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A Zero-Dimensional Burn-up Program for Fast Reactors

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A Zero-Dimensional Burn-up Program for Fast Reactors

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Abstract

PYGRJY is a refined and extended version of the zero-dimensional burn-up code PYRE, which calculates the changes of reactivity, neutron spectrum, and isotopic concentrations with time, taking into account management operations and allowing for a very general isotopic scheme. The code is written in Fortran IV for the IBM 360. An input description and a sample case are presented. Results of a calculation of the transplutonium build-up, including the berkelium and californium isotopes, in thermal fluxes of $5 \times 10^{13} - 3 \times 10^{16}$ cm$^{-2}$ sec$^{-1}$ are presented.
I. Introduction

The code PYME \(^\text{1,7}\) calculates the time dependence of reactivity, power, neutron spectrum, and isotope concentrations for a constant flux or power, taking into account capture, decay and fission product build-up. The version PYGMY has been extended to include

1. the influence of management operations such as shut-down times, different power levels, and charging and discharging of different batches;
2. the possibility of performing pure irradiation calculations excluding the determination of reactivity and neutron spectrum;
3. the calculation of the activity of the individual batches;
4. the influence of \((n,2n)\)-processes;
5. branching of isotopic chains in one process, e.g. competing \(\beta^-\) and \(\beta^+\) decay;
6. a better numerical procedure for the integration of the isotopic equations;
7. automatic adjustment of step length.

A description of the code performance will be given in the next section. Section III provides an input description, section IV the input and results of a sample case. In section V the results of a calculation of the transplutonium build-up in a thermal spectrum of \(5 \times 10^{13} - 3 \times 10^{16}\) \(\text{cm}^{-2}\text{sec}^{-1}\) are presented. 40 isotopes including the elements berkelium and californium have been taken into account in these calculations.

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II. Description of the code

1. Input

In its present version, the program handles up to 40 time dependent isotopes; this number can be easily enlarged by altering the related dimensions. The information on one isotope is collected in two cards of the input (K3 and K5) including all information on transitions leading from this isotope to other isotopes. An exemption is made for the fission process; here, the fission rate is summarized over all isotopes, and from this, the formation of the fission products is derived using the individual values of $\beta$. Decay, capture, and $(n,2n)$-products which shall not be taken into account must not be specified anywhere in the input.

Only down-scattering is admitted. In order to keep the input as small as possible, only sub-diagonals with non-zero elements have to be specified. The number of these sub-diagonals is $\text{NXCM}$; for the ABN-set $\text{NXCM}$ is 10 if hydrogen is included or less if only heavier elements are present.

2. Calculation of reactor characteristics

The first step of the burn-up calculation consists of the determination of breeding ratio, reactivity or buckling, total neutron flux or power, neutron spectrum, some reaction rates, and the activity. In the case of pure irradiation calculations, the determination of reactivity or buckling and of the spectrum is omitted. It is possible to determine either the buckling for a constant reactivity or the reactivity for a constant buckling, which may either be given as input or be determined from a desired value for $k_{\text{eff}}$ at time zero. The average cross sections used for the burn-up may be collapsed either with the spectrum pertaining to the present $k_{\text{eff}}$ or with a spectrum for $k_{\text{eff}}=1$. The spectrum in the output is the spectrum used for the collapsing of the cross sections.
One may choose whether to keep the power or the total flux constant with time, that is constant between two management operations. In the case of irradiation calculations, the spectrum is kept constant too and has to be specified by the user. It needs not to be normalized to the total flux.

3. Management

The input for management is organized in such a way that for each time at which operations take place first the point of time and then all desired operations such as discharging, recharging and changes of power or flux and time step length are specified. The point of time has to coincide with the end of some time step; thus, it is not possible to define step lengths of 10 days and then to require the first management operation at 25 days, but instead one can change the step length after 20 days to 5 days and then perform the management operation at 25 days.

It is possible to treat several charges in one reactor. The burn-up calculations are performed separately for each charge, while the criticality calculations are done for the homogenized charges. On input, a number and a volume is assigned to each charge. The sum of all charge volumes should equal the core volume, or else the homogenized material densities are suitably condensed or diluted. On discharging, one has only to specify the number of the charge and the volume to be discharged; thus, it is possible to discharge only part of a batch. Numbers of completely discharged batches may be reused for new batches, but if this is done with numbers of charges which are not completely discharged the data of the old charge are deleted and a warning is issued.

