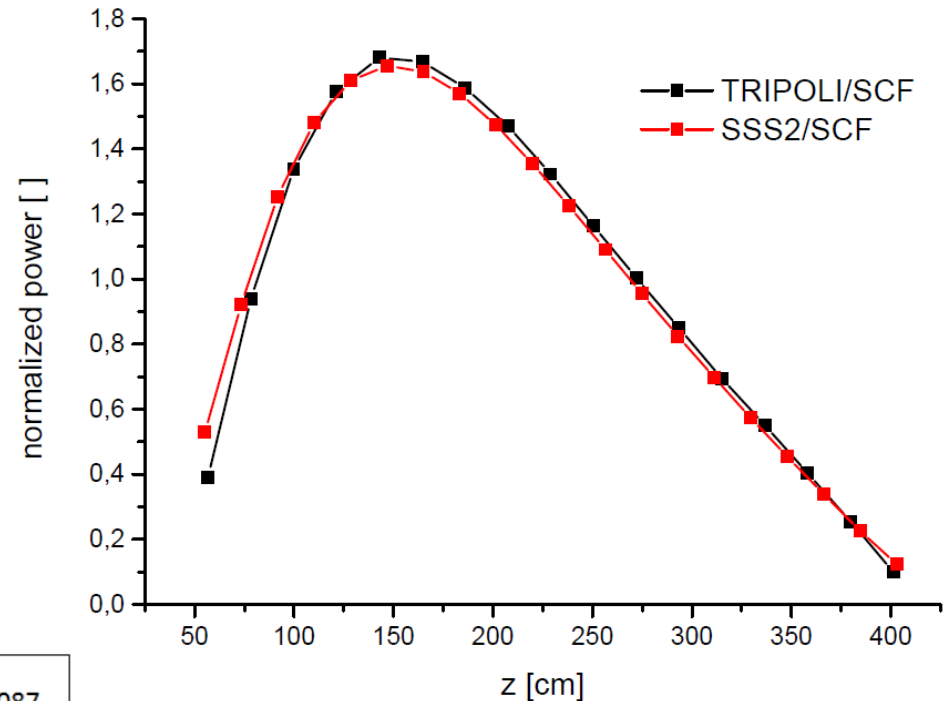
	REFL	REFL	REFL	REFL	REFL
	REFL	1 MOX 4.3%	2 MOX 4.3%	3 MOX 4.3%	REFL
Vacuum	REFL	4 MOX 4.3%	5 UO2 4.5%	6 MOX 4.3%	REFL
	REFL	7 MOX 4.3%	8 MOX 4.3%	9 MOX 4.3%	REFL
	REFL	REFL	REFL	REFL	REFL

Vacuum

Quantity	Value
Power	100 MW
Core mass flow rate	739.08 kg/s
Outlet pressure	15.4 MPa
Coolant inlet temperature	560 K
Boron concentration	200 ppm

# Channel TH solution verification case (2/3)

Coupled Code	$k_{\text{eff}}$
TRIPOLI/SCF	$1.01886 \pm 0.00056$
SSS2/SCF	$1.01825 \pm 0.00002$



Radial power profiles

0.087	0.120	0.087
0.120	0.172	0.120
0.087	0.120	0.087

(a) SSS2/SCF

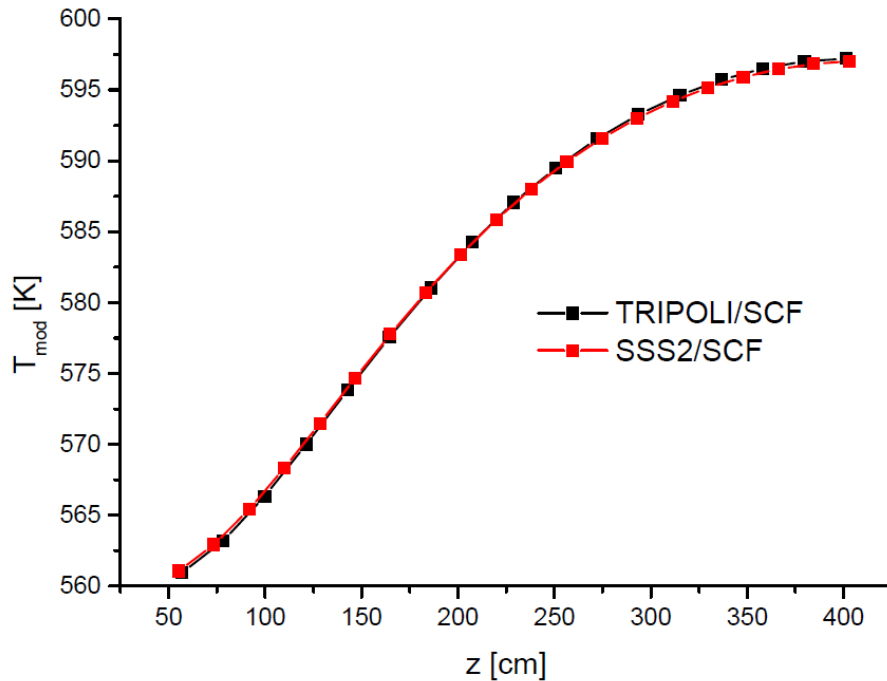
0.087	0.12	0.087
0.12	0.173	0.12
0.086	0.12	0.086

