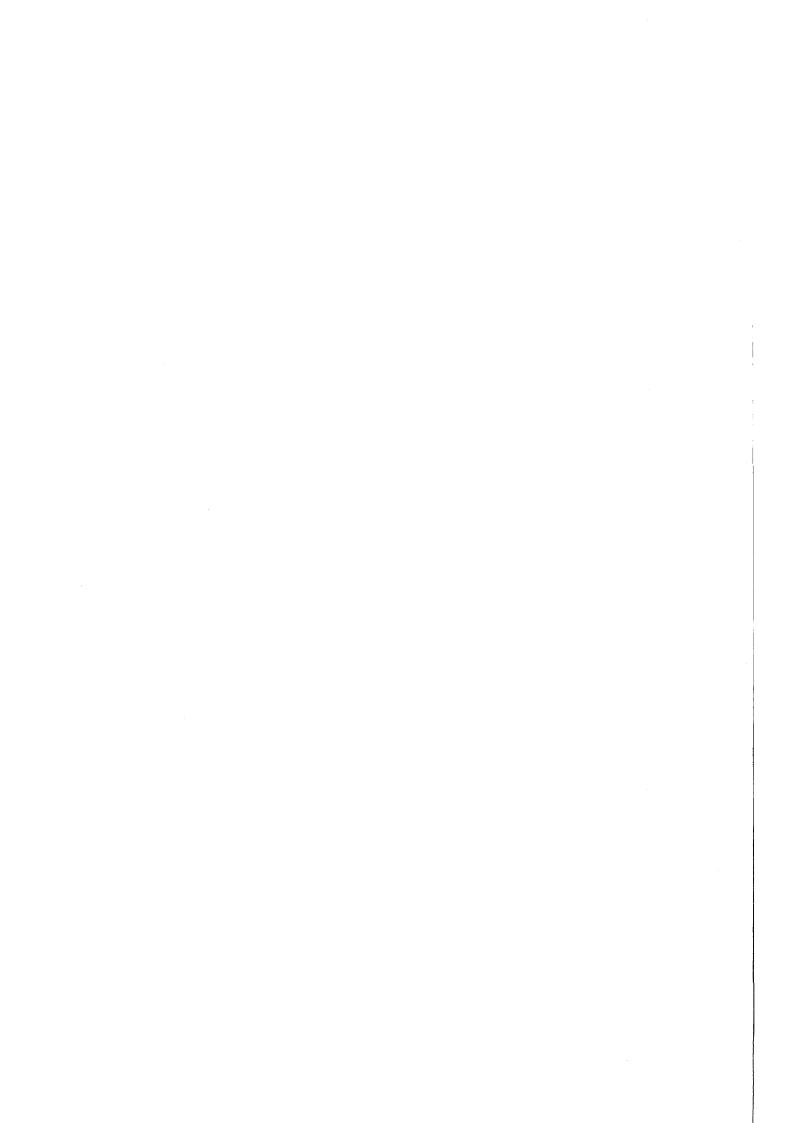
The Karlsruhe 4π Barium Fluoride Detector

K. Wisshak, K. Guber, F. Käppeler, J. Krisch, H. Müller, G. Rupp, F. Voß Institut für Kernphysik Hauptabteilung Ingenieurtechnik

Kernforschungszentrum Karlsruhe



KERNFORSCHUNGSZENTRUM KARLSRUHE Institut für Kernphysik Hauptabteilung Ingenieurtechnik

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Kernforschungszentrum Karlsruhe GmbH, Karlsruhe

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Kernforschungszentrum Karlsruhe GmbH Postfach 3640, 7500 Karlsruhe 1

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ZUSAMMENFASSUNG

DER KARLSRUHER 4π BARIUM FLUORID DETEKTOR

Es wurde ein neuartiges Experiment aufgebaut, um Wirkungsquerschnitte für Neutronen-einfang im Energiebereich von 5 bis 200 keV sehr genau zu bestimmen. Der Karlsruher 4π Barium Fluorid Detektor besteht aus 42 Kristallen in der Form von fünf- und sechseckigen Pyramidenstümpfen. Sie bilden eine Kugelschale mit 10 cm Innenradius und 15 cm Dicke. Jeder Kristall ist mit Reflektor und Photomultiplier ausgerüstet und stellt einen unabhängigen Detektor für Gammastrahlung dar. Jedes Modul erfaßt von einer Gammaquelle im Zentrum des Detektors den gleichen Raumwinkel.

Die Energieauflösung des 4π Detektors beträgt 14% bei $662\,\mathrm{keV}$ und 7% bei $2.5\,\mathrm{MeV}$ Gammaenergie. Die Zeitauflösung ist $500\,\mathrm{ps}$ und die Nachweiswahrscheinlichkeit für die volle Energie der Gammaquanten 90% bei $1\,\mathrm{MeV}$. Diese einmalige Kombination von Eigenschaften wurde jetzt bei einem Detektor für Gammastrahlen ermöglicht, da seit kurzem Barium Fluorid Kristalle mit einem Volumen bis zu $2.5\,\mathrm{I}$ erhältlich sind. Mit dem Detektor kann die Gamma-Kaskade nach Neutroneneinfang mit 95% Wahrscheinlichkeit oberhalb einer Schwelle von $2.5\,\mathrm{MeV}$ nachgewiesen werden.

Die Neutronen werden mit dem gepulsten Protonenstrahl eines Van de Graaff Beschleunigers über die ⁷Li(p,n)⁷Be Reaktion erzeugt. Durch geeignete Wahl der Protonenenergie läßt sich das Neutronenspektrum im Energiebereich von 5 bis 200 keV an die experimentellen Anforderungen anpassen. Ein gebündelter Neutronenstrahl geht durch den Detektor und trifft die Probe in seinem Zentrum. Die Energie der eingefangenen Neutronen wird über Ihre Flugzeit bestimmt, der Flugweg beträgt 77 cm.

Die Kombination aus kurzem Flugweg, 10 cm Innenradius der BaF₂ Kugelschale und dem geringen Einfangquerschnitt von Barium erlaubt es, den Untergrund durch Einfang gestreuter Neutronen im Szintillatormaterial auf Grund seiner Zeitstruktur vom Messeffekt zu unterscheiden. Diese Eigenschaft, zusammen mit der guten Energleauflösung und der hohen Ansprechwahrscheinlichkeit, ermöglicht es, die verschiedenen Komponenten des Untergrundes so gut vom Messeffekt zu trennen, daß das Verhältnis der Wirkungsquerschnitte zweier Isotope mit einer Genauigkeit ≤1.2 % bestimmt werden kann.

Der Detektor wird für astrophysikalische Untersuchungen, die der Erforschung des Ursprungs der schweren Elemente dienen, eingesetzt.

ABSTRACT

A new experimental approach has been implemented for accurate measurements of neutron capture cross sections in the energy range from 5 to 200 keV. The Karlsruhe 4π Barium Fluoride Detector consists of 42 crystals shaped as hexagonal and pentagonal truncated pyramids forming a spherical shell with 10 cm inner radius and 15 cm thickness. All crystals are supplied with reflector and photomultiplier, thus representing independent gamma-ray detectors. Each detector module covers the same solid angle with respect to a gamma-ray source located in the centre.

The energy resolution of the 4π detector is 14% at 662 keV and 7% at 2.5 MeV gamma-ray energy, the overall time resolution is 500 ps and the peak efficiency 90% at 1 MeV. This unique combination of attractive features for a gamma-ray detector became possible by the recent availability of large barium fluoride crystals with volumes up to 2.5 l. The detector allows to register capture cascades with 95% probability above a threshold energy of 2.5 MeV in the sum energy spectrum.

Neutrons are produced via the ⁷Li(p,n)⁷Be reaction using the pulsed proton beam of a Van de Graaff accelerator. The neutron spectrum can be taylored according to the experimental requirements in an energy range from 5 to 200 keV by choosing appropriate proton energies. A collimated neutron beam is passing through the detector and hits the sample in the centre. The energy of captured neutrons is determined via time of flight, the primary flight path being 77 cm.

The combination of short primary flight path, a 10 cm inner radius of the spherical BaF_2 shell, and the low capture cross section of barium allows to discriminate background due to capture of sample scattered neutrons in the scintillator by time of flight, leaving part of the neutron energy range completely undisturbed. This feature together with the high efficiency and good energy resolution for capture gamma-rays allows to separate the various background components reliably enough, that the capture cross section ratio of two isotopes can be determined with an accuracy of $\leq 1.2\%$.

The detector will be used for nuclear astrophysics to investigate the origin of the heavy elements in the slow neutron capture process.

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1 INTRODUCTION

One of the main topics of nuclear astrophysics is the origin of the chemical elements and of their isotopes [1,2,3]. It is generally accepted that only the lightest nuclei are produced in the big bang, i.e. H, He and small amounts of Li. All other elements are built up in stars. While elements lighter than iron (Z < 26) are produced in fusion reactions, all heavier elements from zink up to uranium can only be synthesized by successive neutron capture reactions.

According to the time scale for neutron capture, two nucleosynthesis processes can be distinguished. The slow neutron capture process (s-process) occurring at a neutron density of some 10^8 cm⁻³ is characterized by time intervals of 1 to 10 y between successive capture events. The rapid neutron capture process (r-process) is realized in szenarios with much higher neutron densities of > 10^{20} cm⁻³ leading to capture times of the order of milliseconds.

For any quantitative s-process model the neutron capture cross sections of the involved isotopes are the most important input data [4]. Due to the comparably long time scale, the nuclei synthesized in the s-process are located in the valley of β -stability, and are thus accessible to laboratory experiments. As the s-process occurs in stars during helium burning (i.e. during the late stages of stellar evolution) at typical temperatures of 200 – 300 million K, the corresponding neutron spectrum represents a Maxwell-Boltzmann distribution with a thermal energy around kT=25 keV. Hence, experimental determinations of the relevant capture cross section have to cover the energy range up to 200 keV.

Many investigations during the last years showed [4] that the accuracy of 5-10% that can be achieved for the neutron capture cross sections with established techniques is not sufficient to constrain the physical conditions during the s-process reliably. This would require an accuracy of the order of 0.5 to 1%. In that context, it is sufficient to know the neutron capture cross section ratio relative to the standard cross section of gold with that precision. Therefore, it was our aim to implement a new and precise technique for the determination of neutron capture cross sections in the neutron energy range from 5 to 200 keV.

Detailed design studies resulted in a 4π BaF $_2$ detector with about 100% efficiency for gamma-rays in the energy range up to 10 MeV. It is the first spherical symmetric 4π detector made from this material, which shows outstanding features for gamma-ray detection [5]. The Karlsruhe 4π detector is the second approach of a large BaF $_2$ array after the Crystal Castle [6] that was constructed for investigating heavy ion reactions and has a geometry symmetric to the horizontal plane.

The detector consists of 42 crystals shaped as hexagonal or pentagonal truncated pyramids forming a spherical shell with 10cm inner radius and 15 cm thickness. The spectrometer is a versatile instrument not only suited for neutron capture cross section measurements. It allows for the simultaneous determination of gamma-ray multiplicities, angular distributions, and gamma-ray spectra. In connection with the 3 MV Van de Graaff accelerator, the experimental setup can also be used to measure (p,γ) and (α,γ) reactions, which are of interest for the nucleosynthesis of light elements. If used as a multiplicity spectrometer, the determination of the fission to capture cross section ratio of actinide isotopes, which is of importance for reactor applications is also possible.

The first attempt to measure neutron capture events with a 4π detector of good energy resolution and high efficiency was made by Muradyan et al. [7]. However, the use of NaI(TI) as detector material did not allow for very accurate measurements in the keV neutron energy range (§ 2.2). The same holds for a significantly smaller spectrometer described by Block et al. [8]. Both instruments are well suited for measurements below 1 keV neutron energy, where the detector can easily be shielded from scattered neutrons. BGO as detector material was used by Yamamoto et al. [9]; however, their design is simpler and less efficient, and hence not suited for the accuracy almed at in our approach. Presently, a 4π BaF $_2$ detector is under construction at the LANSCE facility in Los Alamos [10]. It has about the same efficiency as the Karlsruhe detector, but an important feature of the present setup is lost: because the scintillator is immediately surrounding the sample, it does not allow for the discrimination of background due to sample scattered neutrons by time of flight (§ 2.3).

The first proposal for the present detector was still based on BGO as scintillator [11]. The gamma-ray efficiency of a spherical shell of BaF_2 and BGO for monoenergetic

gamma-rays and neutron capture cascades has been calculated by Wisshak et al. [12]. The properties of large BaF_2 crystals for the detection of energetic photons and the first tests of prototype modules for the present design are documented in refs. [13, 14, 15].

In the present paper we summarize in § 2 the basic requirements, which have to be met by a detector for the precise determination of neutron capture cross sections as well as the corresponding design studies. The mechanical construction of the 4π detector and the features of the individual detector modules are given in §§ 3 and 4. The subsequent §§ 5 and 6 describe the electronics, and the detector operation, while the detector performance is presented in § 7. Finally, first results from neutron capture measurements are discussed in § 8, and further improvements are considered in § 9.

2 DESIGN STUDIES FOR A NEUTRON CAPTURE DETECTOR

2.1 BASIC REQUIREMENTS

The unambiguous registration of a neutron capture reaction, which is required for the accurate determination of the cross section is hampered by the fact that there is a more complex signature in the exit channel as, e.g. in (n,p) or (n,α) reactions. Neutron capture events are characterized by a cascade of prompt gamma-rays. The multiplicity and the energies of the individual gamma quanta are determined by the transition probabilities to a great variety of accessible nuclear levels. The only fixed quantity is the sum energy of the cascade that corresponds to the binding energy of the captured neutron (6-8 MeV for most of the isotopes of interest for s-process studies) increased by the kinetic energy of the captured neutron. For isotopes with Z larger than ~26, the level density at excitation energies of several MeV is so large that the capture cross section is composed of contributions from many possible cascades as indicated schematically in fig.1. According to statistical model calculations for neutron captures in gold [16], more than 4000 possible cascades have to be considered in order to cover 95% of the cross section. For medium weight isotopes like ⁵⁶Fe, the respective number is still 300 [12,17]. The average gamma-ray multiplicity of the cascades is 3-4 with maximum values up to 10.

Therefore, the essential requirements of an improved detector for neutron capture cross section measurements are the following:

- (i) Efficiency of about 100% for gamma-ray energies up to 10 MeV.
- (ii) Good energy resolution (10% at 1 MeV).
- (iii) Good time resolution ($\Delta t = 1 \text{ ns}$).
- (iv) Low sensitivity for the detection of neutrons scattered into the detector material.

The first feature guarantees that all gamma-rays of the capture cascade are registered in the detector; their sum corresponds to the total gamma-ray energy, which is the only true signature of a capture event. This feature is also important as it makes the detector efficiency independent of gamma-ray multiplicity.

If the second requirement can be realized simultaneously, the capture events show up in the sum energy spectrum as a sharp line indicated schematically in fig. 1. Hence, they appear well separated from the expected gamma-ray background at low energies, resulting in favorable signal to background ratios. A good time resolution is essential as the energy of the captured neutron has to be determined by the time of flight (TOF) technique. In the present application, it is also useful for the TOF discrimination of background due to sample scattered neutrons (§ 2.3).

The last requirement is of key importance for the neutron energy range above $\sim 1\,\mathrm{keV}$, where the cross sections for neutron scattering are typically 10 to 100 times larger than for capture. If these scattered neutrons are captured in the detector material, it is very difficult to distinguish this background from true capture events in the sample.

Historically, the first approach to measure neutron capture cross sections by the TOF technique was to use large liquid scintillator tanks for the detection of capture gamma-rays [18,19]. The main disadvantage of these detectors is their poor energy resolution, which does not allow to separate capture events sufficiently well from the background due to the 2.2 MeV gamma-ray line from neutron captures in the hydrogen of the scintillator. In addition, the 60% efficiency of a 800 I tank for gamma-rays of 6 MeV is too low to ensure that the detection of a capture cascade does not depend on the multiplicity. As these problems cause systematic uncertainties of about 10%, this method was abandoned some ten years ago.

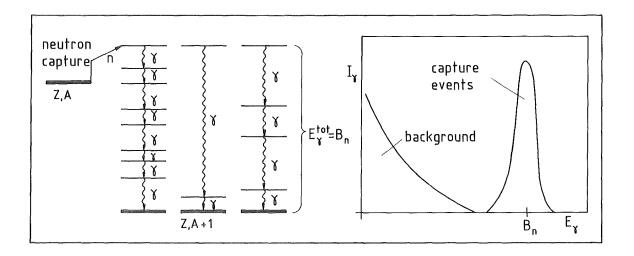


Fig. 1 Left: The excited states in the compound nucleus that are populated by neutron capture can decay via many different gamma-ray cascades. Right: A 4π detector with 100% efficiency adds these cascades in an isolated line at the binding energy of the captured neutron, well separated from most of the background.

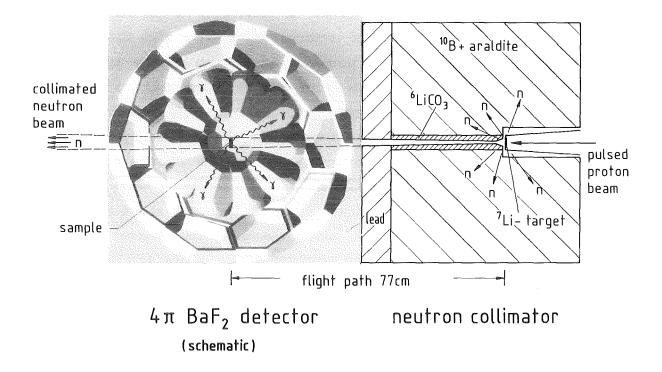


Fig. 2 Schematic setup of the Karlsruhe 4π BaF $_2$ detector for the determination of neutron capture cross sections in the energy range from 5 to 200 keV.

A completely different approach was introduced by Moxon and Rae [20]; the absolute efficiency of their detector is small, but increases linearly with gamma-ray energy. The combination of these features yields a detection probability for capture events independent of gamma-ray multiplicity. The efficiency for a capture cascade is given as the sum over the individual cascade gamma-rays

$$\varepsilon_{capt} = \sum \varepsilon(E_{\gamma}) = \sum k E_{\gamma} = k E_{\gamma,tot}$$

and is thus proportional to the total gamma-ray energy after averaging over a sufficient number of events. Obviously, the detection probability for a cascade of 6 gamma-rays of $1\,\text{MeV}$ is the same as for a single gamma-ray of 6 MeV provided that gamma-rays of the first cascade are not detected simultaneously. The main disadvantage of this method is the low efficiency of about 1% at $1\,\text{MeV}$. In practice, there are also deviations from the ideal shape of the efficiency causing systematic uncertainties of 3-10% depending on the capture gamma-ray spectrum [17,21].

The third method, which was most widely used in the last years [22,23] takes an intermediate position between the two extremes described above. A hydrogen-free liquid scintillator like C_6D_6 or C_6F_6 of about 1 I volume is used for the detection of capture gamma-rays. It combines an efficiency of about 20% for capture cascades with a very low sensitivity to capture of scattered neutrons. For these detectors, a linear increase of the efficiency with gamma-ray energy can only be achieved by means of a so called weighting function: each measured pulse height is multiplied with the corresponding value of the weighting function, such that the inherent efficiency is properly corrected. Traditionally, the weighting function was calculated by considering the response of the scintillator for gamma-rays, but also the influence of detector canning, sample and all surrounding materials of the experimental setup. Recently, the weighting function was determined experimentally [24], showing severe discrepancies to previous calculations at high gamma energies. This implies that the detection of energetic Compton electrons produced outside of the scintillator were probably not correctly treated in the earlier calculations, and may explain large discrepancies in experimental results obtained with different setups [21, 25, 26]. This problem being often not sufficiently considered, casts some doubt on the optimistic uncertainties, that are sometimes claimed for cross sections determined with this method.

In summary, the existing experimental techniques are not suited for obtaining the

accuracy required in analyses of the astrophysical s-process. The present approach returns to the old concept of 100% efficiency for all gamma-rays, but replacing the liquid scintillator by scintillator crystals with good energy resolution. This became possible with the advent of scintillators showing low sensitivity to capture of scattered neutrons.

The design criteria for the new 4π BaF₂ detector are closely related to the experimental conditions at Karlsruhe. Accordingly, fig. 2 shows the schematic setup for measurements using a Van de Graaff accelerator. Neutrons are produced via the $^7\text{LI}(p,n)^7\text{Be}$ reaction with a pulsed proton beam of 250 kHz repetition rate and 0.7 ns pulse width. At proton energies of ~2 MeV, continuous neutron spectra in the required energy range from 5 to 200 keV are obtained. A well collimated neutron beam is produced by a carefully designed shield around the lithium target, and hits the sample in the center of the capture gamma-ray detector at a flight path of about 1 m. The complete gamma-ray cascade is registered in the detector, and the energy of the captured neutron is determined via TOF (typically 100-500 ns depending on neutron energy).

The main sources of background in such an experiment are the following:

- (i) Time independent gamma-rays from natural radioactivity of the scintillator crystal, surrounding materials, cosmic-rays, etc;
- (II) Time dependent and time independent background produced by fast and moderated neutrons escaping from the shielding;
- (III) Time dependent background caused by neutrons scattered in the sample and captured in the scintillator or nearby.

The first two components can be minimized by the design of collimator and shielding, whereas the third one depends on the scintillator and canning materials.

2.2 DETECTOR MATERIAL

Application of the four criteria listed in § 2.1 to those scintillator crystals that are available in appropriate sizes for the 4π detector, i.e. to NaI(TI), BGO, CsI(TI) and BaF₂ rules out all materials containing iodine as ¹²⁷I has a large neutron capture cross section of 635 mb at 30 keV [27]. Consequently, scattered neutrons are

immediately captured in the scintillator material, giving rise to unacceptable backgrounds. In the energy range of interest, shielding the detector from scattered neutrons would require thick layers of ¹⁰B, ⁶Li and H (see § 2.4), which in turn would degrade the capture gamma-ray spectrum significantly, thus destroying the advantage of the good energy resolution. Below ~1 keV neutron energy, however, a thin layer of ¹⁰B is sufficient to absorb scattered neutrons, and therefore NaI(TI) can be used as suggested in refs. [7,8].

Compared to NaI(TI), BaF2 and BGO are significantly less sensitive to keV neutrons. The neutron magic isotope ¹³⁸Ba makes up for 72 % of the natural barium abundance; due to its small capture cross section of 3.9 mb at 30 keV [27] the elemental barium cross section is only 50 mb. The respective value for the monotopic element Bi is 11 mb, while the elemental cross section for germanium is 76 mb. The neutron sensitivity of the detector materials can roughly be estimated as the product of the thickness in molecules per cm2 of a spherical shell with comparable efficiency and the capture cross section at 30 keV. For the scintillator materials NaI(TI), BaF2, and BGO it scales as 15:1:0.6, suggesting BGO to be the best choice. However, the binding energies of 135Ba and 137Ba are 9.1 and 8.6 MeV, with both isotopes accounting for 75% of the elemental capture cross section, whereas the respective values for the even germanium isotopes range between 6.5 and 7.4 MeV, contributing 85%. As most of the isotopes of interest for nuclear astrophysics have binding energies between 6 and 8 MeV a significant fraction of this background can be discriminated in BaF_2 detectors by an upper threshold in the sum energy (see § 8). In this way, the neutron background in an actual experiment will be lower for BaF2 .

Other important aspects in favor of BaF_2 compared to BGO are the superior resolution in gamma-ray energy and, especially, in time. In energy resolution, the difference for large crystals is about a factor of two [14, 28, 29, 30], while the time resolution is at least four times better [14, 31]. The only drawback of BaF_2 crystals is the unavoidable contamination with radium, the chemically homologous element to barium, which causes a relatively high time independent background (§ 4.6)

2.3 DESIGN STUDIES AND MONTE CARLO SIMULATIONS

The two most important features of a 4π detector for the detection of neutron

capture events, the efficiency for neutron capture cascades and the background due to sample scattered neutrons, have been simulated on the computer.

The efficiency of a spherical shell of BGO or BaF2 for monoenergetic gamma-rays in the energy range up to 10 MeV has been calculated by Schatz and Oehlschläger [32] using analytical methods. Capture cascades for neutron capture in ⁵⁶Fe, ¹⁹⁷Au, and ²⁴¹Am, three isotopes with widely different capture gamma-ray spectra, have been calculated previously with the statistical and optical model [16, 17, 33]. The combination of both informations allows to determine the pulse height spectra for the expected sum energies of the respective capture reactions [12]. The essential results are plotted in fig. 3 showing the shape of the capture gamma-ray spectra, and in fig. 4, where the corresponding sum energy spectra are displayed for a spherical shell of BaF₂ with 10 cm inner radius and 15 cm thickness. One finds that roughly 95% of the capture events are registered with a sum energy of more than 2.5 MeV. For the cross section ratios o(Fe)/o(Au) or o(Am)/o(Au), the correction due to differences in efficiency is of the order of only 1%, with the respective systematic uncertaintles being well below 0.5%. This holds the more for measurements on neighboring isotopes, e.g. for the important ratio $\sigma(^{148}\text{Sm})/\sigma(^{150}\text{Sm})$, where only small differences in the shapes of the two gamma-ray spectra are expected.

The background due to neutrons scattered from the sample in the centre of the detector was determined by Monte Carlo calculations; the code (appendix A) follows each neutron until it is either captured in the scintillator or it escapes from the detector. For each possibility the time since emission from the sample, the number of scattering interactions, and the final neutron energy were calculated. For neutron captures, the respective position in the scintillator (radius from the centre) was stored as well. The capture and scattering cross sections of up to three materials were used as input to determine the respective reaction probabilities. For scattering events, the scattering angles were randomly selected according to the angular distributions, and the respective energy losses were considered. In this way, the neutrons were followed for up to 100 interactions. If the randomly selected interaction point was located inside the inner sphere, the next interaction was transferred to the opposite part of the spherical shell following a straight line.

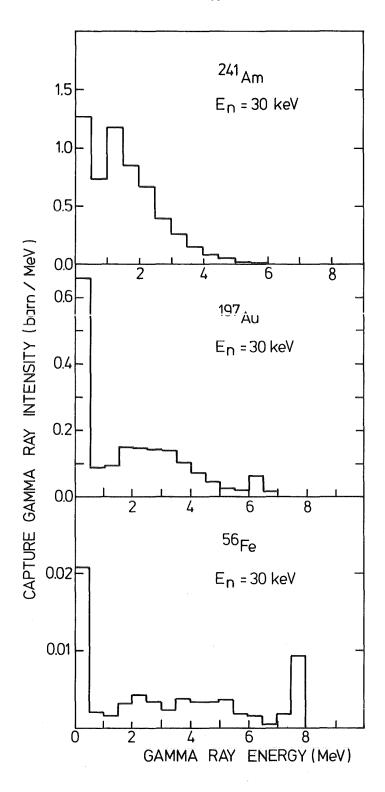


Fig. 3 Gamma-ray spectra calculated for neutron capture in ²⁴¹Am, ¹⁹⁷Au, and ⁵⁶Fe at a neutron energy of 30 keV [16,17].

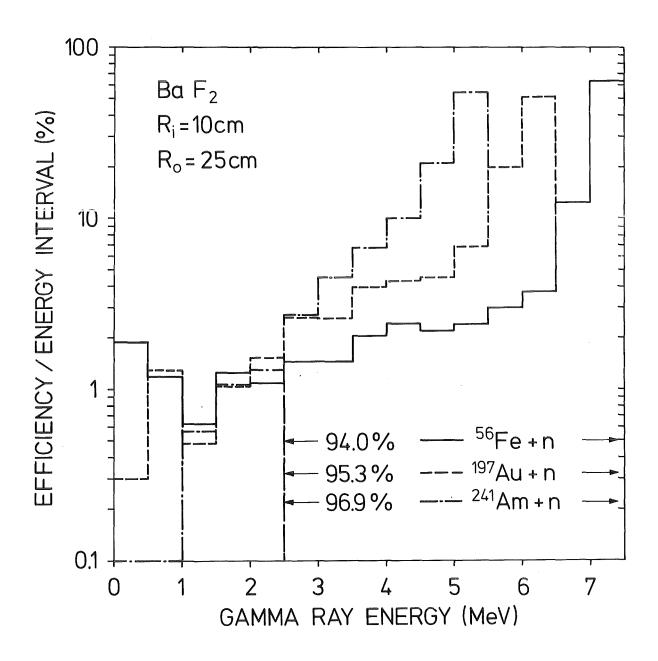


Fig. 4 Calculated pulse height spectra for neutron captures in 56 Fe, 197 Au, and 241 Am for a spherical shell of BaF₂ crystals (R_i = 10 cm, R_o = 25 cm).

Table 1. Capture and escape probabilities for neutrons emitted from the centre of spherical scintillator shells with about equal gamma-ray efficiency. The fourth column denotes the probability for hitting the sample again.