If any management operation takes place the program continues with a new criticality calculation; otherwise, a burn-up calculation ensues.

In order to ensure a correct end of the calculation, especially if other cases follow up, one should discharge the core wholly at the last point of time.
4. Burn-up calculation

The numerical procedure used by PYRE for the integration of the isotopic equations has been discarded in favor of one with better convergence. As in PYRE, the system of differential equations, which shall be denoted by

\[ \dot{N} = A \, N \] (1)

is approximated by

\[ \frac{\Delta N_i - N_{i-1}}{\Delta t} = A \, \frac{N_i + N_{i-1}}{2} \] (2)

\[ \Delta t = t_i - t_{i-1} \]

An iterative procedure is needed for the solution of (2). For PYRE, the iteration

\[ N_i^k = N_{i-1} + \frac{\Delta t}{2} A \left( N_{i-1} + N_{i-1}^{k-1} \right) \] (3)

has been chosen, but this tends to diverge for too big time steps. For PYSMY, (2) is rewritten as follows

\[ \left( E - \frac{\Delta t}{2} A \right) \tilde{N}_i = \left( E + \frac{\Delta t}{2} A \right) \tilde{N}_{i-1} \] (4)

\[ E = \text{unitary matrix} \]

or

\[ M \tilde{N}_i = \tilde{R} \] (5)

With

\[ M = D - L - U \]

D being a diagonal, L a lower triangular, and U an upper triangular matrix, the iterative procedure has been chosen to be

\[ N_i^k = (1-w) N_i^{k-1} + w \left( D - L \right)^{-1} \left( U N_i^{k-1} + \tilde{R} \right) \] (6)

with \( w = 1 \). With \( w \neq 1 \), an over- or under-relaxation method could be employed, but up to now no procedure for estimating \( w \) exists. The
convergence of (6) is the better the more zero-elements are contained in $U$. It is therefore recommendable to arrange the isotopes in the order of their formation, beginning with the fissile and fertile isotopes and ending with the fission products.

The user may employ the automatic step length adjustment. One has then to specify the maximum number of micro-steps into which one time step may be subdivided. At the start of the calculation and after each management operation, this number is used for the burn-up calculation, whereas for all subsequent time steps, the number of micro-steps is reduced if the change of isotopic concentrations in the last micro-step does not exceed 3%. This ensures an accuracy of at least 0.1%. Of course, if the maximum number of micro-steps has to be employed, this accuracy cannot be guaranteed.

A redetermination of neutron spectrum and power or flux level over the time interval is not achieved by use of the automatic step length adjustment. If these quantities change appreciably over one time step, smaller steps should be employed.

If no automatic step length adjustment is used, the number of micro-steps is taken to be 4 at the start and after each management operation and 1 for all subsequent steps.

5. Output

One can choose a full or a partial output. The partial output comprises:

a. Start: All information on isotopes and processes linking them; messages on the type of calculation; data of the initial loading.

b. Burn-up: Reactivity, breeding ratio, total power and flux, buckling, reaction rates; the homogenized atom densities and activities of all isotopes; the group dependent spectrum and fission source.
c. Management: Messages on changes of power, flux, or spectrum; number and volume of discharged batches and their activity; number and volume of recharged batches.

Besides, a complete listing of the input is provided. The full output gives the following additional information:

a. Start: The fission spectrum and a list of the isotope dependent microscopic group cross sections.

b. Burn-up: Macroscopic group cross sections, isotope dependent spectrum averaged cross sections, and composition and activity of individual charges.

c. Management: Composition and activity of individual discharged batches.

The output tends to become very lengthy for a big number of time steps. Therefore, one can use NPRT to get output only after every NPRT time steps and at the end of each case. The messages concerning management are excluded from this automatism.
III. Input description

The input comprises a first part which is only concerned with the definition of the isotopes, the linking processes, and the group cross sections. With the data of the first part, an arbitrary number of cases may be run. The second part of the input comprises the data for the different cases.

As for the notation, Kn defines a set of data starting on a new card and Sn a logical decision concerning the further sequence of data cards. The input is unformatted; this requires that each data set defined by Kn must start with a card containing no blank in column 1 while subsequent cards of the same set must have a blank in column 1.

The character of the numbers is given by their names in the data lists: Names starting with I-N indicate fixed point numbers, while all other names indicate floating point numbers if not explicitly stated as hollerith constants.