(b) TRIPOLI/SCF

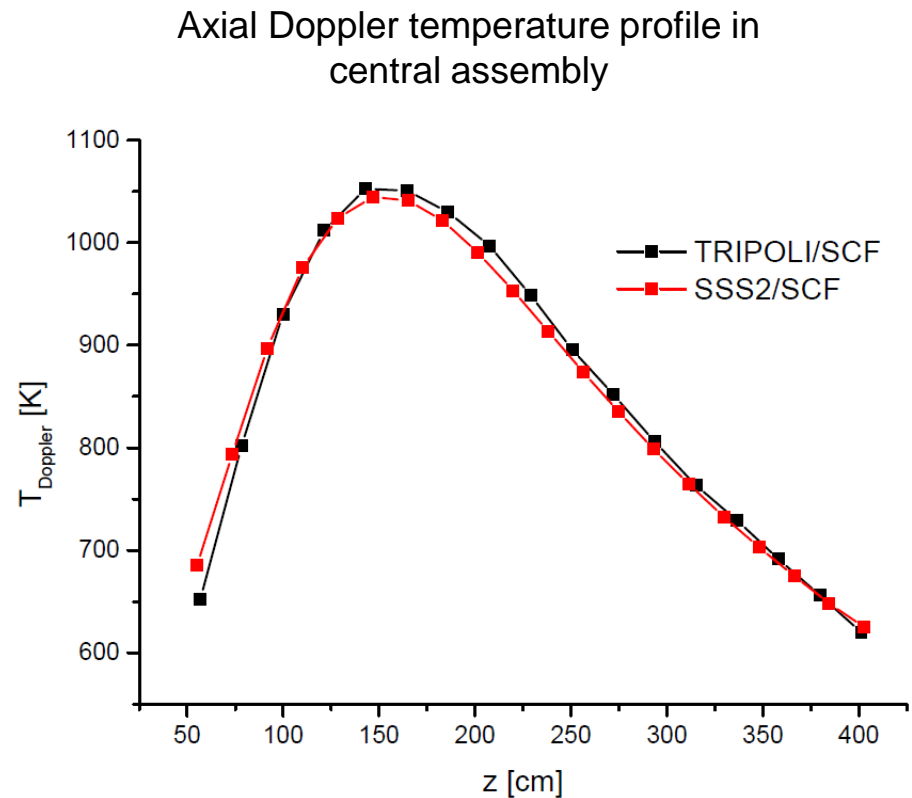
Axial power profile in central assembly

SSS2/SCF: 11 CPU-months  
 on Intel Xeon E5-2670, InfiniBand

# Channel TH solution verification case (3/3)



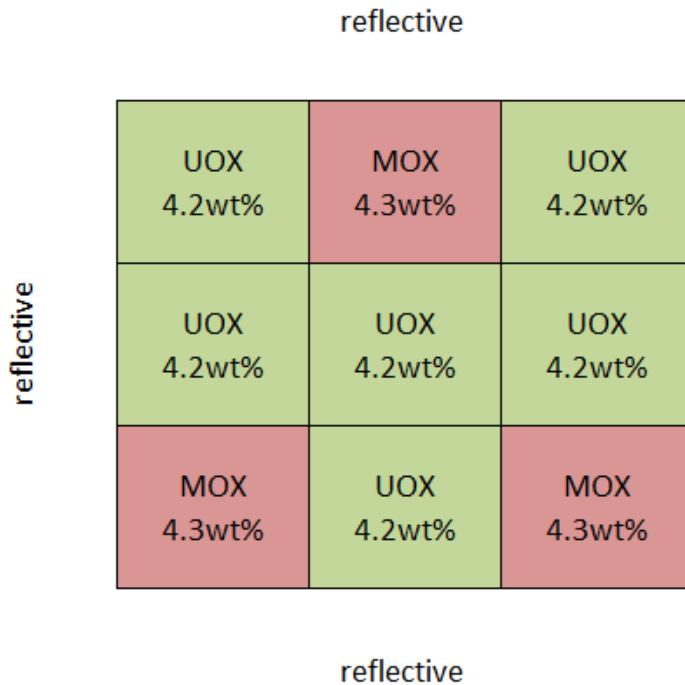
Axial moderator temperature profile in central assembly