Initial neutron		Probability (%)			Average number of interactions		
energy	(keV)	escape	capture	sample	escape	capture	sample
BaF ₂ (in	ner radius	10 cm, t	hickness	15 cm)			
95		93.5	6.5	2.8	19.7	23.3	5.5
85		93.3	6.7	2.5	17.8	21.9	4.8
75		94.0	6.0	1.9	16.0	21.8	5.5
65		93.9	6.1	1.3	16.1	19.9	5.9
55		92.2	7.8	1.8	17.8	21.0	6.6
45		92.1	7.9	1.8	15.8	19.5	5.0
3.5		91.8	8.2	1.6	15.8	19.3	7.2
25		91.3	8.7	2.2	13.9	19.3	4.4
17.5		89.3	10.7	1.8	13.9	19.1	4.2
12.5		87.2	12.8	2.1	14.0	19.0	4.5
7.5		82.3	17.7	2.1	13.9	17.4	5.0
BGO (Inr	ner radius	10 cm, th	nickness	10 cm)			
95		95.7	4.3	2.0	17.1	26.5	6.7
85		95.3	4.7	2.4	17.5	25.1	6.4
75		94.9	5.1	1.8	17.3	26.9	6.4
65		94.9	5.1	2.3	17.6	27.0	6.1
55		93.8	6.2	2.3	18.0	26.9	6.4
45		93.5	6.5	2.0	18.2	25.8	7.4
35		92.5	7.5	2.2	18.6	27.2	7.0
25		90.6	9.4	2.0	19.0	25.6	7.6
17.5		89.5	10.5	2.0	19.6	26.9	8.5
		85.7	14.3	3.0	23.1	28.2	7.0
12.5							

Table 1 continued

Initial neutron	Pro	bability (%	()	Average number of interactions		
energy (keV)	escape	capture	sample	escape	capture	sample
Nal(TI) (inner rad	ius 10 cm,	thickness	25 cm)			
95	59.3	40.7	1.5	9.5	9.3	3.2
85	56.6	43.4	1.5	9.5	9.2	2.9
75	53.7	46.3	1.5	9.7	8.9	2.9
65	51.5	48.5	1.0	9.4	8.9	3.3
55	43.3	56.7	2.2	11.2	9.3	2.7
45	46.0	54.0	1.5	8.6	7.7	2.7
35	41.5	58.5	1.5	8.3	7.4	2.8
25	35.3	64.7	1.4	8.0	7.4	3.2
17.5	28.9	71.1	2.0	8.0	7.0	2.8
12.5	22.6	77.4	1.4	7.7	7.5	2.8
7.5	11.9	88.1	1.5	10.9	10.2	3.4

The resulting time and energy spectra for captured and escaping neutrons were calculated as a function of the initial neutron energy, using the data of spherical shells of BaF2, BGO, and NaI(TI) as input. The probabilities for capture in or escape from the detector are compiled in table 1 for neutrons in the energy range from 5 to 100 keV. The fourth column in table 1 gives the probability that the neutron hits the sphere with 1 cm radius around the centre, showing that the chance for delayed capture events is very small. The dimensions of the detectors were such as to obtain about equal efficiency. The columns 5 to 7 present the respective average number of interactions in the scintillator. The probability for a neutron to escape from the scintillator shows little difference for BaF_2 (91 %) and BGO (92 %), while it is only 41% for Nal(TI). Note, that neutron captures in the first two materials occur on average only after 20 to 25 scattering interactions; this means that these events are strongly delayed in time with respect to the primary interactions. In NaI(TI) neutrons are already captured after 8 interactions. The time and energy spectra for incident neutron energies of 100 and 25 keV and the number of scattering interactions are plotted in fig. 5 for the ${\rm BaF}_2$ scintillator. The total number of Monte Carlo histories is 10000.

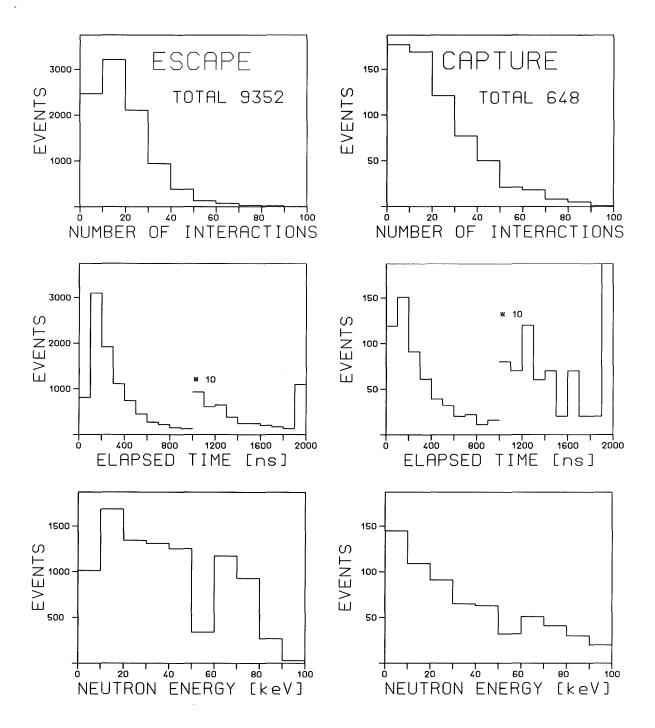


Fig. 5 a) Monte Carlo calculations of the energy and time distributions of neutrons escaping from or being captured in the spherical BaF_2 shell (R_i = 10 cm, R_0 = 25 cm), assuming that 100 keV neutrons start at time zero from the centre. The number of interactions are shown on top.

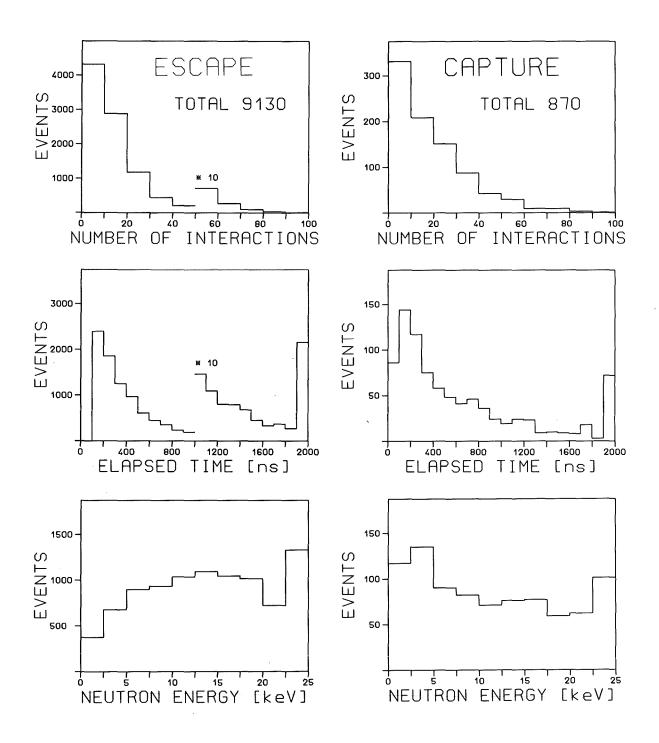


Fig. 5 b) as fig. 5.a, but for 25 keV neutrons.

The situation of an actual experiment is simulated according to the following assumptions:

- (i) The shape of the neutron energy spectrum is that of the ⁷LI(p,n)⁷Be reaction at a proton energy 30 keV above threshold ranging from 5 to 100 keV (§ 8).
- (ii) The capture cross section of the sample follows the 1/v law.
- (iii) The scattering cross section is ten times larger than the capture cross section.
- (iv) The primary flight path is 80 cm.
- (v) The 4π detectors have 10 cm inner radius and about equal gamma- ray efficiency.

The result of this calculation is given in fig. 6, which compares the TOF spectra of the capture events in the sample with the background due to neutrons scattered in the sample and captured in the scintillator. While captures in the sample are concentrated in a time interval of about 200 ns, events due to capture of scattered neutrons are spread out in time over more than 2 µs. Therefore, the pulse repetition rate of the accelerator has to be smaller than 500 kHz to ensure that all neutrons of the previous pulse have escaped the scintillator or are captured (§ 8). Then, most of the related background falls outside the time interval used for data evaluation.

In case of BaF $_2$ and BGO the number of true capture events is slightly larger than the total number of background events. This confirms again the >90% escape probability for the scattered neutrons that compensates for the ten times larger scattering cross section. Note also that there is a neutron energy interval from 100 to 60 keV, which is almost undisturbed by capture of sample scattered neutrons due to the additional 10 cm flightpath between sample and the inner radius of the spherical shell. This region of optimum signal to background ratio will be important for the normalization of the cross section (§ 8). The results for Nal(TI) show a much larger background due to the capture cross section of iodine. As the binding energy of iodine is 6.8 MeV and thus very close to the isotopes to be investigated, there is no chance to reduce this background by cuts in the sum energy spectrum (see below).

As an additional information, the radial distribution of neutron captures in the BaF_2 scintillator was determined for the first 200 ns after scattering in the sample. The results are plotted in fig. 7 for three neutron energies. As most of these events are

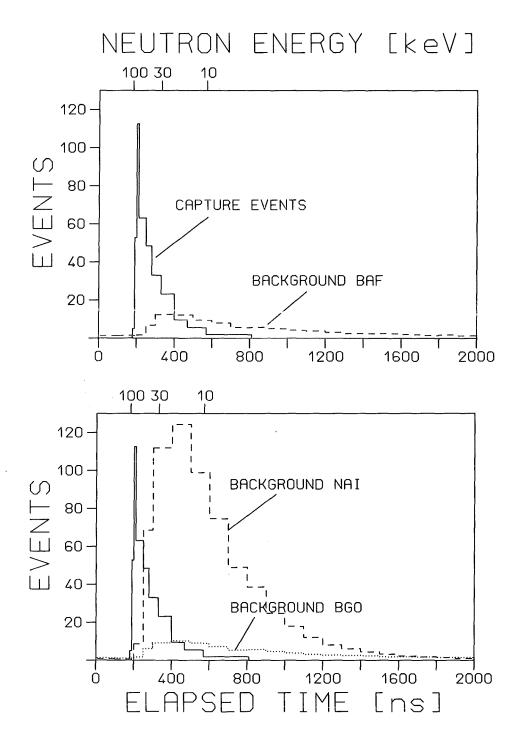


Fig. 6 Time distribution of capture events and background due to sample scattered neutrons, calculated for a neutron spectrum with 100 keV maximum energy, a flight path of 80 cm, a capture to scattering ratio of 1:10. The data are given for scintillator shells of about equal gamma-ray efficiency.

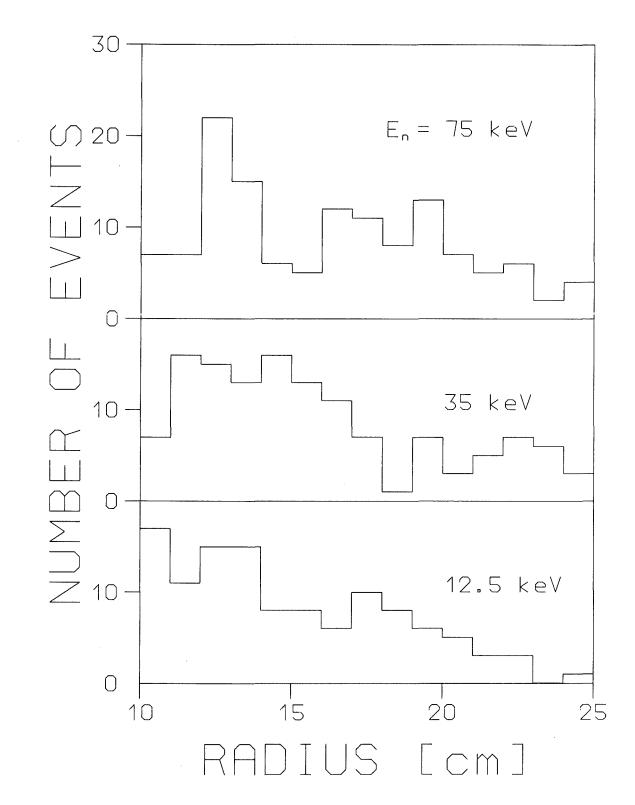


Fig. 7 Radial distribution of capture events in a spherical shell of BaF_2 caused by neutrons starting with different energies from the centre.

concentrated near the inner surface of the detector, there is a high probability for observing the full capture cascade. This offers the possibility to discriminate these events by selecting appropriate energy windows in the sum energy spectra if the binding energy of the measured isotope differs from that of ¹³⁵Ba and ¹³⁷Ba (§ 8).

The above calculations clearly reveal two restrictions for the suggested experimental setup:

- (i) Nal(Ti) cannot be used as detector material for accurate measurements of neutron capture cross sections in the keV range.
- (ii) The TOF discrimination of background from sample scattered neutrons is lost if the primary flight path between neutron source and sample is much longer than the inner radius of the detector. For example, in LINAC experiments the minimum primary flightpath is 10 m. Correspondingly, the above neutron spectrum between 10 and 100 keV covers a time interval of 5 μs in the primary beam. This means that the additional time spread of 2 μs for the sample scattered events does no longer allow to discriminate this type of background; the background spectrum has the same shape and the same size as the measured effect, resulting in a signal to background ratio of unity. The present design is therefore particularly sulted for the short flight paths of Van de Graaff experiments.

2.4 SHIELDING OF SCATTERED NEUTRONS

The Monte Carlo code described above can also be used to calculate the effect of a neutron shield around the sample, if the cross sections for the scintillator are replaced by the respective values for the shielding materials. Efficient shieldings can be constructed using mixtures of boron and hydrogen in the atomic ratios 1:1 or 1:2. Calculations were made for B₁₀H₁₄ assuming 100% enrichment in ¹⁰B (and neglecting that this compound is an explosive). The results for a spherical shell with 2 and 4 cm thickness are compiled in table 2. Even a thickness of 4 cm is found to reduce the flux at 100 keV only by a factor of 10. These results confirm again that Nal(TI) is not a suited scintillator for the present setup even with the best shielding against scattered neutrons. Apart from the fact that the neutron flux at 100 keV is not sufficiently reduced, such shieldings around the sample are severely degrading the gamma-ray spectra by Compton scattering and cannot be used for this reason as well.

Table 2. Capture and escape probabilities for neutrons emitted from the centre of a spherical $B_{10}H_{14}$ shell enriched to 100% in ^{10}B . The fourth column denotes the probability for hitting the sample again.

Initial neutron	P	robability	(%)	Average	number of	interactions
energy (keV)	escape	-	sample	escape	capture	sample
B ₁₀ H ₁₄ (inner radius	s 6 cm, thi	ckness 4	cm)			-
100	10.7	89.3	0.3	3.6	4.2	2.6
90	9.5	90.5	0.4	3.8	4.1	2.5
80	8.8	91.2	0.4	3.8	4.1	2.6
70	7.2	92.8	0.3	3.9	4.1	2.9
60	7.1	92.9	0.3	3.8	4.0	2.7
50	6.0	94.0	0.3	3.9	3.9	2.2
40	4.3	95.7	0.3	4.0	3.8	2.7
30	3.6	96.4	0.3	3.9	3.6	3.1
20	2.8	97.2	0.1	4.2	3.5	2.6
10	1.3	98.7	0.2	3.6	3.1	2.5
B ₁₀ H ₁₄ (inner radius	8 cm, thi	ckness 2	cm)			
100	40.0	60.0	0.4	2.5	3.7	2.5
90	37.1	62.9	0.2	2.6	3.7	2.9
80	35.5	64.5	0.2	2.6	3.7	2.7
70	34.6	65.4	0.3	2.7	3.6	2.6
60	32.9	67.1	0.2	2.7	3.6	3.0
50	29.6	70.4	0.2	2.7	3.5	2.4
40	26.2	73.8	0.1	2.8	3.4	3.7
30	23.0	77.0	0.2	2.8	3.3	2.6
20	21.3	78.7	0.2	2.8	3.2	2.8
10	15.3	84.7	0.1	2.7	2.9	2.8

3 DESIGN OF THE KARLSRUHE 4π BARIUM FLUORIDE DETECTOR

3.1 DETECTOR GEOMETRY

For the design of the detector geometry the following aspects have been considered:

- (i) Maximum efficiency for capture gamma-rays with minimum scintillator volume.
- (II) The efficiency for gamma-rays should be sufficient to register 95 % of the capture events above a threshold energy of 2.5 MeV in the sum energy spectrum.
- (iii) The distance between sample and scintillator should be as large as possible for optimum TOF discrimination of events due to sample scattered neutrons.
- (iv) To minimize the number of modules, the detector should be built from the largest commercially available BaF₂ crystals; at the time of ordering these were rough crystals of 14 cm diameter and 17.5 cm length.

The first item stands for a maximum signal to background ratio with respect to background caused by natural radioactivity in the scintillator and its environment, as well as by moderated neutrons escaping from the collimator. The second feature can be satisfied by a BaF_2 thickness of 15 cm according to ref. [12]. The contradictory points (i) and (iii) were compromised by choosing an inner radius of 10 cm for the spherical shell. Then, the scintillator volume is about 60 I, four times larger than the minimum value for zero inner radius. On the other hand, an inner radius of 10 cm together with the minimum flightpath of 77 cm (§ 8) offers a sufficiently wide region in the TOF spectra free of events from scattered neutrons; this last feature is important for the success of the proposed method (§§ 2, 8).

The problem of subdividing a spherical shell into individual crystals has previously been studied for the 4π Nal(TI) detectors, e.g. the spin spectrometer [34] or the Heidelberg Crystal Ball [35]. Under the constraints of symmetry, ease of construction and minimum cross talk between individual detector modules it was shown that the class of optimum polyhedra always has 12 pentagons and a varying number of hexagons. The configurations can be derived from the classical regular polyhedrons by subdividing the triangle of the icosahedron or the five triangles forming the pentagon of the dodecahedron in an increasing number of new triangles, which are then recombined to pentagons and hexagons. This yields new polyhedra with discrete "magic" numbers of elements, i.e. 32, 42, 72, 92, 122, 132, 162 etc.

A detector for neutron cross section measurements should consist of as few elements as possible, in order to avoid losses in gaps. For the investigation of individual capture cascades and angular distributions, the granularity should be ~5 times larger than the expected average cascade multiplicity of 3 to 4 with only a small fraction being above 6. While an array of 32 elements would be sufficient in this respect, the next "magic" number 42 had to be chosen because of the limited size of the available BaF₂ crystals.

As shown in fig. 8, this configuration is constructed by dividing each of the five triangles forming the pentagon of the dodecahedron into four new triangles. The upper of these triangles together with its neighbors form the new pentagon, while the three lower ones are combined with the respective three of the next triangle to the new hexagon. The arc lengths of the hexagons and pentagons inscribing a touching sphere of unity radius are also given in fig. 8. These values were calculated with the boundary condition that both elements cover the same solid angle. The coordinades of the centres, corners and mid points of the edges of all 42 hexagons and pentagons forming the spherical supporting structure of the detector with 430 mm radius (§ 3.2) are given in Cartesian and polar coordinates in appendix B.

3.2 MECHANICAL SETUP

The final shape of the two types of BaF_2 crystals ordered from the manufacturer (Merck, Darmstadt, Fed. Rep. of Germany) is shown in fig. 9. (A more detailed drawing can be found in appendix C). Each crystal is cut from a cylindrical rough slug of 14 cm diameter and 15 cm thickness, so that at the base about 6% of the truncated pyramids are not filled with BaF_2 ; this part is used for fixing the crystals in the supporting structure. The volume of the real crystals is compared in table 3 with the volume of perfect truncated pyramids. It is shown that the real volume is practically the same as that of the intended spherical shell with 10 cm inner radius and 15 cm thickness.

Each crystal is wrapped in a reflector and supplied with an own photomultiplier, thus representing an independent gamma-ray detector. The mechanical construction is illustrated in fig. 10. The crystal is fixed in a cylindrical glass fibre tube by a metal ring lock. The front end of this tube is shaped such as to use that volume of the

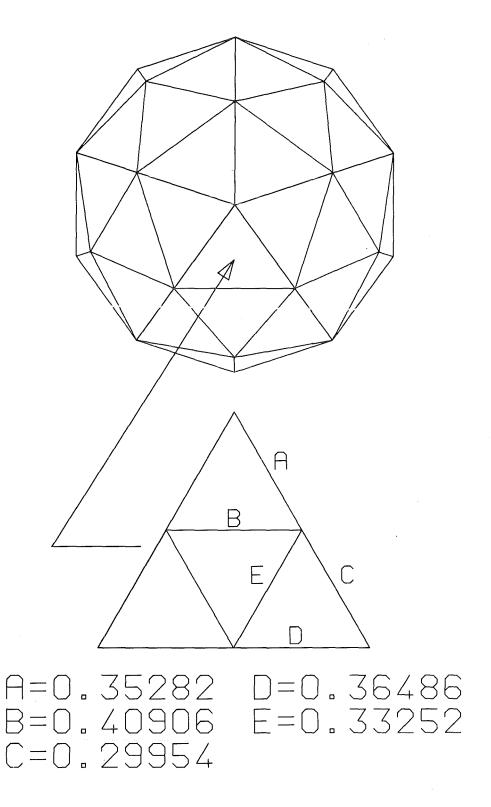


Fig. 8 Arclengths of hexagons and pentagons forming a polyhedron with 42 elements with an inscribed touching sphere of unit radius.

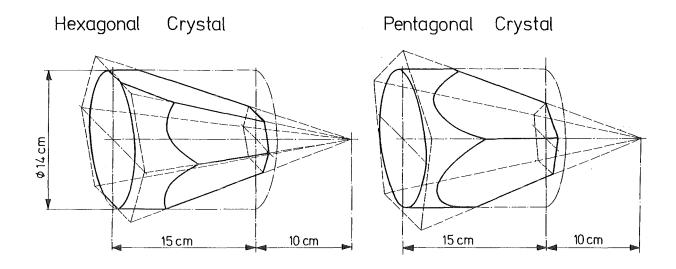
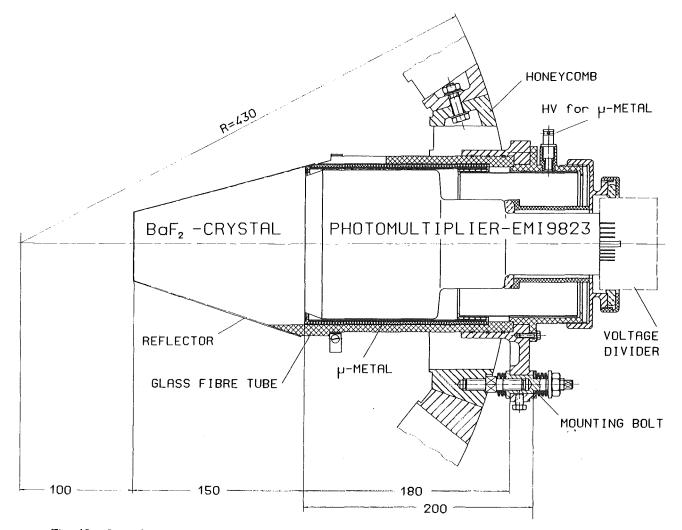


Fig. 9 Shape of the hexagonal and pentagonal BaF $_2$ crystals for the Karlsruhe 4π detector (for details see appendix B).



Flg. 10 Cut through one detector module and its mounting in the supporting structure.

truncated pyramid that is not covered by BaF₂ scintillator. The rear end of the tube is glued into a triangular aluminum flange, which is fixed and adjusted in the supporting honeycomb structure. The crystals are covered on all sides with a reflector for the scintillation light leaving only a circular hole of 12 cm diameter for connection of the photomultiplier.

The reflector consists of two layers of 0.1 mm thick unsintered PTFE tape followed by an 0.1 mm polished aluminum foil, and an outer layer of black tape. The photomultipliers (EMI 9823 QKA) are optically coupled to the crystal using silicon oil (Baisilone) with a viscosity of 500 000 cst. A rubber O-ring is used to prevent the silicon oil from creeping into the reflector. The photomultipliers are magnetically shielded by three layers of 0.1 mm thick μ -metal sheets; optionally this shield can be connected with the negative cathode potential to eliminate the influence of external electric fields. The cross hatched parts in fig. 10 are made from insulating synthetic material, while the hatched parts are from aluminum.

The individual detector modules are fixed in the spherical honeycomb structure consisting of aluminum frames by means of three bolts. A set of elastic springs on each side of the flange provides a flexible mounting. The bolts are subdivided into two parts connected by a thread; continuous variation of their length enables the accurate adjustment of the detector modules.

The hexagonal and pentagonal frames of the honeycomb structure form a sphere with 860 mm diameter. The construction of this sphere as well as of the mounting bolts followed closely the example of the Heidelberg Crystal Ball detector [36]. The sphere is subdivided into two parts with 25 and 17 modules, respectively, which are fixed in octagonal stands as shown in fig. 11. Each stand is mounted on a slide and can be moved separately on rails over a distance of ~1 m. This allows to change the experimental flight path between neutron target and sample and to open the detector for access to the samples. Details of the mechanical construction can be found in appendix C.

The neutron beam passes the detector horizontally through two opposite hexagonal frames. Perpendicular to the beam axis, a sample changer passes through a rectangular grove of 30×10 mm in two opposite crystals; it carries up to eight samples,

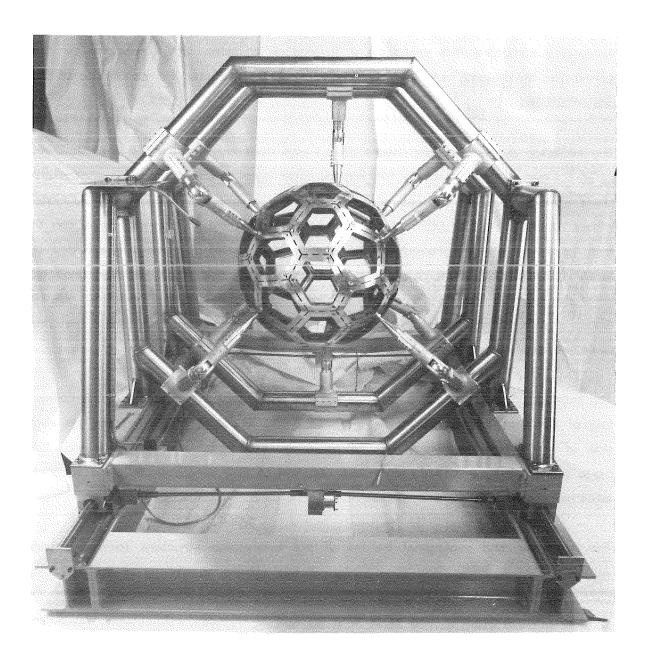


Fig. 11 The supporting honeycomb structure for the detector modules; the octagonal stands move on rails for opening the detector.

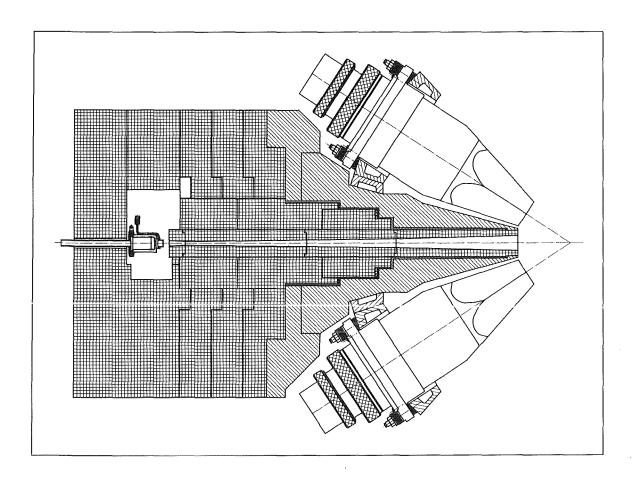


Fig. 12 The neutron target and the central part of the neutron collimator (hatched parts are made from lead and cross hatched parts from a mixture of boron carbide and analdite).

Table 3. Volume of the truncated hexagonal and pentagonal pyramids and the real crystals (liter).

	Hexagon	Pentagon
Truncated pyramid:	1.573	1.571
Real crystal:	1.472	1.484
Difference:	6.4%	5.5%

Volume of a spherical shell with $R_i = 10$ cm and $R_o = 25$ cm : 61.3 |

Volume of 12 pentagonal and 30 hexagonal truncated pyramids: 66.0 l

Volume of 12 pentagonal and 30 hexagonal crystals: 62.0

which can be cycled into the measuring position by means of a computer controlled stepping motor. The samples are fixed on two 0.1 mm thick steel wires at selectable distances of up to 10 cm.

For the passage of the neutron beam two special crystals have been ordered with a central hole of 50 mm diameter. Each of these crystals will be equipped with six 1.5 inch photomultipliers (EMI 9902 QKA).

The water cooled lithium target for neutron production and the central part of the neutron collimator are shown in fig. 12. The first measurements will be performed with the minimum possible flightpath in order to obtain maximum neutron flux at the sample position. For this purpose the hexagonal crystal at the entrance of the neutron beam was removed using the free space for the collimator. The collimator is build in modular form using individual blocks made from natural boron carbide and araldite mixed in a ratio of 5:4 by weight. The inner cylinder can be replaced separately in order to change the beam diameter at the sample position, which is 24 mm in the present design. For the central part, collimator pieces from isotopically enriched ⁶Li carbonate can optionally be used, offering radiationless neutron absorption and somewhat reduced neutron scattering. Towards the detector, the outer part of the collimator is made from antimony free lead to absorb the 478 keV gamma-rays from neutron capture in boron. On all other sides, the collimator is surrounded by at least 25 cm of boron loaded paraffin.

First measurements showed a significant background from neutrons scattered in the air along their flightpath through the detector. For the future it is planned to install an evacuated neutron flight tube with thin steel walls and windows from ~2.5 mg/cm² KAPTON foil.

Fig. 11 shows the supporting honeycomb structure for the detector modules fixed in the octagonal stands. The overall dimensions of the ground frame are 3.5 times 2 m. The completed detector opened for mounting of the samples is shown in fig. 13.

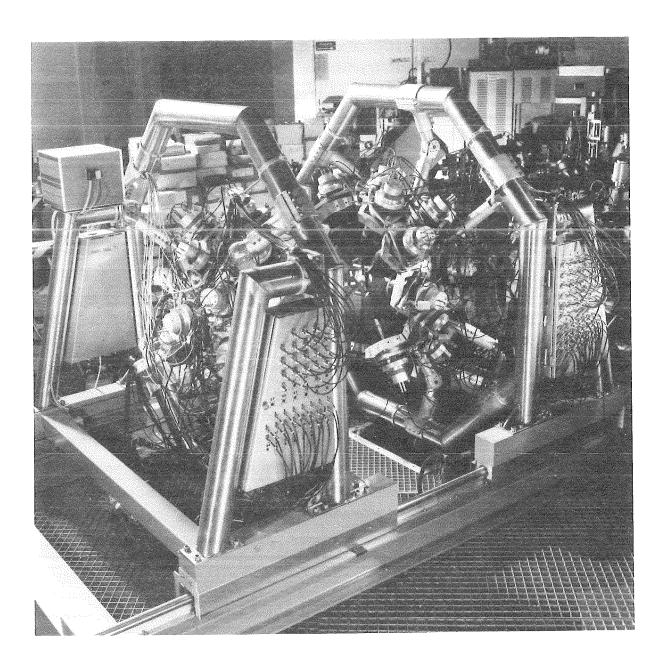


Fig. 13 The completed detector opened for mounting of the samples.

4 THE INDIVIDUAL DETECTOR MODULES

4.1 CRYSTAL HANDLING

The essential features of prototype crystals for the Karlsruhe $4\pi\,\text{BaF}_2$ detector have been published elsewhere [14]. Here, we present more details and describe the modifications that have been made since as well as the properties of all 42 detector modules.