K1 NG Number of groups \( \leq 26 \)
NXCM Number of subdiagonals in the scattering matrix with elements \( \frac{1}{2} < 10 \)
NBE Number of burnable isotopes
NNE Number of non-burnable isotopes
NP = 0 full print
= 1 partial print
S2 for each burnable isotope K3-K5
K3 H0LN Hollerith name (up to 4 characters)
ATW Atomic weight
THALF Half life for unstable isotopes \( \text{days} \)
= 0 for stable isotopes
FE Energy released per fission \( \text{MeV} \)
BETA 0 for fissile or fertile isotopes
Yield for fission products
<table>
<thead>
<tr>
<th>Code</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>LD</td>
<td>Number of decay products</td>
</tr>
<tr>
<td>LC</td>
<td>Number of capture products</td>
</tr>
<tr>
<td>LN</td>
<td>Number of ((n,2n)) products</td>
</tr>
</tbody>
</table>

**S4** if \(LP = LD+LC+LN>0\) then K5, otherwise next isotope

**K5** for each product - first decay, then capture, then \((n,2n)\)

<table>
<thead>
<tr>
<th>Code</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>HNLNP</td>
<td>Hollerith name</td>
</tr>
<tr>
<td>WE</td>
<td>Yield per decay (capture,((n,2n)))</td>
</tr>
</tbody>
</table>

**S6** if \(NNE>0\) then K7, otherwise K8

**K7** for each non-burnable isotope

<table>
<thead>
<tr>
<th>Code</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>HNLNN</td>
<td>Hollerith name (up to 4 characters)</td>
</tr>
<tr>
<td>ATWN</td>
<td>Atomic weight</td>
</tr>
</tbody>
</table>

**K8** (\(CH(I), I=1, N0\)) Fission spectrum

**S9** for each isotope in the order given by K3 and K7 S10-K11

**S10** for each group \(g\) K11

<table>
<thead>
<tr>
<th>Code</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>SIGF</td>
<td>Fission cross section (1^{-})barns (^-7)</td>
</tr>
<tr>
<td>SIGA</td>
<td>Absorption cross section (1^{-})barns (^-7)</td>
</tr>
<tr>
<td>SIGFM</td>
<td>(v\times) fission cross section (1^{-})barns (^-7)</td>
</tr>
<tr>
<td>SIGTR</td>
<td>Transport cross section (1^{-})barns (^-7)</td>
</tr>
<tr>
<td>SN2N</td>
<td>((n,2n)) cross section (1^{-})barns (^-7)</td>
</tr>
</tbody>
</table>

\((SIGS(I),I=1,NXCM)\) Cross sections for down-scattering into group \(g\) starting with the next higher group \(1^{-}\)barns \(^-7\). If \(NG=1\), SIGS must not be specified.