Axial Doppler temperature profile in central assembly

# Sub-channel TH solution verification case (1/3)

- Code-to-code benchmark with MCNP5/SUBCHANFLOW
- 3x3 minicore from HPMC project, sub-channel
- JEFF 3.1.1 CE nuclear data
- Coupled convergence <0.05% for TH fields



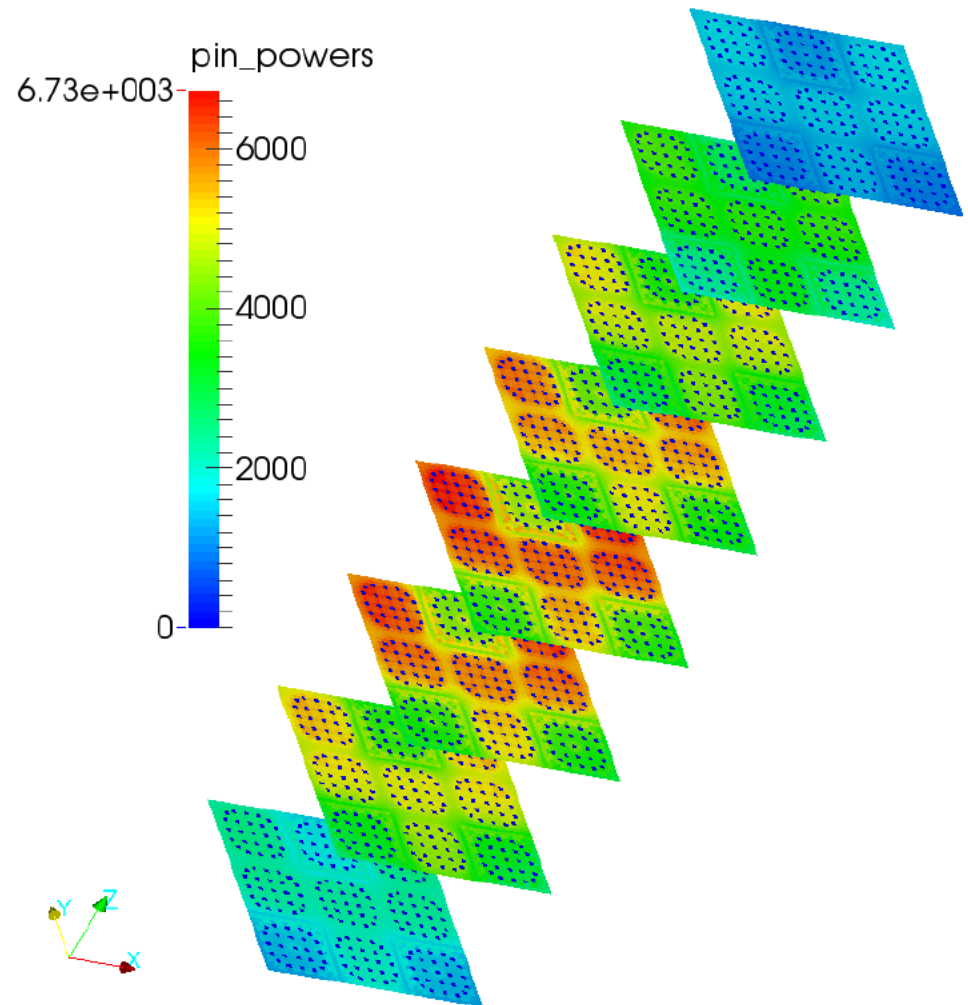
Quantity	Value
Power	166.24 MW
Core mass flow rate	739.09 kg/s
Outlet pressure	15.45 MPa
Coolant inlet temperature	560 K
Boron concentration	1200 ppm

# Sub-channel TH solution verification case (2/3)

Coupled Code	$k_{\text{eff}}$
MCNP5/SCF	$1.22298 \pm 0.00004$
SSS2/SCF	$1.22192 \pm 0.00001$