The ultraviolet scintillation light of BaF_2 at wavelengths between 190 and 410 nm is easily absorbed if the crystal surface is contaminated by grease. Therefore, it is strongly recommended to handle crystals with rubber gloves, which are carefully cleaned with ethanol or a compatible solvent. The crystals delivered by the manufacturer (Dr. Karl Korth, Am Jägersberg 9, 23 Kiel 17, Federal Republic of Germany) were reground by hand to remove possible absorbing impurities from the surface using grinding paper of increasing mesh numbers 350, 600, and 800. A significant amount of material was removed in this process using two sheets of the coarse and one sheet of the two fine mesh sizes for each crystal. Grinding was continued until the papers were saturated. The success of this procedure is demonstrated in fig. 14 showing an improvement in energy resolution for the 137Cs line from 11.4 to 10.0%. It has been argued by Anderson et al. [37] that for small BaF2 crystals this improvement is achieved by simply removing adsorbed humidity from the surface, and that the resolution again deteriorates rapidly afterwards. Our experience is different: at least 2/3 of the observed improvement was permanent. As a general rule, we find that only about 0.5% energy resolution are lost during the first week after grinding.

In handling BaF_2 crystals one should keep in mind that fluorides in general are poisonous. In addition, the non negligible solubility of BaF_2 in water may facilitate the intake of the heavy metal barium. As informations about the real risk of ingested or inhalated BaF_2 are widely discrepant, all grinding was carried out in a chemistry laboratory under an exhaust.

4.2 REFLECTOR, PHOTOMULTIPLIER, AND VOLTAGE DIVIDER

Reflector and optical coupling between crystal and photomultiplier are as described in § 3.2 and ref. [14].

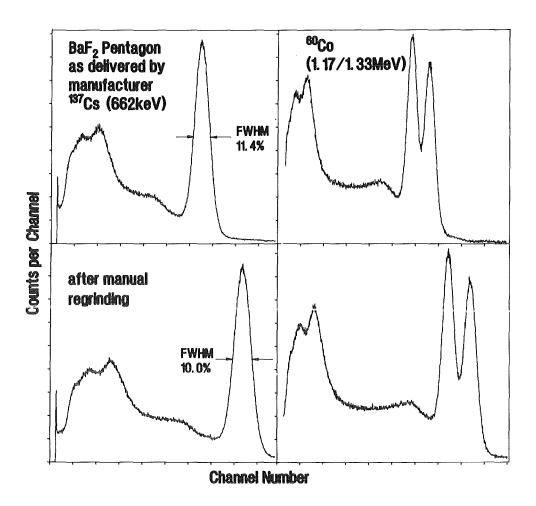


Fig. 14 Gamma-ray spectra from 137 Cs and 60 Co sources measured with a new BaF $_2$ crystal before and after manual regrinding.

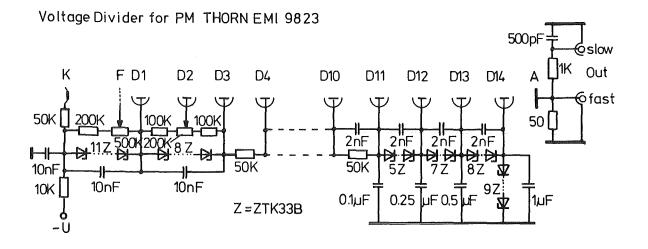


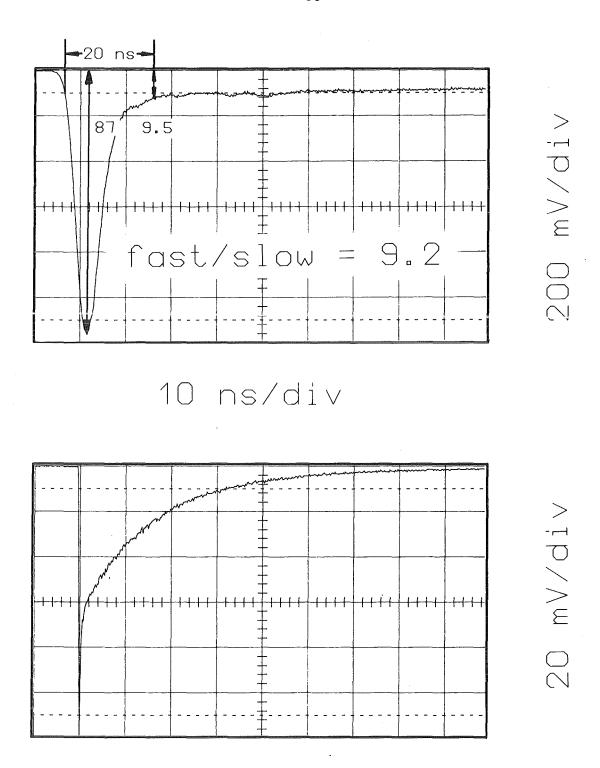
Fig. 15 Optimized voltage divider chain for the EMI 9823 QKA phototube.

To our knowledge, the EMI 9823 QKA is the only available photomultiplier by which good time and energy resolution can be obtained from large BaF_2 crystals simultaneously. Its relevant features are 5 inch diameter, fast rise time, and quartz window. Recently, however, the design of the tube was changed by replacing the conical edges of the quartz window by rectangular ones. These new tubes gave rather poor results with our oversize crystals, probably because the outer, less homogeneous part of the photocathode is more strongly illuminated in the modified version. Even with the outer regions of the cathode covered by inserting a thin ring of aluminum foil with an inner diameter of 12 cm between phototube and crystal, the energy resolution is degraded by at least 1% absolute (e.g. 11 instead of 10% for 137 Cs). Therefore, this new type of photomultipliers was not used in our detector.

For optimum energy and time resolution the voltage divider shown in fig. 15 was carefully adapted to the photomultiplier. Fast and slow outputs are provided for timing and energy measurements, respectively. The resistor chain is enclosed in an aluminum housing of 350 cm³ and produces about 4 W at 2.3 kV cathode voltage. The potentials of the first and last dynodes are fixed by temperature compensated Zener diodes. As these diodes are available with a maximum voltage of only 33 V, each divider contains about 50 diodes. The potential of the focus electrode and the first dynode are adjustable to optimize signal output. All measurements were made with the slow energy signal adjusted for maximum pulse height. The inductances of the connections between dynodes are neutralized to reduce oscillations and to improve the signal rise time. All parts are on printed circuit and are arranged concentrically around the photomultiplier socket, thus minimizing the connection lengths. The voltage divider exhibits good temperature stability and resolution over long periods of time. The final design shown in fig. 15 was slightly modified compared to the version given in ref. [14] to obtain sufficient linearity for the fast component as well (see § 4.5); this improvement resulted in a reduction of the energy resolution, which amounts to \sim 0.4% absolute for the 662 keV line of 137 Cs.

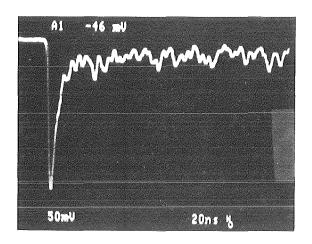
4.3 PULSE SHAPE

The pulse shape of the fast signals from a detector module is shown in figs. 16,17. Figure 16 has been recorded with a ¹³⁷Cs source using a fast digital oscilloscope (LeCroy model 4300) with pulse weighting option. As a criterion for the crystal



500 ns/div

Fig. 16 Signal shape from a detector module for 662 keV gamma-rays from a ¹³⁷Cs source recorded by a digital oscilloscope with pulse averaging option.



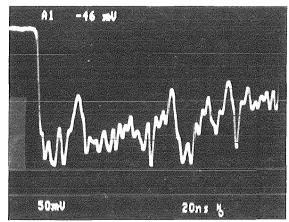
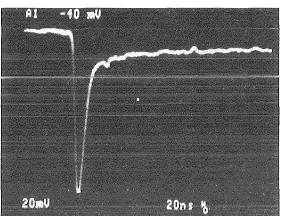


Fig. 17 Signals from a 11 BaF₂ crystal from various sources recorded by a fast oscilloscope with channel plate amplification. The two upper pictures were taken at equal gain (662 keV gamma-rays (upper left), 7.7 MeV α -particles (upper right), cosmic μ -mesons (lower)).



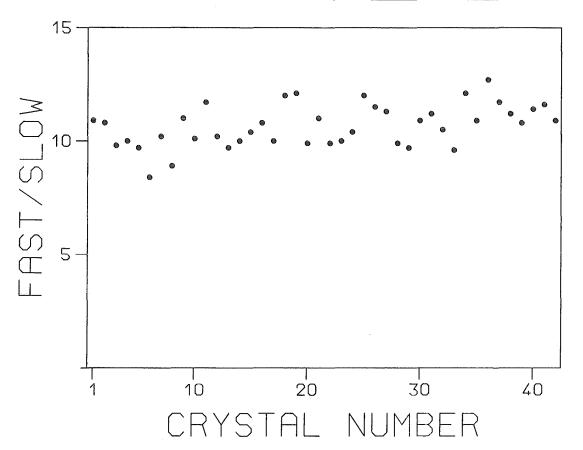


Fig. 18 The fast/slow ratio as defined in fig. 16 plotted for the 42 detector modules

quality a fast/slow ratio is defined by comparing the pulse height maximum with the respective value 20ns after the pulse has passed a threshold corresponding to the height of the slow component as indicated in fig. 16. This ratio was found to range between 8.4 and 12.0 for the 42 crystals of the 4π detector (fig. 18). The lower part of fig. 16 shows that the 600 ns decay time of the slow component requires an integration time of $\geq 3~\mu s$ for accurate energy determination.

Fig. 17 presents single pulses photographed from the screen of a fast oscilloscope with micro channel plate amplification (Tektronix model 2467) for 662 keV gamma rays, 7.7 MeV alpha particles, and cosmic μ -mesons deposing 7 MeV/cm in the crystal [38]. Note the absence of a fast component in the scintillation light induced by alpha particles. As the upper pictures were taken at equal bias voltage, the significant quenching of the alpha induced signals relative to those from gamma-rays can directly be estimated.

4.4 ENERGY AND TIME RESOLUTION

The energy resolution of all crystals was determined in a reference measurement using always the same photomultiplier and voltage divider. In a second series of measurements, the assembled detector modules were tested with the new voltage divider before mounting in the 4π detector. Fig. 19 shows the pulse height spectra from the best detector module for three gamma-ray energies. The measured energy resolution as a function of gamma-ray energy is given in the inset, indicating a clear correlation with photon statistics up to 6 MeV [14]. For all crystals, fig. 20 presents the energy resolution at 662 keV measured in the optimized reference setup and after assembling of the detector modules, the differences being mainly due to the quality of the photomultipliers, and the 0.4% degradation caused by the new voltage divider (§ 4.2). Recently, the energy resolution was remeasured after the modules were assembled for 1.5 to 2 y; only the eight crystals with the highest radium content had been exchanged 3 months before. Within the experimental accuracy, no changes in energy resolution were observed.

As a caveat it should be noted that the energy resolution of BaF_2 crystals is temperature dependent [15]. Therefore, values for the energy resolution should always be given together with the respective temperature. All measurements quoted in this work have been made between 20 and $25\,^{0}C$.

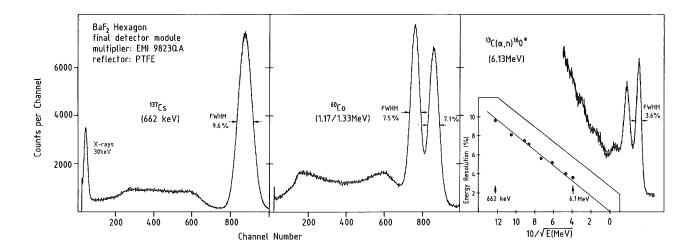


Fig. 19 The energy resolution of one detector module for gamma-rays in the range from 0.6 to 6.1 MeV.

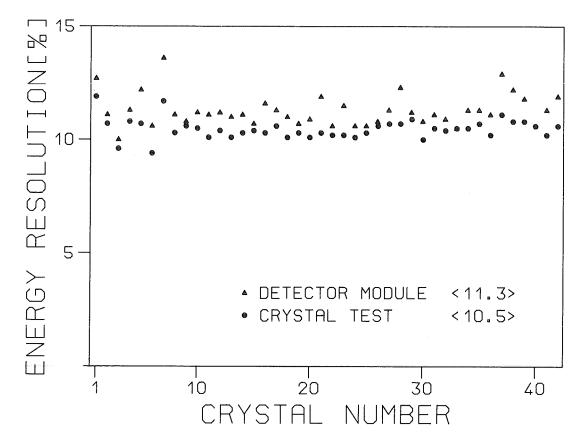


Fig. 20 Energy resolution measured for the 662 keV gamma-rays from a ¹³⁷Cs source during crystal testing and for the final detector modules. The difference is mainly due to the scatter of the photomultiplier quality.

The spectrum of fig. 21 shows the experimental time resolution relative to a fast plastic scintillator [14]. The results for 41 detector modules (fig. 22) have been determined from the completed 4π detector using one module as a start and all other modules as stop detectors. Both, start and stop detectors are connected to the electronics via 50 m long cables (see § 5); home made CAMAC controlled constant fraction discriminators (CFD) were used for the time signals. The so obtained results are slightly worse compared to the laboratory setup used for fig. 21 [14]. The values in fig. 22 represent the combined time resolutions of start and stop detectors, adjusted to the same threshold energy. All observed time peaks are symmetric as in fig. 21; hence, the full width at tenth of the maximum is also \sim 2 times larger than the FWHM.

4.5 LINEARITY

During the neutron capture experiments, a fast decision on the sum energy of an event is made by setting a threshold on a signal obtained by adding only the fast components of the scintillation light from all 42 modules (§ 5.2). This procedure requires a good linearity of the fast component at least up to energies of about 6 MeV. As described in § 4.2, the corresponding change of the voltage divider resulted in a slightly reduced energy resolution. In fig. 23 the energy calibrations for the fast and slow component are plotted for a typical bias voltage. At 6.1 MeV gamma-ray energy, the deviations from linearity are 2.6 and 7% for slow and fast component, respectively.

4.6 BACKGROUND

The only essential drawback of BaF_2 crystals is the background caused by radium impurities, which are always present as radium and barium are homologuous elements. The contributions from the decay chains of ^{226}Ra and ^{228}Ra are indicated in the spectrum of fig. 24, which was taken with a test crystal cooled to $-30\,^{0}C$. At present, the ^{228}Ra contribution is ~ 4 times smaller than that of ^{226}Ra and decreases due to the short ^{228}Ra half-life of 5.8 y. The spectrum is dominated by the four alpha lines from the decay chain of ^{226}Ra . In the present application, however, these lines can easily be discriminated; according to fig. 17, a gamma-ray threshold of $\sim 700\,\text{keV}$ is sufficient to eliminate them completely, and in actual experiments a threshold of

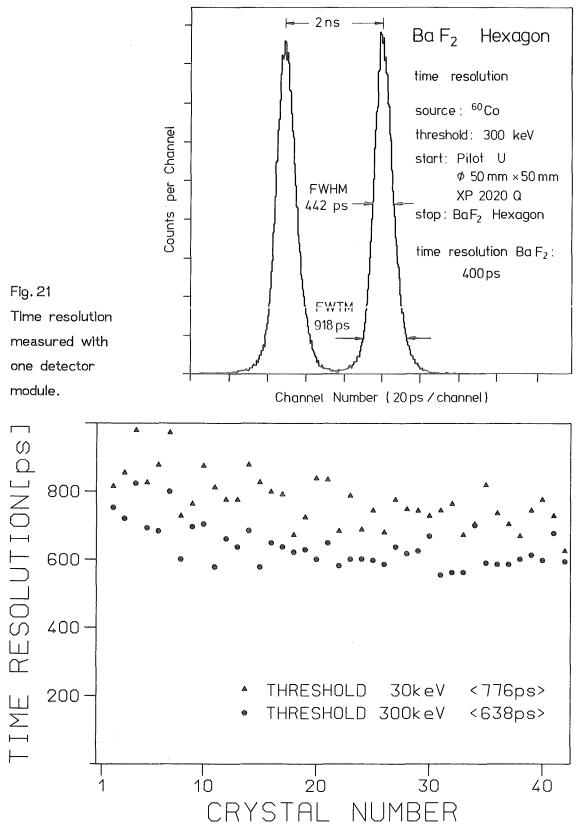


Fig. 22 Time resolution measured in a coincidence experiment with a ⁶⁰Co source using one fixed detector module as start detector and successively all other 41 detector modules as stop detectors. The quoted numbers represent the combined time resolution of start and stop detectors.

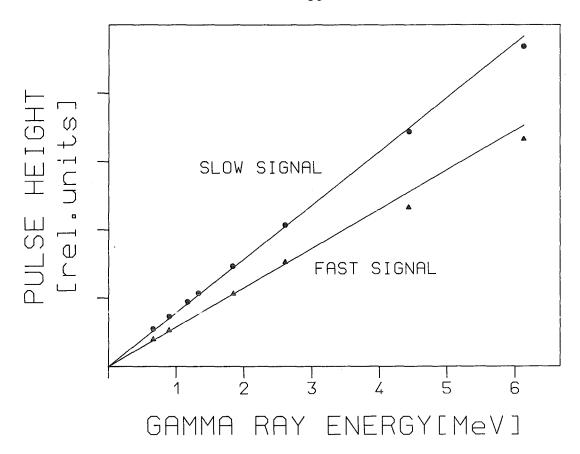


Fig. 23 Pulse heights of the fast and slow component in the scintillation light as a function of gamma-ray energy.

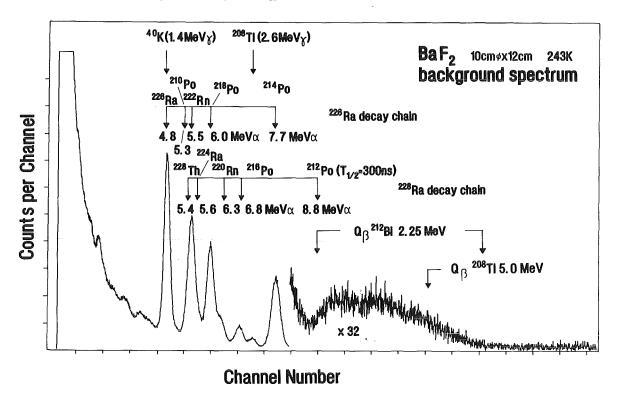


Fig. 24 Background spectrum measured with a cooled test crystal.

2.5 MeV will be used in the fast sum energy signal (§ 5.2). More disturbing is the background due to beta decay, giving rise to electrons and coincident gamma-rays (fig. 25). The decay chain of ²²⁶Ra yields a contribution with a maximum energy of 3.2 MeV, while two components with a maximum energy of 5 and 5.6 MeV are related to the decay chain of ²²⁸Ra. In the latter case, the decay of ²⁰⁸Tl produces electrons and gamma-rays in prompt coincidence, whereas the decay of ²¹²Bl occurs as a delayed coincidence between an electron and an alpha particle from ²¹²Po. Consequently, the second background contribution can also be eliminated by a 2.5 MeV threshold on the fast sum energy, since the alpha induced signal is delayed in time and does not exhibit a fast component.

For characterizing the radium background, the integral count rate of the four strong alpha lines is plotted in fig. 26 for each crystal. The crystals are numbered according to their production date. After this problem was recognized by the manufacturer, the background rate could be reduced to $\sim 200 \text{ s}^{-1}$ per crystal (7.2 kg BaF₂).

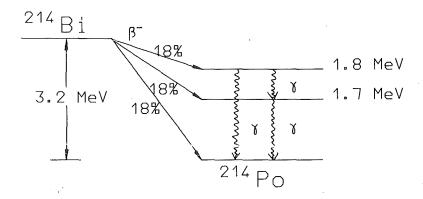
In table 4, intrinsic and external background rates are compared for different threshold energies. For crystals with low radium content one finds that the countrate above 1 MeV is already dominated by room background. The values of table 4 were determined with the modules mounted in the completed 4π detector, and are representative for the experimental environment (including self-shielding of the modules by themselves against the room background from 2 m thick concrete walls).

4.7 LONG TERM STABILITY

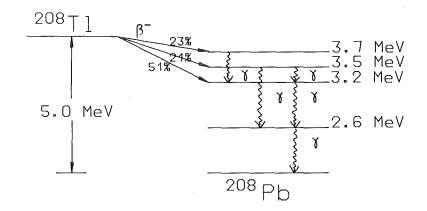
The long term stability of the detector modules was followed over 2.5 y. The energy resolution of a module that was recently removed from the 4π detector was found almost unchanged since it was assembled 1.5 y ago (10.7 instead of 10.3%). However, in the same time the fast component decreased by 20%. After the phototube was disassembled, cleaned, and remounted, the original performance could be completely restored. Obviously, the UV transmission of the optical coupling between crystal and photomultiplier decreases with time so that it may be necessary to replace the silicon oil after several years of operation.

HIGH ENERGY BACKGROUND REACTIONS

From decay of $^{226}\,\mathrm{Ra}$



From decay of ²²⁸Ra



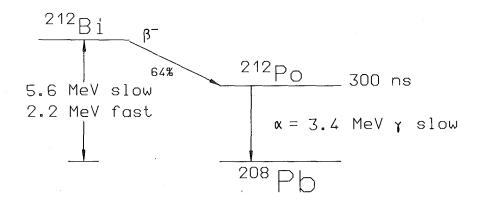


Fig. 25 The radium decay channels giving rise to energetic background.

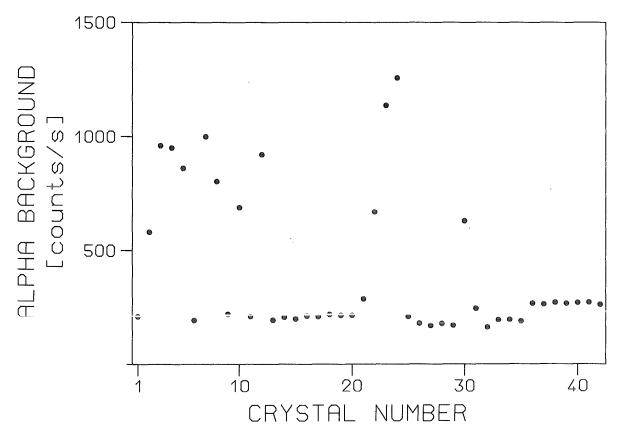


Fig. 26 Background countrate of the 42 crystals integrated over the four prominent alpha lines, and including the contribution from ⁴⁰K.

Table 4. Background countrates of crystals with high and low radium impurities.

amma-ray	Room background gamma-rays (counts/s)		Radium impurities	
threshold			α-particles β+γ (counts/s) (counts/s	
(keV)				
50	low	256	200	324
	high	256	1000	1620
1000	low	74	0	56
	high	74	0	280
2000	low	29	0	23
	high	29	0	110

5 DETECTOR ELECTRONICS

5.1 GENERAL ASPECTS

In the first stage of development the 4π detector is used as a calorimeter. For each accepted event the sum energy and the time of flight is stored together with the gamma-ray multiplicity. The multiplicity is determined by recording a 42 bit pattern indicating those detector modules that have fired. This three-dimensional information ExTOF x MULT is sufficient for the determination of neutron capture cross sections.

In a second stage a multi ADC/TDC system will be installed for recording pulse height and time of flight separately for each detector module. This will improve the gamma-ray energy resolution by eliminating small differences in the response of the individual modules, and will yield additional information on capture gamma-ray spectra and angular distributions.

As typical measuring periods of ~ 2 weeks per sample are expected, a reliable and stable long term operation of the complex 4π detector is required. At present, about 50% of the electronics is used for this purpose. All relevant signals are doubled by fan-out units. Via multiplexers with 42 inputs and one output these signals can be displayed on oscilloscope, or can be used for determination of count rates and for automatic stabilization and adjustment procedures.

As, at present, the signals of the individual modules are added on-line for deriving the sum energy, it is important to maintain equal response for all modules, because later corrections are impossible. Therefore, gain shifts and day-night differences due to temperature changes have to be compensated. The required long term stability of the 42 modules is achieved via the outstanding 7.7 MeV alpha line in the background spectrum (fig. 24) which is used as an internal calibration standard.

Most of the electronics consist of commercial NIM and CAMAC units. The CAMAC discriminators and multiplexers have been copied from the Heidelberg Crystal Ball project. A CAMAC controlled linear gate, a programmable 16db attenuator, a fast 42-fold OR unit, as well as fast and slow preamplifiers for driving the relatively long cables between detector and electronics have been specifically developed for the

present setup. A NOVA4 computer serves for adjustment, control, and permanent stabilization of the 4π detector, and a Data General MV4000 computer is used for data acquisition.

The electronics used with the 4π detector is described in the following subsections, separated according to the aspects of signal processing, detector control, and data acquisition.

5.2 SIGNAL PROCESSING

The electronics for signal processing is illustrated in the block diagram of fig. 27. From the voltage divider of each detector module a fast and a slow signal with a 500 ns time constant are derived. The slow signal is amplified by a factor of 2.5 using a cable driver circuit as shown in fig. 28. The amplifier is separated from the voltage divider by a 10 cm long cable in order to reduce the thermal load of the voltage divider. The signal amplitudes obtained with the 662 keV gamma-rays from a 137Cs source are adjusted to 200 and 600 mV for slow and fast pulses, respectively. The detector in the strongly shielded experimental area is connected with the subsequent electronics by ~50 m long cables. On this way, fast signals loose ~20 % in amplitude though cables with low damping (RG 213) are used, whereas slow signals (RG 58 cables) remain practically unchanged.

At present, fast and slow signals are not completely decoupled; this leads to an increase in the noise level of the slow signal from 2 to about 15 mV, changing the resolution for the 662 keV gamma line of 137 Cs from 10 to $\sim 12\%$. This problem will be solved in the near future by a 1:1 cable driver for the fast signal.

The fast signals pass a CAMAC delay unit (SEN FE292C; 64 steps of 250 ps), by which differences in cable length and electronic transit times are compensated in order to obtain a well defined timing signal for the TOF measurement. The following CAMAC attenuator (16 steps from 0 to 15 db) adapts the pulse height to the input requirements of the following units, and adjusts the fast component of the signals to equal amplitude for all detector modules. By this attenuator, any variations of the fast component with time (see § 4.7) can be compensated.

ELECTRONICS FOR SIGNAL PROCESSING

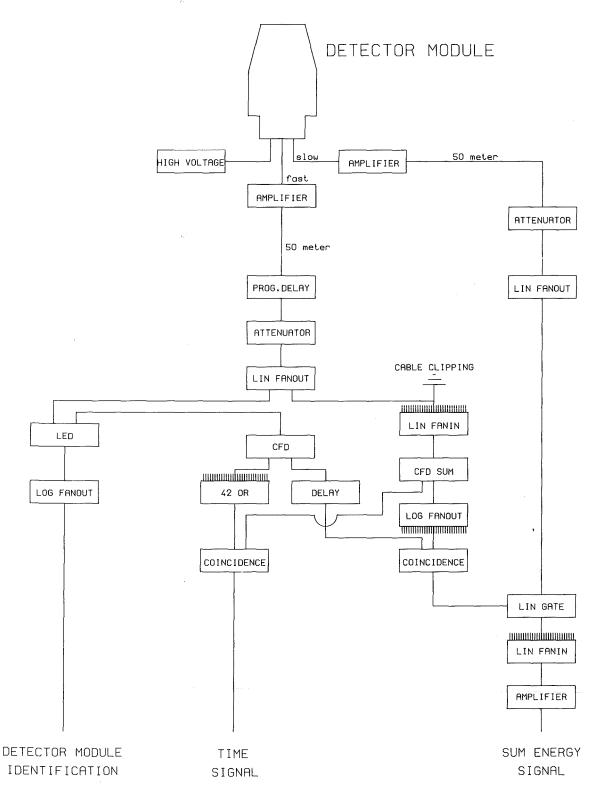


Fig. 27 Electronics for signal processing (modules with 42 inputs or outputs are marked accordingly).

The input of the following fan-out (LeCroy 429A) being limited to -2 V means that fast signals up to 6 MeV gamma-ray energy can be processed linearly in the fast branch of the electronics using attenuation factors of typically 10 db. The respective output signals are used to feed various branches:

(i) In the first branch, the signals are clipped by 2 m long delay cables to remove the slow component. The outputs of all 42 detector modules are then added (LeCroy 429A) to obtain a fast sum energy signal of only 10 ns width, which still yields an energy resolution of ~20% at 1 MeV gamma energy. Only if this fast sum energy signal exeeds a certain threshold, the correlated event might be due to neutron capture and is processed further. In this way, background from low energy gamma-rays, alpha particles, and part of the background from beta decay of radium impurities (§ 4.6) is eliminated. In principle, this threshold should be kept as low as possible because the pulse height distribution of capture events reaches down to the 2 to 3 MeV range (§ 8). In practice, the accepted event rate is limited by the capacity of the magnetic tapes; this implies a threshold of ~2.5 MeV.

(ii) Another output is fed through the bridged input of a leading edge discriminator (LED) to a constant fraction discriminator (CFD), which creates the logic time signals for the TOF measurement; simultaneously, it is used (in coincidence with the main trigger signal) to open the linear gates for the slow energy signals. To avoid multiple triggering from the slow component of the scintillation light a dead time up to $3\,\mu s$ can be selected. This can be tolerated in the present application where the integral countrates of the detector modules are well below $5\,kHz$. It is possible to block the output via CAMAC command, a feature that is important for adjusting the 4π detector (§ 6.2). The logic time signals of all detector modules are combined in a home made 42-fold OR to derive the final start signal for the time to amplitude converter (TAC). The OR unit is designed in SMD technique; it yields an output signal almost independent of the multiplicity pattern at the input (jitter less than 200 ps; see § 7.3). The stop signals for the TAC (Ortec 457) are derived from the accelerator pulses by a pickup electrode.

(iii) in a third branch of the fast signal, a 42 bit pattern is produced for the identification of those detector modules that have fired. The output signals of the LEDs are sent to a home made channel identifier, which adds the digitized information on the

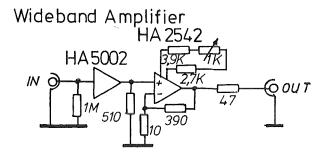


Fig. 28 Wideband amplifier for the slow energy signals.

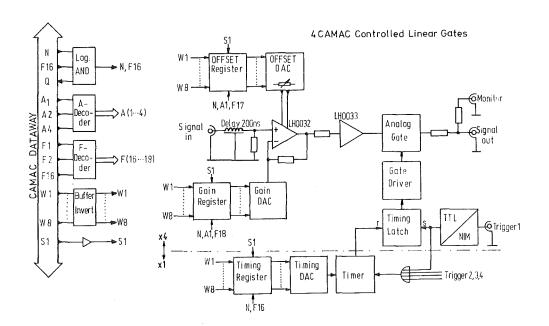


Fig. 29 Schematic diagram of the CAMAC controlled linear gates.