**S12** for each case K13-K31, then K32

**K13** NC Number of the case (\(\neq 0\))

**K14** NOP

<table>
<thead>
<tr>
<th>Code</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>=0:</td>
<td>calculate (k_{\text{eff}}(T)) for a given (k_{\text{eff}}(T=0))</td>
</tr>
<tr>
<td>=1:</td>
<td>calculate (k_{\text{eff}}(T)) for a given (B^2)</td>
</tr>
<tr>
<td>=2:</td>
<td>calculate (B^2(T)) for a given (k_{\text{eff}})</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Code</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>NFP</td>
<td>=0: the power is kept constant</td>
</tr>
<tr>
<td>=1:</td>
<td>the flux is kept constant</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Code</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>NSP</td>
<td>=0: averaged cross section calculated at (k_{\text{eff}}=1)</td>
</tr>
<tr>
<td>=1:</td>
<td>averaged cross section calculated at (k_{\text{eff}}(T))</td>
</tr>
<tr>
<td>=-1:</td>
<td>averaged cross section calculated with constant spectrum specified by the user</td>
</tr>
</tbody>
</table>
NUMT Total number of time steps
NPRT Number of intervals between prints (e.g. =1: print every time, =2: print every other time)
NAUT
\( =0: \) no step length adjustment
\( =1: \) internal step length adjustment
MAX Maximum number of micro-steps per time interval (power of 2)
H Initial step length in days
VOL Core volume in liters
G1
Initial power in wt for NFP=0
Initial flux in \( \text{cm}^{-2} \text{sec}^{-1} \) for NFP=1
G2 \( k_{\text{eff}} \) for NFP=0, 2
\( B^2 \) for NFP = 1
S15 if NSP=1 K16, otherwise K17
K16 (SP(I), I=1, NG) Neutron spectrum
K17 LBS Number of fertile isotopes 1<IBS<10
(LBNO(I), I=1, LBS) For each fertile isotope its number given by the order in K3
LBL Number of fissile isotopes 1<IBL<10
(LBN(I), I=1, LBL) For each fissile isotope its number given by the order in K3
K18 N1 Initial number of charges for each charge K20
K20 NCH Number of the charge
VOLCH Volume in liters
(DN(I), I=1, NEE+NME) Isotope densities in \( \text{cm}^{-3} \cdot 10^{-24} \) in the order given by K3 and K7
S21 for each point of time at which management operations shall take place K22 - K31, then next case
K22 T T Point of time in days
NDIS Number of wholly or partly discharged batches
NRE  Number of recharged batches
NIF  = 1, if power, flux, neutron spectrum, or step
      length is changed
      = 0  otherwise
S23  if NIF=1 K24 - K26, otherwise S27
K24  G1N  New power $\frac{\text{M wt}}{\text{m}}$ for NFP=0
      New flux $\frac{\text{cm}^{-2}\text{sec}^{-1}}{\text{m}}$ for NFP=1
      HN  New step length $\frac{\text{days}}{\text{m}}$
S25  if NSP=-1 K26, otherwise S27
K26  (SPN(I),I=1,NG) New spectrum
S27  if NDIS>0 K28, otherwise S29
K28  for all discharged batches
NCHDIS Number of batch
VOLDIS Volume to be discharged $\frac{\text{litters}}{\text{m}}$
S29  if NRE=0 S30-K31, otherwise next point of time
S30  for every new batch K31
K31  NCHN Number of batch
      VOLN Volume $\frac{\text{litters}}{\text{m}}$
      (DNN(I),I=1,NBE+NNE) Isotope densities $\frac{\text{cm}^{-3},10^{-24}}{\text{m}}$ in the
      order given by K3 and K7
K32  0  Constant
K33  aNUFINT Constant

For a calculation on the Karlsruhe 360/65 the following job control
cards have to be added:
//EXEC FHG,LIB=NUSYS,NAME=PYOGY,REGION,0=200K
//G,F0372004 DD UNIT=SYSDA,SPACE=(200,(200))

Typical running times are 12 sec for the sample case described in
the next section and 92 sec for one flux value in the 40-materials
case from chapter V.

An example for the input is provided by the sample problem.
IV. **Input and results of the sample problem**

A wholly artificial case has been constructed for the sample problem, but in the processes linking the isotopes a certain similarity to realistic cases has been maintained (see fig. 1). Thus, the 7 materials MATA–MATG constitute the fissile and fertile isotopes, POI1–POI4 are the fission products, and STR1 and STR2 are structure materials. The five isotopes MATA–MATE can be interpreted as isotopes of one element with MATD and MATC being isomeric nuclei; MATC has a competing $\gamma$, $\beta^-$- and $\beta^+$-decay, the last two transitions leading to the next higher and next lower element. The capture transition leading from MATF to MATE can be interpreted as a transition leading to very short lived isotope which decays into MATE and which is omitted because of its short life time.

The hypothetical reactor is at first loaded with one charge and operates at full power (1000 Mw) for 80 days. It is then shut down for 10 days, and after two days shut-down time half of the original charge is replaced with a new charge. At T=90 days it is started up again for 80 days at half power and afterwards wholly discharged. The input for this case is given below.

```
2 1 11 2 0
aMATAa 200. 0 200. 0 0 1 0
aMATBa 1.

aMATBa 201. 0 200. 0 0 2 1
aMATCa .8 aMATDa .2 MATA 1.

aMATCa 202. 10. 200. 0 3 1 0
aMATDa .9 aMATCa .06 aMATGa .04 aMATEa 1.

aMATDa 202. 0 200. 0 0 1 1
aMATEa 1. aMATBa 1.

aMATEa 203. 0 200. 0 0 0 1
aMATDa 1.
```
aMATPa 202. .1 200. 0 0 1 0
aMATEa 1.
aMATGa 202. 0 200. 0 0 0 0
aP011a 80. 1. 0 .06 1 0 0
aP012a 1.
aP012a 80. 0 0 .01 0 1 0
aP013a 1.
aP013a 81. 0 0 .03 0 1 1
aP014a 1. aP012a 1.
aP014a 82. 50. 0 0 0 0 0
aSTR1a 50. aSTR2a 2.
1. 0
5. 10. 15. 20. 0 0
600. 650. 1500. 660. 0 .01
.1 4. .3 12. .05 0
0 15. 0 20. 0 .01
2. 8. 6. 15. 0 0
400. 600. 900. 615. 0 .01
15. 30. 40. 35. .02 0
800. 1200. 2000. 1210. 0 .01
1. 10. 3. 18. 03 0
0 15. 0 25. 0 .01
.5 7. 1.5 15. 0 0
0 4. 0 10. 0 .01
.05 .1 .1 4. 0 0
0 .4 0 5. 0 .01
0 0 0 5. 0 0
0 0 0 5. 0 .01
0 1. 0 10. 0 0
0 2000. 0 2010. 0 .01
0 4. 0 10. .1 0
0 4000. 0 4010. 0 .01
The time dependence of the homogenized materials is given in Fig. 2; other results are listed in Table 1.
V. Formation of transplutonium isotopes in a thermal spectrum