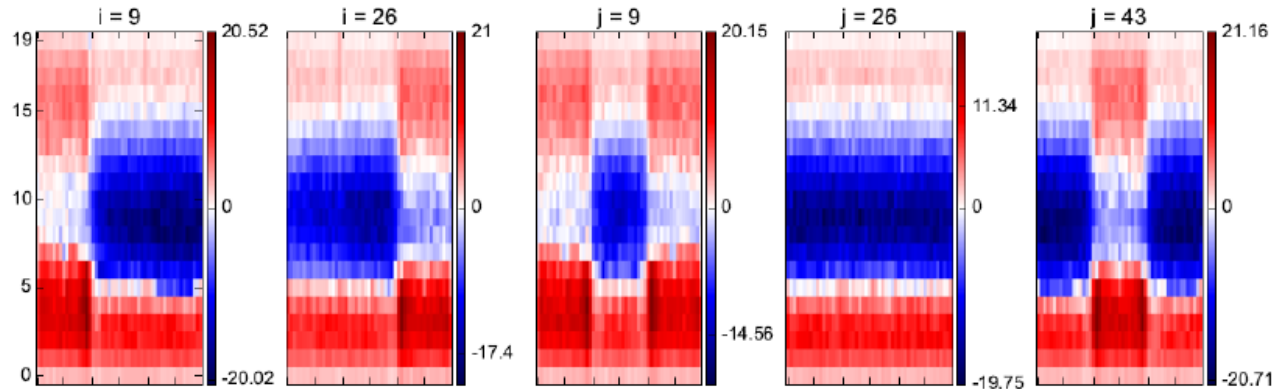
SSS2/SCF: 11.2 CPU-months

on Intel Xeon E5-2670, InfiniBand

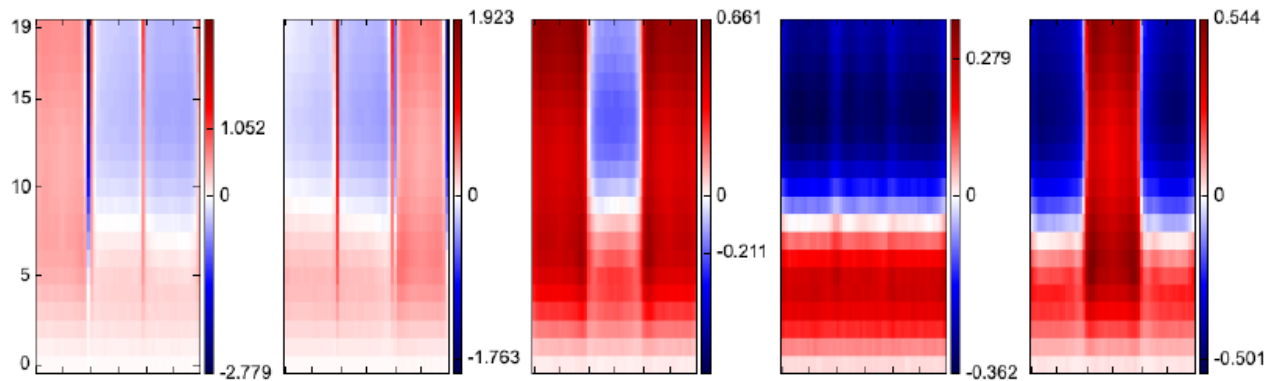


# Sub-channel TH solution verification case (3/3)

- Absolute differences in Kelvin for five vertical cuts through minicore



(a) Effective Doppler temperature



(b) Moderator temperature

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# Full PWR Core Coupled Monte Carlo Neutron Transport and Thermal-Hydraulic Simulation (1/6)

- Channel and sub-channel TH model of OECD NEA and U.S. NRC PWR MOX/UO2 core transient benchmark

U 4.2%	U 4.5%	M 4.3%	U 4.5%						
32.5	17.5	35.0	20.0						
U 4.5%	M 4.0%	U 4.5%	M 4.3%	U 4.2%	U 4.5%				
(CR-C)		(CR-B)		(CR-SC)					
0.15	0.15	0.15	0.15	17.5	32.5				
M 4.3%	U 4.2%	M 4.3%	U 4.5%	U 4.5%	M 4.3%	U 4.5%			
(CR-SB)	(CR-SB)		(CR-SC)						
17.5	32.5	17.5	20.0	0.15	0.15	32.5			
U 4.4%	U 4.2%	U 4.2%	U 4.2%	U 4.2%	U 4.5%	U 4.2%			
(CR-SB)				(CR-D)		(CR-SA)			
37.5	0.15	22.5	0.15	37.5	0.15	17.5			
U 4.5%	M 4.0%	U 4.2%	M 4.0%	U 4.2%	U 4.5%	M 4.3%	U 4.5%		
					(CR-SC)				
0.15	22.5	0.15	37.5	0.15	20.0	0.15	20.0		
U 4.2%	U 4.5%	U 4.2%	U 4.2%	U 4.2%	M 4.3%	U 4.5%	M 4.0%		
(CR-A)		(CR-C)				(CR-B)			
22.5	32.5	22.5	0.15	22.5	17.5	0.15	35.0		
U 4.2%	U 4.2%	U 4.5%	M 4.0%	U 4.2%	U 4.2%	M 4.0%	U 4.5%		
					(CR-SB)				
0.15	17.5	32.5	22.5	0.15	32.5	0.15	17.5		
U 4.2%	U 4.2%	U 4.2%	U 4.5%	UOX 4.5%	M 4.3%	U 4.5%	U 4.2%		
(CR-D)		(CR-A)				(CR-C)			
35.0	0.15	22.5	0.15	37.5	17.5	0.15	32.5		