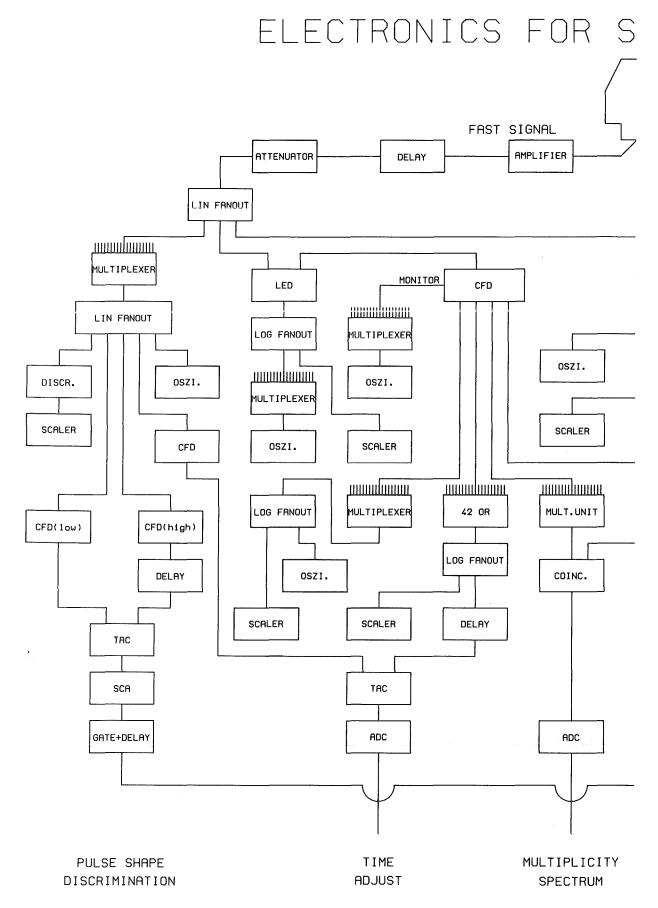
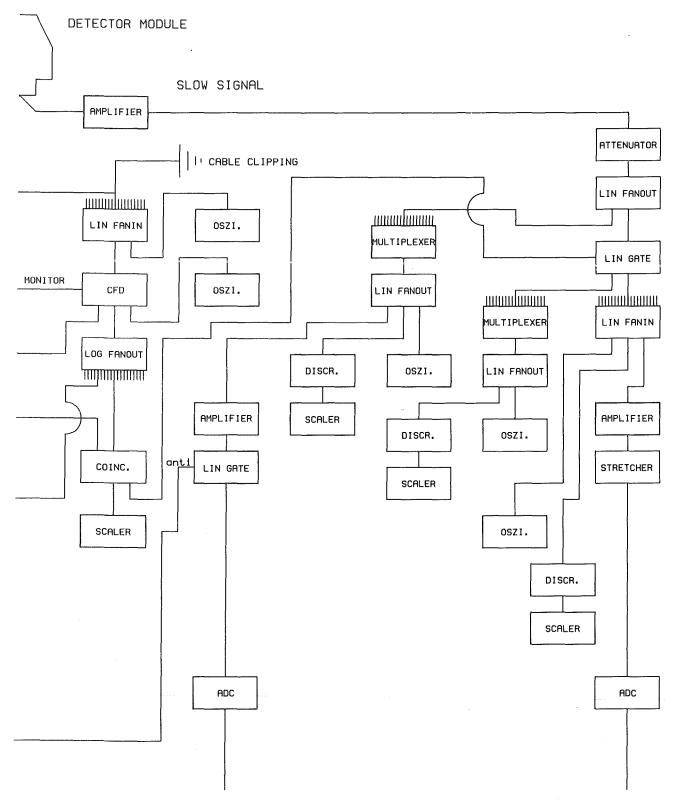


Fig. 30 Electronics for detector control (modules with 42 inputs or outputs are marked

URVEY OF OPERATION



ALPHA SPECTRUM
FOR DETECTOR STABILIZATION

ENERGY SPECTRUM FOR GATE ADJUST

accordingly).

contributing modules to the bit pattern from pulse height and TOF analysis for final storage in the data acquisition computer. Note, that the use of separate discriminators allows to set different thresholds for the sum energy and the multiplicity pattern.

Processing of the slow signals is rather straightforward as indicated in fig. 27; after passing a fixed attenuator (6 db) they are multiplied in a linear fan-out (LeCroy 429A). The adjustments are such that gamma-ray signals up to 12 MeV can be accepted without saturation effects.

The following linear gates are home made CAMAC units (see fig. 29 for a schematic wiring diagram); apart from the possibility to select the gate width between 0.5 and 5 μ s, these units allow to change the input pulse height by $\pm 20\%$ and the offset by ± 10 mV via CAMAC commands. In this way, gain and offset of each detector module can be adjusted independently, without changing the bias voltage and thus the pulse height of the fast signal. This is an important feature as the fast/slow ratio can be different for different crystals (fig.18), and may also change with time (§ 4.7).

The output pulses of the 42 linear gates are added by means of linear fan-in modules (LeCroy 429A) to a sum signal with good energy resolution that is sent to an ADC for final data acquisition. The use of linear gates ensures that only those modules contribute to the final sum signal that have fired in the particular event, thus minimizing the effect of multiplier noise in the summation.

5.3 CONTROL ELECTRONICS

The large fan-out capacity together with a set of six multiplexer units allows to observe all important branches in the electronics on oscilloscope or to handle the respective pulses in further electronics. By means of the home made CAMAC multiplexers any one of the 42 input signals can be selected to appear on output by means of micro relais. As indicated in fig. 30, the following signals are accessible in this way: slow, fast, CFD output, CFD monitor output, LED output, and GATE output.

Two sets of 42 CAMAC scalers (LeCroy 2551) are used for continuous control of the output rate of coincidences and LED discriminators. Four additional scalers are used to monitor the multiplexer outputs; this allows to record the respective count

rates of all 42 detector modules by a computer routine. Two other scalers serve for counting the integral rate of the 42-fold OR and of the CFD in the fast sum signal (fig.30). Other aspects will be discussed in §6.

With these features, the operation of the 4π detector can be surveyed without disturbing data acquisition, even without removing a single cable connection.

5.4 ELECTRONICS FOR DATA ACQUISITION

The electronics for data acquisition is shown in fig. 31. Only events from an appropriate time window between successive accelerator pulses are accepted in the TOF measurement, and a common dead time for TOF and energy branch is introduced after each valid event. This is achieved by means of two gate generators in combination with two updating discriminators and suited delays. The output of the second updating discriminator is also used to ensure that an event is only recorded if both, TOF and sum energy signals are available, and to start the transfer of the 42 bit pattern for identification of the contributing detector modules.

The 64 bit word containing sum energy, TOF, and detector multiplicity is stored in list mode on magnetic tape. Simultaneously, two-dimensional spectra without multiplicity information are accumulated in a megastore in 128 energy times 2048 TOF channels. In addition, up to four single spectra for monitoring the neutron flux or the pulse width of the accelerator are recorded as well. Up to 8 samples are cycled into the neutron beam in intervals (typically 10 min), which are defined by integrating the proton beam current to a preselected charge. During each sample change, the two-dimensional spectrum is added to a respective sum file on magnetic disk. In this way, the accumulated sum spectra of all samples can be followed directly throughout the experiment.

Data acquisition is performed by a 32 bit multi-user computer (Data General MV4000) with 8 Mbyte memory, 760 Mbyte disk, and two high density tapes. A 1 Mbyte megastore and an increment unit with 3 independent 32 bit input channels selectable for list and increment mode is used for data input.

ELECTRONICS FOR DATA ACQUISITION

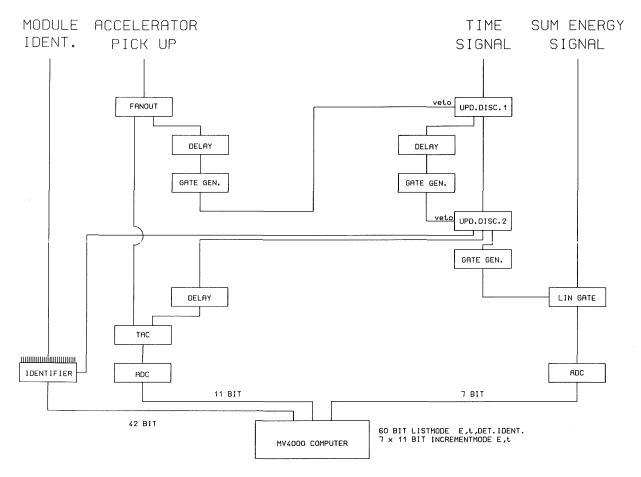


Fig. 31 Electronics for data acquisition.

6. SETTING, CONTROL, AND STABILIZATION OF THE 4π DETECTOR

6.1 SETTING OF INDIVIDUAL PARAMETERS

The detector electronics is controlled by a separate computer (Data General NOVA 4 with 1 Mbyte memory, 73 Mbyte disk, 1600 bpi magnetic tape, and an increment unit for acquisition of single spectra into 32 K of memory) via CAMAC branch driver. The main input-output device is a touch panel display (Kinetic systems). A Silent terminal with paper output is available for documentation. For each detector module a set of 256 parameters is stored on disk; an additional set contains the global parameters of the setup. For all relevant settings, i.e. bias voltage, delay, discriminator thresholds, gain, offset, and gate width, the actual value, a standard value as well as upper and lower limits can be stored simultaneously. This allows to exclude unphysical settings and offers an easy recall of old settings after unsuccessful readjustments. All inputs for individual detector modules are made via touch panel display. There are also routines to set one parameter for all 42 detector modules at a time; this is convenient for fast readjustments of the detector after a power failure or when CAMAC crates have to be modified. Fast changes in the parameter sets can also be made by special editing features.

6.2 AUTOMATIC ADJUSTMENT AND GAIN STABILIZATION

The time consuming energy calibration of the individual detector modules and the adjustments for optimum time resolution are performed by automatic routines.

(i) Adjustment of gain and offset of the linear gates: For obtaining a sum signal with good energy resolution it is important that all detector modules are calibrated to equal values for gain and offset. For this purpose, the sum energy spectrum is measured with a mixed gamma-ray source containing 60Co and 137Cs according to fig. 30. If all but one of the CFDs are blocked by CAMAC commands, the observed "sum" spectrum represents only the single spectrum of the unblocked detector module. After a preselected number of counts are accumulated, the positions of the three prominent gamma-ray lines are roughly obtained by a peaksearch routine, and the exact positions are determined by a gaussian fit of each peak. Fitting the three positions by a straight line according to their energies yields the energy calibration

of the spectrum. By an automatic procedure, gain and offset of the linear gate are changed stepwise until the energy calibration agrees with a preselected standard within specified limits. This procedure can be repeated automatically either for all or for a selected number of detector modules.

(II) Adjustment of the delay for the fast signals: For optimum time resolution, the fast signals have to be adjusted to equal transit times between detector and the 42-fold OR that defines the timing signal for the TOF measurement. This procedure is performed with a ⁶⁰Co source inside the detector. Via multiplexer, the fast signal of a selected reference module is switched to a separate CFD, which yields the start signal for a TAC; the stop signal is provided by the 42-fold OR. Blocking the CFDs of all 42 detector modules except of the reference module means that the TAC is started and stopped by pulses from the same origin; the position of the resulting peak in the time spectrum can be taken as a reference for all other detector modules. By an automatic procedure, each detector module can successively be combined with the reference module by blocking the CFDs of all other detectors. The position of the corresponding time peak is determined by a gaussian fit; it is then shifted to the correct position by an appropriate delay that can be derived from the known time calibration of the TAC.

(iii) Stabilization of the detector: Compensation for long term variations of the photomultiplier gain and for temperature dependent variations of the light output ($\Delta T = 1$ K changes the pulse height by ~2%) requires a stabilization procedure working on the time scale of hours. For this purpose, the alpha lines of the radium impurities are used as internal standards. The fact that signals from alpha particles do not show a fast component can be used for separating them by pulse shape discrimination. The fast and slow signals of a detector module are selected via multiplexer; the slow signal is transfered to a separate ADC, while the fast signal is fed into two CFDs with high and low threshold, respectively. The output of these discriminators are used to start and stop a TAC as shown in fig. 30. The upper threshold corresponds to the pulse height of the fast component for ~600 keV gamma-rays. Gamma-rays with higher energies exceed both thresholds with very short time difference, giving rise to a sharp peak in the observed time spectrum. The pulses from alpha particles either fall below the upper threshold or pass it with a significant time delay compared to gamma-rays. Hence, the sharp peak due to gamma-rays can be selected by a

single-channel-analyser. If the energy spectrum of the detector module is observed in anticolncidence with these gamma-ray signals, an almost background-free alpha particle spectrum is obtained. This is illustrated in fig. 32 showing the spectrum of the mixed 60 Co + 137 Cs source with and without the anticoincidence condition.

From this alpha particle spectrum, the well isolated 7.7 MeV line from the decay of ^{214}Po is used for stabilisation of the 4π detector. Immediately after the settings for gain and offset are found for a particular detector module, the automatic routine described above also records the alpha spectrum for this module, and the position of the 7.7 MeV line is stored. In this way, a definite correlation between the correct gain adjust for the sum energy spectrum and the position of the 7.7 MeV alpha peak is established.

During neutron capture cross section measurements, the alpha spectra of the 42 detector modules are inspected sequentially. If the position of the 7.7 MeV alpha line starts to deviate by more than the shift corresponding to a change of 0.5 V in bias voltage, the setting is changed accordingly. The gain shift as a function of bias voltage has to be determined once by another automatic procedure, and is then stored as a detector parameter. If the determination of the alpha line fails, the change in bias voltage is limited to $\pm 5 \, \text{V}$ in order to avoid dangerous misadjustments. As a 1 V change of the bias voltage modifies the pulse height by approximately 2% (§ 7.4), the energy resolution in the sum spectrum is slightly degraded by this procedure for gain stabilization; smaller voltage steps would require a modification of the respective CAMAC controlled power supplies. Counting times of 5 min are required per detector module to achieve sufficient statistical accuracy for a reliable analysis of the alpha spectra, so that each detector module can be checked every 4 hours.

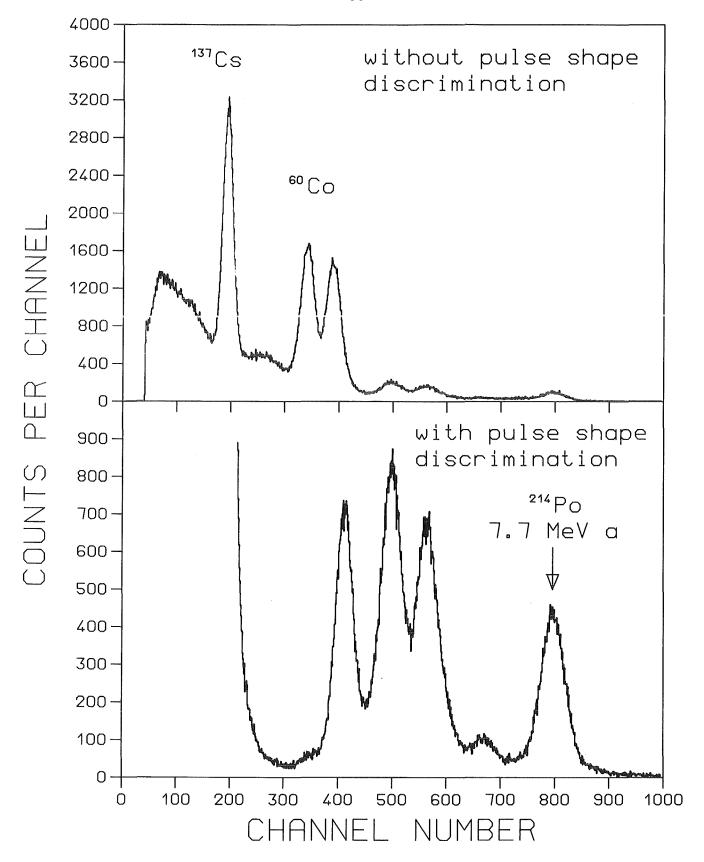


Fig. 32 Spectrum of a mixed ¹³⁷Cs + ⁶⁰Co source used for calibration of the linear gates (top); the same spectrum taken with pulse shape discrimination (bottom) illustrates the perfect separation of alpha particles.

7. PERFORMANCE OF THE 4π DETECTOR

7.1 ENERGY RESOLUTION

The energy resolution obtained in the sum spectra of the 4π detector including 42 detector modules is documented in fig. 33. Gamma-ray sources of 137 Cs, 54 Mn, 65 Zn, 60 Co, and 88 Y as well as the 6.1 MeV gamma-ray line from a (13 C+Pu) source were used in these measurements. The spectra were obtained by summation of the signals from all detector modules as described in § 5.2. The sum energy signal was amplified in a main amplifier (Ortec 572) that was modified by bridging the second differentiation stage and operating with a shaping time of 3 μ s. A pulse stretcher is used to adapt the pulse shape to the ADC (Nuclear Data 582; fixed conversion time 5 μ s).

The energy resolution is plotted in the insert of fig. 33, showing a linear $E^{-1/2}$ dependence with a small deviation at 6.1 MeV. In general, the resolution is worse compared to the mean of the individual detector modules (fig.20), where 11.3, 6, and \sim 5% were obtained at gamma-ray energies of 0.662, 2.5, and 6.1 MeV, respectively. This difference is due to the following reasons:

- (i) In general, the linear gates tend to slightly degrade the energy resolution; this effect is enhanced because about 10% of the integrated slow signals are lost due to the gate width of only $3\,\mu s$ (fig. 16).
- (ii) The gated pulses are affected by the constant noise level of 10 mV due to the incomplete decoupling of fast and slow pulses (§ 5.2). This reduces the resolution for the 137 Cs line by $\sim 2\%$, while it is of minor importance at higher energies.
- (iii) The detector stabilization operates by changing the bias voltage in steps of ± 1 V; this implies a minimum pulse height change of 1.5% on average.
- (iv) The energy resolution at high gamma-ray energies suffers also from nonlinearities in the energy calibration, which can be different for individual detector modules. In general, the nonlinearity increases with increasing voltage, and values between 2100 and 2400 V are necessary for achieving equal pulse heights.
- (v) The high overall detector efficiency results in high count rates even if relatively weak gamma-ray sources are used. Therefore, pile-up effects start to deteriorate the energy resolution.

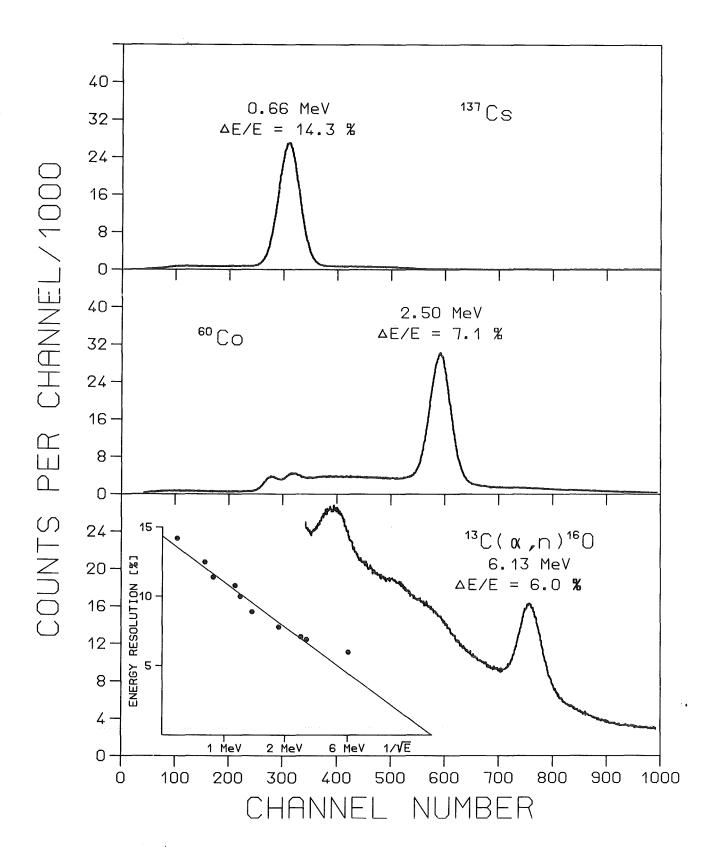


Fig. 33 Energy resolution of the 4π detector in the range from 0.6 to 6.1 MeV (the large background in the lower spectrum is caused by neutrons from the (α,n) reaction).

Further improvements of the energy resolution are expected by decoupling fast and slow signals with additional amplifiers, and by introducing an ADC system for individual pulse height analysis of all detector modules. It is also planned to improve the stability by tuning the gain of the linear gates instead of the bias voltage. A significantly better resolution could finally be achieved by cooling the entire detector to temperatures around $5\,^{\circ}$ C.

7.2 DETECTOR EFFICIENCY

As all capture cross sections are measured relative to the standard gold cross section, only cross section ratios have to be determined experimentally. Therefore, the absolute detector efficiency is not required with high precision. An absolute calibration of the efficiency were possible, e.g. by observing the gamma-ray lines of very weak sources in coincidence with a well calibrated Ge detector. With the present setup, this would be complicated as long as a single ADC is used for analysing all events from the 4π detector. As low thresholds have to be used for the sum energy, alpha particles cannot not be discriminated, leading to a background rate of about $20 \, \text{kHz}$.

Sufficiently precise information on the absolute efficiency could be obtained by means of calibrated gamma-ray sources. The spectra shown in fig. 34 were measured with 65 Zn and 88 Y sources of about 4 kBq, and with a 60 Co source of 37 kBq, all located in the centre of the 4π detector. Starting with the 60 Co spectrum, one finds significant pile-up due to the higher activity. Assuming that all events above the sum energy peak at 2.50 MeV are due to pile-up of full energy signals, a 68 % probability for detecting the sum energy of the 60 Co cascade is achieved. This corresponds to a peak efficiency of about 82 % for 1.25 MeV photons (which is the mean of the two 60 Co energies). The full energy peaks of the individual gamma-rays are observed with an intensity of 1.8 %, corresponding to a probability of 2% for detecting only one of the transitions. Hence, there is a 2% probability for photons of 1.17 and 1.33 MeV for leaving the detector without interaction. Assuming the same escape probability for the 65 Zn source, the upper spectrum of fig. 34 yields a peak efficiency of 89%. In the same way, a peak efficiency of 93% was obtained for 0.66 and 0.83 MeV gamma-rays via 137 Cs and 54 Mn sources.

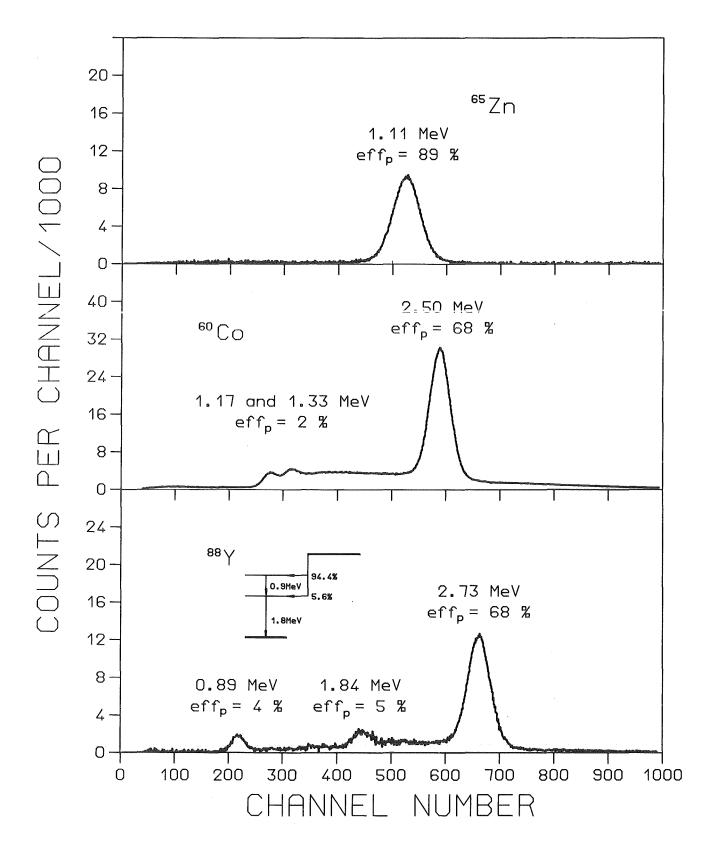


Fig. 34 Pulse height spectra of various gamma-ray sources taken with the 4π detector for determination of the efficiency (the spectra were measured with 42 detector tor modules covering the full solid angle of 4π).

The sum energy peak in the ⁸⁸Y spectrum has an intensity of 68 %, corresponding to a 74% peak efficiency for 1.84 MeV photons. According to the decay scheme indicated in the insert of fig. 34 [39], 5.6% of all ⁸⁸Y decays feed the level at 1.84 MeV. The related gamma-rays being not part of a cascade means that they are expected to contribute 4.1% to the 1.84 MeV peak in the spectrum. The observed intensity of 5% then implies an escape probability of 1% for the 0.89 MeV photons in the cascade. Finally, the observed 4% intensity of the 0.89 MeV peak yields directly a 4% escape probability for the 1.8 MeV photons.

These results are plotted in fig. 35 together with the calculated efficiency values from the design studies (§ 2.3). The peak efficiency was calculated [32] with an optimistic and a pessimistic assumption for treating triple compton scattering events (open circles and triangles in fig. 35). The present results fall between these extremes, but are closer to the optimistic case. The escape probabilities are plotted in the lower part of the figure.

More detailed investigations of the absolute efficiency and the line shape for mono-energetic gamma-rays are planned with a germanium detector for coincidence measurements and using gamma-ray cascades from (p,γ) reactions, which cover a larger energy range.

7.3 TIME RESOLUTION

The time resolution of the detector has been measured with a ⁶⁰Co source as described in § 6.2 using two different versions of the 42-fold OR. Our first design gave optimal results for two-fold coincidences, but events of higher multiplicity appeared to be systematically shifted in time. As the event multiplicity is recorded as well, this constant shift could later be corrected off-line. In practice, however, it is more convenient to avoid this shift, which was practically eliminated in a second version of the 42-fold OR.

The measured time spectrum is shown in fig. 36, and the measured time resolution is plotted in fig. 37 as a function of the gamma-ray threshold. An optimum resolution of about 650 ps is obtained for threshold energies above 300 keV (fig. 37). The 650 ps represent the total time resolution of the experiment. If the time resolution of

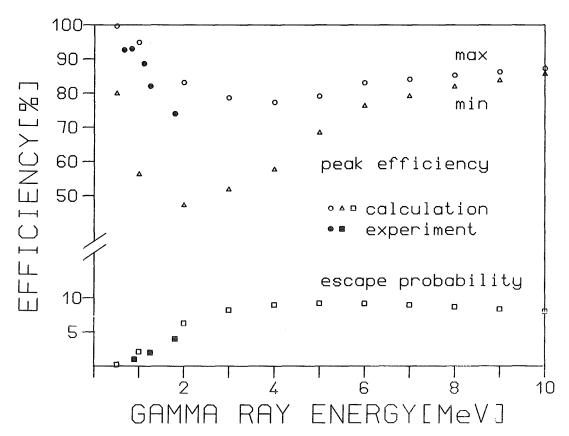


Fig. 35 Measured peak efficiencies and escape probabilities of the 4π detector compared to the calculations of ref.[32]; for details see text.

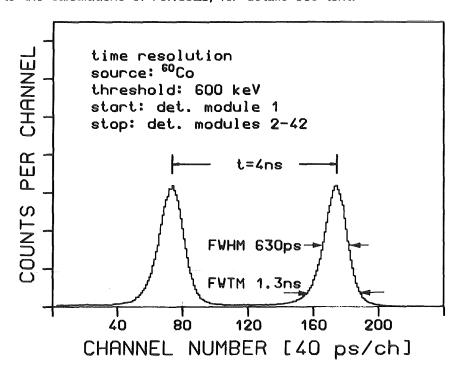


Fig. 36 Optimum time resolution of the 4π detector for two-fold coincidences measured with a 60 Co source (start: detector module 1, stop: detector modules 2-42 combined via 42-fold OR).

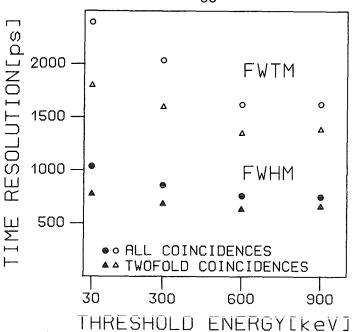


Fig. 37 Time resolution of the 4π detector for two-fold coincidences as well as for all possible multiplicities measured with a 60 Co source for different threshold energies in the same way as in fig. 36.

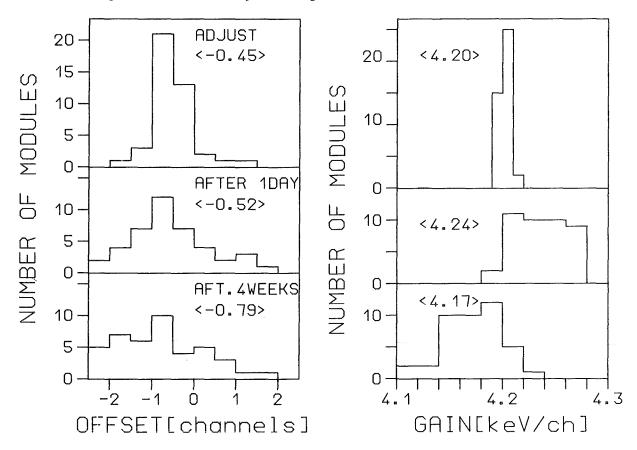


Fig. 38 Offset and gain of the linear gates immediately after adjustment, after a stabilization period of 1 day, and after a measuring period of 1 month; during that time the detector was stabilized via the 7.7 MeV alpha line from radium decay.

the start detector is unfolded, one obtains an overall time resolution of less than 500 ps for the remaining 41 detector modules, an impressive result in view of the 60 I BaF_2 volume.

The results presented in this section demonstrate the attractive features of BaF_2 for gamma-ray detection. For the first time, a 4π detector could be built that combines 7% energy resolution at 2.5 MeV, 500 ps time resolution, and nearly 100% efficiency for gamma-rays up to 10 MeV.