The formation of transplutonium isotopes, including the Bk- and Cf-isotopes, has been calculated using a total of 40 isotopes. Fig. 3 shows the isotopes and the processes linking them. (n,2n)-processes have not been taken into account as their contribution is negligible in a thermal spectrum. Of course, the isotopic scheme depends upon the nature of the problem to be solved. Thus, for the smaller flux values, decay transitions override the capture transitions, so that some isotopes to the lower right edge of the scheme in Fig. 3 (Pu$^{244}$, Pu$^{245}$, Am$^{249}$, Bk$^{251}$) could be dropped without any loss of accuracy. On the other hand, for a high flux, only Bk$^{251}$ turns out to be superfluous.

The neutron spectrum has been chosen to represent the FR2-spectrum and the group cross sections were partly taken from irradiation calculations recently done for an experiment at this reactor [2,7]. As far as possible they are one group cross sections condensed from the 26-group-ABN-set; all other cross sections were taken from either the book of E.K. Hyde [3,7] or the chart of the nuclides [4,7] and corrected for the spectrum and flux depression in the sample. Some values had to be guessed. This, of course, limits the accuracy of the results especially for the higher isotopes; for Bk and Cf absolute numbers have a big error and only relative results are meaningful, but this is inherent in such calculations at the present state of knowledge.

Flux values of $5 \times 10^{13} - 3 \times 10^{16}$ cm$^{-2}$sec$^{-1}$ are examined; the management is always the same: a sample is irradiated for 180 days and then the dying-away of the activity is observed during another 35 days with zero flux.

# the lower value being the flux in the FR2, the highest value lying a little above the fluxes currently discussed for high flux reactors.
The initial composition of the sample is given below:

<table>
<thead>
<tr>
<th>Nuclide</th>
<th>Count (per 10^22 nuclides)</th>
</tr>
</thead>
<tbody>
<tr>
<td>U^{235}</td>
<td>2.7 \times 10^{20}</td>
</tr>
<tr>
<td>U^{238}</td>
<td>3.7 \times 10^{22}</td>
</tr>
<tr>
<td>Pu^{239}</td>
<td>1.45 \times 10^{22}</td>
</tr>
<tr>
<td>Pu^{240}</td>
<td>1.3 \times 10^{21}</td>
</tr>
<tr>
<td>Pu^{241}</td>
<td>1.3 \times 10^{20}</td>
</tr>
<tr>
<td>Pu^{242}</td>
<td>6.4 \times 10^{18}</td>
</tr>
<tr>
<td>Total</td>
<td>5.3 \times 10^{22}</td>
</tr>
</tbody>
</table>

The results are summarized in fig. 4-10. The first four figures show the amount of the four transplutonium elements formed after 180 days of irradiation as function of the flux. There is an optimum flux value for the formation of Am and Cm above which the amount of nuclides decreases again because it is used up for the generation of the higher elements. This optimum value increases for the higher elements and therefore is above the range of flux values under consideration. The same holds for the different isotopes of one element; the wavy structure of some curves for the lower isotopes (Am^{241}, Am^{242}, Am^{242m}) results from the fact that basically two isotopes contribute to the build-up: Pu^{239} and U^{238}. For the lower fluxes the main contribution comes from Pu^{239} and this dies away with increasing fluxes. For a further increase a similar curve originating from U^{238} overlaps.