Quantity	Value
Power	3565 MW
Core mass flow rate	15849.4 kg/s
Inlet pressure	15.5 MPa
Coolant inlet temperature	560 K



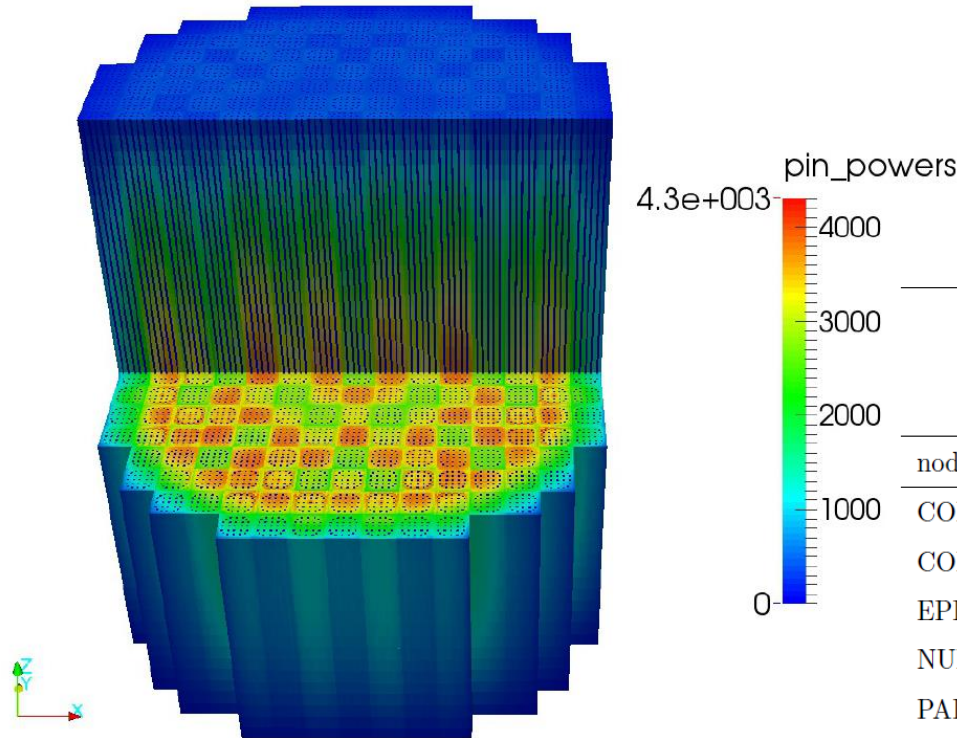
# Full PWR Core Coupled Monte Carlo Neutron Transport and Thermal-Hydraulic Simulation (2/6)

- Neutron transport model test with 2D HZP conditions
- Benchmark based on ENDF/B VI
- SSS2 used ENDF/B VII.0
- Coupled convergence <0.5% TH fields

	Eigenvalue	Assembly power error	
		%PWE	%EWE
nodal			
CORETRAN 1/FA	1.06387	1.06	1.69
CORETRAN 4/FA	1.06379	0.96	1.64
EPISODE	1.06364	0.96	1.64
NUREC	1.06378	0.96	1.63
PARCS 2G	1.06379	0.96	1.63
PARCS 4G	1.06376	0.90	1.42
PARCS 8G	1.06354	0.86	1.25
SKETCH-INS	1.06379	0.97	1.67
pin-by-pin			
BARS	1.05826	1.29	1.92
DeCART	1.05852	ref	ref
DORT	1.06036	0.86	1.12
MCNP	1.05699	0.67	1.26
DYNSUB 8G SP3	1.05888	0.70	1.09
SSS2	1.05862	1.22	1.68
	±0.00001		