7.4 STABILITY

The stability of the detector settings is demonstrated in fig. 38 showing offset and gain of the 42 detector modules immediately after adjustment, after a stabilization time of 1 day, and after a measuring period of 1 month. During this time, the detector was stabilized by changing the bias voltage as to maintain the position of the 7.7 MeV alpha line (§ 6.2). The gain changes during the first day are due to the fact that the bias voltage can only be changed in steps of \pm 1 V. The additional spread during the four weeks of experiment caused only a small reduction in energy resolution (e.g. from 7.3 to 7.8% for the 2.50 MeV 60 Co sum peak), which can easily be tolerated.

Table 5. Energy range of continuous neutron spectra produced via the $^7\text{Li}(p,n)^7\text{Be}$ reaction as a function of proton energy above the reaction threshold at $E_p = 1881 \text{ keV}$, and related informations.

Proton energy above threshold [keV]	Range of neutron spectrum [keV]	Opening angle of neutron cone [deg]	Energy range undisturbed by scattered neutrons [keV]
0	31	0	31
1	20 - 40	< 5	31 – 40
10	8-68	30	53 - 68
20	5 - 88	45	69 - 88
30	5 - 105	60	82 - 105
60	5 - 150	4π	117 - 150
100	5 - 210	4π	164 - 210

8. REGISTRATION OF NEUTRON CAPTURE EVENTS

8.1 NEUTRON SOURCE

The setup for the determination of neutron capture cross sections is briefly described in § 2.1, and a schematic view is given in fig. 2. Neutrons are produced via the $^7\text{Li}(p,n)^7\text{Be}$ reaction, which indeed is well suited for s-process studies. At the reaction threshold of E_p = 1.881 MeV almost monoenergetic neutrons are emitted with an energy of 31 keV, corresponding to the velocity of the compound nucleus. In the centre of mass system, neutrons with practically zero energy are emitted isotropically. Consequently, in the laboratory system all neutrons are emitted in a very narrow forward cone. Rising the proton energy above the reaction threshold yields continuous neutron spectra in an increasingly broader energy range around 31 keV (table 5). Simultaneously, the opening angle of the neutron cone increases, reaching 4π when the proton energy exceeds the reaction threshold by 40 keV.

Energies around 30 keV are also characteristic of the neutron spectrum prevailing during the s-process, which occurs in the helium burning zones of red giant stars. Typical temperatures of these regions are between 200 and 300 million K, corresponding to thermal energies around 25 keV. Neutrons are easily thermalized in the stellar plasma, exhibiting a Maxwellian energy distribution ranging from zero to ~200 keV. Capture cross section measurements should cover this entire range; folding with the stellar spectrum then yields the effective stellar cross section [4]. With the ⁷Li(p,n)⁷Be reaction it is possible to produce neutron spectra in exactly that energy range.

As was shown in § 2.3, the additional 10 cm flight path from the sample to the inner radius of the BaF_2 shell always provides a region at the high energy end of the neutron spectrum that is completely undisturbed by background from sample scattered neutrons. For a flightpath of 77 cm (the minimal flight path that can be presently used) this part of the spectrum is given in the last column of table 5. Obviously, it is possible to move this region over the full spectrum range from 30 to 200 keV by repeated runs at different proton energies. In practice, proton energies should be kept 10 keV above threshold as the neutron yield drops rapidly for lower proton energies, and measurements would be too time consuming.

The possibility to taylor the shape of the neutron spectrum in exactly the energy range that is needed for s-process studies (5-200 keV) is a considerable advantage compared to LINAC sources, where most neutrons are produced at lower and higher energies, so that the related backgrounds disturb the energy range of interest. Moreover, the TOF discrimination of sample scattered neutrons is not possible, as primary flight paths of at least 10 m have to be used in LINAC experiments due to the heavy shield around the neutron target. Hence, the combination of favorable background conditions, short flight paths, and the suited time structure available at Van de Graaff accelerators more than compensate for the lower integral neutron yield. This holds in particular if neutron capture cross sections are to be measured with high precision.

The main parameters of the accelerator are compiled in table 6. The repetition rate of 250 kHz is required to avoid overlap of delayed background events with subsequent pulses.

8.2. MEASUREMENTS AND DATA EVALUATION

Data evaluation and the determination of neutron capture cross sections will be discussed in detail in a forthcoming paper on first measurements with the 4π detector. Here, the relevant features will be presented briefly.

For the determination of neutron capture cross sections relative to a standard, at least four "samples" have to be used in the measurements:

- (i) The Isotope under Investigation: As the neutron capture cross section is characteristic for each isotope, isotopically enriched samples have to be used in order to achieve good accuracy.
- (ii) The gold sample: In most cases, the well known neutron capture cross section of gold is used as a standard. However, for some astrophysical problems, it is sufficient to measure the cross section ratio of two neighboring isotopes, e.g. for ¹⁴⁸Sm and ¹⁵⁰Sm.
- (III) The carbon sample: As neutron capture in carbon is negligible, this sample can be used to simulate the effect of sample scattered neutrons.
- (iv) No sample: With an empty sample position, the time independent background due

to the radium impurities in BaF_2 and from natural radioactivity is determined together with the backgrounds caused by the neutron beam and by neutrons escaping from the target shield.

The samples are mounted on a sample changer and cycled automatically into the measuring position by a computer controlled stepping motor. Up to 8 samples are fixed on two 0.1 mm thick steel wires to minimize disturbing materials in the neutron beam. The distance between the samples is not fixed, but values between 5 and 10 cm are most appropriate. During the experiments, the samples are changed in intervals of ~10 min, defined by integration of the proton beam current to a preselected charge.

As a rule of thumb, a sample mass of 1 g is required if the 30 keV cross section is $\sim 500 \, \mathrm{mb}$; this is considerably less than is normally used in comparable TOF measurements. Correspondingly, sample related uncertainties, e.g. neutron multiple scattering and self-shielding or gamma-ray self-absorption are significantly reduced. Further improvements of the 4π detector (§ 9) will probably allow to use about two times smaller samples.

In the measurements, each event is characterized by a 64 bit data word, containing sum energy, flight time and the detector identification, and is stored in list mode on magnetic tape. Simultaneously, a two-dimensional spectrum of 2048 TOF versus 128 pulse height channels is accumulated in a megastore (without multiplicity information), and up to 4 different control spectra are recorded by a separate increment unit. During the sample change, a new file for the list mode data of the next sample is created on the magnetic tape, and the two-dimensional spectrum is added to a sum file that is stored on disk for each sample separately. The control spectra are also stored on disk for later evaluation. In this way, a two-dimensional spectrum is available for each sample that represents the actual status and that can be used for inspection and control of the ongoing experiment.

Sufficient statistical accuracy is achieved within about 1 to 2 weeks of measuring time for a particular proton energy. The definition of the sample changer intervals by integration of the proton beam current may cause a systematic effect if the neutron yield decreases with time. Then, the first sample in the cycle receives a higher

exposure than the last one. This effect can be corrected by means of two control spectra recorded with $^6\mathrm{Li}$ glass neutron detectors:

- (i) The pulse height spectrum of the first ⁶Li glass detector (located at a distance of about 20 cm from the lithium target perpendicular to the beam axis) monitors the total neutron yield.
- (ii) The second 6 Li glass detector (located in the neutron beam behind the 4π detector at a flight path of 2.5 m) is used for taking a TOF spectrum. As this detector is looking at the neutron target through the sample, the recorded spectra have to be corrected for the respective sample transmissions, which are usually larger than 98%. By this spectrum, neutrons in the direct beam can be distinguished from moderated ones.

The two spectra offer a completely independent normalization for the neutron exposure per sample. The respective corrections are typically ~1% and can be determined with an accuracy of better than 0.2%.

For each sample, the list mode data are sorted off-line into two-dimensional spectra according to multiplicity. In general, five spectra per sample containing multiplicities 1 to 4 and ≥5 were found to be sufficient; these spectra differ widely in their signal to background ratios. If necessary, also higher multiplicities can be treated, at the expense of increasing computing time and storage requirements.

The different steps of background subtraction are illustrated in fig. 39. The spectrum on top shows the uncorrected data obtained with a gold sample containing only events with multiplicities larger than two. At low sum energies, the time independent background is mainly due to the radium impurities of the BaF_2 crystals. Capture events in the gold sample are concentrated around 6.5 MeV, while the background due to sample scattered neutrons, which are ultimately captured in barium is mainly located at sum energies of 9 MeV. It is easy to see that the latter component is more strongly spread in time compared to capture events in the gold peak; even after 3 μs this background is still significant. Consequently, accelerator repetition rates of 250 kHz or even lower should be used in actual experiments.

The background from scattered neutrons falls into three components, a constant part due to moderated neutrons escaping from the shield around the target, and two

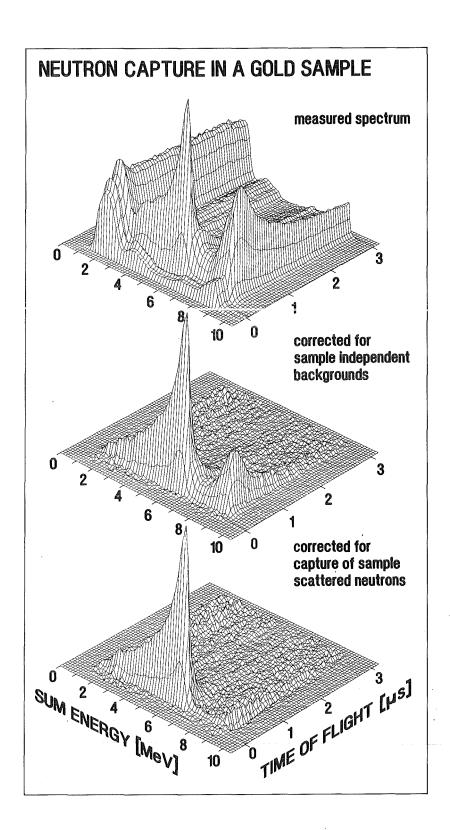


Fig. 39 Two-dimensional spectra of sum energy versus time of flight measured with a gold sample; the various steps of background subtraction are illustrated from top to bottom.

time-dependent parts due to neutrons scattered from the sample or in the air along the flight path through the detector.

The spectrum in the mid part of fig. 39 is obtained after subtraction of background measured without sample, containing only events that are correlated with the sample, i.e. the true capture events around 6.5 MeV sum energy and background due to sample scattered neutrons. The latter component can be accounted for by the properly normalized spectrum measured with the carbon sample, that has been subtracted in the lower part of fig. 39. There, only the true capture events at the 6.5 MeV binding energy of gold are left, which fall in a TOF interval of about 500 ns according to the investigated neutron energy range from 10 to 200 keV (for 77 cm flight path).

The difference in background due to scattered neutrons around 9 MeV, that is observed between the upper and the mid part of fig. 39, indicates that the contributions from scattering in air and in the sample are about equal. Therefore, in future experiments the neutron beam will be guided through the detector in an evacuated flight tube, in order to eliminate air scattering.

The projected sum energy spectrum obtained with the carbon sample is shown in fig. 40. Neutron capture in BaF_2 is dominated by ^{137}Ba and ^{135}Ba with binding energies of 8.6 and 9.1 MeV, respectively. A smaller part due to capture in ^{134}Ba and ^{136}Ba peaks at 6.9 MeV, whereas capture in ^{138}Ba and ^{19}F is almost negligible due to the low capture cross sections of both isotopes. The latter components are problematic as they fall in a sum energy range, where one expects the capture events of gold and of most isotopes of astrophysical interest.

The TOF spectrum of fig. 41 was obtained from the two-dimensional distribution of the gold sample (bottom part of fig. 39) by summation over the energy range around the maximum at 6.5 MeV. The corresponding background due to sample scattered neutrons is included for comparison. Fig. 41 verifies two important features:

- (i) The energy range from 150 to 200 keV is free of background (see § 2.3 and table 5).
- (ii) Sample scattered background is strongly spread in time, confirming the previous calculation (fig.6).

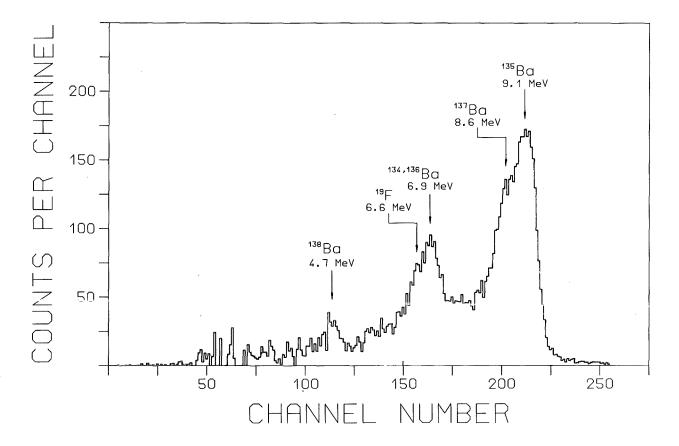


Fig. 40 Sum energy spectrum due to neutron captures in the BaF₂ crystals as measured with a carbon sample. The various components are easily attributed to capture in different barium isotopes.

Table 6. Parameters of the neutron source.

Accelerator: 3.75 MV Van de Graaff

Proton energy: 10 - 100 keV above ⁷Li(p,n)⁷Be threshold

10 100 Key above Expire be direction

Repetition rate: 250 kHz

Pulse width: <1 ns

Beam intensity: 2 μA

Neutron target: ~1.8 mg/cm² metallic lithium on water cooled

copper or silver backing

Neutron spectrum: continuous, ranging in energy from 5 keV to

an upper limit between 70 and ~210 keV.

Flight path: 77 cm

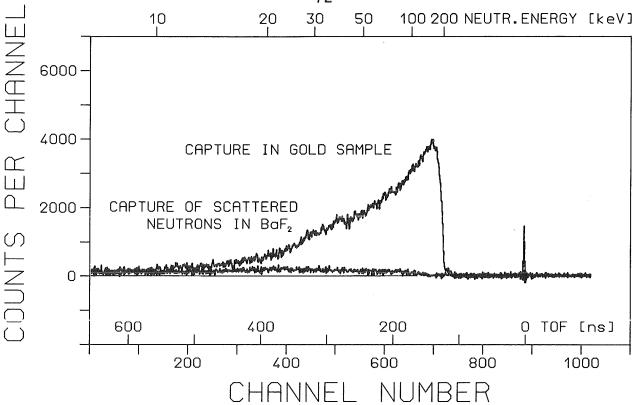


Fig. 41 The net TOF spectrum recorded with a 2 g gold sample in a neutron spectrum ranging from 5 to 200 keV. The background due to sample scattered neutrons that was subtracted before is shown separately. The spectrum was obtained by summation of the pulse height channels around the binding energy (see fig. 42).

(iii) Selecting distinct channels in the sum energy spectrum around the binding energy eliminates most of the background (the calculation in fig. 6 was performed without such selection).

Despite the fact that the cross section ratio for capture and scattering in gold is $\sim 1:20$, the measured signal to background ratio is very favorable; even at 10 keV it is still 2:1. Nevertheless, only the energy range above 20 keV will be evaluated from this spectrum, as better signal to background ratios can be obtained at low energies in runs where the maximum neutron energy is restricted to ≤ 100 keV.

From the spectrum of fig. 41 only the cross section shape can be evaluated. For normalization, sum energy spectra are calculated by adding the TOF channels in the neutron energy range from 150 to 200 keV, the region with the best signal to background ratio. The resulting spectra for gold and rhodium are shown in fig. 42. In both spectra about 95 % of all capture events are observed above the experimental

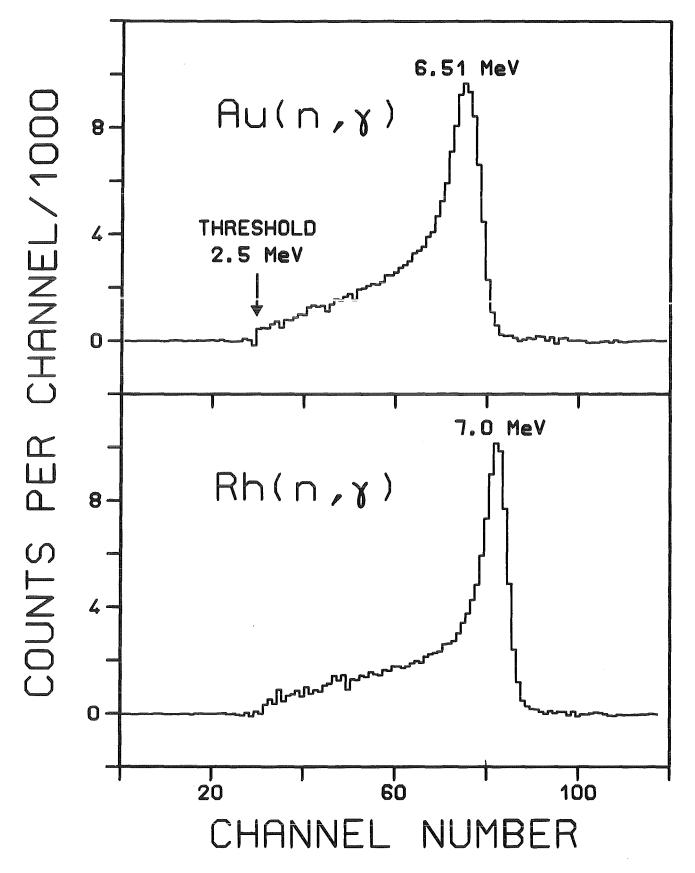


Fig. 42 Sum energy spectra for neutron capture in gold and rhodium. The spectra were obtained by adding the time of flight channels in the neutron energy range from 150 to 200 keV (see fig. 41).

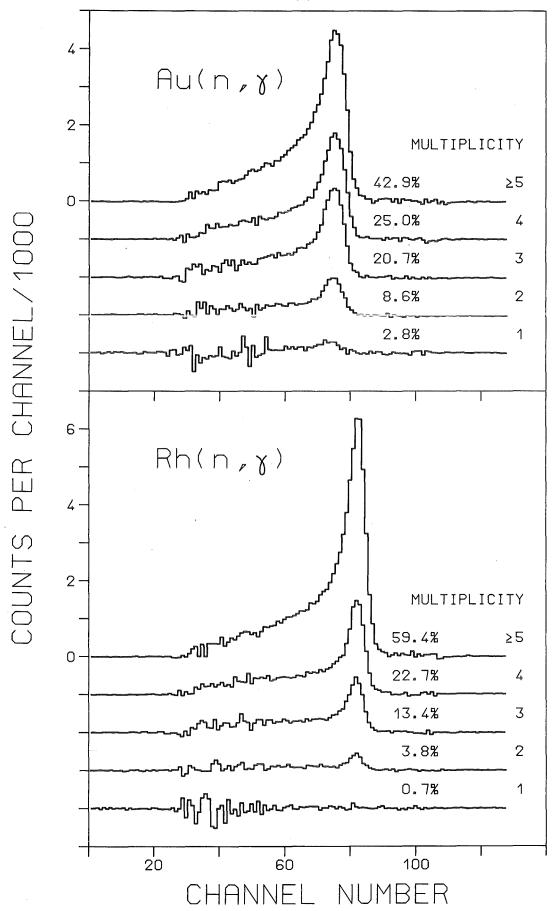


Fig. 43 Sum energy spectra for neutron capture in gold and rhodium for different multiplicities.

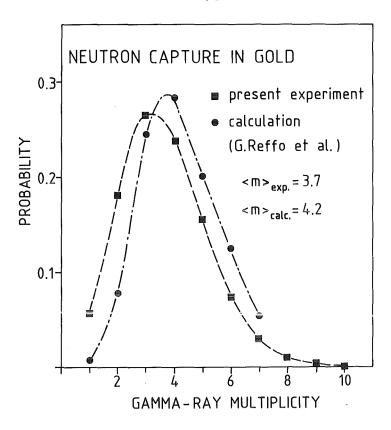


Fig. 44 The uncorrected experimental multiplicity distribution for neutron capture in gold (squares) compared to a previous calculation [16].

threshold of 2.5 MeV. The correction for the cross section ratio $\sigma(Rh)/\sigma(Au)$, which results from extrapolation to lower energies is 0.98 with an absolute uncertainty of \pm 0.6 %.

The dependence of the observed effect on event multiplicity is shown in fig. 43 for gold and rhodium. About 50% of all events exhibit multiplicities of five or more, while only 1 to 2% are observed with multiplicity one. For the gold sample, the measured neutron capture multiplicities are compared in fig. 44 to a theoretical calculation [16]. Reasonable agreement is found if one considers that the experimental results are not yet corrected for detector-detector scattering, for the limited solid angle of that experiment (95% of 4π), and for the threshold energy of about 60 keV in the gamma-ray detectors that cuts off transitions between the first excited states in gold frequently populated in the calculations.

As discussed in detail [40], the overall accuracy obtained in first cross section measurements on samples of niobium, tantalum, and rhodium is about ± 1.2 %. Several improvements (§ 9) that are realized meanwhile or are under development will allow to exceed this result in the future.

9. CONCLUSIONS

9.1 IMPROVEMENTS

During the first capture cross section measurements on samples of niobium, tantalum, and rhodium relative to a gold standard, the experimental method was studied in detail and several possible improvements were persued for future implementation.

At present, the achieved uncertainty of \pm 1.2 % is mainly due to the absolute normalization of the cross section shape. In this step of data analysis, the number of events above the experimental threshold of 2.5 MeV has to be determined including all multiplicities, e.g. from the spectra shown in fig. 43. Although the number of true events with multiplicities 1 or 2 is small, an exact analysis is difficult because of significant statistical fluctuations; these are due to the subtraction of sizeable background from radium impurities in the BaF₂ crystals.

In view of this situation, the following improvements are planned or already realized:

- (i) The spectra shown in fig. 43 have been measured with 40 detector modules covering 95% of the full solid angle; two positions were left open for the neutron beam to pass. This means for a capture cascade of multiplicity 4 that there is already a 20% probability that one of the gamma-rays escapes from the detector without hitting a BaF_2 crystal at all. Hence, the number of events in the full energy peak is reduced and the average multiplicity appears too low. A significant fraction of the missing solid angle presently not filled with BaF_2 will be covered in the future by crystals with a central hole of 50 mm diameter for the neutron beam.
- (ii) The background from radium impurities was reduced meanwhile by 40% as the eight crystals with the largest radium content were replaced. These new crystals are already included in fig. 26; the two modules with decay rates above 1000 s^{-1} shown there will not be used furtheron.
- (iii) The pulsing system of our accelerator is presently modified with the aim to improve the intensity per pulse in the extracted proton beam. Any such improvement will translate linearly in an improved signal to background ratio for that component which is not correlated with the neutron beam.
- (iv) Neutron scattering in the air along the 50 cm flight path through the detector will be eliminated by evacuated flight tubes for the neutron beam, thus reducing the respective background significantly.

9.2 SUMMARY

After 30 years of neutron capture cross section measurements with liquid scintillator tanks, Moxon-Rae detectors, and total energy detectors, the potential of these methods seems to be exhausted. Any further improvement can only be achieved by new techniques. An attempt for establishing such a technique was made with the 4π BaF₂ detector using the impressive features of BaF₂ for gamma-ray detection discovered six years ago.

The favorable combination of a Van de Graaff accelerator and the 4π BaF₂ detector for measurements in the keV neutron energy range was discussed in detail. With the $^7\text{Li}(p,n)^7\text{Be}$ reaction as an efficient source of keV neutrons and with flight paths of less than 1 m, it is well suited for the intended application as neutron production can be restricted exactly to the energy range of astrophysical interest. The setup offers a number of possibilities for background suppression, and the remaining backgrounds can be studied quantitatively. Barium fluoride proved to be the best available scintillator, combining high efficiency, good energy resolution, and excellent timing with a low sensitivity to capture of keV neutrons.

The new method required significant investments for scintillator, electronics, and computers; large amounts of data have to be handled, and painstaking procedures had to be worked out in order to verify each step of data analysis. However, already the first results confirmed that it was worth this effort, and that data with significantly improved accuracy can be expected in the near future.

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APPENDIX A

A FORTRAN code for Monte Carlo simulation of neutron scattering from the capture sample

```
//IAK554F4 JOB (0554,145,P0A0B),WISSHAK,NOTIFY=IAK554,TIME=5
// EXEC F7CLG, PLOT=VERSATEC
//C.SYSPRINT DD DUMMY
//C.SYSIN DD DISP=SHR, DSN=TSO554.WBALL4.FORT
// DD DISP=SHR, DSN=TSO554.PLOT2.CNTL
//L.SYSPRINT DD DUMMY
//L.SYSIN DD *
 ENTRY MAIN
//G.SYSIN DD *
          9
                10000
                                0
                                           0
10.
           25.
                      1.
0.
           1.
 1.680E+22137.
                                                                   0.
                      19.0
                                  0.
                                                       2.
                                            1.
25.
           19.
                      0.
80.
70.
                                            10.
           80.
                      5.
                                  1.126
60.
           70.
                      50.
                                  1.209
                                            10.
50.
           60.
                      100.
                                  1.314
                                            10.
40.
           50.
                      100.
                                  1.453
                                            10.
30.
           40.
                      100.
                                  1.647
                                            10.
20.
                                  1.949
           30.
                      83.
                                            10.
15.
                                  2.330
           20.
                      57.
                                            10.
10.
           15.
                      40.
                                  2.757
                                            10.
5.
           10.
                      26.
                                  3.559
                                            10.
```