Fig. 8 shows the increase with time of Cf-nuclides for the two most extreme fluxes. The relative increase is much bigger for the lower flux values; for example the ratio N_{Cf}(180d)/N_{Cf}(170d) is \approx 1.6 for \phi = 5 \times 10^{13} \text{ cm}^{-2} \text{ sec}^{-1} versus \approx 1.15 for 3 \times 10^{16} \text{ cm}^{-2} \text{ sec}^{-1}. Thus, the optimum irradiation times tend to be higher for the low fluxes than

---

# especially the isotope contributing most of the sum tends to be one with higher atomic number for the higher fluxes.
for the high fluxes, but, looking at the absolute values of $N_{Cf}$ for low fluxes, one can conclude that even longer irradiation times will not appreciably improve the output of the higher elements.

Fig. 9 and 10 show the time and flux dependent behaviour of the activity. From fig. 9 one finds that the activity can be divided into a short, a medium, and a long lived term. The isotopic contribution to the different terms depends upon the flux too and can be found from both figures. In figure 10, isotopes with a half life of less than 1 day are represented by dashed lines, the others by solid lines. The groups are:

1. Short lived term ($T_{1/2} < 5$ h): $^{239}U$ for all flux values and $^{243}Pu$ for medium fluxes.
2. Medium lived term ($T_{1/2} = 2.35$ d): $^{239}$Np for all fluxes.
3. Long lived term ($T_{1/2} > 160$ d): $^{241}Pu$ for low and medium fluxes, $^{242}$Cm for medium fluxes only, and $^{244}$Cm for medium and high fluxes.

The calculations presented demonstrate the good performance of PYGMY. Checks on the accuracy have shown that even for the highest fluxes steps of 10 days with a subdivision into 64 intervals are adequate. It is intended to include the integration procedure in one- and two-dimensional codes to ensure a high flexibility in regard to isotopic combinations.
Literature

2. E. Waibel: private communication
<table>
<thead>
<tr>
<th>$T$/days</th>
<th>$k_{\text{eff}}$</th>
<th>Power/MWt</th>
<th>Breeding ratio</th>
<th>Total flux /cm$^{-2}$sec$^{-1}$</th>
<th>Group 1 flux /cm$^{-2}$sec$^{-1}$</th>
<th>Group 2 flux /cm$^{-2}$sec$^{-1}$</th>
<th>Mean activity /C/cm$^{-2}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>full power</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>0</td>
<td>1.0293</td>
<td>1000.</td>
<td>.5181</td>
<td>1.791$\cdot10^{13}$</td>
<td>1.698$\cdot10^{13}$</td>
<td>9.293$\cdot10^{11}$</td>
<td>0</td>
</tr>
<tr>
<td>20.</td>
<td>1.0287</td>
<td>1000.</td>
<td>.5181</td>
<td>1.792$\cdot10^{13}$</td>
<td>1.700$\cdot10^{13}$</td>
<td>9.298$\cdot10^{11}$</td>
<td>31.775</td>
</tr>
<tr>
<td>40.</td>
<td>1.0281</td>
<td>1000.</td>
<td>.5183</td>
<td>1.794$\cdot10^{13}$</td>
<td>1.700$\cdot10^{13}$</td>
<td>9.302$\cdot10^{11}$</td>
<td>38.678</td>
</tr>
<tr>
<td>60.</td>
<td>1.0275</td>
<td>1000.</td>
<td>.5183</td>
<td>1.794$\cdot10^{13}$</td>
<td>1.701$\cdot10^{13}$</td>
<td>9.305$\cdot10^{11}$</td>
<td>40.419</td>
</tr>
<tr>
<td>80.</td>
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Fig. 1: Material transitions for sample problem
Fig. 2: Time dependent homogeneous material densities for sample case
Fig. 3: Isotopic scheme used for the calculation of the generation of transplutonium isotopes.
Fig. 4: Generation of americium isotopes as a function of the flux
Fig. 5: Generation of curium isotopes as a function of the flux.
Fig 6: Generation of berkelium isotopes as a function of the flux
Fig. 7: Generation of californium isotopes as a function of the flux.
Fig. 8: Time dependent formation of californium

\[ \phi = 5 \times 10^{13} \, \text{cm}^{-2} \text{sec}^{-1} \]

\[ \phi = 3 \times 10^{16} \, \text{cm}^{-2} \text{sec}^{-1} \]
Fig. 9: Time dependence of activity

\[ \Phi = 5 \cdot 10^{13} \text{ cm sec}^{-1} \]

\[ \Phi = 3 \cdot 10^{16} \text{ cm sec}^{-1} \]
Fig. 10 Activity as a function of the flux