# Full PWR Core Coupled Monte Carlo Neutron Transport and Thermal-Hydraulic Simulation (3/6)

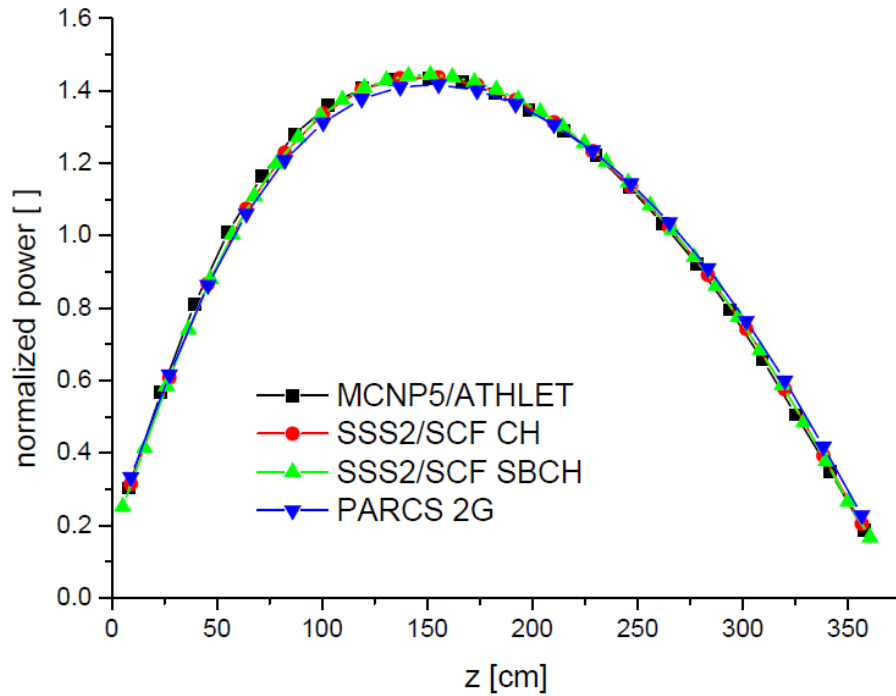
5M neutrons per cycle, 2000 active cycles per iteration



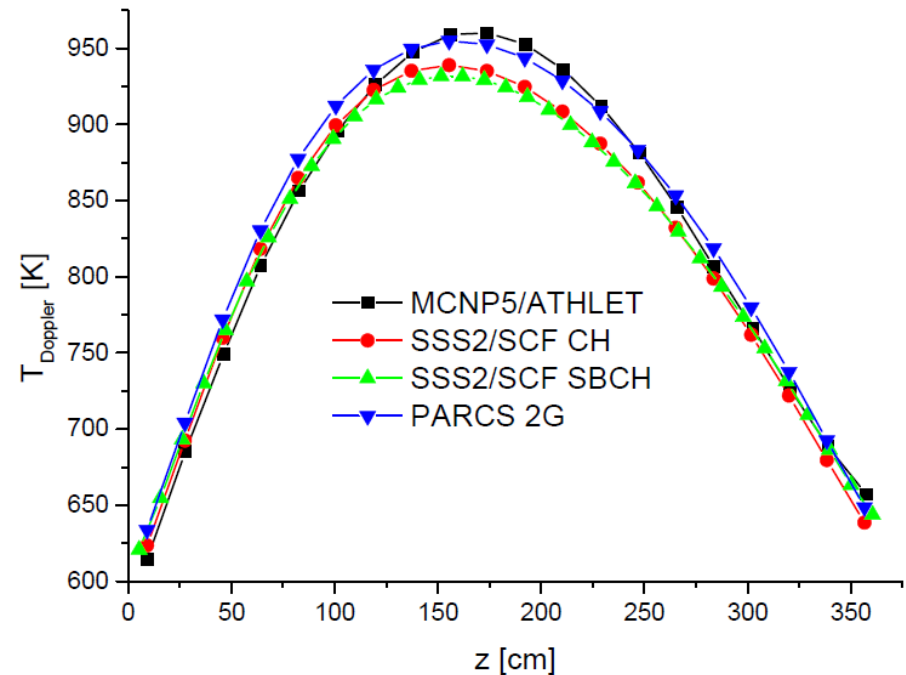
	Critical $c_b$	Average $T_{Dopp}$	Average $\rho_M$	Average $T_M$	Outlet $\rho_M$	Outlet $T_M$
	[ppm]	[K]	[kg/m <sup>3</sup> ]	[K]	[kg/m <sup>3</sup> ]	[K]
nodal						
CORETRAN 1/FA	1647	908.4	706.1	581.0	658.5	598.6
CORETRAN 4/FA	1645	908.4	706.1	581.0	658.5	598.6
EPISODE	1661	846.5	701.8	582.6	697.4	585.5
NUREC	1683	827.8	706.1	581.1	661.5	598.7
PARCS 2G	1679	836.0	706.1	581.3	662.1	598.8
PARCS 4G	1674	836.1	706.1	581.3	662.1	598.8
PARCS 8G	1672	836.2	706.1	581.3	662.1	598.8
SKETCH-INS	1675	836.6	705.5	580.9	659.6	598.9
pin-by-pin						
DYNSUB 8G SP3	1600	824.3	705.1	580.6	678.8	593.1
SSS2/SCF CH	1593	824.6	702.8	582.5	660.5	599.2
SSS2/SCF SBCH	1599	819.7	704.0	582.1	660.8	599.4