0.1 0.103 0.106 0.273	1.535 1.535 1.535 0.82	6.5 100. 6.5 6.4			
0.273	0.80	50.			
0.293	0.78	6.4			
0.40	0.64	7.0			
0.419	0.62	40.			
0.437	0.60	8.0			
1.0	0.36	8.0			
5.0	0.13	7.7			
10.0	0.086	7.4			
15.0	0.067	7.0			
20.0	0.060	6.8			
31.6	0.049	5.5			
32.4	0.048	20.			
33.2	0.047	8.0			
50. 51.8	0.039	5.0 15.			
52.7	0.038	7.0			
70.	0.037	6.5			
71.7	0.032	15.			
73.4	0.0315	6.5			
100.		6.0			
120.	0.025	5.5			
0.1		3.9			
0.5		3.75			
1.0	0.0003	3.7			
5.0	0.0002	3.6			
10.0	0.0001	3.5			
20.0	0.0004	3.5			
25.0	0.002	4.0			
27.5	0.200	50.0			
30.0		4.0			
40.0	0.0005	3.5			
42.5	0.03	4.0			
45.0	0.002	4.5			
50.0	0.04	40.0			
55.0	0.0007	4.5			
60.0	0.0005	3.3			
75.0	0.0005	3.3			
90.0	0.002	10. 25.0			
100.0 115.0	0.006 0.001	7.0			
0.1	0.001	0.0			
//PLOTPARN		0,0			
&PLOT MODE=0, IOMASK=10 &END					
//PL EXEC		. 10 55111			

```
C
                                                                              00000100
С
    PROGRAMM ZUM BERECHNEN DER NEUTRONENEMPFINDLICHKEIT
                                                                              00000200
С
    VON BGO BAF NAJ
                                                                              00000300
С
                                                                              00000400
       COMMON NUNT, NOB, N, M, IY, DENSTY, ESIG, SIGC, SIGN, AI1, AI2, AI3
                                                                              00000500
      DIMENSION NOUT(100), NCAP(100), NIN(100),
                                                                              00000600
     1ESIG(3,100),SIGC(3,100),SIGN(3,100),
                                                                              00000700
     2E(100), XX(100), YY(100), ZZ(100), TT(100), SS(100),
                                                                              00000800
     3STETA(100), SPHI(100), R(100),
                                                                              00000900
     4RMATRX(3,3),SIGANZ(3),
                                                                              00001000
     5NTIMEI(200), NTIMEO(200), NTIMEC(200), NENOUT(100), NENIN(100),
                                                                              00001100
     6NENCAP(100), IFELD(10, 12), OFELD(20, 5), ENEIN(200)
                                                                              00001200
      DIMENSION ENECAP(1000), ENEOUT(1000), UNTCAP(200), EFFEKT(200),
                                                                              00001210
     1ELOWER(20), EUPPER(20), FLUSS(20), SIGMAG(20), FAKTOR(20),
                                                                              00001220
     2TIMELO(20), TIMEUP(20), UNTOUT(200),
                                                                              00001230
     3MTIMEO(20,200), MTIMEC(20,200), MENOUT(20,100), MENCAP(20,100)
                                                                              00001240
      DIMENSION XXX(200), IBUF(8000), YYY(200)
                                                                              00001250
C.... DIMENSION PPS2(100), PPTETA(100), PPPHI(100), PPAAA(100)
                                                                              00001300
C
                                                                              00001400
C
      EINLESEN DER ANFANGSWERTE
                                                                              00001500
C
                                                                              00001600
      READ(5,400)NENER, NEUTRS, NUNT, NOB
                                                                              00001700
      READ(5,401)RIN, ROUT, RPROB
                                                                              00001800
      READ(5,401)GRENZ1,GRENZ2
                                                                              00001900
      READ(5,402)DENSTY, AA1, AA2, AA3, AI1, AI2, AI3
                                                                              00002000
      READ(5,401)SIGANZ(1),SIGANZ(2),SIGANZ(3)
                                                                              00002100
      WRITE (6,403) NENER, NEUTRS, NUNT, NOB
                                                                              00002200
      WRITE (6,404) RIN, ROUT, RPROB
                                                                              00002300
      WRITE (6,405) GRENZ1, GRENZ2
                                                                              00002400
      WRITE(6,406)DENSTY,AA1,AA2,AA3,AI1,AI2,AI3
                                                                              00002500
      WRITE(6,407)SIGANZ(1),SIGANZ(2),SIGANZ(3)
                                                                              00002600
  400 FORMAT(4I10)
                                                                              00002700
  401 FORMAT(3F10.5)
                                                                              00002800
  402 FORMAT(E10.3,6F10.2)
                                                                              00002900
  403 FORMAT('1 ANZENERGIE, ANZNEUTRONEN, FLAGN, FLAGM', 4110)
                                                                              00003000
  404 FORMAT('
                 RIN, ROUT, RPROB ', 3F10.2)
                                                                              00003100
  405 FORMAT('
                                                 ',2F10.4)
                 GRENZE FUER ZUFALLSZAHLEN
                                                                              00003200
                 MOLEK/CM3, MASSE1, 2, 3, HAUFIGKEIT1, 2, 3, E10.3, 6F10.2)
  406 FORMAT('
                                                                              00003300
  407 FORMAT('
                 ANZAHL DES STUETZSTELLEN FUER SIGMA ',3F10.2)
                                                                              00003400
C
                                                                              00003410
C
      EINLESEN DER ENERGIEBEREICHE ETC
                                                                              00003420
C
                                                                              00003430
      DO 124 I=1,10
                                                                              00003431
      TIMELO(I)=0.
                                                                              00003432
      TIMEUP(I)=0.
                                                                              00003433
      ELOWER(I)=0.
                                                                              00003434
      EUPPER(I)=0.
                                                                              00003435
      FLUSS(I)=0.
                                                                              00003436
      FAKTOR(I)=0.
                                                                              00003437
      SIGMAG(I)=0.
                                                                              00003438
  124 CONTINUE
                                                                              00003439
      READ(5,401)FLUGW
                                                                              00003440
  WRITE(6,513)FLUGW
513 FORMAT(' FLUGWEG IN CM ',F10.5)
                                                                              00003450
                                                                              00003460
      DO110 K=1, NENER
                                                                              00003470
      READ(5,510)ELOWER(K), EUPPER(K), FLUSS(K), SIGMAG(K), FAKTOR(K)
                                                                              00003480
```

```
510 FORMAT(5F10.5)
                                                                             00003490
      WRITE(6,511)ELOWER(K), EUPPER(K), FLUSS(K), SIGMAG(K), FAKTOR(K)
                                                                             00003491
  511 FORMAT(' ELOWER, EUPPER, FLUSS, SIGMAG, FAKTOR ', 5F10.5)
                                                                             00003492
  110 CONTINUE
                                                                             00003493
C
                                                                             00003500
C
      ANFANGSWERTE SETZEN UND FELDER NULLEN
                                                                             00003600
C
                                                                             00003700
      IY=37
                                                                             00003800
      PIPI=3.14159
                                                                             00003900
      TTT=22.861
                                                                             00004000
      QRIN=RIN**2
                                                                             00004200
      QROUT=ROUT**2
                                                                             00004300
      QRPROB=RPROB**2
                                                                             00004400
C....TEST FUER ZUFALLSZAHLEN
                                                                             00004500
С
      DO 100 K=1,100
                                                                             00004600
      NOUT(K)=0
                                                                             00004700
C 100 CONTINUE
                                                                             00004800
C
      DO 102 K=1,1000000
                                                                             00004900
\mathbb{C}
      PPP=RANDOM(0.)
                                                                             00005000
C
      IPPP=PPP*100.
                                                                             00005100
C
      IPPP=IPPP+1
                                                                             00005200
C
      IF(IPPP.GT.100)IPPP=100
                                                                             00005300
C
      NOUT(IPPP)=NOUT(IPPP)+1
                                                                             00005400
C 102 CONTINUE
                                                                             00005500
C WRITE(6,408)(NOUT(K),K=1,100)
C 408 FORMAT(' ',10110)
                                                                             00005600
                                                                             00005700
C....TEST ENDE
                                                                             00005800
                                                                             00005810
C
      FELDER FUER BERECHNUNG DER UNTERGRUNDSPEKTREN NULLEN
                                                                             00005820
C
                                                                             00005830
      D0111 I=1,10
                                                                             00005840
      DO111 K=1,100
                                                                             00005850
      MTIMEO(I,K)=0
                                                                             00005860
      MTIMEC(I,K)=0
                                                                             00005870
      MTIMEO(I,100+K)=0
                                                                             00005880
      MTIMEC(I,100+K)=0
                                                                             00005890
      MENOUT(I,K)=0
                                                                             00005891
  111 MENOUT(I,K)=0
                                                                             00005892
      DO 116 K=1,200
                                                                             00005893
      UNTCAP(K)=0.
                                                                             00005894
      EFFEKT(K)=0.
                                                                             00005895
  116 UNTOUT(K)=0.
                                                                             00005896
      DO 122 K=1,1000
                                                                             00005897
      ENECAP(K)=0.
                                                                             00005898
  122 ENEOUT(K)=0.
                                                                             00005899
C
                                                                             00007200
C
      EINLESEN DER WIRKUNGSQUERSCHNITTE
                                                                             00007300
C
                                                                             00007400
      DO 2 I=1,3
                                                                             00007500
      ISIG=SIGANZ(I)
                                                                             00007600
      DO 4 K=1, ISIG
                                                                             00007700
      READ(5,501)ESIG(I,K),SIGC(I,K),SIGN(I,K)
                                                                             00007800
      WRITE(6,501)ESIG(I,K),SIGC(I,K),SIGN(I,K)
                                                                             00007900
    4 CONTINUE
                                                                             00008000
    2 CONTINUE
                                                                             00008100
  501 FORMAT(7F10.4)
                                                                             00008200
C....
                                                                             00008300
```

```
C
                                                                              00008400
C
       EINLESEN DER ZUFALLSZAHLEN
                                                                              00008500
C
                                                                              00008600
C
                                                                              00008700
      READ(5,502)(PPS2(K),K=1,10)
C
       READ(5,502)(PPTETA(K),K=1,10)
                                                                              00008800
C
       READ(5,502)(PPPHI(K),K=1,10)
                                                                              00008900
C
      READ(5,502)(PPAAA(K),K=1,10)
                                                                              00009000
C
  502 FORMAT(10F7.5)
                                                                              00009100
C
  WRITE(6,504)
504 FORMAT(' EINGEGEBENE ZUFALLSZAHLEN
                                                                              00009200
C
                                                                              00009300
C
      WRITE(6,503)(PPS2(K),K=1,10)
                                                                              00009400
C
      WRITE(6,503)(PPTETA(K),K=1,10)
                                                                              00009500
C
      WRITE(6,503)(PPPHI(K),K=1,10)
                                                                              00009600
С
      WRITE(6,503)(PPAAA(K),K=1,10)
                                                                              00009700
C 503 FORMAT(' ',10F10.5)
                                                                              00009800
C....
                                                                              00009900
C
                                                                              00009910
C
      BEGINN EINER DO SCHLEIFE UEBER ANZAHL DER ENERGIEPUNKTE
                                                                              00009920
\mathbf{C}
                                                                              00009930
      DO 4444 L=1, NENER
                                                                              00009940
      ENO=(ELOWER(L)+EUPPER(L))/2.
                                                                              00009950
      WRITE(6,512)L,EN0
                                                                              00009960
  512 FORMAT('1'/' L NEUTRONENERGIE ',I10,F10.5)
                                                                              00009970
      NNN=0
                                                                              00009980
      DO1 K=1,100
                                                                              00009990
      NOUT(K)=0
                                                                              00009991
      NCAP(K)=0
                                                                              00009992
      NIN(K)=0
                                                                              00009993
      NTIMEO(K)=0
                                                                              00009994
      NTIMEC(K)=0
                                                                              00009995
      NTIMEI(K)=0
                                                                              00009996
      NTIMEO(100+K)=0
                                                                              00009997
      NTIMEC(100+K)=0
                                                                              00009998
      NTIMEI(100+K)=0
                                                                              00009999
      NENOUT(K)=0
                                                                              00010000
      NENCAP(K)=0
                                                                              00010001
    1 NENIN(K)=0
                                                                              00010002
С
                                                                              00010010
С
      BEGINN DER DO SCHLEIFE UBER DIE ANZAHL DER NEUTRONEN
                                                                              00010100
С
                                                                              00010200
      DO 1000 N=1, NEUTRS
                                                                              00010300
      KCC=0
                                                                              00010400
      KKK=0
                                                                              00010500
      KPP=0
                                                                              00010600
      MMM=0
                                                                              00010700
      DO 5 K=1,100
                                                                              00010800
      E(K)=0.
                                                                              00010900
      XX(K)=0.
                                                                              00011000
      YY(K)=0.
                                                                              00011100
      ZZ(K)=0.
                                                                              00011200
      TT(K)=0.
                                                                              00011300
      SS(K)=0.
                                                                              00011400
      STETA(K)=0.
                                                                              00011500
      SPHI(K)=0.
                                                                              00011600
    5 R(K) = 0.
                                                                              00011700
C
                                                                              00011800
С
      INTERPOLIEREN DER QUERSCHNITTE UND BERECHNEN DER FREIEN WEGLAENGE 00011900
```

```
C
      UND WECHSELWIRKUNGSWARSCHEINLICHKEITEN FUER DIE ERSTE WW
                                                                               00012000
C
                                                                               00012100
      CALL B10H14(ENO, PATHO, PS1, PS2, PS3)
                                                                               00012200
CC....FUER TESTZWECKE FREIE WEGLAENGE FIX
                                                                               00012300
CC
      PATH0=2.
                                                                               00012400
CC....
                                                                               00012500
  IF(N.LE.NOB.AND.N.GE.NUNT)WRITE(6,671)EN0,PATH0,PS1,PS2,PS3
671 FORMAT(' EN0,PATH0,PS1,PS2,PS3 ',5F10.3)
                                                                               00012600
                                                                               00012700
C
                                                                               00012800
С
      BERECHNUNG DES ORTES DER ERSTEN WW
                                                                               00012900
C
                                                                               00013000
C....TEST OB S2 WIRKLICH EXPONENTIELL VERTEILT IST
                                                                               00013100
      DO 6 K=1,100
                                                                               00013200
C
      E(K) = -PATHO * ALOG(RANDOM(0.))
                                                                               00013300
C
    6 CONTINUE
                                                                               00013400
C WRITE(6,410)(E(K),K=1,100)
C 410 FORMAT('',10F10.5)
C
                                                                               00013500
                                                                               00013600
      DO 7 K=1,100
                                                                               00013700
    7 E(K)=0.
                                                                               00013800
C....TEST ENDE
                                                                               00013900
      PPP=RANDOM(0.)
                                                                               00014000
      PPP=PPS2(1)
                                                                               00014100
      IF(PPP.LT.GRENZ1)PPP=GRENZ1
                                                                               00014200
      IF(PPP.GT.GRENZ2)PPP=GRENZ2
                                                                               00014300
      S2=-PATHO*ALOG(PPP)
                                                                               00014400
      IF(N.GE.NUNT.AND.N.LE.NOB)WRITE(6,411)PPP,S2
                                                                               00014500
  411 FORMAT(' ZUFALLSZAHL UND ERSTES S2 ',2F10.5)
                                                                               00014600
      X2=0.
                                                                               00014700
      Y2=0.
                                                                               00014800
      Z2=RIN+S2
                                                                               00014900
      E(1)=ENO
                                                                               00015000
      XX(1)=0.
                                                                               00015100
      YY(1)=0.
                                                                               00015200
      ZZ(1)=RIN+S2
                                                                               00015300
      TT(1)=TTT*ZZ(1)/SQRT(E(1))
                                                                               00015400
      R(1)=RIN+S2
                                                                               00015500
      SS(1)=S2
                                                                               00015600
      STETA(1)=0.
                                                                               00015700
      SPHI(1)=0.
                                                                               00015800
      IF(S2.LE.(ROUT-RIN))GOTO 12
                                                                               00015900
C
                                                                               00016000
C
      UBERHAUPT KEINE WW IN KUGEL
                                                                               00016100
C
                                                                               00016200
      NOUT(1)=NOUT(1)+1
                                                                               00016300
      TT(1)=TTT*ROUT/SQRT(E(1))
                                                                               00016400
      M=1
                                                                               00016500
      KKK=1
                                                                               00016600
      MMM=1
                                                                               00016700
      IF (N.GE.NUNT.AND.N.LE.NOB) WRITE (6,409) TT(1)
                                                                               00016800
  409 FORMAT(' NEUTRON HAT KUGEL VERLASSEN VOR ERSTER WW, ZEIT: ',F10.5)
                                                                               00016900
      GOTO 1111
                                                                               00017000
C
                                                                               00017100
C
      AUSWUERFELN OB ERSTE WW STREUUNG ODER CAPTURE
                                                                               00017200
C
                                                                               00017300
   12 PPP=RANDOM(0.)
                                                                               00017400
      IF(PPP.LT.GRENZ1)PPP=GRENZ1
                                                                               00017500
```

c	C. 12	IF(PPP.GT.GRENZ2)PPP=GRENZ2 PPP=PPAAA(1)	00017600 00017700
Ì		IF(N.GE.NUNT.AND.N.LE.NOB)WRITE(6,412)PPP	00017700
	412	FORMAT(' ZUFALLSZAHL FUER ERSTE WW ',F10.5)	00017800
	7.2.2.	IF(PPP.LE.PS1)GOTO 15	00017900
		IF(PPP.LE.PS2)GOTO 16	00018000
		IF(PPP.LE.PS3)GOTO 17	00018100
C	•	11 (111.111.115)(6010-17	00018200
C		EINFANG NACH ERSTER WW	00018300
C		TIME AND MADE ERSTEN WW	00018400
Ī		NCAP(1)=NCAP(1)+1	00018500
		KCC=1	00018300
		MMM=1	00018700
		M=1	00018000
		GOTO 1111	00019000
	15	AAA=AA1	00019100
		GOTO 20	00019200
	16	AAA=AA2	00019300
		GOTO 20	00019400
	17	AAA=AA3	00019500
		DO 31 I=1,3	00019600
		DO 31 J=1,3	00019700
	31	RMATRX(I,J)=0.	00019800
		DO 32 I=1,3	00019900
	32	RMATRX(I,I)=1.	00020000
C	;		00020100
C		BEGIN DER DOSCHLEIFE UBER BIS ZU 100 STREUUNGEN	00020200
C	:		00020300
		DO 2222 M=2,100	00020400
		X1=XX(M-1)	00020500
		Y1=YY(M-1)	00020600
		Z1=ZZ(M-1)	00020700
		PPP=RANDOM(0.)	00020800
		IF(PPP.LT.GRENZ1)PPP=GRENZ1	00020900
_	C	IF(PPP.GT.GRENZ2)PPP=GRENZ2	00021000
U	U	PPP=PPTETA(M) THETA=PIPI*PPP	00021100
		IF(N.GE.NUNT.AND.N.LE.NOB)WRITE(6,413)N,M,PPP,THETA	00021200 00021300
	413	FORMAT(' ',2110,' ZUFALLSZAHL UND THETA ',2F10.5)	00021300
	715	PPP=RANDOM(0.)	00021400
		IF(PPP.LT.GRENZ1)PPP=GRENZ1	00021500
		IF (PPP.GT.GRENZ2)PPP=GRENZ2	00021000
С	C	PPP=PPPHI(M)	00021700
Ü	· · · ·	PHI=2.*PIPI*PPP	00021000
		IF(N.GE.NUNT.AND.N.LE.NOB)WRITE(6,414)N,M,PPP,PHI	00022000
	414	FORMAT(' ',2110,' ZUFALLSZAHL UND PHI ',2F10.5)	00022100
		EN=E (M-1)	00022200
C			00022300
C		BERECHNUNG DER ENERGIE NACH DEM STOSS UND THETA IM LAB SYSTHEM	00022400
С			00022500
		CALL CMLAB(EN, THETA, AAA)	00022600
C			00022700
С		INTERPOLATION DER QUERSCHNITTE UND FREIEN WEGLAENGE FUER NAECHSTE	00022800
C		WW	00022900
		CALL B10H14(EN, PATH0, PS1, PS2, PS3)	00023000
	C		00023100
С	C	FESTLEGEN DER FREIEN WEGLAENGE	00023200

```
CC
      PATH0=2.0
                                                                           00023300
CC...
                                                                           00023400
      IF (N.GE.NUNT.AND.N.LE.NOB) WRITE (6,671) EN, PATHO, PS1, PS2, PS3
                                                                           00023500
C
                                                                           00023600
С
      BERECHNUNG DES WEGES BIS ZUR NAECHSTEN WW
                                                                           00023700
C
                                                                           00023800
   39 PPP=RANDOM(0.)
                                                                           00023900
      IF(PPP.EQ.O.)GOTO 39
                                                                           00023910
      IF(PPP.LT.GRENZ1)PPP=GRENZ1
                                                                           00024000
      IF (PPP.GT.GRENZ2)PPP=GRENZ2
                                                                           00024100
CC... PPP=PPS2(M)
                                                                           00024200
      S2=-PATHO*ALOG(PPP)
                                                                           00024300
      IF(N.GE.NUNT.AND.N.LE.NOB)WRITE(6,415)N,M,PPP,S2
                                                                           00024400
  415 FORMAT(' ',2I10,' ZUFALLSZAHL,S2 ',2F10.5)
                                                                           00024500
C
                                                                           00024600
С
      BERECHNEN DER KOORDINATEN DER M-TEN WW
                                                                           00024700
C
                                                                           00024800
      CALL EULER(X1,Y1,Z1,RMATRX,S2,THETA,PHI,X2,Y2,Z2,R2SQR)
                                                                           00024900
      XX(M)=X2
                                                                           00025000
      YY(M)=Y2
                                                                           00025100
      ZZ(M)=Z2
                                                                           00025200
      E(M)=EN
                                                                           00025300
      SS(M)=S2
                                                                           00025400
      STETA(M)=THETA
                                                                           00025500
      SPHI(M)=PHI
                                                                           00025600
      R(M) = SQRT(R2SQR)
                                                                           00025700
      TT(M)=TT(M-1)+TTT*S2/SQRT(EN)
                                                                           00025800
      IF(N.LT.NUNT.OR.N.GT.NOB)GOTO 40
                                                                           00025900
      WRITE(6,678)N,M,X1,Y1,Z1,S2,THETA,PHI,X2,Y2,Z2,R2SQR
                                                                           00026000
  678 FORMAT(216, 'RPOLAR', 10F10.3//)
                                                                           00026100
   40 CONTINUE
                                                                           00026200
C
                                                                           00026300
C
      FESTSTELLEN WO NEUER WW PUNKT LIEGT
                                                                           00026400
С
                                                                           00026500
C
                                                                           00026600
C
      ENTSCHEIDUNG WO NEUTRONENBAHN KUGELSCHALEN MIT RIN, ROUT, RPROBE
                                                                           00026700
С
      TRIFFT
                                                                           00026800
C
                                                                           00026900
   42 XN1=0.
                                                                           00027000
      YN1=R(M-1)
                                                                           00027100
      PYY = (R(M-1)+R(M)+S2)/2.
                                                                           00027200
      IF(PYY.GT.AMAX1(R(M-1),R(M),S2))GOTO 43
                                                                           00027300
C
                                                                           00027400
С
      SPEZIALFALL R(M-1), R(M)UND S2 LIEGEN AUF EINER GERADE
                                                                           00027500
C
                                                                           00027600
      WRITE(6,698)N,M,R(M-1),R(M),S2
                                                                           00027700
  698 FORMAT(' STREUUNG SPEZIELL BEH.DA XN2=0, R(M-1),R(M),S2: ',2I10,3F00027800
     110.5)
                                                                           00027900
      IF(R(M).GE.R(M-1).AND.R(M).GT.ROUT.AND.S2.LT.AMAX1(R(M),R(M-1)))G000028000
     1TO 104
                                                                           00028100
      GOTO 101
                                                                           00028200
  104 DIFF1=R(M)-ROUT
                                                                           00028300
      GOTO 200
                                                                           00028400
  101 IF(R(M).GE.R(M-1).AND.R(M).LE.ROUT.AND.S2.LT.AMAX1(R(M),R(M-1)))G000028500
     1TO 3333
      IF(R(M).LT.R(M-1).AND.R(M).GE.RIN.AND.S2.LT.AMAX1(R(M),R(M-1)))GOTO0028700
```

```
10 3333
                                                                           00028800
      IF(R(M).LT.R(M-1).AND.R(M).LT.RIN.AND.S2.LT.AMAX1(R(M),R(M-1)))GOT00028900
                                                                           00029000
      IF(R(M).LE.ROUT.AND.S2.GT.AMAX1(R(M),R(M-1)))GOTO 103
                                                                           00029100
      IF(R(M).GT.ROUT.AND.S2.GT.AMAX1(R(M),R(M-1)))DIFF1=R(M)-ROUT
                                                                           00029200
                                                                           00029300
  103 S2=S2+2.*RIN
                                                                           00029400
      CALL RPOLAR(X1,Y1,Z1,S2,THETA,PHI,X2,Y2,Z2,R2SQR)
                                                                           00029500
      XX(M)=X2
                                                                           00029600
      YY(M)=Y2
                                                                           00029700
      ZZ(M)=Z2
                                                                           00029800
      SS(M)=S2
                                                                           00029900
      R(M) = SQRT(R2SQR)
                                                                           00030000
      TT(M)=TT(M-1)+TTT*S2/SQRT(E(M))
                                                                           00030100
      IF(N.GE.NUNT.AND.N.LE.NOB)WRITE(6,685)X2,Y2,Z2,R2SQR
                                                                           00030200
      TIMEPR=TT(M-1)+TTT*R(M-1)/SQRT(E(M))
                                                                           00030300
      IF (N.GE.NUNT.AND.N.LE.NOB) WRITE (6,650) TIMEPR
                                                                           00030400
  650 FORMAT( PROBE ZENTRAL DURCHQUERT TIMEPR: ',F10.5)
                                                                           00030500
      GOTO 201
                                                                           00030600
C
                                                                           00030700
C
      NORMALFALL R(M-1), R(M)UND S2 LIEGEN NICHT AUF EINER GERADEN
                                                                           00030800
C
                                                                           00030900
   43 PXX=SQRT((PYY-S2)*(PYY-R(M-1))*(PYY-R(M))/PYY)
                                                                           00031000
      PALPHA=ATAN(PXX/(PYY-S2))
                                                                           00031100
      PALPHA=PALPHA*2.
                                                                           00031200
      XN2=R(M)*SIN(PALPHA)
                                                                           00031300
      YN2=R(M)*COS(PALPHA)
                                                                           00031400
      STEIG=(YN1-YN2)/(XN1-XN2)
                                                                           00031500
      PPPP=2.*STEIG*YN1/(1.+STEIG**2)
                                                                           00031600
      QQQQ = (YN1**2 - RIN**2) / (1. + STEIG**2)
                                                                           00031700
      QQQ1=(YN1**2-RPROB**2)/(1.+STEIG**2)
                                                                           00031800
      QQQ2=(YN1**2-ROUT**2)/(1.+STEIG**2)
                                                                           00031900
      DISK=PPPP**2/4.-QQQQ
                                                                           00032000
      DISK1=PPPP**2/4.-0001
                                                                           00032100
      DISK2=PPPP**2/4.-QQQ2
                                                                           00032200
      IF(N.GE.NUNT.AND.N.LE.NOB)WRITE(6,679)XN1,YN1,PALPHA,XN2,YN2,
                                                                           00032300
     1STEIG, DISK, DISK1, DISK2
                                                                           00032400
  679 FORMAT(' XN1, YN1, PALPHA, XN2, YN2, STEIG, DISK, DISK1, DISK2', /, 10F10.4)00032500
C
                                                                           00032600
C
      FESTSTELLUNG OB NEUE WW PUNKT AUSSERHALB LIEGT
                                                                           00032700
С
                                                                           00032800
      IF(R2SQR.LE.QROUT)GOTO 13
                                                                           00032900
С
                                                                           00033000
С
      BERECHNUNG WANN NEUTRON DIE AUSSENKUGEL DURCHQUERT
                                                                           00033100
C
                                                                           00033200
      XN3 = -PPPP/2. + SQRT(DISK2)
                                                                           00033300
      XN4=-PPPP/2.-SQRT(DISK2)
                                                                            00033400
      YN3=STEIG*XN3+YN1
                                                                           00033500
      YN4=STEIG*XN4+YN1
                                                                           00033600
      DIFF1=SQRT((YN2-YN3)**2+(XN2-XN3)**2)
                                                                           00033700
      DIFF2=SQRT((YN2-YN4)**2+(XN2-XN4)**2)
                                                                           00033800
      IF(N.GE.NUNT.AND.N.LE.NOB)WRITE(6,681)XN3,XN4,YN3,YN4,DIFF1,DIFF2 00033900
  681 FORMAT(' SNITTPUNKTE MIT AUSSENKUGEL XN3, XN4, YN3, YN4, DIFF1, DIFF2 '00034000
     1,6F10.4)
                                                                           00034100
      DIFF1=AMIN1(DIFF1, DIFF2)
                                                                            00034200
  200 TT(M)=TT(M-1)+TTT*(S2-DIFF1)/SQRT(EN)
                                                                            00034300
```

```
IF (N.GE.NUNT.AND.N.LE.NOB) WRITE (6,677) TT (M)
                                                                           00034400
  677 FORMAT(' ZEITPUNKT WANN NEUTRON DIE KUGEL VERLAESST ',F10.5)
                                                                           00034500
      NOUT(M) = NOUT(M) + 1
                                                                           00034600
      KKK=1
                                                                           00034700
      MMM=M
                                                                           00034800
      GOTO 1111
                                                                           00034900
   13 IF(DISK.LE.O.)GOTO 3333
                                                                           00035000
C
                                                                           00035100
C
      NEUTRONENBAHN SCHNEIDET DIE INNENKUGEL
                                                                           00035200
C
                                                                           00035300
      XN3=-PPPP/2.+SQRT(DISK)
                                                                           00035400
      XN4=-PPPP/2.-SORT(DISK)
                                                                           00035500
      YN3=STEIG*XN3+YN1
                                                                           00035600
      YN4=STEIG*XN4+YN1
                                                                           00035700
C
                                                                           00035800
C
      ENTSCHEIDUNG OB NEUTRON NACH INNEN ODER AUSSEN FLIEGT
                                                                           00035900
                                                                           00036000
      IF(XN2*XN3.LT.0.)GOTO 3333
                                                                           00036100
      DIFF1=SQRT((YN1-YN3)**2+(XN1-XN3)**2)
                                                                           00036200
      DIFF2=SQRT((YN1-YN4)**2+(XN1-XN4)**2)
                                                                           00036300
      IF(S2.LE.AMIN1(DIFF1,DIFF2))GOTO 3333
                                                                           00036400
C
                                                                           00036500
С
      BERECHNUNG DES NEUEN KORRIGIERTEN ORTES DER NAECHSTEN WW
                                                                           00036600
С
                                                                           00036700
      S2=S2+ABS(DIFF1-DIFF2)
                                                                           00036800
      IF(N.GE.NUNT.AND.N.LE.NOB)WRITE(6,680)XN3,XN4,YN3,YN4,DIFF1,DIFF2,00036900
                                                                           00037000
  680 FORMAT(' INNENK.DURCHQXN3,XN4,YN3,YN4,DIFF1,DIFF2,S2NEU ',7F10.4)00037100
      CALL RPOLAR(X1,Y1,Z1,S2,THETA,PHI,X2,Y2,Z2,R2SQR)
                                                                           00037200
      XX(M)=X2
                                                                           00037300
      YY(M)=Y2
                                                                           00037400
      ZZ(M)=Z2
                                                                           00037500
      SS(M)=S2
                                                                           00037600
                                                                           00037700
      R(M) = SQRT(R2SQR)
      TT(M)=TT(M-1)+TTT*S2/SQRT(E(M))
                                                                           00037800
      IF(N.GE.NUNT.AND.N.LE.NOB)WRITE(6,685)X2,Y2,Z2,R2SQR
                                                                           00037900
  685 FORMAT(' X2NEU, Y2NEU, Z2NEU, R2SQRNEU ',4F10.4)
                                                                           00038000
      IF(DISK1.LE.O.)GOTO 41
                                                                           00038100
C
                                                                           00038200
C
      NEUTRON HAT BEREICH DER PROBE GETROFFEN
                                                                           00038300
C
                                                                           00038400
      XN3=-PPPP/2.+SQRT(DISK1)
                                                                           00038500
      XN4=-PPPP/2.-SQRT(DISK1)
                                                                           00038600
      YN3=STEIG*XN3+YN1
                                                                           00038700
      YN4=STEIG*XN4+YN1
                                                                           00038800
      DIFF1=SQRT((YN1-YN3)**2+(XN1-XN3)**2)
                                                                           00038900
      DIFF2=SQRT((YN1-YN4)**2+(XN1-XN4)**2)
                                                                           00039000
C
                                                                           00039100
C
      BERECHNUNG DES ZEITPUNKTS WANN PROBE GETROFFEN
                                                                           00039200
C
                                                                           00039300
      DIFF1=(DIFF1+DIFF2)/2.
                                                                           00039400
                                                                           00039500
      TIMEPR=TT(M-1)+TTT*DIFF1/SQRT(E(M))
      IF(N.GE.NUNT.AND.N.LE.NOB)WRITE(6,682)XN3,XN4,YN3,YN4,DIFF1,DIFF2,00039600
                                                                           00039700
  682 FORMAT(' PROBE DURCHQUERT XN3, XN4, YN3, YN4, DIFF1, DIFF2, TIMEPR
                                                                           00039800
                                                                           00039900
     17F10.4)
```