SSS2/SCF CH: 3.7 CPU-years  
 SSS2/SCF SBCH: 5.8 CPU-years  
 on Intel Xeon E5-2670, InfiniBand

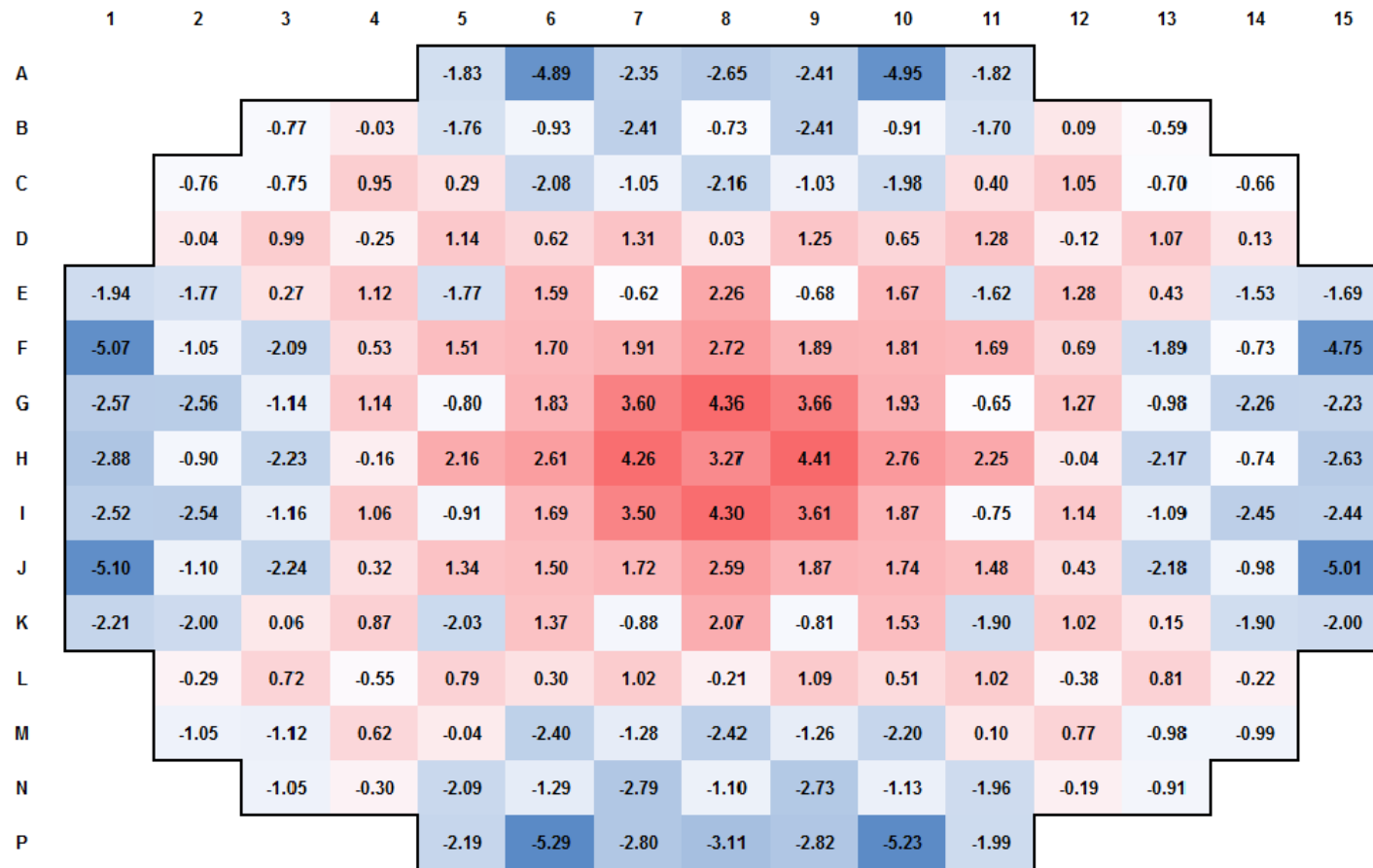
# Full PWR Core Coupled Monte Carlo Neutron Transport and Thermal-Hydraulic Simulation (4/6)