201	MTM/M\-MITM/M\ + 1	000/0000
201	NIN(M)=NIN(M)+1	00040000
	KPP=KPP+1	00040100
	ITIME=TIMEPR/10.	00040200
	ITIME=ITIME+1	00040300
	IF(ITIME.GT.200)ITIME=200	00040400
	NTIMEI(ITIME)=NTIMEI(ITIME)+1	00040500
	IENER=100.*E(M)/ENO	00040600
	IENER=IENER+1	00040700
	IF(IENER.GT.100)IENER=100	00040800
	NENIN(IENER)=NENIN(IENER)+1	00040900
C		00041000
C	FESTSTELLEN OB KORRIGIERTER ORT DER WW NOCH INNERHALB DER KUGEL	00041100
C		00041200
41	IF(R2SQR.LE.QROUT)GOTO 3333	00041300
~	GOTO42	00041400
C		00041500
C	ENTSCHEIDUNG OB NAECHSTE WW EINFANG ODER STREUUNG	00041600
C		00041700
3333	PPP=RANDOM(0.)	00041800
	IF(PPP.LT.GRENZ1)PPP=GRENZ1	00041900
	IF(PPP.GT.GRENZ2)PPP=GRENZ2	00042000
C33	PPP=PPAAA(M)	00042100
	IF(N.GE.NUNT.AND.N.LE.NOB)WRITE(6,694)N,M,PPP	00042200
694	FORMAT(' ',2110, 'ZUFALLSZAHL FUER NAECHSTE WW ',F10.5)	00042300
	IF(PPP.LE.PS1)GOTO 45	00042400
	IF(PPP.LE.PS2)GOTO 46	00042500
	IF(PPP.LE.PS3)GOTO 47	00042600
	NCAP(M)=NCAP(M)+1	00042700
	KCC=1	00042800
	MMM=M	00042900
	IF(N.GE.NUNT.AND.N.LE.NOB)WRITE(6,695)N,M	00043000
695	FORMAT(' ',2110,' NEUTRON EINGEFANGEN ')	00043100
, -	GOTO 1111	00043200
45	AAA=AA1	00043300
1.0	GOTO 2222	00043400
46	AAA=AA2	00043500
	GOTO 2222	00043600
	AAA=AA3	00043700
	CONTINUE	00043800
C	LIEG DEG MANAGONG TON DESIDENT DISTRIBUTE DI	00043900
C	WEG DES NEUTRONS IST BEENDET ENTWEDER ENTKOMMEN ODER EINGEFANGEN	00044000
C	TR/W RO 400 VPT TR / C COCV	00044100
	IF(M.EQ.100)WRITE(6,686)N	00044200
000	FORMAT(' NEUTRON MIT FOLGENDER NUMMER BLEIBT IM KRISTALL ',110)	00044300
	IF(N.LT.NUNT.OR.N.GT.NOB)GOTO 51	00044400
(00	WRITE(6,683)	00044500
663	FORMAT(' E(M), XX(M), YY(M), ZZ(M), TT(M), SS(M), TETA(M), PHI(M), R(M)')	00044600
	DO 50 K=1,M	00044700
	WRITE $(6,684)$ E(K), XX(K), YY(K), ZZ(K), TT(K), SS(K), STETA(K), SPHI(K),	00044800
	IR(K)	00044900
	FORMAT(10F10.4)	00045000
50	CONTINUE LEGAL ATT. AND THE CO. CO.C.	00045100
606	IF(M.LT.NWRITE)WRITE(6,696)	00045200
	FORMAT(' '///)	00045300
2.1	ITIME=TT(M)/10.	00045400
	ITIME=ITIME+1	00045500

```
IF(ITIME.GT.200)ITIME=200
                                                                            00045600
      IENER=100.*E(M)/ENO
                                                                            00045700
      IENER=IENER+1
                                                                            00045800
      IF (IENER.GT.100) IENER=100
                                                                            00045900
      IF(KCC.EQ.1)GOTO 55
                                                                            00046000
      IF(KKK.EQ.1)GOTO 56
                                                                            00046100
      NNN=NNN+1
                                                                            00046200
      GOTO 1000
                                                                            00046300
   55 NTIMEC(ITIME)=NTIMEC(ITIME)+1
                                                                            00046400
      NENCAP(IENER)=NENCAP(IENER)+1
                                                                            00046500
C.... IF(ITIME.LT.20)WRITE(6,651)N,M,ITIME,TT(M),E(M),R(M)
                                                                            00046510
C.651 FORMAT(' NEUTRON EINGEFANGEN N,M,ITIME,TT,E,R ',3I10,3F10.5)
                                                                            00046520
      GOTO 1000
                                                                            00046600
   56 NTIMEO(ITIME)=NTIMEO(ITIME)+1
                                                                            00046700
      NENOUT(IENER)=NENOUT(IENER)+1
                                                                            00046800
C1000 WRITE(6,697)N,M,KKK,KCC,KPP
697 FORMAT('N,M,KKK,KCC,KPP',5110)
                                                                            00046900
                                                                            00047000
 1000 CONTINUE
                                                                            00047100
      WRITE(6,703)
                                                                            00047200
  703 FORMAT('1'/)
                                                                            00047300
      WRITE(6,690)
                                                                            00047400
                                                                            00047500
      WRITE(6,691)
  690 FORMAT('
                               RAUSGESTREUTE NEUTRONEN
                                                                          EI00047600
     1NGEFANGENE NEUTRONEN
                                              NEUTRONEN DIE PROBE TREFFEN 00047700
     2 '/)
                                                                            00047800
  691 FORMAT('
                     KANAL
                              ANZAHL
                                        ENERGIE
                                                               ZEIT2
                                                                         ANZ00047900
                                                     ZETT1
     1AHL
           ENERGIE
                                                                            00048000
                         ZEIT1
                                   ZEIT2
                                             ANZAHL
                                                      ENERGIE
                                                                   ZEIT1
       ZEIT2 '/)
                                                                            00048100
      DO 59 KK1=1,10
                                                                            00048200
      DO 60 KK2=1,10
                                                                            00048300
      K = (KK1-1)*10+KK2
                                                                            00048400
      WRITE(6,692)K, NOUT(K), NENOUT(K), NTIMEO(K), NTIMEO(100+K), NCAP(K),
                                                                            00048500
     1NENCAP(K), NTIMEC(K), NTIMEC(100+K), NIN(K), NENIN(K), NTIMEI(K),
                                                                            00048600
     2NTIMEI(100+K)
                                                                            00048700
                                                                            00048800
   60 CONTINUE
  692 FORMAT(' ',13I10)
                                                                            00048900
      WRITE(6,699)
                                                                            00049000
  699 FORMAT( ' ')
                                                                            00049100
   59 CONTINUE
                                                                            00049200
      WRITE(6,700)
                                                                            00049300
  700 FORMAT(/' GEMITTELTE ERGEBNISSE UEBER 10 KANAELE
                                                                            00049400
      DO 63 KK1=1,10
                                                                            00049500
      DO 63 KK2=1,12
                                                                            00049600
   63 IFELD(KK1,KK2)=0
                                                                            00049700
      DO 61 KK1=1,10
                                                                            00049800
      DO 62 KK2=1.10
                                                                            00049900
      K = (KK1-1)*10+KK2
                                                                            00050000
      IFELD(KK1,1)=IFELD(KK1,1)+NOUT(K)
                                                                            00050100
      IFELD(KK1,2)=IFELD(KK1,2)+NENOUT(K)
                                                                            00050200
      IFELD(KK1,3)=IFELD(KK1,3)+NTIMEO(K)
                                                                            00050300
      IFELD(KK1,4)=IFELD(KK1,4)+NTIMEO(100+K)
                                                                            00050400
      IFELD(KK1,5)=IFELD(KK1,5)+NCAP(K)
                                                                            00050500
      IFELD(KK1,6)=IFELD(KK1,6)+NENCAP(K)
                                                                            00050600
      IFELD(KK1,7)=IFELD(KK1,7)+NTIMEC(K)
                                                                            00050700
      IFELD(KK1,8)=IFELD(KK1,8)+NTIMEC(100+K)
                                                                            00050800
      IFELD(KK1,9)=IFELD(KK1,9)+NIN(K)
                                                                            00050900
```

```
IFELD(KK1,10)=IFELD(KK1,10)+NENIN(K)
                                                                           00051000
     IFELD(KK1,11)=IFELD(KK1,11)+NTIMEI(K)
                                                                           00051100
     IFELD(KK1,12)=IFELD(KK1,12)+NTIMEI(100+K)
                                                                           00051200
  62 CONTINUE
                                                                           00051300
     WRITE(6,692)KK1, (IFELD(KK1,J), J=1,12)
                                                                           00051400
  61 CONTINUE
                                                                           00051500
     DO 64 I=1,12
                                                                           00051510
     DO 64 \text{ K}=2.10
                                                                           00051520
  64 IFELD(1,I)=IFELD(1,I)+IFELD(K,I)
                                                                           00051530
                                                                           00051540
     WRITE(6,701)
                                                                           00051550
 701 FORMAT(/' TOTALE SUMMEN'/)
                                                                           00051560
     WRITE(6,692)K, (IFELD(1,I), I=1,12)
                                                                           00051570
     WRITE (6,693)NNN
                                                                           00051580
 693 FORMAT(/' NEUTRONEN IN DER PROBE STEKENGEBL. ',110)
                                                                           00051600
     AMIOUT=0.
                                                                           00051610
     AMICAP=0.
                                                                           00051620
     AMIIN=0.
                                                                           00051630
     DO 65 K=1,100
                                                                           00051640
     AMIOUT=AMIOUT+FLOAT(K*NOUT(K))
                                                                           00051650
     AMICAP=AMICAP+FLOAT(K*NCAP(K))
                                                                           00051660
     AMIIN=AMIIN+FLOAT(K*NIN(K))
                                                                           00051670
  65 CONTINUE
                                                                           00051680
     AMIOUT=AMIOUT/FLOAT(IFELD(1,1))
                                                                           00051690
     AMICAP=AMICAP/FLOAT(IFELD(1,5))
                                                                           00051691
     AMIIN=AMIIN/FLOAT(IFELD(1,9))
                                                                           00051692
     WRITE (6,702) AMIOUT, AMICAP, AMIIN
                                                                           00051693
 702 FORMAT(/' MITTLERE ANZAHL DER WW, MIOUT, MICAP, MIIN: ',3F10.5)
                                                                           00051694
     DO112 K=1,100
                                                                           00051695
     MENOUT(L,K)=NENOUT(K)
                                                                           00051696
     MENCAP(L,K)=NENCAP(K)
                                                                           00051697
                                                                           00051698
     MTIMEO(L,K)=NTIMEO(K)
     MTIMEC(L,K)=NTIMEC(K)
                                                                           00051699
     MTIMEO(L, 100+K) = NTIMEO(100+K)
                                                                           00051700
     MTIMEC(L, 100+K) = NTIMEC(100+K)
                                                                           00051701
 112 CONTINUE
                                                                           00051702
4444 CONTINUE
                                                                           00051703
                                                                           00051704
     BERECHNUNG DES TOF SPEKTRUMS DES EFFEKT
                                                                           00051705
                                                                           00051706
     DO113 K=1, NENER
                                                                           00051707
     TIMELO(K)=TTT*FLUGW/SQRT(ELOWER(K))
                                                                           00051708
     TIMEUP(K)=TTT*FLUGW/SQRT(EUPPER(K))
                                                                           00051709
 113 CONTINUE
                                                                           00051710
     DO114 K=1, NENER
                                                                           00051711
     KK1=TIMEUP(K)/10.
                                                                           00051712
     KK1=KK1+1
                                                                           00051713
                                                                           00051714
     KK2=TIMELO(K)/10.
     IF(KK2.LT.KK1)KK2=KK1
                                                                           00051715
     AFLUSS=FLUSS(K)*SIGMAG(K)/FLOAT(KK2-KK1+1)
                                                                           00051716
     AFLUSS=AFLUSS*(EUPPER(K)-ELOWER(K))/10.
                                                                           00051717
     DO 115 I=KK1,KK2
                                                                           00051718
     IF(I.GT.200)J=I-200
                                                                           00051719
     J=I
                                                                           00051720
     EFFEKT(J)=EFFEKT(J)+AFLUSS
                                                                           00051721
 115 CONTINUE
                                                                           00051722
```

С

С

C

	114	CONTINUE					00051723
C				<i>2.</i>			00051724
C		BERECHNUNG DER ZEITV			GERREIGNISS	SE	00051725
C		UND NEUTRONEN DIE DI	E KUGEL VEI	RLASSEN			00051726
С					•		00051727
		DO117 K=1, NENER					00051728
		TMIT=(TIMEUP(K)+TIME	LO(K))/2.		•		00051729
		ITMIT=TMIT/10.					00051730
		ITMIT=ITMIT+1	ACI (IZ \ LED A IZM	ND (W) (DT 0 A)	n (NDKIMD a)		00051731
		FLNORM=FLUSS(K)*SIGM FLNORM=FLNORM*(EUPPE			r(NEUTRS)		00051732
		DO 118 I=1,199	K(K)-ELOWEI	(K))/10.			00051733
		J=I+ITMIT		•			00051734 00051735
		IF(J.GT.200)J=J-200					00051735
		UNTCAP(J)=UNTCAP(J)+	FT.በልጥ (Mጥ T MT	CCK III%E	I.NIORM		00051737
		UNTOUT(J)=UNTOUT(J)+					00051737
	118	CONTINUE	1 110111 (111 1111	10 (R,1)) 1.	ычонн		00051738
C		,					00051740
C		UNTERGRUND MIT MEHR	ALS 2 MICRO	OSEC WIRD	ALS KONSTAN	NNTE ADDIER	
C							00051742
		UNTCO1=FLOAT(MTIMEC(K,200))*FLN	NORM			00051743
		UNTCO2=FLOAT(MTIMEO(00051744
		UNTCO1=UNTCO1/200.					00051745
		UNTCO2=UNTCO2/200.					00051746
		DO119 I=1,200					00051747
		UNTCAP(I)=UNTCAP(I)+					00051748
		UNTOUT(I)=UNTOUT(I)+	UNTCO2				00051749
		CONTINUE					00051750
~	11/	CONTINUE					00051751
C		DEDECHMING DED ENEDG	TEUEDODETTIK	IG DED NEU	EDONEN GAD	IND OUR	00051752
C		BERECHNUNG DER ENERG	TEAEKIEIPOL	NG DEK NEU	IKUNEN CAP	UND UU1	00051753 00051754
		DO 120 K=1,NENER					00051754
		FLNORM=FLUSS(K)*SIGM	AG(K)*FAKT(OR (K) /FLOA	r(NEUTRS)		00051756
		FLNORM=FLNORM*(EUPPE			(1,201110)		00051757
		EMIT=(ELOWER(K)+EUPP		. ,,,,			00051758
		DO 121 I=1,100	`				00051759
		EEE=EMIT*FLOAT(I)/10	0EMIT/200).			00051760
		IEEE=EEE/O.1					00051761
		IEEE=IEEE+1					00051762
		IF(IEEE.GT.1000)IEEE					00051763
		ENECAP(IEEE)=ENECAP(•	•	, , ,		00051764
		ENEOUT(IEEE)=ENEOUT(IEEE)+FLOAT	T(MENOUT(K	,I))*FLNORN	1	00051765
		CONTINUE					00051766
	120	CONTINUE					00051767
		DO 125 K=1,200					00051768
		I=(K-1)*5+1 ENECAP(K)=ENECAP(I)+	ENTECAD (T.1.1)	LENECADAT	I O NIENTECATA	(TIS) IENTECA	00051769
		L)	ENECAP (ITI,	TENECAP (I	TZ)TENECAP	(IT3)TENEUA	00051771
		ENEOUT(K)=ENEOUT(I)+	ENEOUT(T+1)	+ENEOUT(I-	+2)+ENEOUT	(T+3)+ENEOU	
		1)				(2.0).2.1200	00051773
		CONTINUE					00051774
		WRITE(6,703)					00051775
		WRITE(6,417)					00051776
		FORMAT(' KANAL	EFFEKT	UNTCAP	UNTOUT	ENECAP	ENE00051777
		LOUT '/)					00051778

```
DO 123 KK1=1,20
                                                                           00051779
    DO 126 KK2=1,10
                                                                           00051780
    K = (KK1-1)*10+KK2
                                                                          00051781
    WRITE(6,416)K, EFFEKT(K), UNTCAP(K), UNTOUT(K), ENECAP(K), ENEOUT(K)
                                                                          00051782
126 CONTINUE
                                                                           00051783
    WRITE(6,699)
                                                                          00051784
123 CONTINUE
                                                                           00051785
    DO 127 KK1=1,20
                                                                           00051786
    DO 127 KK2=1,5
                                                                          00051787
127 OFELD(KK1,KK2)=0.
                                                                          00051788
    WRITE (6,700)
                                                                          00051789
    DO 128 KK1=1,20
                                                                          00051790
    DO 129 KK2=1,10
                                                                          00051791
    K = (KK1-1)*10+KK2
                                                                          00051792
    OFELD(KK1,1)=OFELD(KK1,1)+EFFEKT(K)
                                                                          00051793
    OFELD(KK1,2)=OFELD(KK1,2)+UNTCAP(K)
                                                                          00051794
    OFELD(KK1,3)=OFELD(KK1,3)+UNTOUT(K)
                                                                          00051795
    OFELD(KK1,4)=OFELD(KK1,4)+ENECAP(K)
                                                                          00051796
    OFELD(KK1,5) = OFELD(KK1,5) + ENEOUT(K)
                                                                          00051797
129 CONTINUE
                                                                          00051798
    WRITE(6,416)KK1,(OFELD(KK1,J),J=1,5)
                                                                          00051799
128 CONTINUE
                                                                          00051800
    DO 130 I=1.5
                                                                          00051801
    DO 130 K=2,20
                                                                          00051802
    OFELD(1,I)=OFELD(1,I)+OFELD(K,I)
                                                                          00051803
130 CONTINUE
                                                                          00051804
    K=1
                                                                          00051805
    WRITE(6,701)
                                                                          00051806
WRITE(6,416)K,(OFELD(1,I),I=1,5)
416 FORMAT(' ',I10,5F10.3)
                                                                          00051807
                                                                          00051808
    DO 131 K=1,200
                                                                          00051809
    XXX(K)=FLOAT(K)
                                                                          00051810
131 CONTINUE
                                                                          00051811
    DO 132 K=1,200
                                                                          00051812
    EFFEKT(K)=EFFEKT(K)+UNTCAP(K)
                                                                          00051813
132 CONTINUE
                                                                          00051814
    CALL PLOTS(IBUF, 8000,1)
                                                                          00051815
    CALL PLOT(1.,1.,-3)
                                                                          00051816
    CALL PLOT2(200.,0.,9,1,XXX,1.,200.,10.,0.,200.,EFFEKT,5.,0.,100.,Y00051817
   1YY, YYY, 0
    CALL PLOT2(200.,0.,9,1,XXX,1.,200.,10.,0.,200.,UNTCAP,5.,0.,100.,Y00051819
   1YY, YYY, 0
                                                                          00051820
                                                                           00051821
    CALL SYMBOL(4.,4.,0.25,17HEFFEKT+UNTERGRUND,0.,17)
    CALL PLOT(0.,6.,-3)
                                                                          00051822
    CALL PLOT2(200.,0.,9,1,XXX,1.,200.,10.,0.,200.,UNTCAP,5.,0.,100.,Y00051823
   1YY, YYY, 0)
                                                                           00051824
    CALL SYMBOL(4.,4.,0.25,6HUNTCAP,0.,6)
                                                                          00051825
    CALL PLOT(0.,6.,-3)
                                                                          00051826
    CALL PLOT2(200.,0.,9,1,XXX,1.,200.,10.,0.,200.,UNTOUT,5.,0.,200.,Y00051827
   1YY, YYY, 0)
                                                                           00051828
    CALL SYMBOL(4.,4.,0.25,6HUNTOUT,0.,6)
                                                                           00051829
    IF(AA1.EQ.137)CALL SYMBOL(4.,6.,0.25,3HBAF,0.,3)
                                                                           00051830
    IF(AA1.EQ.209)CALL SYMBOL(4.,6.,0.25,3HBGO,0.,3)
                                                                           00051831
    CALL NUMBER(4.,5.5,0.25,RIN,0.,1)
                                                                           00051832
    CALL NUMBER(6.,5.5,0.25,ROUT,0.,1)
                                                                           00051833
    CALL PLOT(11.,-12.,-3)
                                                                           00051834
```

```
DO 133 K=1,100
                                                                            00051835
      I=(K-1)*2+1
                                                                            00051836
      ENECAP(K) = ENECAP(I) + ENECAP(I+1)
                                                                            00051837
      ENEOUT(K)=ENEOUT(I)+ENEOUT(I+1)
                                                                            00051838
  133 CONTINUE
                                                                            00051839
      CALL PLOT2(200.,0.,9,1,XXX,1.,100.,10.,0.,100.,ENECAP,5.,0.,200.,Y00051840
     1YY, YYY, 0
                                                                            00051841
      CALL SYMBOL(4.,4.,0.25,6HENECAP,0.,6)
                                                                            00051842
      CALL PLOT(0.,6.,-3)
                                                                            00051843
      CALL PLOT2(200.,0.,9,1,XXX,1.,100.,10.,0.,100.,ENEOUT,5.,0.,400.,Y00051844
      CALL SYMBOL(4.,4.,0.25,6HENEOUT,0.,6)
                                                                            00051846
      DO 136 K=1,100
                                                                            00051847
      ENEIN(K)=0.
                                                                            00051848
  136 CONTINUE
                                                                            00051849
      DO 134 K=1, NENER
                                                                            00051850
      KK1=ELOWER(K)
                                                                            00051851
      KK2=EUPPER(K)
                                                                            00051852
      KK2=KK2-1
                                                                            00051853
      DO 135 I=KK1,KK2
                                                                            00051854
      ENEIN(I)=FLUSS(K)
                                                                            00051855
  135 CONTINUE
                                                                            00051856
  134 CONTINUE
                                                                            00051857
      CALL PLOT(0.,6.,-3)
                                                                            00051858
      CALL PLOT2(200.,0.,9,1,XXX,1.,100.,10.,0.,100.,ENEIN,5.,0.,100.,Y 00051859
                                                                            00051860
      CALL SYMBOL(4.,4.,0.25,5HENEIN,0.,5)
                                                                            00051861
      CALL PLOT(0.,0.,999)
                                                                            00051862
  999 STOP
                                                                            00051863
      END
                                                                            00051870
      SUBROUTINE CMLAB (EN, THETA, AAA)
                                                                            00051900
C
                                                                            00052000
С
          INPUT:
                    NEUTRON ENERGY
                                                                            00052100
С
                     STREUWINKLE IN CENTER OF MASS FRAME
                                                                            00052200
С
          OUTPUT : ENERGY & ANGLE , IN LAB. FRAME
                                                                            00052300
C
                                                                            00052400
      COMMON NUNT, NOB, N, M, IY, DENSTY, ESIG, SIGC, SIGN, AI1, AI2, AI3
                                                                            00052500
      DIMENSION ESIG(3,100)
                                                                            00052600
      CTHETA=COS (THETA)
                                                                            00052700
      A1A1=AAA**2+2.*AAA*CTHETA+1.
                                                                            00052800
      IF (AAA.EQ.1..AND.A1A1.EQ.0.) TETLAB=1.5708
                                                                            00052810
      IF(AAA.EQ.1..AND.A1A1.EQ.0.)GOTO 2
                                                                            00052820
      CTHLAB=(AAA*CTHETA+1.)/SQRT(A1A1)
                                                                            00052900
      TETLAB=ACOS (CTHLAB)
                                                                            00053000
    2 ENNEU=EN*A1A1/(AAA+1.)**2
                                                                            00053100
      IF (ENNEU.LE.ESIG(1,1).AND.EN.GT.ESIG(1,1)) WRITE (6,601)N,M
                                                                            00053200
  601 FORMAT(' NEUTRONENERGIE AN UNTERER GRENZE N,M ',2110)
                                                                            00053300
      IF(ENNEU.LE.ESIG(1,1))ENNEU=ESIG(1,1)
                                                                            00053400
      IF (N.GE.NUNT.AND.N.LE.NOB) WRITE (6,600) N.M. THETA, TETLAB, EN, ENNEU,
                                                                            00053500
                                                                            00053510
  600 FORMAT(216, 'CMLAB: TETA-CM, TETA-LAB, EIN, EOUT, AAA', 5F10.3/)
                                                                            00053600
      THETA=TETLAB
                                                                            00053700
      EN=ENNEU
                                                                            00053800
      RETURN
                                                                            00053900
                                                                            00054000
      SUBROUTINE EULER(XIN, YIN, ZIN, RMATRX, R, THETA, PHI, XOUT, YOUT, ZOUT,
                                                                            00054100
```

```
2R2SQR)
                                                                            00054200
      COMMON NUNT, NOB, N, M, IY, DENSTY, ESIG, SIGC, SIGN, A11, A12, A13
                                                                            00054300
      DIMENSION RMATRX(3,3),RR(3,3),EUL(3,3)
                                                                            00054400
С
                  XYZ IN ROTATED FRAME
                                                                            00054500
      X=R*SIN(THETA)*COS(PHI)
                                                                            00054600
      Y=R*SIN(THETA)*SIN(PHI)
                                                                            00054700
      Z=R*COS (THETA)
                                                                            00054800
C
                   XYZ IN LAB. FRAME
                                                                            00054900
      XOUT=XIN+X*RMATRX(1,1)+Y*RMATRX(1,2)+Z*RMATRX(1,3)
                                                                           00055000
      YOUT=YIN+X*RMATRX(2,1)+Y*RMATRX(2,2)+Z*RMATRX(2,3)
                                                                            00055100
      ZOUT=ZIN+X*RMATRX(3,1)+Y*RMATRX(3,2)+Z*RMATRX(3,3)
                                                                           00055200
      R2SQR=XOUT**2+YOUT**2+ZOUT**2
                                                                            00055300
C... IF (M.LT.NWRITE) WRITE (6,600) N, M, XIN, YIN, ZIN, R, THETA, PHI, XOUT, YOUT, 00055400
C... 2ZOUT, R2SQR
                                                                            00055500
C.600 FORMAT(216, 'EULER: XYZ-IN S2 TETAFI-IN XYZ-OUT R2'/10F10.3/) 00055600
          ROTATION MATRIX FOR THE INPUT THETA-PHI VALUES
                                                                           00055700
      EUL(1,1)=COS(THETA)*COS(PHI)
                                                                            00055800
      EUL(1,2) = -SIN(PHI)
                                                                            00055900
      EUL(1,3)=SIN(THETA)*COS(PHI)
                                                                            00056000
      EUL(2,1)=COS(THETA)*SIN(PHI)
                                                                            00056100
      EUL(2,2)=COS(PHI)
                                                                            00056200
      EUL(2,3)=SIN(THETA)*SIN(PHI)
                                                                            00056300
      EUL(3,1) = -SIN(THETA)
                                                                            00056400
      EUL(3,2)=0.
                                                                           00056500
      EUL(3,3) = COS(THETA)
                                                                            00056600
      IF(M.LT.NWRITE)WRITE(6,611)RMATRX,EUL
                                                                            00056700
C.611 FORMAT(2X, 'RMATRX-IN , EUL(TETA,FI)'/9F7.2/9F7.2/)
                                                                           00056800
         ---- ROTATION MATRIX OF THE NEW FRAME ----
                                                                           00056900
      DO 10 I=1,3
                                                                           00057000
      DO 10 J=1,3
                                                                           00057100
   10 RR(I,J)=0.
                                                                            00057200
      DO 100 I=1,3
                                                                           00057300
      DO 100 J=1,3
                                                                           00057400
      DO 100 K=1,3
                                                                           00057500
  100 RR(I,J)=RR(I,J)+RMATRX(I,K)*EUL(K,J)
                                                                           00057600
      DO 11 I=1,3
                                                                           00057700
      DO 11 J=1,3
                                                                           00057800
   11 RMATRX(I,J)=RR(I,J)
                                                                           00057900
С
           THETA-PHI OF NEW Z-AXIS , IN THE LAB. FRAME
                                                                            00058000
      THETA=ARCOS(RMATRX(3,3))
                                                                           00058100
C
      PHI=ARCOS(RMATRX(2,2))
                                                                           00058200
      IF(RMATRX(1,2).GT.0.)PHI=2.*3.1416-PHI
                                                                           00058300
      XZUNIT=RMATRX(1,3)
                                                                            00058400
      YZUNIT=RMATRX(2,3)
                                                                           00058500
      IF(XZUNIT.EQ.0.)PHI=1.5708
                                                                           00058510
      IF(XZUNIT.EQ.0.)GOTO 12
                                                                           00058520
      PHI=ATAN(YZUNIT/XZUNIT)
                                                                           00058600
   12 IF(XZUNIT.LT.O.)PHI=PHI+3.1416
                                                                           00058700
C.612 FORMAT(' RMATRX-OUT TETA, FI-OUT'/2X, 9F10.2/2F10.3/)
                                                                           00058800
      IF (M.LT.NWRITE) WRITE (6,612) RMATRX, THETA, PHI
                                                                           00058900
      RETURN
                                                                           00059000
      END
                                                                            00059100
      SUBROUTINE B10H14(EN, SIGDEN, PPS1, PPS2, PPS3)
                                                                            00059200
C
                                                                            00059300
C
   INPUT: N-ENERGY (EN)
                                                                            00059400
C
   OUTPUT: AVERAGE FREE PATH SIGDEN
                                                                           00059500
           PROBABILITY OF SCATTERING WITH NUCLEUS 1 PPS1
                                                                           00059600
```

```
C
                                      WITH NUCLEUS 1+2
                                                          PPS2
                                                                           00059700
C
                                      WITH NUCLEUS 1+2+3 PPS3
                                                                           00059800
C
                        OF CAPTURE
                                      1-PPS3
                                                                           00059900
C
                                                                           00060000
      COMMON NUNT, NOB, N, M, IY, DENSTY, ESIG, SIGC, SIGN; AI1, AI2, AI3
                                                                           00060100
      DIMENSION ESIG(3,100), SIGC(3,100), SIGN(3,100), SIGC1(3), SIGN1(3)
                                                                           00060200
      DO 1 K=1,3
                                                                           00060300
      SIGC1(K)=0.
                                                                           00060400
      SIGN1(K)=0.
                                                                           00060500
    1 CONTINUE
                                                                           00060600
      II=3
                                                                           00060700
      IF(SIGN(3,1).EQ.0.)II=2
                                                                           00060800
      IF(SIGN(2,1).EQ.0.)II=1
                                                                           00060900
C
                                                                           00061000
C
      LINEARE INTERPOLATION DER STREU UND EINFANGQUERSCHNITTE
                                                                           00061100
C
                                                                           00061200
      DO 5 I=1,II
                                                                           00061300
      D0 6 K=1,99
                                                                           00061400
      IF(EN.LE.ESIG(I,K+1).AND.EN.GE.ESIG(I,K))GOTO 2
                                                                           00061500
      IF(K.EQ.99)WRITE(6,608)EN
                                                                           00061600
  608 FORMAT(' NEUTRONENERGIE NICHT IM BEREICH DER STUETZST. ',F10.5) 00061700
    6 CONTINUE
                                                                           00061800
    2 SIGC1(I)=SIGC(I,K)+(EN-ESIG(I,K))*(SIGC(I,K+1)-SIGC(I,K))/
                                                                           00061900
     1(ESIG(I,K+1)-ESIG(I,K))
                                                                           00062000
      SIGN1(I)=SIGN(I,K)+(EN-ESIG(I,K))*(SIGN(I,K+1)-SIGN(I,K))/
                                                                           00062100
     1(ESIG(I,K+1)-ESIG(I,K))
                                                                           00062200
      IF(N.GE.NUNT.AND.N.LE.NOB)WRITE(6,605)EN,SIGC1(I),SIGN1(I)
                                                                           00062300
  605 FORMAT(' INTERPOLIERTER QUERSCHNITT PRO ATOM ',3F10.5)
                                                                           00062400
    5 CONTINUE
                                                                           00062500
C
                                                                           00062600
С
      GESAMMTQUERSCHNITTE PRO MOLEKUEL CAPTURE, STREUUNG, TOTAL
                                                                           00062700
C
                                                                           00062800
      SIGCTO=AI1*SIGC1(1)+AI2*SIGC1(2)+AI3*SIGC1(3)
                                                                           00062900
      SIGNTO=AI1*SIGN1(1)+AI2*SIGN1(2)+AI3*SIGN1(3)
                                                                           00063000
      SIGTTO=SIGCTO+SIGNTO
                                                                           00063100
      PPS1=AI1*SIGN1(1)/SIGTTO
                                                                           00063200
      PPS2=(AI1*SIGN1(1)+AI2*SIGN1(2))/SIGTTO
                                                                           00063300
      PPS3=(AI1*SIGN1(1)+AI2*SIGN1(2)+AI3*SIGN1(3))/SIGTTO
                                                                           00063400
      IF(N.GE.NUNT.AND.N.LE.NOB)WRITE(6,606)SIGCTO,SIGNTO,SIGTTO
                                                                           00063500
  606 FORMAT(' TOTALE QUERSCHNITTE JE MOLEKUEL, CAPT, SCATT, TOTAL ', 3F10.400063600
                                                                           00063700
      SIGTTO=SIGTTO*1.E-24
                                                                           00063800
      SIGDEN=1./(DENSTY*SIGTTO)
                                                                           00063900
      IF (N.GE.NUNT.AND.N.LE.NOB) WRITE (6,607) SIGDEN
                                                                           00064000
  607 FORMAT(' FREIE WEGLAENGE ',F10.5)
                                                                           00064100
      RETURN
                                                                           00064200
      END
                                                                           00064300
      SUBROUTINE RPOLAR(XIN, YIN, ZIN, R, THETA, PHI, XOUT, YOUT, ZOUT, R2SQR)
                                                                           00064400
C GANZ DUMM : ROUT=RIN+(R,TETA,FI)
                                                                           00064500
      XOUT=R*SIN(THETA)*COS(PHI)+XIN
                                                                           00064600
      YOUT=R*SIN(THETA)*SIN(PHI)+YIN
                                                                           00064700
      ZOUT=R*COS(THETA)+ZIN
                                                                           00064800
      R2SQR=XOUT*XOUT+YOUT*YOUT+ZOUT*ZOUT
                                                                           00064900
      RETURN
                                                                           00065000
      END
                                                                           00065100
      FUNCTION RANDOM(ANY)
                                                                           00065200
   GENERATING RANDON NO. IN (O. BIS 1.) INTERVAL
                                                                           00065300
   INPUT ANY "ANY" VALUE, IT WILL BE IGNORED ANYWAY
                                                                           00065400
```

COMMON NUNT, NOB, N, M, IY, DENSTY, ESIG, SIGC, SIGN, AI1, AI2, AI3	00065500
IX=IY	00065600
CALL RANDU(IX, IY, RA)	00065700
RANDOM=RA	00065800
RETURN	00065900
END	00066000

APPENDIX B Tables of coordinates for a spherical shell of 12 pentagons and 30 hexagons

Table B.1 Midpoints of all hexagons and pentagons forming a sphere with 430 mm radius in Cartesian and polar coordinates.

Number	Туре	X	Υ	Z	δ	φ
1	Р	0	0	430.000	0	0
2	Н	132.877	182.890	365.780	54.000	31.717
3	Н	215.000	-69.858	365.780	342.000	31.717
4	Н	0	-226.064	365.780	270.000	31.717
5	Н	-215.000	-69.859	365.780	198.000	31.717
6	Н	-132.877	182.890	365.780	126.000	31.717
7	Н	0	365.780	226.064	90.000	58.283
8	Р	226.064	311.151	192.302	54.000	63.435
9	Н	347.877	113.032	226.064	18.000	58.283
10	Р	365.780	-118.849	192.302	342.000	63.435
11	Н	215.000	-295.922	226.064	306.000	58.283
12	Р	0	-384.604	192.302	270.000	63.435
13	Н	-215.000	-295.922	226.064	234.000	58.283
14	Р	-365.780	-118.849	192.302	198.000	63.435
15	Н	-347.877	113.032	226.064	162.000	58.283
16	Р	-226.064	311.151	192.302	126.000	63.435
17	Н	132.877	408.954	0	72.000	90.000
18	Н	347.877	252.748	0	36.000	90.000
19	Н	430.000	0	0	0	90.000
20	Н	347.877	-252.748	0	324.000	90.000
21	H	132.877	-408.954	0	288.000	90.000
22	Н	-132.877	-408.954	0	252.000	90.000
23	Н	-347.877	-252.748	0	216.000	90.000
24	Н	-430.000	0	0	180.000	90.000
25	Н	-347.877	252.748	0	144.000	90.000
26	Η.	-132.877	408.954	0	108.000	90.000
27	Р	0	384.604	-192.302	90.000	116.565

Number	Туре	X	Υ	Z	8	φ
28	Н	215.000	295.922	-226.064	54.000	121.717
29	Р	365.780	118.849	-192.302	18.000	116.565
30	Н	347.877	-113.032	-226.064	342.000	121.717
31	Р	226.064	-311.151	-192.302	306,000	116.565
32	Н	0	-365.780	-226.064	270.000	121.717
33	Р	-226.064	-311.151	-192.302	234.000	116.565
34	Н	-347.877	-113.032	-226.064	198.000	121.717
35	Р	-365.780	118.849	-192.302	162.000	116.565
36	Н	-215.000	295.922	-226.064	126.000	121.717
37	Н	0	226.064	-365.780	90.000	148.283
38	Н	215.000	69.858	-365.780	18.000	148.283
39	Н	132.877	-182.890	-365.780	306.000	148.283
40	Н	-132.877	-182.890	-365.780	234.000	148.283
41	Н	-215.000	69.858	-365.780	162.000	148.283
42	Р	0	0	-430.000	0	180.000

Table B.2 Edges of all hexagons and pentagons forming a sphere of 430 mm diameter, the missing second half of the points is obtained by replacing Y by -Y and Z by -Z or δ by 180+ δ and ϕ by 180- ϕ .

Number	Туре	X	Υ	Z	δ	φ
1	PH	0	148.585	403.513	90.000	20.215
2	PH	141.313	45.915	•	18.000	
3	PH	87.336	-120.208		306.000	
4	PH	-87.336	-120.208		234.000	E000 Promi
5	PH	-141.313	45.915		162.000	20.215
6	HH	0	261.037	341.701	90.000	37.377
7	HH	248.261	80.665	T-107 passa	18.000	
8	HH	153.434	-211.183		306.000	
9	HH	-153.434	-211.183		234.000	

Number	Туре	X	Υ	Z	δ	φ
10	НН	-248.261	80.665	1000 4000 \$	162.000	•
11	PH	109.884	299.828	287.973	69.873	47.956
12	PH	251.199	197.156	-,-	38.127	-,-
13	PH	319.109	-11.852		357.873	-,-
14	PH	265.131	-177.980		326.127	**************************************
15	PH	87.339	-307.154	-,-	285.873	
16	PH	-87.339	-307.154	-,-	254.127	
17	PH	-265.131	-177.980	econo promi	213.873	
18	PH	-319.109	-11.852	Minde wind.	182.127	
19	PH	-251.199	197.156	**************************************	141.873	•
20	PH	-109.882	299.829	Street. Annexis	110.127	Ecolo home
21	PH	109.884	391.659	139.388	74.328	71.085
22	PH	338.534	225.535		33.672	
23	PH	406.446	16.524	Name and	2.328	
24	PH	319.109	-252.271	1000 No.	321.672	esina essua O
25	PH	141.313	-318.447	**************************************	290.328	
26	PH	-141.313	-381.447		249.672	
27	PH	-319.109	-252.271		218.328	
28	PH	-406.446	16.524		177.672	
29	PH	-338.534	225.535	•	146.328	
30	PH	-109.884	391.659		105.672	
31	HH	0	422.366	80.665	90.000	79.188
32	HH	401.694	130.518	****	18.000	Boson Boson
33	НН	248.261	-341.701		306.000	
34	HH	-248.261	-341.701	NOUN MODELS	234.000	•
35	HH	-401.694	130.518	4	162.000	
36	PH	251.197	345.744	47.558	54.000	83.650
37	PH	406.446	-132.062		342.000	
38	PH	0	-427.363		270.000	**************************************
39	PH	-406.446	-132.062	-,-	198.000	Motoral Motoral
40	PH	-251.197	345.744	-,-	126.000	

Table B.3 Midpoints of the edges of all hexagons and pentagons forming a sphere of 430 mm diameter. The remaining half of the points is obtained by replacing Y by -Y and Z by -Z or δ by 180+ δ and ϕ by 180- ϕ .

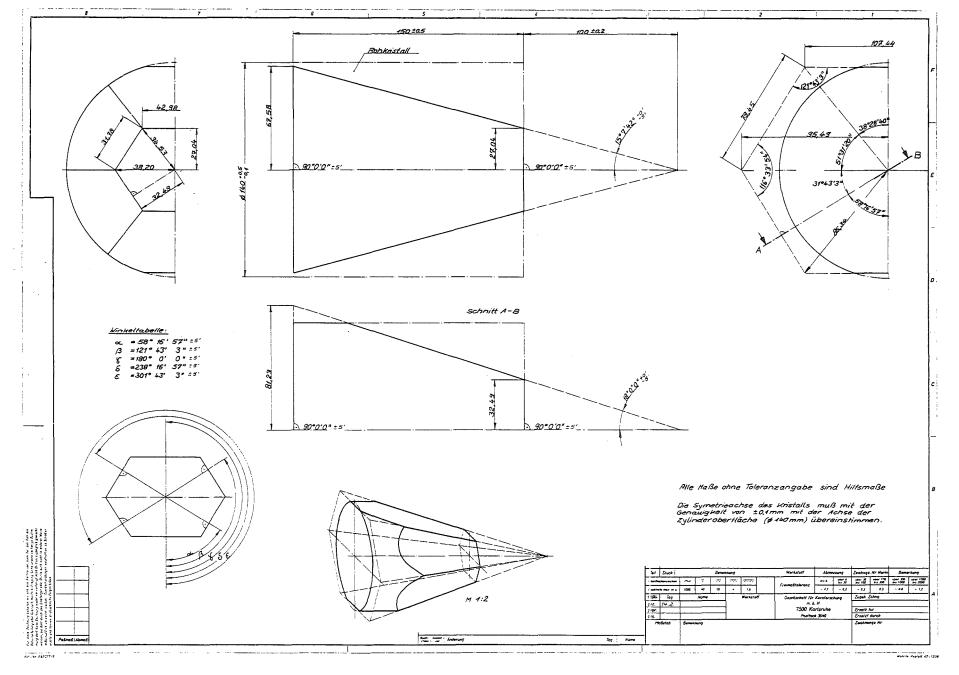
Number	Туре	X	Υ	Z	δ	φ
1	PH	72.161	99.321	412.102	54.000	16.589
2	PH	-116.769	-37.937		198.000	
3	PH	0	-122.768		270.000	
4	PH	116.759	-37.937		342.000	
5	PH	-72.161	99.321	-,-	126.000	
6	HH	0	207.128	376.826	90.000	28.796
7	HH	196.990	64.006		18.000	-,-
8	HH	121.747	-167.570	**************************************	306.000	2000 MOTOR
9	HH	-121.747	-167.570		234.000	• • • • • • • • • • • • • • • • • • •
10	HH	-196.990	64.006		162.000	posso
11	HH	55.565	283.609	318.401	78.915	42.229
12	HH	252.557	140.485		29.085	
13	HH	286,898	34.795		6.915	
14	HH	211.654	-196.784		317.085	, toma
15	HH	121.748	-262.104	-,-	294.915	
16	HH	-121.748	-262.104		245.085	
17	HH	-211.653	-196.784	•	222.915	
18	HH	-286.898	34.795	•	173.085	
19	HH	-252.557	140.485	acces 60000	150.915	
20	HH	-55.565	283.609		101.085	
21	PH	184.383	253.782	294.104	54.000	46.846
22	PH	298.338	-96.936	-,-	342.000	
23	PH	0	-311.692	b	270.000	
24	PH	-298.338	-96.936		198.000	
25	PH	-184.383	253.782		126.000	•
26	PH	112.223	353.103	218.229	72.369	59.502
27	PH	301.143	215.844		35.631	
28	PH	370.500	2.386	-,-	0.369	
29	PH	298.338	-219.705	popes	323.631	

Number	Туре	X	Υ	Z	δ	φ
30	PH	116.760	-351.629	•	288.369	
31	PH	-116.760	-351.629	Minut Nature 6	251.631	Miles Month
32	PH	-298.338	-219.705		216.369	
33	PH	-370.500	2.386		179.631	
34	PH	-301.143	215.844		144.369	
35	PH	-112.221	353.104	6007 600A 6	107.631	•
36	HH	55.563	411.619	111.275	82.312	75.002
37	HH	374.302	180.043	more plant	25.688	60000 600000 8
38	HH	408.643	74.351		10.312	
39	HH	286.897	-300.346		313.688	_,-
40	НН	196.990	-365.667	81000 EFFOR	298.312	
41	HH	-196.990	-365.667	MICHA GALANT	241.688	•
42	HH	-286.897	-300.346	Name Amount	226.312	TOTAL PROPERTY.
43	HH	-408.643	74.351		169.688	•
44	HH	-374.302	180.043	1000 Miles	154.312	
45	HH	-55.565	411.619		97.688	-,-
46	PH	184.259	376.379	96.370	63.916	77.049
47	PH	301.021	291.546	plants proper	44.084	Primit Name B
48	PH	414.897	-58.930		351.916	
49	PH	370.297	-196.195	-,-	332.084	-,-
50	PH	72.164	-412.801	•	279.916	
51	PH	-72.164	-412.801		260.084	
52	PH	-370.297	-196.195		207.916	moves booms
53	PH	-414.897	-58.930	-,-	188.084	
54	PH	-301.021	291.546		135.916	
55	PH	-184.256	376.380		116.084	
56	HH	0	429.674	16.739	90.000	87.769
57	HH	408.644	132.777	NONEY NOMES	18.000	*****
58	HH	252.556	-347.614		306.000	
59	НН	-252.556	-347.614		234.000	Name
60	HH	-408.644	132.777	Prozi Storie •	162.000	

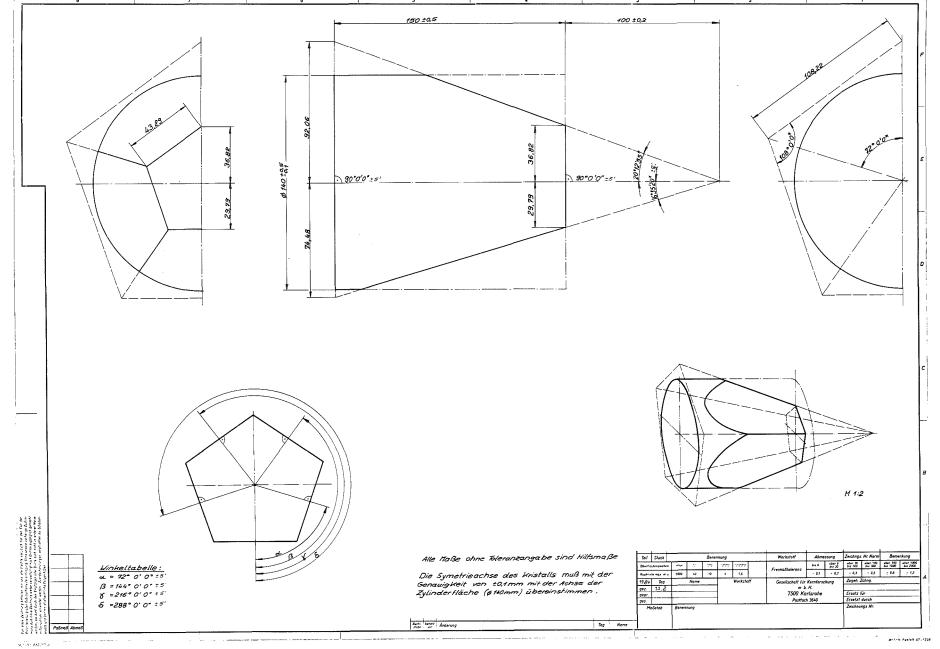
APPENDIX C

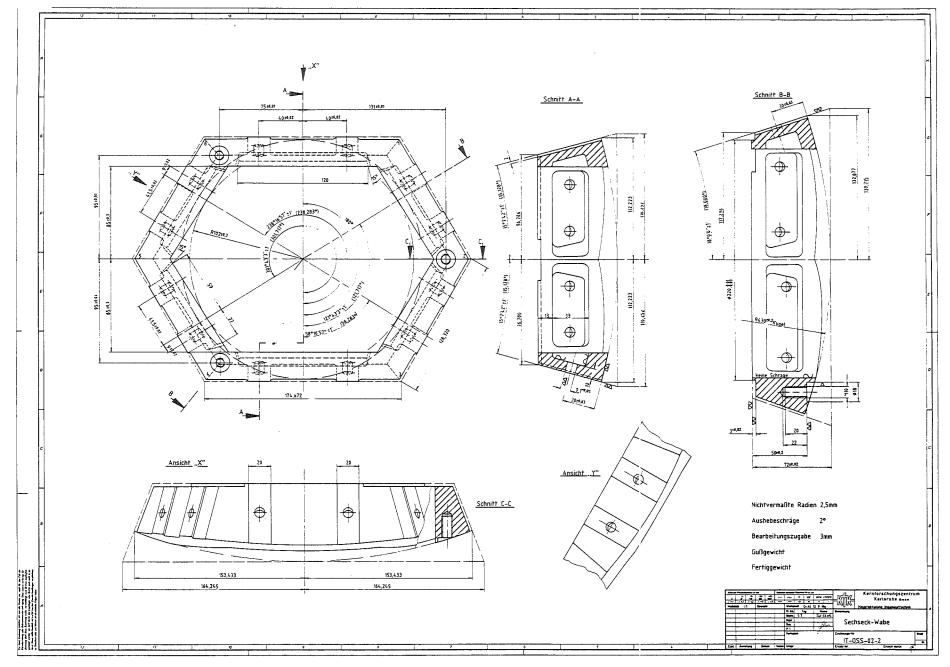
Mechanical construction of the 4π detector

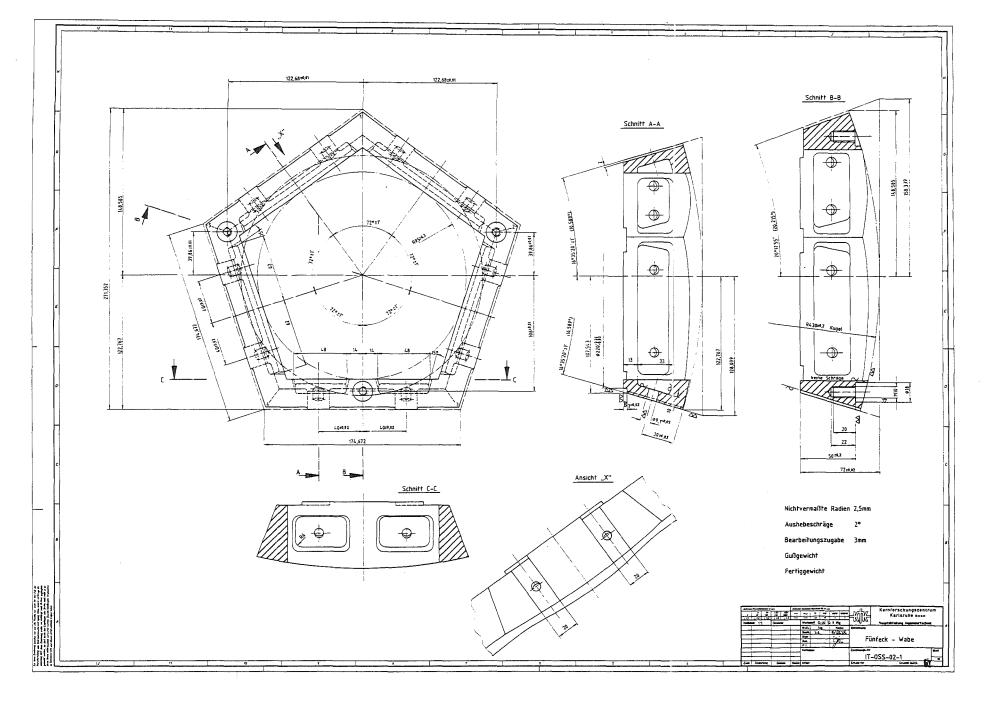
Fig.C1	The hexagonal crystal
Fig.C2	The pentagonal crystal
Fig.C3	Hexagonal honeycomb of the supporting structure
Fig.C4	Pentagonal honeycomb of the supporting structure
Fig.C5	Triagonal flange for the fixation of the hexagonal crystal in the
	supporting structure
Fig.C6	Triagonal flange for the fixation of the pentagonal crystal in the
	supporting structure
Fig.C7	Glass fibre tube for fixation of the hexagonal crystal
Fig.C8	Glass fibre tube for fixation of the pentagonal crystal
Fig.C9	Ground frame for fixation of the spherical honeycomb structure

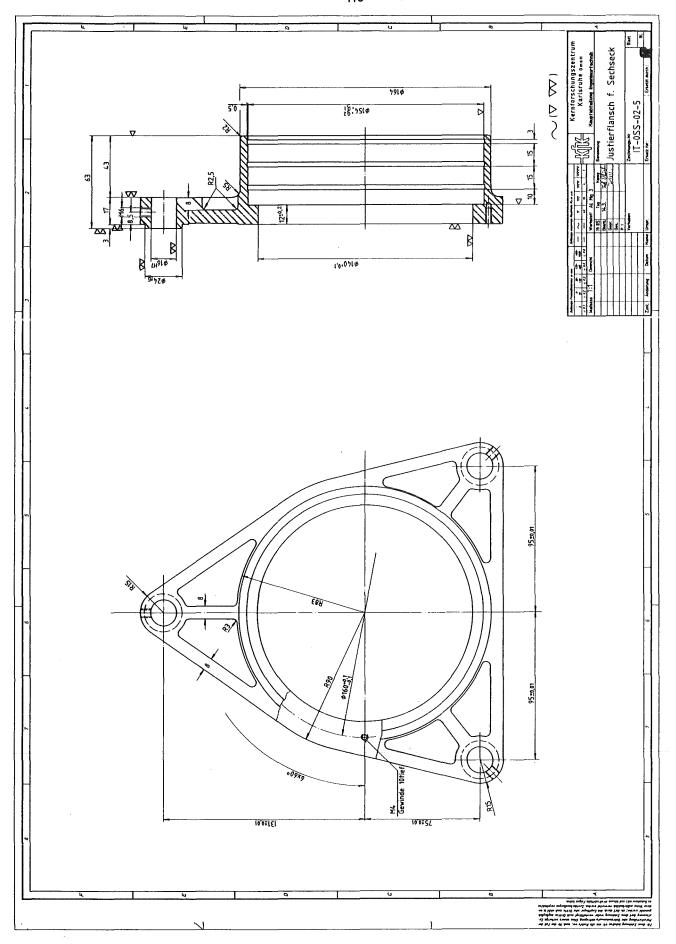


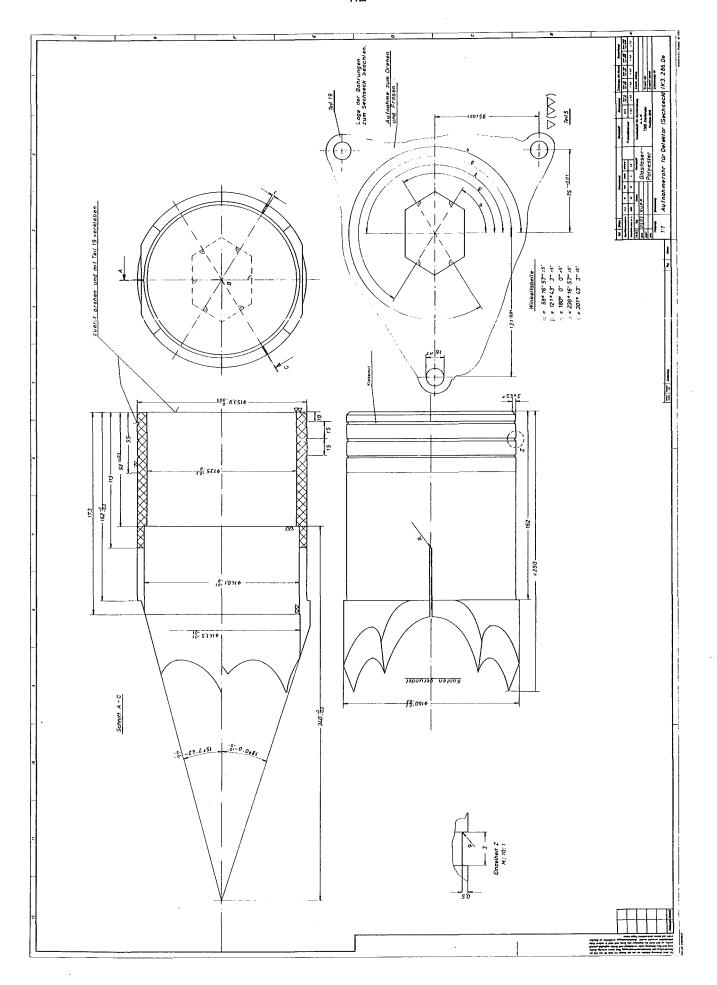


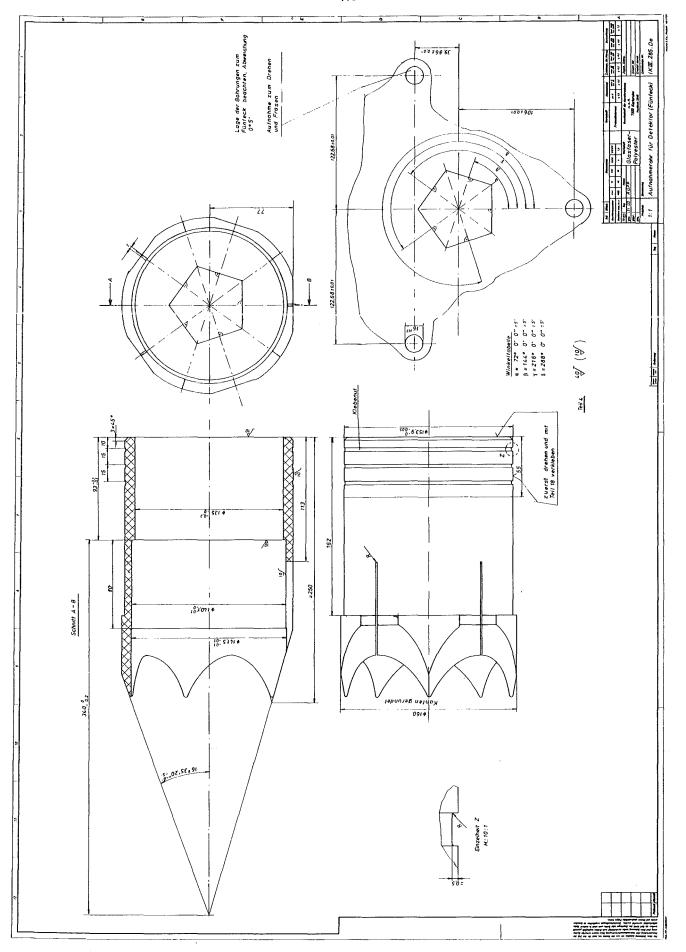


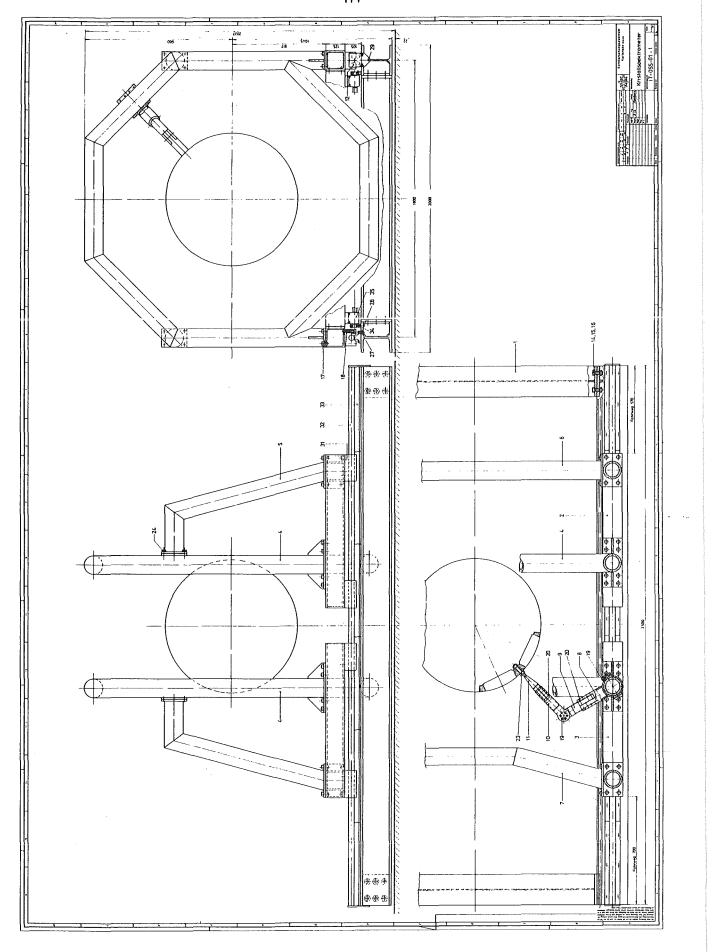












ACKNOWLEDGEMENTS

Design, setup, and operation of such an elaborate detector system was only possible by the help and enthusiasm of many colleagues at KfK and from abroad as well as from various companies. Here, we would like to express our thanks to all who contributed to the success of this project.

In particular we are indebted to Mrs. H. Braun for her care and patience in fabricating the many electronic modules and more than thousand cable connections, and to O. Walz for the adjustment and tests of the home made CAMAC electronics. We although thank Mrs. J. M. Fröhlich for the many drawings and D. Adami for his excellent machining of the complicated honeycomb structure.

Our work was greatly facilitated by the fact that we could make use of the experience from the construction of the Heidelberg crystal ball detector. Thanks to the generous support by Prof. D. Habs and R. Repnow (MPI für Kernphysik Heidelberg), H. Farr and P. von Walter (Elektroniklabor des Physikalischen Instituts, University of Heidelberg), and E. Malwitz (GSI Darmstadt) practically all aspects of the detector development including geometry, mechanical construction, electronics, and automatic operation were influenced and facilitated. In an early stage of the project F. E. Beck from the CRN Strasbourg kindly provided us with the first information on BaF2 scintillators.

Last but not least thanks are due to Dr. K. Korth and E. Merck, the companies which supplied our BaF₂ crystals. Persisting efforts of G. Karschnik, C. D. Knöchel and J. Korth were necessary to produce large crystals with the particular quality that now make the detector so outstanding.