MCNP5/ATHLET  
solution:  
GRS at  
PHYSOR 2012

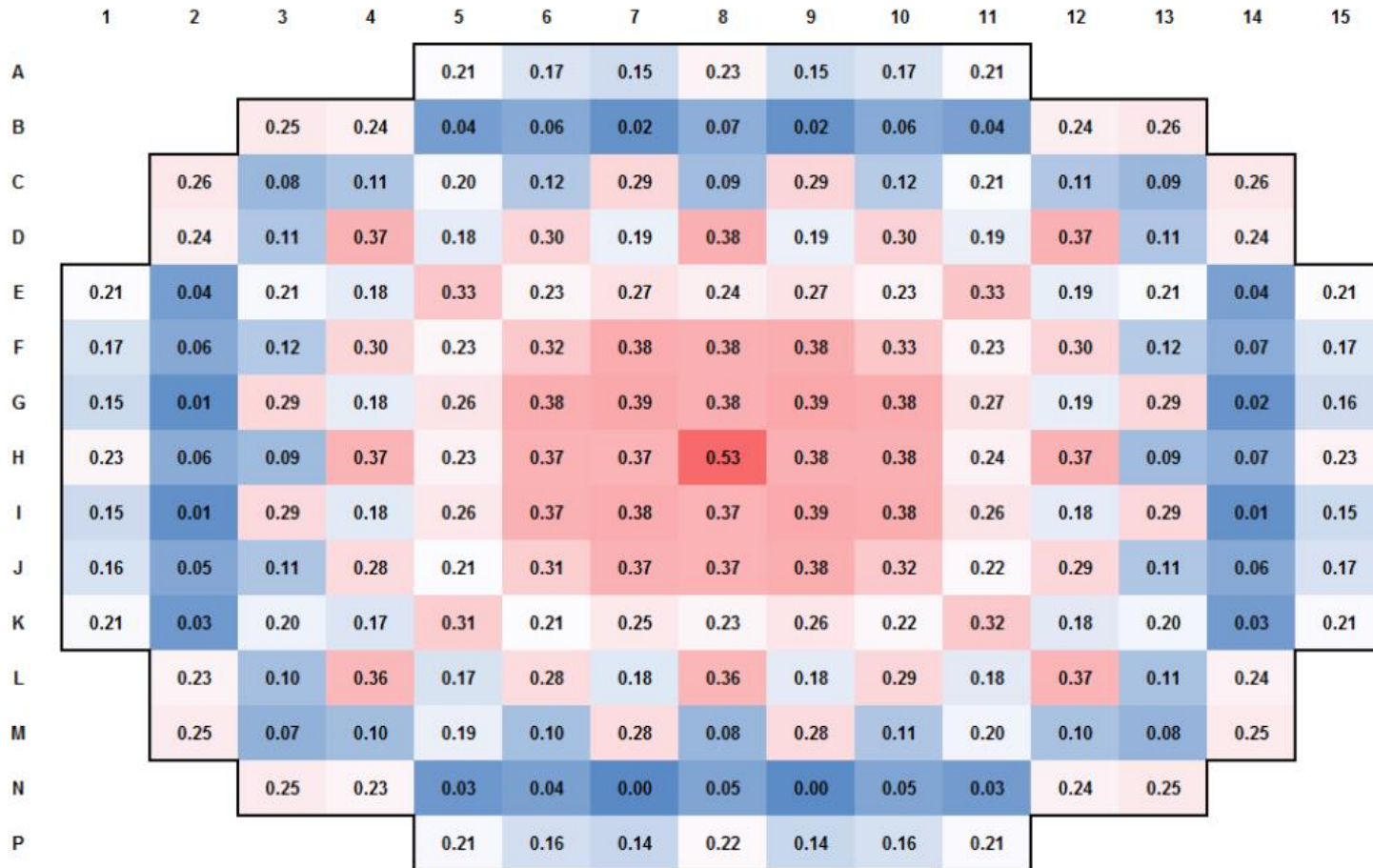


# Full PWR Core Coupled Monte Carlo Neutron Transport and Thermal-Hydraulic Simulation (5/6)



Difference in percent assembly power between SSS2/SCF CH and PARCS 2G

# Full PWR Core Coupled Monte Carlo Neutron Transport and Thermal-Hydraulic Simulation (6/6)



Difference in percent moderator temperature between SSS2/SCF CH and PARCS  
2G

## Future work

- Improve numerical performance and scaling of SSS2/SCF
- Domain decomposition for thermal-hydraulics
- Validate using NPP measurement data
- Work on efficient method to achieve converged fission source
- Extend coupling algorithm to cover burn-up calculations
- Extend coupling to Serpent's dynamic mode (dynSerpent)